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Introducing R: From Your Laptop to HPC and Big Data

Drew Schmidt

July 22, 2013





IPMbda

Affiliations and Support

The pbdR Core Team http://r-pbd.org

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About This Presentation

Downloads

pbdMPI

This presentation and supplemental materials are available at:

Sample R scripts and pbs job scripts available on Nautilus from: /lustre/medusa/mschmid3/tutorial/scripts.tar.gz



IPMbda

Speaking Serial R with a Parallel Accent

The content of this presentation is based in part on the **pbdDEMO** vignette *Speaking Serial R with a Parallel Accent*

http://goo.gl/HZkRt

It contains more examples, and sometimes added detail.



About This Presentation

pbdMPI

Installation Instructions

Installation instructions for setting up a pbdR environment are available:

This includes instructions for installing R, MPI, and pbdR.



About This Presentation

pbdMPI

Conventions For Code Presentation

We will use two different forms of syntax highlighting. One for displaying results from an interactive R session:

```
1 R> "interactive"
2 [1] "interactive"
```

and one for presenting R scripts

```
1 "not interactive"
```



Contents

pbdMPI

- Introduction to pbdMPI
- The Generalized Block Distribution
- Basic Statistics Examples
- Introduction to pbdDMAT and the DMAT Structure
- Examples Using pbdDMAT
- Wrapup



Contents

- Introduction to pbdMPI
 - Managing a Communicator
 - Reduce, Gather, Broadcast, and Barrier
 - Other pbdMPI Tools



Message Passing Interface (MPI)

- MPI: Standard for managing communications (data and instructions) between different nodes/computers.
- Implementations: OpenMPI, MPICH2, Cray MPT, ...
- Enables parallelism (via communication) on distributed machines.
- Communicator: manages communications between processors.



Managing a Communicator

pbdMPI

MPI Operations (1 of 2)

 Managing a Communicator: Create and destroy communicators.

init() — initialize communicator
finalize() — shut down communicator(s)

 Rank query: determine the processor's position in the communicator.

```
comm.rank() — "who am I?"
comm.size() — "how many of us are there?"
```

• **Printing**: Printing output from various ranks.

```
comm.print(x)
comm.cat(x)
```

WARNING: only use these functions on *results*, never on yet-to-be-computed things.



pbdMPI

Quick Example 1

Rank Query: 1_rank.r

```
library(pbdMPI, quiet = TRUE)
  init()
3
  my.rank <- comm.rank()</pre>
  comm.print(my.rank, all.rank=TRUE)
6
  finalize()
```

Execute this script via:

mpirun -np 2 Rscript 1_rank.r

Sample Output:

```
COMM \cdot RANK = O
  [1] 0
2
  COMM.RANK = 1
  [1] 1
```



DMAT

Managing a Communicator

Quick Example 2

Hello World: 2_hello.r

```
library(pbdMPI, quiet=TRUE)
  init()
3
  comm.print("Hello, world")
4
5
  comm.print("Hello again", all.rank=TRUE, quiet=TRUE)
6
7
  finalize()
```

Execute this script via:

```
mpirun -np 2 Rscript 2_hello.r
```

Sample Output:

```
COMM.RANK = O
1
2
  [1]
      "Hello, world"
  [1]
      "Hello again"
  [1]
      "Hello again"
```



Reduce, Gather, Broadcast, and Barrier

MPI Operations

- Reduce
- Gather
- Broadcast
- Barrier



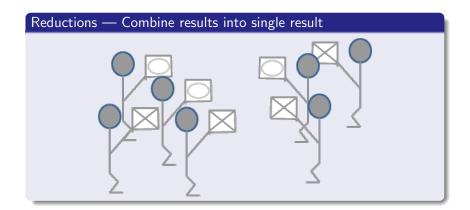
pbdDMAT eg's

Stats eg's

Reduce, Gather, Broadcast, and Barrier

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pbdDMAT eg's Wrapup

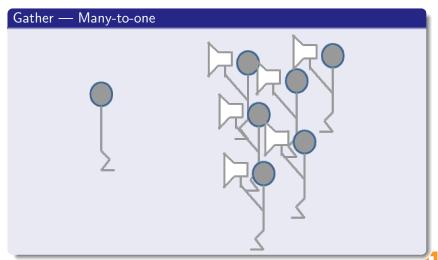
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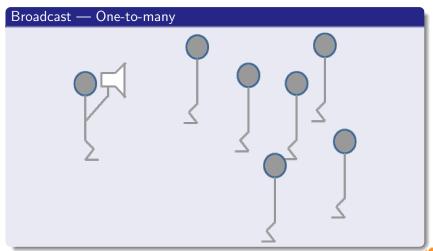
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Reduce, Gather, Broadcast, and Barrier

