

$$\underline{5.} \quad \sqrt{\frac{1-\sin A}{1+\sin A}} = \sqrt{\frac{(1-\sin A)^2}{\cos^2 A}} = \frac{1-\sin A}{\cos A}$$

$$\underline{14.} \quad \frac{\frac{\sin A}{\cos A}}{1 - \frac{\cos A}{\sin A}} + \frac{\frac{\cos A}{\sin A}}{1 - \frac{\sin A}{\cos A}} = \frac{\sin^2 A}{\cos A (\sin A - \cos A)} - \frac{\cos^2 A}{\sin A (\sin A - \cos A)}$$

$$\underline{10.} \quad \frac{\sec^2 A - \tan^2 A}{\sec A - \tan A} = \sec A + \tan A$$

$$\frac{1 + \sin A \cos A}{\sin A \cos A} = \frac{\sin^3 A - \cos^3 A}{\sin A \cos A (\sin A - \cos A)}$$

$$\begin{aligned}
 \underline{23.} \quad & (\csc A + \cot A) - \csc A \\
 &= \csc A - (\csc A - \cot A) \\
 &= \frac{1}{\sin A} - \frac{1}{\csc A + \cot A}
 \end{aligned}$$

$$\underline{24.} \quad \frac{\cot A \cos A (\cot A - \cos A)}{\cot^2 A \cos^2 A}$$

$$\underline{25.} \quad \frac{\cot A + \tan B}{\frac{1}{\tan B} + \frac{1}{\cot A}}$$

$$\underline{26.} \left(\frac{\cos^2 \alpha}{\sin^2 \alpha (1 + \cos^2 \alpha)} + \frac{\sin^2 \alpha}{\cos^2 \alpha (1 + \sin^2 \alpha)} \right) \cos^2 \alpha \sin^2 \alpha$$

$$\frac{\cos^4 \alpha (1 + \sin^2 \alpha) + \sin^4 \alpha (1 + \cos^2 \alpha)}{\sin^2 \alpha \cos^2 \alpha (1 + \cos^2 \alpha) (1 + \sin^2 \alpha)} \quad \cos^3 \alpha \sin^3 \alpha$$

