**Ball on Plate**

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1. **Introduction**

The purpose of this system is to balance a ball on a plate using two stepper motors attached in line to the bottom side of the plate. The ball would be placed on the plate, the plate would move in the desired axis to center the ball on the plate. The biggest challenge for this project is the plate positioning as well as the ball balance math. These must work in kind to produce a position on the plate. The plate is linked via X and Y axis.

**Figure 1.** Mathematical Model of Ball on Plate

1. **Modeling**

The mathematical model for the Ball and Plate system is shown below in Figure 1. The modeling utilized for the X-axis was replicated for the Y-axis due to symmetry in the model. The nonlinear equation of motion for the ball given below was calculated from further examination of the mathematical representation.

Eq. (1)

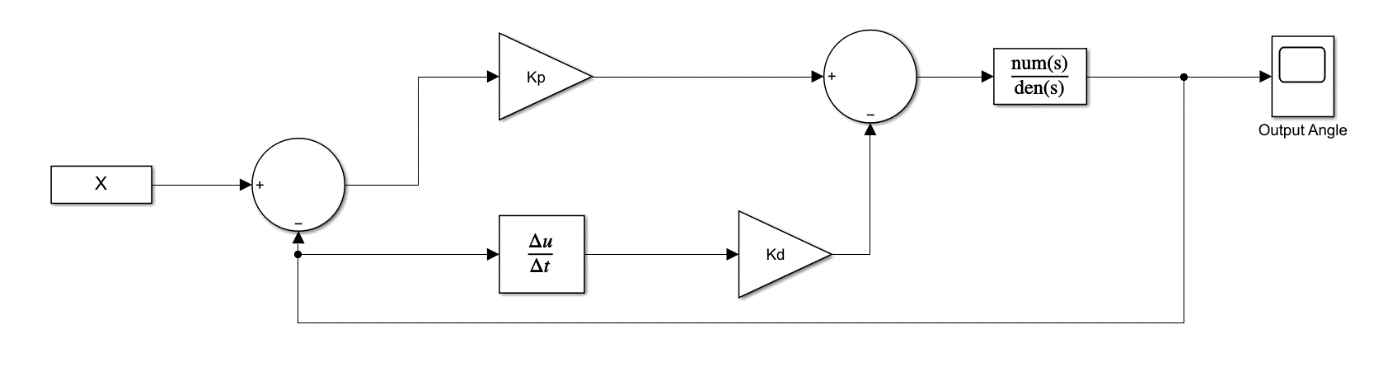
The arm of the motor and its relationship to the angle of the plate can be utilized with small angle approximation to form a near linearization equation.

Eq. (2)

From this point, the Laplace of the linear equation can be used to determine the transfer function.

Eq. (3)

Using the measured ball position, the servo shaft angle is computed to find the desired ball position. The block diagram controls the servo position with the use of proportional and derivative gain.



**Figure 2.** Control System Block Diagram

With the specifications of less than 5% overshoot and a settling time of less than three seconds, the equations for the damping ratio and natural frequency can be determined.

Eq. (4)

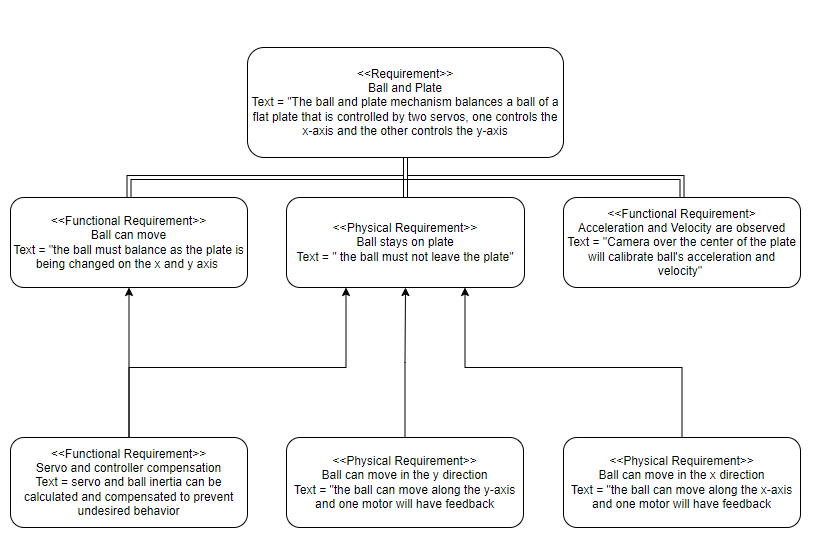
Eq. (5)

Using the values obtained from Eq. (4) and Eq. (5), the proportional and derivative gain can be calculated.

