

(5) Prod \rightarrow Sum/Diff

(6) $3 \sin \alpha = 5 \sin \beta$

$$\frac{\sin \alpha}{\sin \beta} = \frac{5}{3} \quad (\&D)$$

$$\frac{\sin \alpha + \sin \beta}{\sin \alpha - \sin \beta} = \frac{5+3}{5-3} = \frac{8}{2} = 4$$

$$\frac{2 \sin \left(\frac{\alpha + \beta}{2} \right) \cos \left(\frac{\alpha - \beta}{2} \right)}{2 \cos \left(\frac{\alpha + \beta}{2} \right) \sin \left(\frac{\alpha - \beta}{2} \right)} = 4$$

$$\frac{\tan \left(\frac{\alpha + \beta}{2} \right)}{\tan \left(\frac{\alpha - \beta}{2} \right)} = 4$$

(7) $2 \sin A \cos C + 2 \sin A$

$$2 \sin B \cos C + 2 \sin B$$

$$\frac{2 \sin A (\cos C + 1)}{2 \sin B (\cos C + 1)} =$$

(Physics)

COMPOUND ANGLE

A

DPP

Compound Angle

Q.1 If $\sin x + \sin^2 x = 1$, then the value of $\cos^2 x + \cos^4 x$ is -

- (A) 0 (B) 2 (C) 1 (D) 3

Q.2 $2(\sin^6 \theta + \cos^6 \theta) - 3(\sin^4 \theta + \cos^4 \theta) + 1$ is equal to -

- (A) 2 (B) 0 (C) 4 (D) 6

Q.3 $\tan A = -\frac{1}{2}$ and $\tan B = -\frac{1}{3}$, then $A + B =$

- (A) $\frac{\pi}{4}$ (B) $\frac{3\pi}{4}$ (C) $\frac{5\pi}{4}$ (D) $\frac{7\pi}{4}$

Q.4 $\cos^2 48^\circ - \sin^2 12^\circ$ is equal to -

- (A) $\frac{\sqrt{5}-1}{4}$ (B) $\frac{\sqrt{5}+1}{8}$ (C) $\frac{\sqrt{3}-1}{4}$ (D) $\frac{\sqrt{3}+1}{2\sqrt{2}}$

Q.5 The expression $\frac{\sin 8\theta \cos \theta - \sin 6\theta \cos 3\theta}{\cos 2\theta \cos \theta - \sin 3\theta \sin 4\theta}$ is equals.

- (A) $\tan \theta$ (B) $\tan 2\theta$ (C) $\sin 2\theta$ (D) $\cos 2\theta$

Q.6 If $3 \sin \alpha = 5 \sin \beta$, then $\frac{\tan \frac{\alpha + \beta}{2}}{\tan \frac{\alpha - \beta}{2}} =$

- (A) 1 (B) 2 (C) 3 (D) 4

Q.7 $\frac{\sin(A-C) + 2 \sin A + \sin(A+C)}{\sin(B-C) + 2 \sin B + \sin(B+C)}$ is equal to -

- (A) $\tan A$ (B) $\frac{\sin A}{\sin B}$ (C) $\frac{\cos A}{\cos B}$ (D) $\frac{\sin C}{\cos B}$

Q.8 $\frac{1 + \sin 2\theta + \cos 2\theta}{1 + \sin 2\theta - \cos 2\theta} =$

- (A) $\frac{1}{2} \tan \theta$ (B) $\frac{1}{2} \cot \theta$ (C) $\tan \theta$ (D) $\cot \theta$

Q.9 If $A = \tan 6^\circ \tan 42^\circ$ and $B = \cot 66^\circ \cot 78^\circ$, then -

- (A) $A = 2B$ (B) $A = 1/3B$ (C) $A = B$ (D) $3A = 2B$

Q.10 If $x = y \cos \frac{2\pi}{3} = z \cos \frac{4\pi}{3}$ then $xy + yz + zx =$

- (A) -1 (B) 0 (C) 1 (D) 2

Q.11 If $\tan \alpha = (1 + 2^{-1})$, $\beta = (1 + 2^{5+1})^{-1}$, then $\alpha + \beta =$

- (A) $\pi/6$ (B) $\pi/4$ (C) $\pi/3$ (D) $\pi/2$

Q.12 If $\tan A - \tan B + \tan C - \tan A, \tan B, \tan C$, then-

- (A) A, B, C must be angles of a triangle
(B) the sum of any two of A, B, C is equal to the third
(C) $A + B + C$ must be an integral multiple of π
(D) None of these

① Done in copy \downarrow Direct form.

