Intro to R
 pbdR
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 Wrapup

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Introducing R: From Your Laptop to HPC and Big Data

Drew Schmidt and George Ostrouchov

November 18, 2013



Intro to R nbdR IAMpda Stats eg's DMAT pbdDMAT eg's Wrapup

The **pbd**R Core Team

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Support

This work used resources of National Institute for Computational Sciences at the University of Tennessee, Knoxville, which is supported by the Office of Cyberinfrastructure of the U.S. National Science Foundation under Award No. ARRA-NSF-OCI-0906324 for NICS-RDAV center. This work used resources of the Newton HPC Program at the University of Tennessee, Knoxville, This work also used resources of the Oak Ridge Leadership Computing Facility at the Oak Ridge National Laboratory, which is supported by the Office of Science of the U.S. Department of Energy under Contract No. DE-AC05-00OR22725.



¹University of Tennessee. Supported in part by the project "NICS Remote Data Analysis and Visualization Center" funded by the Office of Cyberinfrastructure of the U.S. National Science Foundation under Award No. ARRA-NSF-OCI-0906324 for NICS-RDAV center.

²Oak Ridge National Laboratory. Supported in part by the project "Visual Data Exploration and Analysis of Ultra-large Climate Data" funded by U.S. DOE Office of Science under Contract No. DE-AC05-00OR22725.

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About This Presentation

Downloads

This presentation and supplemental materials are available at:

http://r-pbd.org/tutorial



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About This Presentation

Tutorial Evaluations

http://bit.ly/sc13-tut-mf08



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About This Presentation

Speaking Serial R with a Parallel Accent

The content of this presentation is based in part on the **pbdDEMO** vignette *Speaking Serial R with a Parallel Accent*

http://goo.gl/HZkRt

It contains more examples, and sometimes added detail.



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About This Presentation

Installation Instructions

Installation instructions for setting up a pbdR environment are available:

This includes instructions for installing R, MPI, and pbdR.



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About This Presentation

Conventions For Code Presentation

We will use two different forms of syntax highlighting. One for displaying results from an interactive R session:

```
1 R> "interactive"
2 [1] "interactive"
```

and one for presenting R scripts

```
1 "not interactive"
```



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Contents

- Introduction to R
 - What is R?
 - Basic Numerical Operations in R
 - R Syntax for Data Science: Not A Matlab Clone!



- lingua franca for data analytics and statistical computing.
- Part programming language, part data analysis package.
- Dialect of S (Bell Labs).
- Syntax designed for data.





Intro to R

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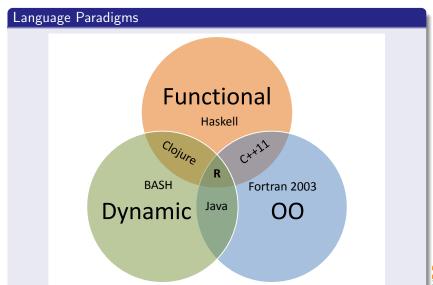
Wrapup

What is R?





What is R?





Data Types

- Storage: logical, int, double, double complex, character
- Structures: vector, matrix, array, list, dataframe
- Caveats: (Logical) TRUE, FALSE, NA

For the remainder of the tutorial, we will restrict ourselves to real number matrix computations.



• The default method is to print:

```
R> sum
2 function (..., na.rm = FALSE) .Primitive("sum")
```

Use <- for assignment:

```
R> x <- 1
2 R> x+1
  [1] 2
```

- Naming rules: mostly like C.
- R is case sensitive.
- We use . the way most languages use _, e.g., La.svd() instead of La svd().
- We use \$ (sometimes @) the way most languages use .



What is R?

Basics (2 of 2)

• Use ? or ?? to search help

```
1 R> ?set.seed
```

- 2 R> ?comm.set.seed
- No documentation for comm.set.seed in specified packages and libraries:
- 4 you could try ??comm.set.seed
- 5 R> ??comm.set.seed



What is R?

Addons and Extras

R has the Comprehensive R Archive Network (CRAN), which is a package repository like CTAN and CPAN.

From R

```
install.packages("pbdMPI") # install
library(pbdMPI) # load
```

From Shell

```
1 R CMD INSTALL pbdMPI_0.1-6.tar.gz
```



```
Lists (1 of 1)
```

```
R>
         <- list(a=1, b="a")
2
  R> 1
  $a
   [1] 1
5
6
7
  $Ъ
       "a"
   [1]
8
  R> 1$a
   [1] 1
10
11
12
  R> list(x=list(a=1, b="a"), y=TRUE)
13
  $x
  $x$a
14
   [1] 1
15
16
17
  $x$b
   [1] "a"
18
19
20
21
  $ v
22
   [1]
       TRUE
```



Vectors and Matrices (1 of 2)

```
R > c(1, 2, 3, 4, 5, 6)
   [1] 1 2 3 4 5 6
3
  R > matrix(1:6, nrow=2, ncol=3)
        [,1] [,2] [,3]
   [1,]
7
   [2,]
8
  R > x < -matrix(1:6, nrow=2, ncol=3)
10
  R > x[, -1]
11
        [,1] [,2]
12
  [1,]
13
   [2,]
14
15
  R > x[1, 1:2]
16
   [1] 1 3
17
```



Vectors and Matrices (2 of 2)

```
R> dim(x)
   [1] 2 3
3
      dim(x) <- NULL
5
  R> x
   [1] 1 2 3 4 5 6
7
  R > dim(x) < -c(3,2)
9
  R> x
         [,1] [,2]
10
   [1,]
11
   [2,]
12
                  5
   [3,]
            3
                  6
13
```



