

## LIMIT

DPP SET 2, 4, 8.

$$Q \lim_{x \rightarrow 1} \left( 1 - x + [x-1] + [1-x] \right) = ?$$

<p>LHL</p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>x \rightarrow 1^-</math>  <math>x = 1-h</math> </div> $\lim_{h \rightarrow 0} \left( x - (x-h) + [x-h-x] + [x-(x-h)] \right)$ $\lim_{h \rightarrow 0} \left( h + [0-h] + [0+h] \right)$ $\lim_{h \rightarrow 0} \boxed{h} + (-1) + 0 = 0 + -1$ $= -1$	<p>RHL</p> $\lim_{x \rightarrow 1^+} \lim_{h \rightarrow 0} \left( x - (x+h) + [x+h-x] + [x-(x+h)] \right)$ $\lim_{h \rightarrow 0} \left( -h + [0+h] + [0-h] \right)$ $\lim_{h \rightarrow 0} \cancel{-h} + 0 + -1$ $-1$
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$$\therefore \lim_{x \rightarrow 1} (1 - x + [x-1] + [1-x]) = -1$$

## LIMIT

$$\text{Q} \lim_{x \rightarrow \infty} \sec^{-1}\left(\frac{x}{x+1}\right) = \text{Not Defined}$$

$$x < x+1$$

$$\frac{x}{x+1} < 1$$

$$\sec^{-1}( < 1)$$

Not in Domain



$$\text{Q} \underset{\substack{\text{Ans} \\ \text{LHL Demanded}}}{\lim_{x \rightarrow 0^-}} \frac{x((\bar{x}) + |x|) \sin[x]}{|x|} = \begin{cases} -\sin 1 & x < 0 \\ \sin 1 & x > 0 \end{cases}$$

$$\lim_{h \rightarrow 0} \frac{-h([0-h] + |-h|) \sin[0-h]}{|-h|}$$

$$\lim_{h \rightarrow 0} \frac{-h(-1+h) \sin(-1)}{h}$$

$$\lim_{h \rightarrow 0} -(-h) \cdot \sin(1) = -(1-0) \sin 1 = -\sin 1$$

## LIMIT

$$\text{Q) } \lim_{\substack{x \rightarrow 1^+ \\ \text{Main}}} \frac{(1 - |x| + \sin |1-x|) \sin \left( \frac{\pi}{2} [1-x] \right)}{|1-x| [1-x]}$$

RHL Demanded

$x = 1+h$

$$\lim_{h \rightarrow 0} \frac{1 - |1+h| + \sin |1-(1+h)|}{|1-(1+h)| [1-(1+h)]} \text{ for } \left( \frac{\pi}{2} [1-(1+h)] \right)$$

$$\lim_{h \rightarrow 0} \frac{1 - (1+h) + \sin(h)}{|-h| [0-h]} \sin \left( \frac{\pi}{2} [0-h] \right)$$

$$\lim_{h \rightarrow 0} \frac{(-h + \sin h) \sin \left( -\frac{\pi}{2} \right)}{h (-1)} = \frac{-1 (-h + \sin h)}{-h}$$

- A) 0      0-1  
 B) DNE      C) 1

Thode Din Thk yad Karlo

1) $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$
2) $\lim_{x \rightarrow 0} \frac{\tan x}{x} = 1$

