

KINEMATICS

(*). Concept of distance & displacement \Rightarrow

\Rightarrow Distance:- It is the ^(actual) path length of the particle.

\Rightarrow Displacement \rightarrow [It is the vector joining initial position to the final position of the particle.]
or, "Change in position vector" \rightarrow [Position vector must be w.r.t origin].

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By Δ -Law of vector addition: \rightarrow

$$\vec{r}_i + \Delta \vec{r} = \vec{r}_f$$

$$\Delta \vec{r} = [\vec{r}_f - \vec{r}_i]$$

[Displacement vector] Change in position vector.

\vec{r}_{AB} = (Displacement vector)

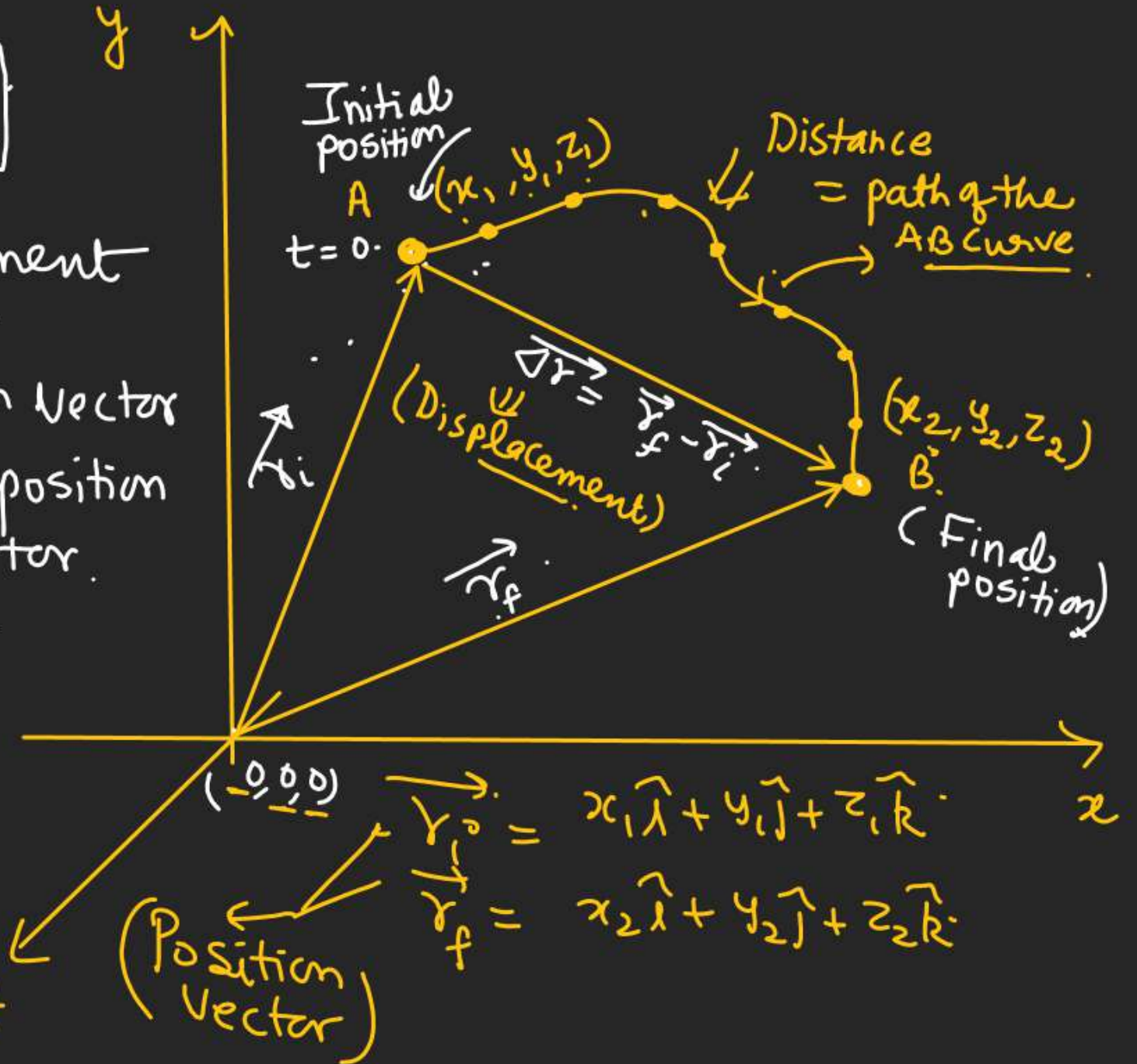
$$= (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}$$

$$|\vec{r}_{AB}| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

$$\Delta \vec{r} = \vec{r}_{AB}$$

Displacement Vector.