Vector and Matrix Arithmetic (1 of 2)

```
R > 1:4 + 4:1
   [1] 5 5 5 5
3
  R > x < -matrix(0, nrow=2, ncol=3)
  R> x
         [,1] [,2] [,3]
8
   [1,]
   [2,]
10
        + 1:3
11
  R.> x
         [,1] [,2]
                    [,3]
12
   [1,]
13
   [2,]
14
```



Vector and Matrix Arithmetic (2 of 2)

```
R> x <- matrix(1:6, nrow=2)
  R> x*x
         [,1]
               [,2] [,3]
   [1,]
                       25
                   9
6
7
   [2,]
                 16
                       36
  R> x %*% x
  Error in x %*% x : non-conformable arguments
10
11
  R> t(x) %*% x
         [,1] [,2]
                     [,3]
12
   [1.]
                 11
                       17
13
   [2,]
           11
                 25
                       39
14
   [3,]
           17
                 39
                       61
15
16
17
  R> crossprod(x)
         [,1] [,2]
                     [,3]
18
   [1,]
            5
                 11
                       17
19
   [2,]
           11
                 25
                       39
20
   [3.]
           17
                 39
                       61
21
```



Linear Algebra (1 of 2): Matrix Inverse

$$x_{n \times n}$$
 invertible $\iff \exists y_{n \times n} (xy = yx = Id_{n \times n})$

```
1 R> x <- matrix(rnorm(5*5), nrow=5)
2 R> y <- solve(x)
3
4 R> round(x %*% y)
5 [,1] [,2] [,3] [,4] [,5]
6 [1,] 1 0 0 0 0
7 [2,] 0 1 0 0 0
8 [3,] 0 0 1 0 0
9 [4,] 0 0 0 1 0
10 [5,] 0 0 0 0 1
```



http://r-pbd.org/tutorial

Linear Algebra (2 of 2): Singular Value Decomposition

$$x = U\Sigma V^T$$

```
x <- matrix(rnorm(2*3), nrow=3)
     svd(x)
  R>
  $d
   [1]
       2.4050716 0.3105008
5
6
7
  $u
              [,1] [,2]
  [1,]
        0.8582569 -0.1701879
        0.2885390
                    0.9402076
        0.4244295 -0.2950353
10
11
12
  $ v
13
                [,1]
                            [,2]
        -0.05024326 -0.99873701
14
   [1,]
15
   [2,]
        -0.99873701 0.05024326
```



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More than just a Matlab clone...

- Data science (machine learning, statistics, data mining, ...) is mostly matrix algebra.
 - So what about Matlab/Python/Julia/...?
- The one you prefer depends more on your "religion" rather than differences in capabilities.
- As a data analysis package, R is king.



Simple Statistics (1 of 2): Summary Statistics

```
R > x < -matrix(rnorm(30, mean=10, sd=3), nrow=10)
  R> mean(x)
   [1] 9.825177
  R> median(x)
   [1] 9.919243
8
  R> sd(as.vector(x))
   [1] 3.239388
10
11
  R> colMeans(x)
12
        9.661822 10.654686 9.159025
13
  [1]
14
     apply(x, MARGIN=2, FUN=sd)
15
  [1] 2.101059 3.377347 4.087131
16
```



Simple Statistics (2 of 2): Sample Covariance

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$

```
1  x <- matrix(rnorm(30), nrow=10)
2  # least recommended
4  cm <- colMeans(x)
5  crossprod(sweep(x, MARGIN=2, STATS=cm))
6  # less recommended
8  crossprod(scale(x, center=TRUE, scale=FALSE))
9  # recommended
11  cov(x)</pre>
```



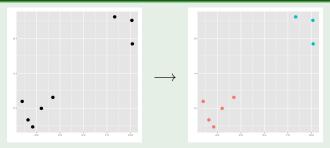
Advanced Statistics (1 of 2): Principal Components

PCA = centering + scaling + rotation (via SVD)

```
R > x < - matrix(rnorm(30), nrow=10)
2
  R> prcomp(x, retx=TRUE, scale=TRUE)
  Standard deviations:
   [1] 1.1203373 1.0617440 0.7858397
6
  Rotation:
                PC1
                            PC2
                                        PC3
8
  [1.]
        0.71697825 -0.3275365
                                 0.6153552
       -0.03382385 0.8653562
                                 0.5000147
   [2,]
10
   [3,]
        0.69627447
                     0.3793133 -0.6093630
11
```



Advanced Statistics (2 of 2): k-Means Clustering



```
1 R> x <- rbind(matrix(rnorm(5*2, mean=0), ncol=2),
matrix(rnorm(3*2, mean=10), ncol=2))
```



Advanced Statistics (2 of 2): k-Means Clustering

```
R> kmeans(x, centers=2)
  K-means clustering with 2 clusters of sizes 5. 3
3
  Cluster means:
           [,1]
                      [,2]
5
  1 -0.1080612 -0.2827576
  2 9.5695365 9.3191892
8
  Clustering vector:
  [1] 1 1 1 1 1 2 2 2
10
11
  Within cluster sum of squares by cluster:
12
  [1] 14.675072 7.912641
13
   (between SS / total SS = 93.9 %)
14
15
16
  Available components:
17
  [1] "cluster"
                     "centers"
                                      "totss"
18
      "withinss"
                      "tot.withinss"
  [6] "betweenss"
                      "size"
19
```



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- pbdR Paradigms



Programming with Big Data in R (pbdR)

Striving for Productivity, Portability, Performance

- Bridging high-performance C with high-productivity of R
- Scalable, big data analytics.
- Free^a R packages.
- Distributed data details implicitly managed.
- Methods have syntax identical to R.
- Powered by state of the art numerical libraries (MPI, ScaLAPACK, . . .)



