















### 17. SIMULATION

### Functions for probability distributions in R

- rnorm: generate random Normal variates with a given mean and standard deviation
- dnorm: evaluate the Normal probability density (with a given mean/SD)
  at a point (or vector of points)
- pnorm: evaluate the cumulative distribution function for a Normal distribution
- rpois: generate random Poisson variates with a given rate















Probability distribution functions usually have four functions associated with them. The functions are prefixed with a

- d for density
- r for random number generation
- p for cumulative distribution
- q for quantile function















Working with the Normal distributions requires using these four functions

```
dnorm(x, mean = 0, sd = 1, log = FALSE)
pnorm(q, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
qnorm(p, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
rnorm(n, mean = 0, sd = 1)
```

If  $\Phi$  is the cumulative distribution function for a standard Normal distribution, then pnorm (q) =  $\Phi(q)$  and qnorm (p) =  $\Phi^{-1}(p)$ .





























Setting the random number seed with set.seed ensures reproducibility.

```
> set.seed(1)
> rnorm(5)
[1] -0.6264538  0.1836433 -0.8356286  1.5952808  0.3295078
> rnorm(5)
[1] -0.8204684  0.4874291  0.7383247  0.5757814 -0.3053884
> set.seed(1)
> rnorm(5)
[1] -0.6264538  0.1836433 -0.8356286  1.5952808  0.3295078
```

Note: Always set the random number seed when conducting a simulation!















### Generating Poisson data

```
> rpois(10, 1)
 [1] 0 0 1 1 2 1 1 4 1 2
> rpois(10, 2)
 [1] 4 1 2 0 1 1 0 1 4 1
> rpois(10, 20)
 [1] 19 19 24 23 22 24 23 20 11 22
> ppois(2, 2) ##Cumulative distribution
[1] 0.6766764 ## P(x \le 2)
> ppois(4, 2)
[1] 0.947347 ## P(x \le 4)
> ppois(6, 2)
[1] 0.9954662 \#P(x \le 6)
```















Suppose we want to simulate from the following linear model

$$y = \beta_0 + \beta_1 + \varepsilon$$

where  $\varepsilon \sim N(0, 2^2)$ . Assume  $x \sim N(0, 1^2)$ ,  $\beta_0 = 0.5$  and  $\beta_1 = 2$ .





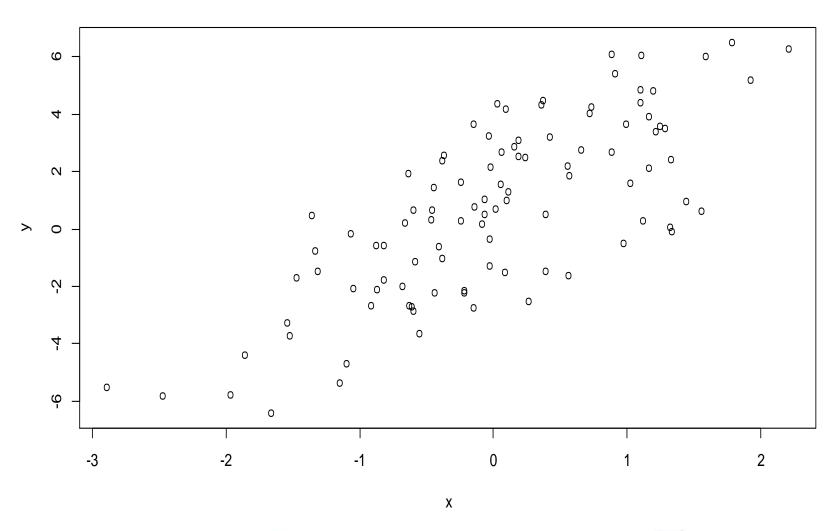
























### What if x is binary?

```
> set.seed(10)
> x <- rbinom(100, 1, 0.5)
> e <- rnorm(100, 0, 2)
> y <- 0.5 + 2 * x + e
> summary(y)
   Min. 1st Qu. Median Mean 3rd Qu. Max.
-3.4936 -0.1409 1.5767 1.4322 2.8397 6.9410
> plot(x, y)
```



