

$$1 + \sqrt{5} + 3$$

$$4 + 2 \cdot 236 = 6 \cdot 236$$

$$(2, -2)$$

$$3 - \sqrt{5} \leq |z| \leq 3 + \sqrt{5}$$

$$-3 < 3 - 2\sqrt{5} < |z| - |w| + 3 \leq \underline{3 + 3 + \sqrt{5}} < 9$$

$$\begin{aligned} -3 - \sqrt{5} &< -|w| \leq 0 \\ 0 &\leq |w| < 3 + \sqrt{5} \end{aligned}$$

$$|u|^2 = (a+b+c)(\bar{a}+\bar{b}+\bar{c})$$

$$|u|^2 = (a+b\omega+c\omega^2)(\bar{a}+\bar{b}\omega^2+\bar{c}\omega) =$$

$\angle 90^\circ$

$$\frac{8t+1 \geq 0}{3(1-t^2)}$$

$$3t-1=t$$

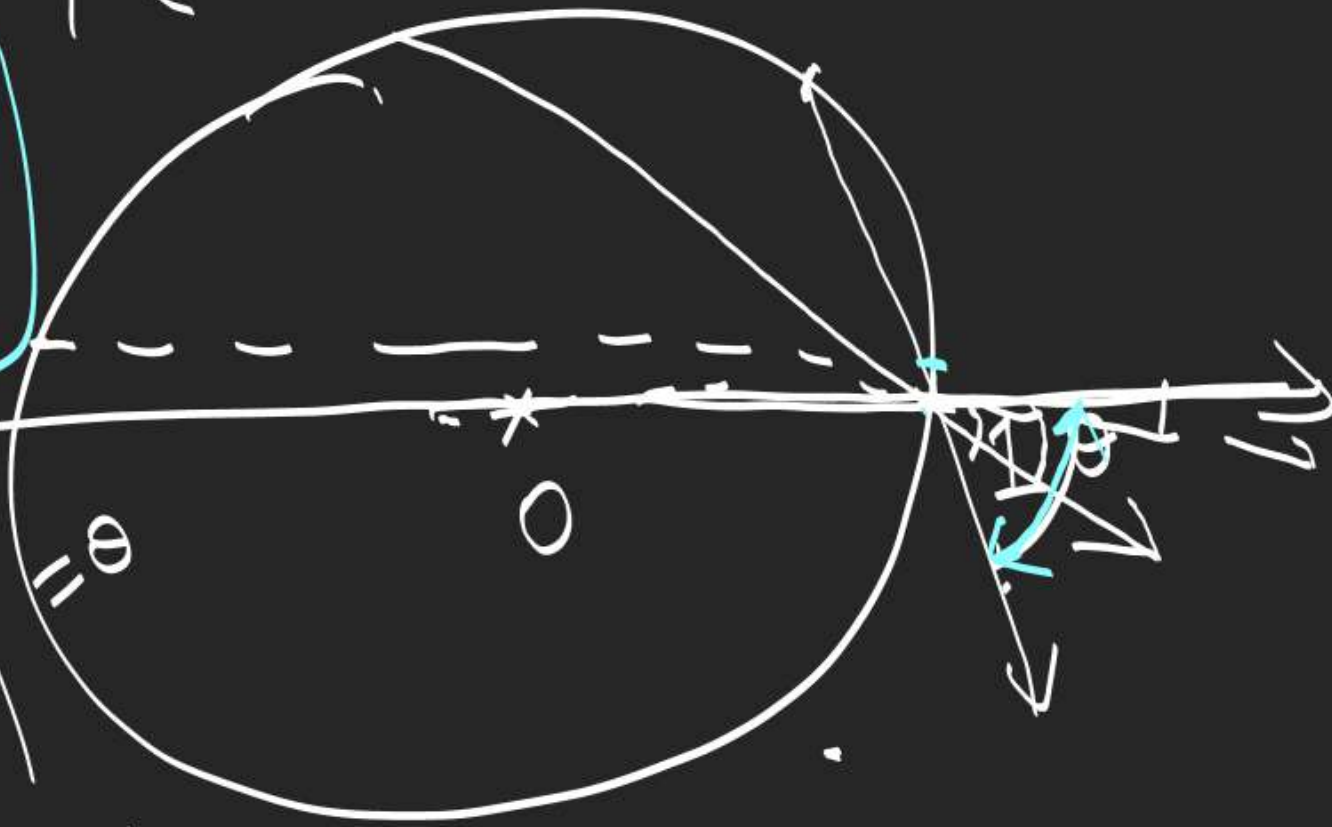
$$3(1-t^2)$$

$$z\bar{z} =$$

$$8t$$

$$\leq 1$$

$$|u|^2 =$$



$$\frac{2i}{\left(\frac{1}{z}\right) - z} = \frac{2i}{\overline{z} - z} = \frac{2i}{-2i \operatorname{Im}(z)}$$

$$= -\frac{1}{\operatorname{Im}(z)} \in [-1, 1]$$

$$(z - z_0)(\bar{z} - \bar{z}_0) = r^2$$

$$\frac{1}{\bar{z}} = \frac{z}{|z|^2}$$

$$(z - z_0)(\bar{z} - \bar{z}_0) = r^2 \Rightarrow |z|^2 - (z\bar{z}_0 + \bar{z}z_0) + |z_0|^2 = r^2 \quad (1)$$

$$(z - z_0)^2 = 4r^2 \Rightarrow \left(\frac{z}{|z|^2} - z_0\right)\left(\frac{\bar{z}}{|z|^2} - \bar{z}_0\right) = 4r^2 \Rightarrow \frac{1}{|z|^2} - \left(\frac{z\bar{z}_0 + \bar{z}z_0}{|z|^2} + |z_0|^2\right) = 4r^2 \quad (2)$$

$$(1) - (2) \times |z|^2$$

$$|z|^2 - 1 = 2(4|z|^2 - 1) \quad |z|^2 - 1 + |z_0|^2(1 - |z|^2) = r^2(1 - 4|z|^2)$$

$$(1 - |z|^2)(1 - |z_0|^2) = (2|z_0|^2 - 2)(1 - 4|z|^2)$$