② $2\{1 - 3 \sin^2 \theta \cos^2 \theta\}$

$$- 3\{1 - 2 \sin^2 \theta \cos^2 \theta\} + 1 = 0$$

(3) $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$

$$= \frac{-\frac{1}{2} + -\frac{1}{3}}{1 - (-\frac{1}{2})(-\frac{1}{3})}$$

$$\tan(A+B) = \frac{-\frac{5}{6}}{\frac{5}{6}} = -1 \mid \frac{3\pi}{4}$$

(4) $\cos^2 B - \sin^2 A = \cos(A+B) \cdot \cos(A-B)$
 $\cos(60^\circ) \cdot \cos(36^\circ) = \frac{1}{2} \times \frac{\sqrt{5}+1}{4}$

$$\Phi_{10} \quad G(180^\circ + 60^\circ) = -G_{60^\circ}$$

$$x = \sqrt{\frac{2\pi}{3}} = 2\sqrt{\frac{\pi}{3}}$$

$$y = y \cdot \cos 120^\circ = 2\cos 240^\circ$$

$$x = -\frac{y}{2} = -\frac{z}{2}$$

$$y = -2x, \quad z = -2x$$

$$xy + yz + zx$$

$$= -2x^2 + (-2x)(-2x) + -2x^2$$

$$= -4x^2 + 4x^2 = 0$$

$$Q_{11} \quad \tan \alpha = (1 + 2^{-x})^{-1}$$

$$\tan \beta = (1 + 2^{x+1})^{-1}$$

(Physics)

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$$(8) \frac{(1 + \cos 2\theta) + \sin 2\theta}{(1 - \cos 2\theta) + \sin 2\theta}$$

$$\frac{2\cos^2 \theta + 2\sin \theta \cos \theta}{2\sin^2 \theta + 2\sin \theta \cos \theta}$$

$$\frac{2\cos \theta (\cos \theta + \sin \theta)}{2\sin \theta (\sin \theta + \cos \theta)} = \cot \theta$$

$$(9) \quad A = \tan 6^\circ \tan 42^\circ$$

$$B = \cot 66^\circ \cot 78^\circ$$

$$\frac{A}{B} = \tan 6^\circ \tan 66^\circ \tan 42^\circ \tan 78^\circ$$

$$\frac{\tan(60-6^\circ) \tan 6^\circ \tan(60+6^\circ) \tan(60-18^\circ) \tan(60+18^\circ) \tan 18^\circ}{\tan 54^\circ \tan 18^\circ}$$

$$\frac{\tan 54^\circ \tan 18^\circ}{\tan 54^\circ \tan 18^\circ} = 1$$

$$A = B$$

$$\tan \alpha = (1 + 2^{-x})^{-1} = \frac{2^x}{1 + 2^x}$$

$$\tan \beta = \frac{1}{1 + 2^{1+x}}$$

$$\begin{aligned} \tan(\alpha + \beta) &= \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \cdot \tan \beta} \\ &= \frac{\frac{2^x}{1 + 2^x} + \frac{1}{1 + 2^{1+x}}}{1 - \frac{2^x}{1 + 2^x} \times \frac{1}{1 + 2^{1+x}}} \end{aligned}$$

$$= \frac{2^x + 2^x \cdot 2^x \cdot 2 + 1 + 2^x}{1 + 2^x + 2^{x+1} + 2^x \cdot 2^x \cdot 2 - 2^x}$$

$$\tan(\alpha + \beta) = \frac{1 + 2 \cdot 2^x + 2(2^x)^2}{1 + 2 \cdot 2^x + 2(2^x)^2} = 1$$

$$\alpha + \beta = \frac{\pi}{4}$$

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$$A + B + C = n\pi$$

then.

$$\tan A + \tan B + \tan C = \tan A \cdot \tan B \cdot \tan C$$

$$\tan A + \tan B + \tan C = \tan A \cdot \tan B \cdot \tan C$$

$$\text{then } A + B + C = ?$$

$$n\pi$$

$$\frac{\sin\left(\frac{36 \times 10}{2}\right)}{\sin\left(\frac{10}{2}\right)} \times \sin\left(\frac{10^\circ + 360^\circ}{2}\right)$$

$$\sin 180^\circ \times \dots = 0$$

Q14 $y = \sin(e^x) = \sqrt{2^x + \frac{1}{2}x}$



Q17 $\sin\left(\frac{\pi}{14}\right) \cdot \sin\left(\frac{3\pi}{14}\right) \cdot \sin\left(\frac{5\pi}{14}\right)$
 $\cos\left(\frac{\pi}{2} - \frac{\pi}{14}\right) \cdot \cos\left(\frac{\pi}{2} - \frac{3\pi}{14}\right) \cdot \cos\left(\frac{\pi}{2} - \frac{5\pi}{14}\right)$
 $\cos\left(\frac{6\pi}{14}\right) \cdot \cos\left(\frac{4\pi}{14}\right) \cdot \cos\left(\frac{2\pi}{14}\right)$
 $= \cos\left(\frac{8\pi}{14}\right) \cdot \cos\left(\frac{4\pi}{14}\right) \cdot \cos\left(\frac{2\pi}{14}\right) =$

(Physics)

