

$$\sin\left(\frac{\pi}{2} - \theta\right) = +\cos\theta$$

$$\sin(\pi - \theta) = +\sin\theta$$

$$\sin\left(7\frac{\pi}{2} + \theta\right) = -\cos\theta$$

Rem=3

$$\sin(32\pi + \theta) = +\sin\theta$$

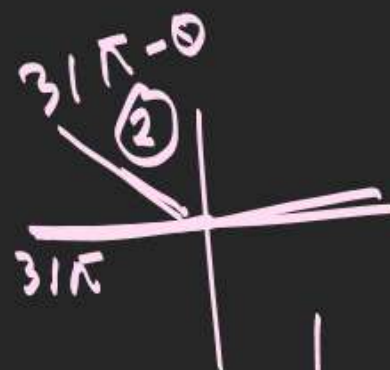
$$\underline{\cos}\left(\overset{\text{Rem}=3}{\frac{7\pi}{2}} - \theta\right) = -\sec \theta$$



$$\tan\left(\frac{7\pi}{2} - \theta\right) = +\cot \theta$$

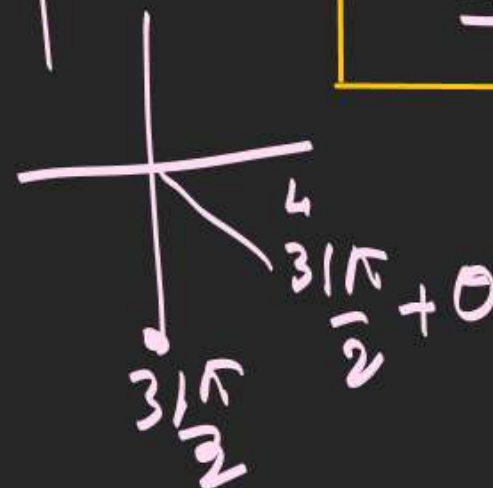
③

$$\underline{\cos}(31\pi - \theta) = +\cos \theta$$



$$\underline{\sec}\left(\overset{4 \times 31}{\frac{31\pi}{2}} + \theta\right) = +\sec \theta$$

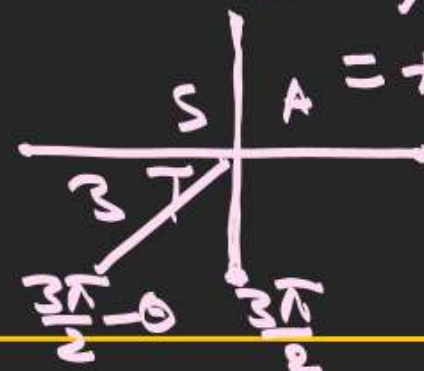
4) 31 | 128  
28  
3



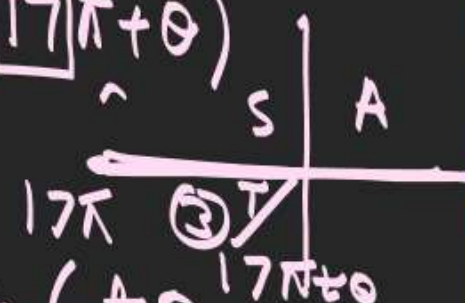
$$\underline{\tan}(\pi + \theta) = +\tan \theta$$



$$\underline{\tan}\left(\frac{3\pi}{2} - \theta\right) = +\cot \theta$$



$$\underline{\cot}(17\pi + \theta) = +\cot \theta$$

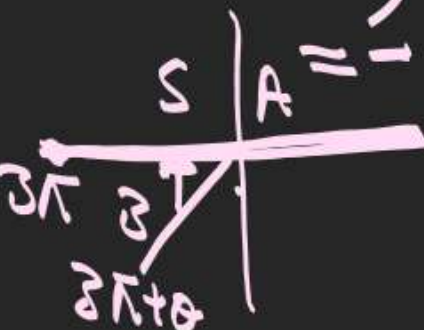


$$\underline{\cos}\left(\frac{9\pi}{2} - \theta\right) = +\sin \theta$$

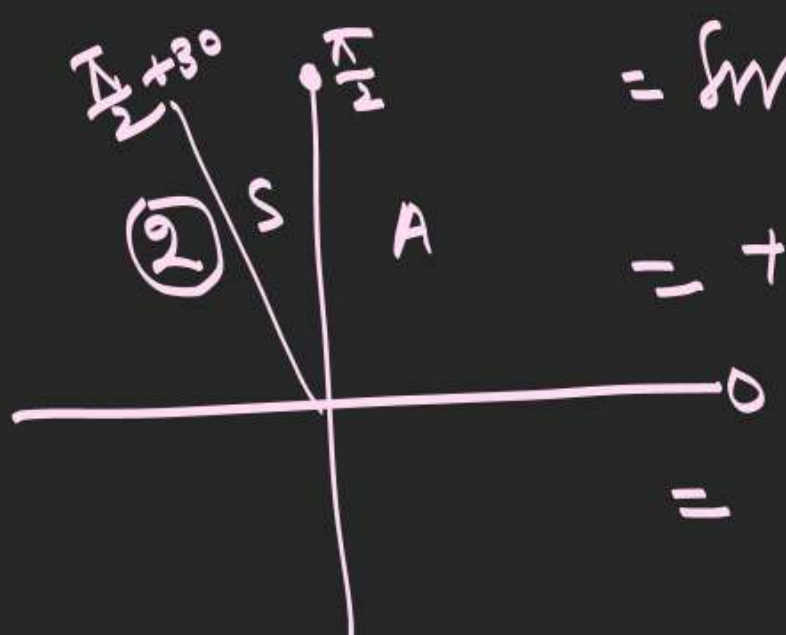
4) 9 | 2  
8  
1




$$\underline{\sin}(3\pi + \theta) = -\sin \theta$$




Q  $\sin(120^\circ) = \sin(90^\circ + 30^\circ)$   
 $= \sin\left(\frac{\pi}{2} + 30^\circ\right)$   
 $= + \underline{\cos 30^\circ}$   
 $= \frac{\sqrt{3}}{2}$




Q  $\cos(120^\circ) = \cos(90^\circ + 30^\circ)$   
 $= \cos\left(\frac{\pi}{2} + 30^\circ\right)$   
 $= - \sin 30^\circ$   
 $= -\frac{1}{2}$



