

Q 6 Newly married couple are in a Bday Party. I H M W 4 ppl can be selected that

A) they form No couple

$${}^6P_4 \times {}^2C_1 \times {}^2C_1 \times {}^2C_1 \times {}^2C_1$$

B) there is exactly one couple

$${}^6C_3 \times {}^3C_1 \times {}^2C_1 \times {}^2C_1$$

(C) Atleast one couple.

$$= 0 \text{ couple} + \text{Exactly 1 couple}$$

$$= {}^6C_4 \times {}^2C_1 \times {}^2C_1 \times {}^2C_1 \times {}^2C_1 + {}^6C_3 \times {}^3C_1 \times {}^2C_1 \times {}^2C_1$$

Q No. of 7 digit No. if Sum of digit is

(1) 63.

$$9999999 \Rightarrow \frac{7!}{7!} = 1$$

(2) 62 हो जाए

$$9999998 \Rightarrow \frac{7!}{6!} = 7$$

(3) 61 हो जाए

$$9999988$$

या

$$9999997 \rightarrow \frac{7!}{6!} = 7$$

$$\frac{7!}{5!2!} = \frac{7 \cdot 6}{2} = 21$$

+

$$= 21 + 7 = 28$$

(4) Sum 60

$$9999888 = \frac{7!}{4!3!} = \frac{7 \cdot 6 \cdot 5}{6} = 35$$

or.

$$9999987 = \frac{7!}{5!} = 7 \cdot 6 = 42$$

or.

$$9999996 = \frac{7!}{6!} = 7$$

84 case

Q There are 10 Seats in Double Decker bus  
6 in lower deck & 4 in Upper. Ten passengers  
board the bus, 3 refuses to go to upper deck  
& 2 insists for upper deck. No of ways pass. can be

accommodated.

$${}^4P_2 \times {}^6P_3 \times 5!$$

Q An old man while dialing a 7 digit  
telephone No. rem. that first 4 digits  
consists of one 1's, one 2's & two 3's  
He also rem that 5<sup>th</sup> digit is either 4 or 5  
While no memory for 6<sup>th</sup> digit, he rem.  
that 7<sup>th</sup> digit is 9 minus sixth digit  
Max<sup>m</sup> No. of distinct trials he has to  
try to dial correct No.