Eq. (6)

Eq. (7)

**Figure 3** shown below represents the requirements of a working Ball and Plate system.



**Figure 3.** Working System Requirements

1. **Controller Design and Simulation**

**Figure 4** and **Figure 5** given below contains the MATLAB code implemented to test the mathematical model. The interpretation of the code is as follows: Clear all possible variables, generate a link to Coppelia, create and set up the physical parameters of the system, run the code if there is a valid connection to Coppelia, and display a “Fail Connection Error” if connection to Coppelia is not secured. If connected to Coppelia, the code will continue to run in the following order: Initialization of Simulink, set up handles, gather required Coppelia data, update Simulink values, run the Simulink, output the data to Coppelia to adjust motor angle, and repeat the process so long as Coppelia is running.

Text

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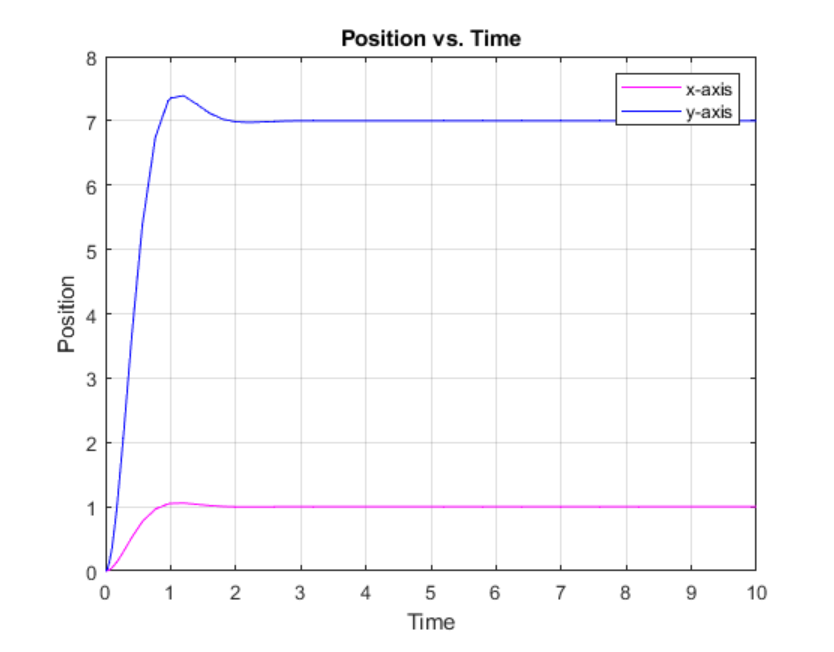
**Figure 4.** MATLAB Code

Graphical user interface, text, application

Description automatically generated

**Figure 5.** MATLAB Code

The output data from MATLAB depicting position vs. time in respect to the ball of the system is given by the graph below. Note the x- and y- positions of the ball are listed independently on the graph and the y-position rapidly increases in relation to the x-position.



