

$$k \sin \alpha =$$

$$\sin(2x - \alpha)$$

$$-1 \leq k \sin \alpha \leq 1$$

$$2x - \alpha = n\pi$$

$$x \in (0, \pi)$$

$$\sin x = 0$$

$$\sin\left(\frac{\pi}{4} + \frac{\sqrt{x}}{2}\right) = \sin \sqrt{x}$$

$$\alpha = 2x - n\pi$$

$$-n\pi < \alpha < 2\pi - n\pi$$

$$(1+k)(\cos(3x - \alpha) + \cos(x - \alpha))$$

$$= 2\cos(x - \alpha) +$$

$$k(\cos(3x - \alpha) + \cos(x + \alpha))$$

$$\Rightarrow k(\cos(x - \alpha) - \cos(x + \alpha)) = \cos(x - \alpha) - \cos(3x - \alpha)$$

$$2k \sin x \sin \alpha = 2 \sin x \sin(2x - \alpha)$$

$$\frac{d(f(x))}{dx} = 0 \quad \forall x \in \mathbb{R}$$

$$x \cos^3 y + 3x \cos y \sin^2 y = 14$$

$$x \sin^3 y + 3x \cos^2 y \sin y = 13$$

$$= \frac{\tan^4 \theta (3 + 2 \tan^2 \theta) - \tan^2 x \tan^2 \theta}{\tan^2 x - \tan^2 \theta}$$

$$\tan^2 \theta = 3$$

$$\frac{3 \tan x + 2 \tan x \tan^2 \theta - \tan^3 x \tan \theta}{(\tan^2 x - \tan^2 \theta) \tan x} = \frac{\tan^2 x \tan \theta \frac{\tan x - \tan \theta}{1 + \tan x \tan \theta} + \tan x + \frac{\tan x + \tan \theta}{1 - \tan x \tan \theta}}{\frac{(\tan^2 x - \tan^2 \theta) \tan x}{(1 - \tan^2 x \tan^2 \theta)}}$$

$$(1 - \cos 2x)^5 + (1 + \cos 2x)^5 = 58 + 29 = 87$$

$$\begin{aligned} & x - \cancel{x^2} - \cancel{x^2} y + x^2 y + x - \cancel{x^3} y^2 \\ & + x + \cancel{x^2} + \cancel{x^2} y + x y^2 \end{aligned}$$

19. $\sin x \cos 2x = \sin 2x \cos 3x - \frac{1}{2} \sin 5x$

$$\sin 3x - \cancel{\sin x} = \cancel{\sin 5x} - \cancel{\sin x} - \cancel{\sin 5x} \Rightarrow \boxed{\sin 3x = 0}$$

$$\frac{n\pi}{3}$$

$$\sin x (3 - 4 \sin^2 x)$$

$$a \cos 2x + |a| \cos 4x = 1 - \cos 6x$$

$$= 2 \sin^2 3x$$

$$(a \in -\infty, -1) \cup \{0\}$$

$$a + |a| = 0 \Rightarrow \boxed{a \leq 0}$$

$$Q \rightarrow x = \frac{n\pi}{3}$$

$$2a \sin 3x \sin x = 2 \sin^2 3x$$

$$[3-4, 3]$$

$$a \sin x = \sin 3x$$

$$a = 3 - 4 \sin^2 x$$

$$\cos\left(\frac{\pi}{2} - \cos x\right) = \cos(\sin x)$$

$$\sin x = 2n\pi + \frac{\pi}{2} - \cos x \quad \text{or} \quad 2n\pi - \frac{\pi}{2} + \cos x$$

$$\sin x + \cos x = 2n\pi + \frac{\pi}{2} \quad \text{or} \quad \sin x - \cos x = 2n\pi - \frac{\pi}{2}$$

$$12 \cdot \sin x \cos 2y = (a^2 - 1)^2 + 1 \geq 1$$

$$a = -1$$

$$\begin{aligned} \sin x \cos 2y &= 1 \\ \cos x \sin 2y &= 0 \end{aligned}$$

$$\alpha + \beta = \tan \theta - 2$$

$$\alpha \beta = -1 - \tan \theta$$

$$\alpha + \beta + \alpha \beta = -3$$

$$(\alpha + 1)(\beta + 1) = -2$$

$$\begin{array}{cc} -2 & -1 \\ 2 & 1 \\ -1 & 2 \\ & -2 \end{array}$$

Simplify

$$\frac{(a^2+b^2+c^2)(a-b)(b-c)(c-a)(a+b+c)}{(c-a)(a+b+c)}$$

$$\frac{2\cos\theta}{4\cos^2\theta-1} = 3-4\sin^2\theta$$

$$\frac{(a^2+b^2+c^2)}{1} \begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$$

$$\begin{vmatrix} (b+c)^2 & a^2 & bc \\ (c+a)^2 & b^2 & ca \\ (a+b)^2 & c^2 & ab \end{vmatrix}$$

$$\frac{(a^2+b^2+c^2)}{1} \begin{vmatrix} a & a^3 & 1 \\ b & b^3 & 1 \\ c & c^3 & 1 \end{vmatrix}$$

$$\frac{\sin^3\theta}{\sin 6\theta} \frac{\sin^3\theta}{\sin 2\theta} \frac{\sin^3\theta}{\sin 3\theta}$$

