

ELECTROSTATICS

Study of ~~rest~~ Charge

Charge \rightarrow It is the basic property of a particle due to which it produces or experience Electric and magnetic effect.

S.I Unit:- Coulomb \rightarrow

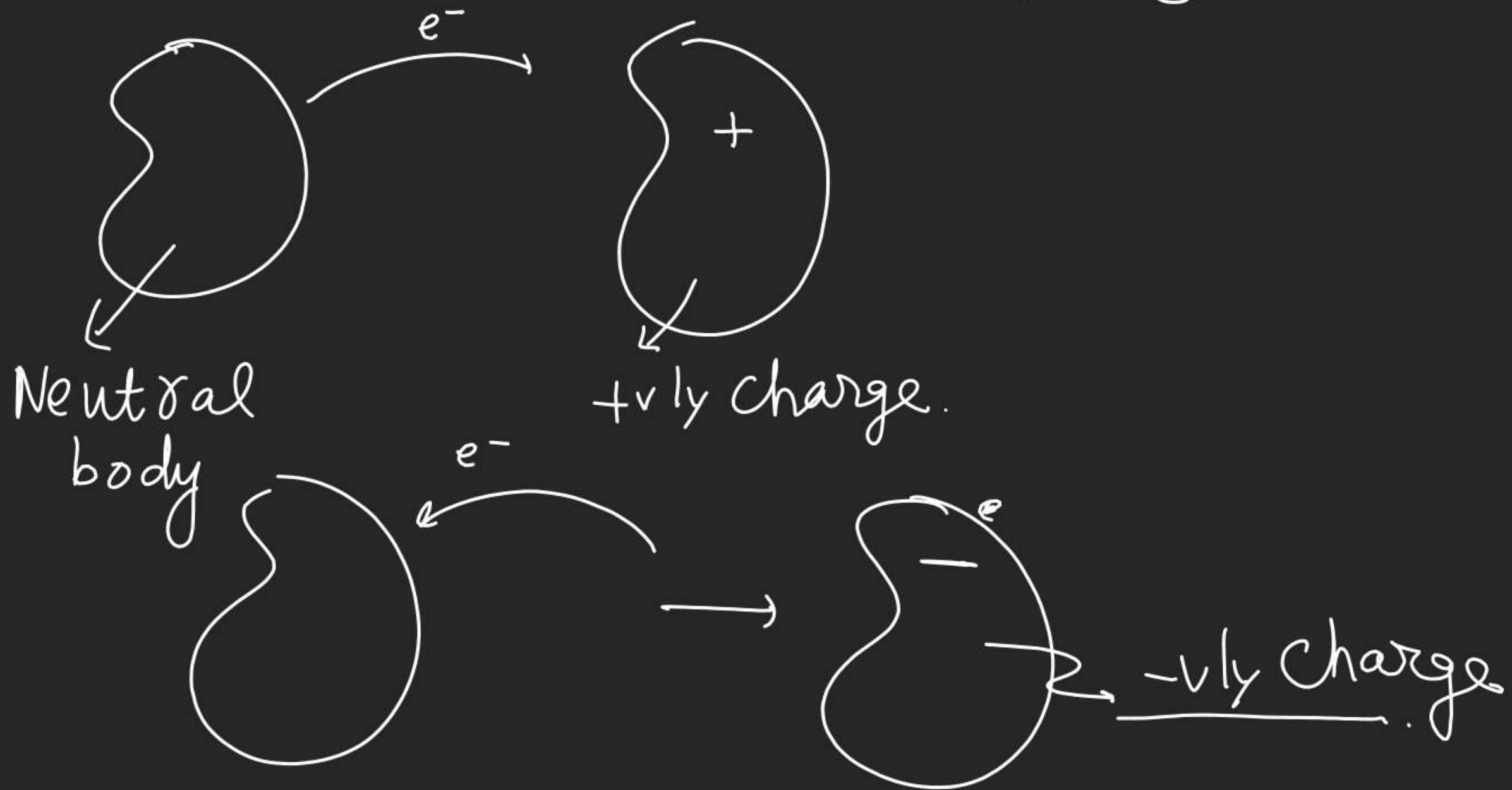
C.G.S Unit \rightarrow Electrostatic Unit \rightarrow e.s.u

