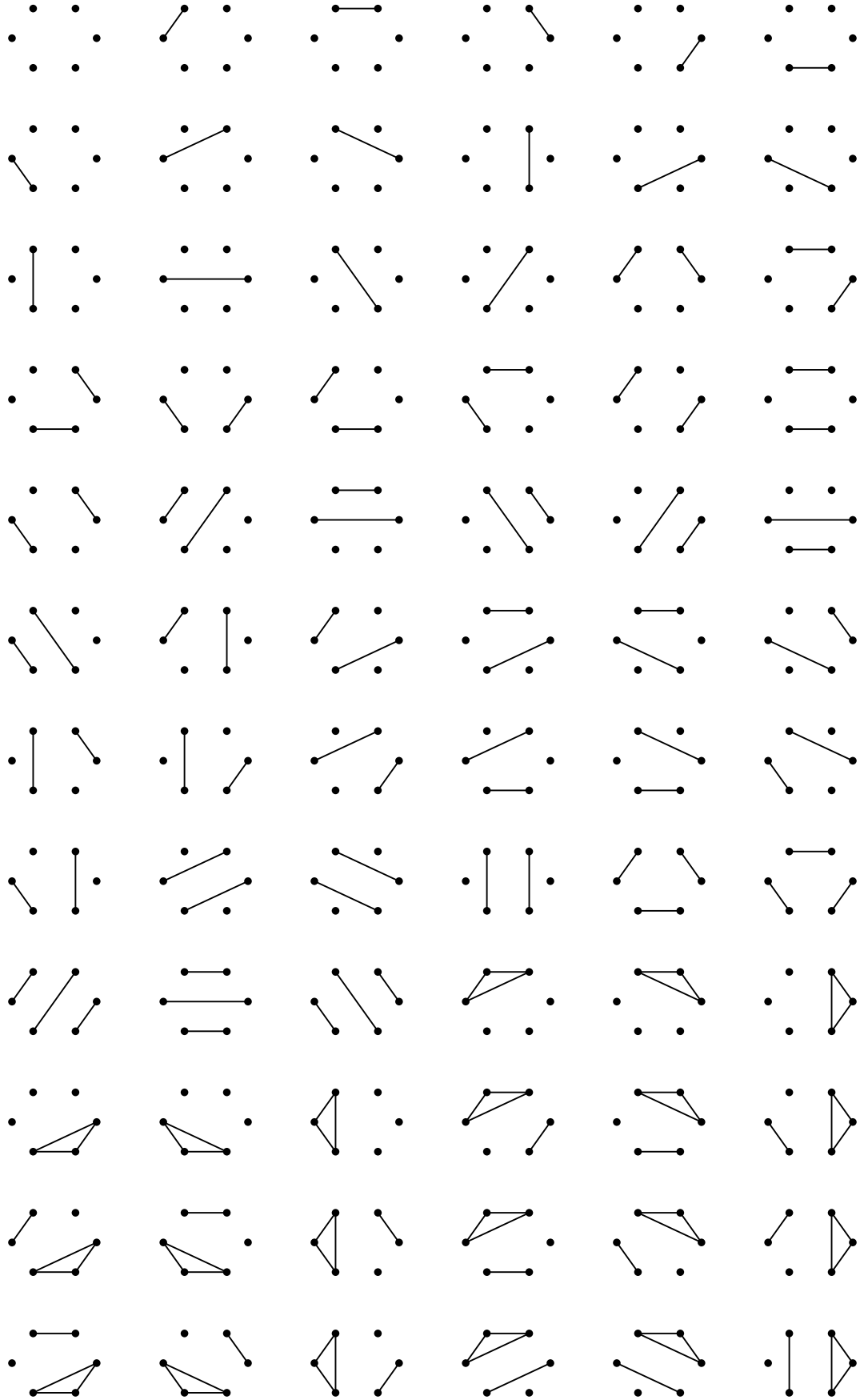
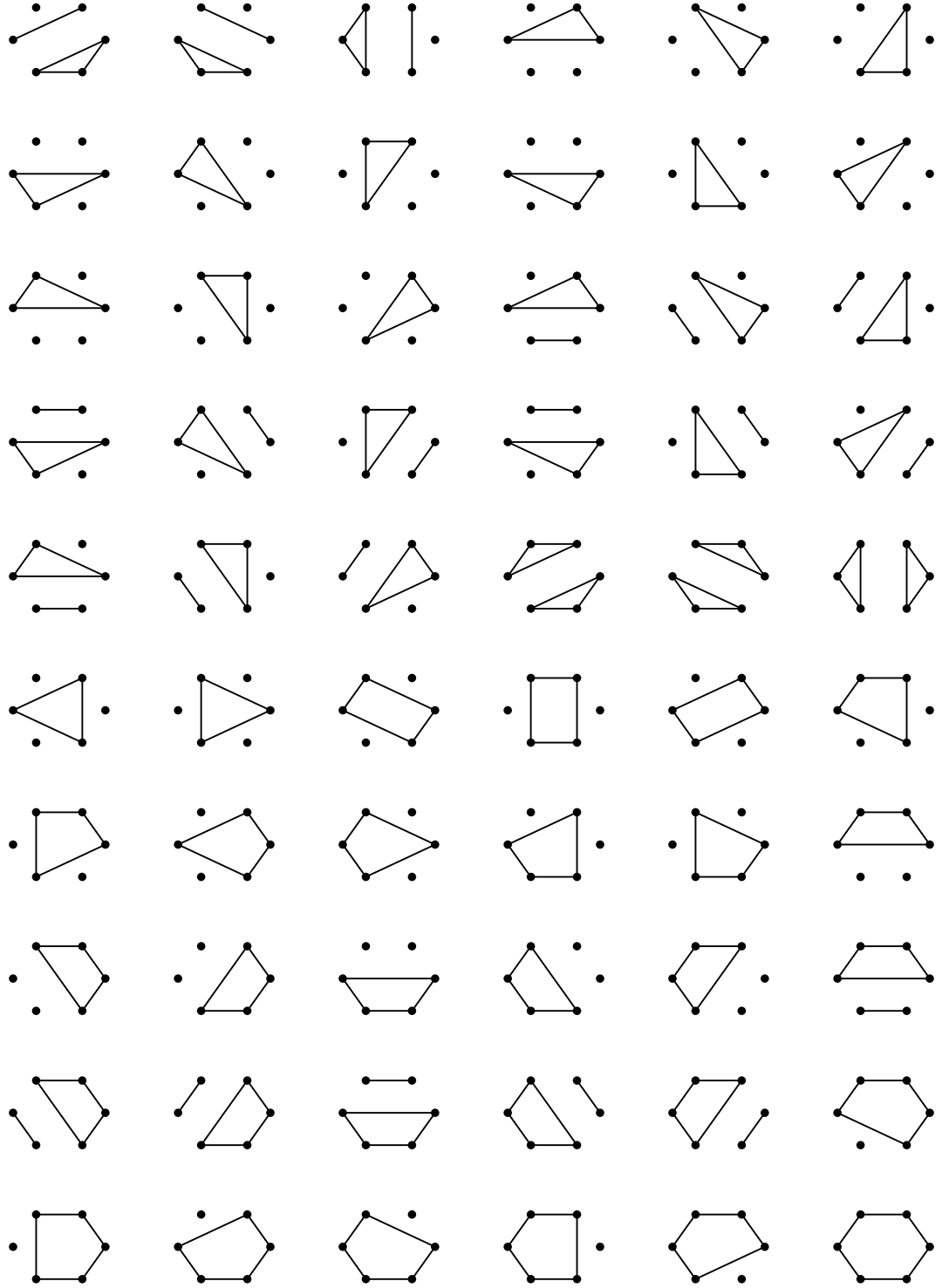


