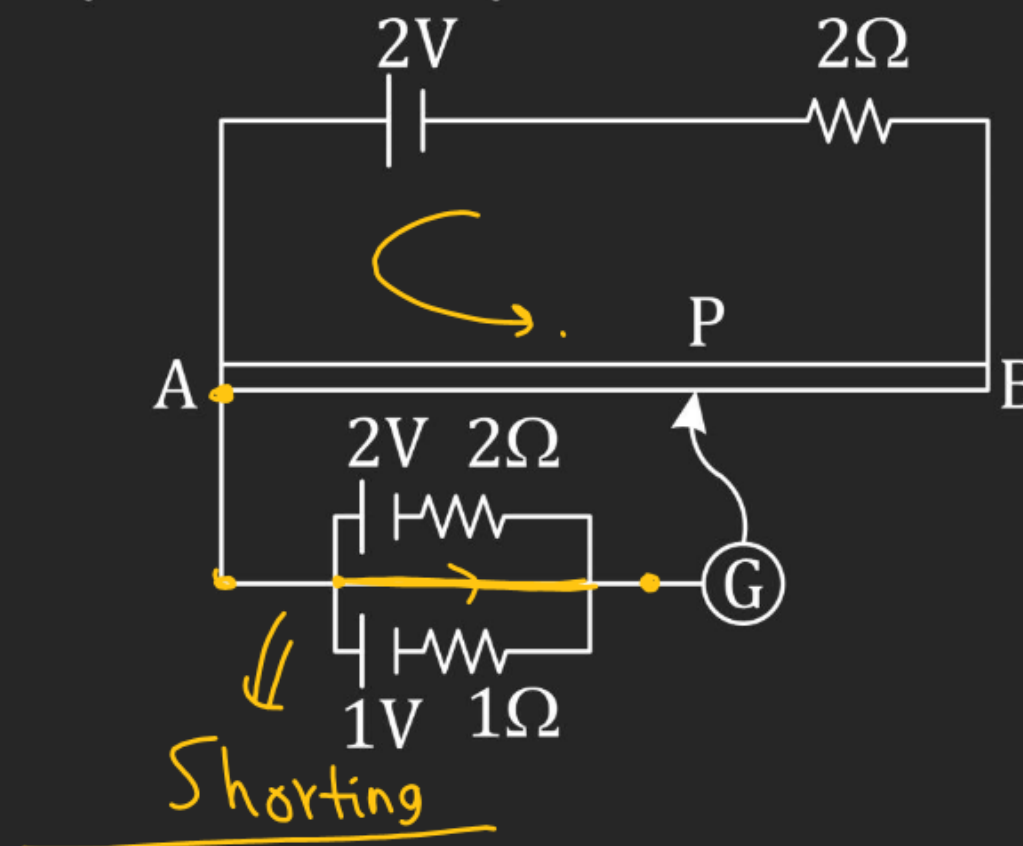


# CURRENT ELECTRICITY

## Potentiometer and Meter Bridge

**Q.6** A battery of emf  $2\text{ V}$  is connected across a long uniform wire  $AB$  of length  $1\text{ m}$  and resistance per unit length  $2\Omega\text{m}^{-1}$ . Two cells of emf  $\varepsilon_1 = 1\text{ V}$  and  $\varepsilon_2 = 2\text{ V}$  are connected as shown in the fig. If the galvanometer shows no deflection at point  $P$ , the distance of point  $P$  from point  $A$  is equal to :

- (A) 0 ✓
- (B) 50 cm
- (C) 100 cm
- (D) 25 cm



# CURRENT ELECTRICITY

## Potentiometer and Meter Bridge

**Q.7** A battery of emf  $\varepsilon_0 = 12\text{ V}$  is connected across a 4 m long uniform wire having resistance  $4\Omega/\text{m}$ . The cells of small emfs  $\varepsilon_1 = 2\text{ V}$  and  $\varepsilon_2 = 4\text{ V}$  having internal resistance  $2\Omega$  and  $6\Omega$  respectively, are connected as shown in the figure. If galvanometer shows no deflection at the point N, the distance of point N from the point A is equal to :

