# Programming with Big Data in R

### Drew Schmidt and George Ostrouchov

#### useR! 2014





# The **pbd**R Core Team

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### About This Presentation

### Downloads

This presentation is available at: http://r-pbd.org/tutorial



### About This Presentation

#### Installation Instructions

Installation instructions for setting up a  $\mbox{\bf pbd}\mbox{\bf R}$  environment are available:

This includes instructions for installing R, MPI, and **pbdR**.



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- Wrapup



### Contents

- Introduction
  - A Concise Introduction to Parallelism
  - A Quick Overview of Parallel Hardware
  - A Quick Overview of Parallel Software
  - Summary



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Programming with Big Data in R

# **Parallelism** Serial Programming Parallel Programming CPU



http://r-pbd.org/tutorial

### Difficulty in Parallelism

- 1 Implicit parallelism: Parallel details hidden from user
- Explicit parallelism: Some assembly required...
- Embarrassingly Parallel: Also called loosely coupled. Obvious how to make parallel; lots of independence in computations.
- Tightly Coupled: Opposite of embarrassingly parallel; lots of dependence in computations.



# Speedup

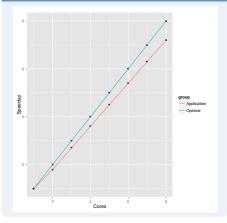
- Wallclock Time: Time of the clock on the wall from start to finish
- Speedup: unitless measure of improvement; more is better.

$$S_{n_1,n_2} = \frac{\text{Run time for } n_1 \text{ cores}}{\text{Run time for } n_2 \text{ cores}}$$

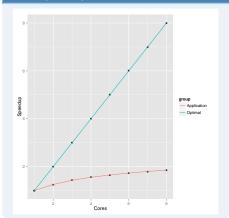
- $n_1$  is often taken to be 1
- In this case, comparing parallel algorithm to serial algorithm



# Good Speedup



### Bad Speedup



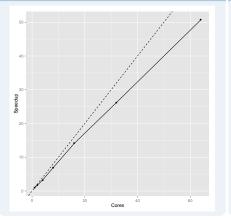


# Scalability and Benchmarking

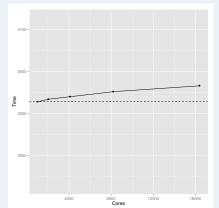
- Strong: Fixed total problem size.
   Less work per core as more cores are added.
- Weak: Fixed local (per core) problem size. Same work per core as more cores are added.



# Good Strong Scaling



# Good Weak Scaling

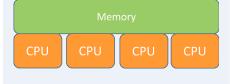




# Shared and Distributed Memory Machines

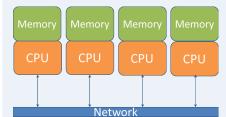
### Shared Memory

Direct access to read/change memory (one node)



#### Distributed

No direct access to read/change memory (many nodes); requires communication





# Shared and Distributed Memory Machines

### **Shared Memory Machines**

#### Thousands of cores



Nautilus, University of Tennessee 1024 cores 4 TB RAM

### Distributed Memory Machines

#### Hundreds of thousands of cores



Kraken, University of Tennessee 112,896 cores 147 TB RAM

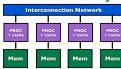


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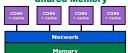


# Three Basic Flavors of Hardware

#### **Distributed Memory**



#### **Shared Memory**



#### Co-Processor

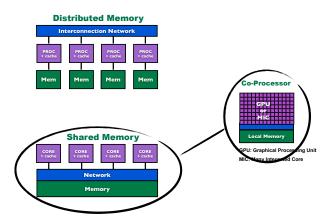


GPU: Graphical Processing Unit

MIC: Many Integrated Core

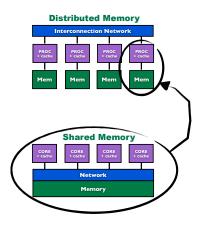


# Your Laptop or Desktop





# A Server or Cluster



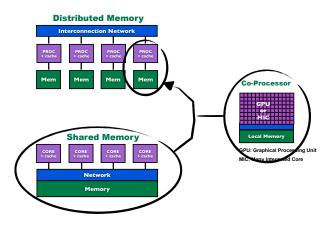




GPU: Graphical Processing Unit MIC: Many Integrated Core

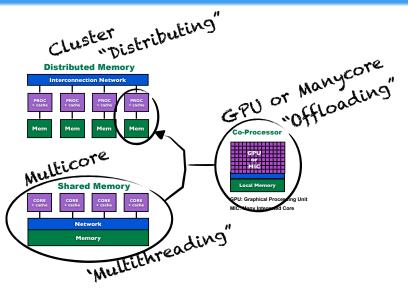


# Server to Supercomputer





# Knowing the Right Words

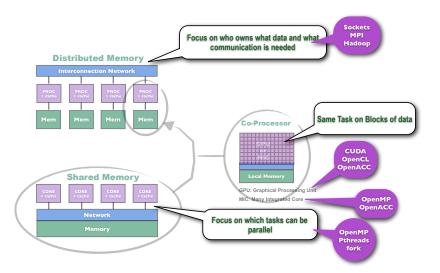




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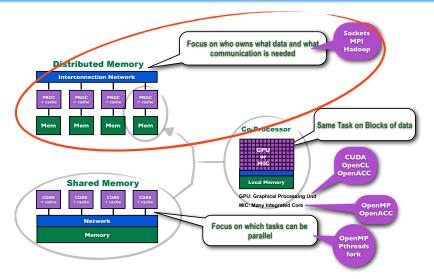


# "Native" Programming Models and Tools



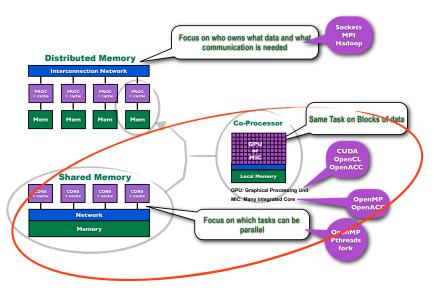


# 30+ Years of Parallel Computing Research





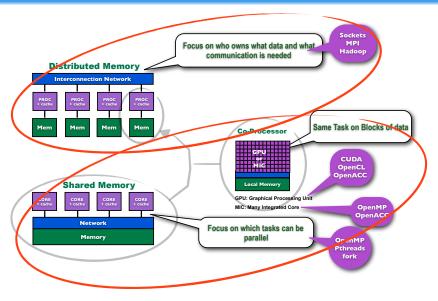
# Last 10 years of Advances





Programming with Big Data in R

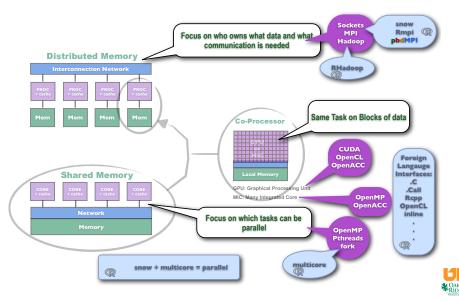
# Putting It All Together Challenge





http://r-pbd.org/tutorial

### R Interfaces to Native Tools



- Introduction
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#### Summary

- Three flavors of hardware
  - Distributed is stable
  - Multicore and co-processor are evolving
  - Two memory models
  - Distributed works in multicore
- Parallelism hierarchy
- Medium to big machines have all three



# Contents

- Profiling and Benchmarking
  - Why Profile?
  - Profiling R Code
  - Advanced R Profiling
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### Performance and Accuracy



Sometimes  $\pi=3.14$  is (a) infinitely faster than the "correct" answer and (b) the difference between the "correct" and the "wrong" answer is meaningless. ... The thing is, some specious value of "correctness" is often irrelevant because it doesn't matter. While performance almost always matters. And I absolutely detest the fact that people so often dismiss performance concerns so readily.