$$1C = 3 \times 10^9 \text{ esu} \checkmark$$

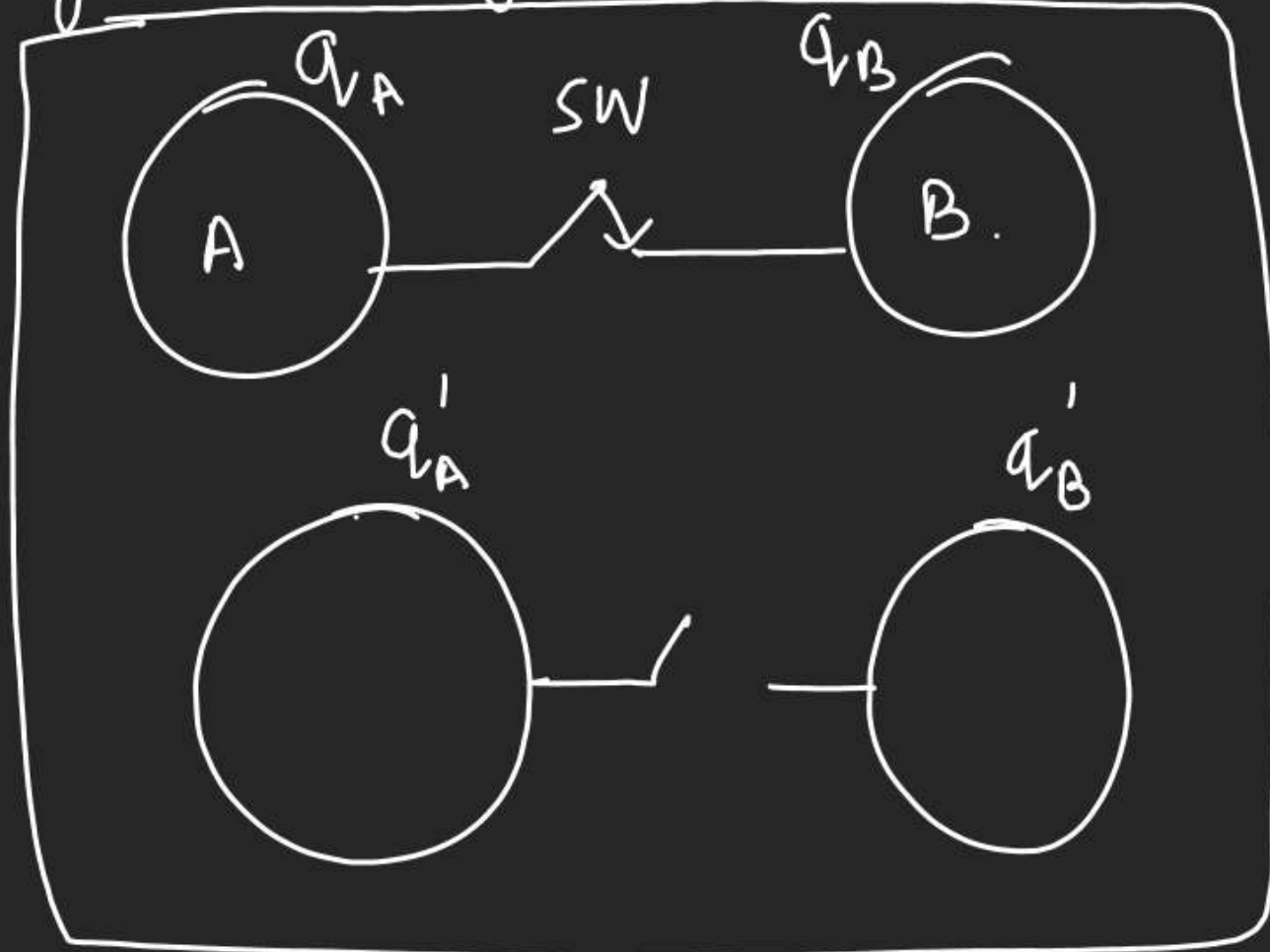
$$\begin{array}{l} 1C \rightarrow \\ \left[\begin{array}{l} 1\mu C \rightarrow 10^{-6} C \\ 1nC \rightarrow 10^{-9} C \\ 1pC \rightarrow 10^{-12} C \\ 1m \rightarrow 10^{-3} C \end{array} \right] \end{array}$$

