

# FRICTION

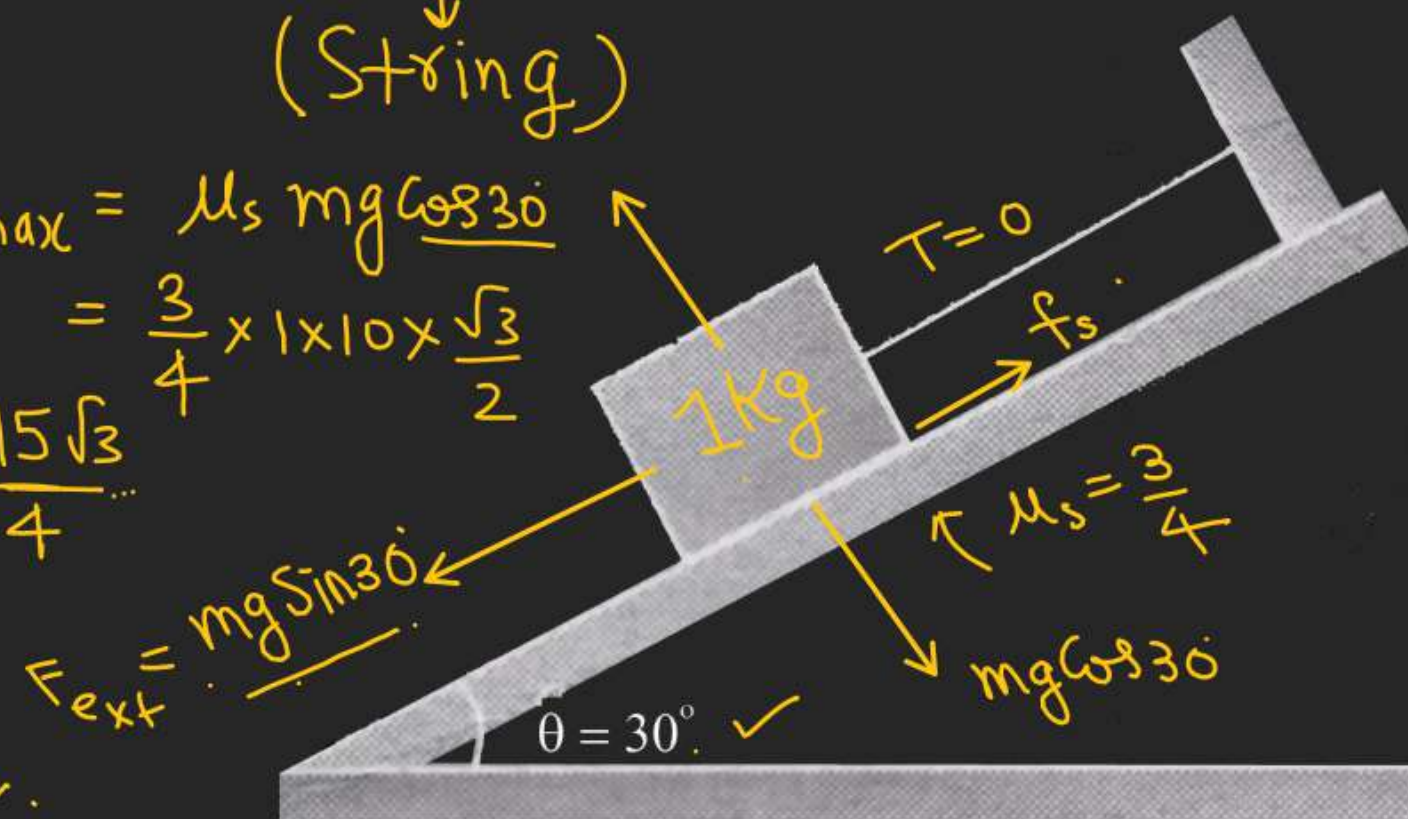
**Q.1** A block of mass 1 kg is placed on a rough inclined plane at angle  $\theta = 45^\circ$  ~~will~~ <sup>30°</sup> ~~with~~ horizontal. The block is connected with a string as shown in Fig. If  $\mu_s = 3/4$ , find the tension in string.