(A)  $\frac{1}{6}\text{ m}$

(B)  $\frac{1}{3}\text{ m3}$

(C) 25 cm

(D) 50 cm

$$R_{AB} = (4 \times 4) = 16\Omega$$

$$i = \frac{12}{16+8} = \frac{12}{24}$$

$$i = \frac{1}{2}\text{ Amp.}$$

$$V_{AN} = \frac{1}{2} \times R_{AN}$$

$$= \frac{1}{2} \times 4 \times l_{AN} = (2l_{AN})$$

$$\Rightarrow V_{AN} = V_C - V_D$$

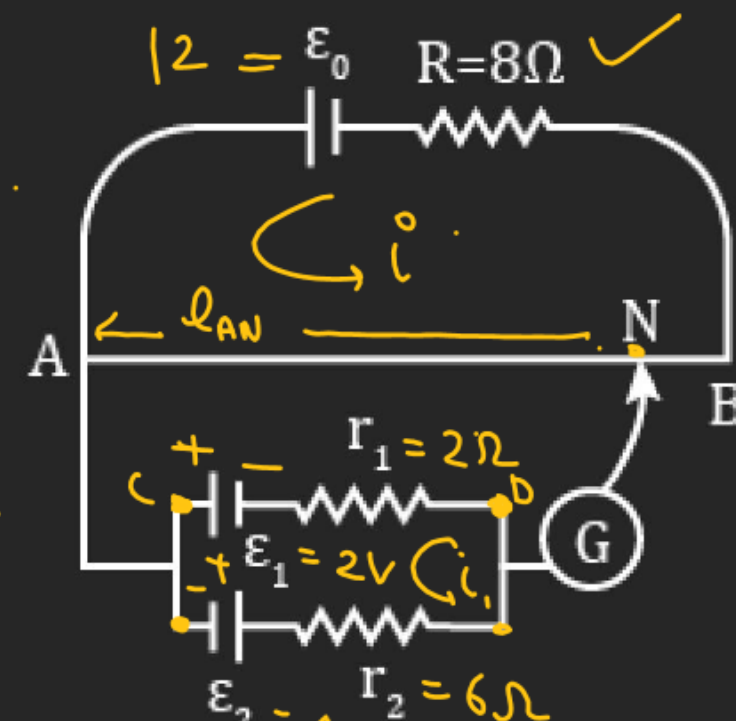
$$\Rightarrow 2l_{AN} = \frac{1}{2}$$

$$\frac{R_{AB}}{L_{AB}} = 4\Omega/\text{m}, \quad L_{AB} = 4\text{m.}$$

$$2 + 4 - 8i_1 = 0$$

$$\frac{6}{8} = i_1$$

$$i_1 = \frac{3}{4}\text{ Amp.}$$



$$l_{AN} = \frac{1}{4} \times 100\text{ cm}$$

$$= 25\text{ cm}$$

$$V_C - \varepsilon_1 + i_1 r_1 = V_D$$

$$V_C - V_D = \varepsilon_1 - i_1 r_1 = 2 - \frac{3}{4} \times 2$$

$$= \frac{1}{2} V_{\text{bal.}}$$

At the time of Null deflection

# CURRENT ELECTRICITY

## Potentiometer and Meter Bridge

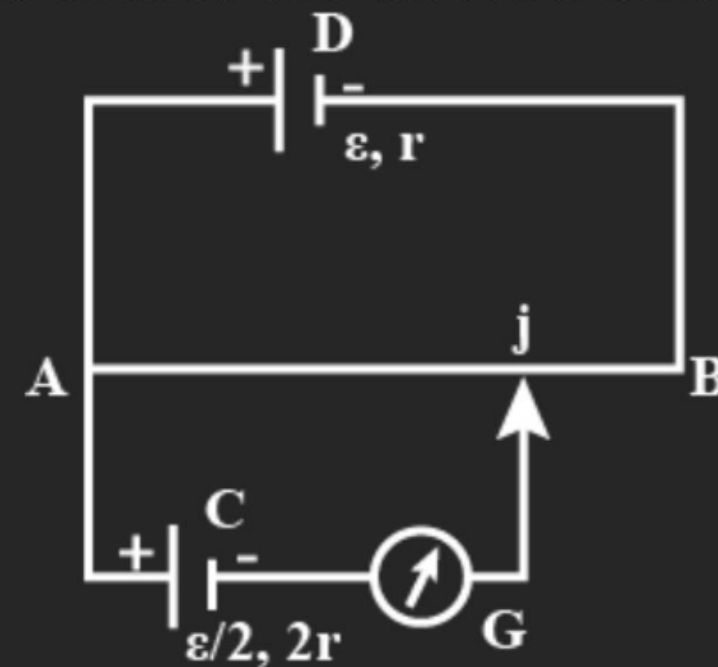
**Q.8** In the figure, the potentiometer wire AB of length  $L$  and resistance  $9r$  is joined to the cell D of emf  $\mathcal{E}$  and internal resistance  $r$ . The cell C's emf is  $\mathcal{E}/2$  and its internal resistance is  $2r$ . The galvanometer G will show no deflection when the length AJ is:

(A)  $\frac{4L}{9}$

(B)  $\frac{5L}{9}$  ✓

(C)  $\frac{7L}{18}$

(D)  $\frac{11L}{18}$





# CURRENT ELECTRICITY

## Potentiometer and Meter Bridge

**Q.9** In the arrangement shown in figure when the switch  $S_2$  is open, the galvanometer shows no deflection for  $l = L/2$ . When the switch  $S_2$  is closed, the galvanometer shows no deflection for  $l = 5L/12$ . The internal resistance (r) of 6 V cell, and the emf  $\mathcal{E}$  of the other battery are respectively:

(A)  $3\Omega, 8\text{ V}$

(B)  $2\Omega, 12\text{ V}$  ✓

(C)  $2\Omega, 24\text{ V}$

(D)  $3\Omega, 12\text{ V}$

When  $S_2$  open

$$6 = \frac{\mathcal{E}}{L} \times \frac{L}{2} \Rightarrow \mathcal{E} = 12\text{ V}$$