**Figure 6.** Ball Position vs Time

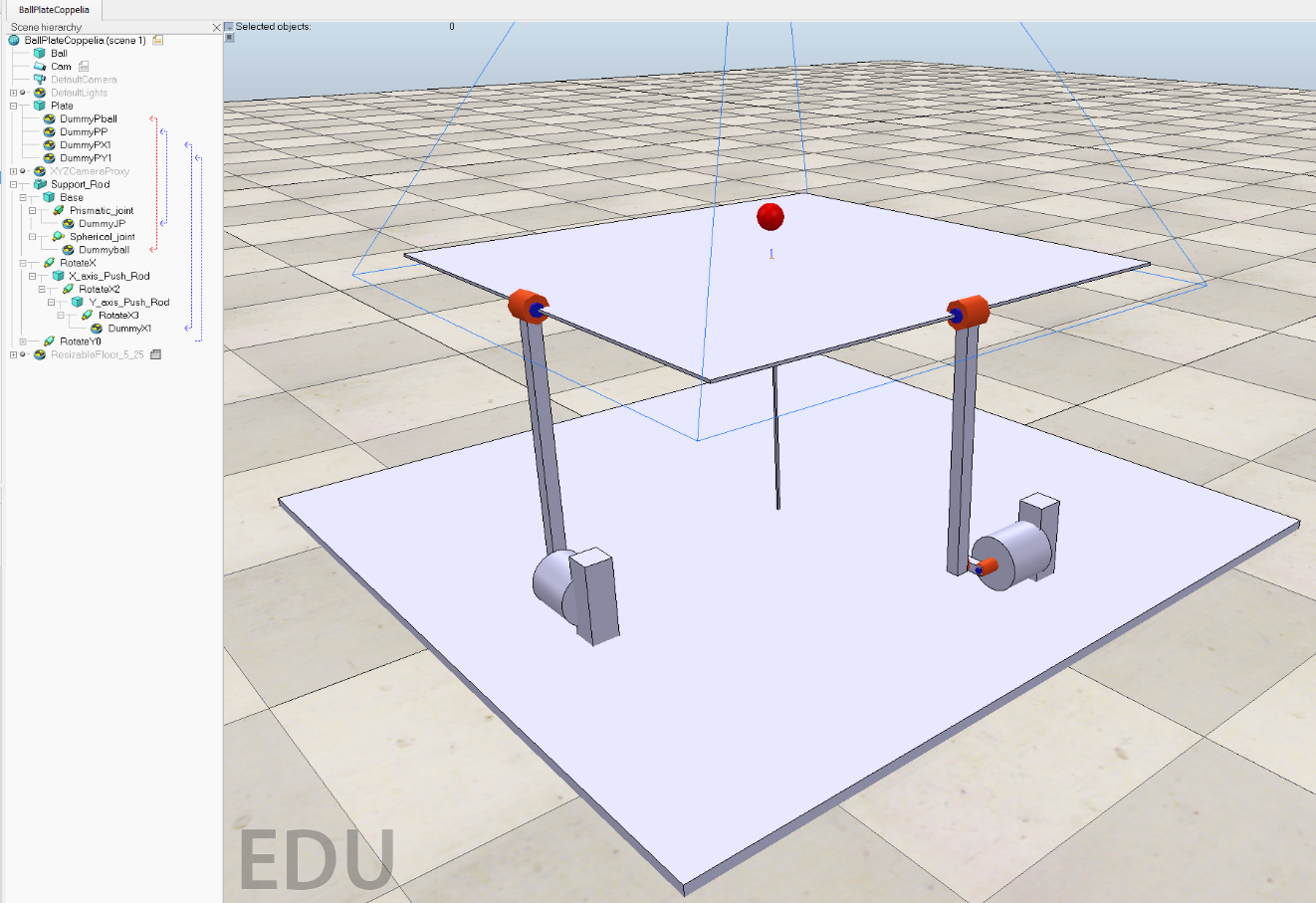
The final Simulink result file implemented for the project is given below. The first step is to enter a desired position for the ball. Once the balls position is obtained, the value is input into the left end. The data obtained is from the Coppelia and MATLAB codes elaborated on in previous sections. The next step is to calculate the motor angle, which results directly from the Simulink simulation. The final step in the Simulink is the reverse of a previous step; the calculated motor angle value is transferred back into the Coppelia and MATLAB code, alerting the motor of the angle required.