Properties of Charge

→ It exist in two form — $\left[\begin{array}{l} +ve \\ -ve \end{array} \right.$



Charge always conserved for an isolated system



$$q_A + q_B = q'_A + q'_B$$

→ Charge is always quantized:-

↳ Charge on any body is integral multiple of fundamental charge i.e. Charge of an electron or proton

$$Q = \pm ne$$

$$n \in \mathbb{I}^+$$

$$\left[\begin{array}{l} 1e^- = -1.6 \times 10^{-19} \text{ C} \\ 1p^+ \rightarrow +1.6 \times 10^{-19} \text{ C} \end{array} \right]$$

(*) Charge always associated with mass.

(*) Charge of a body doesn't depend on the Velocity of body or not on the frame of reference from which it is seen.

but mass is frame dependent

$n \in \mathbb{I}^+$
 $\hookrightarrow \underline{1, 2, 3, 4}$

$$m = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$v \rightarrow$ Speed of mass

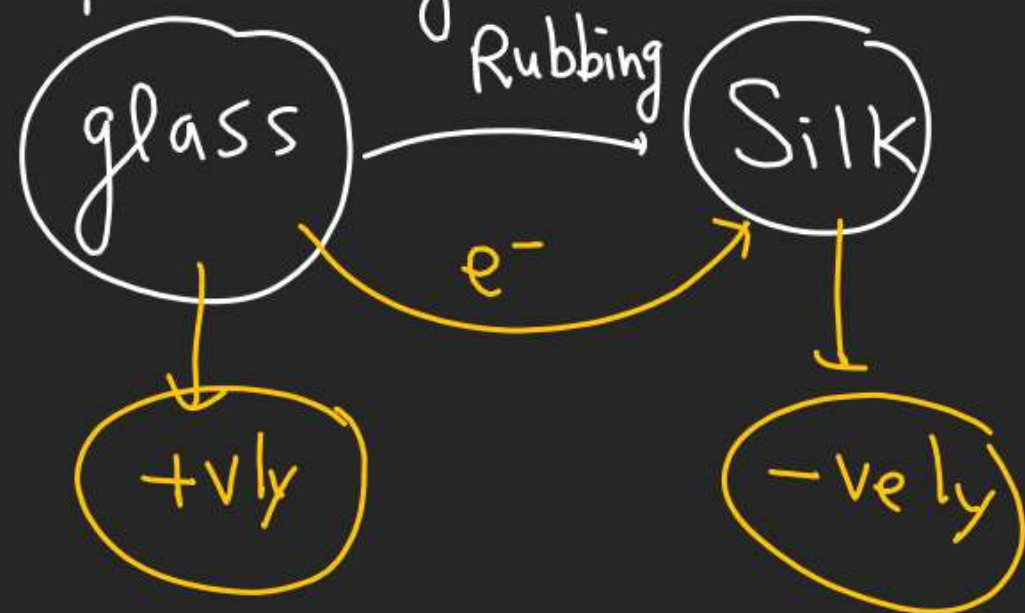
$c \rightarrow$ Speed of light

$c \rightarrow \underline{3 \times 10^8 \text{ m/s}}$

→ How Charge has been produced

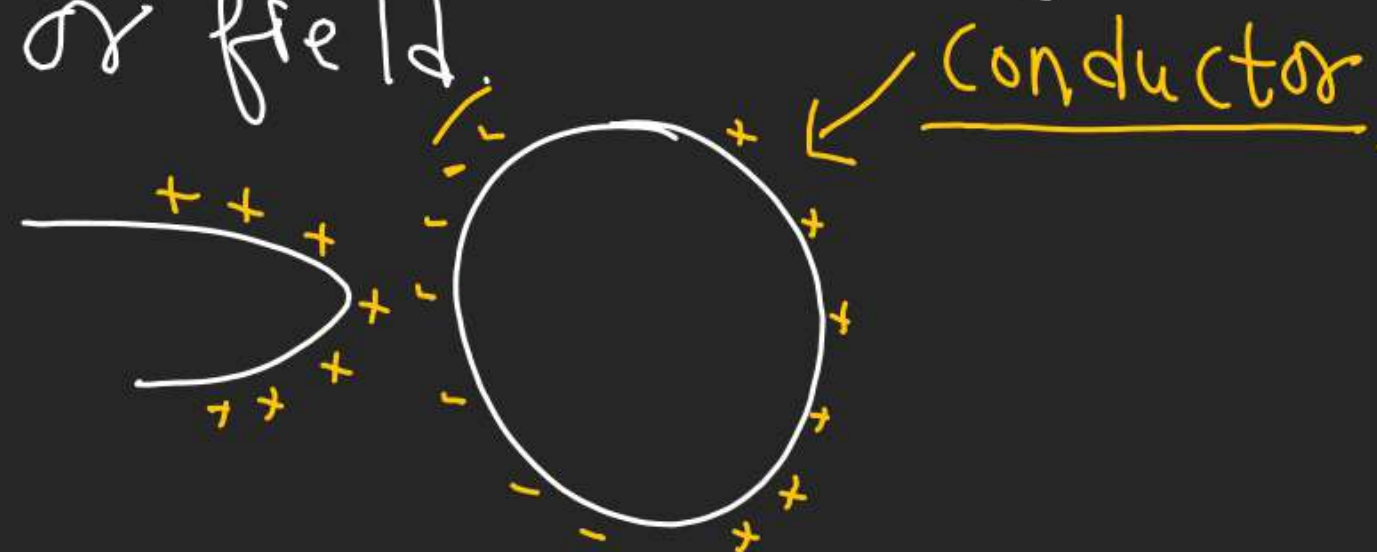
Friction

↳ Actual transfer of Charge.



