

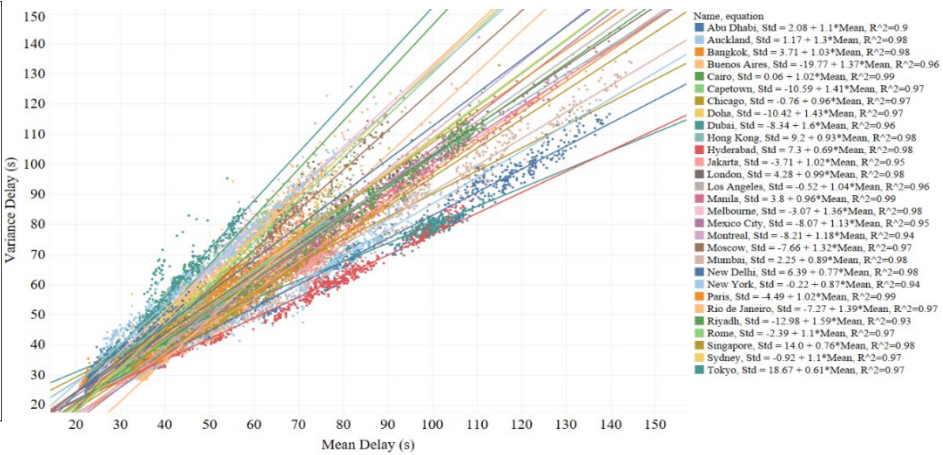
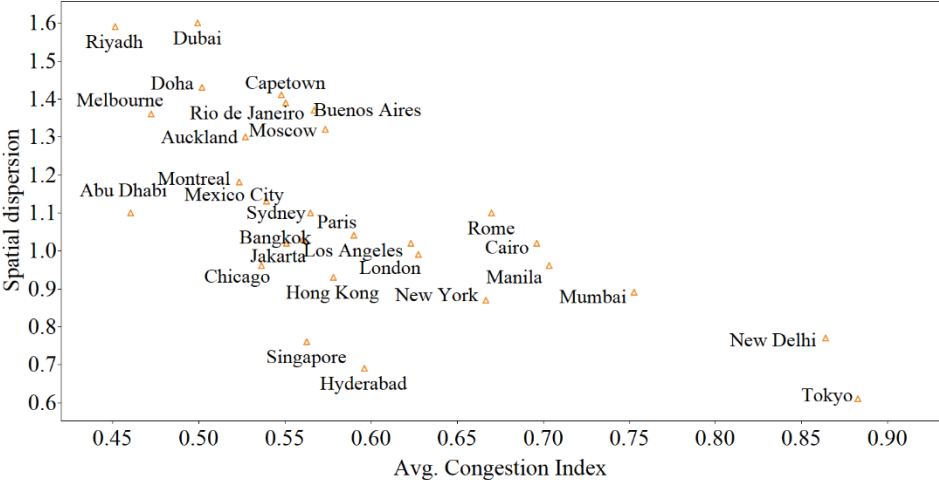
# A simple crowdsourced delay based traffic control