Q  $\tan(120^\circ) = \tan(90^\circ + 30^\circ)$   
 $= \tan\left(\frac{\pi}{2} + 30^\circ\right)$   
 $= -\cot 30^\circ$   
 $= -\sqrt{3}$



Q  $\sin(150^\circ) = \sin(90^\circ + 60^\circ)$   
 $= \sin\left(\frac{\pi}{2} + 60^\circ\right)$   
 $= + \underline{\cos 60^\circ}$   
 $= \frac{1}{2}$





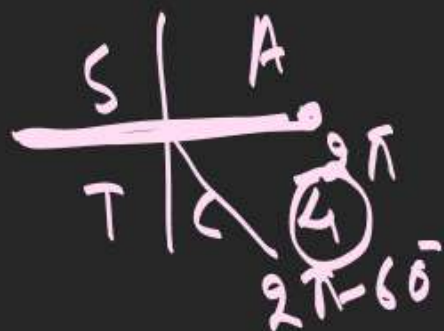
$90^\circ, 180^\circ, 270^\circ, 360^\circ$ 

$$Q \tan 300^\circ = \tan(360^\circ - 60^\circ)$$

$$= \tan(2\pi - 60^\circ)$$

$$= -\tan 60^\circ$$

$$= -\sqrt{3}$$



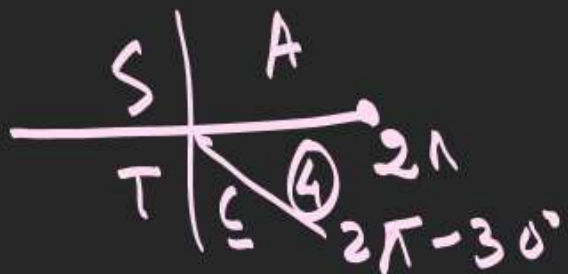
$$Q \sec(330^\circ)$$

$$\sec(360^\circ - 30^\circ)$$

$$= \sec(2\pi - 30^\circ)$$

$$\therefore +\sec 30^\circ$$

$$= \frac{1}{\cos 30^\circ} = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}}$$



Q ~~Sec~~ (240°)

$$= \cos (180^\circ + 60^\circ)$$

$$= \cos (\pi + 60^\circ)$$

$$= -\cos 60^\circ$$

$$= -\frac{1}{2}$$



Q Sec (600°)

$$\sec (630^\circ - 30^\circ)$$

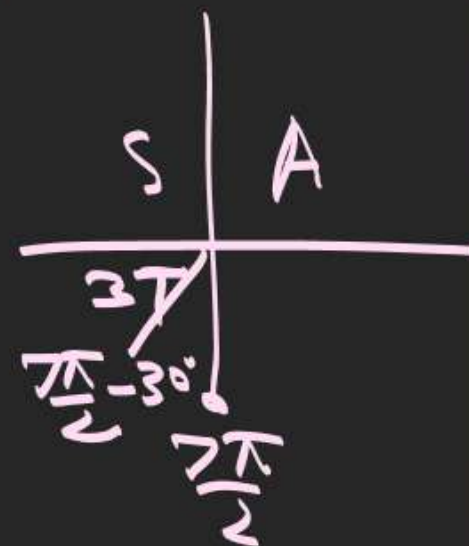
$$\sec \left( \frac{7\pi}{2} - 30^\circ \right)$$

$$= -\sec 30^\circ$$

$$= -\frac{1}{\sin 30^\circ}$$

$$= -\frac{1}{\frac{1}{2}} = -2$$

90°, 180°, 270°, 360°, 450°, 540°, 630°  
 $\frac{7 \times 90^\circ}{2}$   
 $\frac{7\pi}{2}$



Yed

	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$135^\circ$	$150^\circ$	$180^\circ$
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{1}{\sqrt{2}}$	$-\frac{\sqrt{3}}{2}$	-1
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	$\infty$	$-\sqrt{3}$	-1	$-\frac{1}{\sqrt{3}}$	0
$\cot \theta$	$\infty$	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0	$-\frac{1}{\sqrt{3}}$	-1	$-\sqrt{3}$	$-\infty$
$\sec \theta$	$\infty$	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	$\infty$
$\csc \theta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	$\infty$	-2	$-\sqrt{2}$	$-\frac{2}{\sqrt{3}}$	-1