$$F_{\text{ext}} = mg \sin 30^\circ = 1 \times 10 \times \frac{1}{2} = \underline{\underline{5\text{N}}}$$

$$\underline{F_{\text{ext}}} < \underline{(f_s)_{\text{max}}}$$

$$\underline{\underline{f_s}} = F_{\text{ext}} = \underline{\underline{5\text{N}}} \checkmark$$

$$\begin{aligned} (f_s)_{\text{max}} &= \mu_s mg \cos 30^\circ \\ &= \frac{3}{4} \times 1 \times 10 \times \frac{\sqrt{3}}{2} \\ &= \frac{15\sqrt{3}}{4} \end{aligned}$$



# FRICTION

**Q.3** Two blocks M and m are arranged as shown in Fig. If  $M = 50 \text{ kg}$ , then determine the minimum and maximum values of mass of block m to keep the heavy block M stationary.

Sol<sup>n</sup> -

$$(f_s)_{\max} = \mu_s N$$

$$= 0.60 \times 400$$

$$= \underline{\underline{240 \text{ N}}}$$

Minimum

$$N = 50 \times 10 \times \frac{4}{5}$$

$$N = 400 \text{ Newton} \checkmark$$

$$50g \sin 37^\circ = 50 \times 10 \times \frac{3}{5}$$

$$= 50 \times 6$$

$$= \underline{\underline{300 \text{ Newton}}}$$

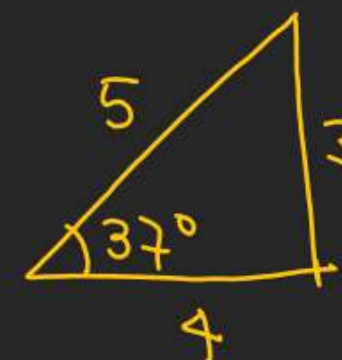
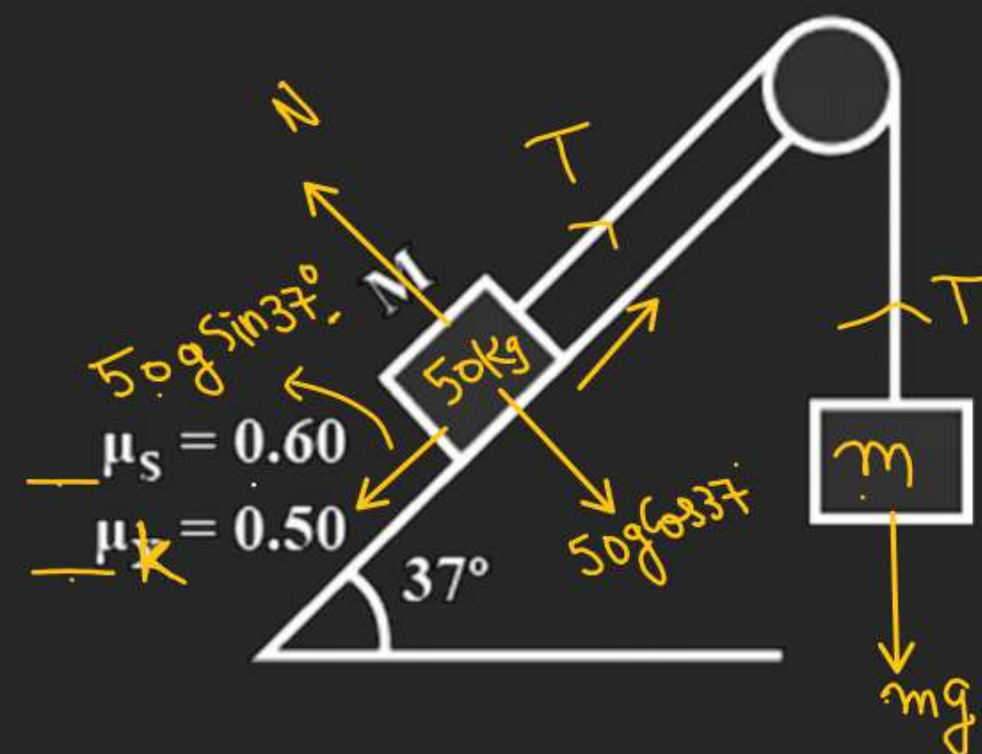
For block not to slide.