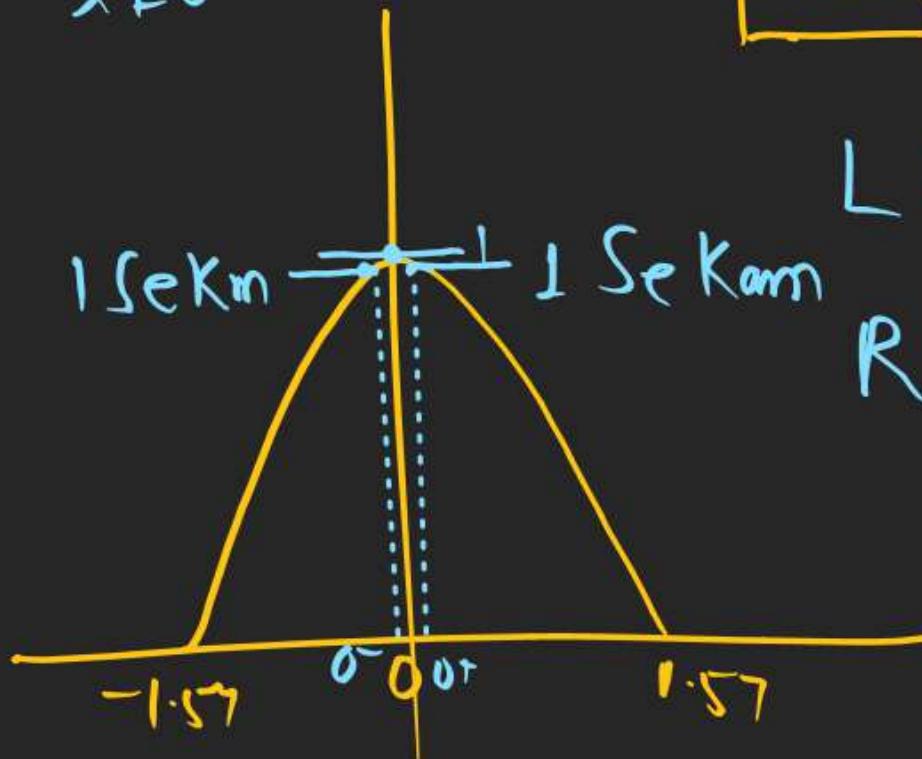
$-1 + 1 = 0$

$$= \lim_{h \rightarrow 0} \frac{h - \sin h}{-h} = \lim_{h \rightarrow 0} \boxed{1} + \boxed{\frac{\sin h}{h}}$$