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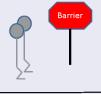
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Barrier — Synchronization Barrier

Stats eg's







Wrapup

Barrier

pbdMPI

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MPI Operations (2 of 2)

- Reduction: each processor has a number x; add all of them up, find the largest/smallest, reduce(x, op='sum') — reduce to one allreduce(x, op='sum') — reduce to all
- Gather: each processor has a number; create a new object on some processor containing all of those numbers. gather(x) — gather to one allgather(x) — gather to all
- Broadcast: one processor has a number x that every other processor should also have. bcast(x)
- Barrier: "computation wall"; no processor can proceed until all processors can proceed. barrier()



Other pbdMPI Tools

pbdMPI

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MPI Package Controls

The .SPMD.CT object allows for setting different package options with **pbdMPI**. See the entry *SPMD Control* of the **pbdMPI** manual for information about the .SPMD.CT object:

http://cran.r-project.org/web/packages/pbdMPI/pbdMPI.pdf



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Random Seeds

pbdMPI offers a simple interface for managing random seeds:

Stats eg's

- comm.set.seed(diff=TRUE) Independent streams via the rlecuyer package.
- comm.set.seed(seed=1234, diff=FALSE) All processors use the same seed seed=1234
- comm.set.seed(diff=FALSE) All processors use the same seed, determined by processor 0 (using the system clock and PID of processor 0).



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Other Helper Tools

pbdMPI Also contains useful tools for Manager/Worker and task parallelism codes:

- Task Subsetting: Distributing a list of jobs/tasks get.jid(n)
- *ply: Functions in the *ply family. pbdApply(X, MARGIN, FUN, ...) — analogue of apply() pbdLapply(X, FUN, ...) — analogue of lapply() pbdSapply(X, FUN, ...) — analogue of sapply()



Quick Comments for Using pbdMPI

Stats eg's

Start by loading the package:

```
library(pbdMPI, quiet = TRUE)
```

② Always initialize before starting and finalize when finished:

```
init()

init()

finalize()
```



Other pbdMPI Tools

Basic MPI Exercises

• Experiment with Quick Examples 1 through 6, running them on 2, 4, and 8 processors.



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pbdMPI

- 2 The Generalized Block Distribution
 - The GBD Data Structure
 - GBD: Example 1
 - GBD: Example 2



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The GBD Data Structure

pbdMPI

Distributing Data

Problem: How to distribute the data

$$x = \begin{bmatrix} x_{1,1} & x_{1,2} & x_{1,3} \\ x_{2,1} & x_{2,2} & x_{2,3} \\ x_{3,1} & x_{3,2} & x_{3,3} \\ x_{4,1} & x_{4,2} & x_{4,3} \\ x_{5,1} & x_{5,2} & x_{5,3} \\ x_{6,1} & x_{6,2} & x_{6,3} \\ x_{7,1} & x_{7,2} & x_{7,3} \\ x_{8,1} & x_{8,2} & x_{8,3} \\ x_{9,1} & x_{9,2} & x_{9,3} \\ x_{10,1} & x_{10,2} & x_{10,3} \end{bmatrix}_{10 \times}$$

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GBD Stats eg's

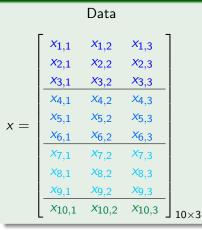
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The GBD Data Structure

pbdMPI

Distributing a Matrix Across 4 Processors: Block Distribution



Processors



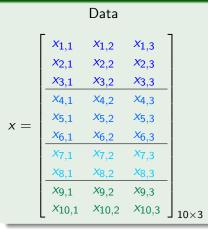
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The GBD Data Structure

Distributing a Matrix Across 4 Processors: Local Load Balance

Stats eg's



Processors



The GBD Data Structure

Throughout the examples, we will make use of the Generalized Block Distribution, or GBD distributed matrix structure.