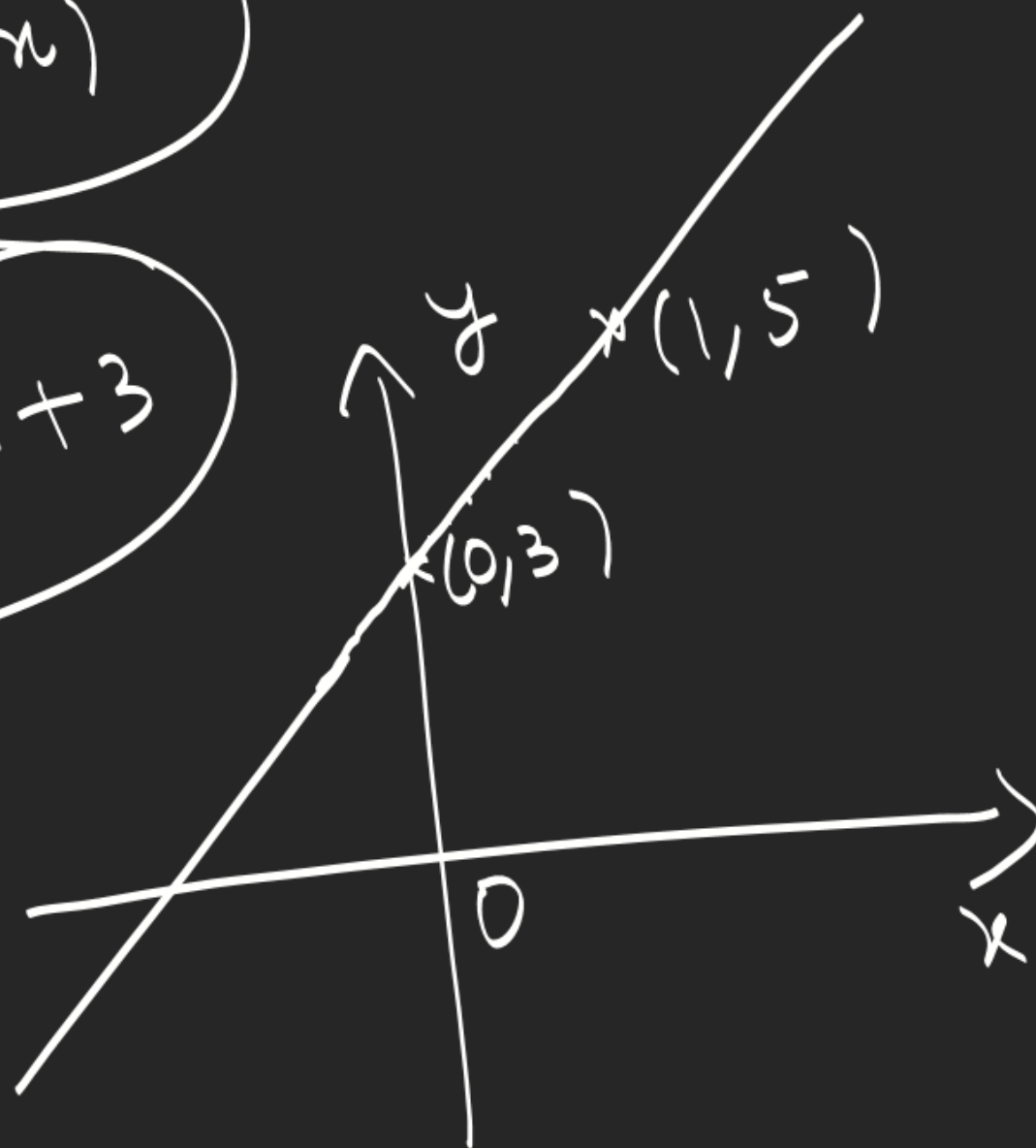
-1+1

$$\frac{\cos^4 \alpha + \sin^4 \alpha + 2 \sin^2 \alpha \cos^2 \alpha - \sin^2 \alpha \cos^2 \alpha}{2 + \sin^2 \alpha \cos^2 \alpha}$$

29. $2 \tan \alpha \cot \beta \left(\frac{1}{\cos \beta} + \frac{1}{\sin \beta} \right) + 2 \cot \beta \sec \alpha$