4

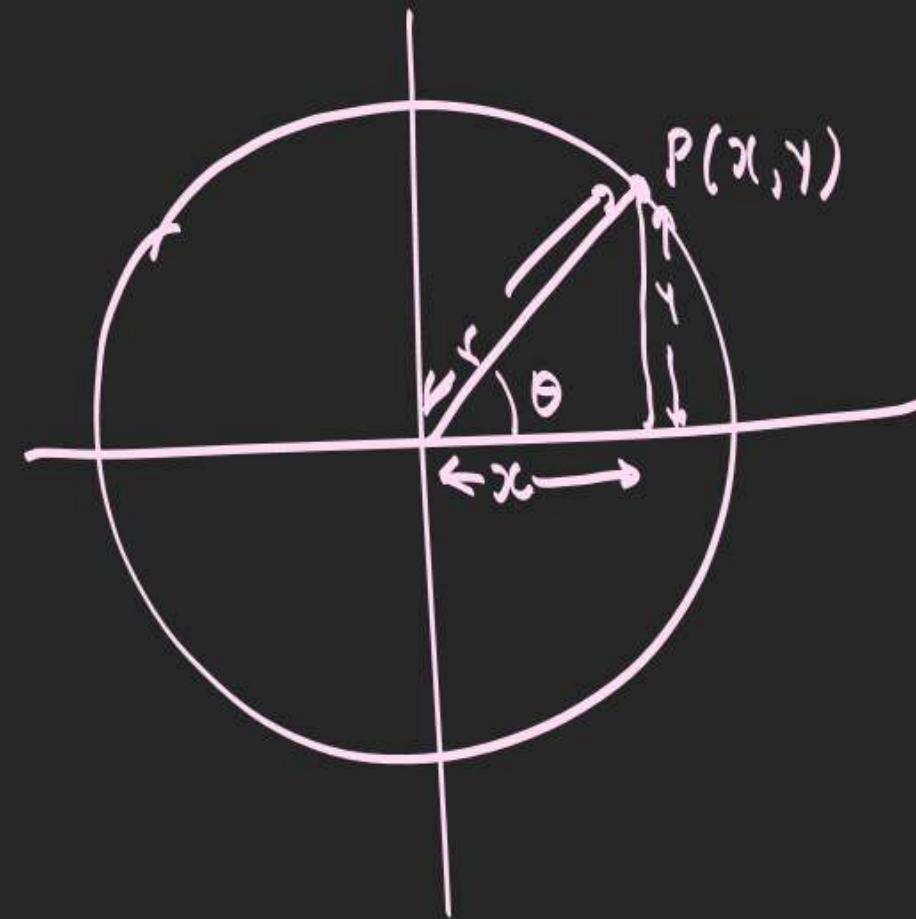
8



## Actual Definition of $\sin \theta$ & $\cos \theta$

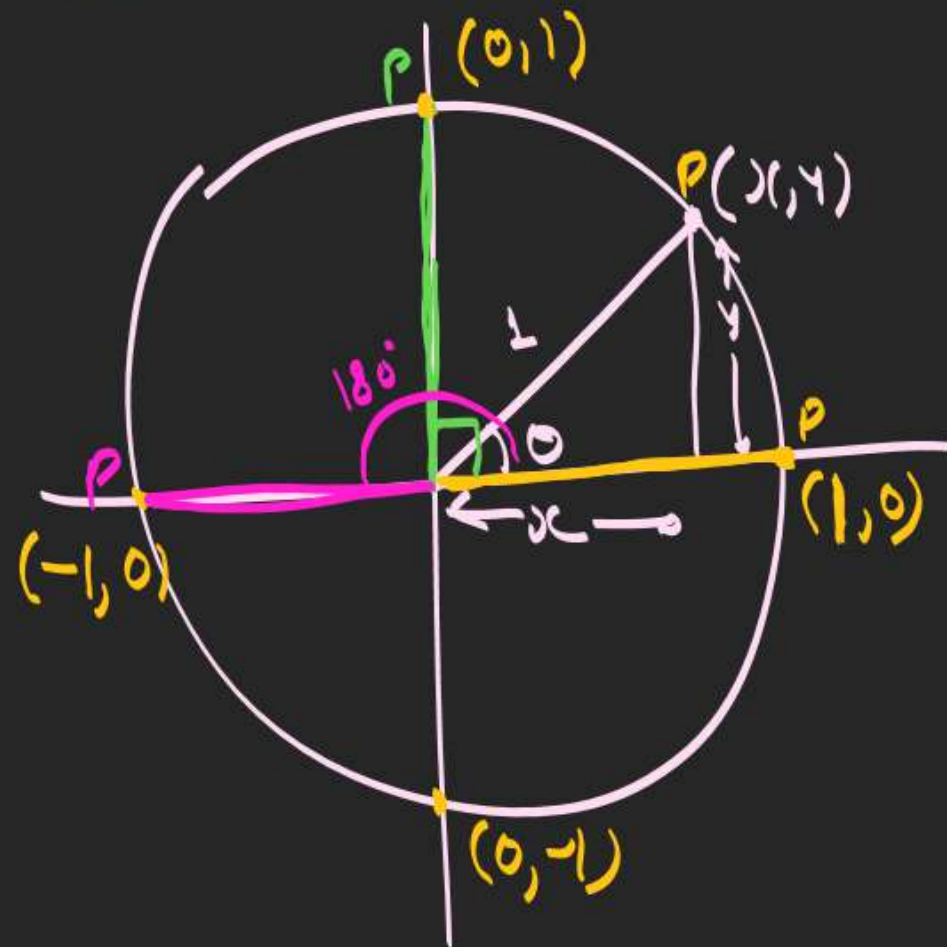
$$\sin \theta = \frac{\text{ordinate of Pt. P}}{\text{rad.}} = \frac{y \text{ coord.}}{\text{rad}}$$

$$\cos \theta = \frac{\text{Abscissa of Pt. P}}{\text{rad}} = \frac{x \text{ coord.}}{\text{rad}}$$



When Circle is Unit Circle.

Unit circle is circle with  $\text{rad} = 1$



$$\sin \theta = \frac{y(\text{coord})}{1} = y$$

$$\cos \theta = \frac{x(\text{coord})}{1} = x$$

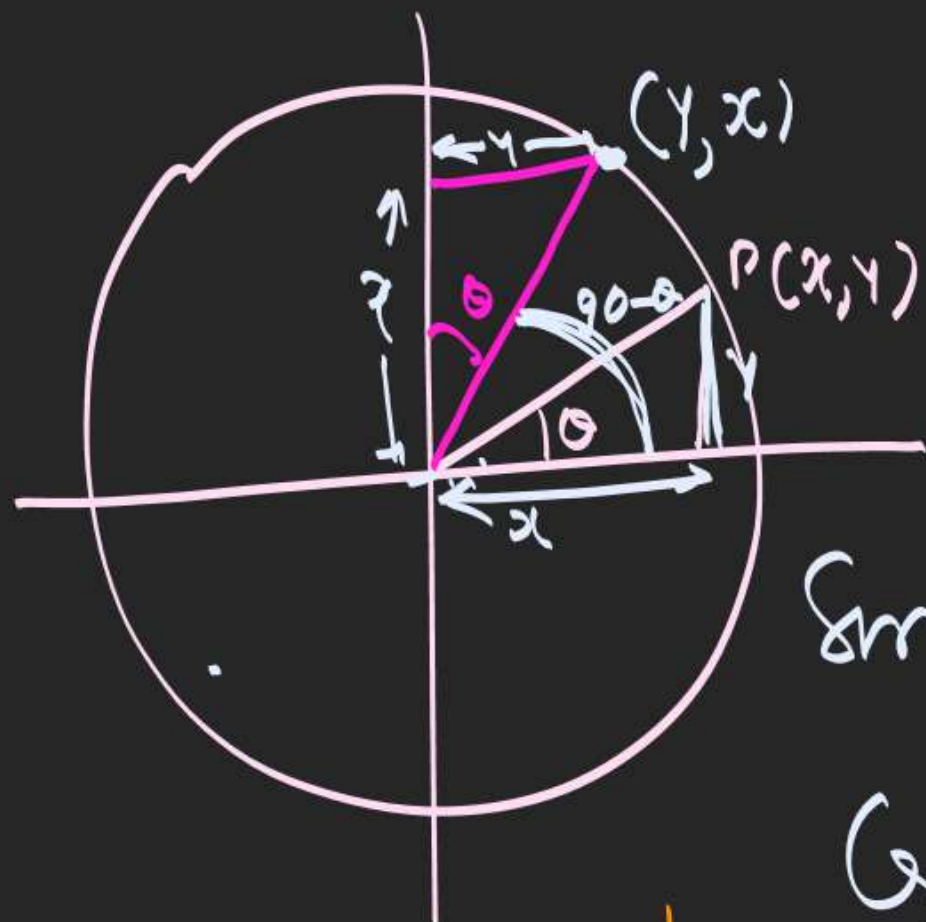
$\cos 0^\circ = \frac{1}{1} = 1$	$\cos 90^\circ = \frac{0}{1} = 0$	$\cos 180^\circ = \frac{-1}{1} = -1$
$\sin 0^\circ = \frac{0}{1} = 0$	$\sin 90^\circ = \frac{1}{1} = 1$	$\sin 180^\circ = \frac{0}{1} = 0$

$\sin(\frac{\pi}{2} - \theta) = + \cos \theta$  Kyu?