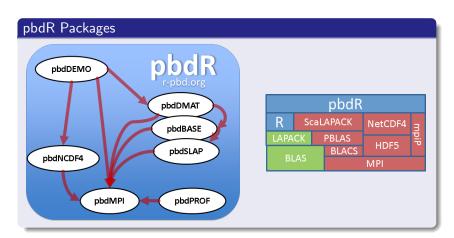
Programming with Big Data in R

^aMPL, BSD, and GPL licensed

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The pbdR Project





The pbdR Project

pbdR on HPC Resources

University of Tennessee

- Kraken (XSEDE)
- Nautilus
- Darter
- Newton

Oak Ridge National Lab

- Titan
- Lens
- Chester
- Sith

Other Resources

- Stampede, TACC (XSEDE)
- tara, UMBC
- Hopper, NERSC
- Edison, NERSC

If you are interested in installing pbdR: RBigData@gmail.com



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The pbdR Project

Example Syntax

```
1 x <- x[-1, 2:5]

2 x <- log(abs(x) + 1)

3 xtx <- t(x) %*% x

4 ans <- svd(solve(xtx))
```

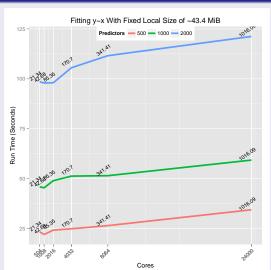
Look familiar?

The above runs on 1 core with R or 10,000 cores with pbdR



The pbdR Project

Least Squares Benchmark





The pbdR Project

Profiling with pbdPROF

1. Rebuild **pbdR** packages

```
R CMD INSTALL
   pbdMPI_0.2-1.tar.gz \
    --configure-args= \
   "--enable-pbdPROF"
```

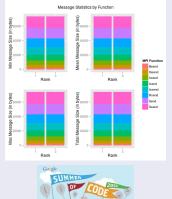
2. Run code

```
mpirun -np 64 Rscript
my_script.R
```

3. Analyze results

```
library(pbdPROF)
prof <- read.prof(
     "profiler_output.mpiP")
plot(prof)</pre>
```

Publication-quality graphs





pbdR Paradigms

pbdR Paradigms

Programs that use pbdR utilize:

- Batch execution
- Single Program/Multiple Data (SPMD) style

And generally utilize:

Data Parallelism



pbdR Paradigms

Batch Execution

- Non-interactive
- Use

```
Rscript my_script.r
```

or

1 R CMD BATCH my_script.r

In parallel:

```
1 mpirun -np 2 Rscript my_par_script.r
```



Single Program/Multiple Data (SPMD)

- Difficult to describe, easy to do...
- Only one program is written, executed in batch on all processors.
- Different processors are autonomous; there is no manager.
- The dominant programming model for large machines.



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Contents

- Introduction to pbdMPI
 - Managing a Communicator
 - Reduce, Gather, Broadcast, and Barrier
 - Other pbdMPI Tools



Managing a Communicator

Message Passing Interface (MPI)

- MPI: Standard for managing communications (data and instructions) between different nodes/computers.
- Implementations: OpenMPI, MPICH2, Cray MPT, . . .
- Enables parallelism (via communication) on distributed machines.
- Communicator: manages communications between processors.



MPI Operations (1 of 2)

 Managing a Communicator: Create and destroy communicators.

```
init() — initialize communicator
finalize() — shut down communicator(s)
```

 Rank query: determine the processor's position in the communicator.

```
comm.rank() — "who am I?"
comm.size() — "how many of us are there?"
```

• **Printing**: Printing output from various ranks.

```
comm.print(x)
comm.cat(x)
```

WARNING: only use these functions on *results*, never on yet-to-be-computed things.



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Managing a Communicator

Quick Example 1

Rank Query: 1_rank.r

```
library(pbdMPI, quiet = TRUE)
  init()
3
  my.rank <- comm.rank()</pre>
  comm.print(my.rank, all.rank=TRUE)
6
  finalize()
```

Execute this script via:

mpirun -np 2 Rscript 1_rank.r

Sample Output:

```
COMM \cdot RANK = O
  [1] 0
2
  COMM.RANK = 1
  [1] 1
```



Managing a Communicator

Quick Example 2

Hello World: 2_hello.r

```
library(pbdMPI, quiet=TRUE)
init()

comm.print("Hello, world")

comm.print("Hello again", all.rank=TRUE, quiet=TRUE)

finalize()
```

Execute this script via:

```
mpirun -np 2 Rscript 2_hello.r
```

Sample Output:

```
COMM.RANK = 0

[1] "Hello, world"

[1] "Hello again"

[1] "Hello again"
```



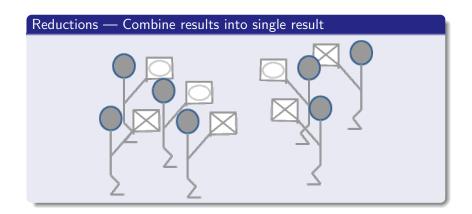
Reduce, Gather, Broadcast, and Barrier

MPI Operations

- Reduce
- Gather
- Broadcast
- Barrier

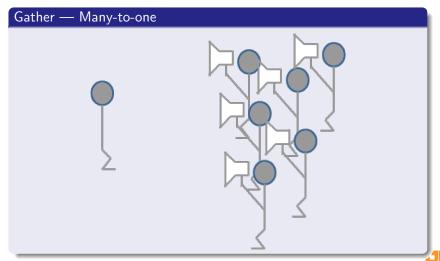


Reduce, Gather, Broadcast, and Barrier



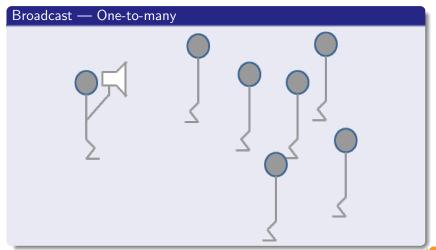


Reduce, Gather, Broadcast, and Barrier





Reduce, Gather, Broadcast, and Barrier





Reduce, Gather, Broadcast, and Barrier

Barrier — Synchronization Barrier **Barrier** Barrier



Reduce, Gather, Broadcast, and Barrier

MPI Operations (2 of 2)