$$300 = 240 + T$$

$$mg = T = 60 \text{ N}$$

$$m = 6 \text{ kg} \checkmark$$

(minimum value)



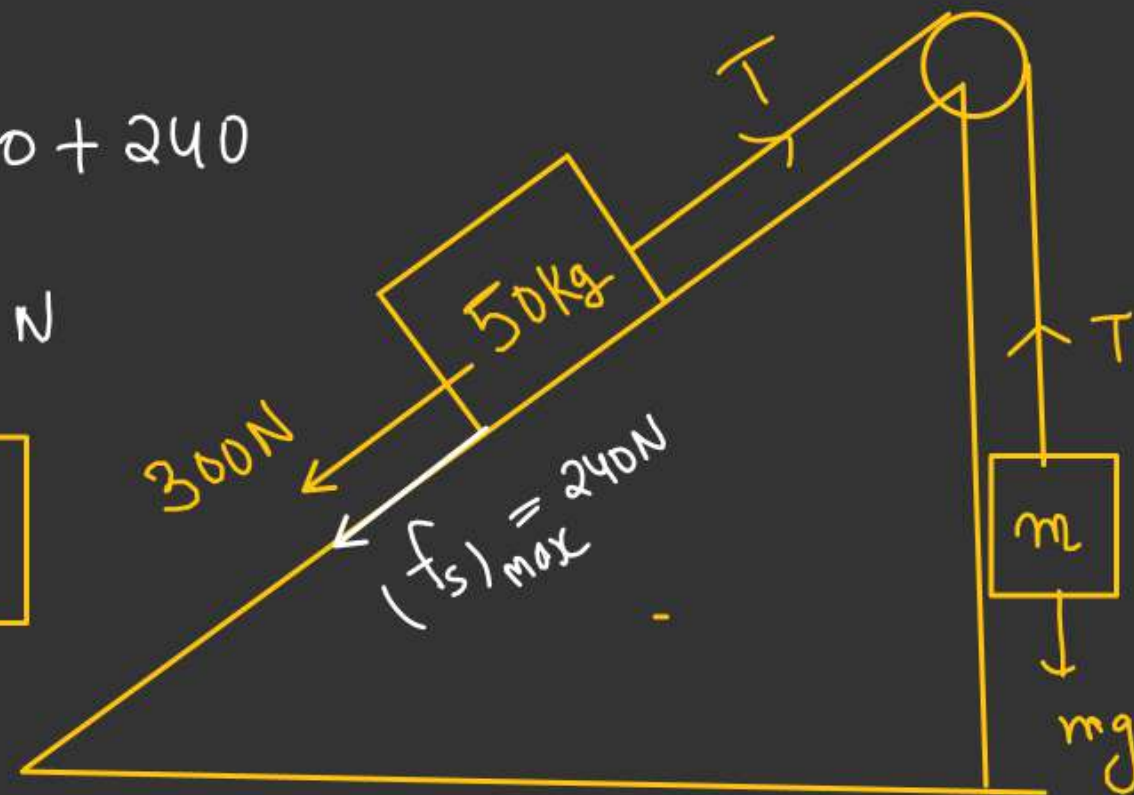


For  $m \rightarrow$  maximum

$$mg = 300 + 240$$

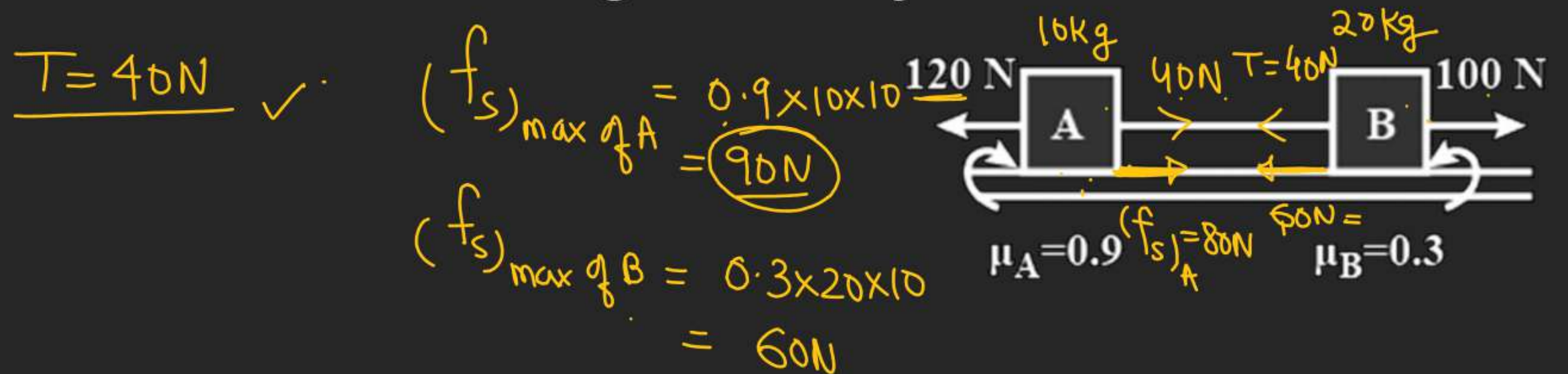
$$mg = 540 \text{ N}$$

$$m = 54 \text{ Kg}$$



# FRICTION

**Q.4** Two blocks A and B of mass  $m_A = 10 \text{ kg}$  and  $m_B = 20 \text{ kg}$  are placed on rough horizontal surface. The blocks are connected with a string. If the coefficient of friction between block A and ground is  $\mu_A = 0.9$  and between block B and ground is  $\mu_B = 0.3$ , find Fig. the tension in the string in situation as shown in Fig. Forces 120 N and 100 N start acting when the system is at rest?