$\sin(\frac{\pi}{2} - \theta) = + \sin \theta$  Kyu

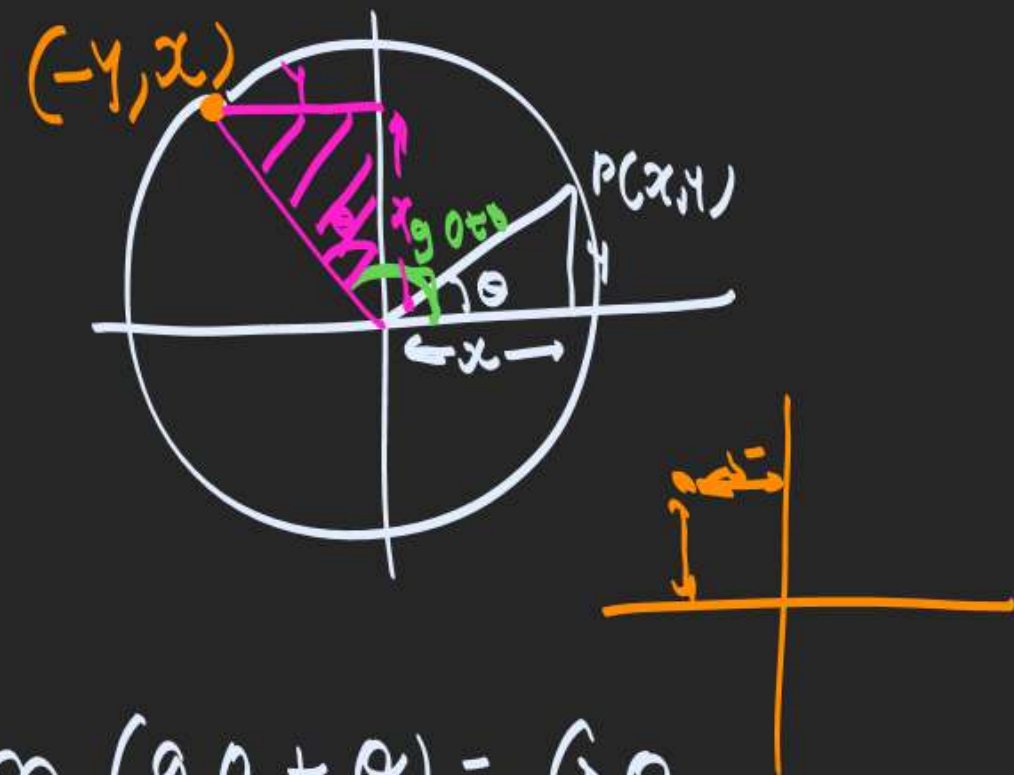
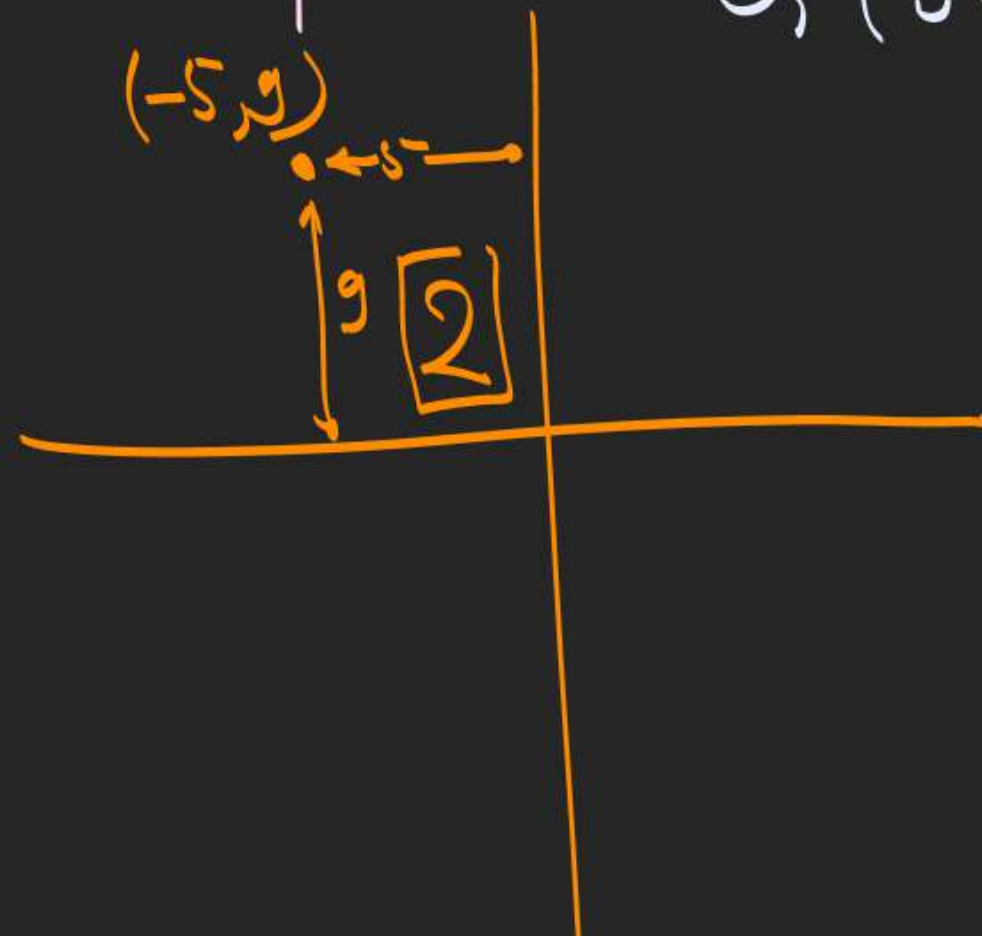
Logic Adv Level