\vec{r}_i = position vector
 \vec{r}_f = final position vector



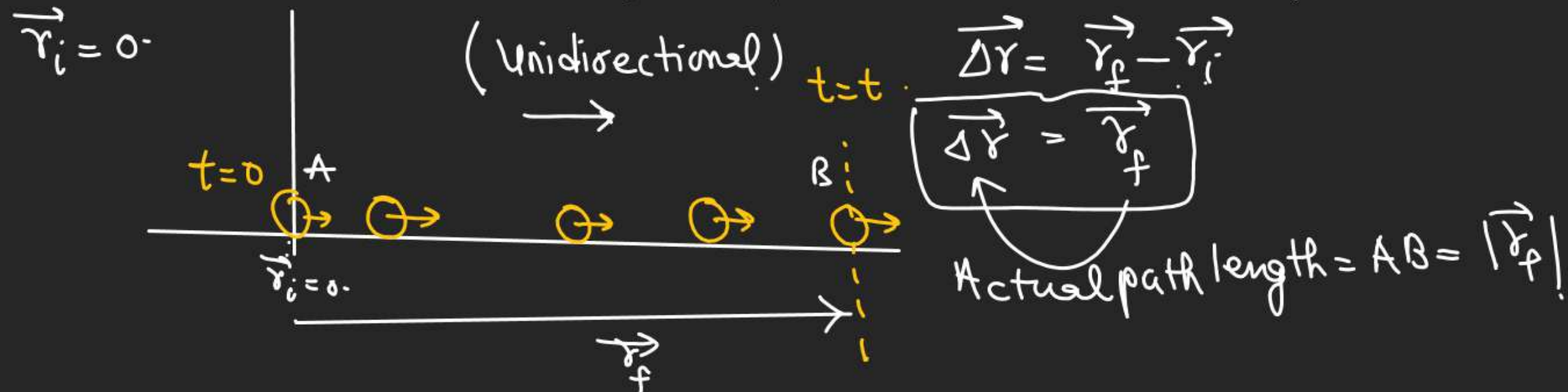
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(*) \Rightarrow Distance \gg |Displacement|.

\Rightarrow Distance is always +ve it is a Scalar quantity but displacement can be (+ve) or (-ve) and it is a vector quantity.

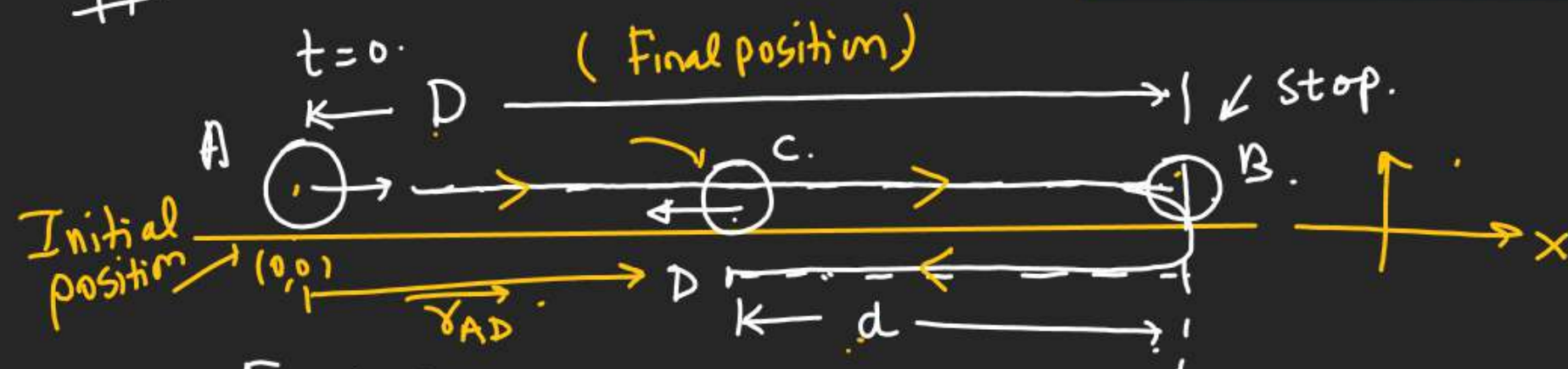
\Rightarrow [Distance = Displacement]