COMPOUND ANGLE

A

- Q.13 The value of $\sin 10^\circ + \sin 20^\circ + \sin 30^\circ + \dots + \sin 360^\circ$ is equal to -
 (A) 0 (B) 1 (C) $\sqrt{3}$ (D) 2
- Q.14 The number of real solutions of the equation $\sin(e^x) = 2^x + 2^{-x}$ is -
 (A) 1 (B) 0 (C) 2 (D) Infinite
- Q.15 If $f(x) = \frac{\sin 3x}{\sin x}$, $x = 11\pi$, then the range of values of $f(x)$ for real values of x is -
 (A) $[-1, 3]$ (B) $(-\infty, -1]$ (C) $(3, +\infty)$ (D) $[-1, 3]$
- Q.16 If $\cos x + \cos y + \cos \alpha = 0$ and $\sin x + \sin y + \sin \alpha = 0$, then $\cot\left(\frac{x+y}{2}\right) =$
 (A) $\sin \alpha$ (B) $\cos \alpha$ (C) $\cot \alpha$ (D) $2\sin \alpha$
- Q.17 The value of $\sin \frac{\pi}{14} \sin \frac{3\pi}{14} \sin \frac{5\pi}{14}$ is :-
 (A) $\frac{1}{16}$ (B) $\frac{1}{8}$ (C) $\frac{1}{2}$ (D) 1
- Q.18 Maximum and minimum value of $2\sin^2 \theta - 3\sin \theta + 2$ is -
 (A) $\frac{1}{4}, -\frac{7}{4}$ (B) $\frac{1}{4}, \frac{21}{4}$ (C) $\frac{21}{4}, -\frac{3}{4}$ (D) $7, \frac{7}{8}$
- Q.19 For $\theta \in (0, \pi/2)$, the maximum value of $\sin\left(\theta + \frac{\pi}{6}\right) + \cos\left(\theta + \frac{\pi}{6}\right)$ is attained at $\theta =$
 (A) $\frac{\pi}{12}$ (B) $\frac{\pi}{6}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{4}$
- Q.20 Minimum value of the expression $\cos^2 \theta - (6\sin \theta \cos \theta) + 3\sin^2 \theta + 2$, is -
 (A) $4 + \sqrt{10}$ (B) $4 - \sqrt{10}$ (C) 0 (D) 4

$$\cos \theta \cdot \cos 2\theta \cdot \cos 4\theta = \frac{\sin(2 \cdot LA)}{2^n (\sin(SA))}$$

$$\cos\left(\frac{14\pi - 6\pi}{14}\right) = \cos\left(\pi - \frac{6\pi}{14}\right) = \cos \frac{6\pi}{14}$$

$$= \frac{\sin\left(2 \times \frac{8\pi}{14}\right)}{2^3 \sin\left(\frac{2\pi}{14}\right)} = \frac{\sin\left(\frac{14\pi + 2\pi}{14}\right)}{8 \cdot \sin\left(\frac{2\pi}{14}\right)} = \frac{\sin\left(\pi + \frac{2\pi}{14}\right)}{8 \sin\left(\frac{2\pi}{14}\right)}$$

Q16.

$$\cos x + \cos y = -\cos x \Rightarrow 2\cos\left(\frac{x+y}{2}\right) \cdot \cos\left(\frac{x-y}{2}\right) = -\cos x$$

$$\sin x + \sin y = -\sin x \Rightarrow 2\sin\left(\frac{x+y}{2}\right) \cdot \cos\left(\frac{x-y}{2}\right) = -\sin x$$

$$\cot\left(\frac{x+y}{2}\right) = \cot x$$

Sum of Any +ve No / fcn with its Reciprocal is always gr than

$$2^x + \frac{1}{2}x \geq 2 \text{ or equal to}$$

Q15 $y = \frac{\sin 3x}{\sin x} = \frac{3\sin x - 4\sin^3 x}{\sin x}$

$$y = \frac{\sin x (3 - 4\sin^2 x)}{\sin x} \Rightarrow y = 3 - 4\sin^2 x$$

$$0 \leq \sin^2 x \leq 1$$

$$0 \geq -4\sin^2 x \geq -4$$

$$3 \geq 3 - 4\sin^2 x \geq -1$$

$$y \in [-1, 3] = \frac{1}{8}$$


$$+ \left(\cos \frac{2\pi}{14} \right)$$

$$8 \cos\left(\frac{2\pi}{14}\right)$$

$$\frac{\sin\left(\frac{36 \times 10}{2}\right)}{\sin\left(\frac{10}{2}\right)} \times \sin\left(\frac{10^\circ + 360^\circ}{2}\right)$$

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$$1 - \frac{9}{16}$$

$$y = 2\sin^2 \theta - 3\sin \theta + 2$$

$$= 2\left(\sin^2 \theta - \left[\frac{3}{2}\right]\sin \theta + 1\right)^{3/4}$$

$$= 2\left(\left(\sin \theta - \frac{3}{4}\right)^2 - \left(\frac{3}{4}\right)^2 + 1\right)$$

$$= 2\left(\left(\sin \theta - \frac{3}{4}\right)^2 + \frac{7}{16}\right)$$

$$2\left(0 + \frac{7}{16}\right) \quad 2\left(\left(1 - \frac{3}{4}\right)^2 + \frac{7}{16}\right)$$

$$\frac{7}{8}$$

Ex2 $\xrightarrow{2 \text{ parts}}$ 15(x)
Ratte

Ex1
Yad Rakhnahai



Quadratic Eqn.