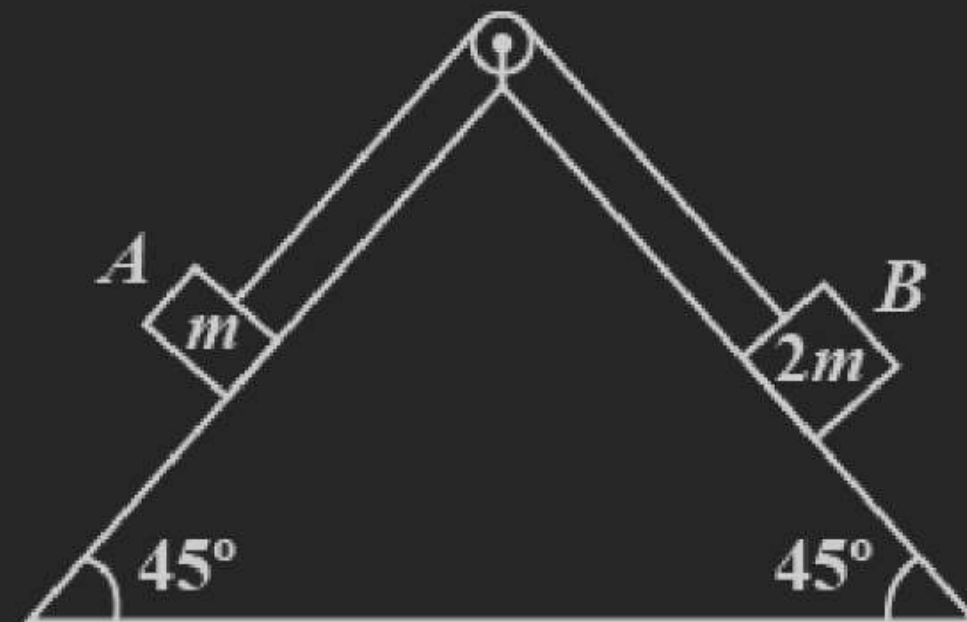


# FRICTION

H.W.

**Q.5** Block A of mass  $m$  and block B of mass  $2m$  are placed on a fixed triangular wedge by means of a light and inextensible string and a frictionless pulley as shown in Fig. The wedge is inclined at  $45^\circ$  to the horizontal on both sides. The coefficient of friction between the block A and the wedge is  $2/3$  and that between the block B and the wedge is  $1/3$ . If the system of A and B is released from rest, then find,

- the acceleration of A
- tension in the string
- the magnitude and direction of the frictional force acting on A