- GBD is distributed. No processor owns all the data.
- Q GBD is non-overlapping. Rows uniquely assigned to processors.
- **3** GBD is *row-contiguous*. If a processor owns one element of a row, it owns the entire row.
- 4 GBD is globally row-major, locally column-major.
- 6 GBD is often locally balanced, where each processor owns (almost) the same amount of data. But this is not required.

x _{1,1}	<i>x</i> _{1,2}	<i>x</i> _{1,3}
x _{2,1}	$x_{2,2}$	$x_{2,3}$
<i>x</i> _{3,1}	X3,2	<i>X</i> 3,3
X4,1	X4,2	X4,3
<i>X</i> 5,1	<i>X</i> 5,2	<i>X</i> 5,3
<i>X</i> 6,1	<i>x</i> _{6,2}	<i>x</i> _{6,3}
<i>X</i> 7,1	<i>X</i> 7,2	<i>X</i> 7,3
X8,1	X8,2	<i>X</i> 8,3
X9,1	X9,2	X9,3
X _{10,1}	X _{10,2}	X _{10,3}

- 6 The last row of the local storage of a processor is adjacent (by global row) to the first row of the local storage of next processor (by communicator number) that owns data.
- GBD is (relatively) easy to understand, but can lead to bottlenecks if you have many more columns than rows.



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GBD: Example 1

pbdMPI

Understanding GBD: Global Matrix

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



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GBD: Example 1

pbdMPI

Understanding GBD: Load Balanced GBD

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processors = 0 1 2 3 4 5



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GBD: Example 1

pbdMPI

Understanding GBD: Local View

$$\begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \end{bmatrix}_{2\times9}$$

$$\begin{bmatrix} x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \end{bmatrix}_{2\times9}$$

$$\begin{bmatrix} x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \end{bmatrix}_{2\times9}$$

$$\begin{bmatrix} x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \end{bmatrix}_{1\times9}$$

$$\begin{bmatrix} x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \end{bmatrix}_{1\times9}$$

$$\begin{bmatrix} x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{1\times9}$$

Processors = 0 1 2 3 4 5



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GBD: Example 2

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Understanding GBD: Non-Balanced GBD

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```
X_{11}
         X<sub>12</sub>
                  X<sub>13</sub>
                           X14
                                     X<sub>15</sub>
                                              X16
                                                       X17
                                                                X<sub>18</sub>
                                                                         X19
X21
         X22
                  X23
                           X24
                                     X25
                                              X26
                                                       X27
                                                                X28
                                                                         X29
X31
         X32
                  X33
                           X34
                                     X35
                                              X36
                                                       X37
                                                                X38
                                                                         X39
X41
         X42
                  X43
                           X44
                                     X45
                                              X46
                                                       X47
                                                                X48
                                                                         X49
                           X54
                                                                X58
                                                                         X59
X_{51}
         X_{52}
                  X53
                                     X55
                                              X56
                                                       X57
X<sub>61</sub>
         X_{62}
                  X63
                           X<sub>64</sub>
                                     X<sub>65</sub>
                                              X<sub>66</sub>
                                                       X<sub>67</sub>
                                                                X<sub>68</sub>
                                                                         X69
X71
         X72
                           X74
                                              X76
                                                       X77
                                                                X78
                                                                         X79
                  X73
                                     X75
X<sub>81</sub>
         X82
                  X83
                           X84
                                     X85
                                              X86
                                                       X87
                                                                X88
                                                                         Xgg
X91
         X92
                  X93
                           X94
                                     X95
                                              X96
                                                       X97
                                                                X98
                                                                         Xgg
```

Processors = 0 1 2 3 4 5



GBD: Example 2

pbdMPI

Understanding GBD: Local View $\int_{0\times9}$ *X*₁₆ X₁₇ X_{11} X_{12} X_{13} X_{14} X_{15} *X*₁₈ X_{19} X22 X21 X23 X24 X25 X26 X27 X28 X29 X31 X32 X33 X34 X35 X36 X37 X38 X39 X45 X46 X₄₁ X42 X43 X44 X47 X48 X49 X51 *X*52 X53 X55 *X*56 X57 *X*58 *X*59 X₆₁ X₆₂ X₆₃ X₆₄ X₆₅ X₆₆ X67 X₆₈ X69 *X*71 X72 X73 X76 X78 X79 X74 X75 X77 $\int_{0\times9}$ X₈₁ X82 X83 X84 X85 X86 X87 X88 X92 X99 X91 X93 X94 X95 X96 X97 *X*98



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GBD: Example 2

Quick Comment for GBD

Local pieces of GBD distributed objects will be given the suffix .gbd to visually help distinguish them from global objects. This suffix carries no semantic meaning.



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- Basic Statistics Examples
 - pbdMPI Example: Monte Carlo Simulation
 - pbdMPI Example: Sample Covariance
 - pbdMPI Example: Linear Regression



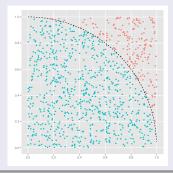
pbdMPI Example: Monte Carlo Simulation

pbdMPI

Example 1: Monte Carlo Simulation

Sample N uniform observations (x_i, y_i) in the unit square $[0,1] \times [0,1]$. Then

$$\pi pprox 4\left(rac{\#\ \textit{Inside Circle}}{\#\ \textit{Total}}
ight) = 4\left(rac{\#\ \textit{Blue}}{\#\ \textit{Blue} + \#\ \textit{Red}}
ight)$$





Example 1: Monte Carlo Simulation GBD Algorithm

- Let *n* be big-ish; we'll take n = 50,000.
- Generate an $n \times 2$ matrix x of standard uniform observations.
- **3** Count the number of rows satisfying $x^2 + y^2 < 1$
- Ask everyone else what their answer is; sum it all up.
- 5 Take this new answer, multiply by 4 and divide by n
- If my rank is 0, print the result.



pbdMPI Example: Monte Carlo Simulation

Example 1: Monte Carlo Simulation Code

Serial Code

