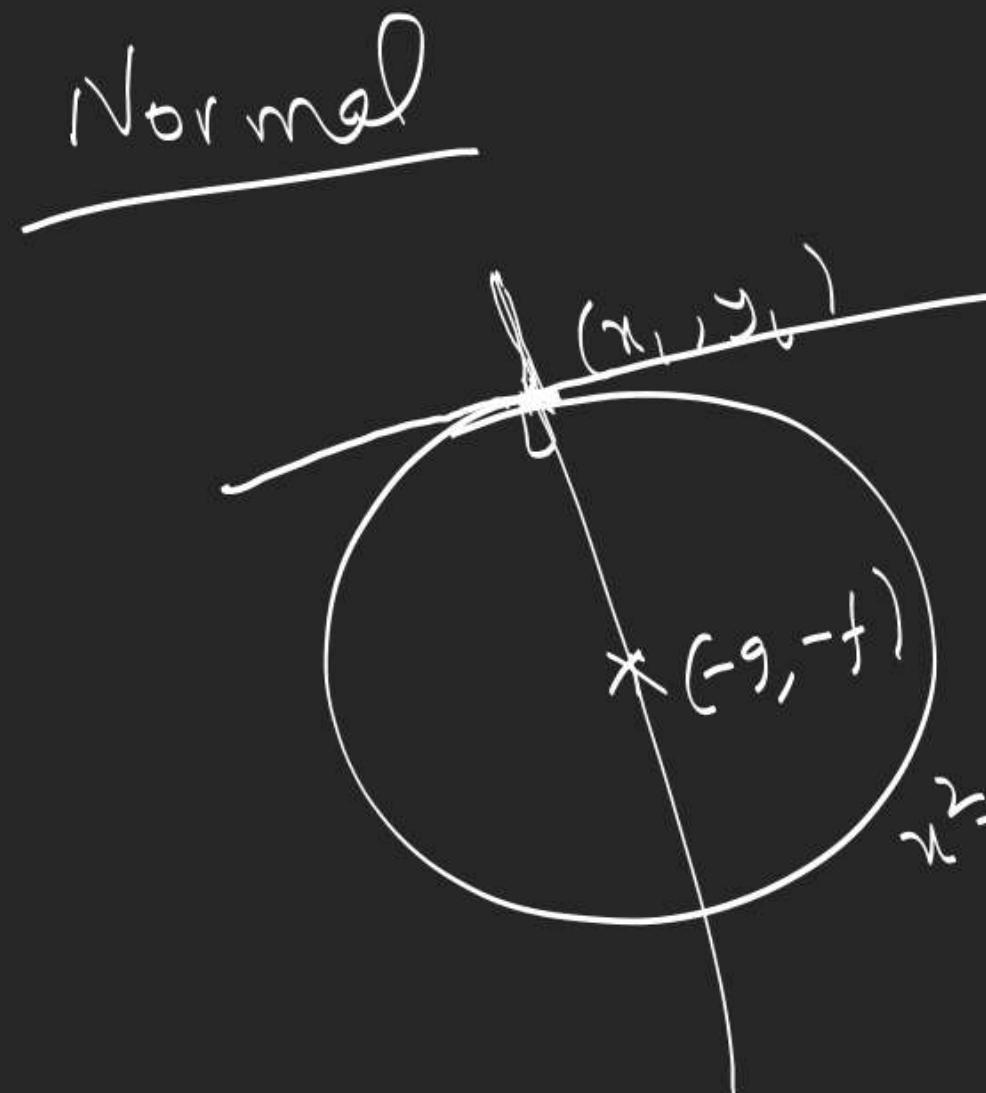


$$\begin{aligned}
 & -\frac{x_1+g}{y_1+f} (x-x_1) = y-y_1 \\
 & -x_1x + x^2 - gx + gy_1 = yy_1 - y^2 + fy - fy_1 \\
 & xx_1 + yy_1 + gy + fy = x_1^2 + y_1^2 + gx_1 + fy_1 \\
 & xx_1 + yy_1 + g(x+x_1) + f(y+y_1) + c = x_1^2 + y_1^2 + 2gx_1 + 2fy_1 + c \\
 & = x_1^2 + y_1^2 + 2gx_1 + 2fy_1 + c
 \end{aligned}$$

$$\begin{aligned}
 & xx_1 + yy_1 + g(x+x_1) + f(y+y_1) + c = 0 \\
 & = T
 \end{aligned}$$

