

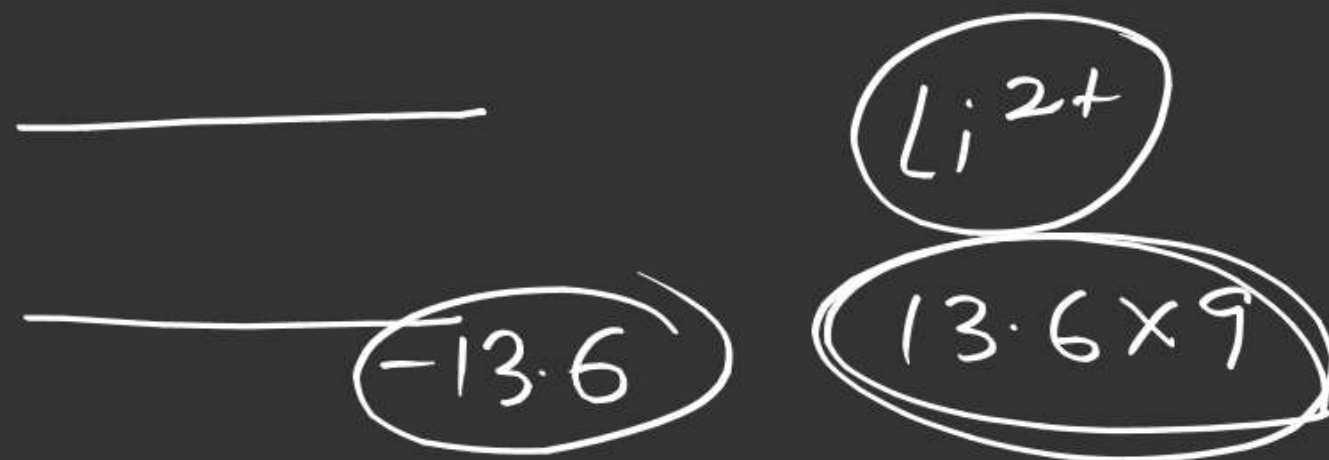
(42)  $e^-$   $p$   $\alpha$

$$\lambda = \frac{h}{\sqrt{2 m \cdot KE}}$$

$$m_{\text{proton}} = 1840 m_e$$

$$m_{\alpha} = 4 m_{\text{proton}}$$

(40)