- Reduction: each processor has a number x; add all of them up, find the largest/smallest,
 reduce(x, op='sum') reduce to one
- allreduce(x, op='sum') reduce to all
- Gather: each processor has a number; create a new object on some processor containing all of those numbers.
 gather(x) — gather to one allgather(x) — gather to all
- Broadcast: one processor has a number x that every other processor should also have.
 bcast(x)
- Barrier: "computation wall"; no processor can proceed until all processors can proceed.
 barrier()



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Other pbdMPI Tools

MPI Package Controls

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The .SPMD.CT object allows for setting different package options with **pbdMPI**. See the entry *SPMD Control* of the **pbdMPI** manual for information about the .SPMD.CT object:

http://cran.r-project.org/web/packages/pbdMPI/pbdMPI.pdf



- comm.set.seed(diff=TRUE) Independent streams via the rlecuyer package.
- comm.set.seed(seed=1234, diff=FALSE) All processors use the same seed seed=1234
- comm.set.seed(diff=FALSE) All processors use the same seed, determined by processor 0 (using the system clock and PID of processor 0).



Other pbdMPI Tools

Other Helper Tools

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pbdMPI Also contains useful tools for Manager/Worker and task parallelism codes:

- Task Subsetting: Distributing a list of jobs/tasks get.jid(n)
- *ply: Functions in the *ply family.
 pbdApply(X, MARGIN, FUN, ...) analogue of apply()
 pbdLapply(X, FUN, ...) analogue of lapply()
 pbdSapply(X, FUN, ...) analogue of sapply()



```
Start by loading the package:
```

```
1 library(pbdMPI, quiet = TRUE)
```

Always initialize before starting and finalize when finished:

```
init()

;

;

;

;

;

finalize()
```



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Other pbdMPI Tools

Basic MPI Exercises

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• Experiment with Quick Examples 1 through 6, running them on 2, 4, and 8 processors.



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Contents

- The Generalized Block Distribution
 - The GBD Data Structure
 - GBD: Example 1GBD: Example 2



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The GBD Data Structure

Distributing Data

Problem: How to distribute the data

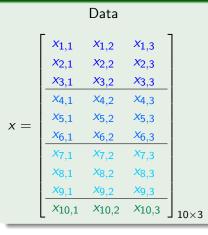
$$x = \begin{bmatrix} x_{1,1} & x_{1,2} & x_{1,3} \\ x_{2,1} & x_{2,2} & x_{2,3} \\ x_{3,1} & x_{3,2} & x_{3,3} \\ x_{4,1} & x_{4,2} & x_{4,3} \\ x_{5,1} & x_{5,2} & x_{5,3} \\ x_{6,1} & x_{6,2} & x_{6,3} \\ x_{7,1} & x_{7,2} & x_{7,3} \\ x_{8,1} & x_{8,2} & x_{8,3} \\ x_{9,1} & x_{9,2} & x_{9,3} \\ x_{10,1} & x_{10,2} & x_{10,3} \end{bmatrix}$$

?



The GBD Data Structure

Distributing a Matrix Across 4 Processors: Block Distribution



Processors

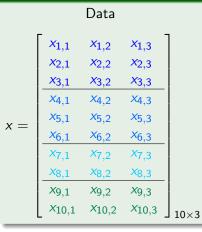


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The GBD Data Structure

Distributing a Matrix Across 4 Processors: Local Load Balance



Processors

0

1 2 3



The GBD Data Structure

The GBD Data Structure

Throughout the examples, we will make use of the Generalized Block Distribution, or GBD distributed matrix structure.

 $x_{1.1}$

 $X_{2.1}$

X3.1

X4.1

X5.1

 $x_{6,1}$

X7.1

X9.1

X10.1

X1.2

 $X_{2,2}$

X3.2

X4.2

X5.2

 $x_{6,2}$

X7.2

X8.2

X9.2

 $X_{10.2}$

 $x_{1.3}$

 $X_{2.3}$

X3,3

X4.3

X5,3

 $x_{6.3}$

X7.3

X8.3

X9.3

X10.3

- GBD is distributed. No processor owns all the data.
- ② GBD is non-overlapping. Rows uniquely assigned to processors.
- 3 GBD is row-contiguous. If a processor owns one element of a row, it owns the entire row.
- 4 GBD is globally row-major, locally column-major.
- GBD is often locally balanced, where each processor owns (almost) the same amount of data. But this is not required.

0	The last row of the local storage of a processor is adjacent (by global row) to
	the first row of the local storage of next processor (by communicator number)
	that owns data.

Q GBD is (relatively) easy to understand, but can lead to bottlenecks if you have many more columns than rows.