$T=0$



$$x^2 + y^2 + 2gx + 2fy + c = 0$$
$$y - y_1 = \left(\frac{y_1 + f}{x_1 + g} \right) (x - x_1)$$

Chord whose midpoint is given

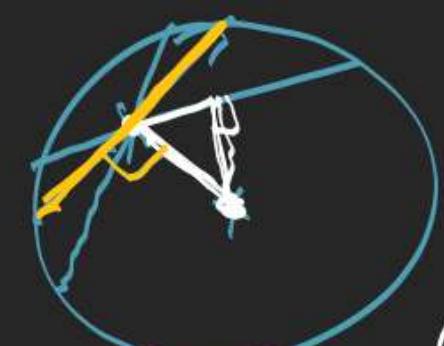
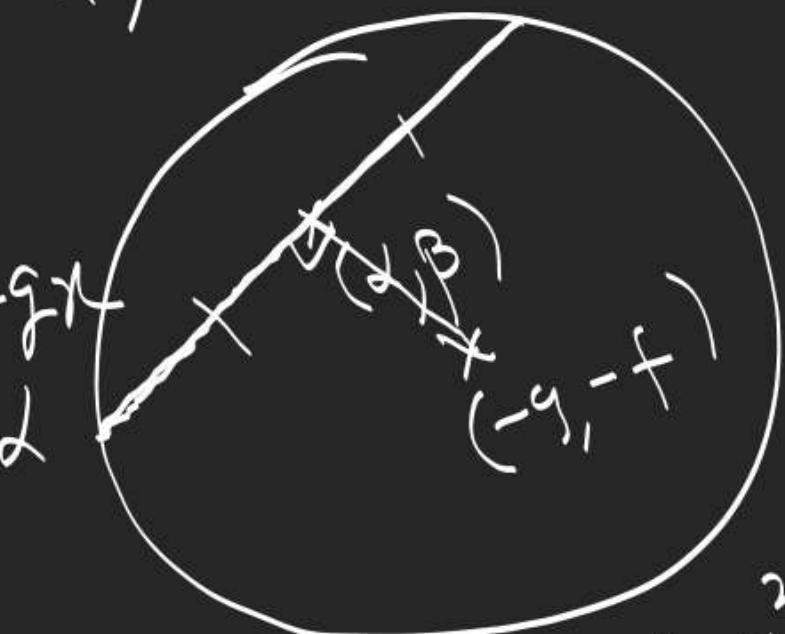


passing thru (α, β) situated

at max. distance from centre

$$\gamma - \beta = - \left(\frac{\alpha + \beta}{\beta - f} \right) (\chi - \alpha)$$

$$\gamma \beta - \beta^2 + fy - \beta f = - \alpha \chi + \alpha^2 - g \chi + g \alpha$$



Shortest chord
thru (α, β)