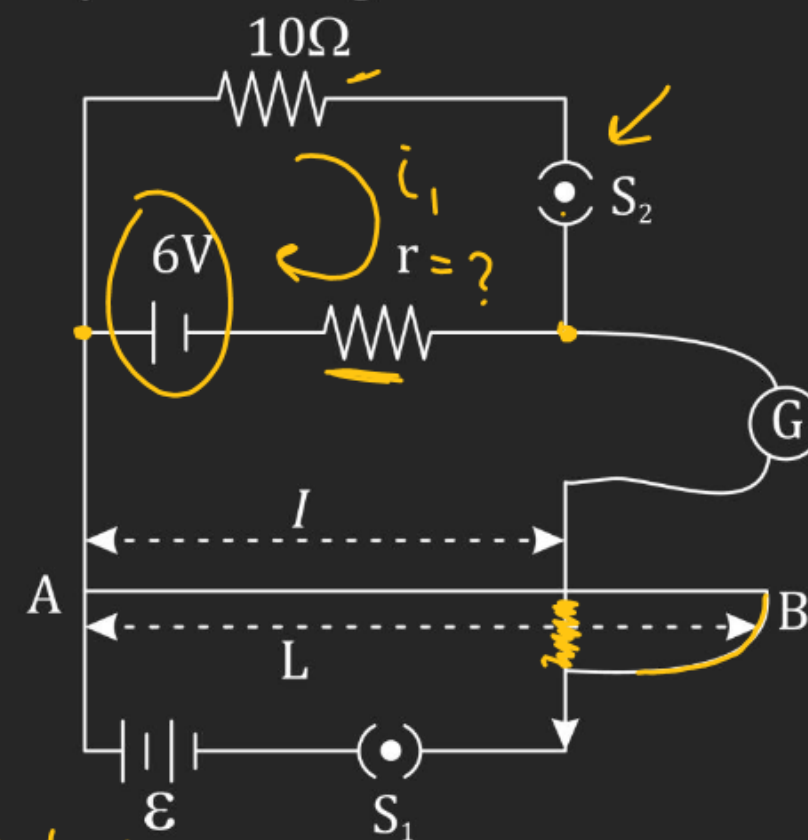
Potential gradient =  $\left(\frac{\mathcal{E}}{L}\right)$

$$l_1 = \left(\frac{6}{10+r}\right)$$

When  $S_2$  closed.

$$6 - l_1 r = \frac{\mathcal{E}}{L} \times \frac{5L}{12} = \frac{5\mathcal{E}}{12}$$

$$6 - \frac{6r}{10+r} = 5 \Rightarrow \frac{6r}{10+r} = 1 \Rightarrow 6r = 10+r \Rightarrow 5r = 10 \Rightarrow r = 2\Omega$$



# CURRENT ELECTRICITY

## Potentiometer and Meter Bridge

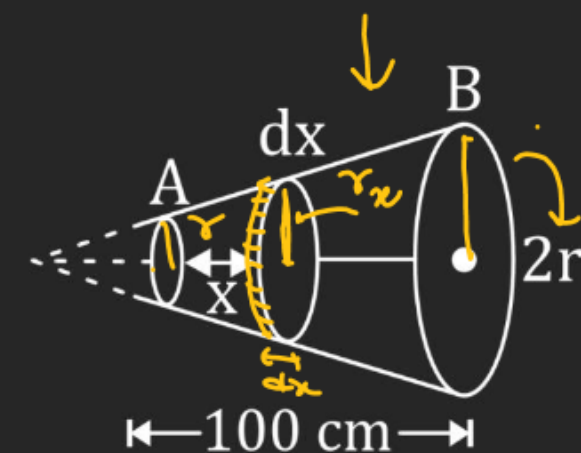
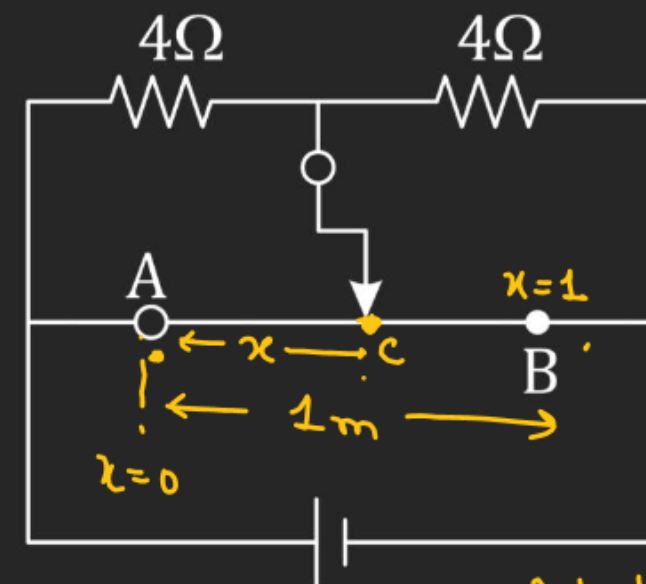
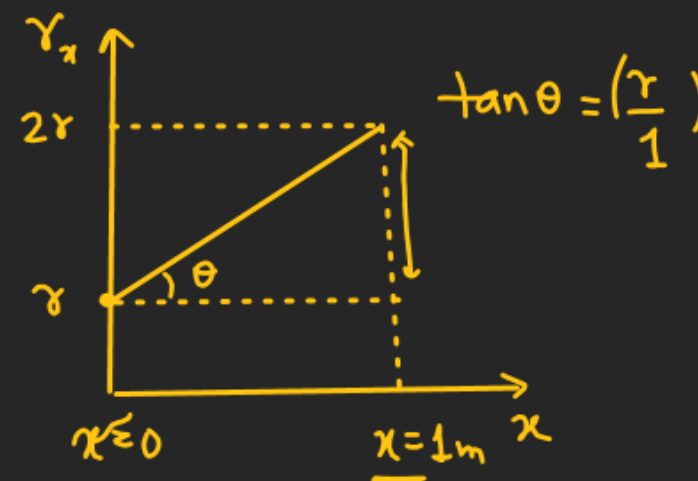
**Q.12** The wire AB of a meter bridge changes linearly from radius  $r$  to  $2r$  from left end to right end. Where should the free end of the galvanometer be connected on AB so that the deflection in the galvanometer is zero?