```
N <- 50000
X <- matrix(runif(N * 2), ncol=2)</pre>
r \leftarrow sum(rowSums(X^2) \leftarrow 1)
PI <- 4*r/N
print(PI)
```

Parallel Code

```
library(pbdMPI, quiet = TRUE)
  init()
  comm.set.seed(diff=TRUE)
  N.gbd <- 50000 / comm.size()
  X.gbd <- matrix(runif(N.gbd * 2), ncol = 2)</pre>
  r.gbd <- sum(rowSums(X.gbd^2) <= 1)
  r <- allreduce(r.gbd)
  PI <- 4*r/(N.gbd * comm.size())
  comm.print(PI)
11
  finalize()
```



pbdMPI Example: Monte Carlo Simulation

Note

For the remainder, we will exclude loading, init, and finalize calls.



pbdMPI Example: Sample Covariance

Example 2: Sample Covariance

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$



Example 2: Sample Covariance GBD Algorithm

- lacktriangle Determine the total number of rows N.
- 2 Compute the vector of column means of the full matrix.
- 3 Subtract each column's mean from that column's entries in each local matrix.
- 4 Compute the crossproduct locally and reduce.
- **5** Divide by N-1.



pbdMPI Example: Sample Covariance

pbdMPI

Example 2: Sample Covariance Code

Serial Code

```
N \leftarrow nrow(X)
  mu <- colSums(X) / N
3
  X <- sweep (X, STATS=mu, MARGIN=2)
  Cov.X \leftarrow crossprod(X) / (N-1)
6
  print(Cov.X)
```

Parallel Code

```
N <- allreduce(nrow(X.gbd), op="sum")</pre>
 mu <- allreduce(colSums(X.gbd) / N, op="sum")</pre>
3
  X.gbd <- sweep(X.gbd, STATS=mu, MARGIN=2)</pre>
  Cov.X <- allreduce(crossprod(X.gbd), op="sum") / (N-1)
  comm.print(Cov.X)
```



Example 3: Linear Regression

Find β such that

$$\mathsf{y} = \mathsf{X} oldsymbol{eta} + oldsymbol{\epsilon}$$

When X is full rank,

$$\hat{oldsymbol{eta}} = (\mathbf{X}^{\mathsf{T}}\mathbf{X})^{-1}\mathbf{X}^{\mathsf{T}}\mathbf{y}$$



Example 3: Linear Regression GBD Algorithm

- Locally, compute $tx = x^T$
- 2 Locally, compute A = tx * x. Query every other processor for this result and sum up all the results.
- **3** Locally, compute B = tx * y. Query every other processor for this result and sum up all the results.
- **1** Locally, compute $A^{-1} * B$



Example 3: Linear Regression Code

Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4 ols <- solve(A) %*% B
```

Parallel Code

```
tX.gbd <- t(X.gbd)
tX.gbd <- t(X.gbd)
tX.gbd %*% X.gbd, op = "sum")
B <- allreduce(tX.gbd %*% y.gbd, op = "sum")
type ols <- solve(A) %*% B</pre>
```



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pbdMPI Example: Linear Regression

MPI Exercises

• Experiment with Statistics Examples 1 through 3, running them on 2, 4, and 8 processors.