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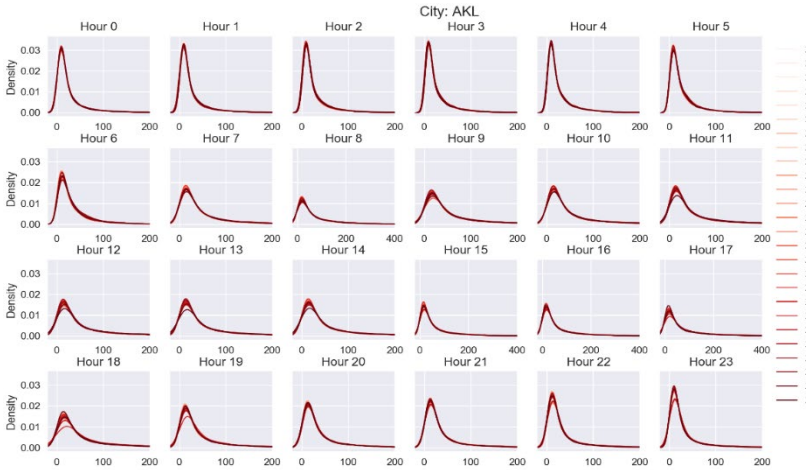
In collaboration with: Divya Nair, Sai Chand, Michael Levin and David Rey  
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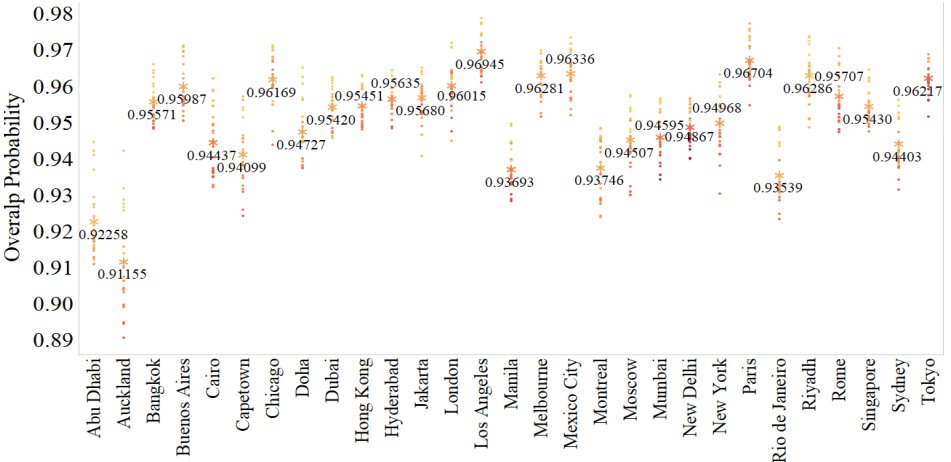
# Multicity Traffic conditions