Diagram, schematic

Description automatically generated

**Figure 7.** Simulink

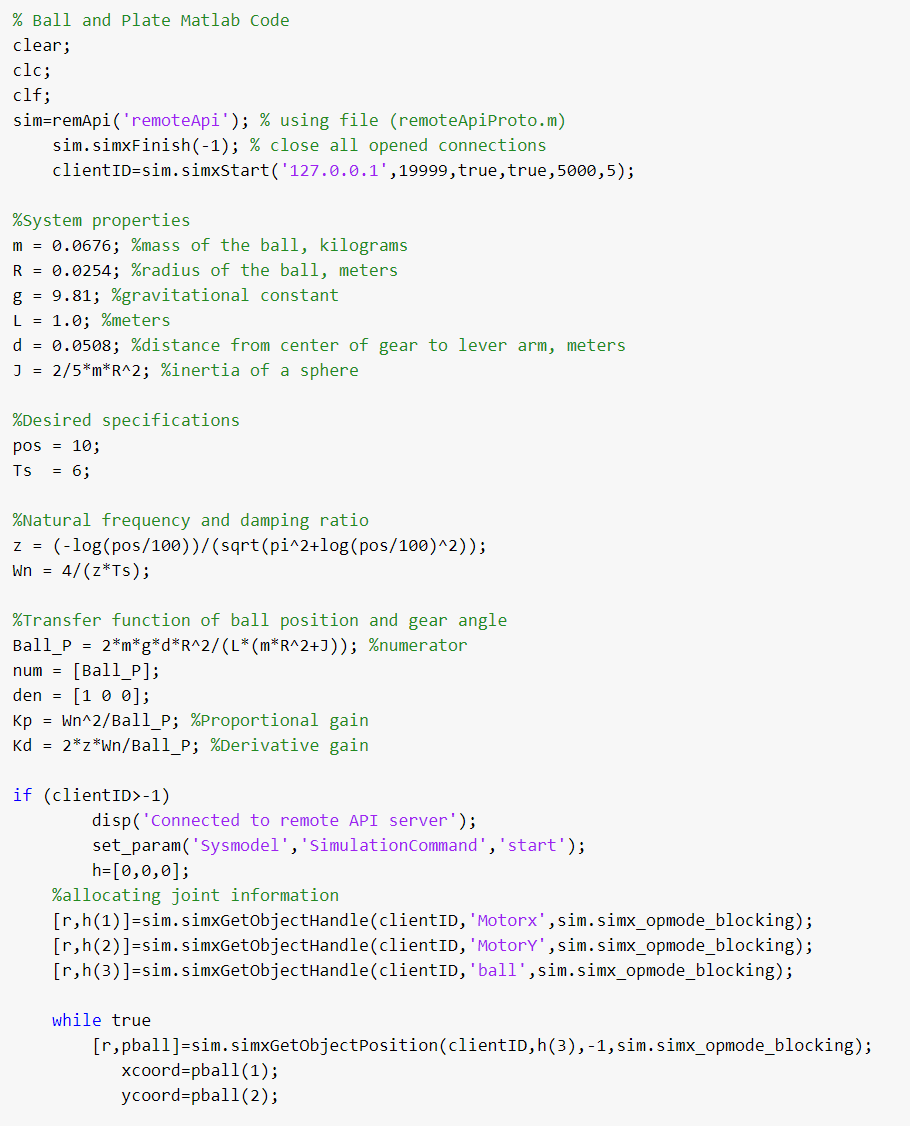
In order to physically model the ball on plate system, CoppeliaSim was utilized. The model used multiple joint connections as well as dynamic objects. The plate was held in place using a series of rods and joints. More specifically, a spherical joint served as the direct connection to the plate, allowing the plate to swivel and rotate in all directions. Connected to the spherical joint are two support rods with linearly sliding prismatic joints. The joint serves as a connection for the two support rods and allows the plate vertical motion. The combination of unique joints and rods allows the system three degrees of freedom. The motion of the support rods is provided by two motors. The final modeled object is a vision sensor positioned above the plate. This location provides a birds-eye view of the plate which allows for sensing ball position and movement.



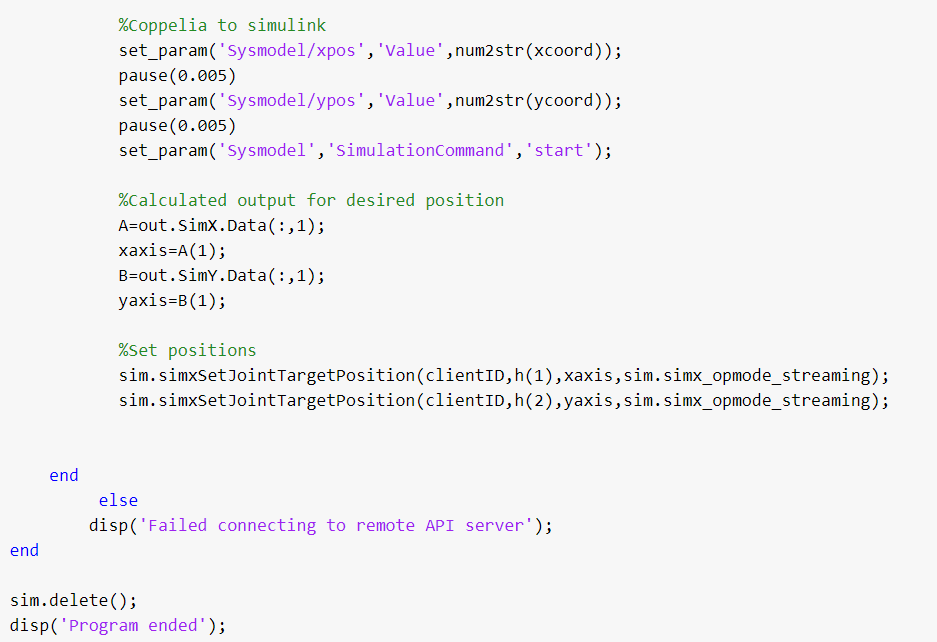
**Figure 8.** CoppeliaSim Model

1. **Conclusion**

**Appendix A**

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**Appendix A**

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**References**

Bayar, G. “Theoretical and Experimental Investigation of Backlash Effects on a 2-DOF

Robotic Balancing Table.” Mechanika (Kaunas, Lithuania : 1995), vol. 23, no. 1, Kauno

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*2 DOF Ball Balancer Workbook*, https://www.made-for-science.com/en/quanser/?df=made-for-science-quanser-2-dof-ball-balancer-coursewarestud-matlab.pdf.