X X X X X (X) X

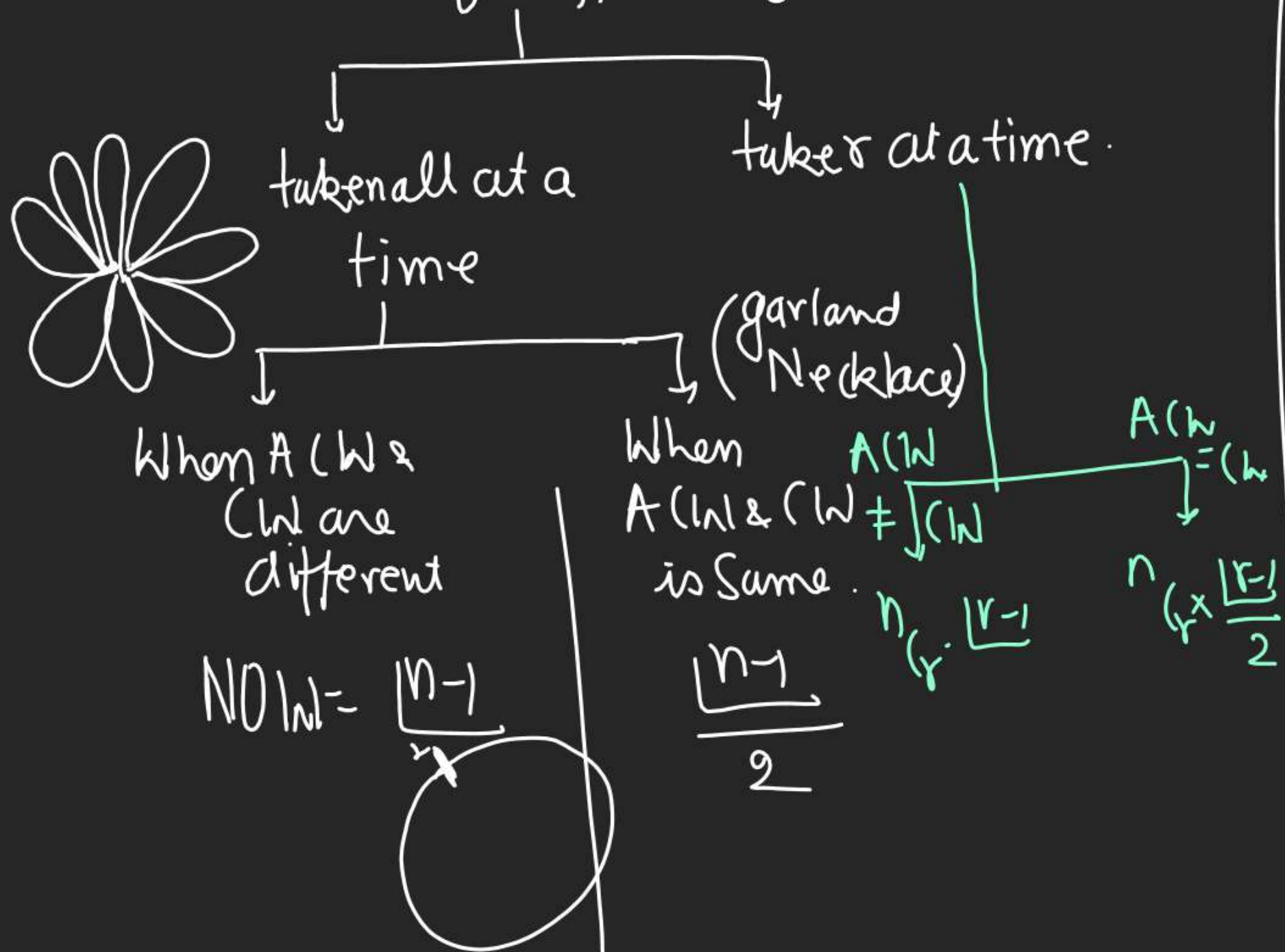
1 2 3 3 4

$$\frac{4!}{2!} \times {}^2P_1 \times {}^{10}P_1 \times 1 = 12 \times 2 \times 10 = 240$$

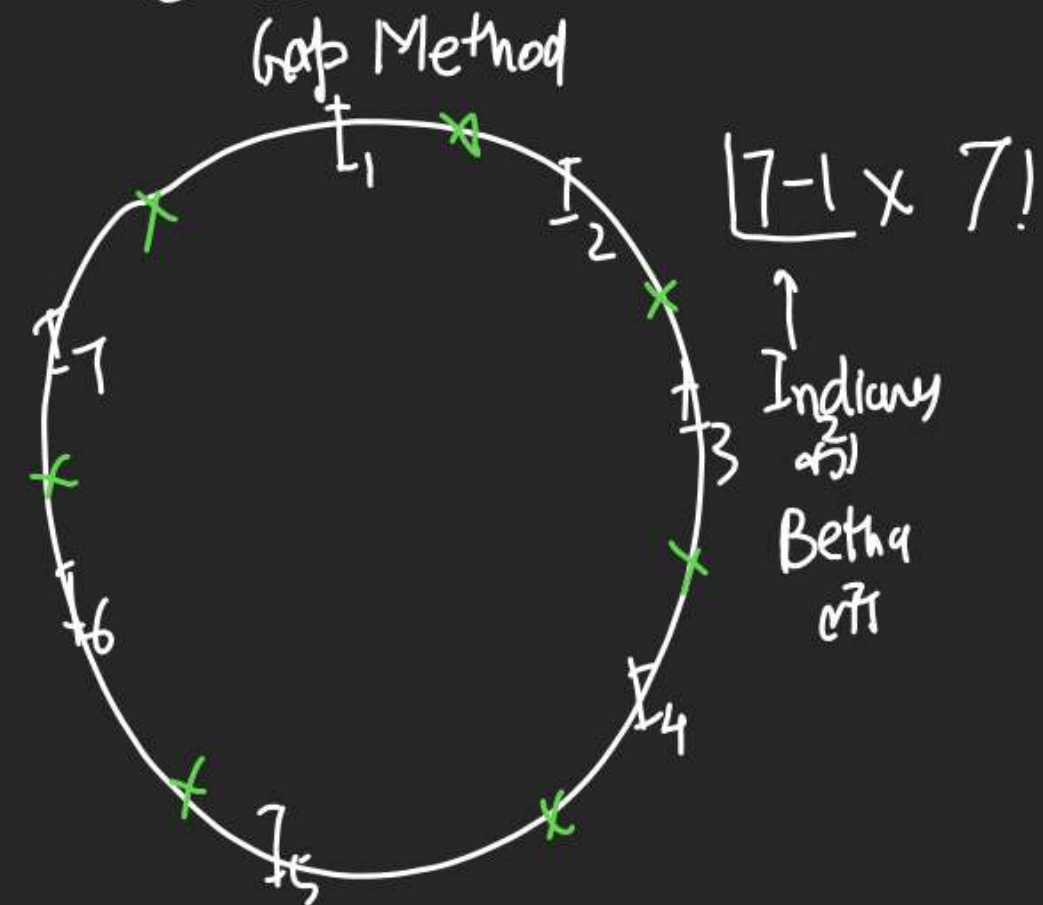
$$X_7 = 9 - X_6 = 9$$



# Circular Permutation. of $n$ different Object.



Q Now to arrange 7 American & 7 Indian ppl (can be seated on a Round table) that No 2 Americans are consecutive.



