

1. If  $\sin \alpha = \frac{3}{5}$  and  $\cos \beta = \frac{9}{41}$ , find the value of  $\sin (\alpha - \beta)$  and  $\cos (\alpha + \beta)$ .
2. If  $\sin \alpha = \frac{15}{53}$  and  $\sin \beta = \frac{33}{65}$ , find the values of  $\sin (\alpha - \beta)$  and  $\sin (\alpha + \beta)$ .
3. If  $\sin \alpha = \frac{15}{17}$  and  $\cos \beta = \frac{12}{13}$ , find the values of  $\sin (\alpha + \beta)$ ,  $\cos (\alpha - \beta)$ , and  $\tan (\alpha + \beta)$ .
4. Prove that  $\cos (45^\circ - A)\cos (45^\circ - B) - \sin (45^\circ - A)\sin (45^\circ - B) = \sin (A + B)$
5. Prove that  $\sin (45^\circ + A)\cos (45^\circ - B) + \cos (45^\circ + A)\sin (45^\circ - B) = \cos (A - B)$
6.  $\frac{\sin (A-B)}{\cos A \cos B} + \frac{\sin (B-C)}{\cos B \cos C} + \frac{\sin (C-A)}{\cos C \cos A} = 0$
7.  $\sin 105^\circ + \cos 105^\circ = \cos 45^\circ$
8.  $\sin 75^\circ - \sin 15^\circ = \cos 105^\circ + \cos 15^\circ$
9.  $\cos \alpha \cos (\gamma - \alpha) - \sin \alpha \sin (\gamma - \alpha) = \cos \gamma$
10.  $\cos (\alpha + \beta) \cos \gamma - \cos (\beta + \gamma) \cos \alpha = \sin \beta \sin (\gamma - \alpha)$
11.  $\sin (n+1) A \sin (n-1) A + \cos (n+1) A \cos (n-1) A = \cos 2A$
12.  $\sin (n+1) A \sin (n+2) A + \cos (n+1) A \cos (n+2) A = \cos A$

Answer Key

1.  $-\frac{133}{205}; -\frac{84}{205}$
2.  $\frac{1596}{3445}; \frac{3444}{3445}$
3.  $\frac{220}{221}; \frac{171}{221}; \frac{220}{21}$