function of distance with  $x$

radius at  $x$   $\rightarrow r_x = (r + \frac{r}{1}x)$

$$r_x = r(1+x)$$

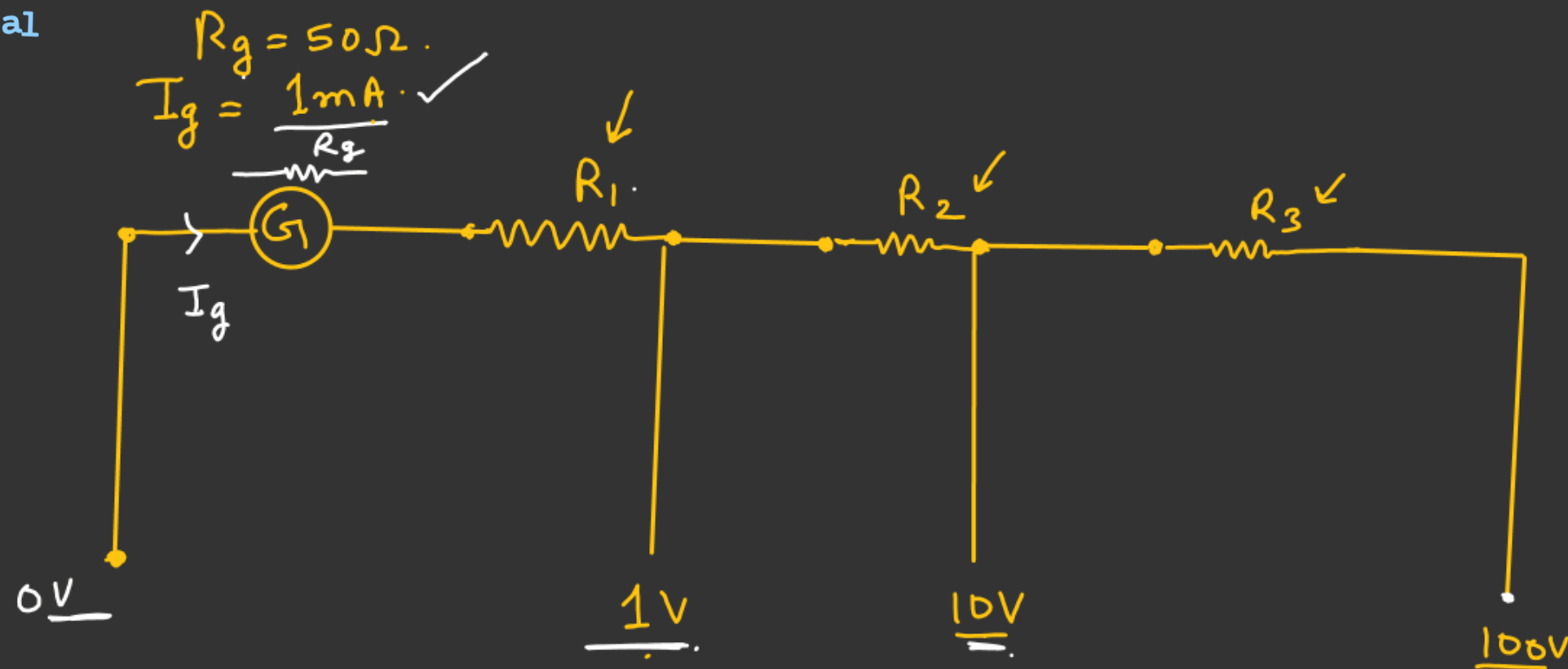
$$dR = \left( \frac{\rho dx}{\pi r_x^2} \right)$$



At the time of Null deflection

$$\frac{R_{AC}}{4} = \frac{R_{CB}}{4} \Rightarrow R_{AC} = R_{CB}$$

#



To measure the voltage  $1V$ ,  $10V$ , &  $100V$ . find  $R_1$ ,  $R_2$  &  $R_3$  to be added to the galvanometer

$$I_g(R_g + R_1) = 1V$$

$$R_g + R_1 = \frac{1}{I_g} = \frac{1}{1 \times 10^{-3}}$$

$$R_1 = 1000 - R_g$$

$$R_1 = 1000 - 50$$

$$R_1 = \underline{950\Omega} \quad \checkmark$$

For  $10V$

$$I_g(R_g + R_1 + R_2) = 10$$

$$I_g(R_g + R_1) + I_g R_2 = 10$$

$$I_g R_2 = 10 - 1 = 9$$

$$\underline{R_2} = \frac{9}{I_g} = \underline{9000\Omega} = \underline{9 \times 10^3\Omega}$$