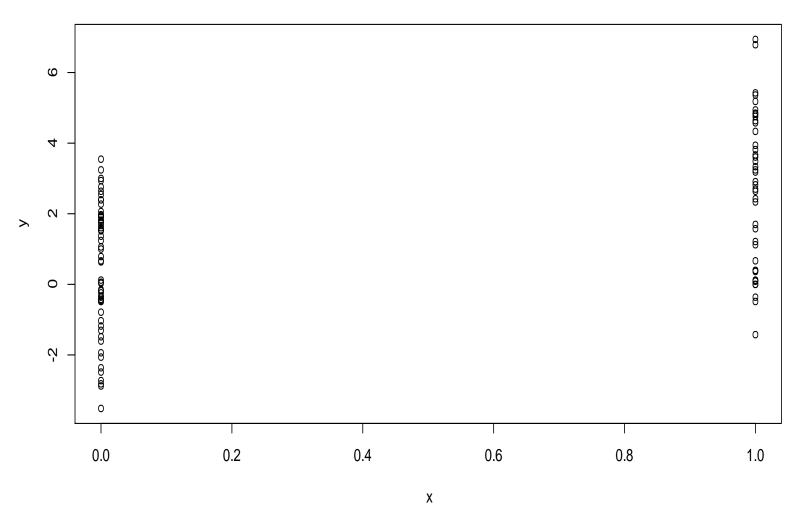


























### GENERATING RANDOM NUMBERS FROM A GENERALIZED LINEAR MODEL

Suppose we want to simulate from a Poisson model where

```
Y \sim Po~(\mu) log~(\mu) = ~\beta_0 + \beta_1 x~ and ~\beta_0 = 0.5~ and ~\beta_1 = 0.3. We need rpois function
```

```
> set.seed(1)
> x <- rnorm(100)
> log.mu <- 0.5 + 0.3 * x
> y <- rpois(100, exp(log.mu))
> summary(y)
   Min. 1st Qu. Median Mean 3rd Qu. Max.
   0.00   1.00   1.55   2.00   6.00
> plot(x, y)
```







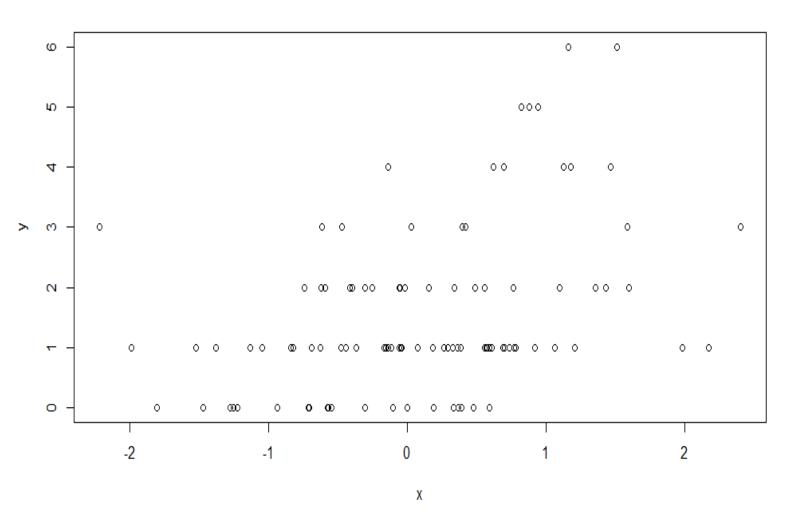








# GENERATING RANDOM NUMBERS FROM A GENERALIZED LINEAR MODEL

















#### **RANDOM SAMPLING**

The sample function draws randomly from a specified set of (scalar) objects allowing you to sample from arbitrary distributions.

```
> set.seed(1)
> sample(1:10, 4)
[1] 3 4 5 7
> sample(1:10, 4)
[1] 3 9 8 5
> sample(letters, 5)
[1] "q" "b" "e" "x" "p"
> sample(1:10) ## permutation
              6 9 2 8 3 1 5
> sample(1:10)
> sample(1:10, replace = TRUE)
 [1] 2 9 7 8 2 8 5 9 7 8
```















#### **SIMULATION**

### Summary

- Drawing samples from specific probability distributions can be done with r\* functions
- Standard distributions are built in: Normal, Poisson, Binomial, Exponential, Gamma, etc.
- The sample function can be used to draw random samples from arbitrary vectors
- Setting the random number generator seed via set.seed is critical for reproducibility