— Linus Torvalds, August 8, 2008



#### Why Profile?

- Because performance matters.
- Bad practices scale up!
- Your bottlenecks may surprise you.
- Because R is dumb.
- R users claim to be data people...so act like it!



# Compilers often correct bad behavior...

#### A Really Dumb Loop

```
int main(){
    int x, i;
    for (i=0: i<10: i++)
        x = 1:
    return 0:
```

#### clang -O3 example.c

```
main:
         .cfi_startproc
 BB#0:
        xorl
                %eax.
             %eax
        ret.
```

#### clang example.c

```
main:
        .cfi_startproc
# BB#0:
        movl
                $0, -4(\% rsp)
                $0, -12(%rsp)
        movl
.LBB0_1:
                $10, -12(%rsp)
        cmpl
                .LBBO 4
        jge
# BB#2:
                $1, -8(%rsp)
        movl
# BB#3:
                -12(%rsp), %eax
        movl
        addl
                $1, %eax
                %eax, -12(%rsp)
        movl
        jmp
                .LBBO 1
.LBB0_4:
        movl
                $0. %eax
        ret
```



### R will not!

#### Dumb Loop

```
for (i in 1:n){
   tA <- t(A)
   Y <- tA %*% Q
   Q <- qr.Q(qr(Y))
   Y <- A %*% Q
   Q <- qr.Q(qr(Y))
}
</pre>
```

#### Better Loop

```
tA <- t(A)

for (i in 1:n){
    Y <- tA %*% Q
    Q <- qr.Q(qr(Y))
    Y <- A %*% Q
    Q <- qr.Q(qr(Y))
    Y <- Q <- qr.Q(qr(Y))
    Y <- Q <- qr.Q(qr(Y))
    Y <- Q <- qr.Q(qr(Y))
```



# Example from a Real R Package

#### Exerpt from Original function

```
while (i <= N) {
   for (j in 1:i) {
      d.k <- as.matrix(x) [1==j,1==j]
      ...</pre>
```

#### Exerpt from Modified function

```
1  x.mat <- as.matrix(x)
2
3  while(i<=N){
4   for(j in 1:i){
5     d.k <- x.mat[l==j,l==j]
6     ...</pre>
```

By changing just 1 line of code, performance of the main method improved by **over 350%!** 



# Some Thoughts

- R is slow.
- Bad programmers are slower.
- R isn't very clever (compared to a compiler).
- The Bytecode compiler helps, but not nearly as much as a compiler.



- Profiling and Benchmarking
  - Why Profile?
  - Profiling R Code
  - Advanced R Profiling
  - Summary



## Timings

Getting simple timings as a basic measure of performance is easy, and valuable.

- system.time() timing blocks of code.
- Rprof() timing execution of R functions.
- Rprofmem() reporting memory allocation in R .
- tracemem() detect when a copy of an R object is created.
- The **rbenchmark** package Benchmark comparisons.



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# Other Profiling Tools

- perf (Linux)
- PAPI
- MPI profiling: fpmpi, mpiP, TAU



# Profiling MPI Codes with pbdPROF

### 1. Rebuild **pbdR** packages

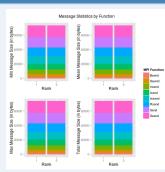
```
R CMD INSTALL pbdMPI_0.2-1.tar.gz \
--configure-args= \
"--enable-pbdPROF"
```

#### 2. Run code

```
mpirun -np 64 Rscript my_script.R
```

### 3. Analyze results

```
library(pbdPROF)
prof <- read.prof( "output.mpiP")
plot(prof, plot.type="messages2")</pre>
```







## Profiling with **pbdPAPI**

- Performance Application Programming Interface
- High and low level interfaces
- Linux only :(



Function	Description of Measurement		
system.flips()	Time, floating point instructions, and Mflips		
<pre>system.flops()</pre>	Time, floating point operations, and Mflops		
<pre>system.cache()</pre>	Cache misses, hits, accesses, and reads		
<pre>system.epc()</pre>	Events per cycle		
<pre>system.idle()</pre>	Idle cycles		
<pre>system.cpuormem()</pre>	CPU or RAM bound*		
<pre>system.utilization()</pre>	CPU utilization*		



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### Summary

- Profile, profile, profile.
- Use system.time() to get a general sense of a method.
- Use rbenchmark's benchmark() to compare 2 methods.
- Use Rprof() for more detailed profiling.
- Other tools exist for more hardcore applications (pbdPAPI and pbdPROF).



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- The pbdR Project
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## Programming with Big Data in R (pbdR)

## Striving for *Productivity, Portability, Performance*

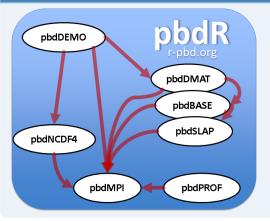


- Free<sup>a</sup> R packages.
- Bridging high-performance compiled code with high-productivity of R
- Scalable, big data analytics.
- Offers implicit and explicit parallelism.
- Methods have syntax identical to R.

<sup>a</sup>MPL. BSD. and GPL licensed



# pbdR Packages



pbdR					
R	ScaLAPACK		APACK	NetCDF4	퍼
LAPA	СК	PBLAS		LIDEE	팊
BLAS		BLACS	HDF5		
		MPI			



Why HPC libraries (MPI, ScaLAPACK, PETSc, ...)?

- The HPC community has been at this for decades.
- They're tested. They work. They're fast.
- You're not going to beat Jack Dongarra at dense linear algebra.