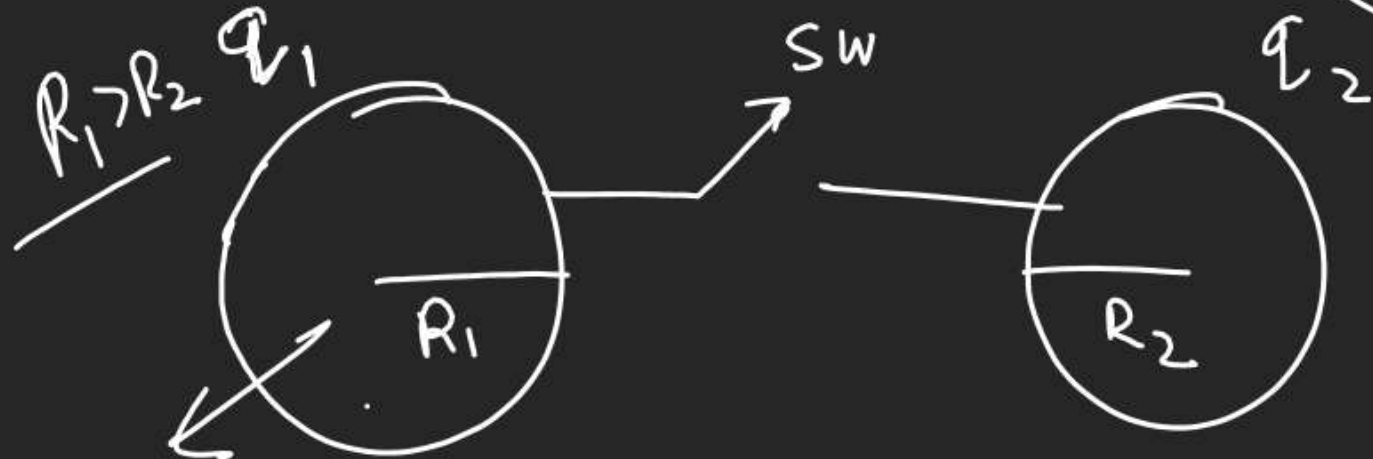
Induction ✓

↳ It is redistribution of Charge in a body Under the influence of Some external Charge or field.

