

$${}^nC_r = \frac{S_3 S_1 S_6 S_7 S_5}{S_1 S_3 S_5 S_6 S_7}$$

Arrange  $n$  person in  $r$  seat  $n$   $0 \leq r \leq n$

$$P_1 P_2 \dots P_r$$

$$P_1 P_3 P_4 \dots P_r P_{r+1} \rightarrow r!$$

$${}^nP_r =$$

$$r! + r! + r! + \dots + r!$$

${}^nC_r$  times

$${}^nC_r = \frac{{}^nP_r}{r!} = \frac{n!}{(n-r)! r!}$$

30 students arrange 30 students in chairs  $\rightarrow {}^{30}P_5 = \frac{30!}{25!}$   
 $\downarrow$  select 5  $= {}^{30}C_5 \cdot 5!$

$$= {}^{30}C_5 = \frac{30!}{25! 5!} = \frac{30 \times 29 \times 28 \times 27 \times 26}{5 \times 4 \times 3 \times 2 \times 1}$$

$${}^nC_r = {}^nC_{n-r} \rightarrow \text{Pascal's mirror formula.}$$

$$\frac{n!}{(n-r)! (n-(n-r))!} = \frac{n!}{(n-r)! r!}$$

$${}^nC_r = {}^{n-1}C_r + {}^{n-1}C_{r-1} \rightarrow \text{Pascal's triangle formula}$$

$$r {}^nC_r = n {}^{n-1}C_{r-1}$$

$$\frac{{}^nC_r}{r+1} = \frac{{}^{n+1}C_{r+1}}{n+1}$$

$n$   
 $\swarrow$   $\searrow$   
 $r$  objects  $n-r$

Select 'r' persons out of 'n' given persons;  
 $P_1, P_2, P_3, \dots, P_n$

$$= {}^nC_r$$

=  $P_1$  is present in the selection +  $P_1$  is not present in selection.

$$= 1 \times {}^{n-1}C_{r-1} + {}^{n-1}C_r$$

select  $P_1$

select  $r-1$  persons



P.T.  ${}^n P_r = r \cdot {}^{n-1} P_{r-1} + {}^{n-1} P_r$

arrange!  
 in person  
 in 'r' seats =  $P_1$  is there +  $P_1$  is not there  
 $= r \times {}^{n-1} P_{r-1} + {}^{n-1} P_r$   
 arrange  $P_1$       arranging remaining persons

— — —  $P_1$  — — —

$${}^nC_r = n {}^{n-1}C_{r-1}$$

select 'r' person out of 'n' persons

$$= {}^nC_r$$

$$= n \times {}^{n-1}C_{r-1}$$

select 1st person

selecting remaining persons

$P_1$

$P_2 P_3 \dots P_r$

$P_2$

$P_1 P_3 \dots P_r$

$P_3$

$P_1 P_2 P_4 \dots P_r$

⋮

$P_r$

$P_1 P_2 \dots P_{r-1}$

1. (2)  ${}^{10}C_3 - {}^4C_3$  or  $0 + {}^4C_2 \times {}^6C_1 + {}^4C_1 {}^6C_2 + {}^6C_3$   
 6 points (no 3 are collinear)

Find no. of (3)  ${}^{10}C_4 - ({}^4C_4 + {}^4C_3 {}^6C_1)$

(1) straight lines  ${}^4C_2$  or  ${}^4C_2 {}^6C_2 + {}^4C_1 {}^6C_3 + {}^6C_4$

(2) triangles

(3) quadrilaterals

using these points.

4 collinear points.

(1)  ${}^{10}C_2 - {}^4C_2 + 1$   
 $1 + {}^4C_1 {}^6C_1$  or  ${}^6C_2$   
 $\frac{10!}{8!2!} - \frac{4!}{2!2!} + 1$   
 $= \frac{10 \times 9}{2 \times 1} - \frac{4 \times 3}{2 \times 1} + 1$   
 $= 45 - 6 + 1$   
 $= 40$



