

$$\begin{array}{l}
 \geq 90 \checkmark \\
 \boxed{\mu \geq 80} \\
 +5 \rightarrow \left[ \frac{a+b}{c} \right] = \underbrace{\sum \frac{a+b}{c}}_{< 3} - \underbrace{\left\{ \frac{a+b}{c} \right\}}_{< 3} \\
 \text{sum} \\
 +10 \\
 < 50 \\
 \boxed{\geq 50\% \checkmark} \\
 > 6 - (1+1+1) \\
 = 3 \\
 \boxed{= 4}
 \end{array}$$

$P(x)$ 

$$\begin{array}{r} P(1) = \underline{10} \\ \underline{2} \quad 20 \\ 3 \quad 30 \end{array}$$

$$\underbrace{P(x) - 10x}_{\substack{(120 + 11 \times 10 \times 9 \times (12 - 2)) + (-80 + (-9)(-10)(-11) \\ (-8 - 2))}} = (x-1)(x-2)(x-3)(x-4)$$


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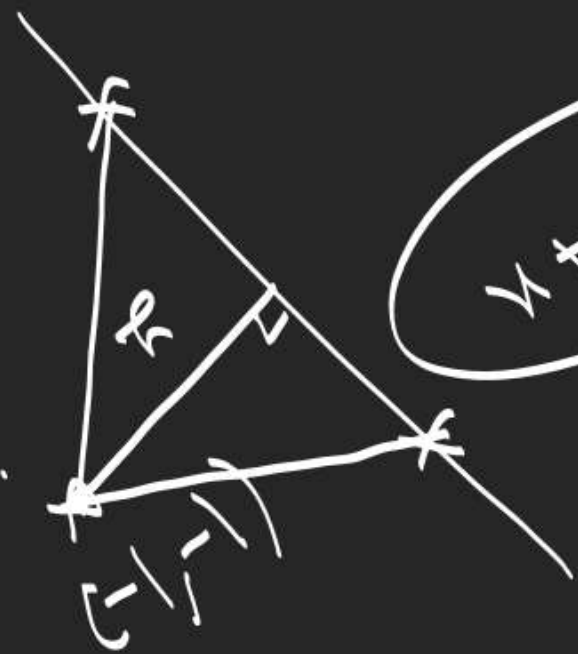
10

$$x^3 + 3xy + y^3 = 1$$

$$x^3 + y^3 + (-1)^3 = 3xy(-1)$$

$$x + y - 1 = 0 \text{ or } x = y = -1$$

$$a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$$



$$x + y = 1$$

$$\Delta = \frac{\sqrt{3}}{2}$$

$$= \left(\frac{3}{\sqrt{2}}\right)^2 \frac{1}{\sqrt{3}} =$$

$$= (a+b+c) \frac{1}{2} \left( (a-b)^2 + (b-c)^2 + (c-a)^2 \right)$$

19.

$$y = x - 2$$

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$$y = \frac{x^2 - 4}{x + 2}$$

