

DPP4

$$9) \int (\sec x \cdot \sqrt{\sin x} \cdot \csc x)$$

$$\int (-\csc^2 x) \sqrt{\sin x} \cdot \csc x$$

$$\sin x = t$$

$$6) \log(x + \sqrt{x^2+1}) - t$$

Q9) Hold

$$19) \int \sqrt{\sec x - 1} \, dx$$

$$\int \sqrt{1 - \frac{1}{(\sec x)^2}} \cdot d\sec x = \int \frac{\sqrt{2 \tan^2 \frac{x}{2}}}{\sqrt{2 \sec^2 \frac{x}{2} - 1}} \cdot d\sec x = \int \frac{\tan \frac{x}{2}}{\sqrt{(\sqrt{2} \sec \frac{x}{2})^2 - 1^2}} \cdot \sqrt{2} \sec \frac{x}{2} = \int \frac{d\sec x}{\sqrt{\sec^2 x - 1^2}} = 2 \int \frac{dt}{\sqrt{t^2 - 1^2}}$$

$$(16)^* \int \frac{\sqrt{\tan x} \cdot d\tan x}{\sin x \cdot \csc x}$$

$$\int \frac{\sqrt{\sin x}}{\sqrt{\csc x}} \times \frac{1}{\csc x \cdot \csc x}$$

$$\int \frac{d\tan x}{(\tan x)^{1/2} (\csc x)^{3/2}} \cdot \frac{(\csc x)^{1/2}}{(\csc x)^{1/2}} \quad \frac{1}{2} + \frac{3}{2} = 2$$

$\tan x = t$
 $\sec^2 x \, dx = dt$

$$2\int t \, dt \Leftrightarrow \int \frac{\sec^2 x \cdot d\tan x}{(\tan x)^{1/2}} \quad \tan x = t$$

$$\int \frac{d\tan x}{\sqrt{\tan^2 x - 1^2}} = 2 \int \frac{dt}{\sqrt{t^2 - 1^2}} \quad \int \frac{dx}{\sqrt{\frac{1}{2} \tan^2 \frac{x}{2} \times \frac{1}{2}}} = dt$$

$$Q_{22} \int \frac{dx}{\sin^{3/2}x \cdot \csc^{5/2}x} \quad \frac{3}{2} + \frac{5}{2} = 4$$

Even.

$$\int \frac{dx}{\sin^{3/2}x \cdot \csc^{5/2}x \cdot \csc^{3/2}x}$$

$\csc^{3/2}x$

$$\int \frac{\sec^2 x \cdot \sec^2 x \cdot dx}{(\tan x)^{3/2}} = \int \frac{(1 + \tan^2 x) \cdot \sec^2 x}{(\tan x)^{3/2}}$$

$$\int \frac{(1+t^2) dt}{t^{3/2}} = \int t^{-3/2} + t^{1/2} \cdot dt$$

$$(13) \quad x + \tan x = t$$

$$1 + \frac{1}{1+x^2} \cdot dx = dt$$

$$\frac{x^2+1}{x^2+1} \cdot dx = dt$$

$$Q_{26} \int \sqrt{\frac{1-\sqrt{x}}{1+\sqrt{x}}} \cdot dx$$

30, 31, 32 hold

$$\int \frac{1-\sqrt{x}}{1-(\sqrt{x})^2} \cdot dx$$

$$\int \frac{1-\sqrt{x}}{1-x} \cdot dx$$

$$\int \frac{1}{1-x} \cdot dx - \int \frac{\sqrt{x} \cdot dx}{1-(\sqrt{x})^2}$$

$$\int \frac{1}{x} \cdot dx = \ln|x|$$

$$\int \frac{1}{x^2} \cdot dx = -\frac{1}{x}$$

$$\int \frac{1}{\sqrt{x}} = 2\sqrt{x}$$

$$\int \sqrt{x} \cdot dx = \frac{2}{3} x^{3/2}$$

$$\int \sec x \cdot dx = -\ln|\sec x|$$

$$\int a^x = \frac{a^x}{\ln a}$$

$$\int \ln x = x \ln x - x$$

$$\int \tan x = \ln|\sec x|$$

$\int (\sec x \cdot dx) = \ln \sec x + \tan x = \ln \tan(\frac{\pi}{4} + \frac{x}{2}) $	$\int (\sec^2 x) = \tan x$
$\int (\sec x \cdot \tan x) = -\csc x$	$\int (\sec x \cdot \csc x) = \sec x$
	$\int (\sec x \cdot \csc x \cdot \cot x) = -\csc x$