$$y = f(x)$$

$$y = 2x + 3$$



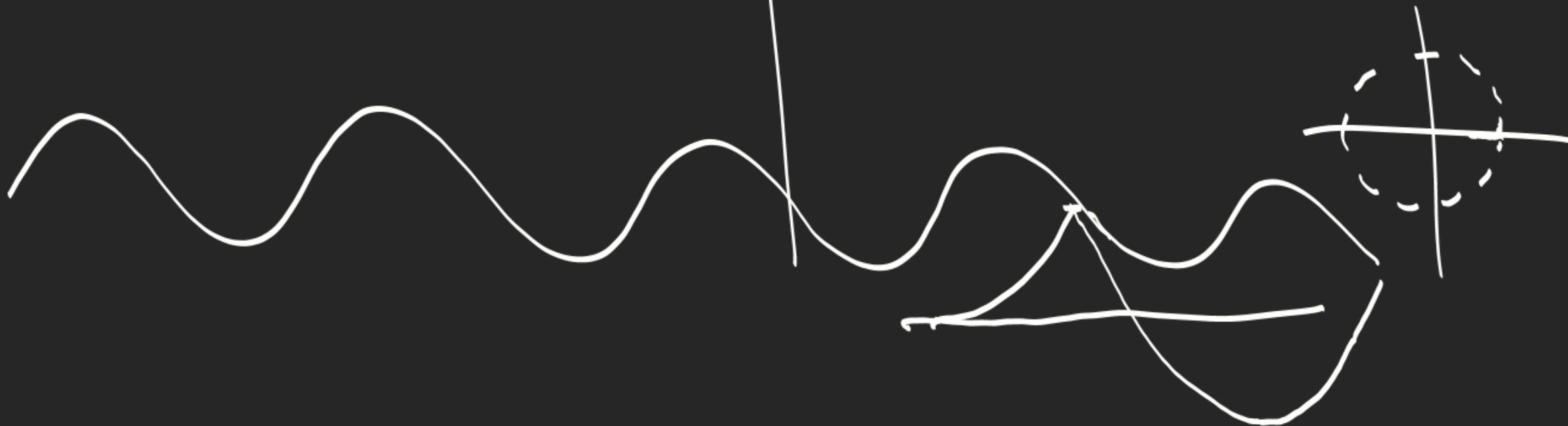
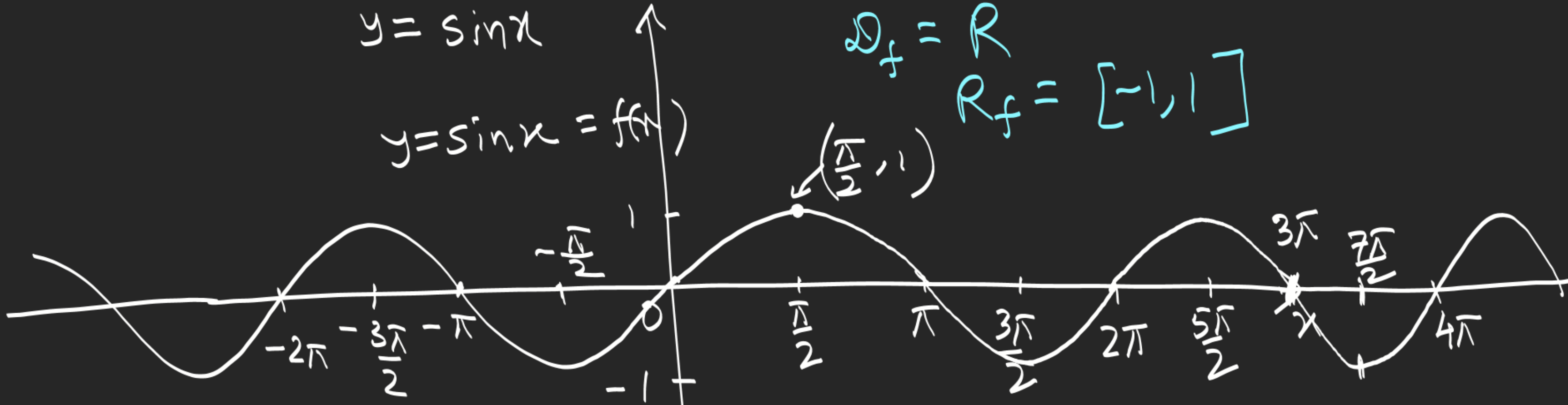
$$y = \sin x$$