$$\sin(90 - \theta) = \frac{x}{r} = \cos \theta$$

$$\cos(90 - \theta) = \frac{y}{r} = \sin \theta$$

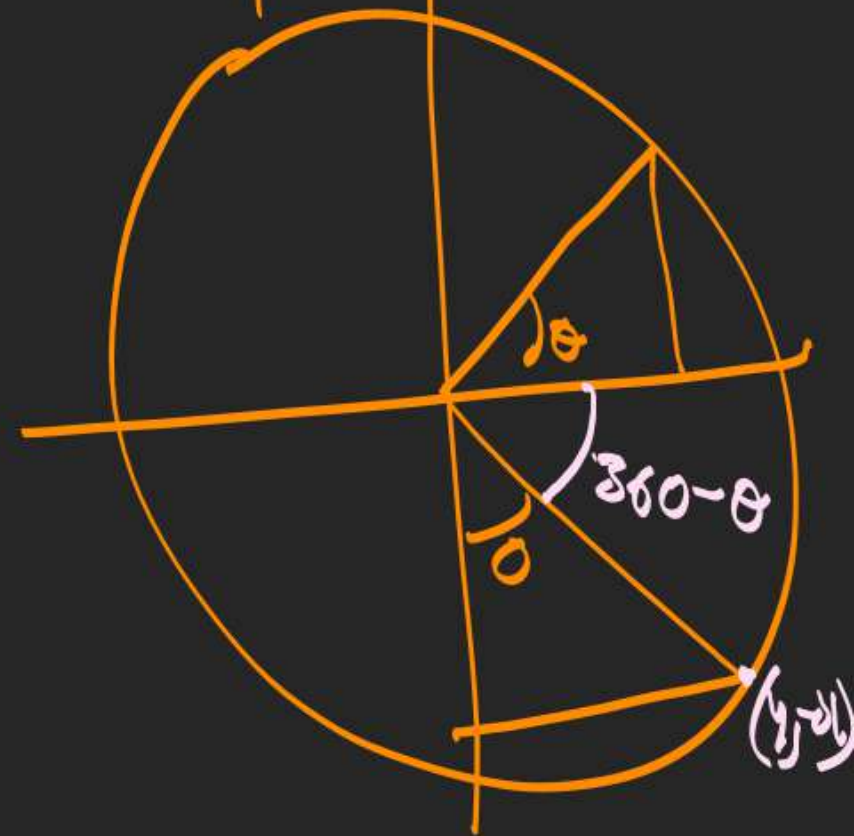
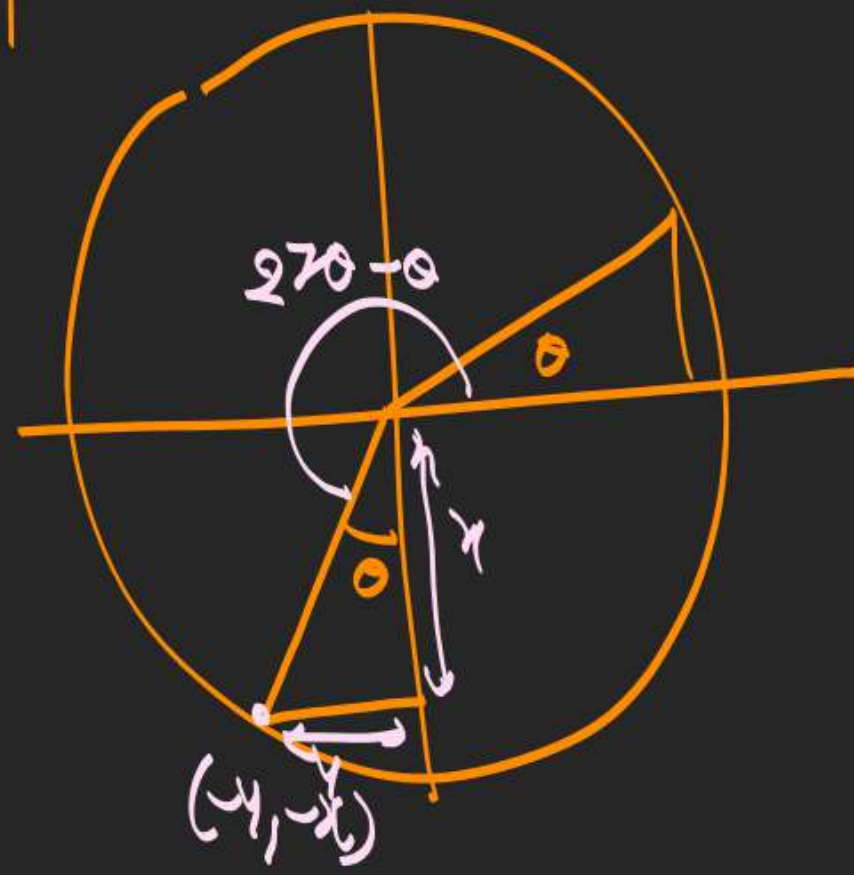