$$\int \frac{dx}{x^2 + a^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right| + C$$

$$\int \frac{dx}{a^2 - x^2} = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right| + C$$

$$\int \frac{dx}{\sqrt{x^2 + a^2}} = \ln |x + \sqrt{x^2 + a^2}| + C$$

$$\int \frac{dx}{\sqrt{x^2 - a^2}} = \ln |x + \sqrt{x^2 - a^2}|$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a}$$

$$\int \sqrt{x^2 + a^2} \cdot dx = \frac{x}{2} \sqrt{x^2 + a^2} + \frac{a^2}{2} \ln |x + \sqrt{x^2 + a^2}|$$

$$\int \sqrt{x^2 - a^2} \cdot dx = \frac{x}{2} \sqrt{x^2 - a^2} - \frac{a^2}{2} \ln |x + \sqrt{x^2 - a^2}|$$

$$\int \sqrt{a^2 - x^2} \cdot dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \ln |x + \sqrt{a^2 - x^2}|$$

$$\int \frac{(x^2 - 1) + \tan\left(\frac{x^2 + 1}{x}\right)}{(x^4 + 3x^2 + 1) \cdot \tan\left(\frac{x^2 + 1}{x}\right)} dx$$

Sin 2x Based Qs.

A) $\int \sin 2x \, dx$ is im Nr.

$$Q \int \frac{\sin 2x \cdot dx}{1 + 2 \sin^2 x} \quad Q \int \frac{\sin 2x \cdot dx}{3 + 4 \cos^2 x}$$

$$Q \int \frac{\sin 2x \cdot dx}{3 \sin^2 x + 4 \cos^2 x} \quad Q \int \frac{\sin 2x \cdot dx}{a^2 + b^2 \tan^2 x}$$

$$Q \int \frac{\sin 2x \cdot dx}{\sqrt{a^2 \sin^2 x + b^2 \cos^2 x}}$$

$$Q_2 \int \frac{\sin 2x \cdot dx}{3 + 4 \cos^2 x} \quad 3 + 4 \cos^2 x = t$$

$$-\frac{1}{4} \int \frac{dt}{t} \\ \Rightarrow -\frac{1}{4} \ln |t| + C$$

$$Q \leq \int \frac{\sin 2x \cdot dx}{\sqrt{a^2 \sin^2 x + b^2 \cos^2 x}}$$

$$\frac{1}{a^2 - b^2} \int \frac{dt}{\sqrt{t}}$$

$$\frac{2\sqrt{t}}{a^2 - b^2} + C$$

$$a^2 \sin^2 x + b^2 \cos^2 x = t$$

$$a^2 \sin 2x - b^2 \cos 2x = dt$$

$$\sin 2x (a^2 - b^2) \cdot dx = dt$$

$$\sin 2x \cdot dx = \frac{dt}{a^2 - b^2}$$

(B) When $\sin 2x$ is in Dr.

