

Eg:  $n = 8$ ,  $Arr = [4, 2, 5, 4, 2, 3, 3, 1]$

Take XOR of all Number

	8	4	2	1
4	0	1	0	0
2	0	0	1	0
5	0	1	0	1
4	0	1	0	0
2	0	0	1	0
3	0	0	1	1
3	0	0	1	1
1	0	0	0	1
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	0	1	0	0

$$4 \wedge 2 \wedge 5 \wedge 4 \wedge 2 \wedge 3 \wedge 3 \wedge 1$$

$$= 5 \wedge 1 = 4$$

→  $5 \wedge 1$  can be written as

$$\begin{array}{r} 0 \ 1 \ 0 \ 1 \\ 0 \ 0 \ 0 \ 1 \\ \hline 0 \ 1 \ 0 \ 0 \end{array}$$

Every Bit with 0 is same, But Every bit with 1 is different

This says that → Every Bit with One group up to form 5 & Every bit with 0 group up to form 1

So from 4 [0 1 0 0] → we can Extract 5, 1

# Grab Every bit with 1

$$= 4 \wedge 5 \wedge 4 = 5$$



# Grab Every bit with 0

$$2 \wedge 2 \wedge 3 \wedge 3 \wedge 1$$

$$= 1$$

$$\# op = [5, 1]$$

4	0	1	0	0
2	0	0	1	0
5	0	1	0	1
4	0	1	0	0
2	0	0	1	0
3	0	0	1	1
3	0	0	1	1
1	0	0	0	1
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	0	1	0	0

# Example 2:  $N=8$ ,  $[36, 50, 24, 56, 36, 24, 42, 50]$

XOR	32	16	8	4	2	1
36	1	0	0	1	0	0
50	1	1	0	0	1	0
24	0	1	1	0	0	0
56	1	1	1	0	0	0
36	1	0	0	1	0	0
24	0	1	1	0	0	0
42	1	0	1	0	1	0
50	1	1	0	0	1	0
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18	0	1	0	0	1	0

From 18, We need to Extract a distinct Number

$$XOR = 36 \wedge 50 \wedge 24 \wedge 56 \wedge 36 \wedge 24 \wedge 42 \wedge 50$$

$$= 56 \wedge 42 = 18$$

we can also write 18 as  $56 \wedge 42$

56:	1	1	1	0	0	0
42:	1	0	1	0	1	0
	0	1	0	0	1	0

Observe, where ever there is One the bits are different

The Rightmost bit tells that

0 → makes up 56

1 → makes up 42

$$0 = 36 \wedge 24 \wedge 56 \wedge 36 \wedge 2/4$$

$$= 56$$

$$1 = 50 \wedge 42 \wedge 50$$

$$= 42$$

[56, 42]

	32	16	8	4	2	1
36	1	0	0	1	0	0
50	1	1	0	0	1	0
24	0	1	1	0	0	0
56	1	1	1	0	0	0
36	1	0	0	1	0	0
24	0	1	1	0	0	0
42	1	0	1	0	1	0
50	1	1	0	0	1	0

Check Right Most bit

0 1 0 0 1 0