GBD: Example 1

Understanding GBD: Global Matrix

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



GBD: Example 1

Understanding GBD: Load Balanced GBD

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

 $Processors = 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5$



http://r-pbd.org/tutorial

GBD: Example 1

Understanding GBD: Local View

```
X<sub>12</sub>
                 X13
                         X14
                                X<sub>15</sub>
                                        X16
                                                X17
                                                        X<sub>18</sub>
                                                                X19
  x_{21}
         X22
                 X23
                         X24
                                 X25
                                        X26
                                                X27
                                                        X28
                                                                X29
  X31
         X32
                 X33
                         X34
                                X35
                                        X36
                                                X37
                                                        X38
                                                                X39
 X41
         X42
                 X43
                         X44
                                 X45
                                        X46
                                                X47
                                                        X48
                                                                X49
                         X54
                                 X55
                                        X56
                                                X57
                                                        X58
                                                                X59
         X62
                         X<sub>64</sub>
  X_{61}
                                 X<sub>65</sub>
                                        X66
                                                X67
                                                        X68
                                                                X69
X<sub>71</sub>
          X72
                 X73
                         X74
                                 X75
                                         X76
                                                X77
                                                        X78
  X81
          X82
                 X83
                         X84
                                 X85
                                         X86
                                                X87
                                                        X88
  X91
          X92
                 X93
                         X94
                                 X95
                                         X96
                                                X97
                                                        X98
```

Processors = 0 1 2 3 4 5



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GBD: Example 2

Understanding GBD: Non-Balanced GBD

•00

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ \hline x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ \hline x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ \hline x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



GBD: Example 2

Understanding GBD: Local View $\int_{0\times9}$ *X*₁₆ X₁₇ X_{11} X_{12} X_{13} X_{14} X_{15} X_{18} X_{19} X22 X21 X23 X24 X25 X26 X27 X28 X29 X31 X32 X33 X34 X35 X36 X37 X38 X39 X45 X46 X₄₁ X42 X43 X44 X47 X48 X49 X51 *X*52 X53 X55 X56 X57 *X*58 *X*59 X₆₁ X₆₂ X₆₃ X₆₄ X₆₅ X₆₆ X67 X₆₈ X69 *X*71 X72 X73 X78 X79 X74 X75 X76 X77 ∫0×9 X₈₁ X82 X83 X85 X86 X87 X88 X98 X91 X92 X93 X94 X95 X96 X97 *X*99 Processors = 0 3

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GBD: Example 2

Quick Comment for GBD

Local pieces of GBD distributed objects will be given the suffix .gbd to visually help distinguish them from global objects. This suffix carries no semantic meaning.



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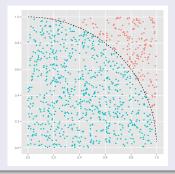
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pbdMPI Example: Monte Carlo Simulation

Example 1: Monte Carlo Simulation

Sample *N* uniform observations (x_i, y_i) in the unit square $[0,1] \times [0,1]$. Then

$$\pi pprox 4\left(rac{\#\ \textit{Inside Circle}}{\#\ \textit{Total}}
ight) = 4\left(rac{\#\ \textit{Blue}}{\#\ \textit{Blue} + \#\ \textit{Red}}
ight)$$





pbdMPI Example: Monte Carlo Simulation

Example 1: Monte Carlo Simulation GBD Algorithm

- Let n be big-ish; we'll take n = 50,000.
- **2** Generate an $n \times 2$ matrix x of standard uniform observations.
- **3** Count the number of rows satisfying $x^2 + y^2 \le 1$
- Ask everyone else what their answer is; sum it all up.
- \odot Take this new answer, multiply by 4 and divide by n
- 1 If my rank is 0, print the result.



Example 1: Monte Carlo Simulation Code

Serial Code

```
1 N <- 50000
2 X <- matrix(runif(N * 2), ncol=2)
3 r <- sum(rowSums(X^2) <= 1)
4 PI <- 4*r/N
5 print(PI)</pre>
```

Parallel Code

```
library(pbdMPI, quiet = TRUE)
init()
comm.set.seed(diff=TRUE)

N.gbd <- 50000 / comm.size()
X.gbd <- matrix(runif(N.gbd * 2), ncol = 2)
r.gbd <- sum(rowSums(X.gbd^2) <= 1)
r <- allreduce(r.gbd)
PI <- 4*r/(N.gbd * comm.size())
comm.print(PI)

finalize()
```



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pbdMPI Example: Monte Carlo Simulation

Note

For the remainder, we will exclude loading, init, and finalize calls.



pbdMPI Example: Sample Covariance

Example 2: Sample Covariance

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$



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pbdMPI Example: Sample Covariance

Example 2: Sample Covariance GBD Algorithm

- lacktriangle Determine the total number of rows N.
- 2 Compute the vector of column means of the full matrix.
- 3 Subtract each column's mean from that column's entries in each local matrix.
- 4 Compute the crossproduct locally and reduce.
- **5** Divide by N-1.



pbdMPI Example: Sample Covariance

Example 2: Sample Covariance Code

Serial Code

```
1  N <- nrow(X)
2  mu <- colSums(X) / N
3
4  X <- sweep(X, STATS=mu, MARGIN=2)
5  Cov.X <- crossprod(X) / (N-1)
6
7  print(Cov.X)</pre>
```