# Simple Interface for MPI Operations with **pbdMPI**

### Rmpi

```
# int
mpi.allreduce(x, type=1)
# double
mpi.allreduce(x, type=2)
```

### pbdMPI

```
allreduce(x)
```

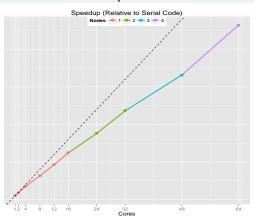
### Types in R

```
> is.integer(1)
[1] FALSE
> is.integer(2)
[1] FALSE
> is.integer(1:2)
[1] TRUE
```



# Distributed Matrices and Statistics with pbdDMAT

### Matrix Exponentiation

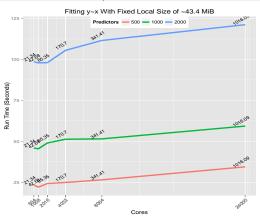


```
1 library(pbdDMAT)
2 dx <- ddmatrix("rnorm", 5000, 5000)
4 expm(dx)</pre>
```



# Distributed Matrices and Statistics with **pbdDMAT**

## Least Squares Benchmark



```
x <- ddmatrix("rnorm", nrow=m, ncol=n)
y <- ddmatrix("rnorm", nrow=m, ncol=1)
mdl <- lm.fit(x=x, y=y)</pre>
```



# Getting Started with HPC for R Users: pbdDEMO



Programming with Big Data in R

Speaking Serial R with a Parallel Accent

Package Examples and Demonstrations

pbdR Core Team

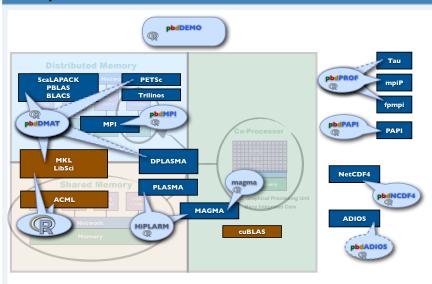
- 140 page, textbook-style vignette.
- Over 30 demos, utilizing all\* packages.
- Not just a hello world!
- Demos include:
  - PCA
  - Regression
  - Parallel data input
  - Model-based clustering
  - Simple Monte Carlo simulation
  - Bayesian MCMC



- The pbdR Project
  - The pbdR Project
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## R and pbdR Interfaces to HPC Libraries





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### pbdR Paradigms

pbdR programs are R programs!

#### Differences:

- Batch execution (non-interactive).
- Parallel code utilizes Single Program/Multiple Data (SPMD) style
- Emphasizes data parallelism.



#### **Batch Execution**

• Running a serial R program in batch:

```
1 Rscript my_script.r
```

or

```
1 R CMD BATCH my_script.r
```

• Running a parallel (with MPI) R program in batch:

```
mpirun -np 2 Rscript my_par_script.r
```



# Single Program/Multiple Data (SPMD)

- SPMD is a programming paradigm.
- Not to be confused with SIMD.

### **Paradigms**

**Programming models** 

OOP, Functional, SPMD, ...

### **SIMD**

Hardware instructions

MMX, SSE, ...



# Single Program/Multiple Data (SPMD)

SPMD is arguably the simplest extension of serial programming.

- Only one program is written, executed in batch on all processors.
- Different processors are autonomous; there is no manager.
- Dominant programming model for large machines for 30 years.



### Summary

- pbdR connects R to scalable HPC libraries.
- The **pbdDEMO** package offers numerous examples and explanations for getting started with distributed R programming.
- pbdR programs are R programs.



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- Introduction to pbdMPI
  - Managing a Communicator
  - Reduce, Gather, Broadcast, and Barrier
  - Other pbdMPI Tools
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## Message Passing Interface (MPI)

- MPI: Standard for managing communications (data and instructions) between different nodes/computers.
- Implementations: OpenMPI, MPICH2, Cray MPT, ...
- Enables parallelism (via communication) on distributed machines.
- Communicator: manages communications between processors.



http://r-pbd.org/tutorial

# MPI Operations (1 of 2)

- Managing a Communicator: Create and destroy communicators.
   init() initialize communicator
  - finalize() shut down communicator(s)
- Rank query: determine the processor's position in the communicator.
   comm.rank() "who am I?"
   comm.size() "how many of us are there?"
- **Printing**: Printing output from various ranks.

```
comm.print(x)
comm.cat(x)
```

**WARNING**: only use these functions on *results*, never on yet-to-be-computed things.



# Quick Example 1

### Rank Query: 1\_rank.r

```
library(pbdMPI, quietly = TRUE)
init()

my.rank <- comm.rank()
comm.print(my.rank, all.rank=TRUE)

finalize()</pre>
```

## Execute this script via:

```
mpirun -np 2 Rscript 1_rank.r
```

### Sample Output:

```
COMM.RANK = 0
[1] 0
COMM.RANK = 1
[1] 1
```



## Quick Example 2

#### Hello World: 2\_hello.r

```
library(pbdMPI, quietly=TRUE)
init()

comm.print("Hello, world")

comm.print("Hello again", all.rank=TRUE, quietly=TRUE)

finalize()
```

#### Execute this script via:

### Sample Output:

```
mpirun -np 2 Rscript 2_hello.r

1 COMM.RANK = 0
2 [1] "Hello, world"
3 [1] "Hello again"
4 [1] "Hello again"
```



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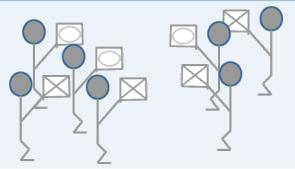


# **MPI** Operations

- Reduce
- Gather
- Broadcast
- Barrier



# Reductions — Combine results into single result

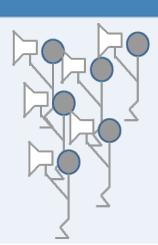




# Gather — Many-to-one

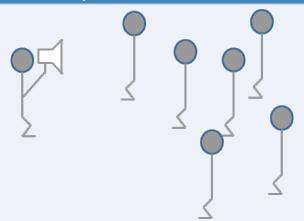
http://r-pbd.org/tutorial





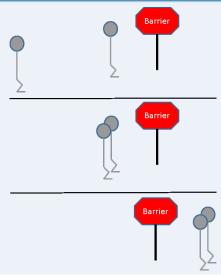


## Broadcast — One-to-many





# Barrier — Synchronization





# MPI Operations (2 of 2)

• **Reduction**: each processor has a number x; add all of them up, find the largest/smallest, . . .

```
reduce(x, op='sum') — reduce to one
allreduce(x, op='sum') — reduce to all
```

 Gather: each processor has a number; create a new object on some processor containing all of those numbers.
 gather(x) — gather to one

```
allgather(x) — gather to one
```

 Broadcast: one processor has a number x that every other processor should also have.
 bcast(x)

 Barrier: "computation wall"; no processor can proceed until all processors can proceed.
 barrier()



#### Quick Example 3

#### Reduce and Gather: 3\_gt.r

```
library(pbdMPI, quietly=TRUE)
init()

comm.set.seed(diff=TRUE)

n <- sample(1:10, size=1)

gt <- gather(n)
comm.print(unlist(gt))

in sm <- allreduce(n, op='sum')
comm.print(sm, all.rank=T)

finalize()</pre>
```

#### Execute this script via:

```
mpirun -np 2 Rscript 3_gt.r
```

#### Sample Output:

```
1 COMM.RANK = 0
2 [1] 2 8
3 COMM.RANK = 0
4 [1] 10
5 COMM.RANK = 1
6 [1] 10
```



#### Quick Example 4

#### Broadcast: 4\_bcast.r

```
library(pbdMPI, quietly=T)
init()

init()

if (comm.rank()==0){
    x <- matrix(1:4, nrow=2)
    } else {
    x <- NULL
    }

y <- bcast(x, rank.source=0)

comm.print(y, rank=1)

finalize()</pre>
```

#### Execute this script via:

#### Sample Output:



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#### Random Seeds

**pbdMPI** offers a simple interface for managing random seeds:

- comm.set.seed(seed=1234, diff=FALSE) All processors use the same seed.
- comm.set.seed(seed=1234, diff=FALSE) All processors use the same seed.