$$\textcircled{1} \quad y = x^2 + \boxed{x} + 1 \quad \xrightarrow{1/2}$$

$$= \left(x + \frac{1}{2}\right)^2 - \left(\frac{1}{2}\right)^2 + 1$$

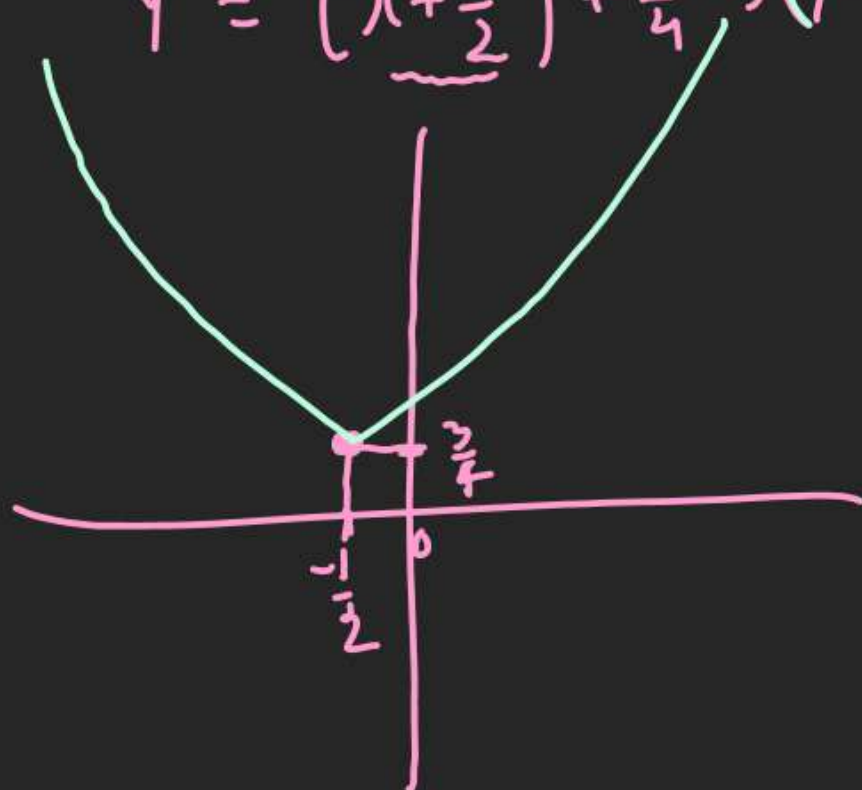
$$y = x^2 \quad \text{✓}$$

$$y = -x^2 \quad \text{✗}$$

$$y = \left(x + \frac{1}{2}\right)^2 + \frac{3}{4} \Rightarrow \left(y - \frac{3}{4}\right) = \left(x + \frac{1}{2}\right)^2$$

$$\rightarrow x = -\frac{1}{2}$$

$$\rightarrow y = \frac{3}{4}$$



[12-15 Lec]

→ {4 Lec Adv. Level.}

(hutti le lena.
 ✗ NaaraZ nahi
 hona!!)

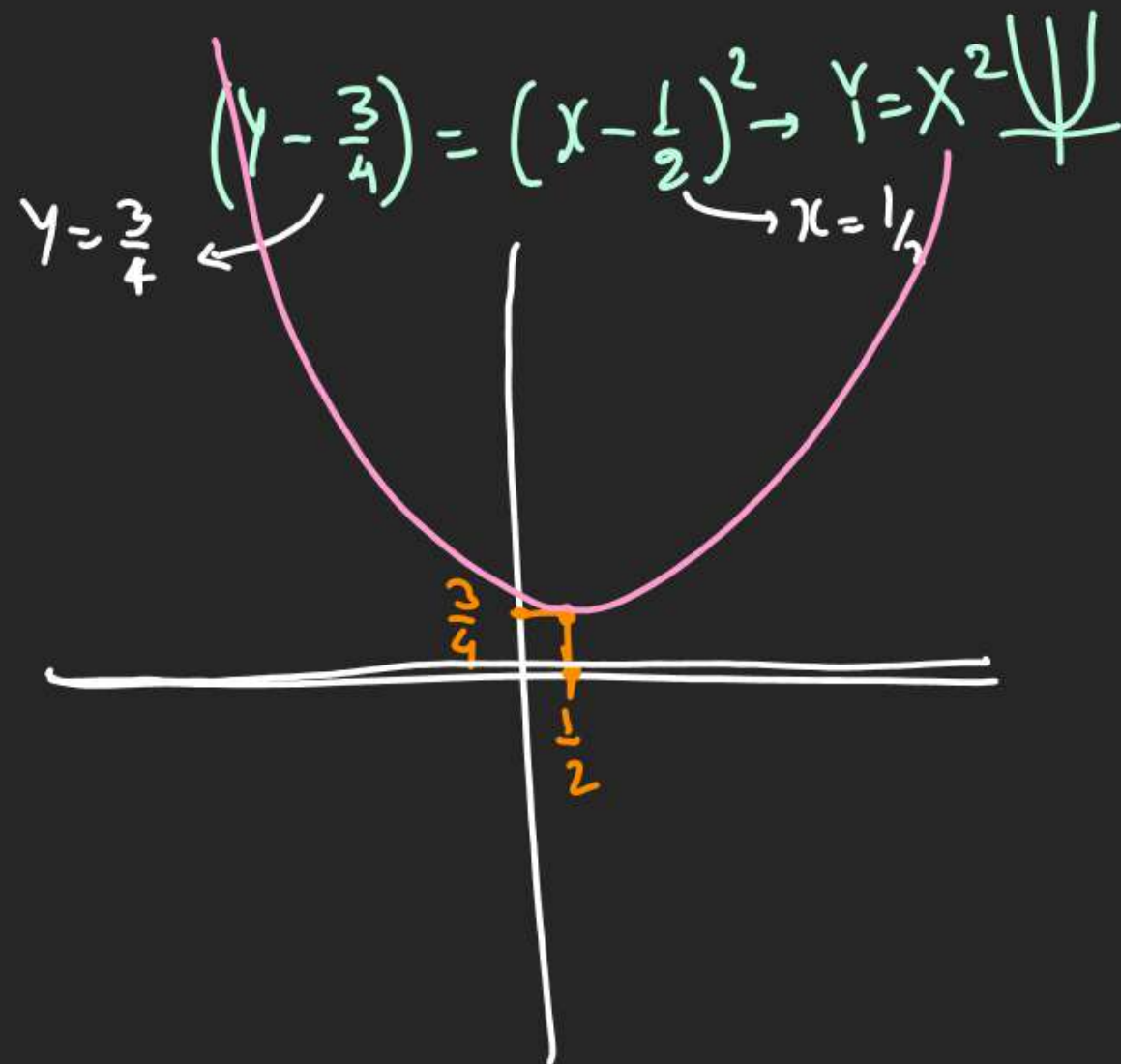
$$(2) \ y = x^2 - \boxed{x} + 1 \xrightarrow{1/2}$$