Parallel Code

```
1 N <- allreduce(nrow(X.gbd), op="sum")
2 mu <- allreduce(colSums(X.gbd) / N, op="sum")
3 
4 X.gbd <- sweep(X.gbd, STATS=mu, MARGIN=2)
5 Cov.X <- allreduce(crossprod(X.gbd), op="sum") / (N-1)
6 
7 comm.print(Cov.X)</pre>
```



pbdMPI Example: Linear Regression

Example 3: Linear Regression

Find β such that

$$\mathsf{y} = \mathsf{X} oldsymbol{eta} + oldsymbol{\epsilon}$$

When **X** is full rank,

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$$



- Locally, compute $tx = x^T$
- 2 Locally, compute A = tx * x. Query every other processor for this result and sum up all the results.
- **3** Locally, compute B = tx * y. Query every other processor for this result and sum up all the results.
- **1** Locally, compute $A^{-1} * B$



pbdMPI Example: Linear Regression

Example 3: Linear Regression Code

Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4 ols <- solve(A) %*% B
```

Parallel Code

```
tX.gbd <- t(X.gbd)
tX.gbd <- t(X.gbd)
tX.gbd <- t(X.gbd %*% X.gbd, op = "sum")
B <- allreduce(tX.gbd %*% y.gbd, op = "sum")
tols <- solve(A) %*% B</pre>
```



pbdMPI Example: Linear Regression

MPI Exercises

• Experiment with Statistics Examples 1 through 3, running them on 2, 4, and 8 processors.



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pbdMPI Example: Linear Regression

Advanced MPI Exercises I

- Write a script that will have each processor randomly take a sample of size 1 of TRUE and FALSE. Have each processor print its result.
- Modify the script in Exercise 1 above to determine if any processors sampled TRUE. Do the same to determine if all processors sampled TRUE. In each case, print the result. Compare to the functions comm.all() and comm.any().
- **3** Generate 50,000,000 (total) random normal values in parallel on 2, 4, and 8 processors. Time each run.



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pbdMPI Example: Linear Regression

Advanced MPI Exercises II

- Obstribute the matrix x <- matrix(1:24, nrow=12) in GBD format across 4 processors and call it x.spmd.
 - Add x.spmd to itself.
 - 2 Compute the mean of x.spmd.
 - 3 Compute the column means of x.spmd.



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 - Introduction to Distributed Matrices
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Introduction to Distributed Matrices

Distributed Matrices

Most problems in data science are matrix algebra problems, so:

Distributed matrices ⇒ Handle Bigger data



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Introduction to Distributed Matrices

Distributed Matrices

High level OOP allows *native* serial R syntax:

```
1 x <- x[-1, 2:5]

2 x <- log(abs(x) + 1)

3 xtx <- t(x) %*% x

4 ans <- svd(solve(xtx))
```

However. . .



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Introduction to Distributed Matrices

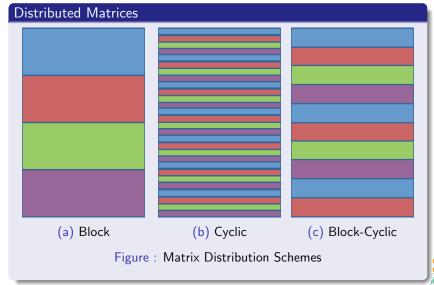
Distributed Matrices

DMAT:

- Distributed MATrix data structure.
- No single processor should hold all of the data.
- Block-cyclic matrix distributed across a 2-dimensional grid of processors.
- Very robust, but confusing data structure.



Introduction to Distributed Matrices



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Introduction to Distributed Matrices

Distributed Matrices (a) 2d Block (b) 2d Cyclic (c) 2d Block-Cyclic Matrix Distribution Schemes Onto a 2-Dimensional Grid

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Introduction to Distributed Matrices

Processor Grid Shapes

$$\begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}^{T} \qquad \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$
(a) 1×6 (b) 2×3 (c) 3×2 (d) 6×1

Table: Processor Grid Shapes with 6 Processors



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Introduction to Distributed Matrices

Distributed Matrices

The data structure is a special R class (in the OOP sense) called ddmatrix. It is the "under the rug" storage for a block-cyclic matrix distributed onto a 2-dimensional processor grid.

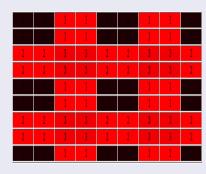
with prototype