\Rightarrow When motion of the particle is a straight line and unidirectional



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\Rightarrow Find Distance and displacement for the motion A C B D

Displacement $\Rightarrow \vec{x}_{AD} = (D-d)\hat{i}$

$|\vec{x}_{AD}| = (D-d) \text{ m}$

Distance = Actual path length
of A C B D $= (D+d) \text{ m}$

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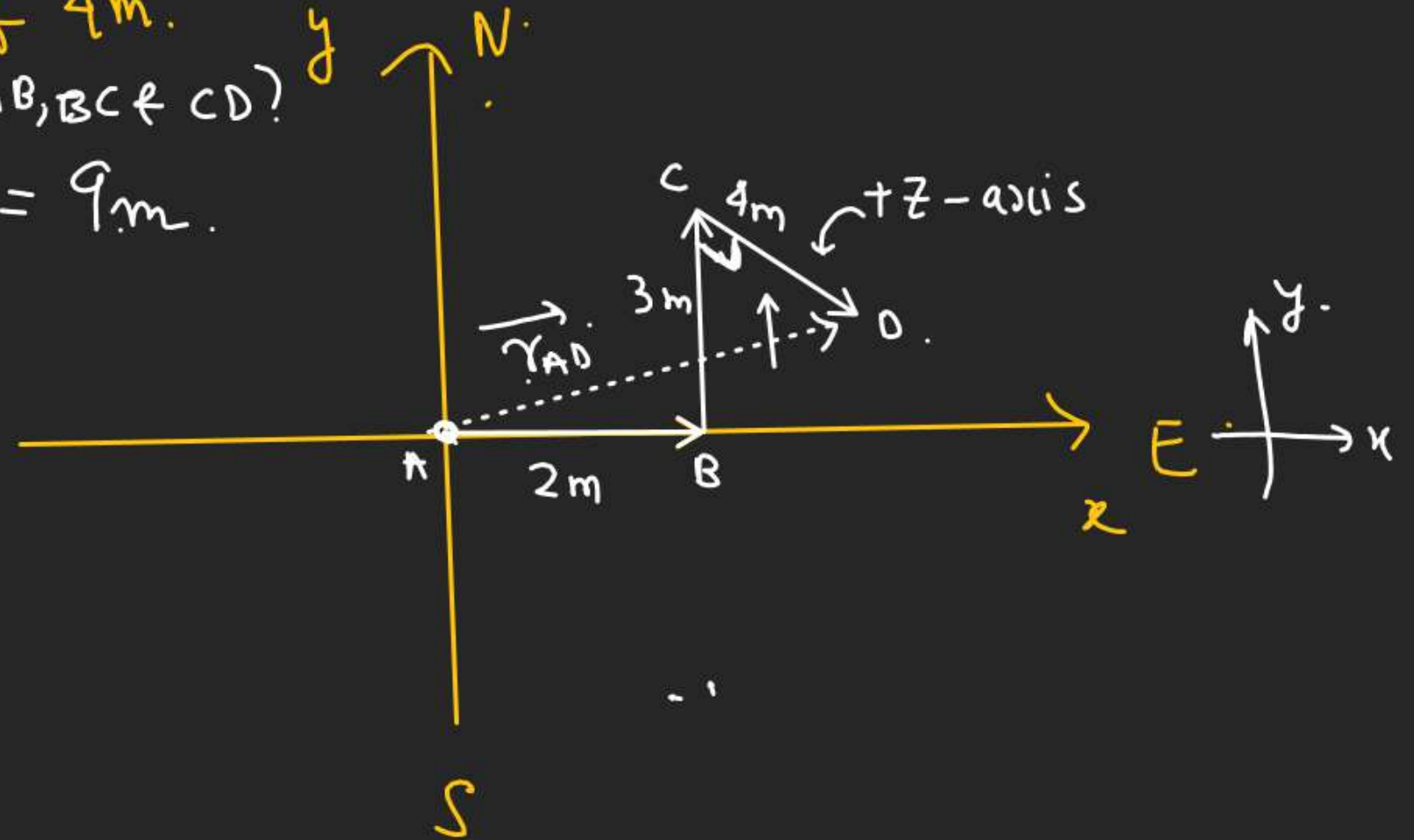
A bird starts flying in east direction and cover a distance of 2m after that it turns towards north and cover a distance of 3m. and finally move perpendicularly outward and cover a distance of 4m.
 [Find 1) distance = (path length of AB, BC & CD) ?
 2) displacement = $2 + 3 + 4 = 9\text{m}$.

