

Rotated and Sorted

Brute force

* Idea: Rotate the array each time & then compare it to the sorted array. If the array after rotating equal sorted array, then the array was rotated

Eq: $[3, 4, 5, 1, 2]$

Ans: sorted array = $[1 \ 2 \ 3 \ 4 \ 5]$

① $4 \ 5 \ 1 \ 2 \ 3 = 1 \ 2 \ 3 \ 4 \ 5 \times$

② $5 \ 1 \ 2 \ 3 \ 4 = 1 \ 2 \ 3 \ 4 \ 5 \times$

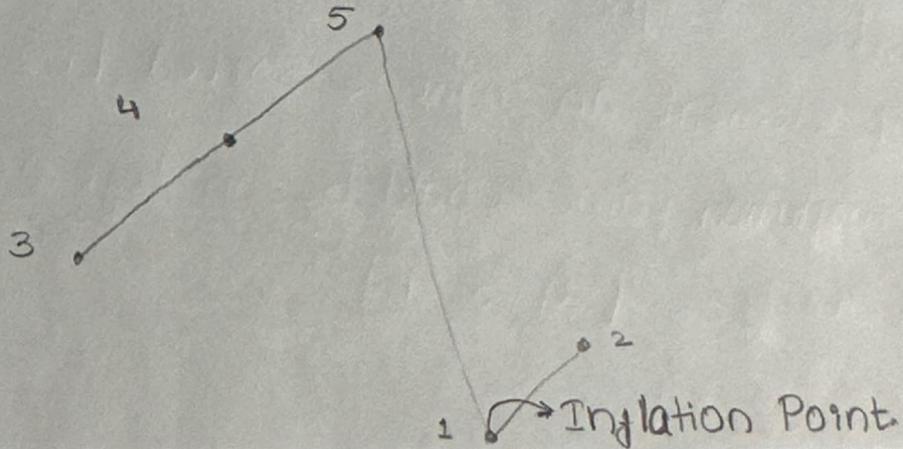
③ $1 \ 2 \ 3 \ 4 \ 5 = 1 \ 2 \ 3 \ 4 \ 5 \checkmark$

so, we rotate by removing element from front & attaching to the end.

Inflation point

Inflation point is a point where the actual array got split to be rotated

Eq:



So, previously we rotated the array for Every Element & Checked if the array was sorted.

Now we find the inflation point & the check if the array was sorted.

There are 2 ways to find out the inflation point.

- ① Comparing with previous element
- ② Binary Search.

Comparing with previous Element:

$[3 \ 4 \ 5 \ 1 \ 2]$

$3 > 4 ? \rightarrow \text{No}$

$4 > 5 ? \rightarrow \text{No}$

$5 > 1 \rightarrow \text{Yes} \rightarrow \text{Inflation point found}$

Rotate the array from here & check if the array is sorted.

$[1 \ 2] [3 \ 4 \ 5] \rightarrow 1 \ 2 \ 3 \ 4 \ 5 \checkmark$

② Binary Search

We know that, when array is sorted, $\text{right} > \text{left}$.

$$[1 \ 2 \ 3 \ 4 \ 5] \quad 5 > 1 \rightarrow \text{This will always be true.}$$

When the array gets rotated

Condition 1 : $\text{mid} > \text{right}$:

$$[3 \ 4 \ 5 \ 1 \ 2]$$

$\uparrow \quad \uparrow$
 $\text{mid} \quad \text{right}$

* If $\text{mid} > \text{right}$: $5 > 2$

- Every Element on left is sorted $\rightarrow [3 \ 4 \ 5]$
- So we are sure that the inflation point lies to the right of mid

$[1 \ 2]$

Condition 2 : $\text{mid} < \text{right}$

$$[4 \ 5 \ 1 \ 2 \ 3]$$

$\uparrow \curvearrowright$
 $\text{mid} \quad \text{right}$

- Every Element on right is sorted $[1 \ 2 \ 3]$

- The inflation point could be on Left or
mid itself

$[4 \ 5 \ 1]$

$$Eq [3 \ 4 \ 5 \ 1 \ 2]$$

* $[3 \ 4 \ 5 \ 1 \ 2]$
 ↑ ↑
 mid right

$5 > 2 \rightarrow$ So Inflation point will be to right of mid

$$\text{Left} = \text{mid} + 1$$

$$* [\textcircled{1} \ 2]$$

↑ ↑
 mid right

$1 < 2 \rightarrow$ so Inflation point can be mid itself or
to the left

$$\text{right} = \text{mid}$$

$$* [\text{ }] = \text{Inflation point found}$$

↑↑
 left right

→ rotate here and check with sorted array

$$[1 \ 2 \ 3 \ 4 \ 5] \rightarrow \underline{1 \ 2 \ 3 \ 4 \ 5}$$

Count Inflation point (Optimal Solution)

Until now we saw that we can only have 1 inflation point
If there are more than one, then the array is not sorted.

→ Idea is to count the inflation point.

We Count the inflation point, by comparing the value with its previous Element

If we take an array, [3 4 5 1 2]

We know 4 comes after 3.

[3 ↗ 4 5 1 2]

Similarly 5 comes after 4

[3 ↗ 4 ↗ 5 1 2]

But 1 does not come after 5

hence we found 1 inflation point

Comparison

[3 ↗ 4 ↗ 5 ↗ 1 ↗ 2]
 ↑

Why do we compare 3 with 2

If we take a sorted array before rotation

$[1 \overset{1}{2} \overset{2}{3} \overset{3}{4} \overset{4}{5}] \rightarrow$ The array got chopped at 2

so It became $[3 \ 4 \ 5 \ 1 \ 2]$, so the Element
that comes previous to 3 is 2.

How do we do this mathematically

$$B[i] = A[i - 1 \% n]$$

so when $i = 0$

$$B[0] = A[0 - 1 \% 5] = A[-1 \% 5] = A[-1]$$

$$i=1, B[1] = A[1 - 1 \% 5] = A[0 \% 5] = A[0]$$

$$i=2, B[2] = A[2 - 1 \% 5] = A[1 \% 5] = A[1]$$

$$i=3, B[3] = A[3 - 1 \% 5] = A[2 \% 5] = A[2]$$

$$i=4, B[4] = A[4 - 1 \% 5] = A[3 \% 5] = A[3]$$

$$i=5, B[5] = A[5 - 1 \% 5] = A[4 \% 5] = A[4]$$

so $[3 \overset{1}{4} \overset{2}{5} \overset{3}{1} \overset{4}{2}]$