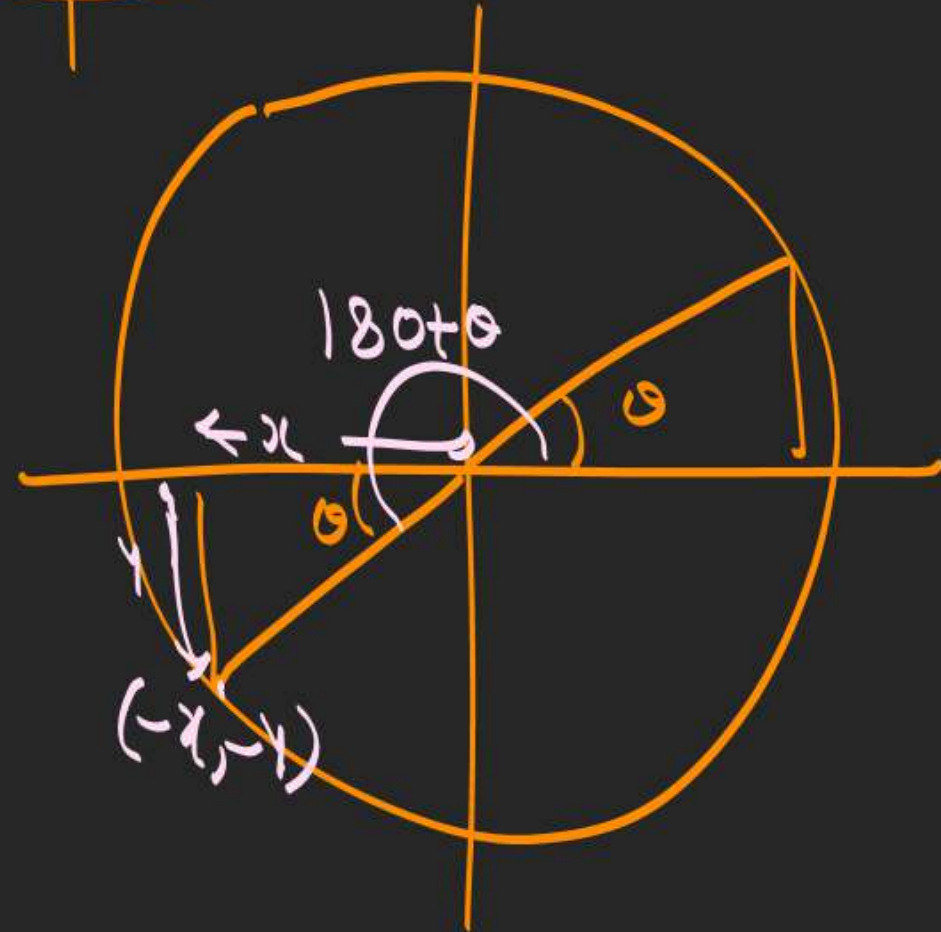
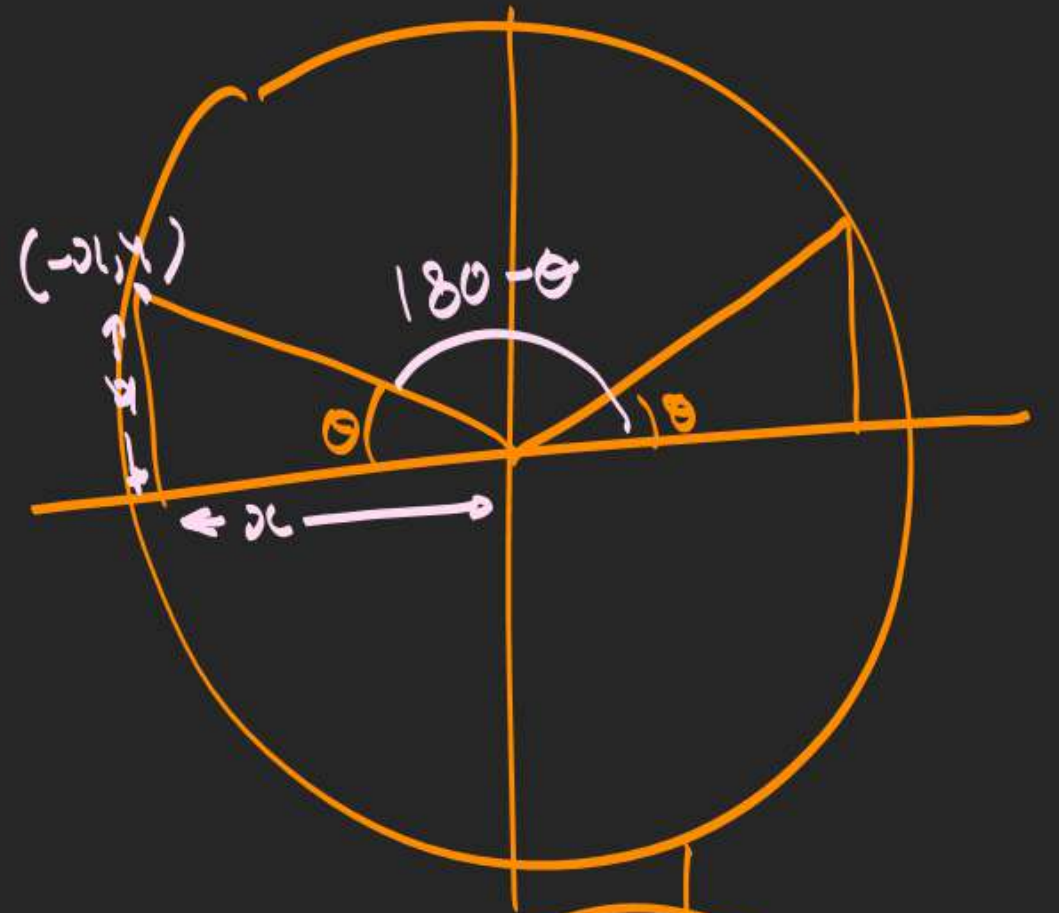
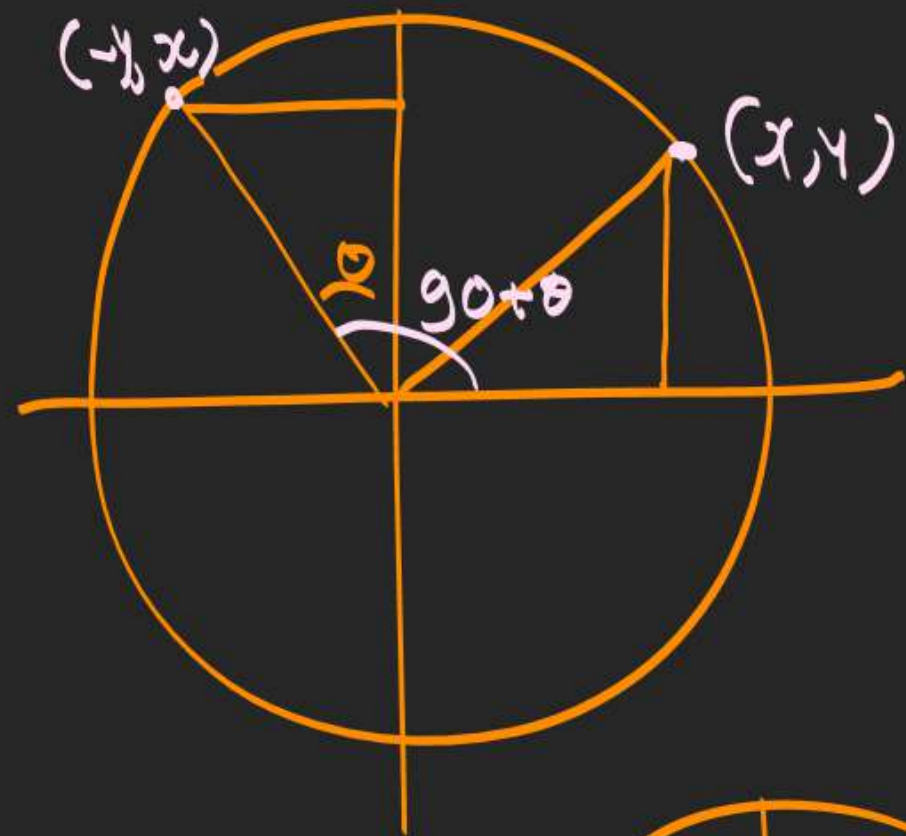
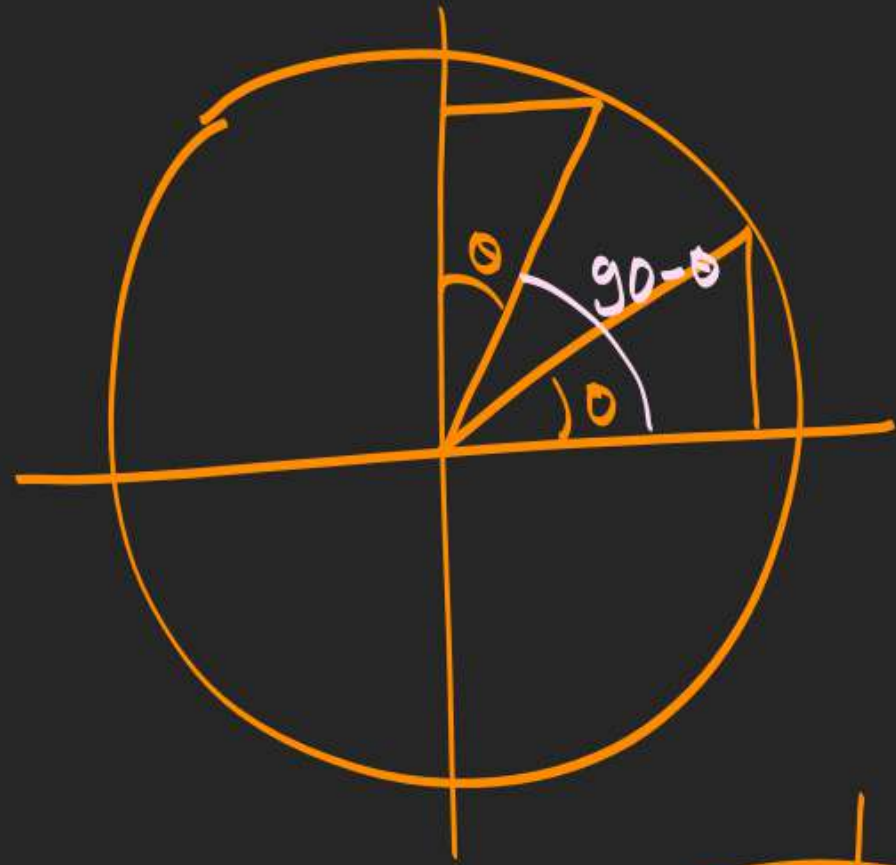