Displacement \Rightarrow ?

$$\vec{r}_{AD} = \vec{r}_{AB} + \vec{r}_{BC} + \vec{r}_{CD}$$

$$= (2\hat{i} + 3\hat{j} + 4\hat{k})$$

$$|\vec{r}_{AD}| = \sqrt{(2)^2 + (3)^2 + (4)^2} = \sqrt{29}\text{m}$$



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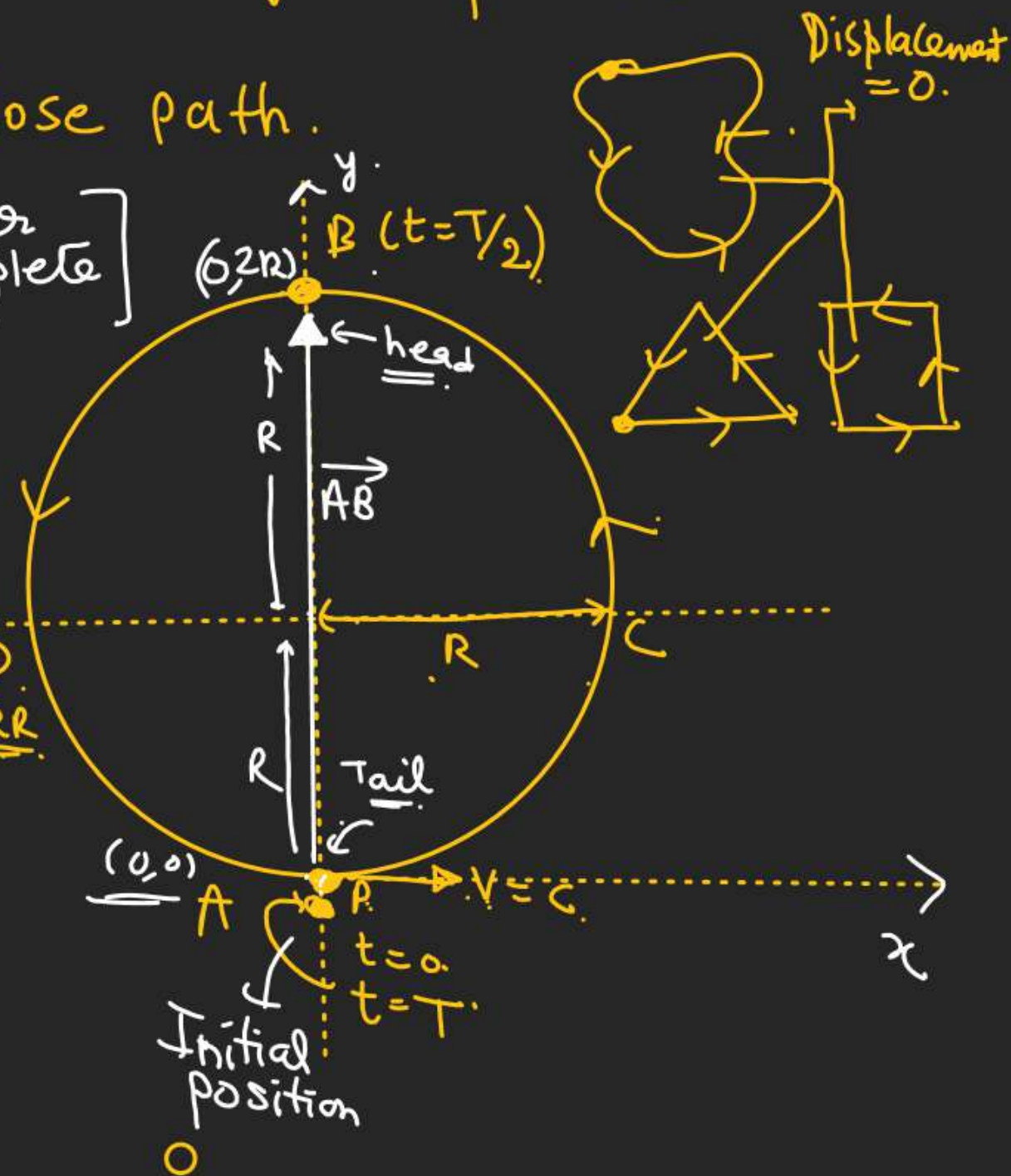
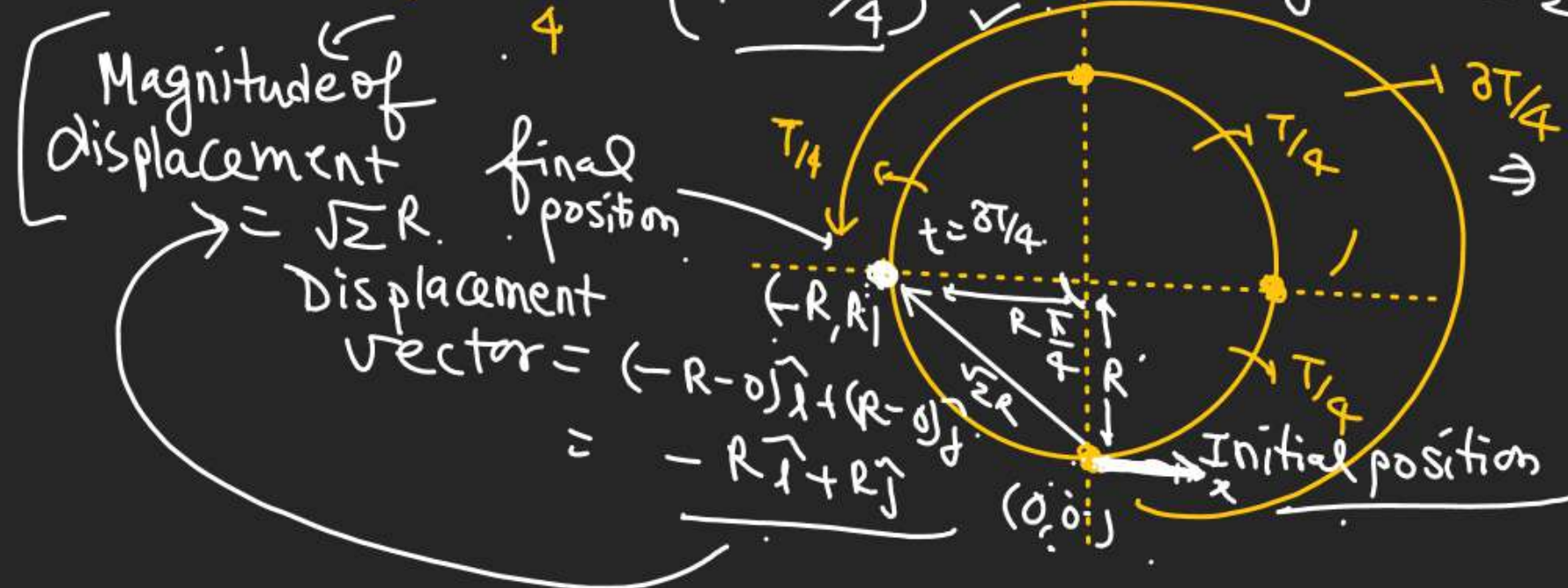
⇒ "Displacement is always zero if initial and final position vector is same."
possible when particle is moving in a close path.