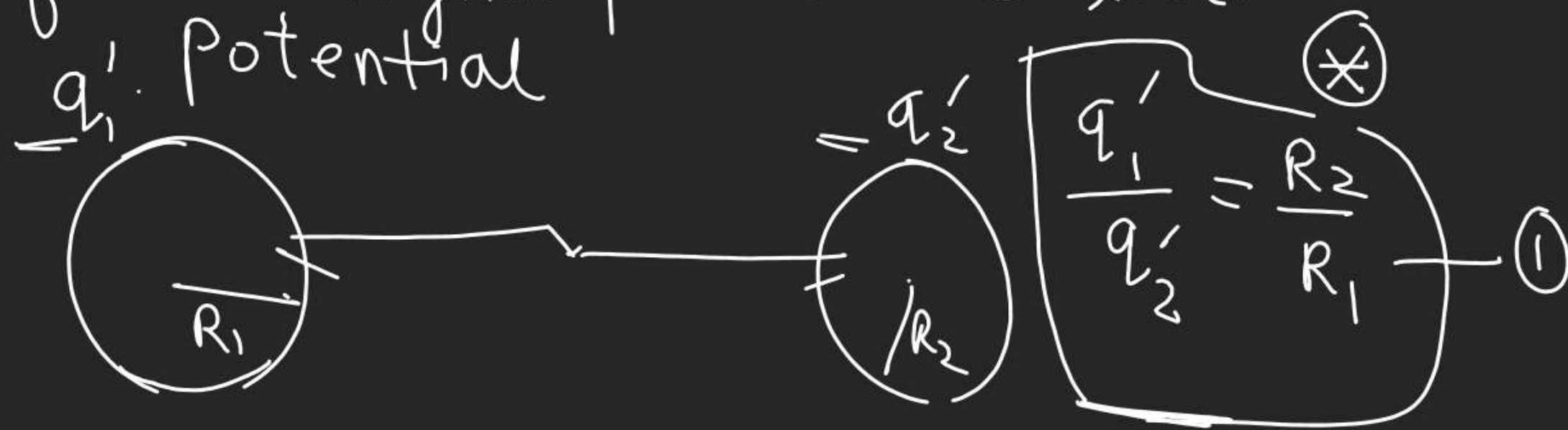


Conduction :-

Potential $V = \frac{kq}{r}$



⇒ Charge transfer takes place from higher potential to lower q_1 potential



$$q_1 + q_2 = q_1' + q_2' \quad (2)$$

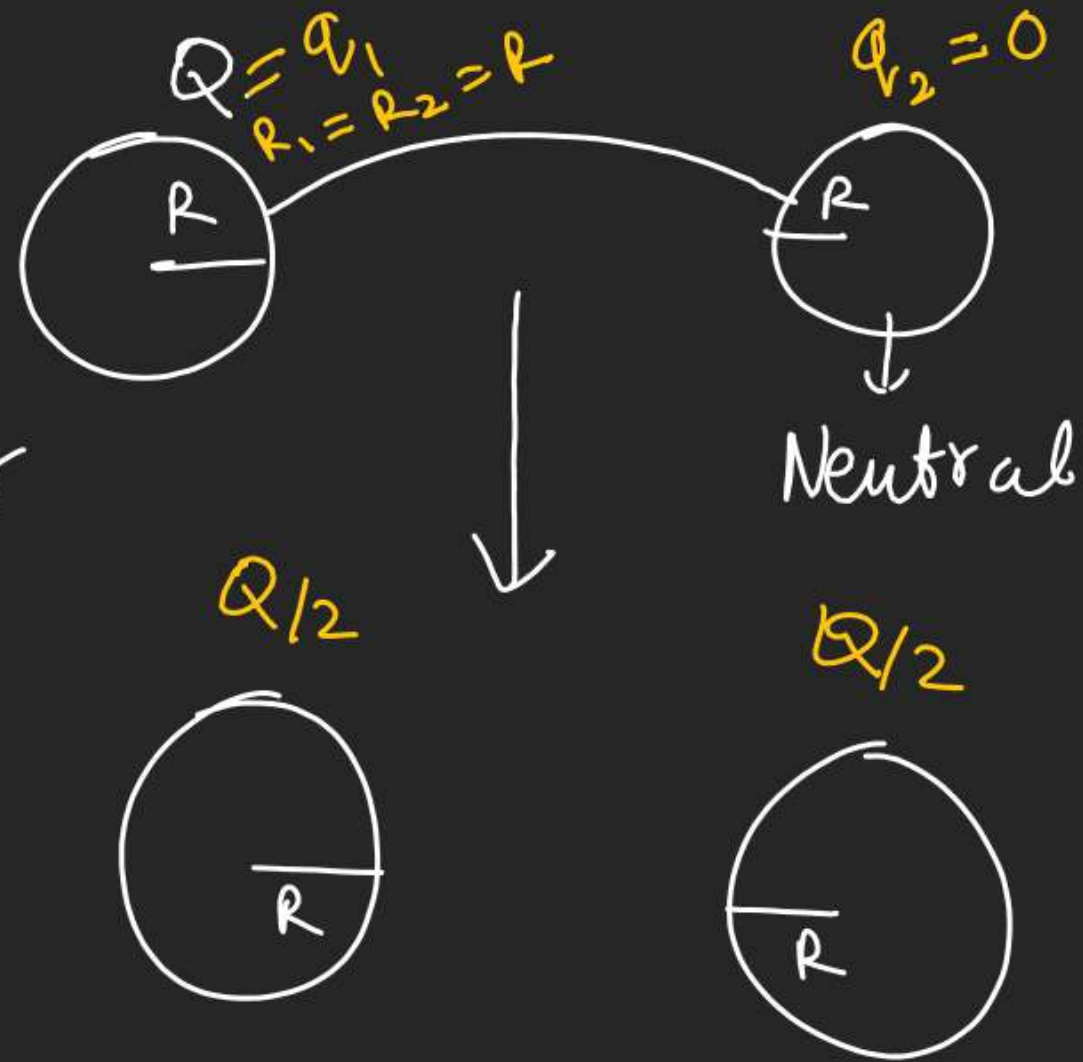
$$q_1 + q_2 = \left(\frac{R_2}{R_1} + 1\right) q_2'$$

$$q_2' = \frac{R_1 (q_1 + q_2)}{R_1 + R_2}$$

$$q_1' = \frac{R_2 (q_1 + q_2)}{R_1 + R_2}$$

$$\frac{q_1'}{q_2'} = \frac{R_2}{R_1} \quad (1)$$

#



After
Connecting

$$q_1' = \frac{R_2 (q_1 + q_2)}{R_1 + R_2} = \frac{Q}{2}$$

$$q_2' = \frac{R_1 (q_1 + q_2)}{R_1 + R_2} = \frac{Q}{2}$$

ELECTROSTATICS

↳ Influence of Charge around its Surrounding

→ Rest Charge

(+q)

Rest charge have influence around its surrounding called Electric field.