```
\label{eq:new("ddmatrix")} \begin{split} \text{new("ddmatrix")} &= \begin{cases} \textbf{Data} &= \text{matrix}(0.0) \\ \textbf{dim} &= \text{c(1,1)} \\ \textbf{ldim} &= \text{c(1,1)} \\ \textbf{bldim} &= \text{c(1,1)} \\ \textbf{CTXT} &= 0.0 \end{cases} \end{split}
```



Distributed Matrices: The Data Structure

Example: an 9×9 matrix is distributed with a "block-cycling" factor of 2×2 on a 2×2 processor grid:



$$= \begin{cases} \textbf{Data} &= \texttt{matrix}(\ldots) \\ \textbf{dim} &= \texttt{c}(9, 9) \\ \textbf{Idim} &= \texttt{c}(\ldots) \\ \textbf{bIdim} &= \texttt{c}(2, 2) \\ \textbf{CTXT} &= 0 \end{cases}$$

See http://acts.nersc.gov/scalapack/hands-on/datadist.html



DMAT Distributions

Understanding Dmat: Global Matrix X11 X₁₂ X₁₃ X14 X₁₅ X16 X17 X₁₈ X19 X21 X22 X23 X24 X25 X26 X27 X28 X29 X31 X32 X33 X34 X35 X36 X37 X38 X39 X46 X49 X_{41} X42 X43 X44 X45 X47 X48 x = X_{51} X₅₂ X53 X54 X55 *X*56 X57 X58 X59 X61 X62 X63 X64 *X*65 X66 X67 X68 *X*69 X74 X76 X78 X71 X72 *X*73 *X*75 *X*77 *X*79 X81 X82 X83 X84 X85 X86 *X*87 X88 *X*89 X91 X92 *X*93 X94 X95 X96 X97 *X*98 *X*99



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DMAT Distributions

DMAT: 1-dimensional Row Block

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (1,0) \\ (2,0) \\ (3,0) \end{vmatrix}$$



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DMAT Distributions

DMAT: 2-dimensional Row Block

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ \hline x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



DMAT Distributions

DMAT: 1-dimensional Row Cyclic

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ \hline X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ \hline X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ \hline X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ \hline X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ \hline X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ \hline X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ \hline X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ \hline X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (1,0) \\ (2,0) \\ (3,0) \end{vmatrix}$$



http://r-pbd.org/tutorial

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DMAT Distributions

DMAT: 2-dimensional Row Cyclic

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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DMAT Distributions

DMAT: 2-dimensional Block-Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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pbdDMAT

The DMAT Data Structure

The more complicated the processor grid, the more complicated the distribution.



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pbdDMAT

DMAT: 2-dimensional Block-Cyclic with 6 Processors

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ \hline X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



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X54

X₆₄

X94

X19

X29

X59

X69

*X*99

X39

X49

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pbdDMAT

Intro to R

Understanding DMAT: Local View

*X*13

X23

X53

X63

X93

$$(0,1)$$
 $(0,1)$

 X_{16}

 X_{26}

X56

X66

X96

X36

X46

X86

X55

X95

X35

X₄₅

Processor grid =

X31

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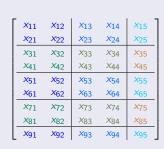
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pbdDMAT

The DMAT Data Structure

- ① DMAT is distributed. No one processor owns all of the matrix.
- ② DMAT is non-overlapping. Any piece owned by one processor is owned by no other processors.
- ① DMAT can be row-contiguous or not, depending on the processor grid and blocking factor used.
- OMAT is locally column-major and globally, it depends...
- GBD is a generalization of the one-dimensional block DMAT distribution. Otherwise there is no relation.
- O DMAT is confusing, but very robust.





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pbdDMAT

Pros and Cons of This Data Structure

Pros

 Fast for distributed matrix computations

Cons

• Literally everything else

This is why we hide most of the distributed details.

The details are there if you want them (you don't want them).



pbdDMAT

Distributed Matrix Methods

pbdDMAT has over 100 methods with *identical* syntax to R:

- `[`, rbind(), cbind(), ...
- lm.fit(), prcomp(), cov(), ...
- `%*%`, solve(), svd(), norm(), ...
- median(), mean(), rowSums(), ...

Serial Code

1 cov(x)

Parallel Code

1 cov(x)



pbdDMAT

Comparing pbdMPI and pbdDMAT

pbdMPI:

- MPI + sugar.
- GBD not the only structure pbdMPI can handle (just a useful convention).

pbdDMAT:

- More of a software package.
- DMAT structure must be used for pbdDMAT.
- If the data is not 2d block-cyclic compatible, DMAT will definitely give the wrong answer.



Quick Comments for Using pbdDMAT

Start by loading the package:

```
library(pbdDMAT, quiet = TRUE)
```

② Always initialize before starting and finalize when finished:

```
init.grid()
3
  finalize()
```

3 Distributed DMAT objects will be given the suffix .dmat to visually help distinguish them from global objects. This suffix carries no semantic meaning.



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- Examples Using pbdDMAT
 - Statistics Examples with pbdDMAT
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Statistics Examples with pbdDMAT

Linear Regression

Serial Code

Parallel Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4
5 ols <- solve(A) %*% B
6
7 # or
8 ols <- lm.fit(X, y)
```



Statistics Examples with pbdDMAT

Example 5: PCA

PCA: pca.r

```
library(pbdDMAT, quiet=T)
    init.grid()
2
3
4
5
6
7
   n <- 1e4
   p <- 250
   comm. set . seed ( diff=T)
8
   x.dmat <- ddmatrix("rnorm", nrow=n, ncol=p, mean=100, sd=25)
10
    pca <- prcomp(x=x.dmat. retx=TRUE, scale=TRUE)</pre>
11
    prop_var <- cumsum(pca$sdev)/sum(pca$sdev)</pre>
12
    i \leftarrow max(min(which(prop_var > 0.9)) - 1, 1)
13
14
   y.dmat \leftarrow pcax[, 1:i]
15
   comm.cat("\nCols: ", i, "\n", quiet=T)
16
   comm. cat("\%Cols:", i/dim(x.dmat)[2], "\n\n", quiet=T)
17
18
19
    finalize()
```

Execute this script via:

Sample Output:

```
1 mpirun -np 2 Rscript 5-pca.r 1 Cols: 221 %Cols: 0.884
```



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Statistics Examples with pbdDMAT

Distributed Matrices

pbdDEMO contains many other examples of reading and managing GBD and DMAT data



RandSVD

Randomized SVD1

Prototype for Randomized SVD

Given an $m \times n$ matrix A, a target number k of singular vectors, and an exponent q (say, q = 1 or q = 2), this procedure computes an approximate rank-2k factorization $U\Sigma V^*$, where U and V are orthonormal, and Σ is nonnegative and diagonal.

Stage A:

- Generate an $n \times 2k$ Gaussian test matrix Ω .
- 2 Form Y = (AA*)^qAΩ by multiplying alternately with A and A*. 3 Construct a matrix Q whose columns form an orthonormal basis for
 - the range of Y.
- Stage B: 4 Form $B = Q^*A$.
- Compute an SVD of the small matrix: $B = \tilde{U}\Sigma V^*$.
- 6 Set $U = O\widetilde{U}$.

