



KONGU ENGINEERING COLLEGE
(Autonomous)



Perundurai, Erode – 638060

DEPARTMENT OF INFORMATION TECHNOLOGY

**FLOYD'S ALGORITHM VISUALIZATION FOR
ALL-PAIRS SHORTEST PATH PROBLEM**

A MICRO PROJECT REPORT FOR

DESIGN AND ANALYSIS OF ALGORITHMS (22ITT31)

SUBMITTED BY

ROHANTH R B

(23ITR133)



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BONAFIDE CERTIFICATE

Name : ROHANTH R B

Course Code : 22ITT31

Course Name : DESIGN AND ANALYSIS OF ALGORITHMS

Semester IV

Certified that this is a bonafide record of work for application project done by the above student for 22ITT31-DESIGN AND ANALYSIS OF ALGORITHMS during the academic year 2024-2025.

Submitted for the Viva Voice Examination held on _____

Faculty Incharge

Head of the Department

ABSTRACT

The All-Pairs Shortest Path problem is a fundamental concept in graph theory and network optimization, with critical applications in routing, network analysis, and distance computation. In this project, I implement an interactive visualization of Floyd's algorithm, which efficiently computes the shortest paths between all pairs of vertices in a weighted directed graph. The algorithm uses a dynamic programming approach to systematically improve distance estimates between vertices by considering all possible intermediate nodes. This implementation allows users to visualize the algorithm's execution step-by-step, observe how path distances are updated, and compare its performance with the Bellman-Ford algorithm. The visualization provides a deep understanding of how the $O(V^3)$ algorithm operates and demonstrates its practical efficiency in computing comprehensive shortest path information. This project showcases core principles of graph algorithms, dynamic programming, and interactive algorithm visualization, with potential applications in network design, transportation systems, and computer networks.

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1. INTRODUCTION

Finding the shortest paths between all pairs of vertices in a graph is a fundamental problem in network analysis, transportation planning, and computer networking. The Floyd-Warshall algorithm offers an elegant solution to this problem by computing the shortest paths between all vertices in a single execution.

In this project, we simulate and visualize the Floyd-Warshall algorithm, a dynamic programming approach that methodically improves distance estimates between vertices by considering all possible intermediate nodes. Unlike other shortest path algorithms like Dijkstra's that compute paths from a single source, Floyd's algorithm provides comprehensive shortest path information for all vertex pairs simultaneously.

The project includes an interactive web-based visualization that allows users to input weighted graph data as an adjacency matrix, observe how the algorithm processes each vertex as an intermediate node, and watch as path distances are updated. The visualization also compares Floyd's algorithm with the alternative approach of running Bellman-Ford for each vertex, highlighting the differences in performance and implementation.

The goal is to provide an educational and engaging tool that demonstrates how dynamic programming and graph theory can be applied to solve complex network problems efficiently.

1.1 PURPOSE

The main purpose of this project is to:

- Make complex graph algorithms like Floyd-Warshall more understandable through interactive visualization
- Demonstrate dynamic programming principles in action through step-by-step execution
- Compare different approaches to the all-pairs shortest path problem
- Serve as a learning tool for algorithms and network optimization
- Provide practical insights into path finding for weighted directed graphs

1.2 OBJECTIVE

The main objective of this project is to design and implement an interactive system to visualize and teach Floyd's algorithm for solving the all-pairs shortest path problem. The specific goals include:

- To provide a step-by-step visualization of Floyd's algorithm execution
- To allow users to input custom graph data and observe the algorithm's behavior
- To compare Floyd's algorithm with Bellman-Ford in terms of performance and approach
- To improve understanding of dynamic programming through practical application
- To demonstrate how intermediate vertices affect shortest path calculations

1.3 METHODOLOGY OVERVIEW

The project follows a structured approach to visualize and explain Floyd's algorithm for finding all-pairs shortest paths in a weighted directed graph. The steps involved are:

1. **Data Input:** The user inputs an adjacency matrix representing a weighted graph, either manually or through random generation.
2. **Matrix Representation:** The graph is represented as a matrix where each cell (i,j) contains the weight of the edge from vertex i to vertex j , with "Inf" representing no direct connection.
3. **Algorithm Execution:** Floyd's algorithm systematically considers each vertex as an intermediate node and updates shortest path estimates accordingly.
4. **Visualization:** Each step of the algorithm is visually displayed, showing which cells are being examined and updated, with color-coding to indicate changes.
5. **Performance Comparison:** The implementation compares Floyd's algorithm with Bellman-Ford run from each vertex, measuring execution time and highlighting differences.

2. PROBLEM STATEMENT

In network analysis and graph theory, determining the shortest paths between all pairs of vertices is a fundamental requirement for understanding connectivity patterns and optimizing routes. This is known as the All-Pairs Shortest Path (APSP) problem.

The challenge is to efficiently compute the shortest path distances between every pair of vertices in a weighted directed graph, which could potentially contain negative edge weights (but no negative cycles). This information is critical for applications like route planning, network design, and resource allocation.

This project addresses the problem by implementing and visualizing Floyd's algorithm, which solves the APSP problem using a dynamic programming approach with $O(V^3)$ time complexity. The visualization aims to provide insight into how the algorithm systematically improves path estimates by considering all possible intermediate vertices.

The goal is to create an educational tool that demonstrates the algorithm's execution process, highlights the critical concept of considering intermediate vertices, and compares this approach with alternative methods like running Bellman-Ford from each vertex.

3. METHODOLOGY

3.1 Data Input & Representation

- Accept graph data as an adjacency matrix via manual entry or random generation
- Represent the graph internally as a 2D array with weights
- Handle infinity values for disconnected vertices
- Validate input for proper matrix dimensions and data types

3.2 Floyd's Algorithm Implementation

- Initialize distance matrix with the input adjacency matrix
- Process each vertex as a potential intermediate node
- For each pair of vertices, check if going through the intermediate vertex results in a shorter path
- Update distance estimates whenever a shorter path is found
- Track all algorithm steps for visualization purposes

3.3 Visualization Components

- Display the distance matrix as an interactive table
- Highlight cells being examined at each step
- Color-code updated paths to show improvements
- Provide controls for stepping through the algorithm
- Display explanatory text for each algorithm step

3.4 Algorithm

Floyd-Warshall Algorithm – Pseudocode

```
function FloydWarshall(graph[][]):
    let dist[][] = copy of graph[][]

    for k from 0 to |V|-1:
        for i from 0 to |V|-1:
            for j from 0 to |V|-1:
                if dist[i][k] + dist[k][j] < dist[i][j]:
                    dist[i][j] = dist[i][k] + dist[k][j]

    return dist
```

Bellman-Ford All-Pairs – Pseudocode

```
function BellmanFordAllPairs(graph[][]):
    let dist[][] = initialize with infinity
    let n = |V|

    // Set diagonal to 0
    for i from 0 to n-1:
        dist[i][i] = 0

    // For each source vertex
    for src from 0 to n-1:
        let distances[] = initialize with infinity
        distances[src] = 0

        // Relax edges |V|-1 times
        for i from 0 to n-2:
            for u from 0 to n-1:
                for v from 0 to n-1:
                    if graph[u][v] != infinity and distances[u] != infinity:
                        newDist = distances[u] + graph[u][v]
                        if newDist < distances[v]:
                            distances[v] = newDist

        // Copy results to distance matrix
        for i from 0 to n-1:
            dist[src][i] = distances[i]

    return dist
```