$$\sin(90 + \theta) = \cos \theta$$

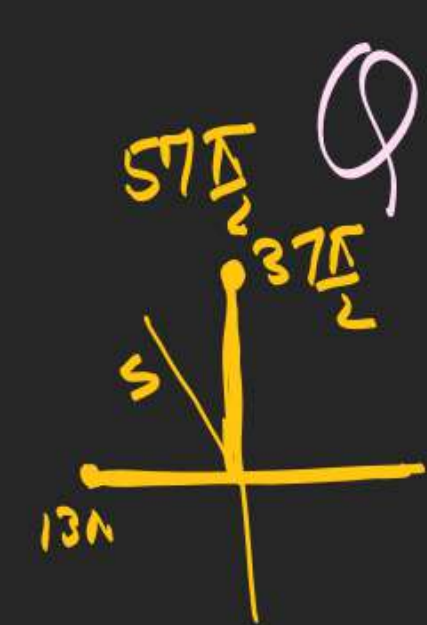
$$\cos(90 + \theta) = -\sin \theta$$

$$\sin(90 + \theta) = \frac{y(\text{coord})}{r} = \frac{x}{r} = \cos \theta$$

$$\cos(90 + \theta) = \frac{x(\text{coord})}{r} = -\left(\frac{y}{r}\right) = -\sin \theta$$







$$\sin\left(\frac{31\pi}{2} + \theta\right) \cos(13\pi + \theta) \cdot \sin\left(\frac{26\pi}{2} - \theta\right) \cdot \cos\left(\theta - \frac{57\pi}{2}\right)$$

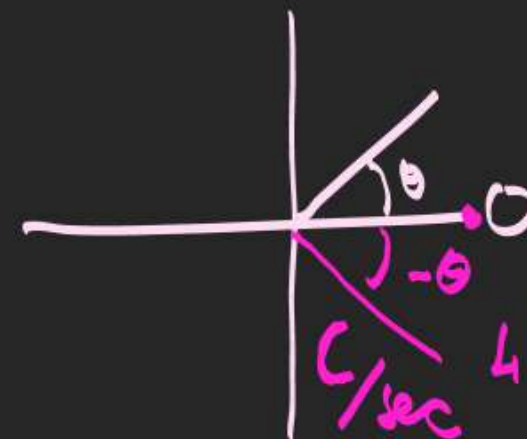
$$\sin\left(\frac{37\pi}{2} + \theta\right) \cos(13\pi + \theta) \sin(13\pi - \theta) \{-\cos\left(\frac{57\pi}{2} - \theta\right)\}$$

$$(+\cos\theta) (-\cos\theta) (+\sin\theta) \{+(-\sin\theta)\}$$

$$- \cos^2\theta \times \sin^2\theta$$

$$- \cancel{\cos^2\theta} \times \frac{\sin^2\theta}{\cancel{\cos^2\theta}} = -\sin^4\theta$$

Cos, Sec - Minus  
Ko kha Jate  
(-θ) hone Par h.