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$$\frac{C_1 \rightarrow C_1 + C_2 - 2C_3}{(a^2+b^2+c^2)}$$

$$\frac{(a^2+b^2+c^2)}{abc} \begin{vmatrix} a & a^3 & abc \\ b & b^3 & abc \\ c & c^3 & abc \end{vmatrix}$$

$$C_2 \rightarrow C_2 - 3\sin\theta C_1 + 4C_3$$

$$\begin{vmatrix} 1 & a^2 & bc \\ 1 & b^2 & ca \\ 1 & c^2 & ab \end{vmatrix}$$

$$\begin{vmatrix} a & a^3 & abc \\ b & b^3 & abc \\ c & c^3 & abc \end{vmatrix}$$

$\Delta =$ 

$$\begin{vmatrix} 1 & x & x^2 \\ 1 & y & y^2 \\ 1 & z & z^2 \end{vmatrix}$$

$$= (x-y)(y-z)(z-x)$$

$$\xrightarrow[R_3 \rightarrow R_3 - R_1]{R_2 \rightarrow R_2 - R_1} \begin{vmatrix} 1 & x & x^2 \\ 0 & y-x & y^2-yx \\ 0 & z-x & z^2-zx \end{vmatrix}$$

$$\begin{vmatrix} 1 & x & x^2 \\ 0 & y-x & y^2-yx \\ 0 & z-x & z^2-zx \end{vmatrix}$$

$$\begin{vmatrix} x^2 & x & 1 \\ y^2 & y & 1 \\ z^2 & z & 1 \end{vmatrix}$$

$$= (y-x)(z-x)(z-y)$$

Put $y=x$ $y=z$ $z=x$

$$\boxed{\Delta = 0}$$

$$\begin{vmatrix} 1 & x & x^3 \\ 1 & y & y^3 \\ 1 & z & z^3 \end{vmatrix} = (x-y)(y-z)(z-x)(x+y+z)$$

$$\Delta = k(x-y)(y-z)(z-x)$$

$$x=0, y=1, z=-1$$

$$k=-1 \quad \Rightarrow \quad k(-1)(2)(-1) =$$

$$\begin{vmatrix} 1 & 0 & 0 \\ 1 & 1 & 1 \\ 1 & -1 & -1 \end{vmatrix} = 2$$

$$\begin{vmatrix} 1 & x^2 & x^3 \\ 1 & y^2 & y^3 \\ 1 & z^2 & z^3 \end{vmatrix} = (x-y)(y-z)(z-x)(xy+yz+zx)$$

$$\begin{vmatrix} a & -b & -c \\ b & c & a \\ c & a & b \end{vmatrix} = 3abc - a^3 - b^3 - c^3$$

$R_1 \rightarrow R_1 + R_2 + R_3$

$$(x+bc) \begin{vmatrix} 1 & 1 & 1 \\ b & c & a \\ c & a & b \end{vmatrix} = a(bc-a^2) - b(b^2-ac) + c(ab-c^2)$$

\downarrow
 $c_2 \rightarrow c_2 - c_1$
 $c_3 \rightarrow c_3 - c_1$

3. P.T. $\begin{vmatrix} 1+a & 1 & 1 \\ 1 & 1+b & 1 \\ 1 & 1 & 1+c \end{vmatrix} = abc \left(1 + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right)$

$$= abc \begin{vmatrix} 1+\frac{1}{a} & \frac{1}{a} & \frac{1}{a} \\ \frac{1}{a} & 1+\frac{1}{b} & \frac{1}{b} \\ \frac{1}{a} & \frac{1}{b} & 1+\frac{1}{c} \end{vmatrix} \xrightarrow{R_1 \rightarrow R_1 + R_2 + R_3} abc \left(1 + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right) \begin{vmatrix} 1 & 1 & 1 \\ \frac{1}{b} & 1+\frac{1}{b} & \frac{1}{b} \\ \frac{1}{c} & \frac{1}{c} & 1+\frac{1}{c} \end{vmatrix}$$

$$\xrightarrow{\begin{matrix} C_2 \rightarrow C_2 - C_1 \\ C_3 \rightarrow C_3 - C_1 \end{matrix}} abc \left(1 + \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right) \begin{vmatrix} 1 & 0 & 0 \\ \frac{1}{b} & 1 & 0 \\ \frac{1}{c} & 0 & 1 \end{vmatrix}$$

Trig. Eqn

Ex-III, IV ✓