

Count total set bits

$$n = 11$$

[Note: 2^x can be written as: $(1 \ll x)$]

For a given number n, first we need to know the Largest Power of 2 that is present.
why?

Because It is easier to calculate the number of set bit in this

when $n = 11$

	8	4	2	1	
0	0	0	0	0	
1	0	0	0	1	$\rightarrow 2^0$
2	0	0	1	0	$\rightarrow 2^1$
3	0	0	1	1	
4	0	1	0	0	$\rightarrow 2^2$
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	$\rightarrow 2^3$
9	1	0	0	1	
10	1	0	1	0	
11	1	0	1	1	

\rightarrow It is easier to calculate number of set bit here as 2^3 is the Largest power of 2 for $n=11$

$$\text{so here } x=3, \text{ no of set bits} = \frac{x \cdot 2^{x-1}}{2} \\ = 3 \cdot 2^{3-1} = 3 \cdot 2^2 = 3 \cdot 4 = 12$$

This means, there are 3 column, each having $2^3 = 8$ now
No of Set bit = $\frac{8}{2} * \frac{8}{2} * \frac{8}{2} = 4 \cdot 4 \cdot 4 = 4 \times 3 = 12$

why $8/2 \rightarrow$ because 4 are set & 4 unset.

Next: From n to 2^x , find the NO of One in MSB
i.e bin 8 to 11

$$\text{i.e } n - 2^x + 1 = 11 - 8 + 1 = 3 + 1 = 4$$

Now observe

8	4	2	1
0	0	0	0
1	0	0	1
2	0	0	1
3	0	0	1
4	0	1	0
5	0	1	0
6	0	1	0
7	0	1	1

→ up until here we know no of set bits

$$\text{i.e } x * 2^{x-1}$$

8	1	0	0	0
9	1	0	0	1
10	1	0	1	0
11	1	0	1	1

→ For this we know NO of set bits
in MSB = $n - 2^x + 1$

↓
Now if we consider this

4	2	1
0	0	0

0	0	0	0
1	0	0	1

$\rightarrow 2^0 \rightarrow$ this becomes a subproblem

$\rightarrow 2^1 \rightarrow$ for $n=4$

3 0 1 1

we do this as long as $n=0$