$$\chi^2 + y^2 + 2gx + 2fy + c = 0$$

$$T = S_1$$

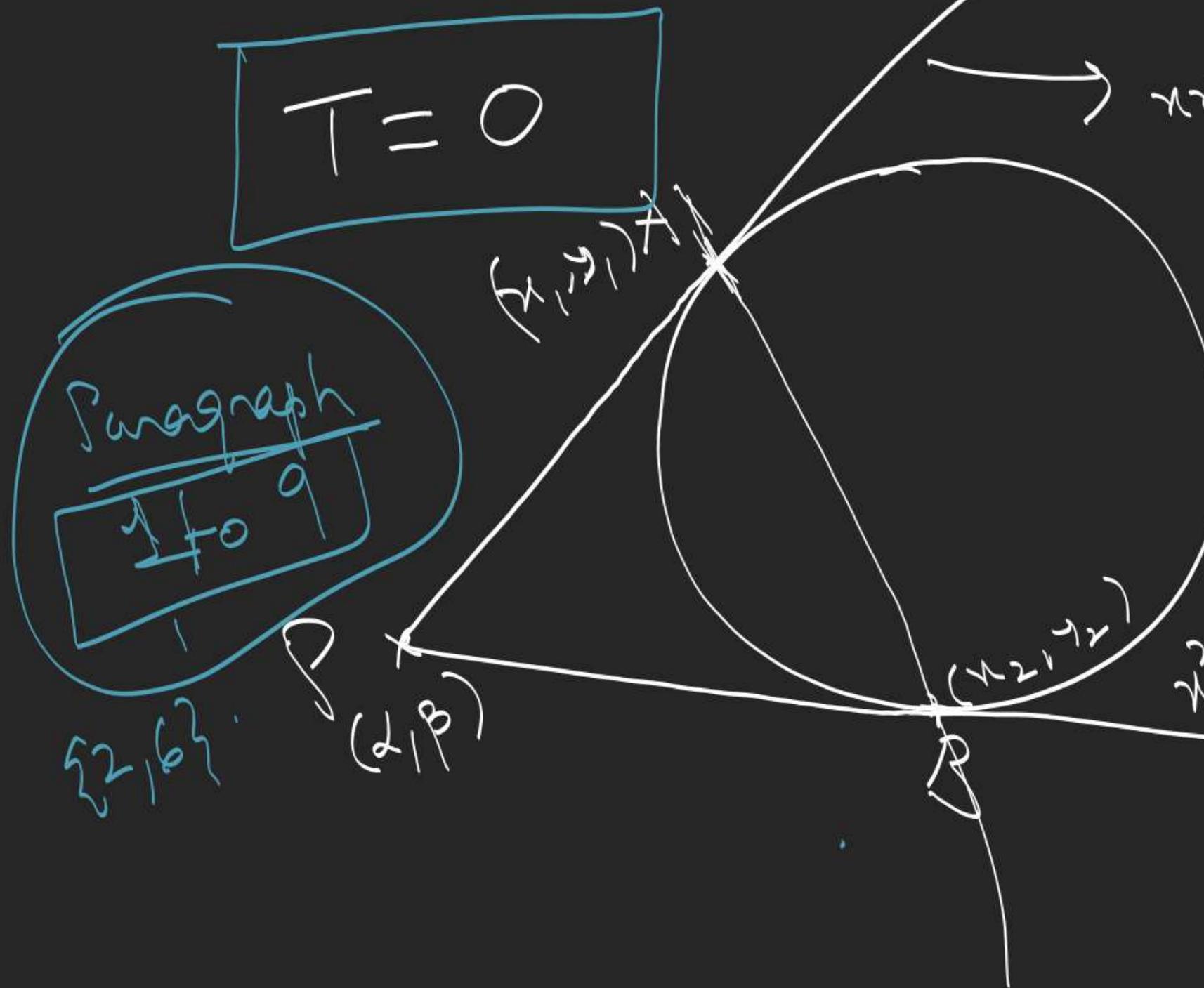
$$\alpha \chi + \beta y + g(\chi + \alpha) + f(y + \beta) = \alpha^2 + \beta^2 + 2g\alpha + 2f\beta + c$$

$$\alpha \chi + \beta y + g(\chi + \alpha) + f(y + \beta) - \alpha^2 - \beta^2 - 2g\alpha - 2f\beta - c$$



$$2\sqrt{r^2 - p^2} = l$$

Chord of Contact of a point w.r.t Circle



$$\alpha x_1 + \beta y_1 + g(x_1 + \alpha) + f(y_1 + \beta) + c = 0$$

$$\alpha x_2 + \beta y_2 + g(x_2 + \alpha) + f(y_2 + \beta) + c = 0$$

$$\alpha x_2 + \beta y_2 + g(x_2 + \alpha) + f(y_2 + \beta) + c = 0$$

$$\alpha^2 x_1^2 + 2\alpha x_1 + 2\alpha y_1 + 2f y_1 + g(x_1 + \alpha) + f(y_1 + \beta) + c = 0$$

$$\alpha^2 x_2^2 + 2\alpha x_2 + 2\alpha y_2 + 2f y_2 + g(x_2 + \alpha) + f(y_2 + \beta) + c = 0$$

$$\alpha^2 x_1^2 + 2\alpha x_1 + 2\alpha y_1 + 2f y_1 + g(x_1 + \alpha) + f(y_1 + \beta) + c = 0$$

Chord of Contact