## Spatial Heterogeneity



## Network Stability

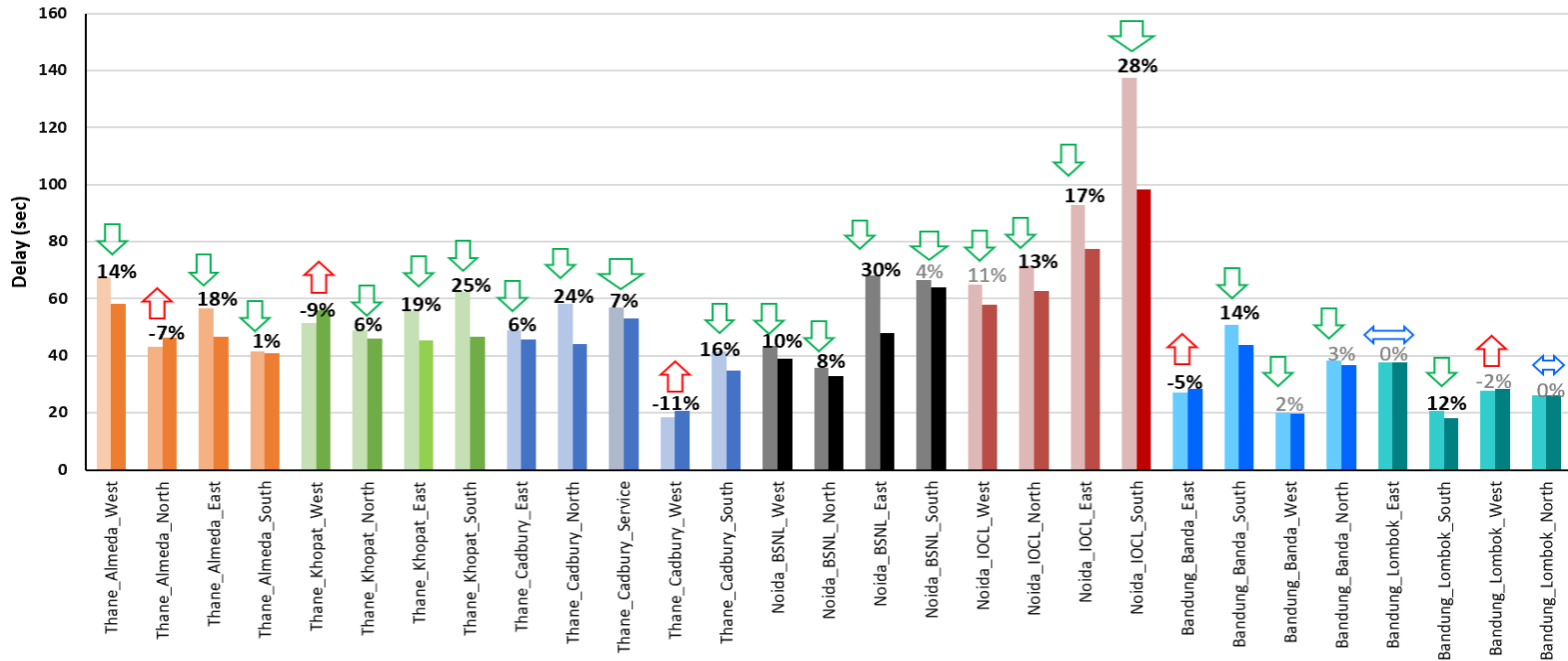


# Individual Intersection

**Theorem:** Given a fixed cycle time, a green time that ensures clearance of queues is

$$g_i^* = \frac{(T_i/\mu_i)}{\sum_j (T_j/\mu_j)} (C - L). \text{ This policy is stable only if } \lambda_i \leq \frac{(C-L)}{\sum_j (T_j/\mu_j)}$$

Max Pressure Term:  $P_i = T_i/\mu_i$



# Literature on Max Pressure

study	weight	pressure	proved stable
<i>Wongpiromsarn et al. (17)</i>	$w_{ij} = x_i(t) - x_j(t)$	$w_{ij}(t)\xi_i(p, \mathcal{L}_i, \mathcal{L}_i, z_i(t))$	Y
<i>Varaiya (15)</i>	$w_{ij} = x_{ij} - \sum_{k \in \Gamma_j^+} x_{jk} p_{jk}$	$Q_{ij} w_{ij} S_{ij}$	Y
<i>Xiao et al. (19)</i>	/	$P_{ij}(t) = \frac{\alpha_{ij} \left[ \sum_{(i', j') \in \mathcal{L}_{ij}^{(in)} x_{i' j'}(t) \right]}{Q_{ij}} x_{ij}(t)$	Y
<i>Gregoire et al. (2)</i>	$w_{ij}(t) = \min(x_{ij}(t)/Q_{ij}, 1) \max(P_i(t) - P_j(t), 0)$	$P_i(t) = \sum_{j \in \Gamma_i^+} P_{ij}(x_{ij}) = \sum_{j \in \Gamma_i^+} \theta_{ij} x_{ij}$	N
<i>Le et al. (6)</i>	$w_{ij} = x_{ij} - \sum_{k \in \Gamma_j^+} x_{jk} p_{jk}$	/	Y
<i>Gregoire et al. (3)</i>	$w_{ij} = \max(P_i(t) - P_j(t), 0)$	$P_i(x_i) = \min \left( 1, \frac{\frac{x_i}{Q_\infty} + (2 - \frac{x_i}{Q_\infty})(\frac{x_i}{Q_i})^m}{1 + (\frac{x_i}{Q_i})^{m-1}} \right)$	Y
<i>Pumir et al. (11)</i>	$w_{ij} = x_{ij} - \sum_{k \in \Gamma_j^+} x_{jk} p_{jk}$	$Q_{ij} w_{ij} S_{ij}$	Y
<i>Zaidi et al. (20)</i>	$w_{ij}(t) = \max \{x_i(t) - x_j(t), 0\}$	$w_{ij}(t) S_{ij}(t)$	N
<i>Le et al. (7)</i>	$w_\psi(t) = \sum_{i \in \Gamma_j^-} \psi_i(x_i(t) - \sum_{j \in \Gamma_i^+} \bar{\theta}_{ij}(t) x_j(t))$	/	Y
<i>Hsieh et al. (4)</i>	$w_{ij} = x_{ij} - \sum_{k \in \Gamma_j^+} x_{jk} p_{jk}$	$Q_{ij} w_{ij} S_{ij}$	Y
<i>Wu et al. (18)</i>	$w_{ij}(t) \triangleq T_{ij}(t)$	$\gamma_{ij} w_{ij}(t) S_{ij}$	Y
<i>Li and Jabari (8)</i>	$w_{ij}(t) = f(l_i, l_j, c_{ij}, \pi_{ij}, \delta_{ij}, \theta_j)$	$w_{ij}(t) \mathbb{E}^{\rho(t)} q_{ij}(p)$	Y
<i>Rey and Levin (12)</i>	$w_{ij} = x_{ij} - \sum_{k \in \Gamma_j^+} x_{jk} p_{jk}$	$w_i(t) y_i(t)$	Y
<i>Lioris et al. (9)</i>	$w_{ij} = x_{ij} - \sum_{k \in \Gamma_j^+} x_{jk} p_{jk}$	$Q_{ij} w_{ij} S_{ij}$	N
<i>Kouvelas et al. (5)</i>	/	$P_i(t) = \left[ \frac{x_i(t)}{x_{i, \max}} - \sum_{j \in O_n} \frac{\beta_{ij} x_j(t)}{x_{j, \max}} S_n(t) \right] Q_i, i \in I_n$	N