$$D = (-1)^2 - 4 \times 1 \times 1 = (x - \frac{1}{2})^2 - (\frac{1}{2})^2 + 1$$

$$\boxed{D = -3} = -ve$$

Total Graph above
x Axis

$$y = (x - \frac{1}{2})^2 + \frac{3}{4}$$



$$(3) \ y = 2x^2 - 4x + 7 \text{ 's graph.}$$

$$= 2 \left[x^2 - \boxed{2x} + \frac{7}{2} \right]$$

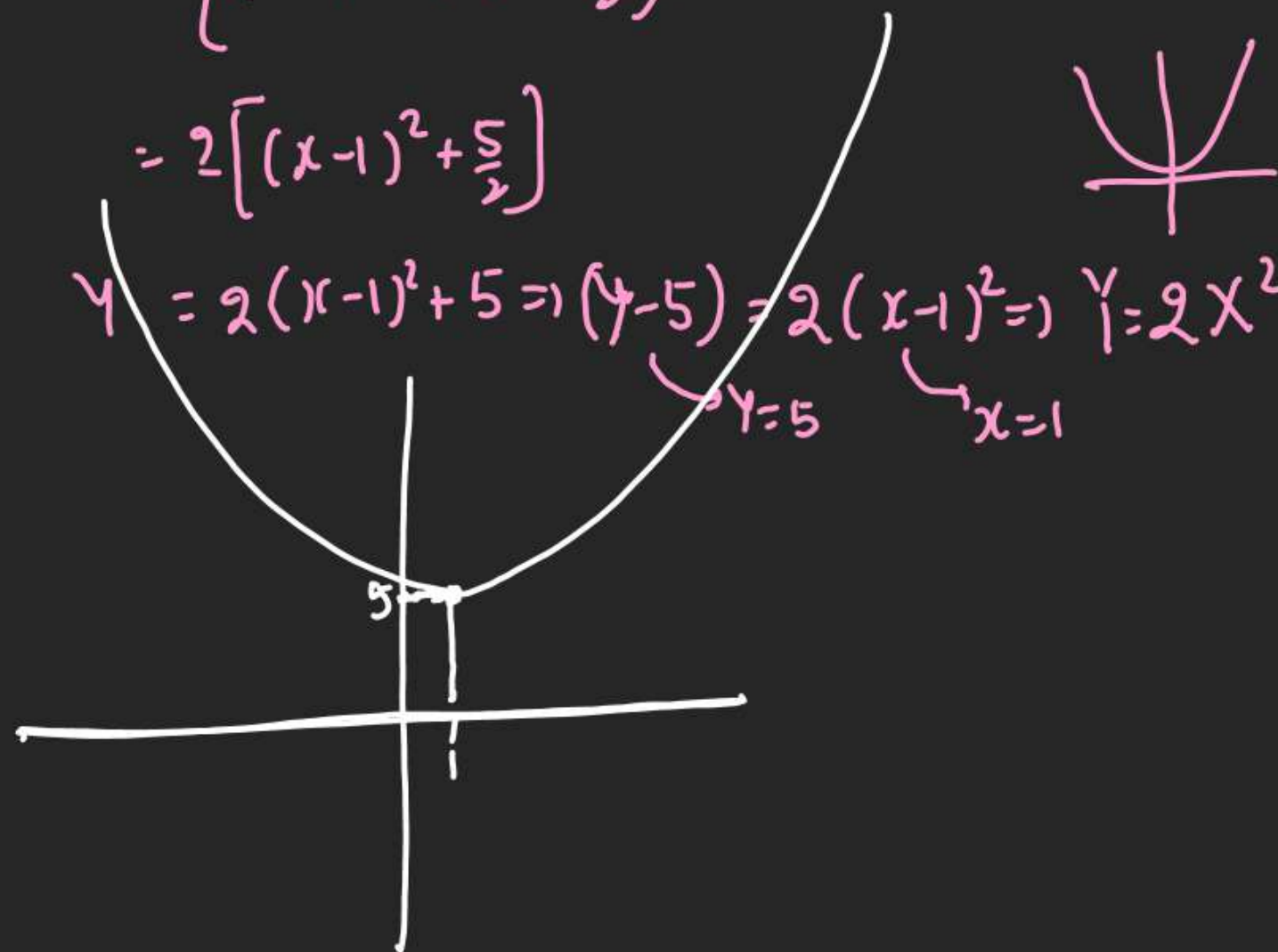
$$= 2 \left[(x - 1)^2 - (1)^2 + \frac{7}{2} \right]$$