Find Distance and displacement. $[T \rightarrow \text{To Cover one complete rotation}]$

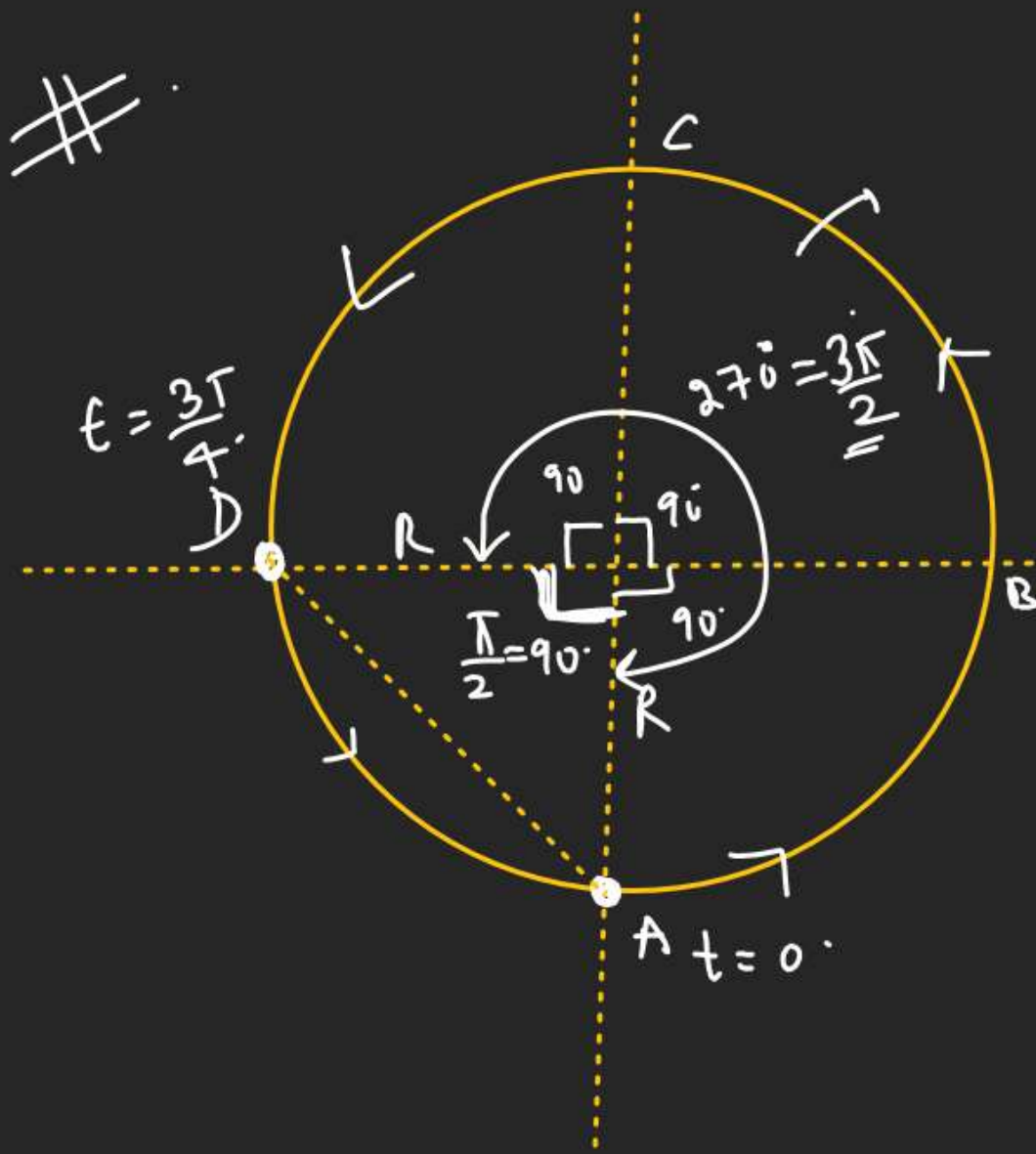
✓ a) for $t=0$ to $t=T \rightarrow$ $\begin{cases} \text{Distance} = 2\pi R \\ \text{Displacement} = 0 \end{cases} T = \left[\frac{2\pi R}{v} \right]$

- b) for $t=0$, to $t = T/2$ $\begin{cases} \text{Distance} = \text{path length ACB} \\ \text{Displacement} = (2R)\hat{j} \end{cases}$

✓ c) for $t=0$, to $t = \frac{3T}{4}$ $\begin{cases} \text{Distance} = \text{path length ACB} \\ \text{Displacement} = (2R)\hat{j} \end{cases}$
 \downarrow $t = \frac{3T}{4} = (T - T/4)$ \downarrow $\text{magnitude} = \sqrt{(2R)^2} = 2R$



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$$L = R\theta$$

↓
radian.

$$[L_{ABCD}]$$

→ major arc

$$= R \times \frac{3\pi}{2}$$

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Q.8 Distance and displacement at an angular displacement ' θ ' in uniform circular motion ($v=c$)

