



definiendo estados:

$$U = V_0 \quad x_1 = \theta_1, \quad x_2 = \dot{x}_1, \quad x_3 = \theta_2, \quad x_4 = \dot{x}_3$$

$$\begin{aligned} F_{k1} &= k_1 x_1 & F_{b1} &= b_1 x_2 & F_{k3} &= J_1 x_2 \\ F_{k2} &= k_2 x_3 & F_{b2} &= b_2 x_4 & F_{k3} &= J_2 x_4 \end{aligned}$$

$$0 = J_1 x_2 + k_1 x_1 + b_1 x_2 + k_3 (x_1 - x_3)$$

$$k_3 (x_1 - x_3) = J_2 x_4 + k_2 x_3 + b_2 x_4$$

$$\dot{x}_2 = -\left(\frac{k_1}{J_1} + \frac{k_3}{J_1}\right)x_1 - \frac{b_1}{J_1}x_2 + \frac{k_3}{J_1}x_3 + \frac{U}{J_1}$$

$$\dot{x}_4 = \frac{k_3}{J_2}x_1 - \left(\frac{k_2}{J_2} + \frac{k_3}{J_2}\right)x_3 - \frac{b_2}{J_2}x_4$$

$$\vec{\dot{x}} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -\frac{k_1+k_3}{J_1} & -\frac{b_1}{J_1} & \frac{k_3}{J_1} & 0 \\ 0 & 0 & 0 & 1 \\ \frac{k_3}{J_2} & 0 & -\frac{k_2+k_3}{J_2} & -\frac{b_2}{J_2} \end{bmatrix} \vec{x} + \begin{bmatrix} 0 \\ \frac{1}{J_1} \\ 0 \\ 0 \end{bmatrix} U$$

Las salidas son \$x_1\$ y \$x_3\$

$$\vec{y} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \vec{x} + \vec{0} U$$