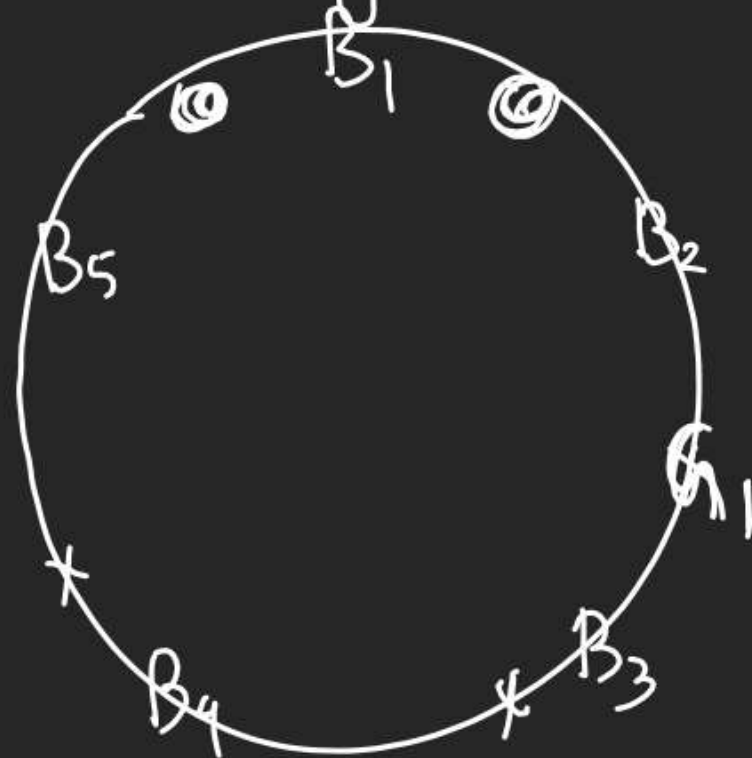
Q out of 10 flowers of different colors.  
how many different garlands can be made. if each garland consists 6 flowers of different colors.

$${}^{10}C_6 \times \frac{6-1}{2} = {}^{10}C_6 \times \frac{5}{2}$$

Q I H M N letters of word "TERRORISM"  
can be arranged in a circle?

$$\text{NOW} = \frac{9-1}{3!} = \frac{8!}{3!}$$

Q NOW 5 boys & 5 girls can be seated on a circle alternatively, if a particular Boy & Girl are Never Adjacent.



$B_1, G_1$   
~~~~~  
If da

$$\frac{15-1}{3!} \times 3! \times 1 \times 4!$$

1<sup>st</sup> Boys are Sitting |  $B_1, G_1$  are Remaining 3 places |  $\times$  Remaining 4 girls.



## ★ ★ Imp fundamental

No. of ways  $r$  ppl out of  $n$  ppl.

are not consecutive in a Line =  ${}^{n-r+1}C_r$

NO. of ways  $r$  ppl out of  $n$  ppl  
are not consecutive in a circle =  ${}^{n-r+1}C_r - {}^{n-r-1}C_{r-2}$

Q If  $n$  ppl are sitting on a circle, NOW in which  
3 ppl are selected such that no 2 of them are consecutive.

$${}^{n-3+1}C_3 - {}^{n-3-1}C_{3-2} = {}^{n-2}C_3 - {}^{n-4}C_1$$

Selection from n DIFFERENT things

(1) No of ways to select at least 1 thing out of n different things

$${}^nC_1 + {}^nC_2 + {}^nC_3 + \dots + {}^nC_n = 2^n - 1$$

(2) No of ways to select or not select at least 1 thing out of n different thing

$$\underbrace{{}^nC_0 + {}^nC_1 + {}^nC_2 + {}^nC_3 + \dots + {}^nC_n}_{= 2^n}$$

(3) NO of ways to select at least 1 object out of n Identical object.

$${}^nC_1 + {}^nC_2 + {}^nC_3 + \dots + {}^nC_n$$

$$1 + 1 + 1 + \dots + 1 = n \text{ ways.}$$

(4) No of ways to select or not select at least 1 object out of n Identical object

$$1 + \underbrace{1 + 1 + 1 + \dots + 1}_{= n+1}$$

Q  $a^3b^2$ ; 3 alike a & 2 alike b

then find

Q  $a^3b^2$ , 3 alike a & 2 alike b.

then Now to select atleast

1 object.

$$(3+1)(2+1) - 1$$

→ કો (use) જો  
Apple નો

નહોં ચુનો

← Banana નો  
નહોં ચુનો

3 apple મેં

1 નો Apple

ચુનો, નહોં ચુનો

2 Banana મેં

સે 1 નો Banana

ચુનો યો નહોં ચુનો

Q  $a^5b^4o^3$  alike

No of ways to select  
atleast one fruit.

$$(5+1)(4+1)(3+1) - 1$$

Q alike  $a^5b^4o^3$  No of ways to select atleast one  
"a"

$$(5)(4+1)(3+1) = 5 \times 5 \times 4$$

Q alike  $a^5b^4o^3$  Now to select atleast one a  
& one b.

$$= (5)(4)(3+1)$$