$$\vec{r}_{PQ} = (R\cos\theta - R)\hat{i} + (R\sin\theta)\hat{j}$$

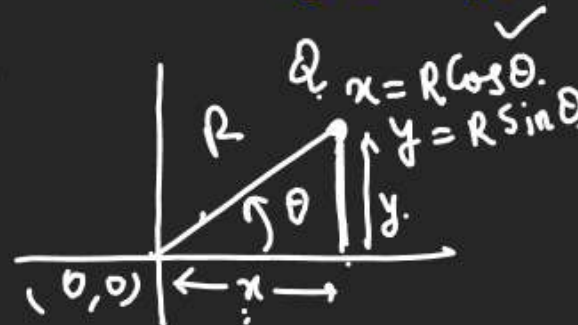
Displacement Vector

$$|\vec{r}_{PQ}| = \sqrt{R^2(\cos\theta - 1)^2 + R^2\sin^2\theta}$$

$$= R \sqrt{\cos^2\theta + 1 - 2\cos\theta + \sin^2\theta}$$

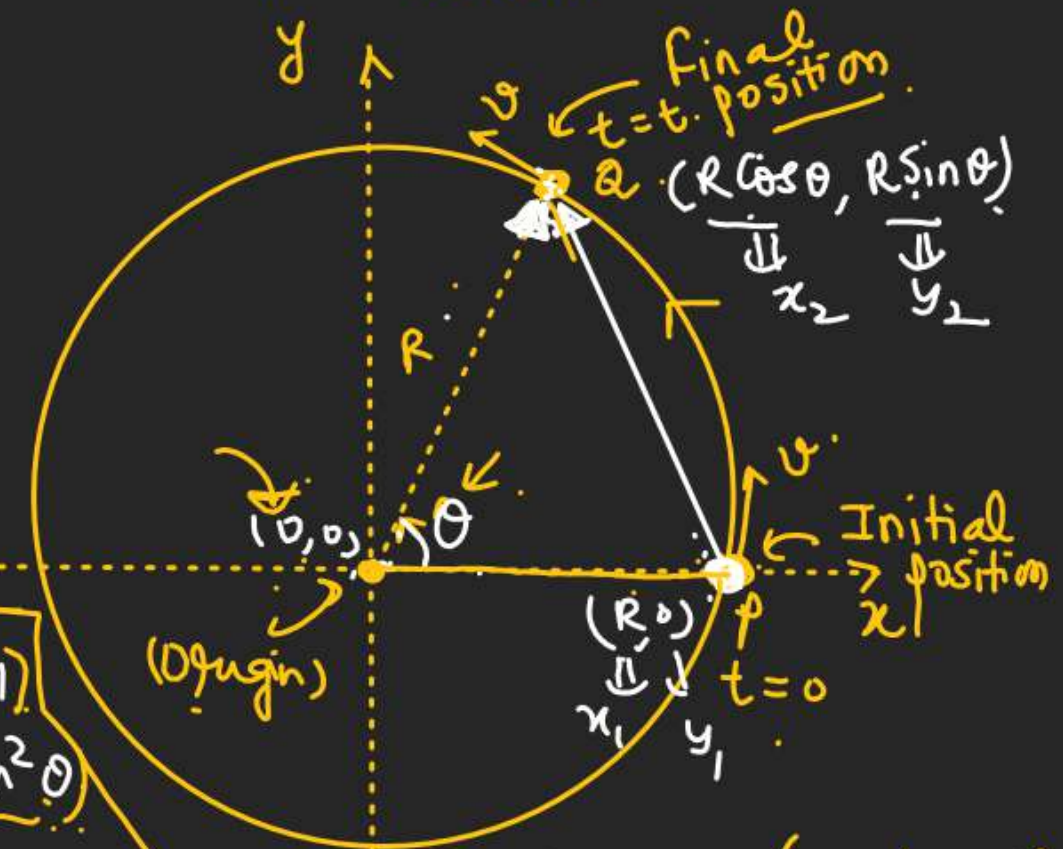
$$= R \sqrt{2 - 2\cos\theta}$$

$$|\vec{r}_{PQ}| = R \sqrt{2(1 - \cos\theta)} = R \sqrt{2 \left[1 - \left(1 - 2\sin^2\frac{\theta}{2} \right) \right]} = R \sqrt{4\sin^2\frac{\theta}{2}} = \left[2R\sin\frac{\theta}{2} \right]$$



$$\cos 2\theta = (2\cos^2\theta - 1)$$

$$\cos\theta = \left(1 - 2\sin^2\frac{\theta}{2} \right)$$



Distance = (Arc length PQ)

$$= R[\theta] \text{ radian}$$

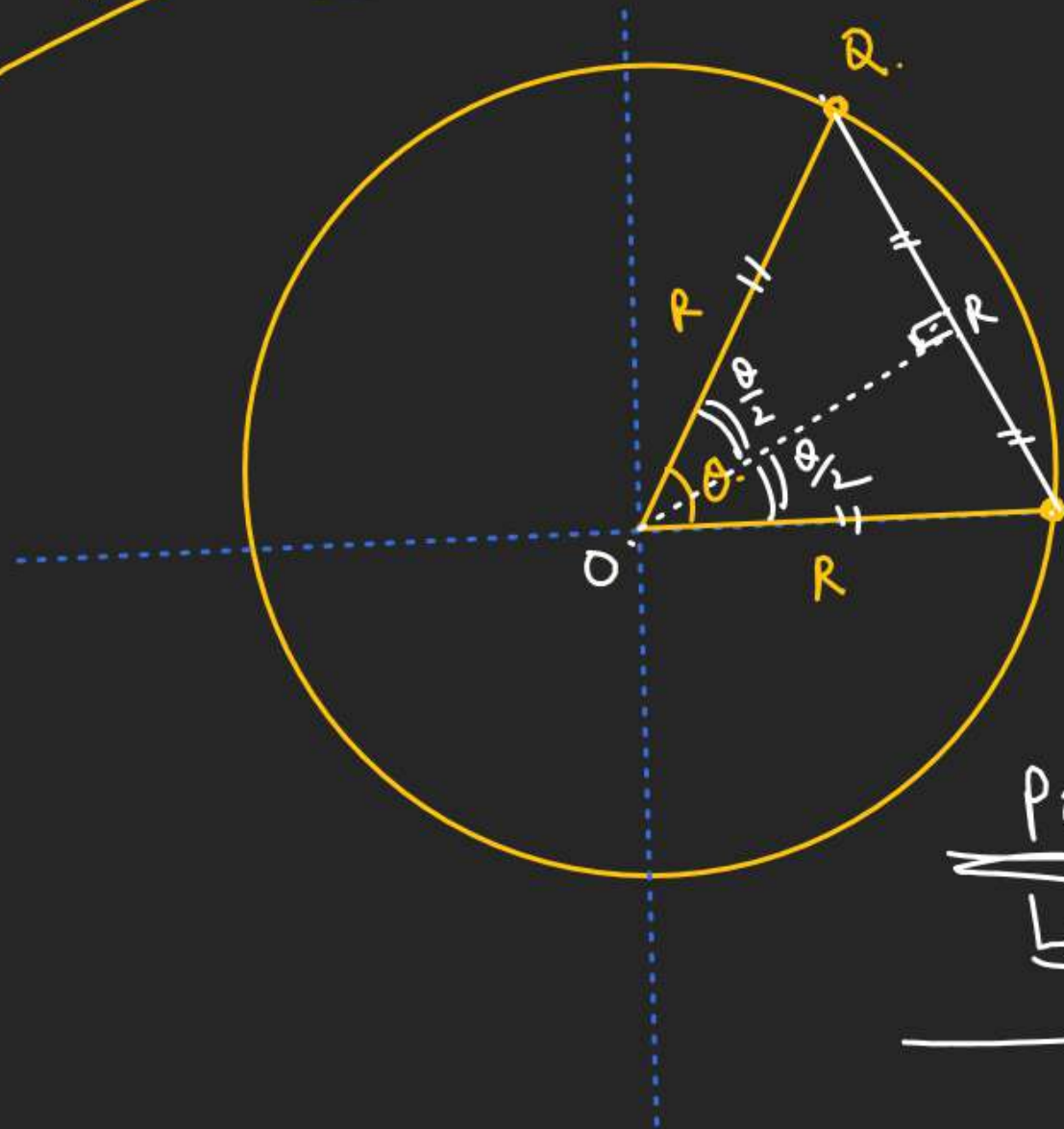
$$= R \times \frac{\pi}{180} \times \theta$$

if θ in degree

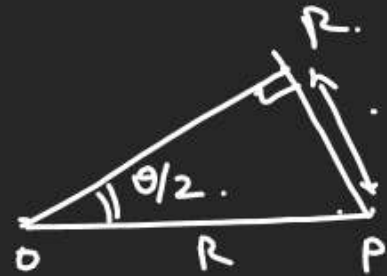
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Another
method

For displacement:



In $\triangle OPR$



$$\sin \frac{\theta}{2} = \frac{PR}{R}$$

$$\underline{PR} = \left[R \sin \frac{\theta}{2} \right]$$

$$\underline{\underline{PQ}} = 2PR = \left[2R \sin \frac{\theta}{2} \right]$$

↳ Magnitude of displacement

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HW

Q. A particle moves in a semicircular path of radius R from O to A (Fig.) Then it moves parallel to z – axis covering a distance R upto B . Finally it moves along BC parallel to y – axis through a distance $2R$. Find the ratio of D/s .