$$= x - 2$$

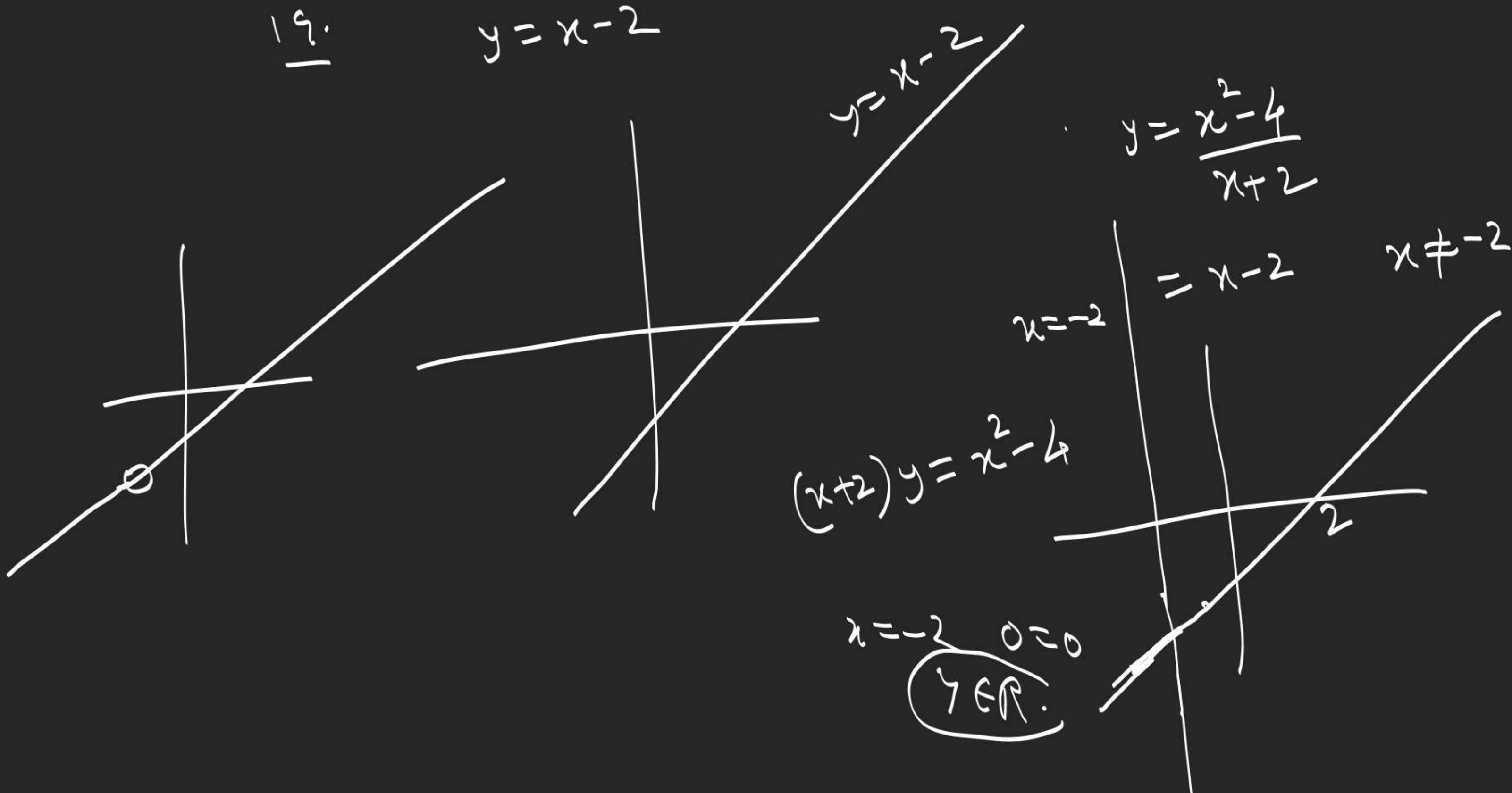
$$x \neq -2$$

$$x = -2$$

$$(x + 2)y = x^2 - 4$$

$$x = -2 \quad 0 = 0$$

$$y \in \mathbb{R}.$$

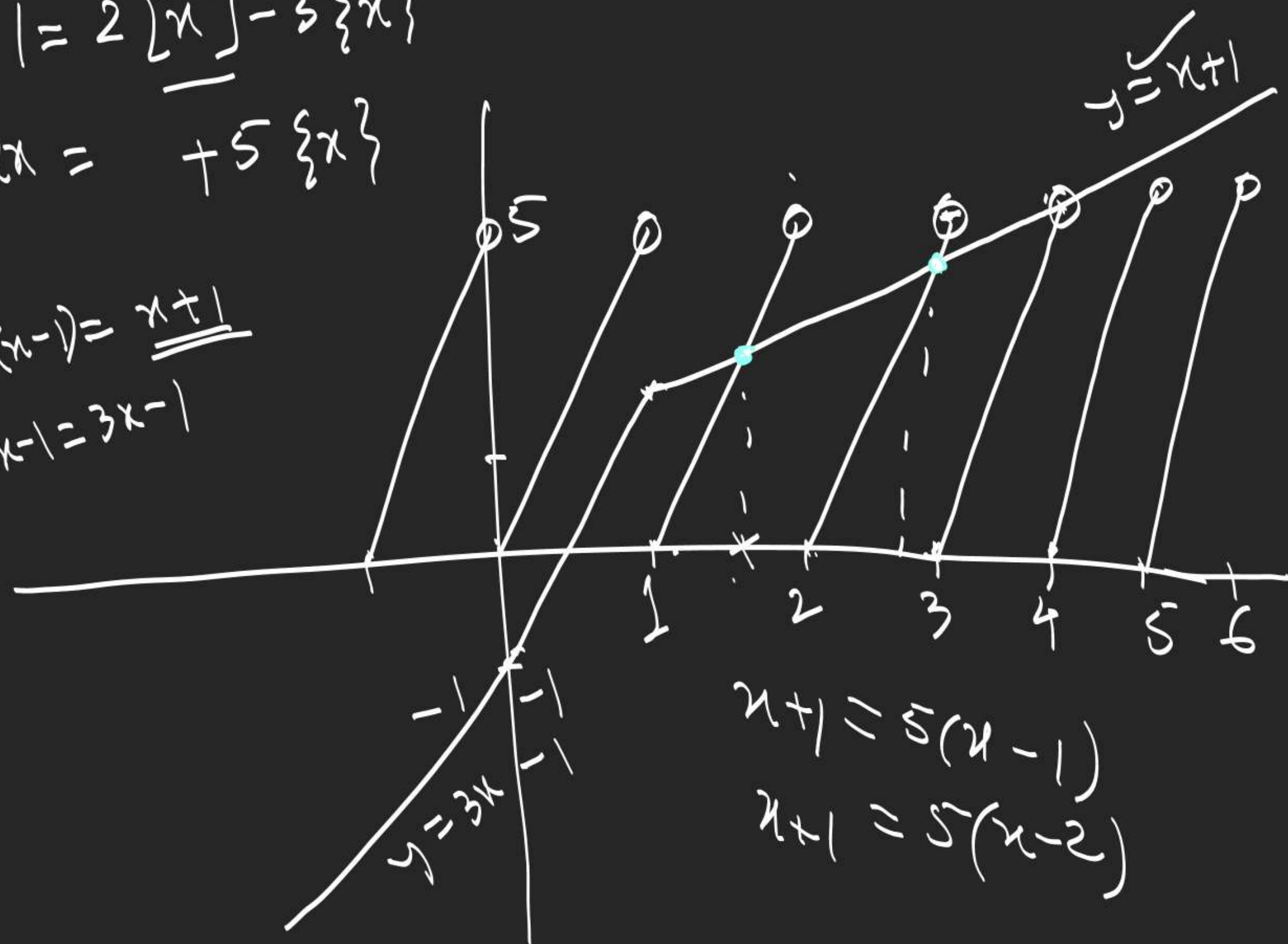




4.  $|x-1| = 2[x] - 3\{x\}$

$-|x-1| + 2x = +5\{x\}$

$x \geq 1, 2x - (x-1) = \underline{\underline{x+1}}$   
 $x < 1, 2x + x - 1 = 3x - 1$



$x+1 = 5(x-1)$

$x+1 = 5(x-2)$

$$\underline{2.} \quad \cos^{-1}x - \cos^{-1}\frac{x}{2} = \alpha$$

$$\cos\left(\cos^{-1}x - \cos^{-1}\frac{x}{2}\right) = \cos \alpha$$

$$x\left(\frac{x}{2}\right) + \sqrt{1-x^2} \sqrt{1-\frac{x^2}{4}} = \cos \alpha$$

$$\sqrt{1-x^2} \sqrt{1-\frac{x^2}{4}}$$

$$(1-x^2)\left(1-\frac{x^2}{4}\right)$$

$$= \cos \alpha - \frac{xy}{2}$$

$$= \cos^2 \alpha + \frac{x^2 y^2}{4} - \frac{xy \cos \alpha}{2}$$

$$4x^2 \quad \left(0, \frac{\pi}{2}\right)$$

$$\sin\left(\frac{\pi}{2} - 2 \tan^{-1} \cos \alpha\right) = \sin \alpha$$

$$\cos\left(2 \tan^{-1} \cos \alpha\right) = \sin \alpha$$

$$7. \tan(2 \tan^{-1} y) = \tan(\tan^{-1} x + \tan^{-1} z)$$

$$\frac{2y}{1-y^2} = \frac{2x}{1-xz}$$

$$xz = y^2$$

$$y = \frac{3x - x^3}{1 - 3x^2}$$

$$x = y = z$$

$$\tan y = 3 \tan^{-1} x$$

# Limits

$f(x)$  gets arbitrarily close to a value ' $L$ ' for all  $x$  sufficiently close to  $x_0$ , then we say that limit of  $f(x)$  is  $L$  as  $x$  approaches