$$\frac{\sin 2x}{\sin 2x} \xrightarrow{\text{Remove}} 1 - (1 - \sin 2x) \leftarrow$$

$$Q_1 \int \frac{\sin x + \cos x}{9 + 16 \sin 2x} \quad Q_2 \int \frac{\cos x - \sin x}{7 - 9 \sin 2x}$$

$$Q_3 \int \frac{1}{\sin x + \cos x}$$

$$Q_4 \int \frac{\cos x - \sin x}{\sqrt{\sin 2x}}$$

$$Q_5 \int \frac{\sin x + \cos x}{\sqrt{\sin 2x}}$$

$$Q_6 \int \frac{\cos x}{\sqrt{\sin 2x}}$$

$$Q_1 \int \frac{\sin x + \cos x}{\sqrt{\sin 2x}} = \int \frac{\sin x + \cos x}{\sqrt{1 - (1 - \sin 2x)}} = \int \frac{\sin x + \cos x \cdot dx}{\sqrt{1 - (\sin x - \cos x)^2}}$$

$$= \int \frac{dt}{\sqrt{1-t^2}} = \sin^{-1} t + C \quad \begin{aligned} \sin x - \cos x &= t \\ (\cos x + \sin x)dx &= dt \end{aligned}$$

$$Q_2 \int \frac{\cos x - \sin x \cdot dx}{\sqrt{\sin x}} = \int \frac{\cos x - \sin x}{\sqrt{(1 + \sin 2x) - 1}} = \int \frac{\cos x - \sin x \cdot dx}{\sqrt{(\sin x + \cos x)^2 - 1}}$$

$$Q_3 \int \frac{dt}{\sqrt{t^2 - 1}} = \ln |t + \sqrt{t^2 - 1}| + C \quad \begin{aligned} \sin x + \cos x &= t \\ (\cos x - \sin x)dx &= dt \end{aligned}$$

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$$B Q_3 \int \frac{\cos x}{\sqrt{\sin 2x}} dx = \frac{1}{2} \int \frac{2 \cos x \cdot dx}{\sqrt{\sin 2x}} = \frac{1}{2} \int \frac{\cos x + \sin x + \cos x - \sin x}{\sqrt{\sin 2x}} dx$$

$$Q_1 \downarrow \quad Q_2 \downarrow$$

$$\int \frac{dx}{\sin x + \sec x} = \int \frac{\csc x \cdot dx}{\csc x (\csc x + 1)} = \int \frac{2 \csc x}{2 + \sin 2x} \cdot dx$$

$$= \int \frac{\csc x + \sin x}{2 + \sin 2x} + \frac{\csc x - \sin x}{2 + \sin 2x} \cdot dx$$

$$\Rightarrow \int \frac{(\csc x + \sin x) \cdot dx}{2 + 1 - (1 - \sin 2x) - 1} + \int \frac{\csc x - \sin x}{2 + (1 + \sin 2x) - 1}$$

$$\Rightarrow \int \frac{(\csc x + \sin x) \cdot dx}{3 - (\sin x - \csc x)^2} + \int \frac{\csc x - \sin x \cdot dx}{1 + (\tan x + \csc x)^2}$$

$$\Rightarrow 2 \int \frac{dt}{(1-t^2)(1+t^2)} = 2 \int \frac{3 dt}{(2-t^2)(1+t^2)}$$

$$\Rightarrow \frac{2}{3} \int \frac{(2-t^2)+(1+t^2)}{(2-t^2)(1+t^2)} dt \quad \text{Simplify Int}$$

$$\int \frac{dx}{(\csc^3 x - \sin^3 x)} = \int \frac{dx}{(\csc x - \sin x)(\csc^2 x + \sin^2 x + \sin x \csc x)}$$

$$\Rightarrow 2 \int \frac{dx}{(\csc x - \sin x)(2 + \sin 2x)}$$

$$\Rightarrow 2 \int \frac{(\csc x - \sin x) \cdot dx}{(\csc x - \sin x)^2 \cdot (2 + \sin 2x)}$$

$$\Rightarrow 2 \int \frac{(\csc x - \sin x) dx}{(1 - (\sin x + \csc x))^2 (2 + (1 + \sin 2x) - 1)}$$

$$\Rightarrow 2 \int \frac{(\csc x - \sin x) dx}{(1 - (\sin x + \csc x))^2 (2 + (1 + \sin 2x) - 1)}$$

$$\Rightarrow 2 \int \frac{(\csc x - \sin x) dx}{(1 - (\sin x + \csc x))^2 (1 + (\sin x + \csc x)^2)} \frac{(\csc x - \sin x) dx}{dx}$$