→ (+q)

$V = C$

↳ It has two influence
→ Electric field
→ Magnetic field }

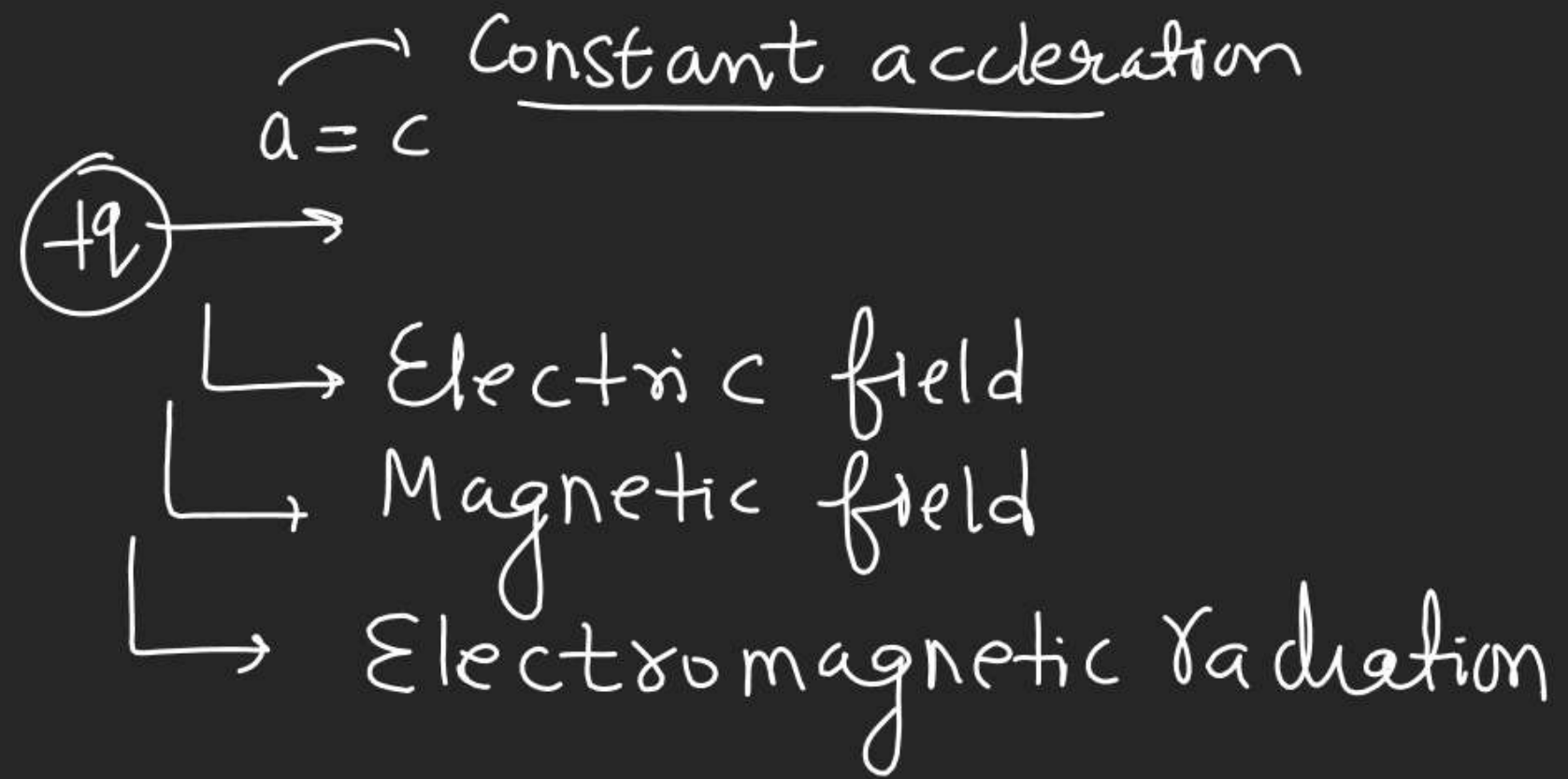
Field

It is influence of certain things around its surrounding

(+m)

→ Gravitational field

(A).