# Network Max Pressure

$$x_{ij}(t+1) = x_{ij}(t) - y_{ij}(t) + \sum_{h \in \Gamma_i^-} y_{hi}(t) p_{ij}(t)$$

$$x_{ij}(t+1) = x_{ij}(t) - y_{ij}(t) + d_i(t) p_{ij}(t)$$

$$y_{ij}(t) = \min \{Q_{ij} s_{ij}(t), x_{ij}(t)\}$$

$$\forall i \in \mathcal{L}_{\text{int}}, h \in \Gamma_i^-, j \in \Gamma_i^+$$

$$\forall i \in \mathcal{L}_{\text{entry}}, j \in \Gamma_i^+$$

**Flow Propagation**

$$w_{ij}(t) = \tau_{ij}(t) - \sum_{k \in \Gamma_j^+} \tau_{jk}(t) p_{jk}(t)$$

**Weights**

$$S^*(t) = \arg \max_{S_n \in \mathcal{S}_n} \left\{ \sum_{(i,j)} Q_{ij} w_{ij}(t) s_{ij}(t) \right\}$$

**pressure**

# Travel Time Function

*Total Travel Time:*  $T_{ij}(t) = \sum_{\tau=1}^{\infty} \tau x_{ij}^{\tau}(t)$  **Monotonic**

*Average Travel Time:*  $\tau_{ij}(t) = \frac{\sum_{\tau=1}^{\infty} \tau x_{ij}^{\tau}(t)}{x_{ij}(t)}$  **Non-Monotonic**