## Other Helper Tools

**pbdMPI** Also contains useful tools for Manager/Worker and task parallelism codes:

- Task Subsetting: Distributing a list of jobs/tasks get.jid(n)
- \*ply: Functions in the \*ply family.
  pbdApply(X, MARGIN, FUN, ...) analogue of apply()
  pbdLapply(X, FUN, ...) analogue of lapply()
  pbdSapply(X, FUN, ...) analogue of sapply()



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#### Summary

Start by loading the package:

```
1 library(pbdMPI, quiet = TRUE)
```

• Always initialize before starting and finalize when finished:

```
1 init()
2
3 # ...
4
5 finalize()
```



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- The Generalized Block Distribution
  - GBD: a Way to Distribute Your Data
  - Example GBD Distributions
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## Distributing Data

#### **Problem:** How to distribute the data

$$x = \begin{bmatrix} x_{1,1} & x_{1,2} & x_{1,3} \\ x_{2,1} & x_{2,2} & x_{2,3} \\ x_{3,1} & x_{3,2} & x_{3,3} \\ x_{4,1} & x_{4,2} & x_{4,3} \\ x_{5,1} & x_{5,2} & x_{5,3} \\ x_{6,1} & x_{6,2} & x_{6,3} \\ x_{7,1} & x_{7,2} & x_{7,3} \\ x_{8,1} & x_{8,2} & x_{8,3} \\ x_{9,1} & x_{9,2} & x_{9,3} \\ x_{10,1} & x_{10,2} & x_{10,3} \end{bmatrix}_{10 \times 3}$$





# Distributing a Matrix Across 4 Processors: Block Distribution

# $x = \begin{bmatrix} x_{1,1} & x_{1,2} & x_{1,3} \\ x_{2,1} & x_{2,2} & x_{2,3} \\ x_{3,1} & x_{3,2} & x_{3,3} \\ \hline x_{4,1} & x_{4,2} & x_{4,3} \\ x_{5,1} & x_{5,2} & x_{5,3} \\ x_{6,1} & x_{6,2} & x_{6,3} \\ \hline x_{7,1} & x_{7,2} & x_{7,3} \\ x_{8,1} & x_{8,2} & x_{8,3} \\ \hline x_{9,1} & x_{9,2} & x_{9,3} \\ \hline x_{10,1} & x_{10,2} & x_{10,3} \end{bmatrix}_{10 \times 3}$

Data

## **Processors**

1 2 3



# Distributing a Matrix Across 4 Processors: Local Load Balance

		Dutu		
<i>x</i> =	x <sub>1,1</sub>	<i>x</i> <sub>1,2</sub>	<i>X</i> 1,3	]
	<i>x</i> <sub>2,1</sub>	<i>X</i> 2,2	<i>x</i> <sub>2,3</sub>	
	<i>x</i> <sub>3,1</sub>	<i>x</i> <sub>3,2</sub>	<i>x</i> <sub>3,3</sub>	
		<i>X</i> <sub>4,2</sub>	X <sub>4,3</sub>	ļ
	<i>X</i> 5,1	<i>X</i> 5,2	<i>X</i> 5,3	İ
	<i>x</i> <sub>6,1</sub>	<i>x</i> <sub>6,2</sub>	<i>x</i> <sub>6,3</sub>	İ
	×7,1	<i>X</i> 7,2	X7,3	
	<i>x</i> <sub>8,1</sub>	<i>x</i> <sub>8,2</sub>	<i>x</i> <sub>8,3</sub>	İ
	X <sub>9,1</sub>	<i>X</i> 9,2	X9,3	İ
	X <sub>10,1</sub>	<i>x</i> <sub>10,2</sub>	<i>X</i> <sub>10,3</sub>	] <sub>10×3</sub>

Data

## **Processors**

1 2 3



#### The GBD Data Structure

Throughout the examples, we will make use of the Generalized Block Distribution, or GBD distributed matrix structure.

- GBD is distributed. No processor owns all the data.
- ② GBD is non-overlapping. Rows uniquely assigned to processors.
- GBD is row-contiguous. If a processor owns one element of a row, it owns the entire row.
- 4 GBD is globally row-major, locally column-major.
- GBD is often locally balanced, where each processor owns (almost) the same amount of data. But this is not required.

$x_{1,1}$	<i>x</i> <sub>1,2</sub>	x <sub>1,3</sub>
$x_{2,1}$	$x_{2,2}$	$x_{2,3}$
<i>x</i> <sub>3,1</sub>	<i>x</i> <sub>3,2</sub>	X3,3
X4,1	X4,2	X4,3
<i>x</i> 5,1	<i>X</i> 5,2	X5,3
<i>x</i> <sub>6,1</sub>	<i>x</i> <sub>6,2</sub>	<i>x</i> <sub>6,3</sub>
x <sub>7,1</sub>	<i>x</i> <sub>7,2</sub>	x <sub>7,3</sub>
<i>X</i> 8,1	X8,2	X8,3
X9,1	X9,2	X9,3
$x_{10,1}$	X <sub>10,2</sub>	<i>x</i> <sub>10,3</sub>

- The last row of the local storage of a processor is adjacent (by global row) to the first row of the local storage of next processor (by communicator number) that owns data.
- GBD is (relatively) easy to understand, but can lead to bottlenecks if you have many more columns than rows.



- 5 The Generalized Block Distribution
  - GBD: a Way to Distribute Your Data
  - Example GBD Distributions
  - Summary



#### Understanding GBD: Global Matrix

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9 \times 9}$$



## Understanding GBD: Load Balanced GBD

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ \hline x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9}$$



# Understanding GBD: Local View



## Understanding GBD: Non-Balanced GBD



#### Understanding GBD: Local View

```
X19
                  X<sub>13</sub>
                           X14
                                   X15
                                            X<sub>16</sub>
                                                     X17
                                                              X<sub>18</sub>

    X21
    X22
    X23
    X24

    X31
    X32
    X33
    X34

                                   X25
                                            X26
                                                     X27
                                                              X28
                                                                       X29
                                 X<sub>35</sub> X<sub>36</sub> X<sub>37</sub>
                                                              X38
                                                                       X39
                  X43
                           X44
                                   X45
                                            X46
                                                     X47
                                                                       X_{49} \rfloor_{4\times9}
                                                              X48
         X_{52} X_{53} X_{54} X_{55} X_{56} X_{57} X_{58}
                  X<sub>63</sub> X<sub>64</sub> X<sub>65</sub> X<sub>66</sub>
                                                      X67
                                                               X68
          X72 X73 X74 X75 X76 X77
                          X84
                                                                        X89
                                    X85
                                             X86
                                                      X87
                                                               X88
                           X94
                                    X95 X96
                                                   X97
                                                               X98
```



- 5 The Generalized Block Distribution
  - GBD: a Way to Distribute Your Data
  - Example GBD Distributions
  - Summary



## Summary

- Need to distribute your data? Try splitting by row.
- May not work well if your data is square (or longer than tall).