For  $100V$

$$I_g(R_g + R_1 + R_2 + R_3) = 100$$

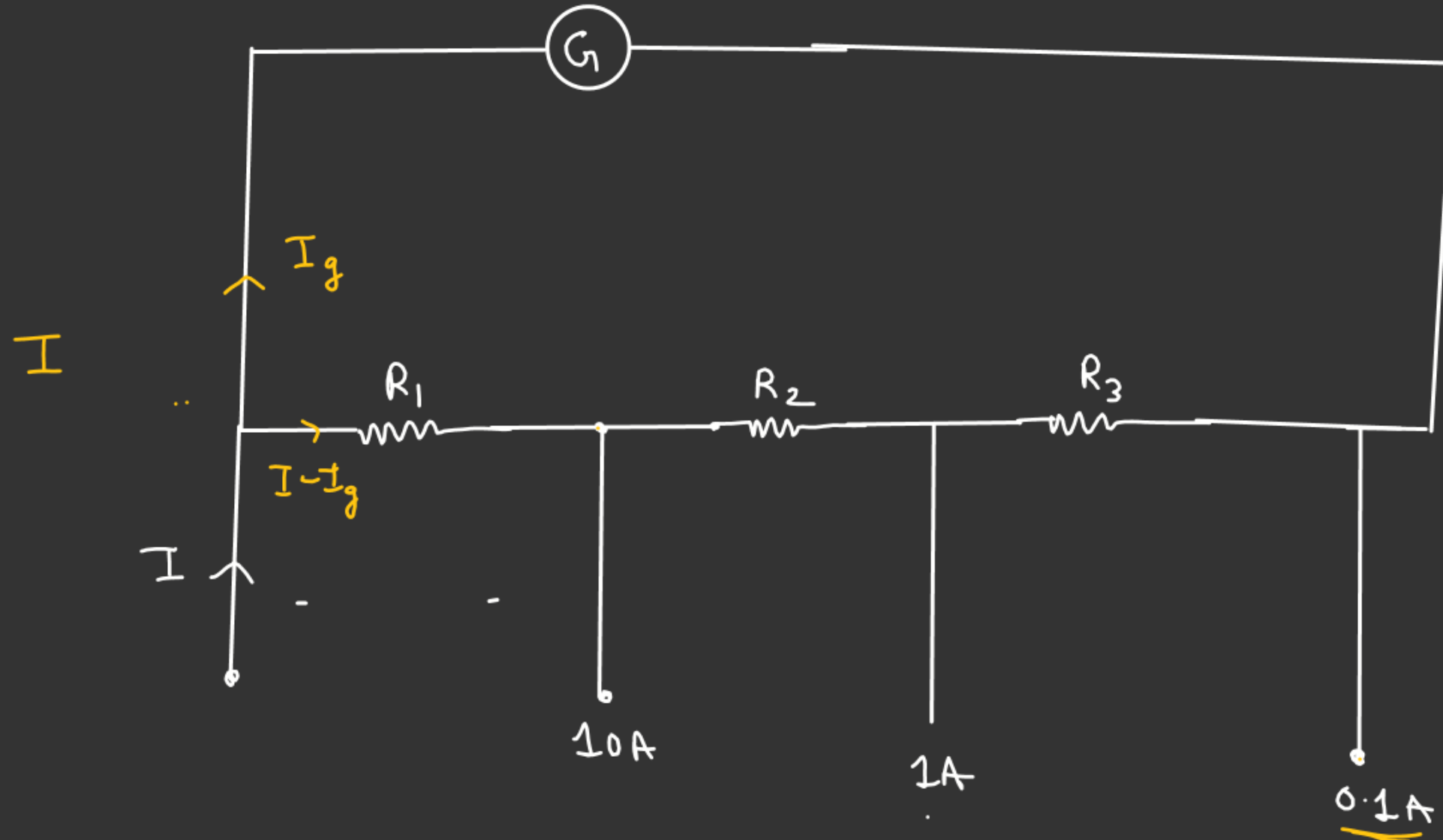
$$I_g(R_g + R_1 + R_2) + I_g R_3 = 100$$

$$10 + I_g R_3 = 100$$

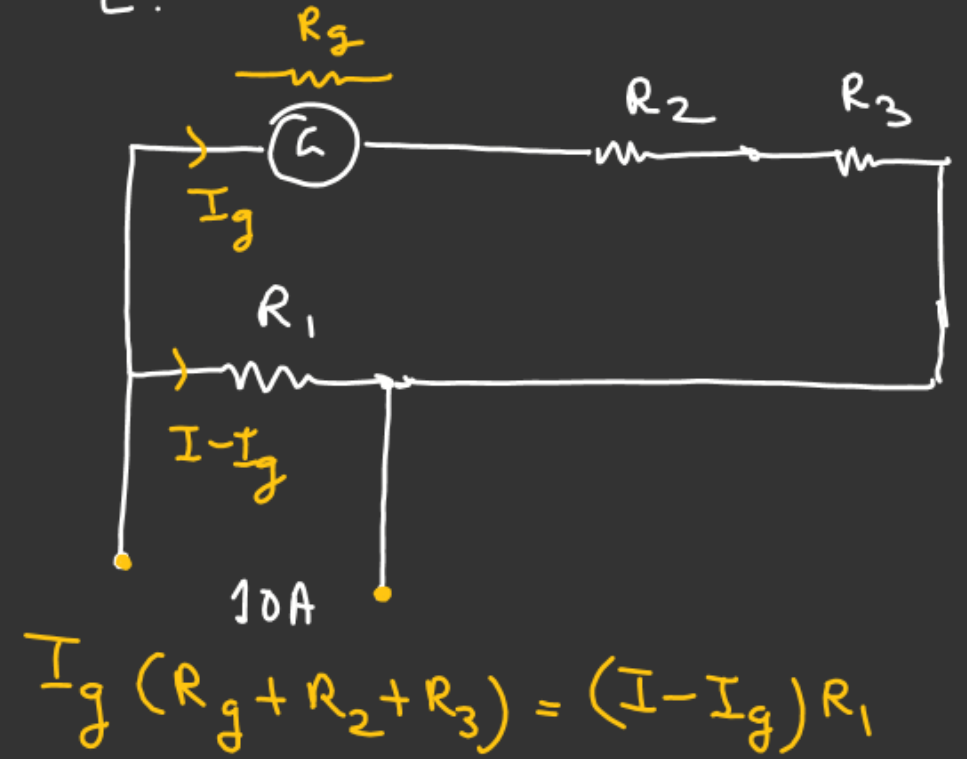
$$R_3 = \frac{90}{I_g} = \frac{90}{10^{-3}} = \underline{9 \times 10^4\Omega}$$