$$x_{ij}^3(t) = 2$$
$$\Rightarrow w_{ij}(t) = \frac{3 \times 2}{2} = 3$$

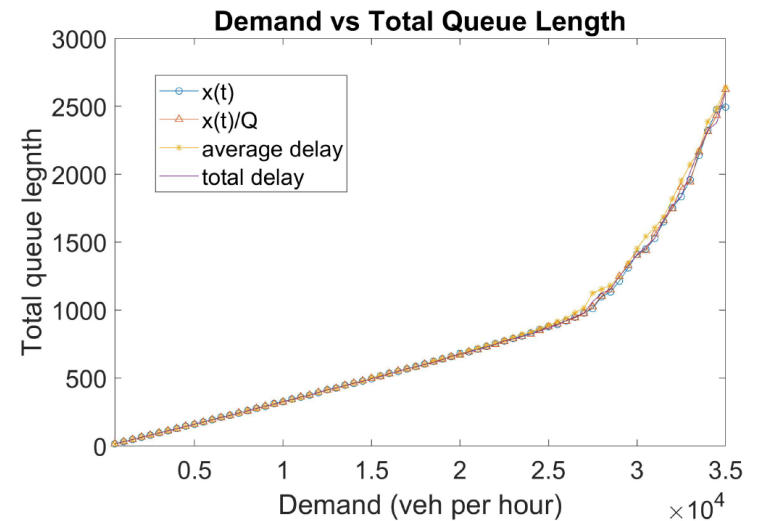
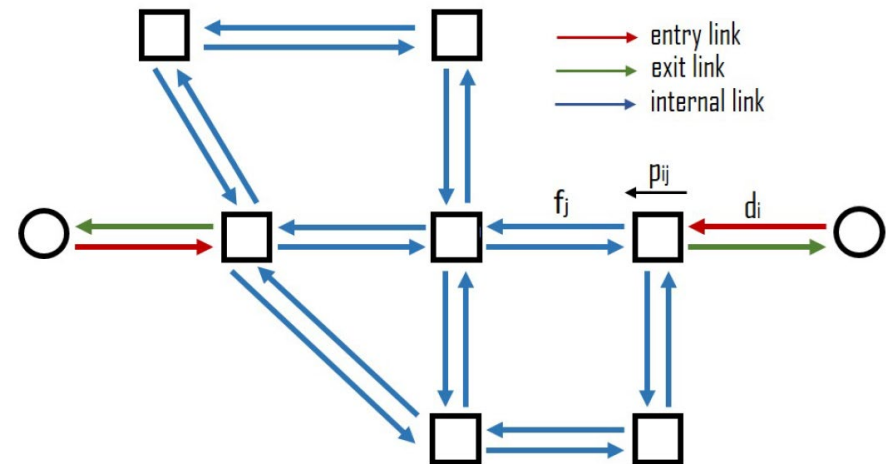
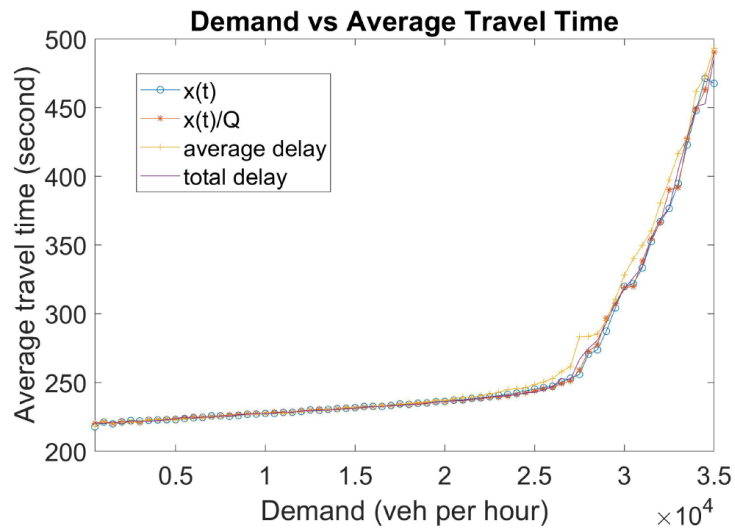
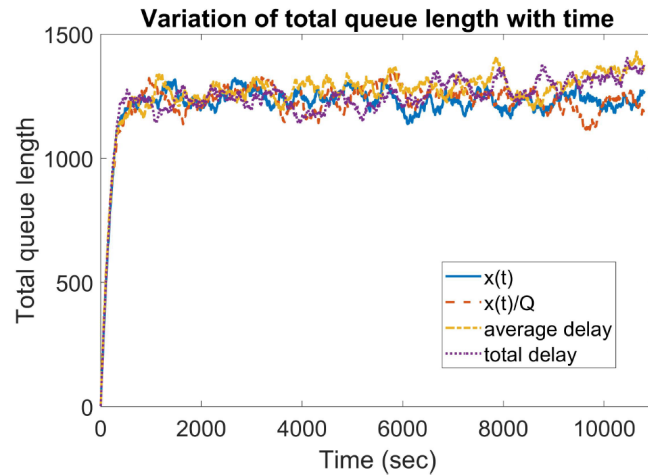
$$\sum_j y_{ij}(t+1) = 1$$
$$\sum_j y_{ji}(t+1) = 2$$

$$x_{ij}^3(t+1) = 2$$
$$\Rightarrow w_{ij}(t+1) = \frac{1 \times 2 + 1 \times 4}{3} = 2$$

*Travel Time:*  $w_{ij}(t) = \frac{x_{ij}(t)}{Q_{ij}(t)}$  **Monotonic**



# Simulation Results



**THANK YOU!**