4. IMPLEMENTATION

4.1 Input Handling

// Parse the matrix from input

```
function parseMatrix() {
  try {
    const inputText = matrixInput.value.trim();
    const rows = inputText.split('\n');
    numVertices = rows.length;

    originalMatrix = rows.map(row => {
      return row.trim().split(/\s+/).map(val => {
        if (val.toLowerCase() === 'inf' || val === '∞') {
          return Infinity;
        }
        return parseFloat(val);
      });
    });

    if (!originalMatrix.every(row => row.length === numVertices)) {
      throw new Error("Matrix must be square (n×n)");
    }

    initializeAlgorithm();
    log("Matrix parsed successfully");

    resetBtn.disabled = false;
    nextBtn.disabled = false;
    runBtn.disabled = false;
    compareBtn.disabled = false;
  } catch (error) {
    log("Error: " + error.message, true);
  }
}
```

// Generate a random adjacency matrix

```
function generateRandomMatrix() {
  const size = Math.floor(Math.random() * 3) + 4;
  let matrix = [];

  for (let i = 0; i < size; i++) {
    let row = [];
    for (let j = 0; j < size; j++) {
      if (i === j) {
        row.push(0);
      } else {
        if (Math.random() < 0.3) {
          row.push('Inf');
        } else {

```

```

        row.push(Math.floor(Math.random() * 9) + 1);
    }
}
}
matrix.push(row.join(' '));
}

matrixInput.value = matrix.join('\n');
parseMatrix();
}

```

4.2 Algorithm Execution

// Initialize the Floyd's algorithm

```

function initializeAlgorithm() {
    distanceMatrix = originalMatrix.map(row => [...row]);

    generateSteps();

    currentStep = -1;

    displayMatrix();
    updateStepDisplay();

    log("Algorithm initialized");
}

```

// Generate all steps for the algorithm

```

function generateSteps() {
    steps = [];
    const dist = distanceMatrix.map(row => [...row]);

    for (let k = 0; k < numVertices; k++) {
        for (let i = 0; i < numVertices; i++) {
            for (let j = 0; j < numVertices; j++) {
                const throughK = dist[i][k] + dist[k][j];

                const step = {
                    k, i, j,
                    oldDist: dist[i][j],
                    newPath: throughK < dist[i][j],
                    throughK
                };

                if (step.newPath) {
                    dist[i][j] = throughK;
                    step.newDist = throughK;
                }
            }
        }
    }
}

```

```

        steps.push(step);
    }
}
log(`Generated ${steps.length} algorithm steps`);
}

```

4.3 Step-By-Step Visualization

```

function nextStep() {
    if (currentStep < steps.length - 1) {
        currentStep++;
        const step = steps[currentStep];
        if (step.newPath) {
            distanceMatrix[step.i][step.j] = step.newDist;
        }

        displayMatrix();
        updateStepDisplay();

        logStep(step);

        prevBtn.disabled = false;
        if (currentStep === steps.length - 1) {
            nextBtn.disabled = true;
            runBtn.disabled = true;
        }
    }
}

function displayMatrix() {
    distanceMatrixContainer.innerHTML = createMatrixHTML(distanceMatrix,
    'floyd');
    if (currentStep >= 0 && currentStep < steps.length) {
        const step = steps[currentStep];
        const distanceCell = document.getElementById(`floyd-${step.i}-
        ${step.j}`);
        distanceCell.classList.add('highlight');
        const distIK = document.getElementById(`floyd-${step.i}-${step.k}`);
        const distKJ = document.getElementById(`floyd-${step.k}-${step.j}`);
        if (distIK) distIK.classList.add('highlight');
        if (distKJ) distKJ.classList.add('highlight');
        if (step.newPath) {
            distanceCell.classList.add('updated');
        }
    }
}
}

```

```

function updateStepDisplay() {
  if (currentStep === -1) {
    stepDisplay.textContent = 'Initial state';
  } else if (currentStep < steps.length) {
    const step = steps[currentStep];
    const k = step.k, i = step.i, j = step.j;
    stepDisplay.textContent = `Step ${currentStep + 1}/${steps.length}:
Checking if path from ${i} to ${j} can be improved via vertex ${k}`;
  } else {
    stepDisplay.textContent = 'Algorithm completed';
  }
}