$$R_g = 50\Omega$$

$$I_g = 1\text{mA}$$

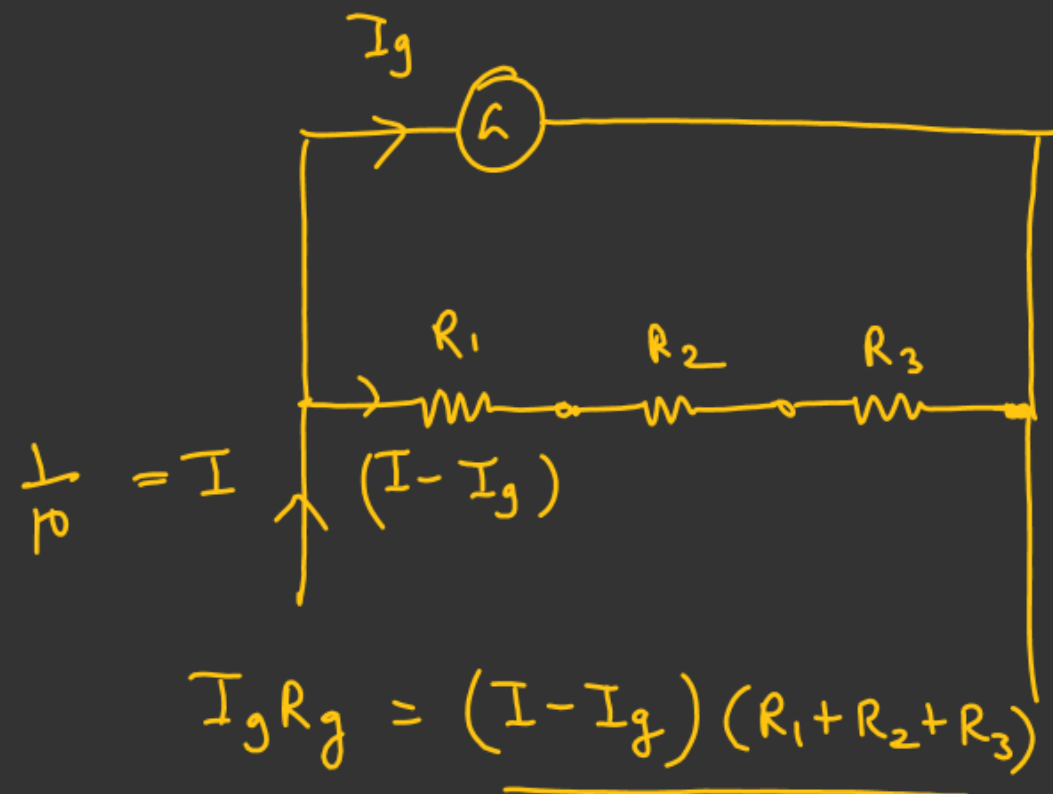


For this galvanometer to measure current  $0.1\text{A}$ ,  $1\text{A}$  &  $10\text{Amp}$ . find  $R_1$ ,  $R_2$  &  $R_3$ .



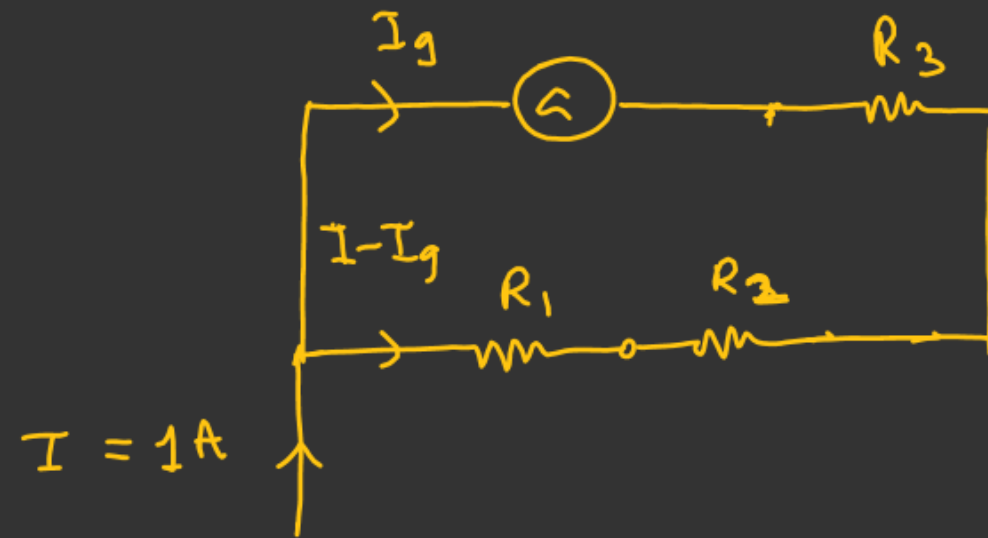
$$I_g (R_g + R_2 + R_3) = (I - I_g) R_1$$