$x_0$  . i.e.

$$\lim_{x \rightarrow x_0} f(x) = L.$$



$$\lim_{x \rightarrow x_0} f(x)$$



$[2, 2.001]$

rational num arbitrarily close to 2

$x=2$

$\delta$   
 $\epsilon$



$$\lim_{x \rightarrow x_0} f(x)$$

$$(x_0 - \delta, x_0) \cup (x_0, x_0 + \delta)$$

value  $f(x)$  tend to attain  
for all  $x$  close to  $-2$ .

$$f(x) = \frac{x^2 - 4}{x + 2}$$

$$= x - 2 \quad x \neq -2$$

$$\lim_{x \rightarrow -2} f(x) = -4$$

$$x \rightarrow -2$$

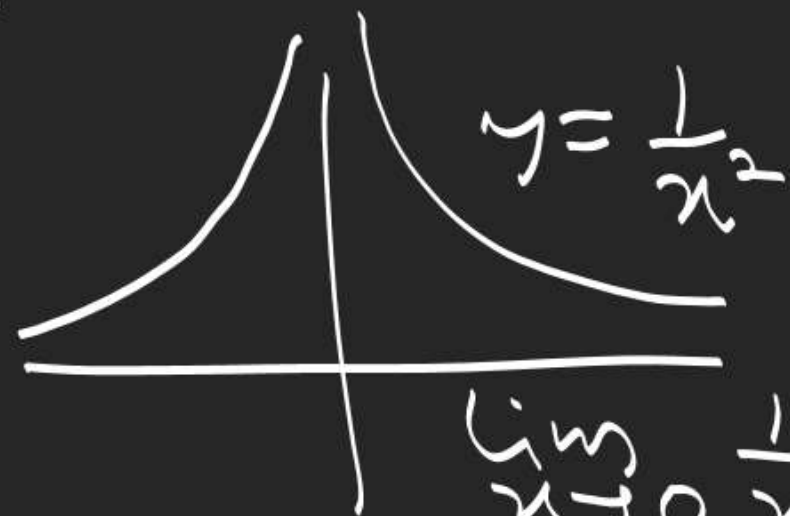
$$x \neq -2 \checkmark$$

$$(-2, -4)$$

$$-2$$

$$2$$

$$\text{Left hand limit} = \text{LHL} = \lim_{x \rightarrow x_0^-} f(x)$$



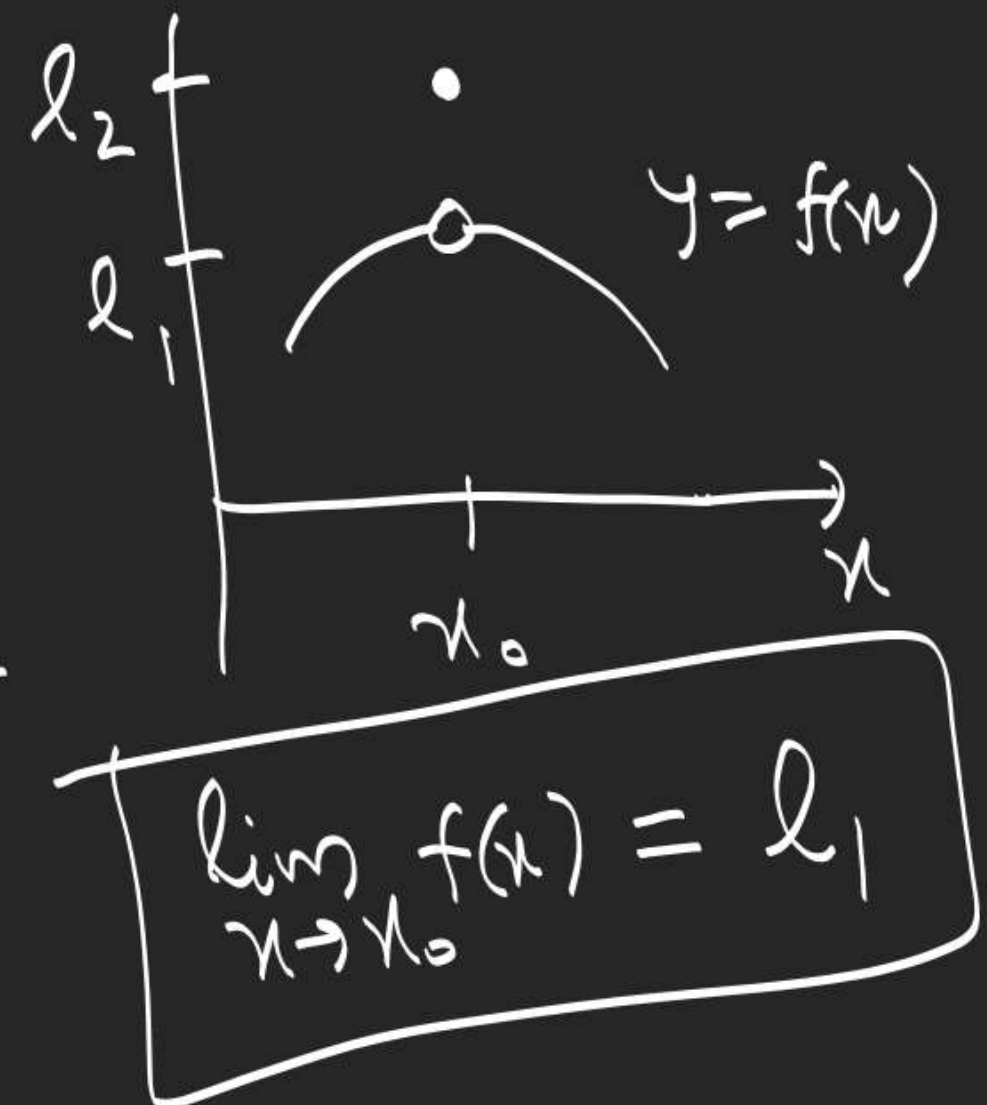
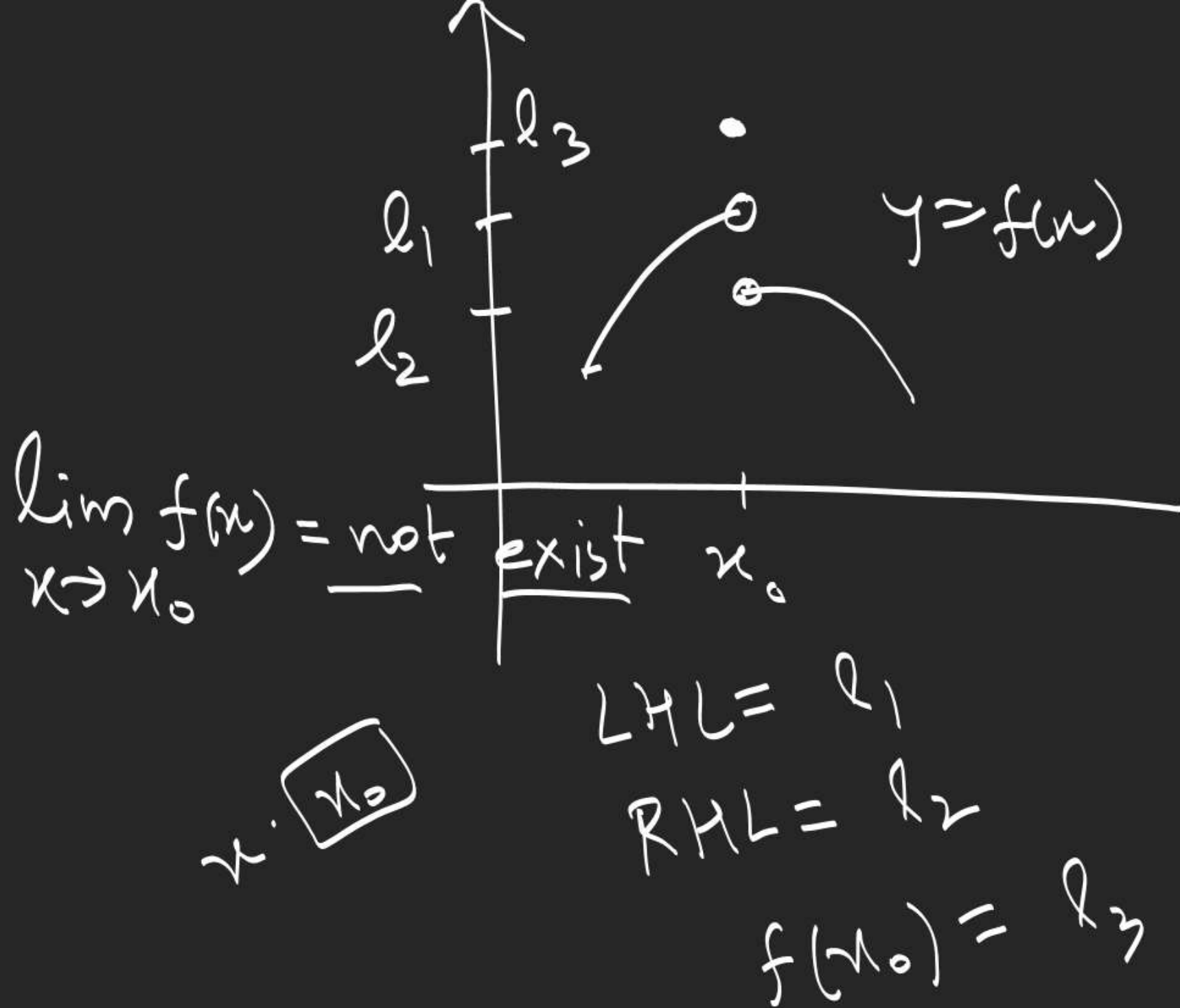
$$= \lim_{h \rightarrow 0} f(x_0 - h), \quad h > 0$$