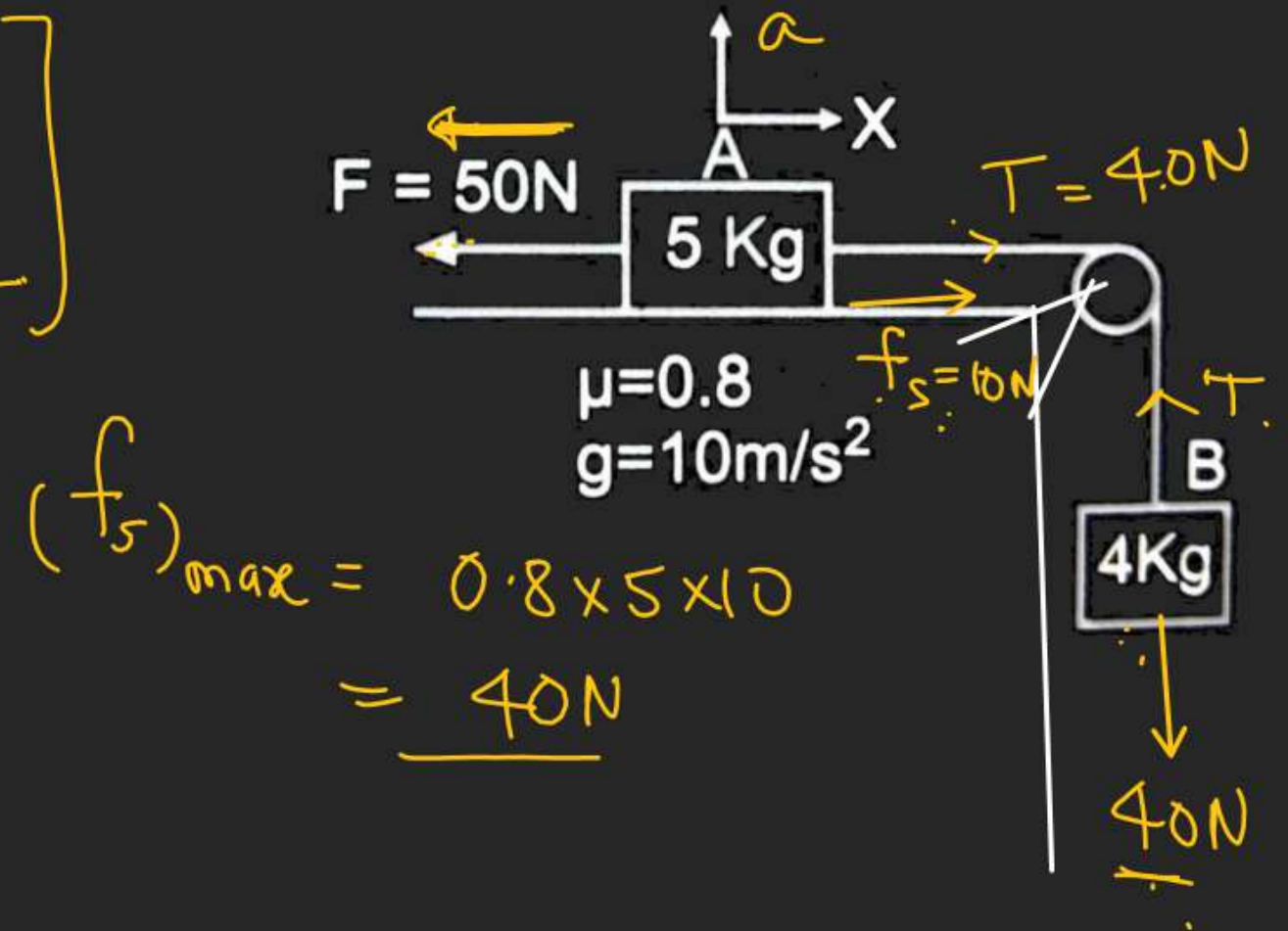




# FRICTION

**Q.1** Find the acceleration of the block and magnitude and direction of frictional force between block A and table, if