$$= 2 \left[(x - 1)^2 + \frac{5}{2} \right]$$

$$y = 2(x - 1)^2 + 5 \Rightarrow (y - 5) = 2(x - 1)^2 \Rightarrow y = 2x^2$$

$$D = (-4)^2 - 4 \times 2 \times 7 = 16 - 56 = -40 = -ve$$

\therefore Graph Above x Axis



$$(4) y = 2x^2 + 4x + 1$$

$$= 2 \left[x^2 + 2x + \frac{1}{2} \right]$$

$$= 2 \left[(x+1)^2 - 1^2 + \frac{1}{2} \right]$$

$$= 2 \left[(x+1)^2 - \frac{1}{2} \right]$$

$$y = 2(x+1)^2 - 1$$

$$(y+1) = 2(x+1)^2 \rightarrow y = 2x^2$$

$$y = -1$$

$$x = -1$$



$$1) D = 4^2 - 4 \times 2 \times 1$$

$$D = 8 + ve$$

X Axis ko cut

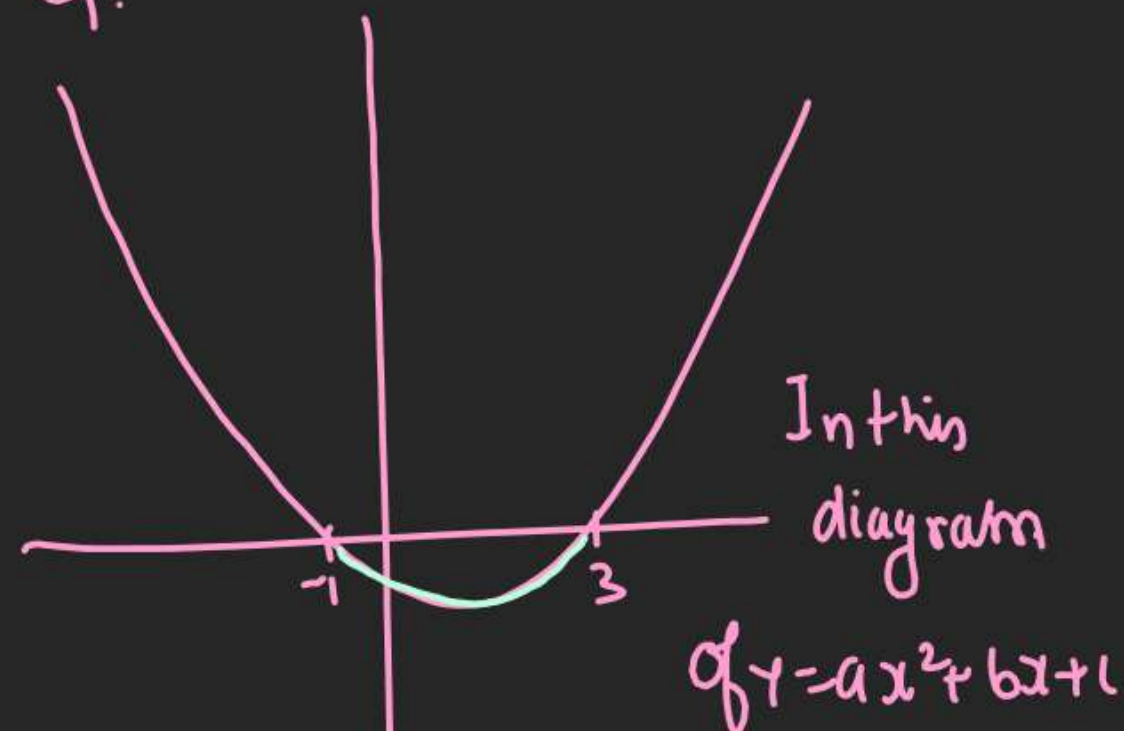
2) Places where

Graph cut
X Axis is known
as Roots

$$x = \frac{-4 \pm \sqrt{4^2 - 4 \times 2 \times 1}}{2 \times 2}$$

$$x = \frac{-4 \pm 2\sqrt{2}}{2 \times 2} \Rightarrow \begin{cases} \frac{-2 + \sqrt{2}}{2} \\ \frac{-2 - \sqrt{2}}{2} \end{cases}$$

Q.



A) $y < 0$ in $x \in (a, b)$
find a & b .