Stats eg's

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pbdMPI

Advanced MPI Exercises I

- Write a script that will have each processor randomly take a sample of size 1 of TRUE and FALSE. Have each processor print its result.
- Modify the script in Exercise 1 above to determine if any processors sampled TRUE. Do the same to determine if all processors sampled TRUE. In each case, print the result. Compare to the functions comm.all() and comm.any().
- Generate 50,000,000 (total) random normal values in parallel on 2, 4, and 8 processors. Time each run.



pbdMPI Example: Linear Regression

pbdMPI

Advanced MPI Exercises II

- O Distribute the matrix x <- matrix(1:24, nrow=12) in</p> GBD format across 4 processors and call it x.spmd.
 - Add x.spmd to itself.
 - Compute the mean of x.spmd.
 - Compute the column means of x.spmd.



Contents

- Introduction to pbdDMAT and the DMAT Structure
 - Introduction to Distributed Matrices
 - DMAT Distributions
 - pbdDMAT



Wrapup

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Introduction to Distributed Matrices

Distributed Matrices

Most problems in data science are matrix algebra problems, so:

Distributed matrices ⇒ Handle Bigger data



Introduction to Distributed Matrices

Distributed Matrices

High level OOP allows native serial R syntax:

Stats eg's

```
x \leftarrow x[-1, 2:5]
x \leftarrow log(abs(x) + 1)
xtx < -t(x) %*% x
ans <- svd(solve(xtx))
```

However...



Distributed Matrices

DMAT:

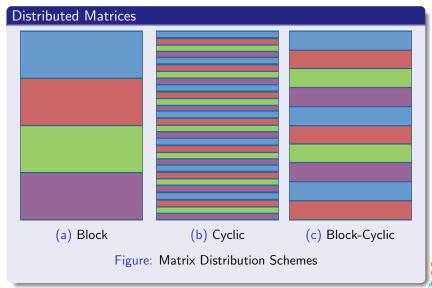
- Distributed MATrix data structure.
- No single processor should hold all of the data.
- Block-cyclic matrix distributed across a 2-dimensional grid of processors.
- Very robust, but confusing data structure.



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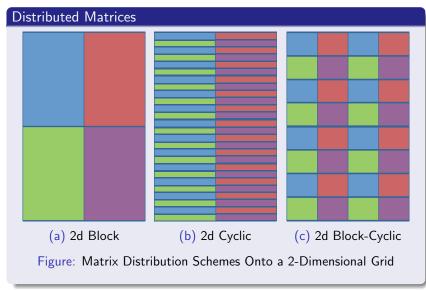
Introduction to Distributed Matrices



DMAT pbdDMAT eg's Wrapup 00000000

Introduction to Distributed Matrices

pbdMPI



Stats eg's

Processor Grid Shapes

$$\begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}^{T} \qquad \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \quad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \quad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$
(a) 1×6 (b) 2×3 (c) 3×2 (d) 6×1

Table: Processor Grid Shapes with 6 Processors



Introduction to Distributed Matrices

pbdMPI

Distributed Matrices

The data structure is a special R class (in the OOP sense) called ddmatrix. It is the "under the rug" storage for a block-cyclic matrix distributed onto a 2-dimensional processor grid.

```
S4 local submatrix, an R matrix
                      S4 dimension of the global matrix, a numeric pair
ddmatrix = { | Idim | S4 dimension of the local submatrix, a numeric pair
              bldim S4 ScaLAPACK blocking factor, a numeric pair
                      S4 BLACS context, an numeric singleton
```

with prototype

```
Data
                                                                                              = matrix(0.0)
                                                                                             = c(1,1)
\label{eq:new} \begin{split} \text{new("ddmatrix")} &= \begin{cases} \text{dim} &= \text{c(1,1)} \\ \text{ldim} &= \text{c(1,1)} \\ \text{bldim} &= \text{c(1,1)} \end{cases} \end{split}
```



