

Ellipse① If 2nd deg Eqn.

$$ax^2 + by^2 + 2hxy + 2gx + 2fy + c = 0$$

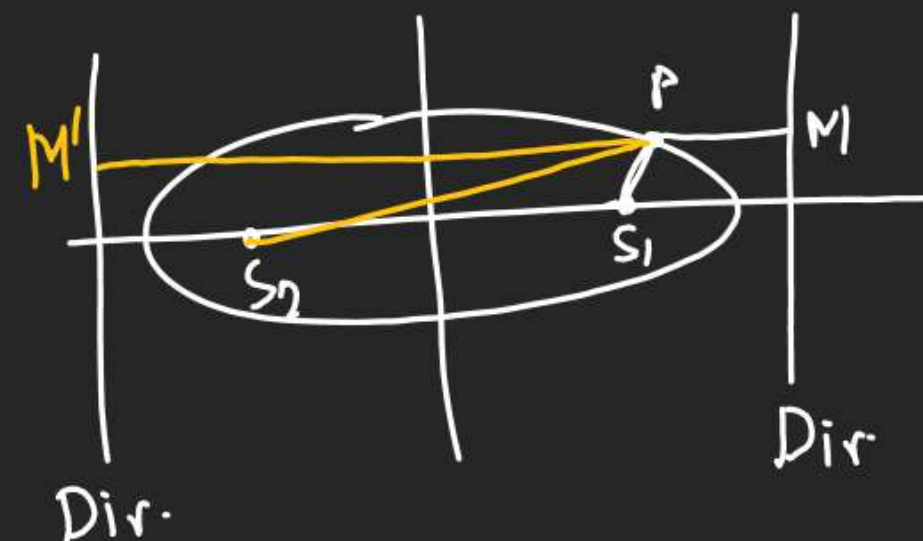
A) $\Delta \neq 0$

B) $h^2 < ab$

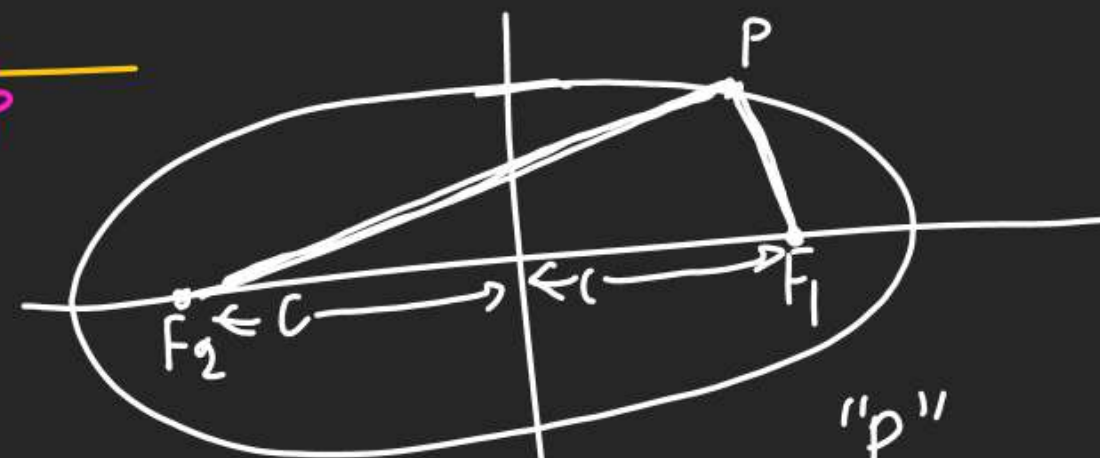
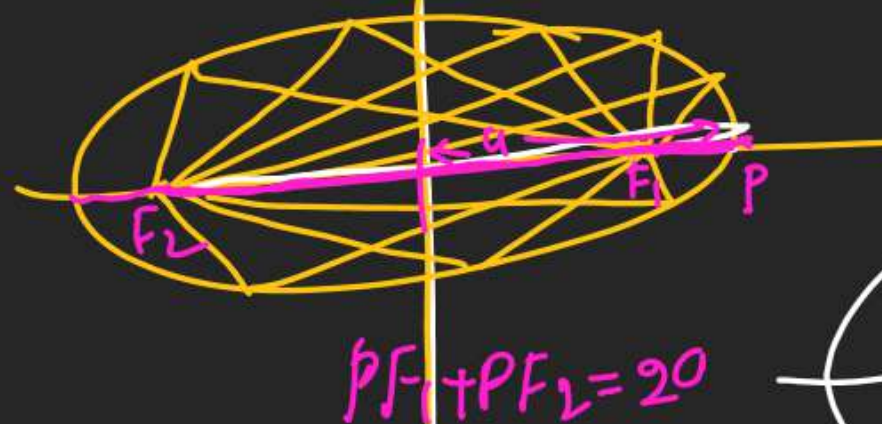
(2) By Eccentricity