block A is pulled towards left with a force of 50 N.

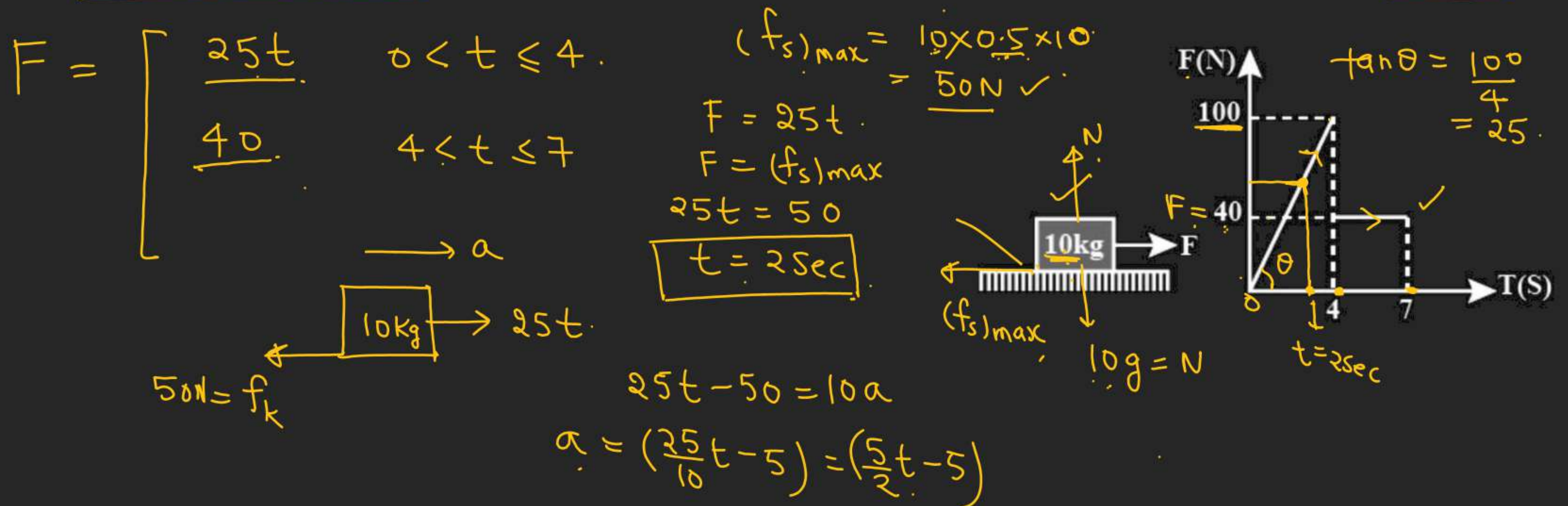
$$\left[ \begin{array}{l} a = 0 \\ f_s = 10 \text{ N} \end{array} \right]$$