## Contents

- 6 Basic Statistics Examples
  - pbdMPI Example: Monte Carlo Simulation
  - pbdMPI Example: Sample Covariance
  - pbdMPI Example: Linear Regression
  - Summary



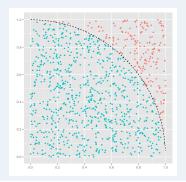
- Basic Statistics Examples
  - pbdMPI Example: Monte Carlo Simulation
  - pbdMPI Example: Sample Covariance
  - pbdMPI Example: Linear Regression



## Example 1: Monte Carlo Simulation

Sample N uniform observations  $(x_i, y_i)$  in the unit square  $[0, 1] \times [0, 1]$ . Then

$$\pi \approx 4 \left( \frac{\# \ \textit{Inside Circle}}{\# \ \textit{Total}} \right) = 4 \left( \frac{\# \ \textit{Blue}}{\# \ \textit{Blue} + \# \ \textit{Red}} \right)$$





## Example 1: Monte Carlo Simulation GBD Algorithm

- Let n be big-ish; we'll take n = 50,000.
- ② Generate an  $n \times 2$  matrix x of standard uniform observations.
- **Ount the number of rows satisfying**  $x^2 + y^2 \le 1$
- Ask everyone else what their answer is; sum it all up.
- Take this new answer, multiply by 4 and divide by n
- If my rank is 0, print the result.



#### Example 1: Monte Carlo Simulation Code

#### Serial Code

```
N <- 50000
2 X <- matrix(runif(N * 2), ncol=2)
3 r \leftarrow sum(rowSums(X^2) \leftarrow 1)
4 PI <- 4*r/N
5 print (PI)
```

#### Parallel Code

```
library(pbdMPI, quiet = TRUE)
2 init()
  comm.set.seed(seed=1234567, diff=TRUE)
  N.gbd <- 50000 / comm.size()
  X.gbd <- matrix(runif(N.gbd * 2), ncol = 2)</pre>
  r.gbd <- sum(rowSums(X.gbd^2) <= 1)</pre>
8 r <- allreduce(r.gbd)</pre>
9 PI <- 4*r/(N.gbd * comm.size())
10 comm.print(PI)
11
12 finalize()
```

## Note

For the remainder, we will exclude loading, init, and finalize calls.



- 6 Basic Statistics Examples
  - pbdMPI Example: Monte Carlo Simulation
  - pbdMPI Example: Sample Covariance
  - pbdMPI Example: Linear Regression
  - Summary



# Example 2: Sample Covariance

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$



# Example 2: Sample Covariance GBD Algorithm

- $\bigcirc$  Determine the total number of rows N.
- Ompute the vector of column means of the full matrix.
- Subtract each column's mean from that column's entries in each local matrix.
- Compute the crossproduct locally and reduce.
- O Divide by N-1.



## Example 2: Sample Covariance Code

#### Serial Code

```
N \leftarrow nrow(X)
 mu <- colSums(X) / N
 X <- sweep(X, STATS=mu, MARGIN=2)
 Cov.X <- crossprod(X) / (N-1)
6
 print(Cov.X)
```

#### Parallel Code

```
N <- allreduce(nrow(X.gbd), op="sum")</pre>
mu <- allreduce(colSums(X.gbd) / N, op="sum")</pre>
X.gbd <- sweep(X.gbd, STATS=mu, MARGIN=2)
Cov.X <- allreduce(crossprod(X.gbd), op="sum") / (N-1)
comm.print(Cov.X)
```



http://r-pbd.org/tutorial

- 6 Basic Statistics Examples
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  - Summary



# Example 3: Linear Regression

Find  $\beta$  such that

$$y = X\beta + \epsilon$$

When X is full rank,

$$\hat{\boldsymbol{\beta}} = (\boldsymbol{X}^T \boldsymbol{X})^{-1} \boldsymbol{X}^T \boldsymbol{y}$$



# Example 3: Linear Regression GBD Algorithm

- Locally, compute  $tx = x^T$
- ② Locally, compute A = tx \* x. Query every other processor for this result and sum up all the results.
- **①** Locally, compute B = tx \* y. Query every other processor for this result and sum up all the results.
- Locally, compute  $A^{-1} * B$



# Example 3: Linear Regression Code

#### Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4 ols <- solve(A) %*% B
```

#### Parallel Code

```
tX.gbd <- t(X.gbd)
A <- allreduce(tX.gbd %*% X.gbd, op = "sum")
B <- allreduce(tX.gbd %*% y.gbd, op = "sum")
ols <- solve(A) %*% B
```



- Basic Statistics Examples
  - pbdMPI Example: Monte Carlo Simulation
  - pbdMPI Example: Sample Covariance
  - pbdMPI Example: Linear Regression
  - Summary



## Summary

- SPMD programming is (often) a natural extension of serial programming.
- More pbdMPI examples in pbdDEMO.



## Contents

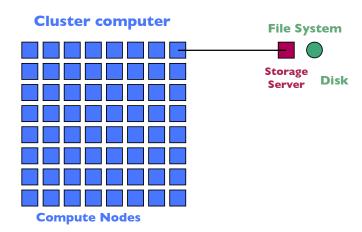
- Data Input
  - Cluster Computer and File System
  - Serial Data Input
  - Parallel Data Input
  - Summary



- Data Input
  - Cluster Computer and File System
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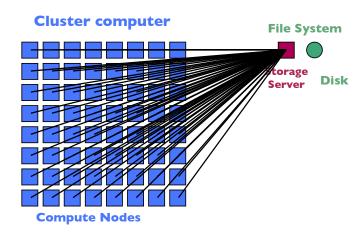


# One Node to One Storage Server



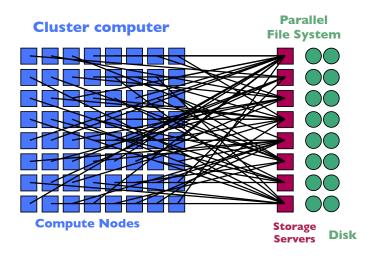


# Many Nodes to One Storage Server



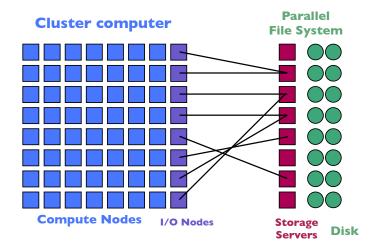


# Many Nodes to Few Storage Servers



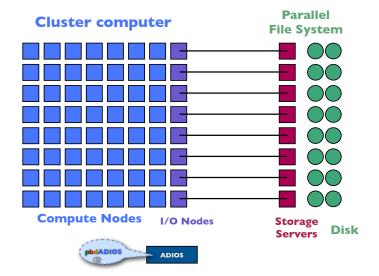


# Few Nodes to Few Storage Servers - Default





# Few Nodes to Few Storage Servers - Coordinated





- Data Input
  - Cluster Computer and File System
  - Serial Data Input
  - Parallel Data Input
  - Summary



# Separate manual: http://r-project.org/

- scan()
- read.table()
- read.csv()
- socket



#### CSV Data: Read Serial then Distribute

#### Listing:

```
library(pbdDMAT)
  if(comm.rank() == 0) { # only read on process 0
    x <- read.csv("myfile.csv")</pre>
  } else {
    x <- NUI.I.
7
  dx <- as.ddmatrix(x)</pre>
```



- Data Input
  - Cluster Computer and File System
  - Serial Data Input
  - Parallel Data Input
  - Summary



#### New Issues

- How to read in parallel?
- CSV, SQL, NetCDF4, HDF, ADIOS, custom binary
- How to partition data across nodes?
- How to structure for scalable libraries?
- Read directly into form needed or restructure?
- . . .
- A lot of work needed here!



#### **CSV Data**

#### Serial Code

```
1 x <- read.csv("x.csv")
2 x
```

#### Parallel Code



## Binary Data: Vector

```
## set up start and length for reading a vector of n doubles
  size <- 8 # bytes
  my_ids <- get.jid(n, method="block")</pre>
  my_start <- (my_ids[1] - 1)*size</pre>
  my_length <- length(my_ids)</pre>
  con <- file("binary.vector.file", "rb")</pre>
  seekval <- seek(con, where=my_start, rw="read")</pre>
11 x <- readBin(con, what="double", n=my_length, size=size)
```



#### Binary Data: Matrix

```
1 ## read an nrow by ncol matrix of doubles split by columns
  size <- 8 # bvtes
3
  my_ids <- get.jid(ncol, method="block")</pre>
  my_ncol <- length(my_ids)</pre>
6 my_start <- (my_ids[1] - 1)*nrow*size
  my_length <- my_ncol*nrow</pre>
9 con <- file("binary.matrix.file", "rb")</pre>
10 seekval <- seek(con, where=my_start, rw="read")
11 x <- readBin(con, what="double", n=my_length, size=size)
12
13 ## glue together as a column-block ddmatrix
14 gdim <- c(nrow, ncol)
15 | ldim <- c(nrow, my_ncol)
16 bldim <- c(nrow, allreduce(my_ncol, op="max"))
17 X <- new("ddmatrix", Data=matrix(x, nrow, my_ncol),</pre>
            dim=gdim, ldim=ldim, bldim=bldim, ICTXT=1)
18
19
20 ## redistribute for ScaLAPACK's block-cyclic
21 X <- redistribute(X, bldim=c(2, 2), ICTXT=0)
22 Xprc <- prcomp(X)
```

#### NetCDF4 Data

```
### parallel read after determining start and length
nc <- nc_open_par(file_name)

nc_var_par_access(nc, "variable_name")
new.X <- ncvar_get(nc, "variable_name", start, length)
nc_close(nc)

finalize()</pre>
```



- Data Input
  - Cluster Computer and File System
  - Serial Data Input
  - Parallel Data Input
  - Summary



#### Summary

- Mostly "do it yourself"
- Parallel file system for big data
  - Binary files for true parallel reads
  - Know number of readers vs number of storage servers
- Redistribution help from ddmatrix functions
- More help under development



## Contents

- Introduction to pbdDMAT and the ddmatrix Structure
  - Introduction to Distributed Matrices
  - pbdDMAT
  - Summary

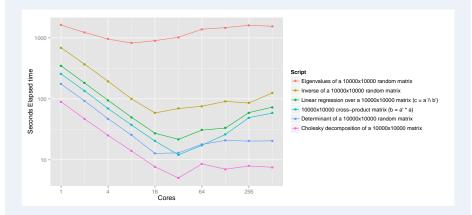


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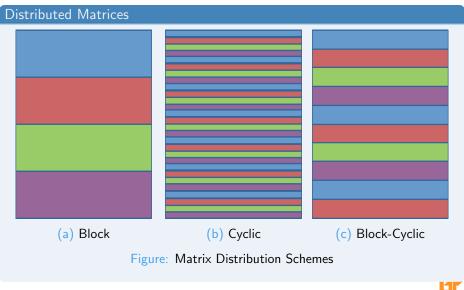
#### Distributed Matrices

# You can only get so far with one node...



The solution is to distribute the data.







# Distributed Matrices (b) 2d Cyclic (a) 2d Block (c) 2d Block-Cyclic Figure: Matrix Distribution Schemes Onto a 2-Dimensional Grid



## Processor Grid Shapes

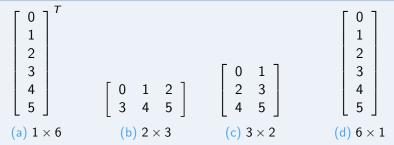


Table: Processor Grid Shapes with 6 Processors



#### The ddmatrix Class

For **d**istributed **d**ense **matrix** objects, we use the special S4 class ddmatrix.

$$\mathtt{ddmatrix} = \begin{cases} \textbf{Data} & \mathsf{The\ local\ submatrix}\ (\mathsf{an\ R\ matrix}) \\ \textbf{dim} & \mathsf{Dimension\ of\ the\ global\ matrix} \\ \textbf{Idim} & \mathsf{Dimension\ of\ the\ local\ submatrix} \\ \textbf{bldim} & \mathsf{Dimension\ of\ the\ blocks} \\ \textbf{ICTXT} & \mathsf{MPI\ Grid\ Context} \end{cases}$$



## Understanding ddmatrix: Global Matrix

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{0 \times 0}$$



http://r-pbd.org/tutorial

#### ddmatrix: 1-dimensional Row Block

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9}$$

Processor grid = 
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (1,0) \\ (2,0) \\ (3,0) \end{vmatrix}$$



#### ddmatrix: 2-dimensional Row Block

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ \hline x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9 \times 9}$$

Processor grid = 
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



#### ddmatrix: 1-dimensional Row Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid = 
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (1,0) \\ (2,0) \\ (3,0) \end{vmatrix}$$



#### ddmatrix: 2-dimensional Row Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid = 
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



#### ddmatrix: 2-dimensional Block-Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9}$$

Processor grid = 
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



- Introduction to pbdDMAT and the ddmatrix Structure
  - Introduction to Distributed Matrices
  - pbdDMAT
  - Summary



#### The ddmatrix Data Structure

The more complicated the processor grid, the more complicated the distribution.



## ddmatrix: 2-dimensional Block-Cyclic with 6 Processors

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9}$$

Processor grid = 
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



# Understanding ddmatrix: Local View

$$\begin{bmatrix} x_{11} & x_{12} & x_{17} & x_{18} \\ x_{21} & x_{22} & x_{27} & x_{28} \\ x_{51} & x_{52} & x_{57} & x_{58} \\ x_{61} & x_{62} & x_{67} & x_{68} \\ x_{91} & x_{92} & x_{97} & x_{98} \end{bmatrix}_{5\times4} \begin{bmatrix} x_{13} & x_{14} & x_{19} \\ x_{23} & x_{24} & x_{29} \\ x_{53} & x_{54} & x_{59} \\ x_{63} & x_{64} & x_{69} \\ x_{93} & x_{94} & x_{99} \end{bmatrix}_{5\times3} \begin{bmatrix} x_{15} & x_{16} \\ x_{25} & x_{26} \\ x_{55} & x_{56} \\ x_{65} & x_{66} \\ x_{95} & x_{96} \end{bmatrix}_{5\times2}$$

$$\begin{bmatrix} x_{31} & x_{32} & x_{37} & x_{38} \\ x_{41} & x_{42} & x_{47} & x_{48} \\ x_{71} & x_{72} & x_{77} & x_{78} \\ x_{81} & x_{82} & x_{87} & x_{88} \end{bmatrix}_{4\times4} \begin{bmatrix} x_{33} & x_{34} & x_{39} \\ x_{43} & x_{44} & x_{49} \\ x_{73} & x_{74} & x_{79} \\ x_{83} & x_{84} & x_{89} \end{bmatrix}_{4\times3} \begin{bmatrix} x_{35} & x_{36} \\ x_{45} & x_{46} \\ x_{75} & x_{76} \\ x_{85} & x_{86} \end{bmatrix}_{4\times2}$$

Processor grid = 
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



#### The ddmatrix Data Structure

- ddmatrix is distributed. No one processor owns all of the matrix
- ddmatrix is non-overlapping. Any piece owned by one processor is owned by no other processors.
- ddmatrix can be row-contiguous or not, depending on the processor grid and blocking factor used.
- ddmatrix is locally column-major and globally, it depends...

x <sub>11</sub>	<i>x</i> <sub>12</sub>	X <sub>13</sub>	X <sub>14</sub>	X <sub>15</sub>
x <sub>21</sub>	<i>x</i> <sub>22</sub>	X <sub>23</sub>	<i>x</i> <sub>24</sub>	X <sub>25</sub>
X31	X32	X33	X34	X35
X41	X42	X43	X44	X45
X <sub>51</sub>	X52	X53	<i>X</i> 54	<i>X</i> 55
<i>X</i> 61	X62	X63	<i>X</i> 64	<i>X</i> 65
<i>x</i> <sub>71</sub>	<i>X</i> <sub>72</sub>	X73	X74	<i>X</i> 75
X81	X82	X83	X84	X85
<i>X</i> 91	X92	X93	X94	X95

- GBD is a generalization of the one-dimensional block ddmatrix distribution. Otherwise there is no relation.
- ddmatrix is confusing, but very robust.



http://r-pbd.org/tutorial

#### Pros and Cons of This Data Structure

#### Pros

 Robust for matrix computations.

#### Cons

Confusing layout.

This is why we hide most of the distributed details.

The details are there if you want them (you don't want them).



# Methods for class ddmatrix

pbdDMAT has over 100 methods with identical syntax to R:

- `[`, rbind(), cbind(), ...
- lm.fit(), prcomp(), cov(), ...
- `%\*%`, solve(), svd(), norm(), ...
- median(), mean(), rowSums(), ...

## Serial Code

1 cov(x)

#### Parallel Code

1 cov(x)



# Comparing pbdMPI and pbdDMAT

## pbdMPI:

- MPI + sugar.
- GBD not the only structure pbdMPI can handle (just a useful convention).

## pbdDMAT:

- Distributed matrices + statistics.
- The ddmatrix structure must be used for pbdDMAT.
- If the data is not 2d block-cyclic compatible, ddmatrix will *definitely* give the wrong answer.



- Introduction to pbdDMAT and the ddmatrix Structure
  - Introduction to Distributed Matrices
  - pbdDMAT
  - Summary



# Summary

Start by loading the package:

```
1 library (pbdDMAT, quiet = TRUE)
```

Always initialize before starting and finalize when finished:

```
init.grid()
2
4
 finalize()
```



# Contents

- Examples Using pbdDMAT
  - RandSVD
  - Summary



- Examples Using pbdDMAT
  - RandSVD
  - Summary



#### Randomized SVD<sup>1</sup>

#### PROTOTYPE FOR RANDOMIZED SVD

Given an  $m \times n$  matrix A, a target number k of singular vectors, and an exponent q (say, q = 1 or q = 2), this procedure computes an approximate rank-2k factorization  $U\Sigma V^*$ , where U and V are orthonormal, and  $\Sigma$  is nonnegative and diagonal.

#### Stage A:

- Generate an  $n \times 2k$  Gaussian test matrix  $\Omega$ .
- Form  $Y = (AA^*)^q A\Omega$  by multiplying alternately with A and  $A^*$ . Construct a matrix Q whose columns form an orthonormal basis for

#### the range of Y.

- Stage B: Form  $B = Q^*A$ .
- Compute an SVD of the small matrix:  $B = \widetilde{U}\Sigma V^*$ .
- Set U = QU.

Note: The computation of Y in step 2 is vulnerable to round-off errors. When high accuracy is required, we must incorporate an orthonormalization step between each application of A and  $A^*$ ; see Algorithm 4.4.

Algorithm 4.4: Randomized Subspace Iteration Given an  $m \times n$  matrix A and integers  $\ell$  and a, this algorithm computes an  $m \times \ell$  orthonormal matrix Q whose range approximates the range of A. Draw an  $n \times \ell$  standard Gaussian matrix  $\Omega$ . Form  $Y_0 = A\Omega$  and compute its QR factorization  $Y_0 = Q_0R_0$ . for j = 1, 2, ..., qForm  $\tilde{Y}_{i} = A^{*}Q_{i-1}$  and compute its QR factorization  $\tilde{Y}_{i} = \tilde{Q}_{i}\tilde{R}_{i}$ . Form  $Y_i = A\widetilde{Q}_i$  and compute its QR factorization  $Y_i = Q_iR_i$ .

#### Serial R

```
randSVD \leftarrow function(A, k, q=3)
 2
 3
        ## Stage A
         Omega <- matrix(rnorm(n*2*k),
                   nrow=n. ncol=2*k)
         Y <- A %*% Omega
        Q \leftarrow qr.Q(qr(Y))
         At \leftarrow t(A)
 9
         for(i in 1:q)
10
11
             Y <- At %*% Q
12
             Q \leftarrow qr.Q(qr(Y))
             Y <- A %*% Q
13
             Q \leftarrow ar.Q(ar(Y))
14
15
16
17
        ## Stage B
        B <- t(Q) %*% A
18
19
        U <- La.svd(B)$u
20
        U <- Q %*% U
        U[, 1:k]
22
```

 $<sup>^{1}</sup>$ Halko N, Martinsson P-G and Tropp J A 2011 Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions SIAM Rev. 53 217-88



21

end  $Q = Q_q$ .

#### Randomized SVD

#### Serial R

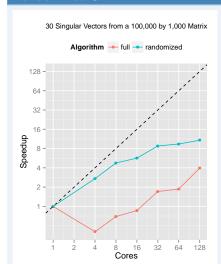
```
randSVD \leftarrow function(A, k, q=3)
 1
2
3
        ## Stage A
 4
        Omega <- matrix(rnorm(n*2*k),
5
6
7
               nrow=n. ncol=2*k)
        Y <- A %*% Omega
        Q \leftarrow qr.Q(qr(Y))
8
        At < -t(A)
9
         for(i in 1:q)
10
11
             Y <- At %*% Q
12
             Q \leftarrow qr.Q(qr(Y))
             Y <- A %*% Q
13
14
             Q \leftarrow qr.Q(qr(Y))
15
16
17
        ## Stage B
18
        B <- t(Q) %*% A
19
        U <- La.svd(B)$u
20
        U <- Q %*% U
21
        U[, 1:k]
22
```

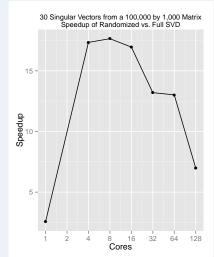
## Parallel pbdR