**LIMIT**

$$\textcircled{Q} \lim_{\substack{x \rightarrow 0 \\ x \neq 0}} [\cos x]$$

[Trigo] then use graph  
at given limit

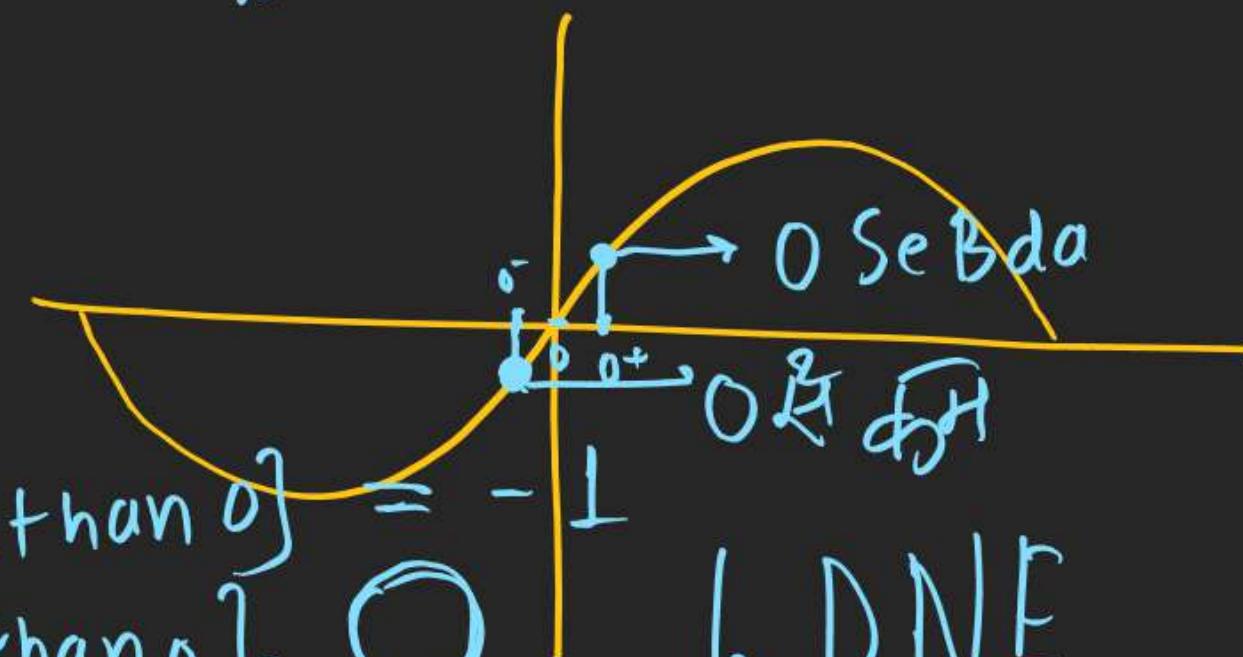


$$\begin{aligned} LHL &= [\cos(0-h)] = [less than 1] = 0 \\ RHL &= [\cos(0+h)] = [less than 1] = 0 \end{aligned}$$

$$\therefore \lim_{x \rightarrow 0} [\cos x] = 0$$

$$\textcircled{Q} \lim_{\substack{x \rightarrow 0 \\ x \neq 0}} [\sin x]$$

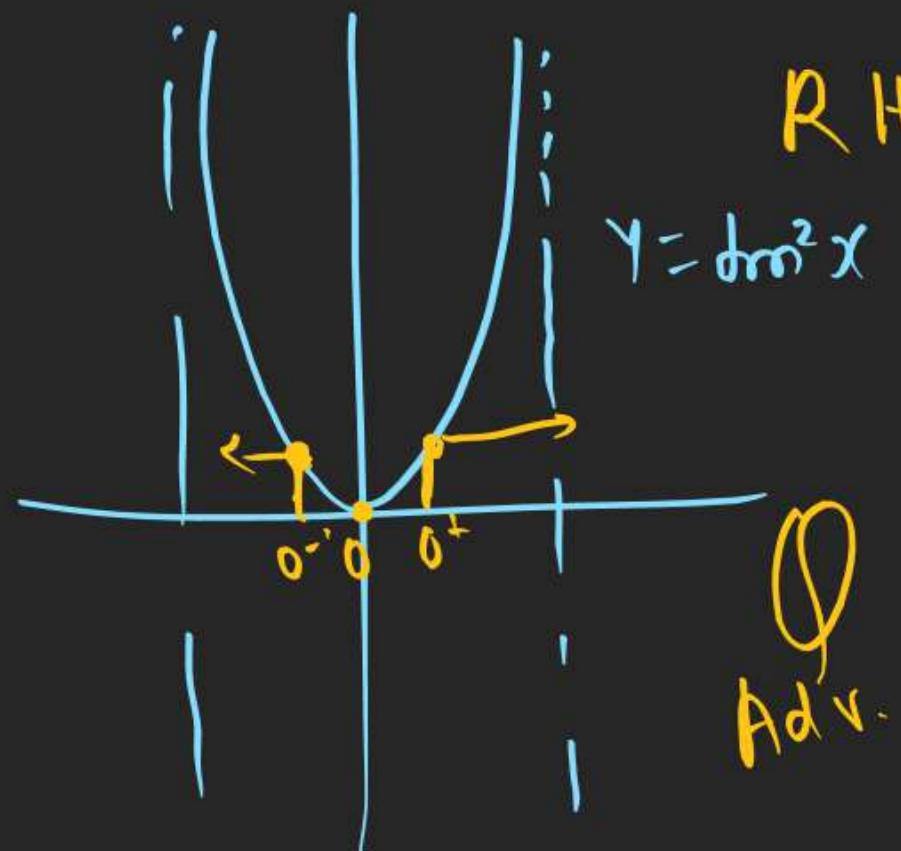
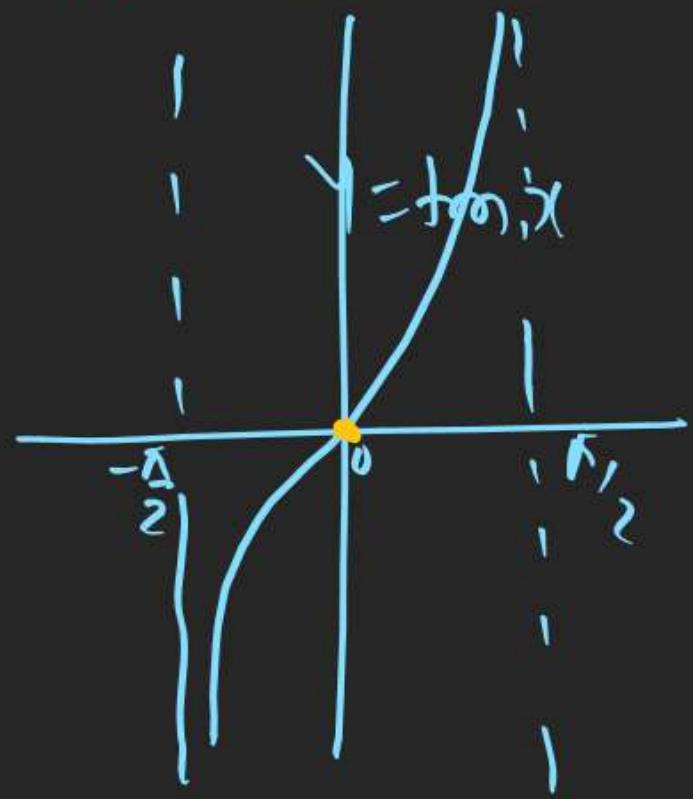
$$\begin{aligned} LHL &= [\sin(0-h)] = [less than 0] = -1 \\ RHL &= [\sin(0+h)] = [greater than 0] = +1 \end{aligned}$$