$$\sin(-\theta) = \sin(0 - \theta) = -\sin\theta$$

$$\cos(-\theta) = +\cos\theta$$

$$\tan(-\theta) = -\tan\theta$$

$$\cot(-\theta) = -\cot\theta$$

$$\sec(-\theta) = -\sec\theta$$

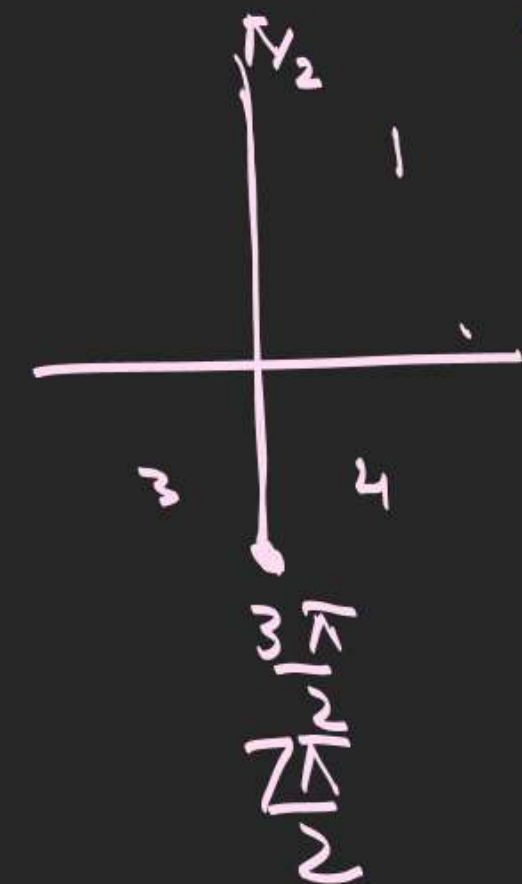
$$\csc(-\theta) = -\csc\theta$$



$$Q \quad \frac{\tan\left(x - \frac{\pi}{2}\right) \cdot \sec\left(\frac{3\pi}{2} + x\right) \cdot \sec^3\left(\frac{\pi}{2} - x\right)}{\sec\left(x - \frac{\pi}{2}\right) \cdot \tan\left(\frac{3\pi}{2} + x\right)} = ?$$

$$\frac{\tan\left(-\left(\frac{\pi}{2} - x\right)\right) \sec\left(\frac{3\pi}{2} + x\right) \left(\sec\left(\frac{\pi}{2} - x\right)\right)^3}{\sec\left(+\left(\frac{\pi}{2} - x\right)\right) \tan\left(\frac{3\pi}{2} + x\right)}$$

$$\frac{+ \left(\cancel{\sec x}\right) \left(+\cancel{\tan x}\right) \left(+\sec x\right)^3}{\left(+\cancel{\sec x}\right) \left(-\cancel{\tan x}\right)} = -\sec^3 x$$



-1

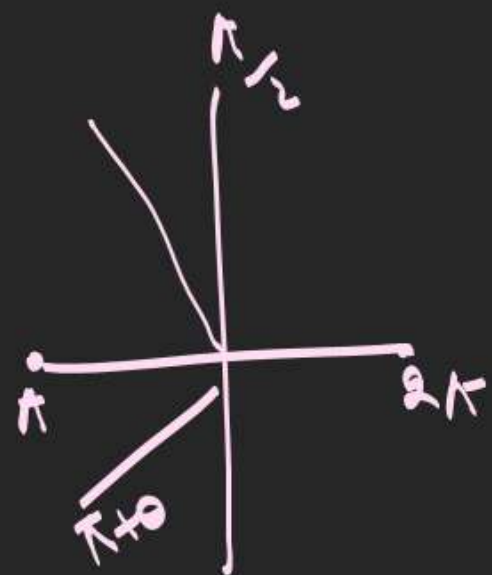
$$Q \quad \frac{\sin(90+\theta) \sec(-\theta) \tan(180+\theta)}{\sec(360-\theta) \sin(180+\theta) \cot(90-\theta)} = ?$$

$$\sec(360-\theta) \sin(180+\theta) \cot(90-\theta)$$

$$\sin\left(\frac{\pi}{2}+\theta\right) \cdot \sec \theta \cdot \tan(\pi+\theta)$$

$$\sec(2\pi-\theta) \sin(\pi+\theta) \cot\left(\frac{\pi}{2}-\theta\right)$$

$$\frac{(+\sin/\theta) \cancel{\sec \theta} \times (+\tan \theta)}{(+\cancel{\sec \theta}) (+\cancel{\sin \theta}) (+\tan \theta)} = 1$$



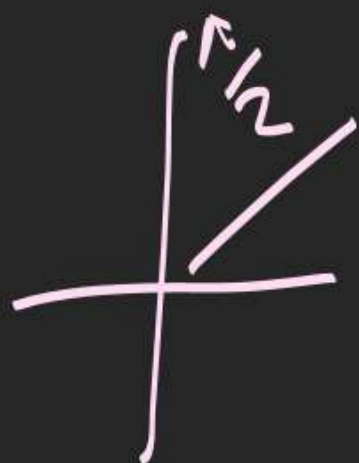
$$\frac{-\sin \theta \sec \theta + \tan \theta}{\sec \theta - \sin \theta \tan \theta} = 1$$



$$Q \sin(-65^\circ) = -\sin 65^\circ$$

$$Q \cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$$

$$\cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 27^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$$



$$\sin(90-63^\circ) \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\sin 63^\circ}$$

$$+ \cos 63^\circ \times \frac{1}{\cos 63^\circ} = 1$$

P.T.

$$Q \tan \theta + \tan(\pi - \theta) + \cot\left(\frac{\pi}{2} + \theta\right) - \tan(2\pi - \theta) = 0$$

$$Q \frac{\tan(90+\theta) \cdot \sec(180+\theta)}{\cos(180+\theta) \sec(-\theta)} = -1$$

$$Q \frac{\cos}{\sin(90+\theta)} + \frac{\sin(-\theta)}{\sin(180+\theta)} - \frac{\tan(90+\theta)}{\cot \theta} = 3$$

$$Q \frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ} = 3 + 2\sqrt{2}$$



$$Q \quad 4 \cot^2 45^\circ - \sec^2 60^\circ + \sin^2 30^\circ = \frac{1}{4}$$

$$Q \quad \tan^2 \frac{\pi}{6} + \tan^2 \frac{\pi}{4} + \tan^2 \frac{\pi}{3} = \frac{13}{3}.$$