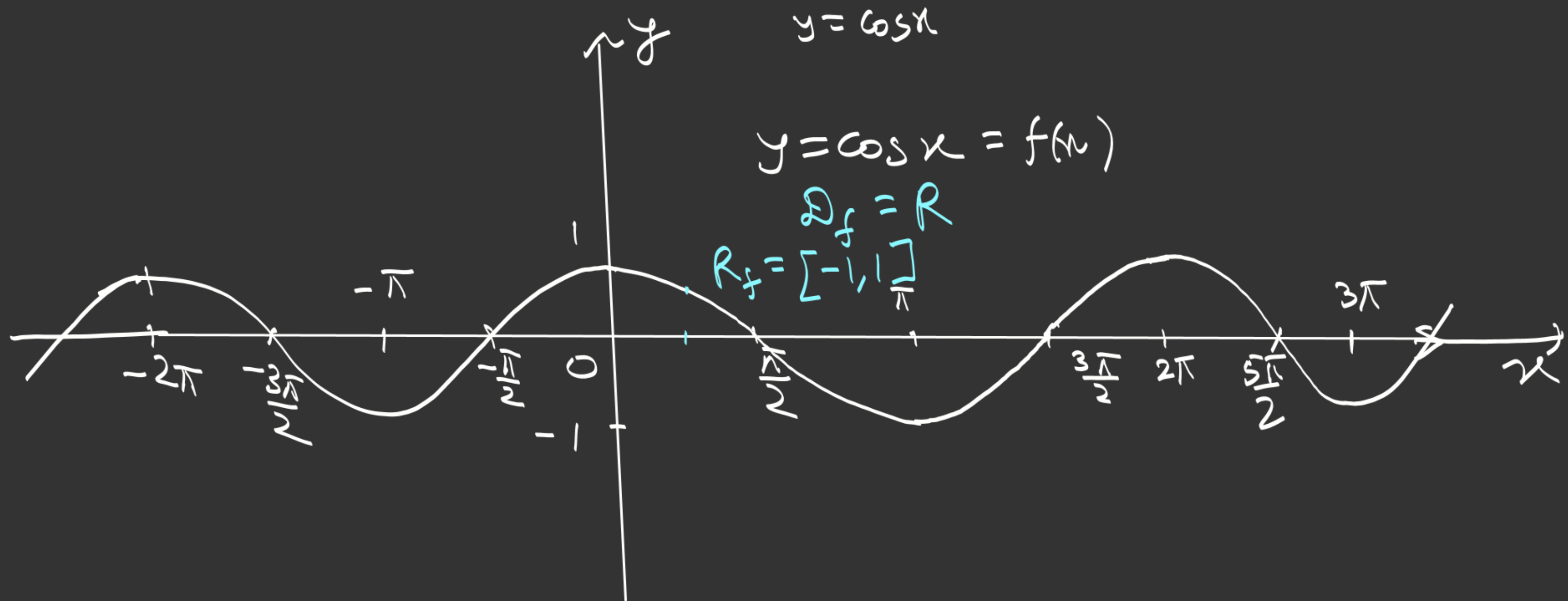
$$y = \sin x = f(x)$$

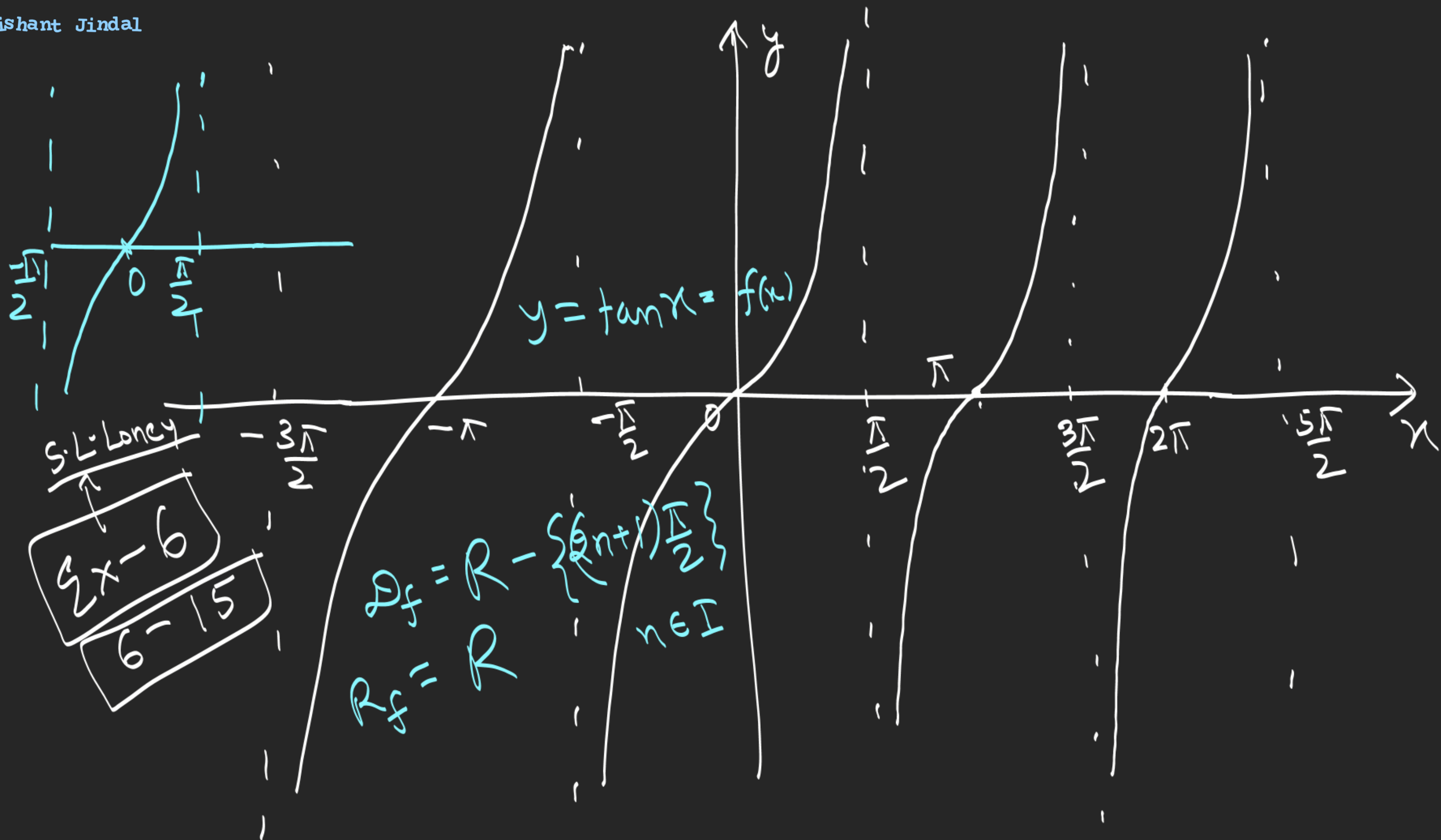
$$D_f = \mathbb{R}$$

$$R_f = [-1, 1]$$

$$\left(\frac{\pi}{2}, 1\right)$$







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$$\frac{2x-6}{6-15}$$

$$D_f = \mathbb{R} - \left\{ (2n+1)\frac{\pi}{2} \right\}$$

$$R_f = \mathbb{R}$$

$$n \in \mathbb{I}$$

Function

$$y = f(x) = x^3 - 3x^2 + \sin x$$

$$1 - 3 + \sin 1$$