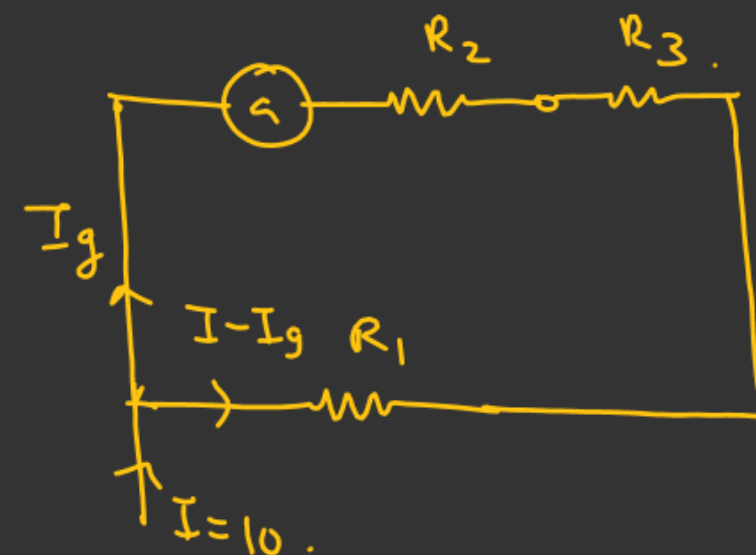


$$R_1 + R_2 + R_3 = \frac{I_g R_g}{I - I_g} = \frac{\frac{1}{1000} \times 5}{\left(\frac{1}{10} - \frac{1}{1000}\right)}$$