$$\int \frac{dx}{(g(x)(x+1)(\ln(x+1)-\ln x))^{10}} = \int \frac{1+x^{2007}-x^{2007}}{x(x^{2007}+1)} \int \frac{\sec^2 x \cdot dx}{\tan^4 x (1+\tan^7 x)^{4/7}}$$

$$\ln(x+1) - \ln x = t \quad \begin{aligned} &= \int \frac{1+x^{2007}}{x((1+x^{2007})^{2007})} \int \frac{x^{2007} \cdot dx}{x(x^{2007}+1)} \frac{dt}{t^4 (1+t^7)^{4/7}} \\ &\quad \text{let } \tan x = t \end{aligned}$$

$$\int \frac{(g(x)+\sin x \cdot dx)}{x(g(x)-x)} \Rightarrow |n| x^{-2007} \int \frac{dx}{t^4} \quad \text{from}$$

$$\int \frac{(g(x)+\tan x \cdot dx)}{x^2(g(x)-1)} \quad \frac{g(x)-1}{x} = t$$

$$\int \frac{dt}{t^8 (1+\frac{1}{t^7})^{4/7}} \quad \begin{aligned} &\text{let} \\ &1 + \frac{1}{t^7} = z \end{aligned}$$

$$-\frac{1}{7} \int \frac{dz}{z^{4/7}}$$

$$-\frac{1}{7} \cdot \frac{dt}{t^8} = dz$$

$$\frac{dt}{t^8} = -\frac{dz}{7}$$

$$\int \frac{\sec^2 x \cdot dx}{(\tan^{101} x + \tan x)} = g(x) + C$$

$$g\left(\frac{\pi}{4}\right) = -\frac{1}{100} \lim_{x \rightarrow \frac{\pi}{2}} g(x)$$

$$\int \frac{\sec^2 x \cdot dx}{\tan^{101} x (1+\tan^{-100} x)}$$

$$1 + \tan^{-100} x = t$$

$$-100 \tan^{-101} x \cdot \sec^2 x dx = dt$$

$$\frac{\sec^2 x \cdot dx}{\tan^{101} x} = -\frac{dt}{100}$$

$$-\frac{1}{100} \int \frac{dt}{t} = -\frac{1}{100} \ln |t| + C$$

$$\int \frac{(g(x)^6 x \cdot dx)}{\tan^4 x ((g(x)^7 x + \tan^7 x)^{4/7})^{6m}}$$

$$-\frac{1}{7} \int z^{-4/7} dz$$

$$\int \frac{(g(x)^6 x \cdot dx)}{\tan^4 x \cdot (g(x)^4 x \cdot (1+\tan^7 x)^{4/7} \div g^3 x)}$$

$$\int \frac{(P \cdot x^{P+2q-1} - q \cdot x^{q-1}) dx}{x^{2P+2q} + 2x^{P+q} + 1}$$

$$\Rightarrow \int \frac{P \cdot \cancel{x^P}}{(x^{P+q} + 1)^2} dx$$

$$\Rightarrow \int \frac{P \cdot x^{P+2q-1} - q \cdot x^{q-1}}{x^{2q} (x^P + x^{-q})^2}$$

$$\Rightarrow \int \frac{P \cdot x^{P-1} - q \cdot x^{-q-1}}{(x^P + x^{-q})^2} dx = P + x^{-q} = t$$

$$\int \frac{dt}{t^2} = -\frac{1}{t} + C$$

$$\int \frac{x^{3-1}}{(x^{q+1})(x+1)}$$

$$\Rightarrow \int \frac{(x^4 + x^3) - x^{q+1}}{(x^{q+1})(x+1)} \cdot dx$$

$$\int \frac{x^3(x+1)}{(x^{q+1})(x+1)} - \frac{1(x^{q+1})}{(x^{q+1})(x+1)} \cdot dx$$

$$\Rightarrow \int \frac{dx}{t} = -\ln|x+1| + C$$