h DNE

## LIMIT

$$\text{Q} \lim_{x \rightarrow 0} [\tan^2 x]$$



$$\text{LHL} = [\tan^2(0-h)] = [\text{hrthm o}] = 0$$

$$\text{RHL} = [\tan^2(0+h)] = [\text{hrthm o}] = 0$$

$$\lim_{x \rightarrow 0} [\tan^2 x] = 0$$

Q  
Adv.

(check (cont) of  $y = [\tan^2 x]$  at  $x=0$ )

Next chapter

$$\text{LHL} = [\tan^2(0-h)] = 0 \quad \left. \begin{array}{l} \text{txnm} \\ \text{conts} \end{array} \right\}$$

$$\text{RHL} = [\tan^2(0+h)] = 0 \quad \left. \begin{array}{l} \text{txnm} \\ \text{conts} \end{array} \right\}$$

$$f'(0) = [0] = 0$$

## LIMIT

$$\text{Q} \lim_{\substack{\text{Sheets} \\ (\rightarrow 0)}} \frac{\sin[(\lambda)x]}{1 + [(\lambda)x]}$$

$$\frac{\sin 0}{1+0} = \frac{0}{1} = 0$$

$$\text{HHL} \text{ Q} \lim_{x \rightarrow 2^-} [2-x] + [(-x)] - x$$

(-3)

Ans of L in Normal one  $\Rightarrow$  L DE

$$\Rightarrow \text{LHL} = \text{RHL} \Rightarrow \left| \frac{1}{\lambda} \right| = \left| \frac{1}{\lambda-1} \right| \Rightarrow |\lambda| = |\lambda-1|$$

$$\begin{aligned} x &= x-1 \\ 0 &= -1 \end{aligned}$$

$$\lim_{x \rightarrow 0} [6x] = 0$$

$\text{Q} [\ ] \text{ If } \text{ If for some } \lambda \in \mathbb{R} - \{0, 1\}$

~~2020~~ Main  $\lim_{x \rightarrow 0} \left| \frac{1-x+|x|}{\lambda-x+|\bar{x}|} \right| = L \text{ then } L = ?$

$$\text{LHL} \lim_{h \rightarrow 0} \left| \frac{1-(-h)+|-h|}{\lambda-(-h)+|-\bar{h}|} \right| = L$$

$$\lim_{h \rightarrow 0} \left| \frac{1+h+h}{\lambda+h-1} \right| = L \Rightarrow \left| \frac{1}{\lambda-1} \right| = L$$

$$\text{RHL} \lim_{h \rightarrow 0} \left| \frac{1-h+|h|}{\lambda-h+|\bar{h}|} \right| = L$$

$$\lim_{h \rightarrow 0} \left| \frac{1-h+0}{\lambda-h+0} \right| = L \Rightarrow \left| \frac{1}{\lambda} \right| = L$$