Stats eg's

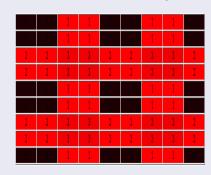
0000000

Introduction to Distributed Matrices

IPMbda

Distributed Matrices: The Data Structure

Example: an 9×9 matrix is distributed with a "block-cycling" factor of 2×2 on a 2×2 processor grid:



$$= \begin{cases} \textbf{Data} &= \texttt{matrix}(\ldots) \\ \textbf{dim} &= \texttt{c}(9, 9) \\ \textbf{Idim} &= \texttt{c}(\ldots) \\ \textbf{bIdim} &= \texttt{c}(2, 2) \\ \textbf{CTXT} &= 0 \end{cases}$$

See http://acts.nersc.gov/scalapack/hands-on/datadist.html



GBD Stats eg's

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 pbdDMAT eg's

DMAT Distributions

pbdMPI

Understanding Dmat: Global Matrix

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$



GBD Stats eg's DMAT pbdDMAT eg's Wrapup

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DMAT Distributions

pbdMPI

DMAT: 1-dimensional Row Block

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ \hline x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ \hline x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ \hline x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (0,1) \\ (1,0) \\ (1,1) \end{vmatrix}$$



GBD Stats eg's DMAT pbdDMAT eg's Wrapup

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DMAT Distributions

pbdMPI

DMAT: 2-dimensional Row Block

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ \hline X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



DMAT Distributions

DMAT: 1-dimensional Row Cyclic

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (0,1) \\ (1,0) \\ (1,1) \end{vmatrix}$$



DMAT Distributions

pbdMPI

DMAT: 2-dimensional Row Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



Wrapup

DMAT Distributions

pbdMPI

DMAT: 2-dimensional Block-Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ \hline x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



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pbdDMAT

The DMAT Data Structure

The more complicated the processor grid, the more complicated the distribution.



pbdDMAT

pbdMPI

DMAT: 2-dimensional Block-Cyclic with 6 Processors

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



pbdDMAT

pbdMPI

Understanding DMAT: Local View

X37

X47

X77

X87

X32

X42

X72

X82

*X*38

X48

X78

X88

X34

 X_{44}

X74

X84

$$\begin{bmatrix} x_{69} \\ x_{99} \end{bmatrix}_{1}$$

X49

X79

X89

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$

X33

X43

X73

X83



X31

X41

X71

X81



pbdDMAT

IPMbda

The DMAT Data Structure

- ① DMAT is distributed. No one processor owns all of the matrix.
- ② DMAT is non-overlapping. Any piece owned by one processor is owned by no other processors.
- ① DMAT can be row-contiguous or not, depending on the processor grid and blocking factor used.
- OMAT is locally column-major and globally, it depends...
- GBD is a generalization of the one-dimensional block DMAT distribution. Otherwise there is no relation.
- O DMAT is confusing, but very robust.

<i>x</i> ₁₁	<i>x</i> ₁₂	X ₁₃	X ₁₄	X ₁₅
<i>x</i> ₂₁	X22	X23	X24	X25
X31	X32	X33	X34	X35
X41	X42	X43	X44	X45
X51	<i>X</i> 52	<i>X</i> 53	X54	<i>X</i> 55
<i>X</i> 61	<i>X</i> 62	X63	X ₆₄	<i>X</i> 65
X71	X72	X73	X74	<i>X</i> 75
X81	X82	X83	X84	X85
X91	X92	<i>X</i> 93	X94	X95



Pros and Cons of This Data Structure

Pros

 Fast for distributed matrix computations

Cons

Literally everything else

This is why we hide most of the distributed details.

The details are there if you want them (you don't want them).



Distributed Matrix Methods

pbdDMAT has over 100 methods with *identical* syntax to R:

- `[`, rbind(), cbind(), ...
- lm.fit(), prcomp(), cov(), ...
- `%*%`, solve(), svd(), norm(), ...
- median(), mean(), rowSums(), ...

Serial Code

1 cov(x)

Parallel Code

1 cov(x)



Comparing pbdMPI and pbdDMAT

pbdMPI:

- MPI + sugar.
- GBD not the only structure pbdMPI can handle (just a useful convention).

pbdDMAT:

- More of a software package.
- DMAT structure must be used for pbdDMAT.
- If the data is not 2d block-cyclic compatible, DMAT will definitely give the wrong answer.



Quick Comments for Using pbdDMAT

Start by loading the package:

```
1 library(pbdDMAT, quiet = TRUE)
```

② Always initialize before starting and finalize when finished:

```
1 init.grid()
2
3 # ...
4
5 finalize()
```

Oistributed DMAT objects will be given the suffix .dmat to visually help distinguish them from global objects. This suffix carries no semantic meaning.



