

K-closest points to Origin → QuickSelect + Binary Search

Eq:  $[-2 \ 10] \ [-4 \ -8] \ [10 \ 7] \ [-4 \ -7]$

Initially: Hypothetically assume, we do not know what our pivot Index is, We have to find One pivot Idx

This pivot Index should be found in such a way that, all the elements to the left of the pivot Index, should be smaller than the Selected Pivot Index.

Assume Initially

pivotIdx = n

Left = 0 , right = n-1 , K = 3

# We check if pivotIdx = k, if equal then all element to left are smaller than pivotIdx, hence we have found k smallest | closest point.

$[-2 \ 10] \ [-4 \ -8] \ [10 \ 7] \ [-4 \ -7]$

↑  
left

↑  
right

↑  
pivotIdx

we perform binary Search on array & find a new pivotIdx,

We Keep doing this Until pivotIdx = k.

$[-2 \ 10, -4 \ -8, 10 \ 7, -4 \ -7]$

left

mid

right

# Now keep pushing element greater than mid to its right

$[-4 \ -7 \ -4 \ -8 \ 10 \ 7 \ -2 \ 10]$

left

right

$[-4 \ -7 \ -4 \ -8 \ 10 \ 7 \ -2 \ 10]$

left

right

$[-4 \ -7 \ 10 \ 7 \ -4 \ -8 \ -2 \ 10]$

left

right

$[-4 \ -7 \ 10 \ 7 \ -4 \ -8 \ -2 \ 10]$

right

left

If  $\text{left} < \text{pivot}$ :

then return  $\text{left} + 1$ , because all the values to left must be smaller than the new pivot that we return.

But here  $\text{left} > \text{pivot}/\text{mid}$ :

so we just return  $\text{left}$ , Because Everything to left is sorted.

new-pivot-idx = 1 j = k.

so we repeat Binary Search

But this time we perform Binary Search on adjusted  
Left & right pointer

[ -4 -7 10 7 -4 -8 -2 10 ]  
↳ new pivot

If we carefully observe all the elements to the left of  
new pivot, will for sure be smaller.

But there is no such guarantee for elements to the right of  
it.

→ Now we check, if our k is to left of new pivot point  
then our right = new-pivot - 1

→ If our k is to right of new-pivot then our left will  
be equal to new-pivot, because there is no guarantee  
that our elements on right are completely greater  
than current value.

so left = new-pivot

Second iteration

[ -4 -7 10 7 -4 -8 -2 10 ]  
↑                              ↑  
left                          right  
                            mid.

$$[-4-7 \quad -2 \ 10 \quad -4 \overset{\text{mid}}{-8} \quad 10 \ 7]$$

↑                   ↑  
left              right

$$[-4-7 \quad -4 \overset{\text{mid}}{-8} \quad -2 \ 10 \quad 10 \ 7]$$

↑  
left  
right

$$[-4-7 \quad -4-8 \quad -2 \overset{\text{mid}}{10} \quad 10 \ 7]$$

↑                   ↑  
right              left

since our left is not less than our mid, we return  
left are new-pivot

since our new-pivot < k

we perform binary search of right side

$$[-4-7 \quad -4-8 \quad -2 \overset{\text{mid}}{10} \quad 10 \ 7]$$

↑                   ↑  
left              right

$$[-4-7 \quad -4-8 \quad -2 \overset{\text{mid}}{10} \quad 10 \ 7]$$

↑                   ↑  
left              right

$$[-4-7 \quad -4-8 \quad 10 \ 7 \quad -2 \overset{\text{mid}}{10}]$$

↑                   ↑  
left              right

$$[-4-7 \quad -4-8 \quad \underset{\text{right}}{10 \ 7} \quad \underset{\text{mid}}{10 \ 7} \quad -2 \ 10]$$

our new-pivot = 2

$2 < k(3)$

we perform binary search on right part

lyt = new-pivot

4th iteration

$\begin{bmatrix} -4 & -7 & -4 & -8 & 10 & 7 & -2 & 10 \end{bmatrix}$

↑              ↑  
lyt            right

$\begin{bmatrix} -4 & -7, -4 & -8, -2 & 10, 10 & 7 \end{bmatrix}$

↑      ↑  
lyt    right

$\begin{bmatrix} -4 & -7, -4 & -8, -2 & 10, 10 & 7 \end{bmatrix}$

↑      ↑  
right   lyt

our new-pivot = k :

hence we return every element to the left of it

$\begin{bmatrix} [-4, -7], [-4, -8], [-2, 10] \end{bmatrix}$

Now, if we observe carefully, we see that all the elements to the left of pivot are smaller than pivot