$$e = \frac{SP}{PM} < 1$$

$$SP < PM$$

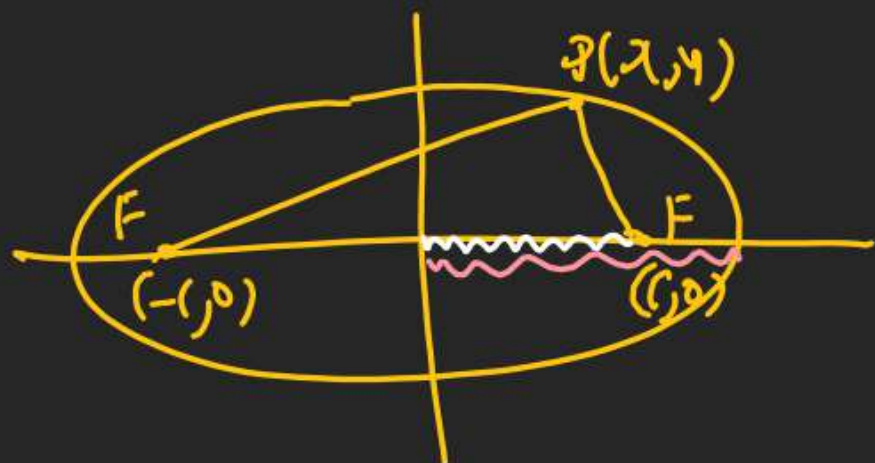
(3) For Ellipse Required condⁿ is

$$PF_1 + PF_2 = 2a \text{ \& } 2a > 2c$$



Ellipse is locus of a Ptⁿ such that
the sum of distance from 2 fixed
Pts (F₁, F₂) remains constant

(5)



$$PF_1 + PF_2 = 2a$$

$$\sqrt{(x-c)^2 + y^2} + \sqrt{(x+c)^2 + y^2} = 2a$$

After Solving

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{a^2 - c^2} = 1$$

$$\Rightarrow \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

$$R.K. \Rightarrow \underbrace{a^2 - c^2}_{c^2 = a^2 - b^2} = b^2$$

$$2a > 2c$$

$$\Rightarrow a > c$$

$$\Rightarrow a^2 > c^2$$

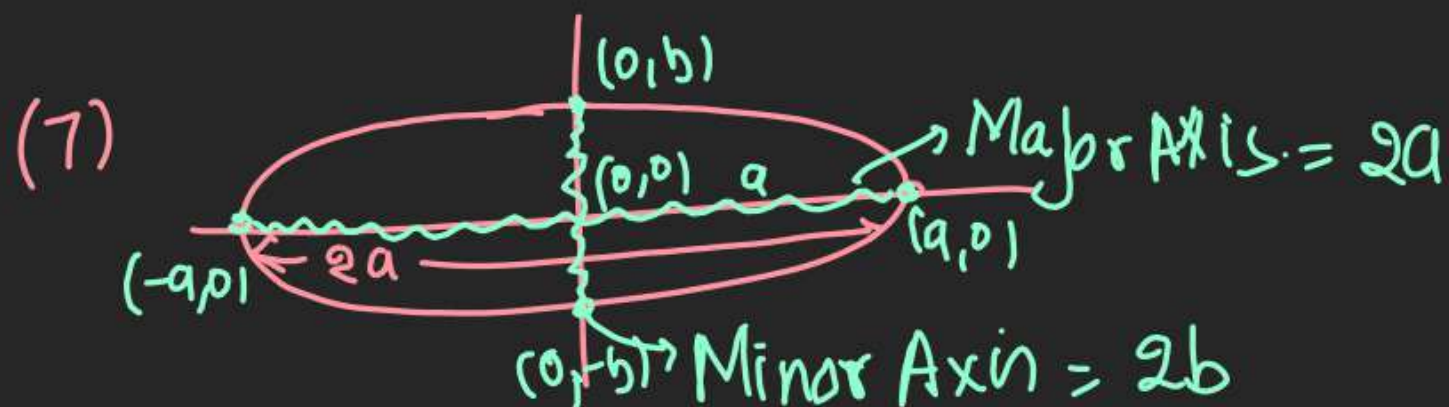
$$\Rightarrow a^2 - c^2 > 0$$

$a^2 - c^2$ will be a +ve No

any +ve No. can be sq of some No.

(6) Eccentricity1st day Learning

$$e = \frac{c}{a} = \frac{\text{dist. of Focus from Centre}}{\text{dist of vertex from Centre}}$$

(8) do we know $e = \frac{c}{a}$

$$\Rightarrow e^2 = \frac{c^2}{a^2} \Rightarrow 1 - e^2 = 1 - \frac{c^2}{a^2}$$

$$\boxed{b^2 = a^2(1 - e^2)}$$

$$1 - e^2 = \frac{b^2}{a^2}$$