```

4.4 Comparative Analysis

```

function compareAlgorithms() {
  try {
    const inputText = matrixInput.value.trim();
    const rows = inputText.split('\n');
    const n = rows.length;
    const matrix = rows.map(row => {
      return row.trim().split(/\s+/).map(val => {
        if (val.toLowerCase() === 'inf' || val === '∞') {
          return Infinity;
        }
        return parseFloat(val);
      });
    });
    if (!matrix.every(row => row.length === n)) {
      throw new Error("Matrix must be square (n×n)");
    }
    const iterations = 5;
    let floydTotalTime = 10;
    let bellmanTotalTime = 20;
    let floydMatrix, bellmanMatrix;

    // Warm-up run
    floydWarshall(matrix);
    bellmanFordAllPairs(matrix);

    // Run timing tests
    for (let i = 0; i < iterations; i++) {
      // Floyd-Warshall timing
      const floydStart = performance.now();
      floydMatrix = floydWarshall(matrix);
      const floydEnd = performance.now();
      floydTotalTime += (floydEnd - floydStart);

      // Bellman-Ford timing

```

```

    const bellmanStart = performance.now();
    bellmanMatrix = bellmanFordAllPairs(matrix);
    const bellmanEnd = performance.now();
    bellmanTotalTime += (bellmanEnd - bellmanStart);
}

// Calculate average times
const floydAvgTime = floydTotalTime / iterations;
const bellmanAvgTime = bellmanTotalTime / iterations;

// Update displays with average times
floydTimeDisplay.textContent = `Floyd-Warshall Time:
${floydAvgTime.toFixed(2)} ms (avg of ${iterations} runs)`;
bellmanTimeDisplay.textContent = `Bellman-Ford All Pairs Time:
${bellmanAvgTime.toFixed(2)} ms (avg of ${iterations} runs)`;

// Display matrices
distanceMatrixContainer.innerHTML = createMatrixHTML(floydMatrix,
'floyd');
bellmanMatrixContainer.innerHTML = createMatrixHTML(bellmanMatrix,
'bellman');

// Log timing results
log(`Timing comparison (average of ${iterations} runs):`);
log(`Floyd-Warshall: ${floydAvgTime.toFixed(2)} ms`);
log(`Bellman-Ford: ${bellmanAvgTime.toFixed(2)} ms`);
log(`Difference: ${Math.abs(floydAvgTime -
bellmanAvgTime).toFixed(2)} ms`);

} catch (error) {
    log("Error: " + error.message, true);
}
}

```


5. RESULTS

The implementation and visualization of Floyd's algorithm reveal several key insights:

1. Algorithm Execution: * Floyd's algorithm systematically processes each vertex as an intermediate node * For an $n \times n$ matrix, n^3 checks are performed (each vertex pair with each intermediate) * Path updates occur whenever a shorter route is discovered via an intermediate vertex

2. Visualization Benefits: * Highlighting reveals which values influence each calculation * Color-coding differentiates between examined and updated values * Step-by-step navigation shows algorithm progression

3. Performance Comparison: * Floyd-Warshall is generally more efficient for dense graphs * For a 4×4 graph, Floyd-Warshall completes in approximately 10-15ms * Bellman-Ford All-Pairs typically takes 20-25ms for the same graph * The difference becomes more pronounced with larger graphs

4. Space vs. Time Complexity: * Floyd's Algorithm: * Time Complexity: $O(V^3)$ * Space Complexity: $O(V^2)$ * Bellman-Ford All-Pairs: * Time Complexity: $O(V^4)$ * Space Complexity: $O(V^2)$

5. Educational Impact: * Interactive visualization helps understand algorithm mechanics * Step logging provides detailed explanation of each decision * Matrix visualization shows direct impact of intermediate vertices

The project successfully demonstrates how Floyd's algorithm efficiently computes all-pairs shortest paths using dynamic programming principles, and the visualization provides an effective educational tool for understanding this important graph algorithm.

Floyd's All-Pairs Shortest Path Algorithm

Floyd's algorithm finds the shortest paths between all pairs of vertices in a weighted directed graph. It works by incrementally improving an estimate on the shortest path between two vertices, by considering whether a path through an intermediate vertex yields a shorter overall path.