For  $n = 6$ , there are 132 such partitions:





In fact, for any  $n$ , the number of such partitions is the Catalan number  $c_n$ .

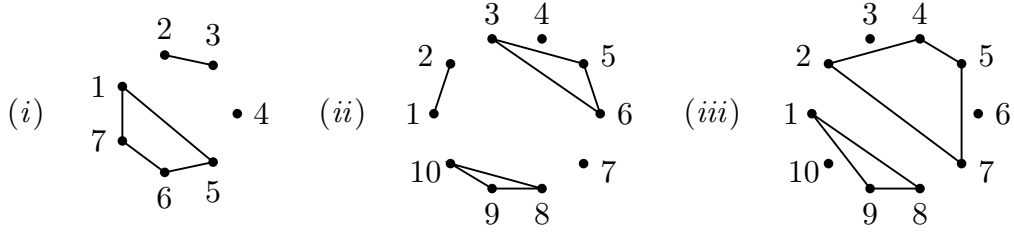
*Connection with the first bracket problem*

Given a balanced string of  $n$  left and  $n$  right brackets, we obtain the corresponding partition as follows. First we choose a starting position, choose clockwise direction to draw  $n$  dots and name these dots from 1 to  $n$ . Also name the left brackets in the balanced string from 1 to  $n$ . Read from the left of the balanced string: if there is a block of  $k$  right brackets R, then join the integers corresponding to the matching L by a  $k$ -gon [1-gon is a point, 2-gon is a line].

Given such a partition, we first choose a starting position for the partition and choose clockwise direction to construct the corresponding balanced string of bracket, by reversing the above procedures.

*Remark:* This is closely related to the noncrossing partitions problem and the non-crossing Murasaki diagrams problem.

1. Construct balanced strings of brackets corresponding to the following partition:



*Solution.*

The corresponding balanced strings of brackets are:

- (i) LLLRRLRLLLRRRR  
(ii) LLRLLRLLRRRLRLLLRRR  
(iii) LLLRLLLRLRRRRLLLRRRR

2. For the following balanced strings of brackets, construct the corresponding partitions:

- (i) LLRLRLLLRLRRRR  
(ii) LRLLRRLRLRLLRRR  
(iii) LLRRRLLLLLLLLRRRRLLRRRRR

*Solution.*

The corresponding partitions are:

