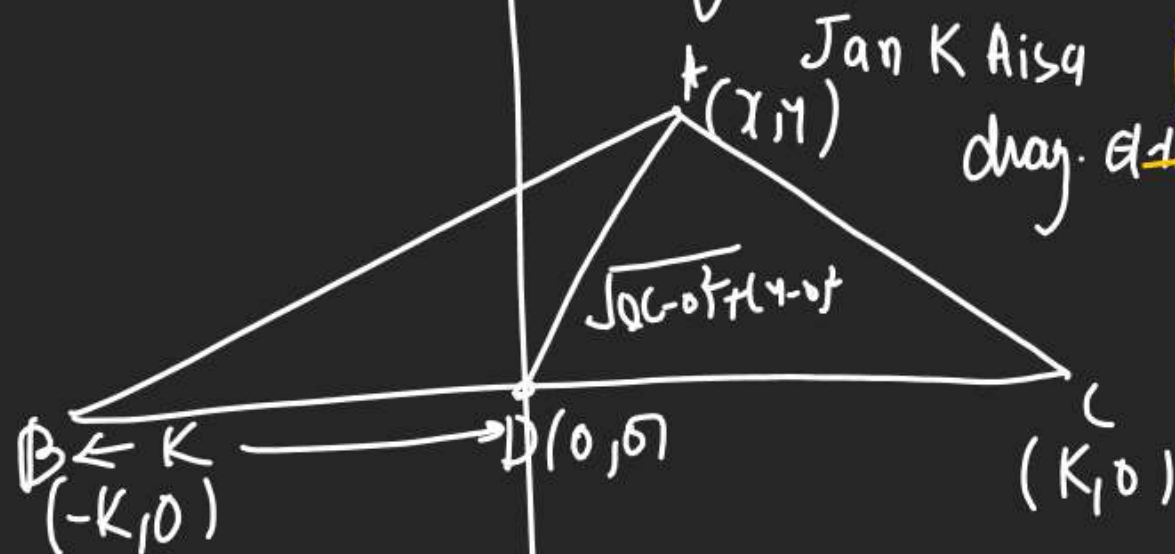


Q Prove Apollonius Theorem.

$$AB^2 + AC^2 = 2(AD^2 + BD^2)$$

D = Mid Pt of BC



LHS = $AB^2 + AC^2$

$$= (x+K)^2 + (y-0)^2 + (x-K)^2 + (y-0)^2$$

$$= 2x^2 + 2y^2 + 2K^2 = 2(x^2 + y^2 + K^2)$$

RHS = $2(AD^2 + BD^2)$

$$= 2(x^2 + y^2 + K^2) = \text{LHS} = \text{H.P.}$$

A)

$$\sqrt{0^2 + 2\sqrt{3}^2} = 12$$

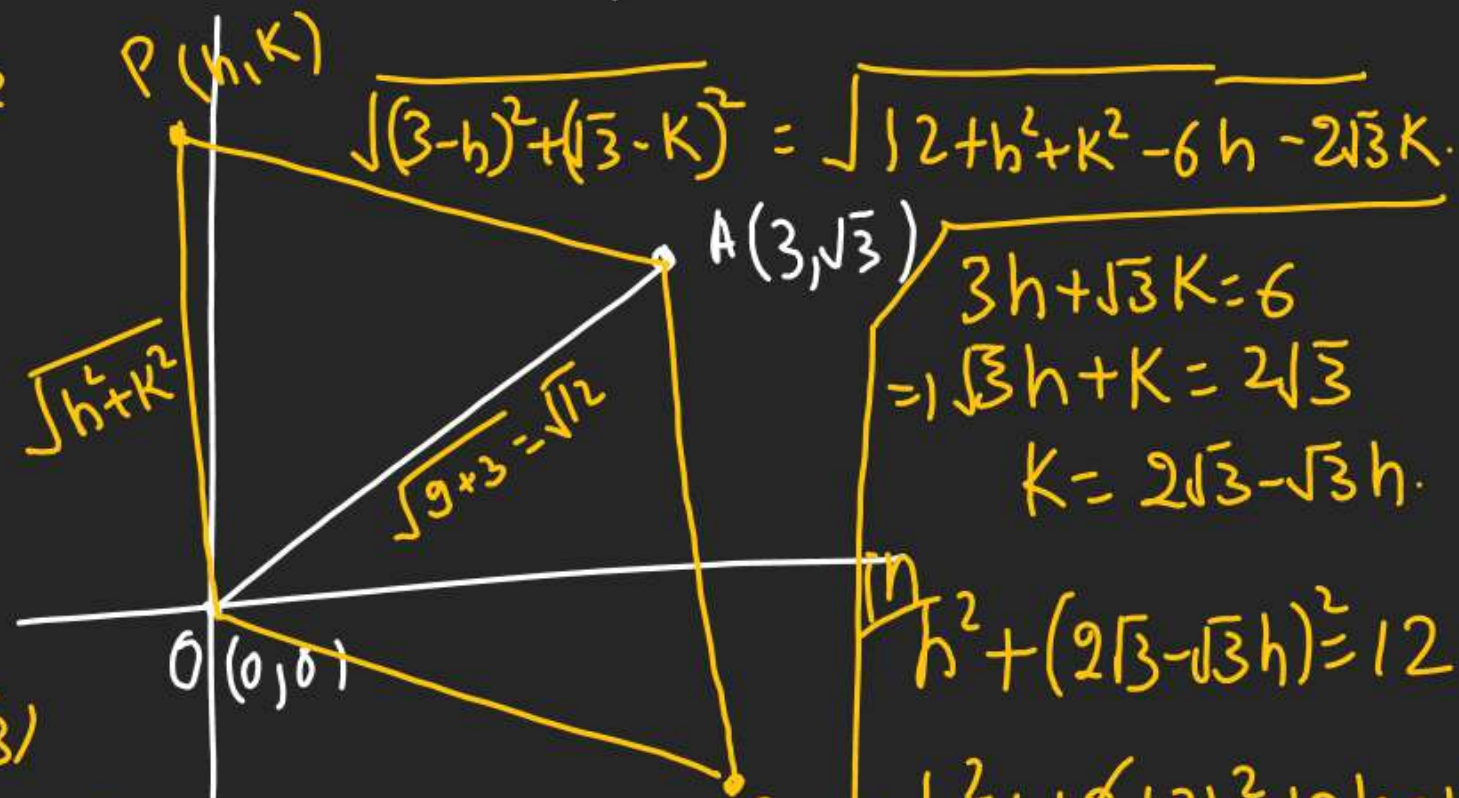
$$\left[\begin{array}{l} P = (3, -\sqrt{3}) \\ O = (0, 0) \\ A = (3, \sqrt{3}) \end{array} \right] = \sqrt{9+3} = 12$$

(B) $h=0, K=2\sqrt{3}$

$$\left[\begin{array}{l} P(0, 2\sqrt{3}) \\ O(0, 0) \\ A(3, \sqrt{3}) \end{array} \right] = 12$$

$P = (3, -\sqrt{3})$ & $(0, 2\sqrt{3})$

Q 2 pts O(0,0) & A(3,√3) with another pt. P form an eq^l Δ. find P.



① $\sqrt{12+h^2+k^2-6h-2\sqrt{3}k} = \sqrt{12}$

$$h^2 + k^2 - 6h - 2\sqrt{3}k = 0$$

② $h^2 + k^2 = 12$

(3) $\sqrt{12+h^2+k^2-6h-2\sqrt{3}k} = \sqrt{h^2+k^2}$

$$6h + 2\sqrt{3}k = 12 \rightarrow 3h + \sqrt{3}k = 6$$

$$3h + \sqrt{3}k = 6$$

$$\Rightarrow \sqrt{3}h + k = 2\sqrt{3}$$

$$k = 2\sqrt{3} - \sqrt{3}h$$

$$h^2 + (2\sqrt{3} - \sqrt{3}h)^2 = 12$$

$$h^2 + 12 + 3h^2 - 12h = 12$$

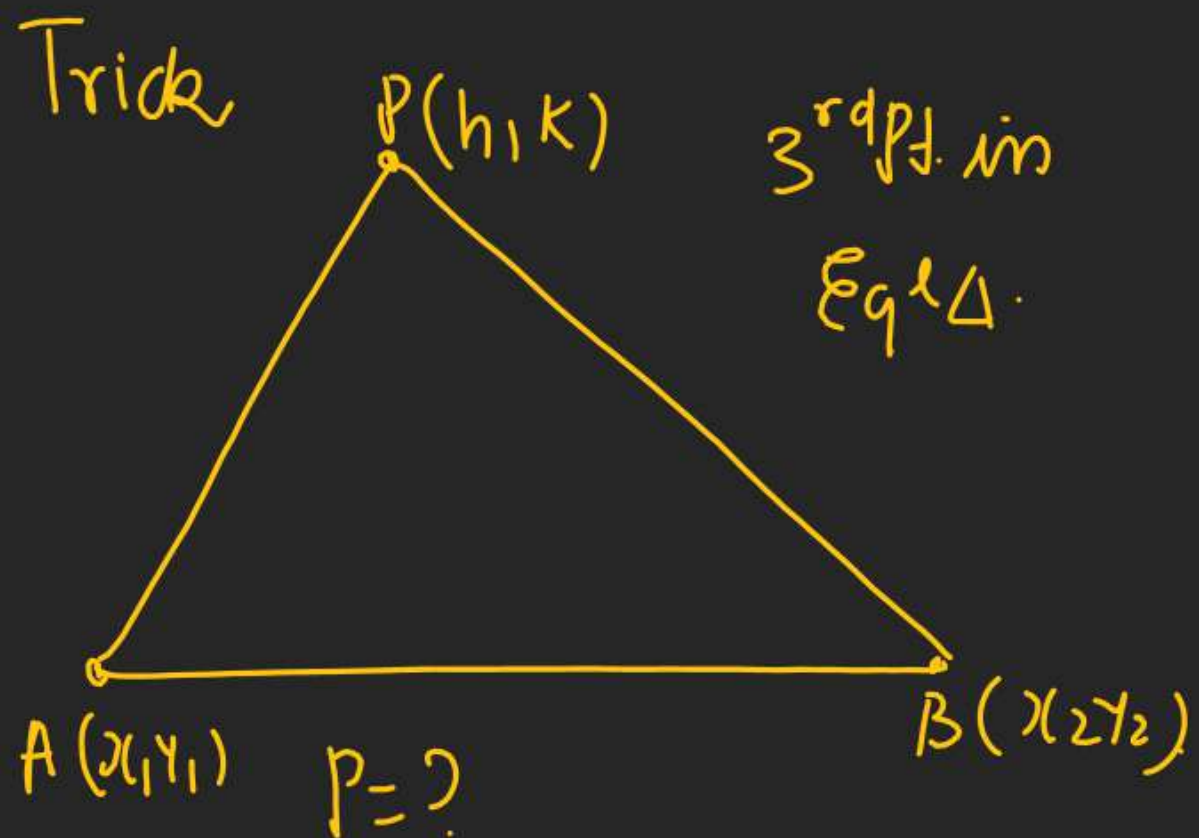
$$4h^2 - 12h = 0 \Rightarrow h = 3$$

$$\therefore k = 2\sqrt{3} - 3\sqrt{3} = -\sqrt{3}$$

$P = (3, -\sqrt{3})$

if $h=0, k=\pm 2\sqrt{3}$

Trick



$$h = \frac{(x_1 + x_2) \pm \sqrt{3}(y_1 - y_2)}{2}$$

$$k = \frac{(y_1 + y_2) \mp \sqrt{3}(x_1 - x_2)}{2}$$

$$Q \quad O \equiv (0, 0), A = (3, \sqrt{3})$$

$$(x_1, y_1) \quad (x_2, y_2)$$

$$P = (h, k)$$

$$h = \frac{(0+3) \pm \sqrt{3}(0-\sqrt{3})}{2} = \frac{3 + \sqrt{3}(-\sqrt{3})}{2},$$

$$k = \frac{(0+\sqrt{3}) \mp \sqrt{3}(0-3)}{2} = \frac{\sqrt{3} + \sqrt{3}(+3)}{2},$$

$$(h, k) = (0, 2\sqrt{3})$$

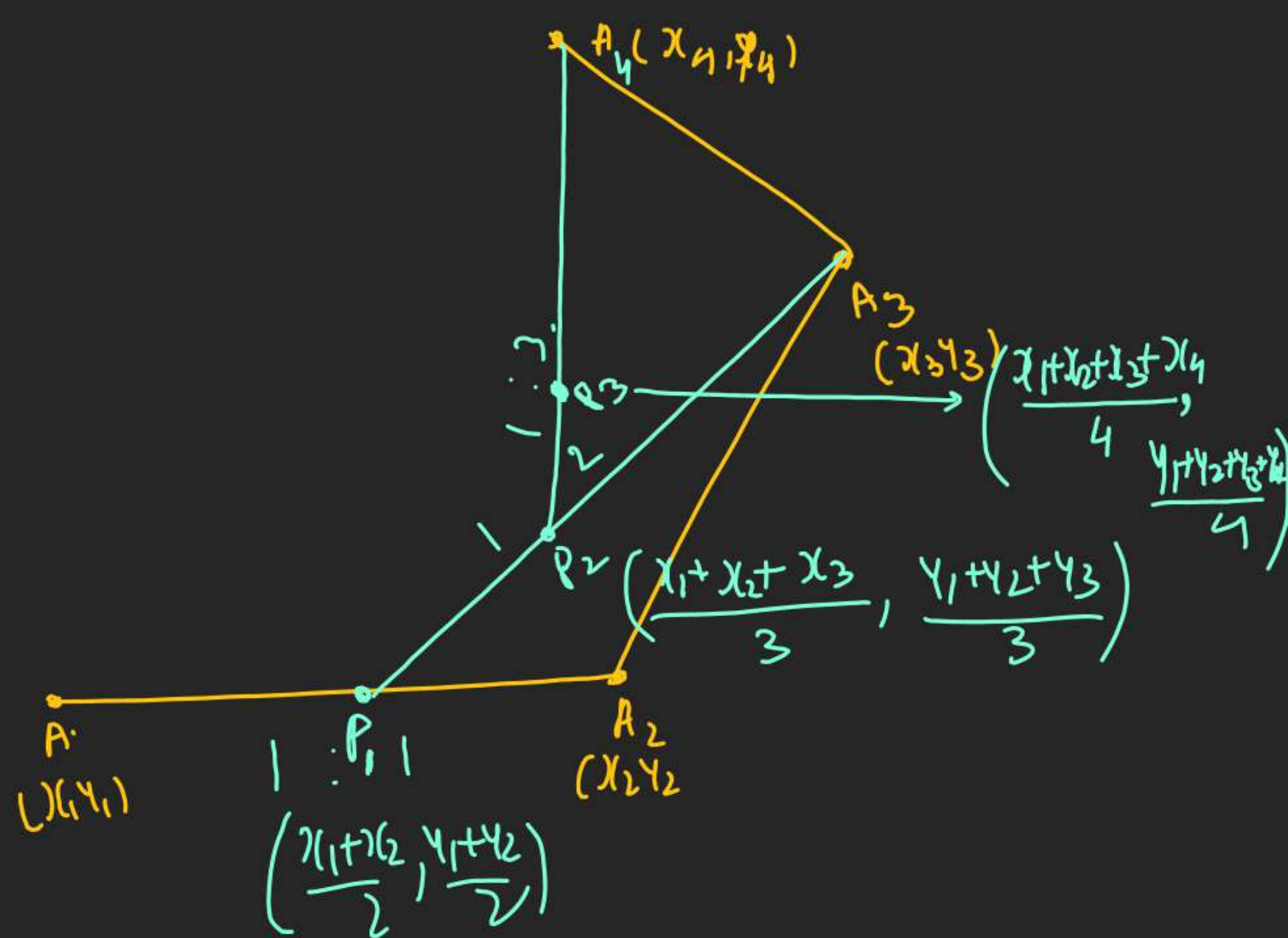
$$\frac{3 - \sqrt{3}(-\sqrt{3})}{2} = 3$$

$$\frac{\sqrt{3} + \sqrt{3}(-3)}{2} = -\sqrt{3}$$

$$(3, -\sqrt{3})$$

Q. Let $A_1, A_2, A_3, \dots, A_n$ are n pts.
in a plane whose coord. are
 $(x_1, y_1), (x_2, y_2), (x_3, y_3), \dots, (x_n, y_n)$

A_1, A_2 is Bisected at P_1 , P_1, A_3 is
divided in Ratio $1:2$ at P_2 , P_2, A_4 is
divided in Ratio $1:3$ at P_3 , P_3, A_5 is
divided in Ratio $1:4$ at P_4 & so on
untill all n pts are exhausted. Find
Coord. of final Pt.



$$\text{Final Pt } P_n \left(\frac{x_1+x_2+x_3+\dots+x_n}{n}, \frac{y_1+y_2+y_3+\dots+y_n}{n} \right)$$

Relation betⁿ H, G, O

Relation betⁿ Orthocentre, centroid, circumcentre.

depends on Δ .

(1) If Δ is equilateral Δ then H, G, I, O will coincide.



(2) Δ other than eq^l Δ then H, G, O will be in a line always.



(3) Ratio of $HG:GO = 2:1$ always.

$$G = \left(\frac{a(\cos\theta_1 + \cos\theta_2 + \cos\theta_3)}{3}, \frac{a(\sin\theta_1 + \sin\theta_2 + \sin\theta_3)}{3} \right)$$

$$\frac{a}{3}(\cos\theta_1 + \cos\theta_2 + \cos\theta_3) = 0$$

$$\cos\theta_1 + \cos\theta_2 + \cos\theta_3 = 0$$

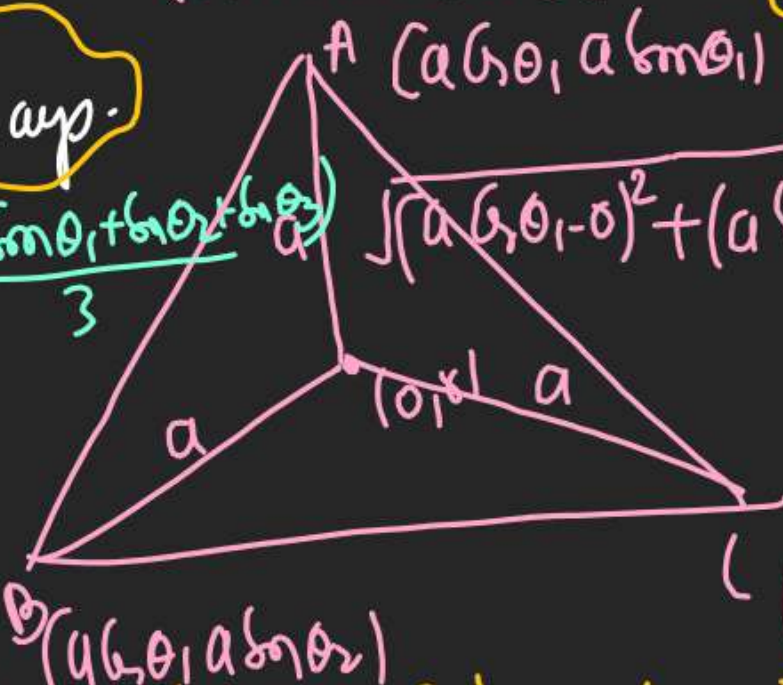
$$\frac{a}{3}(\sin\theta_1 + \sin\theta_2 + \sin\theta_3) = 0$$

$$\sin\theta_1 + \sin\theta_2 + \sin\theta_3 = 0$$

Q ΔABC have vertices $A(a\cos\theta_1, a\sin\theta_1)$, $B(a\cos\theta_2, a\sin\theta_2)$, $C(a\cos\theta_3, a\sin\theta_3)$ in an equilateral Δ then P.T. $\cos\theta_1 + \cos\theta_2 + \cos\theta_3 = \sin\theta_1 + \sin\theta_2 + \sin\theta_3 = 0$ J.I.P

(Common Sense

(1) If all vertices are



$(0,0)$ is the centroid.

$$\sqrt{(a\cos\theta_1 - 0)^2 + (a\sin\theta_1 - 0)^2}$$

$$= \sqrt{a^2(\cos^2\theta_1 + \sin^2\theta_1)}$$

$$= \sqrt{a^2(1)}$$

$$= a$$

(2) If all vertices are equidistant from $(0,0)$ then $(0,0)$ is the circumcentre = centroid = $(0,0)$