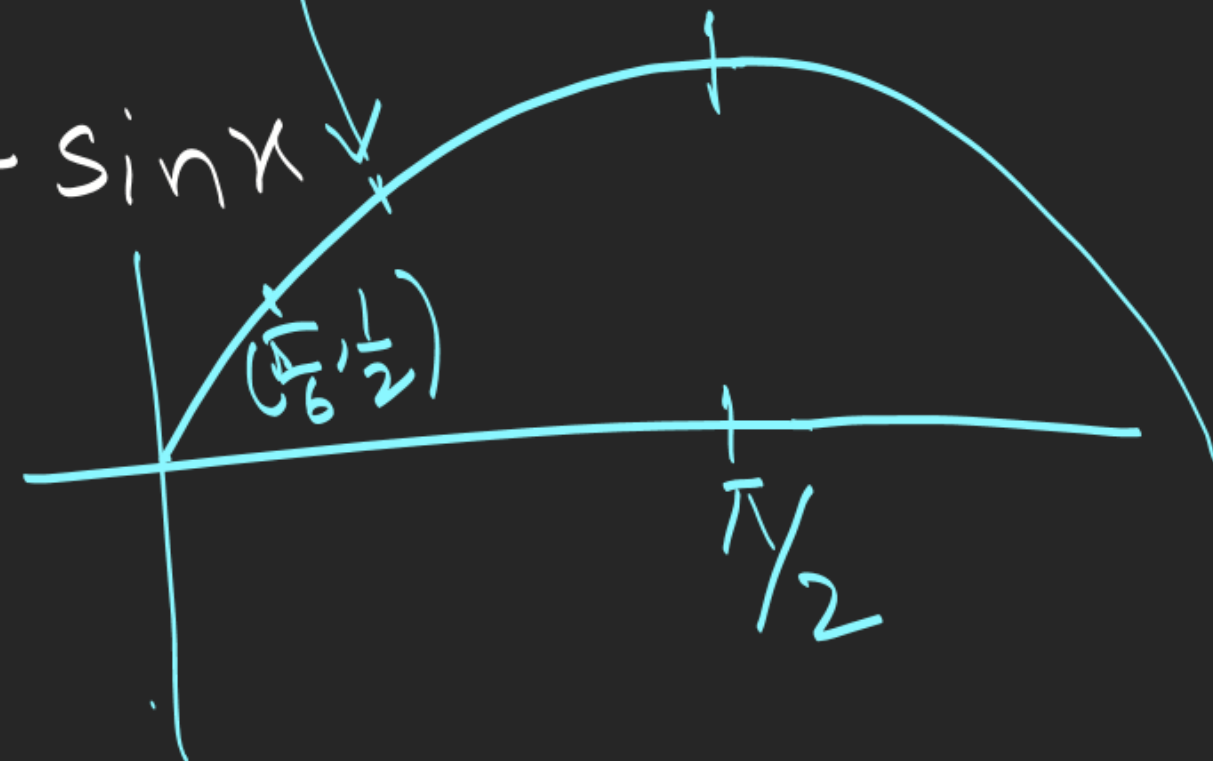
$$(x, y) = (1, \sin 1 - 2)$$

$$y = \sin x$$

$$\left(\frac{\pi}{4}, \frac{1}{\sqrt{2}}\right)$$

$$\left(\frac{\pi}{6}, \frac{1}{2}\right)$$

$$\frac{\pi}{2}$$



Domain of Function

$$D_f = (-\infty, 1] \cup \{2\} \cup [3, \infty)$$

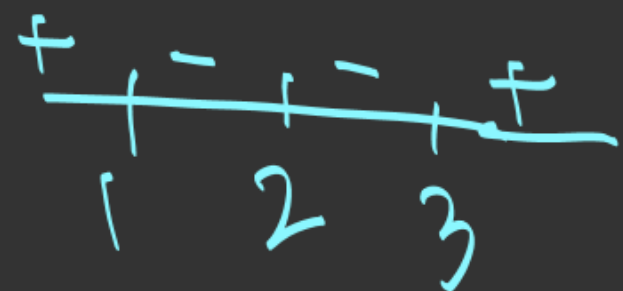
Set of all x such that $f(x)$ is defined

$$f(x) = \frac{1}{x^2 - 3x + 2}$$

$$f(x) = \sqrt{(x-1)(x-2)^2(x-3)}$$

$$D_f = \mathbb{R} - \{1, 2\}$$

$$= (-\infty, 1) \cup (1, 2) \cup (2, \infty)$$



$$(x-1)(x-2)^2(x-3) \geq 0$$

Range of Function

$$y = f(x)$$

← set of all y values attained is called range.

Range ← $y = f(x)$ → Domain

$$f(x) = \frac{1}{x}$$

$$D_f = \mathbb{R} - \{0\}$$

$$R_f = \mathbb{R} - \{0\}$$

$$y = -367 \text{ at } x = -\frac{1}{367}$$

$$\frac{1}{x} = y$$

$$\frac{33}{5} = y$$

$$x = \frac{5}{33}$$