$$L = \left| \frac{1}{\lambda} \right| = 2$$

$$\left| \frac{1}{\lambda} \right| = 2$$

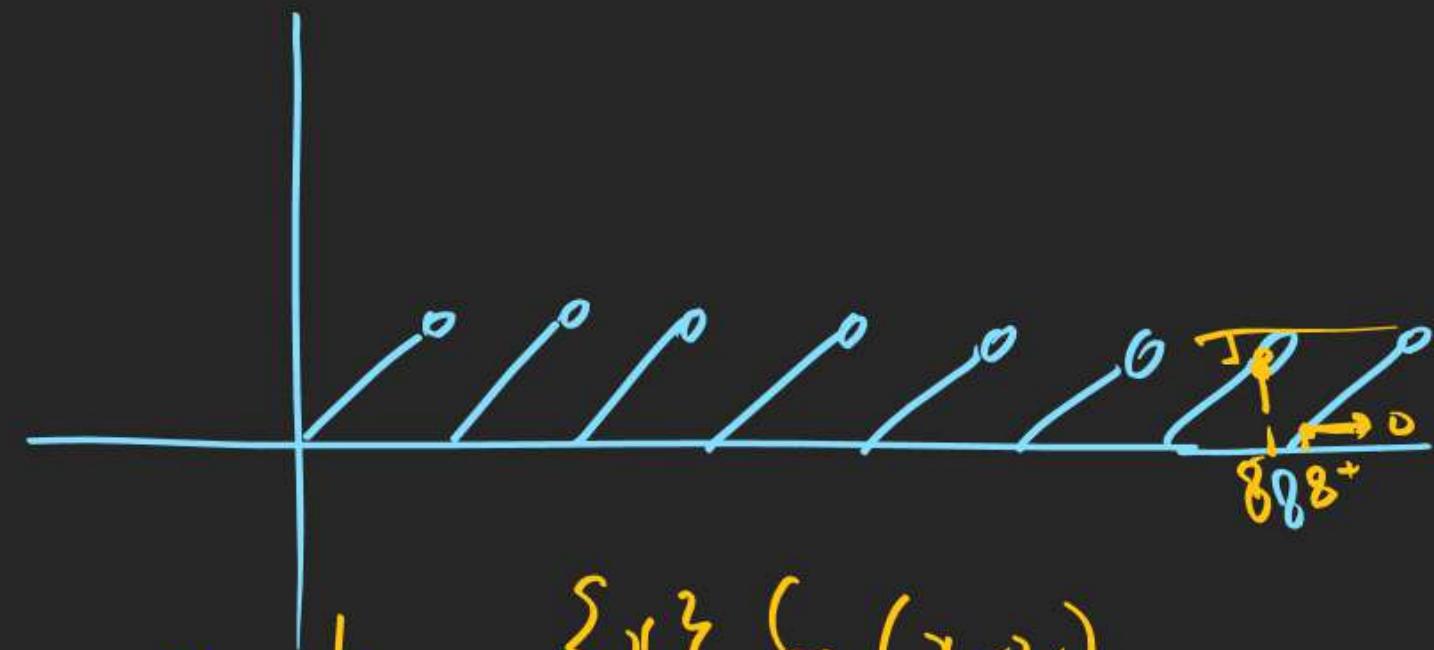
## LIMIT

$$\text{Q } \lim_{x \rightarrow 2} \{x^2\} \text{ Akashan}$$

LHL	$\left  \begin{array}{l} \text{RHL} \\ x \rightarrow 2^+ \\ \lim_{h \rightarrow 0} \{2+h\} \\ \{h\} \\ = \lim_{h \rightarrow 0} h \\ = 0 \end{array} \right.$
$x \rightarrow 2^-$	
$\lim_{h \rightarrow 0} \{2-h\}$	
$\{ -h \}$	
$\lim_{h \rightarrow 0} 1-h$	
$1-0$	
$= 1$	

$$\therefore LHL = RHL$$

LDNE



$$\text{Q } \lim_{x \rightarrow 2^+} \frac{\{x\} \ln(x-2)}{(x-2)^2} = ?$$

RHL Demanded  
 $x = 2+h$

$$\lim_{h \rightarrow 0} \frac{\{2+h\} \ln(2+h-2)}{(2+h-2)^2} = \lim_{h \rightarrow 0} \frac{\{h\} \ln h}{h^2}$$