ELECTROSTATICS

→ Coulomb's Law :-

↳ According to Coulomb:-

The Electrostatic force of interaction b/w two Charge particle is → ① directly proportional to product of the magnitud^{-e} of the charges.



$$|F_{1/2}| = |F_{2/1}| \propto \frac{|q_1| |q_2|}{r^2}$$

② Inversely proportional to Square of the distance b/w them.

$$|F_{1/2}| = |F_{2/1}| = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$\epsilon_0 \rightarrow$ [Permittivity in free space]
or Vacuum.

Limitation

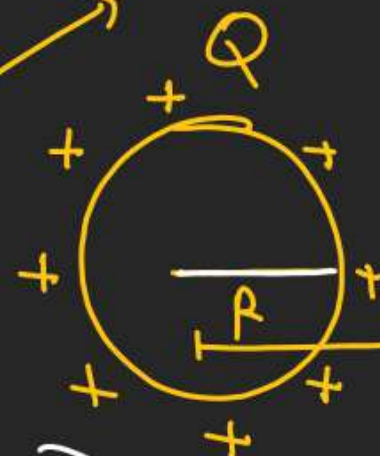
- Applicable for point Charge.

Properties of Coulomb's law

- Like Charge always repel each other and unlike charges attract each other.

Point Charge

$$d \gg R$$



Dimension of body where Charge is kept is much smaller than the distance where its influence is calculated

ELECTROSTATICS

(*)

Coulomb's law in certain medium

Medium (ϵ_m) →

$$F_{\text{medium}} = \frac{F_{\text{air}}}{\epsilon_r}$$

$+q_1$ ← $F'_{1/2}$

$+q_2$ → $F'_{2/1}$

← r →

$$|F'_{1/2}| = |F'_{2/1}| = \frac{1}{4\pi\epsilon_m} \frac{q_1 q_2}{r^2}$$

$$|F'_{1/2}| = |F'_{2/1}| = \frac{1}{4\pi\epsilon_0 \epsilon_r} \frac{q_1 q_2}{r^2}$$

$$|F'_{1/2}| = |F'_{2/1}| = \frac{|F_{1/2}|}{\epsilon_r}$$

✓ ϵ_0 → Property of a medium

✓ ϵ_m = Permittivity of a medium.

ϵ_r = Relative Permittivity

$\epsilon_r = \frac{\text{Permittivity in medium}}{\text{Permittivity in air}}$

$\epsilon_r = \frac{\epsilon_m}{\epsilon_0}$

$$\epsilon_m = \epsilon_0 \epsilon_r$$

$$\epsilon_r \rightarrow \textcircled{K}$$

Relative permittivity

or

Dimension formula

Dielectric Constant

$$F = ma$$

$$= \underline{MLT^{-2}}$$

$$\epsilon_0 = \left(\frac{1}{4\pi} \right) \frac{q_1 q_2}{r^2}$$

$$[\epsilon_0] = \frac{A^2 T^2}{MLT^{-2} \cdot L^2}$$

$$[\epsilon_0] = [M^{-1} L^{-3} T^4 A^2]$$

$$I = \frac{q}{t}$$

$$q = It$$

$$[q] = [AT]$$

$$F = \left(\frac{1}{4\pi\epsilon_0} \right) \frac{q_1 q_2}{r^2}$$

K = Constant

$$K = 9 \times 10^9 \frac{N-m^2}{C^2}$$

$$\epsilon_0 = \frac{8.85 \times 10^{-12} C^2}{N-m^2}$$