Contents

- 5 Examples Using pbdDMAT
 - Statistics Examples with pbdDMAT
 - RandSVD



```
Sample Covariance
                           Serial Code
 Cov.X <- cov(X)
 print(Cov.X)
                           Parallel Code
 Cov.X <- cov(X)
 print(Cov.X)
```



Linear Regression

Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
5 ols <- solve(A) %*% B
6
7 # or
8 ols <- lm.fit(X, y)</pre>
```

Parallel Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4
5 ols <- solve(A) %*% B
6
7 # or
8 ols <- lm.fit(X, y)</pre>
```



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Statistics Examples with pbdDMAT

Example 5: PCA

PCA: pca.r

```
library(pbdDMAT, quiet=T)
    init.grid()
2
3
4
5
6
7
   n <- 1e4
   p <- 250
   comm. set . seed ( diff=T)
8
   x.dmat <- ddmatrix("rnorm", nrow=n, ncol=p, mean=100, sd=25)
10
    pca <- prcomp(x=x.dmat. retx=TRUE, scale=TRUE)</pre>
11
    prop_var <- cumsum(pca$sdev)/sum(pca$sdev)</pre>
12
    i \leftarrow max(min(which(prop_var > 0.9)) - 1, 1)
13
14
   y.dmat \leftarrow pcax[, 1:i]
15
   comm.cat("\nCols: ", i, "\n", quiet=T)
16
   comm. cat("\%Cols:", i/dim(x.dmat)[2], "\n\n", quiet=T)
17
18
19
    finalize()
```

Execute this script via:

Sample Output:

```
1 mpirun —np 2 Rscript 5-pca.r
```

1 Cols: 221 2 %Cols: 0.884



pbdMPI GBD Stats eg's DMAT pbdDMAT eg's Wrapup

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Statistics Examples with pbdDMAT

Distributed Matrices

pbdDEMO contains many other examples of reading and managing GBD and DMAT data



RandSVD

Randomized SVD3

Prototype for Randomized SVD

Given an $m \times n$ matrix A, a target number k of singular vectors, and an exponent q (say, q = 1 or q = 2), this procedure computes an approximate rank-2k factorization $U\Sigma V^*$, where U and V are orthonormal, and Σ is nonnegative and diagonal.

Stage A:

- Generate an $n \times 2k$ Gaussian test matrix Ω .
- 2 Form Y = (AA*)^qAΩ by multiplying alternately with A and A*. 3 Construct a matrix Q whose columns form an orthonormal basis for

the range of Y. Stage B:

- 4 Form $B = Q^*A$.
- Compute an SVD of the small matrix: $B = \tilde{U}\Sigma V^*$.

6 Set $U = Q\widetilde{U}$.

 $Q = Q_a$.

Note: The computation of Y in step 2 is vulnerable to round-off errors. When high accuracy is required, we must incorporate an orthonormalization step between each application of A and A^* ; see Algorithm 4.4.

Algorithm 4.4: Randomized Subspace Iteration Given an $m \times n$ matrix A and integers ℓ and q, this algorithm computes an $m \times \ell$ orthonormal matrix Q whose range approximates the range of A. Draw an $n \times \ell$ standard Gaussian matrix Ω . Form $Y_0 = A\Omega$ and compute its OR factorization $Y_0 = Q_0R_0$. for j = 1, 2, ..., qForm $\tilde{Y}_i = A^*Q_{i-1}$ and compute its QR factorization $\tilde{Y}_i = \tilde{Q}_i\tilde{R}_i$. Form $Y_i = A\widetilde{Q}_i$ and compute its QR factorization $Y_i = Q_iR_i$. 6 end

Serial R

```
randSVD \leftarrow function(A, k, g=3)
2
3
        ## Stage A
        Omega <- matrix(rnorm(n*2*k),
4
5
                   nrow=n. ncol=2*k)
        Y <- A %*% Omega
6
        Q \leftarrow qr.Q(qr(Y))
8
         At \leftarrow t(A)
9
         for(i in 1:q)
10
              Y <- At %*% O
11
12
             Q \leftarrow qr.Q(qr(Y))
             Y <- A %*% Q
13
             Q \leftarrow ar.Q(ar(Y))
14
15
16
17
        ## Stage B
        B <- t(Q) %*% A
18
        U <- La.svd(B)$u
19
20
        U <- Q %*% U
21
        U[, 1:k]
22
```