$y < 0$ means places where
graph below x Axis
 $\therefore y < 0$ in $x \in (-1, 3)$
 $a = -1, b = 3$

(B) $y > 0$ in $x \in \dots$

$y > 0$ means graph above X Axis

$$y > 0 \text{ in } x \in (-\infty, -1) \cup (3, \infty)$$

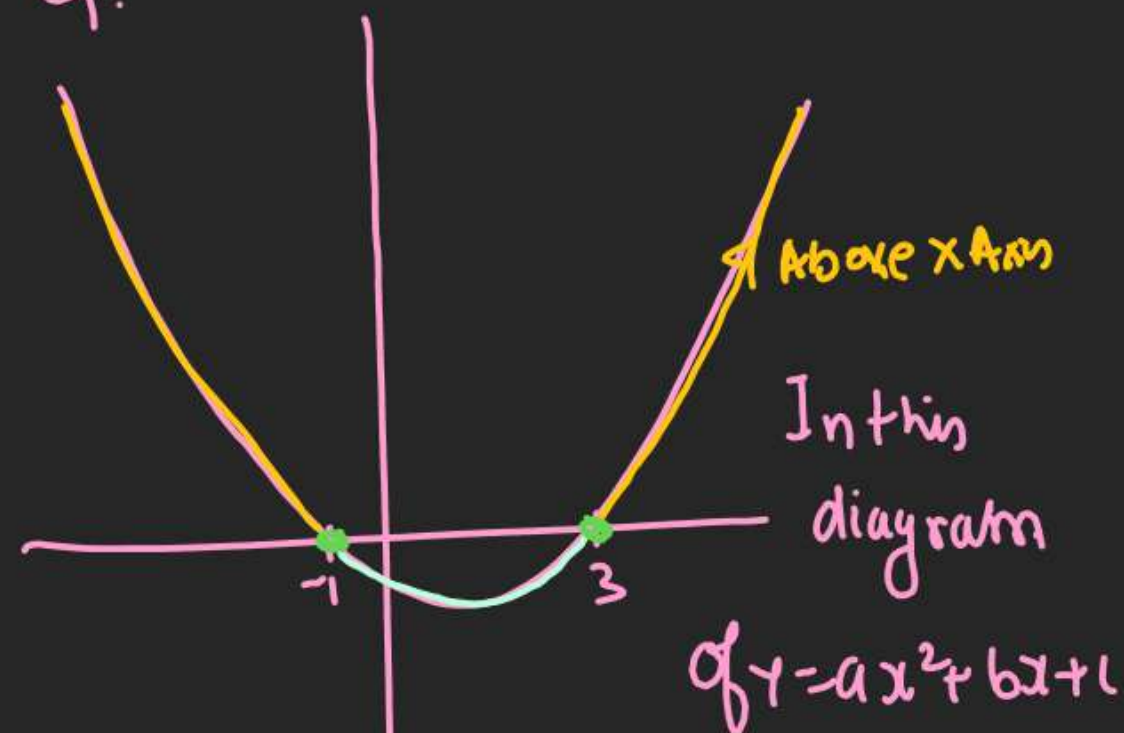
(C) $y = 0$ at $x \in ?$

Graph cuts X Axis at

$$x = -1, 3$$

$$x \in \{-1, 3\}$$

Q.