$$R_1 + R_2 + R_3 = \frac{5}{\frac{990}{1000}} = \frac{5}{99} \Omega$$



$$I_g(R_3 + R_g) = (I - I_g)(R_1 + R_2) \quad \text{--- (2)}$$



$$(I - I_g) R_1 = I_g(R_2 + R_3) \quad \text{--- (3)}$$

$$R_1, R_2 \text{ \& } R_3 = ??$$



$$\gamma_n = r(1+x)$$

$$dR = \frac{p dx}{\pi \gamma_n^2}$$

$$\int_0^{R_{AC}} dR = \frac{p}{\pi r^2} \int_0^x \frac{dx}{(1+x)^2} \quad /$$

$$R_{AC} = \frac{p}{\pi r^2} \left[ -\frac{1}{(1+x)} \right]_0^x$$

$$R_{AC} = \frac{p}{\pi r^2} \left[ -\frac{1}{1+x} + 1 \right]$$

$$R_{AC} = \frac{p}{\pi r^2} \left[ \frac{x}{1+x} \right] \checkmark$$

$$\int_0^{R_{CB}} dR = \frac{p}{\pi r^2} \int_0^1 \frac{dx}{(1+x)^2}$$

$$R_{CB} = \frac{p}{\pi r^2} \left[ -\frac{1}{1+x} \right]_0^1 \textcircled{1}$$

$$= \frac{p}{\pi r^2} \left[ -\frac{1}{2} + \frac{1}{1+x} \right]$$

$$= \frac{p}{\pi r^2} \left[ \frac{-1-x+2}{2(1+x)} \right]$$

$$= \frac{p}{\pi r^2} \frac{(1-x)}{2(1+x)} \checkmark$$

For Null deflection

$$R_{AC} = R_{CB}$$

$$\frac{x}{1+x} = \frac{1-x}{2(1+x)}$$

$$2x = 1-x$$

$$3x = 1$$

$$\boxed{x = \frac{1}{3}} \checkmark$$

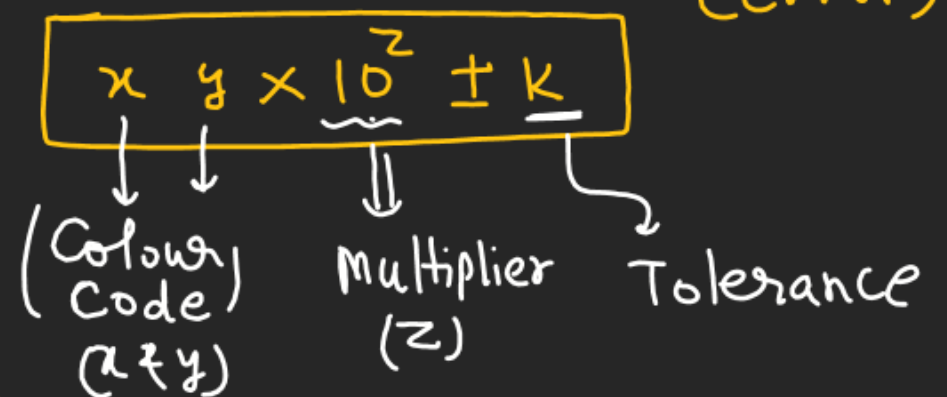
	Color	Color Code	Multiplier	Tolerance (%)
B ←	black	0	$\times 1$	$\Rightarrow$ (error)
B ←	brown	①	$\times 10^1$	1
R ←	red	2	$\times 100 / 10^2$	2
O ←	orange	3	$\times 1 \text{ K} / 10^3$	
Y ←	yellow	4	$\times 10 \text{ K} / 10^4$	
G ←	green	5	$\times 100 \text{ K} / 10^5$	0.5
B ←	blue	⑥	$\times 1 \text{ M} / 10^6$	0.25
V ←	violet	7	$\times 10 \text{ M} / 10^7$	0.1
G ←	grey	8	$\times 100 \text{ M} / 10^8$	0.05
W ←	white	9	$\times 1 \text{ G} / 10^9$	
	gold		$\times 0.1$	⑤
	silver		$\times 0.01$	10
	none			20

## Colour Coding

First two colour  $\rightarrow$  (colour code)

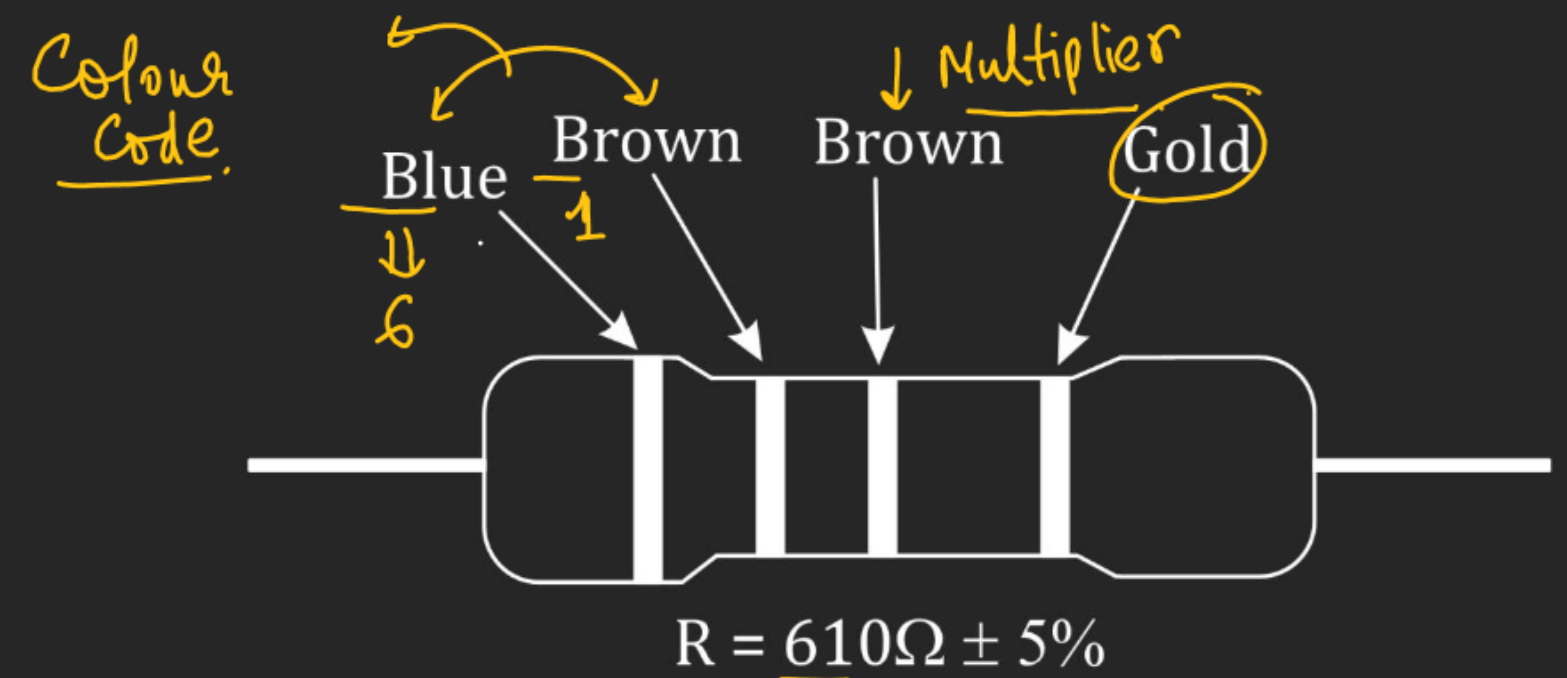
Next colour  $\rightarrow$  Multiplier

Last colour  $\rightarrow$  Tolerance (error)



[ B B R O Y of G r e a t B r e t a i n   
 have v e r y G o o d W i f e .

[ B r i g h t B o y s R a c e O v e r Y o u n g  
G i r l s B u t V o i e t G e n e r a l l y W i n s



$$R = (61) \times 10^1 \times \pm 5\%$$

9th July (Jee Mains)  
Test Syllabus.

60% ← [Capacitor  
Electrical Instrument  
Current Electricity  
Electrostatics]

40% ←