$$\lim_{h \rightarrow 0} \frac{h \ln h}{h^2} = 1$$

## LIMIT

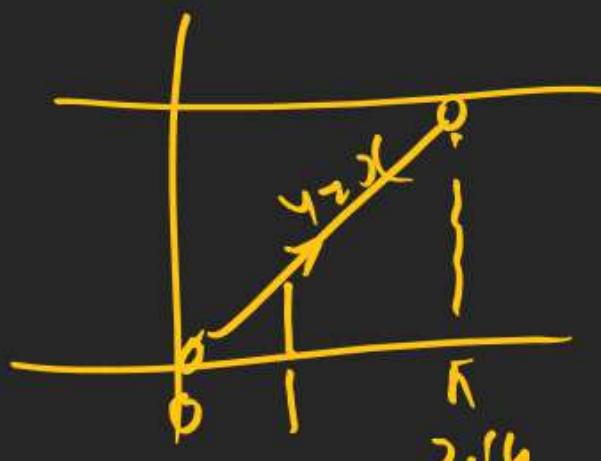
$$\text{Q} \lim_{x \rightarrow 0^-} (\cot^{-1}(\{x\}) \cot \{x\}) = ?$$

$$x=0-h \lim_{h \rightarrow 0} (\cot^{-1}(\{-h\}) \cot \{-h\})$$

$$\lim_{h \rightarrow 0} (\cot^{-1}((1-h) \cot(1-h)))$$

$$(\cot^{-1}(1) \cot(1))$$

$$(\cot^{-1}(1) \cot 1) = 1$$



$$\{-h\} = 1-h$$

$$\{-2\} = 1-2$$

$$\{2\} = 2$$

$$\text{Q} \lim_{x \rightarrow 0^+} \frac{\tan^2 \{x\}}{x^2 - [x]^2}$$

$$\lim_{h \rightarrow 0} \frac{\tan^2 \{h\}}{h^2 - [0+h]^2}$$

$$\lim_{h \rightarrow 0} \frac{\tan^2 h}{h^2 - 0} = \lim_{h \rightarrow 0} \left( \frac{\tan h}{h} \right)^2 = 1^2 = 1$$

## LIMIT

If  $f(x)$  is  
Defined  
fxn.

$$f(x) = \begin{cases} \frac{\tan^2\{x\}}{x^2 - [x]^2} & x > 0 \\ 1 & x = 0 \\ \cot^{-1}\{\{x\}\} \cot\{\{x\}\} & x < 0 \end{cases}$$

LHL      RHL  
RHL      then find  $\lim_{x \rightarrow 0^+} f(x) = ?$

$$\text{LHL } \boxed{x=0-h} \rightarrow x < 0$$

$$\lim_{x \rightarrow 0^-} \cot^{-1}\{\{x\}\} \cot\{\{x\}\} = 1$$

$$\text{RHL } \boxed{x=0+h} \rightarrow x > 0$$

$$\lim_{x \rightarrow 0^+} \frac{\tan^2\{x\}}{x^2 - [x]^2} = 1$$

$$\text{LHL} = \text{RHL}$$

$$\lim_{x \rightarrow 0} f(x) = 1$$

Nxt Chapter Aise Qs Se Bhra

Pda Rahega

$$\left. \begin{array}{l} \text{LHL} = 1 \\ \text{RHL} = 1 \\ f(0) = 1 \end{array} \right\} \text{(Ans at } x=0)$$

## LIMIT

$$\text{Q } f(x) = \begin{cases} x-1 & x \geq 1 \\ 2x^2-2 & x < 1 \end{cases}, \quad g(x) = \begin{cases} x+1 & x > 0 \\ -x^2+1 & x \leq 0 \end{cases} \quad \& \quad r(x) = |x|$$

$$\therefore \lim_{x \rightarrow 0} f(g(r(x))) \text{ fnd } \lim_{x \rightarrow 0} f(g(\sqrt{r(x)}))$$