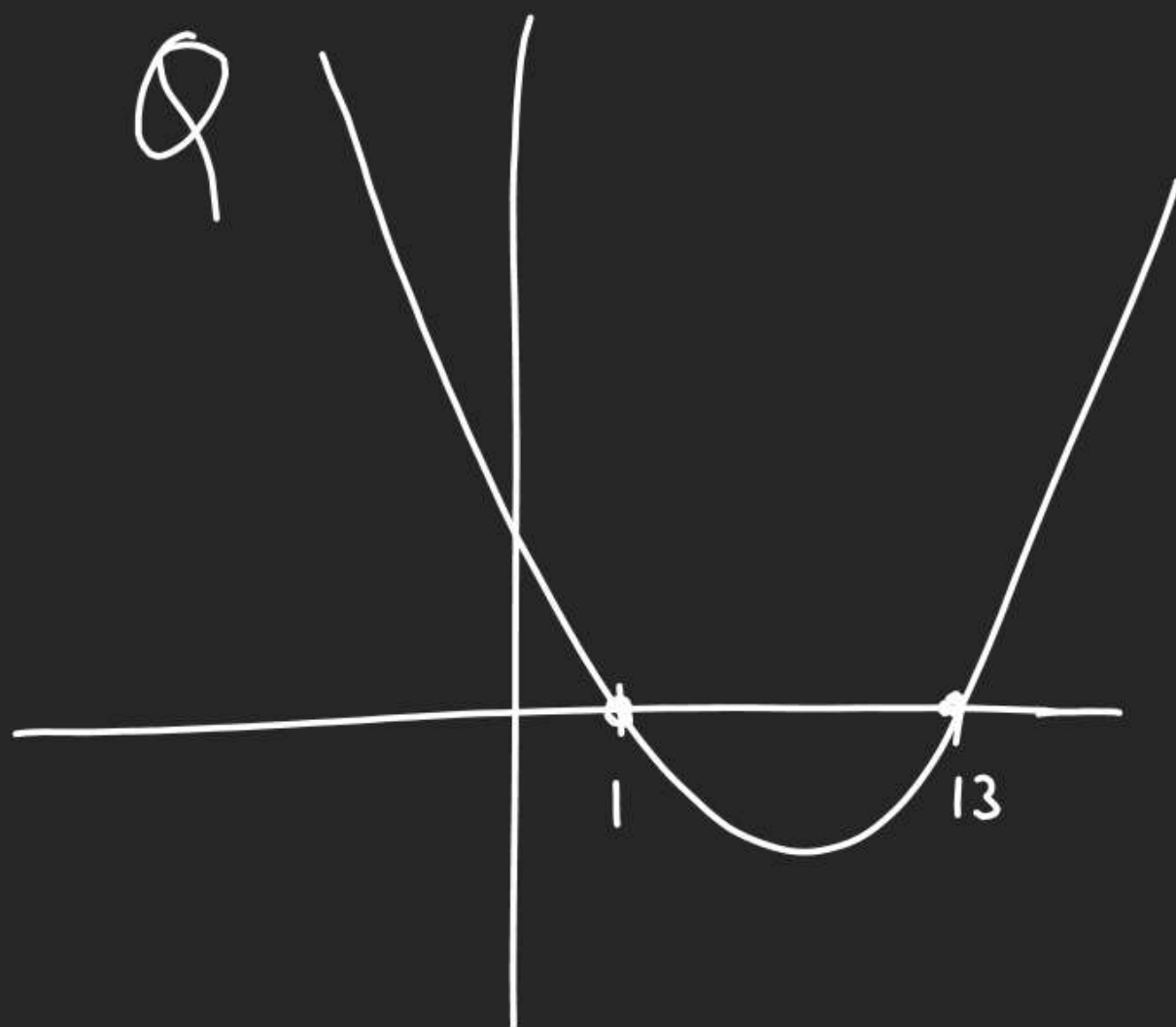


A) $y < 0$ in $x \in (a, b)$
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$y < 0$ means places where graph below X Axis

$$\therefore y < 0 \text{ in } x \in (-1, 3)$$

$$a = -1, b = 3$$



(1) $y > 0$?

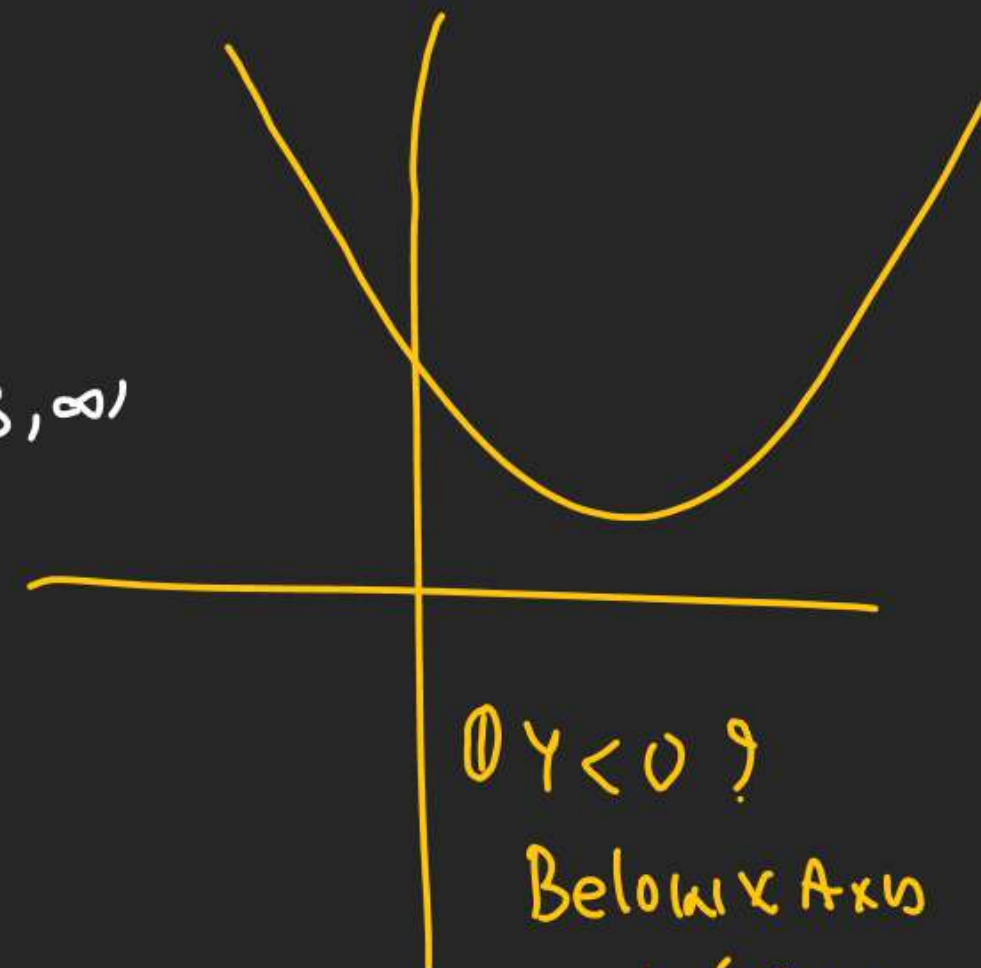
$x \in (-\infty, 1) \cup (13, \infty)$

(2) $y < 0$??

$x \in (1, 13)$

(3) $y = 0$?

$x \in \{1, 13\}$



(1) $y < 0$?

Below x Axis

$x = \phi$ (Kahin
Below x Axis
Nhi hai)

(2) $y > 0$?

$x \in (-\infty, \infty)$ at all pts

(3) $y = 0$?

x Axis Par no cut $\Rightarrow x = \phi$

1) $y = 3x^2 - 4x + 5$'s graph

2) $y = 2x^2 - 4x + 1$'s graph