$$\lim_{x \rightarrow 0} \frac{1}{x^2} = \infty \quad \text{not exist.}$$

$$\text{Right hand limit} = \text{RHL} = \lim_{x \rightarrow x_0^+} f(x) = \lim_{h \rightarrow 0} f(x_0 + h)$$

$$\left( \lim_{x \rightarrow x_0} f(x) \right), \text{ exist } \vee \text{ LHL} = \text{RHL} = \text{finite} = L$$

$$\Rightarrow \lim_{x \rightarrow x_0} f(x) = L$$





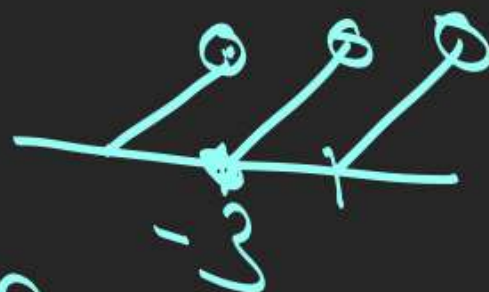
$$\boxed{\varepsilon x - \Pi u}$$

not exist

$$\lim_{x \rightarrow 0} x^3 = 0$$

$$\lim_{x \rightarrow -3} (x^3)$$

$$LHL = 1$$

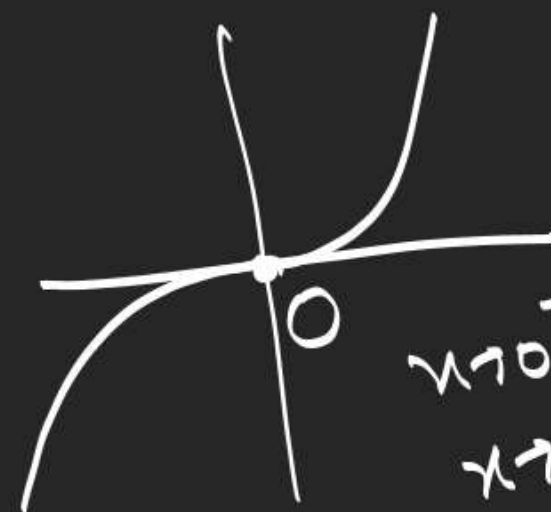


$$RHL = 0$$

$$\varepsilon - \delta = FPF$$

$$\lim_{x \rightarrow 0} \tan^{-1} \frac{1}{x}$$

not exist



$$x \rightarrow 0^-, \frac{1}{x} \rightarrow -\infty$$

$$x \rightarrow 0^+, \frac{1}{x} \rightarrow \infty$$

$$LHL = \lim_{x \rightarrow 0^-} \tan^{-1} \left( \frac{1}{x} \right) = -\frac{\pi}{2}$$

$$RHL = \lim_{x \rightarrow 0^+} \tan^{-1} \left( \frac{1}{x} \right) = \frac{\pi}{2}$$