$\text{LHL}$ $\lim_{x \rightarrow 0^-} f(g(r(0-h)))$ $\lim_{h \rightarrow 0} f(g( -h ))$ $\lim_{h \rightarrow 0} f(g(\sqrt{ h })) \xrightarrow{\text{O Bda}}$ $\lim_{h \rightarrow 0} f(h+1) \xrightarrow{\text{f is O Bda}} f(1)$ $\lim_{h \rightarrow 0} (h+1) - f(1) = 0$
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$\text{RHL}$ $\lim_{x \rightarrow 0^+} f(g(r(0+h)))$ $\lim_{h \rightarrow 0} f(g( h ))$ $\lim_{h \rightarrow 0} f(g(h)) \xrightarrow{\text{O Bda}}$ $\lim_{h \rightarrow 0} f(h+1) = \lim_{h \rightarrow 0} (h+1) - f(1) = 0$
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## LIMIT

$$\text{Q} \lim_{x \rightarrow 1} \left[ x \left[ \frac{1}{x} \right] \right]$$

LHL  $x = 1 - h$ 

$$\lim_{h \rightarrow 0} \left[ (1-h) \left[ \frac{1}{1-h} \right] \right]$$

I<sup>2</sup>Bda

$$\left[ (1-h) \times 1 \right]$$

$$\left[ 1-h \right] = 0$$

RHL  $x = 1+h$ 

$$\lim_{h \rightarrow 0} \left[ (1+h) \left[ \frac{1}{1+h} \right] \right]$$

I<sup>2</sup>Kmm

$$\left[ (1+h) \times 0 \right]$$

$$\left[ 0 \right] = 0$$

$$\therefore \lim_{x \rightarrow 1} \left[ x \left[ \frac{1}{x} \right] \right] = 0$$

Concept

$$\frac{1}{g} = \text{I}^2 \text{Bda}$$

$$\frac{10}{g} = "$$

$$\frac{10}{11} = "$$

$$\frac{10}{11} = "$$

$$\lim_{t \rightarrow 0} \left( \frac{2^t}{t^2} \right) \rightarrow \infty$$

Difficult Make graph of fxn.

$$f(x) = \lim_{t \rightarrow 0} \frac{2^x}{t^2} \cdot \cot \frac{x}{t^2} - ?$$

$$\lim_{t \rightarrow 0} \left( \frac{2^t}{t^2} \right) \rightarrow -\infty$$

$x = -ve$

$$\lim_{t \rightarrow 0} \frac{2^x}{t^2} \cot^{-1} \left( \frac{x}{t^2} \right) \rightarrow 0$$

$$\frac{2^x}{t^2} \cdot \cot^{-1}(-\infty)$$

$$Y = \frac{2^x}{t^2} \times K$$

$$Y = \frac{2^x}{t^2} \times 2$$

thought → Here we have 2 Variabls. x & t

2)  $t \rightarrow 0$  given But we do not have.

Idea about x.

$$x = 0$$

$$Y = \frac{2^x}{t^2} \cot \left( \frac{0}{t^2} \right)$$

$$\lim_{t \rightarrow 0} \frac{2^x}{t^2} \cdot \cot(0)$$

$$\frac{2^x}{t^2} \cdot \frac{1}{2} = x = 0$$



$$x = -ve$$

$$x = +ve$$

$$Q \lim_{x \rightarrow 0^+} \frac{x}{a} \left[ \frac{b}{x} \right] \quad a, b \neq 0$$

$$\lim_{h \rightarrow 0} \frac{h}{a} \left[ \frac{b}{h} \right] \quad 0 \times \infty$$

$\bar{x} = x - \{x\}$   
 $\{x\} \in [0,1)$

(M1)  $\lim_{h \rightarrow 0} \frac{h}{a} \left( \frac{b}{h} - \left\{ \frac{b}{h} \right\} \right)$

$$\frac{b}{a} - \lim_{h \rightarrow 0} \frac{h}{a} \cdot \left\{ \frac{b}{h} \right\}$$

$$\frac{b}{a} - \lim_{h \rightarrow 0} \frac{h}{a} \times (\text{any value between 0 to 1})$$

$$\frac{b}{a} - \frac{0}{a} \times (0 \text{ to } 1) = \frac{b}{a} - 0 = \frac{b}{a}$$

