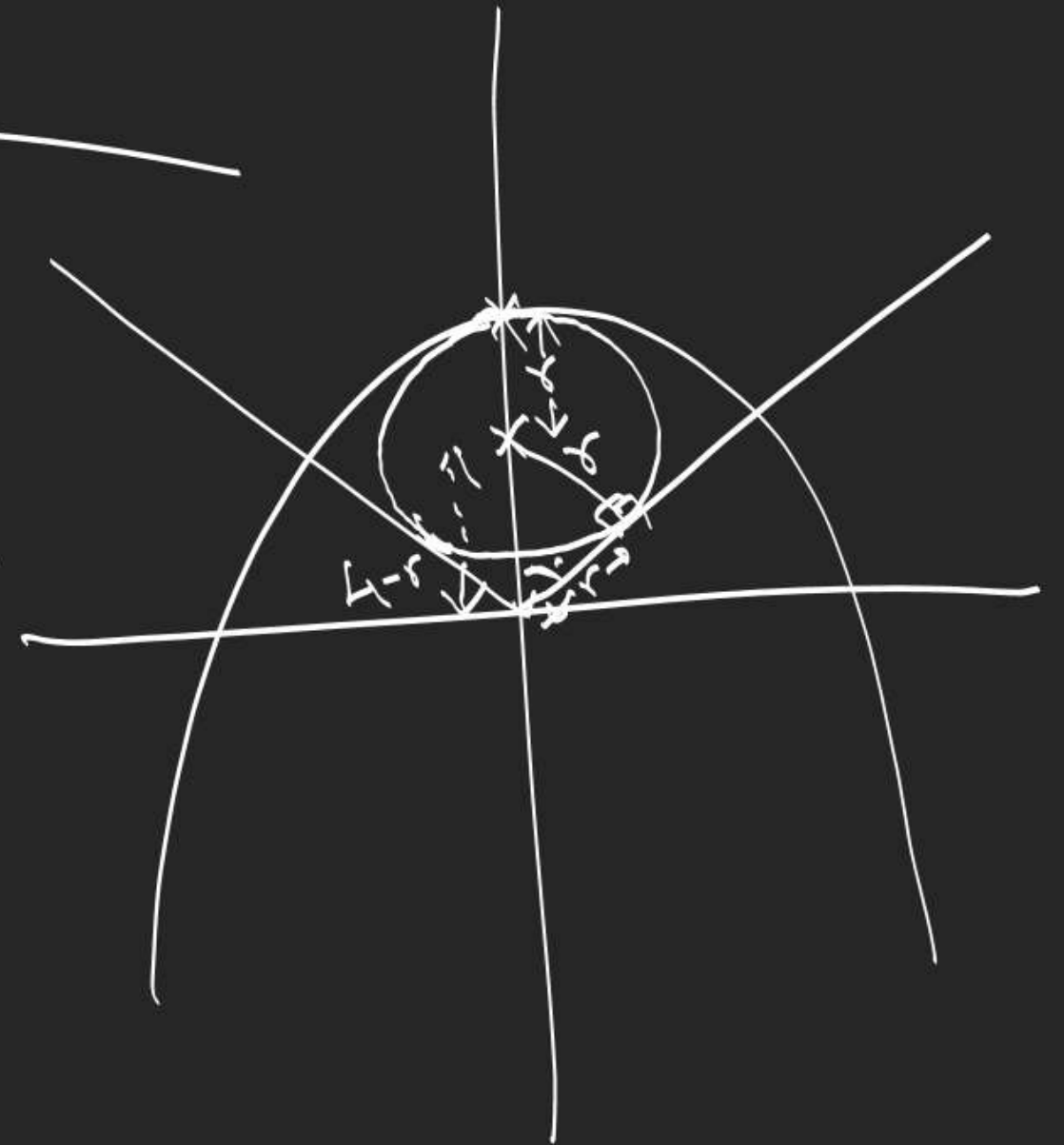


$$r\sqrt{2} = 4 - r$$



Permutation

number of arrangements

A B

B A

Combination

selection or collection

AB

BA

$P(n, n) = {}^n P_n$ = no. of permutation of 'n' distinct
 objects taken all at a time.
 $= n!$

n boys

— — — — — — — — — —
 — — — — — — — — — — n seats
 $n \times (n-1) \times (n-2) \times (n-3) \times \dots \times 1$

$P(n, r) = {}^n P_r$ = no. of permutation of 'n' distinct objects taken 'r' at a time. ($0 \leq r \leq n$)

n Boys

$${}^n P_r = \frac{n!}{(n-r)!}$$

r seats

$${}^n P_r = n \times (n-1) \times (n-2) \times (n-3) \cdots \cdots (n-(r-1)) = n(n-1) \cdots \cdots (n-r+1)(n-r)(n-r-1) \cdots \cdots \times 2 \times 1$$

Arrange 'n' boys in r seats

$$= \frac{n!}{(n-r)!}$$

$$\frac{n(n-1) \cdots \cdots (n-r+1)(n-r)(n-r-1) \cdots \cdots \times 2 \times 1}{(n-r)(n-r-1) \cdots \cdots \times 2 \times 1}$$

Find no. of ways to arrange 6 boys
in 10 seats.

no. of permutation of 'n' boys in 'r' places
 $r > n \implies {}^r P_n$
 — — — — —
 10 seats

$$10 \times 9 \times 8 \times 7 \times 6 \times 5 = \frac{10!}{4!}$$

${}^nC_r = C(n, r) = \text{no. of combinations of 'n' distinct objects taken 'r' at a time } (0 \leq r \leq n)$

$r! + r! + r! + \dots + r!$

n Boys
 $\boxed{\checkmark B_1 B_2 \dots B_r} \rightarrow r!$ (no. of selection of r boys) times
 $\boxed{\checkmark B_1 B_3 B_4 \dots B_r B_{r+1}} \rightarrow r!$
 r seats

Find no. of ways to arrange ' n ' boys in r seats

$$\Rightarrow {}^nP_r = {}^nC_r \times r!$$

$${}^nC_r = \frac{{}^nP_r}{r!} = \frac{n!}{(n-r)! r!}$$