¹Halko N, Martinsson P-G and Tropp J A 2011 Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions SIAM Rev. 53 217-88

RandSVD

Randomized SVD

Serial R

```
randSVD \leftarrow function(A, k, q=3)
 2
 3
         ## Stage A
 4
         Omega <- matrix(rnorm(n*2*k),
                nrow=n. ncol=2*k)
6
         Y <- A %*% Omega
         Q \leftarrow qr.Q(qr(Y))
8
         At \leftarrow t(A)
9
         for(i in 1:q)
10
11
              Y <- At %*% Q
12
             Q \leftarrow qr.Q(qr(Y))
13
              Y <- A %*% Q
14
             Q \leftarrow qr.Q(qr(Y))
15
16
17
         ## Stage B
18
         B <- t(Q) %*% A
19
         U <- La.svd(B)$u
20
         U <- Q %*% U
21
         U[, 1:k]
22
```

Parallel pbdR

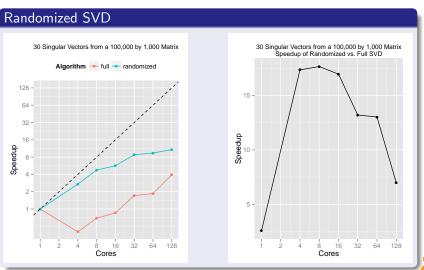
```
randSVD \leftarrow function(A, k, q=3)
 3
        ## Stage A
         Omega <- ddmatrix("rnorm",
               nrow=n. ncol=2*k)
6
         Y <- A %*% Omega
        Q \leftarrow qr.Q(qr(Y))
         At \leftarrow t(A)
         for(i in 1:q)
10
11
             Y <- At %*% Q
12
             Q \leftarrow qr.Q(qr(Y))
13
             Y <- A %*% Q
14
             Q \leftarrow qr.Q(qr(Y))
15
16
17
         ## Stage B
18
         B <- t(Q) %*% A
19
         U <- La.svd(B)$u
20
         U <- Q %*% U
21
         U[, 1:k]
22
```



pbdMPI Stats eg's DMAT pbdDMAT eg's 0000

Wrapup





RandSVD

DMAT Exercises

• Experiment with DMAT Examples 1 through 5, running them on 2 and 4 processors.



pbdMPI

Advanced DMAT Exercises I

- Subsetting, selection, and filtering are basic matrix operations featured in R. The following may look silly, but it is useful for data processing. Let x.dmat <- ddmatrix(1:30, 10, 3). Do the following:
 - y.dmat <- x.dmat[c(1, 5, 4, 3),]
 y.dmat <- x.dmat[c(10:3, 5, 5),]
 y.dmat <- x.dmat[1:5, 3:1]</pre>
 - y.dmat <- x.dmat[x.dmat[, 2] > 13,]
 y.dmat <- x.dmat[x.dmat[, 2] > x.dmat[, 3],]
 y.dmat <- x.dmat[, x.dmat[2,] > x.dmat[3,]]
 y.dmat <- x.dmat[c(1, 3, 5), x.dmat[, 2] >
 x.dmat[, 3]]



RandSVD

pbdMPI

Advanced DMAT Exercises II

- The method crossprod() is an optimized form of the crossproduct computation t(x.dmat) %*% x.dmat. For this exercise, let x.dmat <- ddmatrix(1:30, nrow=10, ncol=3).
 - Verify that these computations really do produce the same results.
 - ② Time each operation. Which is faster?
- The prcomp() method returns rotations for all components. Computationally verify by example that these rotations are orthogonal, i.e., that their crossproduct is the identity matrix.



 pbdMPI
 GBD
 Stats eg's
 DMAT
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 Wrapup

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Contents





Where to Learn More

- Our website http://r-pbd.org/
- The pbdDEMO package
 http://cran.r-project.org/web/packages/pbdDEMO/
- The pbdDEMO Vignette: http://goo.gl/HZkRt
- Our Google Group: http://group.r-pbd.org



IPMbda

Tutorials

pbdMPI

- OLCF Data Workshop, August 8, Oak Ridge National Laboratory
- SC13, November 17-22, Denver, Colorado

Invited Talks

- JSM 2013, August 3-8, Montréal, Québec
- IASC, Aug 22-23, Seoul
- World Statistics Congress, August 25-30, Hong Kong



Thanks for coming!

Questions? Comments?