M12 funda

$\lim_{x \rightarrow \infty} \bar{x} = \infty$

$\lim_{h \rightarrow 0} \frac{h}{a} \left[ \frac{b}{h} \right]$  Indicate to  $\infty$

$$\lim_{h \rightarrow 0} \frac{h}{a} \times \frac{b}{h}$$

$$= \frac{b}{a} \rightarrow \frac{1}{0} \rightarrow \infty \rightarrow \infty$$

Main

$Q \lim_{x \rightarrow 0^+} x \left( \left[ \frac{1}{x} \right] + \left[ \frac{2}{x} \right] + \dots + \left[ \frac{15}{x} \right] \right)$

$$\Rightarrow x \left( \frac{1}{x} + \frac{2}{x} + \frac{3}{x} + \dots + \frac{15}{x} \right) = 1+2+3+\dots+15$$

$$\therefore \frac{(15)(16)}{2} = 120$$

DPP2

1)  $f: R \rightarrow \left[\frac{\pi}{6}, \frac{\pi}{4}\right]$

$$y = \frac{x^2+1}{x^2+\sqrt{3}}$$

$$\sqrt{3}x^2 + \sqrt{3}y = x^2 + 1$$

$$x^2(y-1) = 1 - \sqrt{3}y$$

$$\textcircled{X} \quad \frac{x^2(1-\sqrt{3}y)}{y-1} \geq 0$$

$$\frac{(\sqrt{3}y-1)}{(y-1)} < 0$$

$$\begin{array}{|c|c|} \hline & - \\ \hline - & + \\ \hline \end{array}$$

$\text{Sur} \rightarrow \text{Onto} \checkmark$   
 $\times \text{Inj} \rightarrow 1-2-1$

$$f(x) = \tan\left(\frac{x^2+1}{x^2+\sqrt{3}}\right)$$

$$f'(x) = \frac{1}{1 + \left(\frac{x^2+1}{x^2+\sqrt{3}}\right)^2} \times \frac{(x^2+\sqrt{3})2x - (x^2+1)2x}{(x^2+\sqrt{3})^2}$$

$$= \frac{1}{1 + \left(\frac{x^2+1}{x^2+\sqrt{3}}\right)^2} \times \frac{2x\sqrt{3} + 2\sqrt{3}(1 - 2\sqrt{3}) - 2x}{(x^2+\sqrt{3})^2}$$

$$f'(x) = \frac{1}{1 + \left(\frac{x^2+1}{x^2+\sqrt{3}}\right)^2} \times \left( \frac{2x(\sqrt{3}-1)}{(x^2+\sqrt{3})^2} \right)$$

$$f(x) = \tan y$$

$$f'(x) = \frac{1}{1+y^2}$$

$$y \in \left[\frac{1}{\sqrt{3}}, 1\right)$$

$$\frac{x^2+1}{x^2+\sqrt{3}} \in \left[\frac{1}{\sqrt{3}}, 1\right)$$

$$\tan\left(\frac{x^2+1}{x^2+\sqrt{3}}\right) \in \left[\tan\frac{1}{\sqrt{3}}, \tan 1\right]$$

$$\notin \left[\frac{\pi}{6}, \frac{\pi}{4}\right]$$

$$\in \left[\frac{\pi}{6}, \frac{\pi}{4}\right]$$

$f'(x) \nearrow +ve$   
 $f'(x) \searrow -ve$   
M12

$$\frac{Q_4 \ln((\log x)^2 - 2\log x + 2) + \ln((\log x)^2 - 2\log x + 2) + G_1((\log x)^2 - 1) \log x}{(\log^2 x - 2\log x + 2)}$$

$$\ln(1) + \ln(1) + G_1(-1)$$

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{4} = 1$$

$$P = \frac{7}{4}$$

$$-1 \leq (\log x)^2 - 2\log x + 2 \leq 1$$

$$-1 \leq (\log_{10} x - 1)^2 + 1 \leq 1$$

$$\log_{10} x - 1 = 0$$

$$\log_{10} x = 1$$

$$x = 10$$