Note: The computation of Y in step 2 is vulnerable to round-off errors. When high accuracy is required, we must incorporate an orthonormalization step between each application of A and A^* ; see Algorithm 4.4.

Algorithm 4.4: Randomized Subspace Iteration Given an $m \times n$ matrix A and integers ℓ and q, this algorithm computes an $m \times \ell$ orthonormal matrix Q whose range approximates the range of A. Draw an $n \times \ell$ standard Gaussian matrix Ω .

- Form $Y_0 = A\Omega$ and compute its OR factorization $Y_0 = Q_0R_0$. for j = 1, 2, ..., q
- Form $\tilde{Y}_i = A^*Q_{i-1}$ and compute its QR factorization $\tilde{Y}_i = \tilde{Q}_i\tilde{R}_i$. Form $Y_i = A\widetilde{Q}_i$ and compute its QR factorization $Y_i = Q_iR_i$.
- 6 end $Q = Q_a$.

¹Halko N, Martinsson P-G and Tropp J A 2011 Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions SIAM Rev. 53 217-88

Serial R

```
randSVD \leftarrow function(A, k, g=3)
2
3
        ## Stage A
         Omega <- matrix(rnorm(n*2*k),
4
5
                   nrow=n. ncol=2*k)
        Y <- A %*% Omega
6
 7
        Q \leftarrow qr.Q(qr(Y))
8
         At \leftarrow t(A)
9
         for(i in 1:q)
10
              Y <- At %*% O
11
12
             Q \leftarrow qr.Q(qr(Y))
             Y <- A %*% Q
13
              Q \leftarrow ar.Q(ar(Y))
14
15
16
17
        ## Stage B
        B <- t(Q) %*% A
18
        U <- La.svd(B)$u
19
20
        U <- Q %*% U
21
        U[, 1:k]
22
```

RandSVD

Randomized SVD

Serial R

```
randSVD \leftarrow function(A, k, q=3)
 2
 3
         ## Stage A
 4
         Omega <- matrix(rnorm(n*2*k),
                nrow=n. ncol=2*k)
 6
         Y <- A %*% Omega
         Q \leftarrow qr.Q(qr(Y))
8
         At \leftarrow t(A)
9
         for(i in 1:q)
10
11
              Y <- At %*% Q
12
             Q \leftarrow qr.Q(qr(Y))
13
              Y <- A %*% Q
14
              Q \leftarrow qr.Q(qr(Y))
15
16
17
         ## Stage B
18
         B <- t(Q) %*% A
19
         U <- La.svd(B)$u
20
         U <- Q %*% U
21
         U[, 1:k]
22
```

Parallel pbdR

```
randSVD \leftarrow function(A, k, q=3)
 3
        ## Stage A
         Omega <- ddmatrix("rnorm",
                nrow=n. ncol=2*k)
6
         Y <- A %*% Omega
         Q \leftarrow qr.Q(qr(Y))
         At \leftarrow t(A)
         for(i in 1:q)
10
11
              Y <- At %*% Q
12
              Q \leftarrow qr.Q(qr(Y))
13
              Y <- A %*% Q
              Q \leftarrow qr.Q(qr(Y))
14
15
16
17
         ## Stage B
18
         B <- t(Q) %*% A
19
         U <- La.svd(B)$u</p>
20
         U <- Q %*% U
21
         U[, 1:k]
22
```

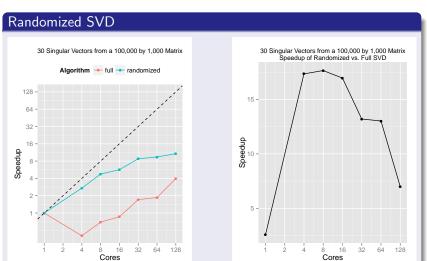


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RandSVD





RandSVD

DMAT Exercises

• Experiment with DMAT Examples 1 through 5, running them on 2 and 4 processors.



- Subsetting, selection, and filtering are basic matrix operations featured in R. The following may look silly, but it is useful for data processing. Let x.dmat <- ddmatrix(1:30, 10, 3). Do the following:
 - y.dmat <- x.dmat[c(1, 5, 4, 3),]
 y.dmat <- x.dmat[c(10:3, 5, 5),]
 y.dmat <- x.dmat[1:5, 3:1]</pre>
 - y.dmat <- x.dmat[x.dmat[, 2] > 13,]
 y.dmat <- x.dmat[x.dmat[, 2] > x.dmat[, 3],]
 y.dmat <- x.dmat[, x.dmat[2,] > x.dmat[3,]]
 y.dmat <- x.dmat[c(1, 3, 5), x.dmat[, 2] >
 x.dmat[, 3]]



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RandSVD

Advanced DMAT Exercises II

- The method crossprod() is an optimized form of the crossproduct computation t(x.dmat) %*% x.dmat. For this exercise, let x.dmat <- ddmatrix(1:30, nrow=10, ncol=3).
 - Verify that these computations really do produce the same results.
 - ② Time each operation. Which is faster?
- The prcomp() method returns rotations for all components. Computationally verify by example that these rotations are orthogonal, i.e., that their crossproduct is the identity matrix.



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The pbdR Project

- Our website: http://r-pbd.org/
- Email us at: RBigData@gmail.com
- Our google group: http://group.r-pbd.org/

Where to begin?

- The **pbdDEMO** package http://cran.r-project.org/web/packages/pbdDEMO/
- The **pbdDEMO** Vignette: http://goo.gl/HZkRt



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Thanks for coming!

Questions?



http://r-pbd.org/

Be sure to come to our R BoF: Wednesday 5:30-7:00 room 404

Tutorial evaluations: http://bit.ly/sc13-tut-mf08