$$\begin{aligned} (f_s)_{\max} &= 0.8 \times 5 \times 10 \\ &= \underline{40 \text{ N}} \end{aligned}$$

# FRICTION

**Q.2** The 10 kg block is resting on the horizontal surface when the force 'F' is applied to it for 7 second. The variation of 'F' with time is shown. Calculate the maximum velocity reached by the block and the total time 't' during which the block is in motion. The coefficient of static and kinetic friction are both 0.50.





$$0 < t \leq 4 \text{ sec}$$

$$a = \frac{5}{2}t - 5$$

$$\frac{dv}{dt} = \left(\frac{5}{2}t - 5\right)$$

$$\int_0^v dv = \int_2^4 \left(\frac{5}{2}t - 5\right) dt$$

$$v = \frac{5}{2} \int_2^4 t dt - 5 \int_2^4 dt$$

$$v = \frac{5}{2} \left[ \frac{t^2}{2} \right]_2^4 - 5 [t]_2^4$$

$$v = \frac{5}{2} (16 - 4) - 5(4 - 2)$$

$$v = (5 \times 3 - 10) = \underline{5 \text{ m/s}}$$

M-2

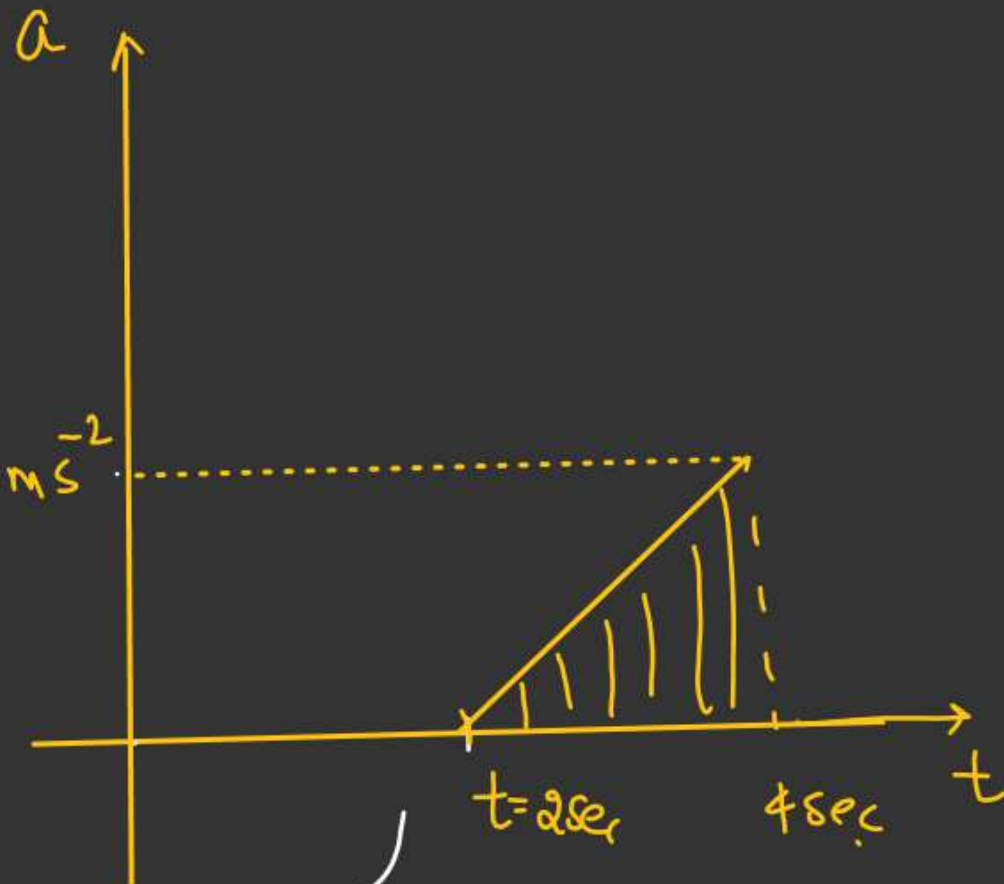
Area of trapezium

$$= \Delta V$$

$$= v - 0$$

$$\frac{1}{2} [5 + 10] \times 2 = \underline{v}$$

$$5 \text{ m/s}^2$$



$$\Delta V = \frac{1}{2} \times 2 \times 5$$

Area under  
a vs t

$$\underline{\Delta V = 5 \text{ m/s}^2}$$



# FRICTION

Q.6 What is the maximum value of the force  $F$  such that the block shown in the arrangement, does not move ~~question~~:

(a) 20 N

(b) 10 N

(c) 12 N

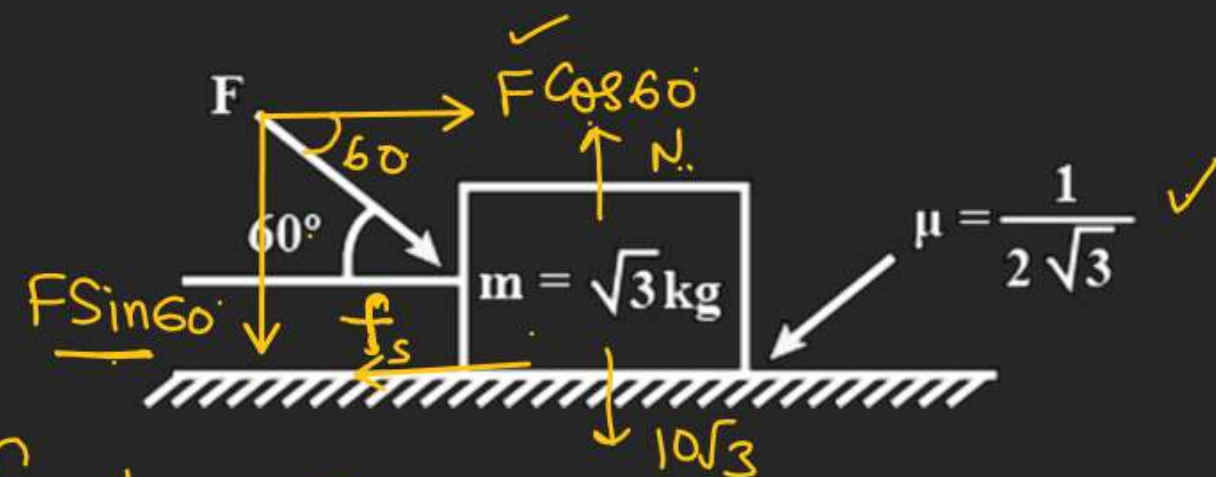
(d) 15 N

For block not to move.

$$F \cos 60^\circ = f_s$$

$$\frac{F}{2} = f_s$$

$$\underline{F_{\max} = 20 \text{ N}}$$



$$(f_s) \leq (f_s)_{\max}$$

$$\frac{F}{2} \leq \frac{1}{2\sqrt{3}} \left[ 10\sqrt{3} + \frac{F\sqrt{3}}{2} \right]$$

$$\frac{F}{2} \leq 5 + \frac{F}{4}$$

$$\frac{F}{4} \leq 5$$

$$\underline{F \leq 20 \text{ N}}$$