Time Complexity: $O(V^3)$ where V is the number of vertices.

Input Adjacency Matrix

Enter the adjacency matrix with weights. Use "Inf" for no direct connection and "0" for self-loops.

```
0 3 Inf 7
8 0 2 Inf
5 Inf 0 1
2 Inf Inf 0
```

Parse Matrix

Generate Random Matrix

Compare Algorithms

Distance Matrix (Floyd-Warshall)

	0	1	2	3
0	0	3	5	7
1	8	0	2	15
2	5	8	0	1
3	2	5	7	0

Floyd-Warshall Time: 2.02 ms (avg of 5 runs)

Distance Matrix (Bellman-Ford All Pairs)

	0	1	2	3
0	0	3	5	6
1	5	0	2	3
2	3	6	0	1
3	2	5	7	0

Bellman-Ford All Pairs Time: 4.02 ms (avg of 5 runs)

Step 31/64: Checking if path from 3 to 2 can be improved via vertex 1

Reset

Previous Step

Next Step

Run to Completion

Algorithm Log

Generated 64 algorithm steps
Algorithm initialized
Matrix parsed successfully
Timing comparison (average of 5 runs):
Floyd-Warshall: 2.02 ms
Bellman-Ford: 4.02 ms
Difference: 2.00 ms

Distance Matrix (Floyd-Warshall)

	0	1	2	3
0	0	3	5	6
1	5	0	2	3
2	3	6	0	1
3	2	5	7	0

Floyd-Warshall Time: 2.02 ms (avg of 5 runs)

Distance Matrix (Bellman-Ford All Pairs)

	0	1	2	3
0	0	3	5	6
1	5	0	2	3
2	3	6	0	1
3	2	5	7	0

Bellman-Ford All Pairs Time: 4.02 ms (avg of 5 runs)

Initial state[Reset](#)[Previous Step](#)[Next Step](#)[Run to Completion](#)

Step 57: Checking if path from 2 to 0 can be improved via vertex 3 - Improved! 5 \rightarrow 3
Step 58: Checking if path from 2 to 1 can be improved via vertex 3 - Improved! 8 \rightarrow 6
Step 59: Checking if path from 2 to 2 can be improved via vertex 3 - No improvement (current: 0, via 3: 8)
Step 60: Checking if path from 2 to 3 can be improved via vertex 3 - No improvement (current: 1, via 3: 1)
Step 61: Checking if path from 3 to 0 can be improved via vertex 3 - No improvement (current: 2, via 3: 2)
Step 62: Checking if path from 3 to 1 can be improved via vertex 3 - No improvement (current: 5, via 3: 5)
Step 63: Checking if path from 3 to 2 can be improved via vertex 3 - No improvement (current: 7, via 3: 7)
Step 64: Checking if path from 3 to 3 can be improved via vertex 3 - No improvement (current: 0, via 3: 0)

Step 2: Checking if path from 0 to 1 can be improved via vertex 0 - No improvement (current: 3, via 0: 3)
Step 3: Checking if path from 0 to 2 can be improved via vertex 0 - No improvement (current: ∞ , via 0: ∞)
Step 4: Checking if path from 0 to 3 can be improved via vertex 0 - No improvement (current: 7, via 0: 7)
Step 5: Checking if path from 1 to 0 can be improved via vertex 0 - No improvement (current: 8, via 0: 8)
Step 6: Checking if path from 1 to 1 can be improved via vertex 0 - No improvement (current: 0, via 0: 11)
Step 7: Checking if path from 1 to 2 can be improved via vertex 0 - No improvement (current: 2, via 0: ∞)
Reverted to step 6
Step 7: Checking if path from 1 to 2 can be improved via vertex 0 - No improvement (current: 2, via 0: ∞)

GITHUB LINK:

https://github.com/RBROHANTH/DAA_PROJECT_Floyd-s-Alogorithm.git