```
randSVD <- function(A, k, q=3)
 3
        ## Stage A
        Omega <- ddmatrix("rnorm",
               nrow=n. ncol=2*k)
        Y <- A %*% Omega
        Q \leftarrow qr.Q(qr(Y))
         At \leftarrow t(A)
 9
         for(i in 1:q)
10
11
              Y <- At %*% Q
12
             Q \leftarrow qr.Q(qr(Y))
             Y <- A %*% Q
13
14
             Q \leftarrow qr.Q(qr(Y))
15
16
17
        ## Stage B
        B <- t(Q) %*% A
18
19
        U <- La.svd(B)$u
20
        U <- Q %*% U
21
        U[, 1:k]
22
```



#### Randomized SVD







- Examples Using pbdDMAT
  - RandSVD
  - Summary



# Summary

- pbdDMAT makes distributed (dense) linear algebra easier.
- Can enable rapid prototyping at large scale.



# Contents

- MPI Profiling
  - Profiling with the pbdPROF Package
  - Installing pbdPROF
  - Example
  - Summary



- **MPI** Profiling
  - Profiling with the pbdPROF Package
  - Installing pbdPROF
  - Example

http://r-pbd.org/tutorial

Summary



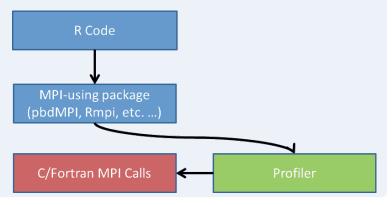
# Introduction to pbdPROF

- Successful Google Summer of Code 2013 project.
- Available on the CRAN.
- Enables profiling of MPI-using R scripts.
- **pbd**R packages officially supported; can work with others...
- Also reads, parses, and plots profiler outputs.



#### How it works

MPI calls get hijacked by profiler and logged:





# Introduction to pbdPROF

- Currently supports the profilers fpmpi and mpiP.
- **fpmpi** is distributed with **pbdPROF** and installs easily, but offers minimal profiling capabilities.
- mpiP is fully supported also, but you have to install and link it yourself.



- MPI Profiling
  - Profiling with the pbdPROF Package
  - Installing pbdPROF
  - Example
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# Installing pbdPROF

- Build pbdPROF.
- 2 Rebuild **pbdMPI** (linking with **pbdPROF**).
- Run your analysis as usual.
- Interactively analyze profiler outputs with pbdPROF.

This is explained at length in the **pbdPROF** vignette.



# Rebuild **pbdMPI**

```
R CMD INSTALL pbdMPI_0.2-2.tar.gz
--configure-args="--enable-pbdPROF"
```

- Any package which explicitly links with an MPI library must be rebuilt in this way (pbdMPI, Rmpi, ...).
- Other pbdR packages link with pbdMPI, and so do not need to be rebuilt.
- See **pbdPROF** vignette if something goes wrong.



- MPI Profiling
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# An Example from **pbdDMAT**

- Compute SVD in **pbdDMAT** package.
- Profile MPI calls with mpiP.



# Example Script

#### my\_svd.r

```
1 library(pbdMPI, quietly=TRUE)
2 library(pbdDMAT, quietly=TRUE)
3 init.grid()
4 5 6 n <- 1000 7 x <- ddmatrix("rnorm", n, n)
8 9 my.svd <- La.svd(x)
10 11 12 finalize()</pre>
```



# Example Script

#### Run example with 4 ranks:

```
$ mpirun -np 4 Rscript my_svd.r
mpiP:
mpiP: mpiP: mpiP V3.3.0 (Build Sep 23 2013/14:00:47)
mpiP: Direct questions and errors to
    mpip-help@lists.sourceforge.net
mpiP:
Using 2x2 for the default grid size

mpiP:
mpiP: Storing mpiP output in [./R.4.5944.1.mpiP].
mpiP:
```



#### Read Profiler Data into R

## Interactively (or in batch) Read in Profiler Data

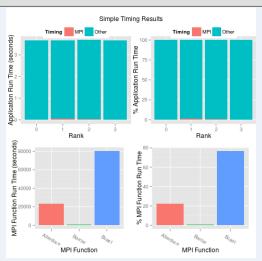
```
1 library(pbdPROF)
2 prof.data <- read.prof("R.4.28812.1.mpiP")</pre>
```

# Partial Output of Example Data

```
> prof.data
An mpip profiler object:
[[1]]
  Task AppTime MPITime MPI.
     0
         5.71 0.0387 0.68
         5.70 0.0297 0.52
2
  2 5.71 0.0540 0.95
3
    3 5.71 0.0355 0.62
4
5
     * 22.80 0.1580 0.69
[[2]]
   ID Lev File.Address Line_Parent_Funct MPI_Call
       0 1.397301e+14
                               [unknown] Allreduce
1
       0 1.397301e+14
                               [unknown]
                                            Bcast
```

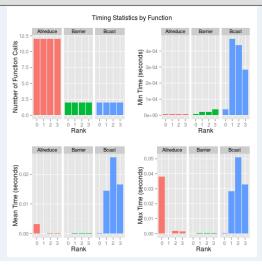


plot(prof.data)



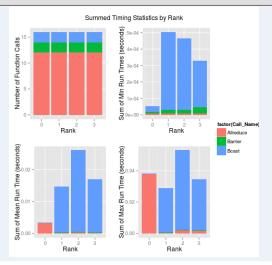


plot(prof.data, plot.type="stats1")





plot(prof.data, plot.type="stats2")





plot(prof.data, plot.type="messages1")



plot(prof.data, plot.type="messages2")





- MPI Profiling
  - Profiling with the pbdPROF Package
  - Installing pbdPROF
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# Summary

- pbdPROF offers tools for profiling R-using MPI codes.
- Easily builds fpmpi; also supports mpiP.



# Contents

Wrapup



## Summary

- Profile your code to understand your bottlenecks.
- pbdR makes distributed parallelism with R easier.
- Distributing data to multiple nodes
- For truly large data, I/O must be parallel as well.



## The pbdR Project

- Our website: http://r-pbd.org/
- Email us at: RBigData@gmail.com
- Our google group: http://group.r-pbd.org/

# Where to begin?

- The pbdDEMO package http://cran.r-project.org/web/packages/pbdDEMO/
- The pbdDEMO Vignette: http://goo.gl/HZkRt



# Thanks for coming!

# Questions?



http://r-pbd.org/

Come see our poster on Wednesday at 5:30!