$$KE = 13.6 \times 8 \text{ eV}$$

(45)  
 47  
 48

$$\lambda = \sqrt{\frac{150}{13.6 \times 8}}$$

$$(37) \quad (\phi = 40 \text{ eV})$$

22 volt

$$KE_{\max} = \underline{22 \text{ eV}}$$

$$KE_{\max} = 22 = h\nu - 40$$

$$\underline{62 = h\nu}$$

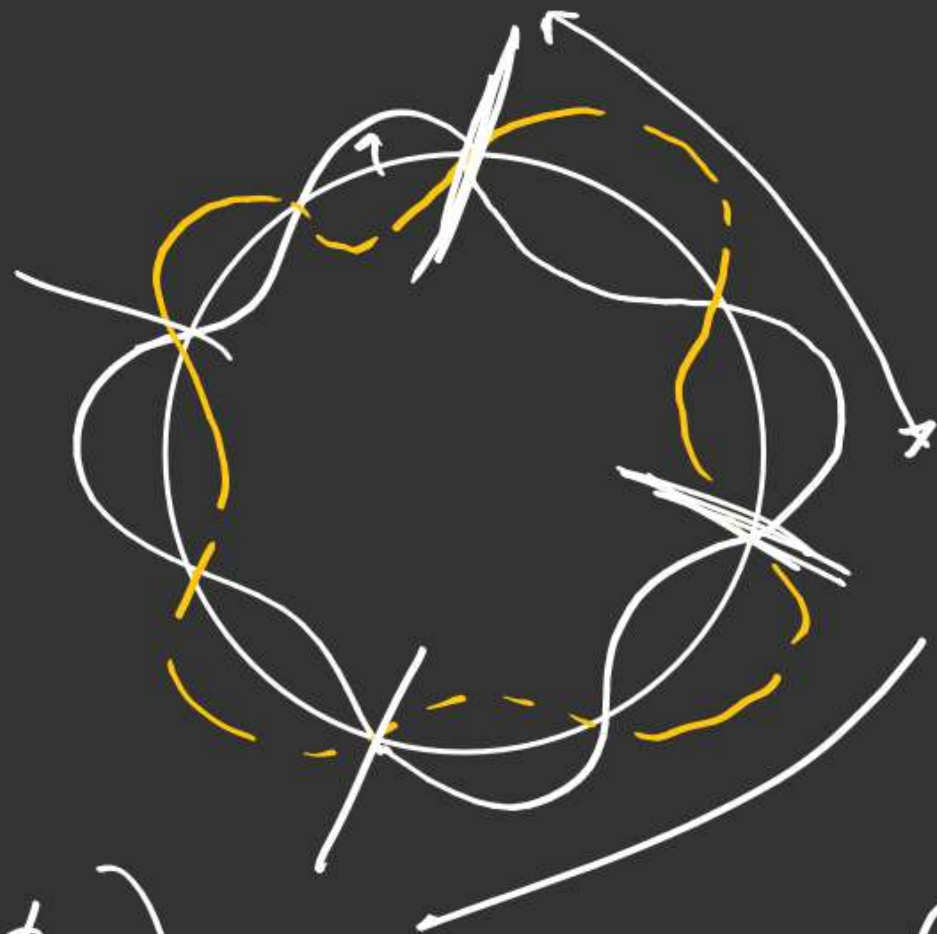
Standing wave



$$2\pi r = n\lambda$$

$$2\pi \left( 0.529 \frac{n^2}{Z} \text{Å} \right) = n\lambda$$

$$\lambda = 2\pi \left( 0.529 \frac{n^2}{Z} \right) \text{Å}$$



$$2\pi r = n\lambda$$

$$2\pi r = n \frac{h}{mv}$$

$$mvr = n \frac{h}{2\pi}$$



# Heisenberg uncertainty principle: →

→ It is impossible to determine the exact position and momentum of a microscopic particle (like  $e^-$ ) simultaneously.

$$\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$$

error or uncertainty in position

error in momentum

$$\hbar = \frac{h}{2\pi}$$

for minimum error

$$\Delta x \cdot \Delta p = \frac{h}{4\pi}$$

$$dx \cdot dp = \frac{h}{4\pi}$$

$$dx \cdot dv = \frac{h}{4\pi m}$$

↑  
error in speed

Q. Calculate minimum error in velocity, if error in position is  $\pm 1 \text{ \AA}$  for an  $e^-$ .

$$\Delta x \cdot \Delta v = \frac{h}{4\pi m}$$

$$(10^{-10}) \cdot \Delta v = \frac{6.62 \times 10^{-34}}{4 \times \pi \times 9.1 \times 10^{-31}}$$

$$\Delta v = \frac{6.62}{4\pi \times 9.1} \times 10^7$$

Q. Calculate  $\Delta v$  if  $\Delta x = 1 \text{ cm}$  for a particle having  $m = 100 \text{ gm}$ .

$$2 \times 10^4$$

$$10^{-2} \times \Delta v = \frac{6.62 \times 10^{-34}}{4\pi \times 0.1}$$

$$\Delta v = \frac{6.62}{4\pi} \times 10^{-31}$$

$$dx \cdot dp = \frac{h}{4\pi}$$

$$\begin{cases} p = mv \\ dp = m dv \end{cases}$$

$$dx \cdot dv = \frac{h}{4\pi m}$$

$$\left[ \frac{1}{2}mv^2 = E \right]$$

$$\underline{dx} \left( \frac{h}{\lambda^2} d\lambda \right) = \frac{h}{4\pi}$$

error in  
de broglie wavelength

$$\begin{aligned} p &= \frac{h}{\lambda} \\ dp &= -\frac{h}{\lambda^2} d\lambda \end{aligned}$$

$$\lambda = \frac{h}{mv} = \frac{h}{p}$$



# Schrodinger eq<sup>n</sup> :-

- He considered the dual nature of particles.
- The wave associated with an  $e^-$  is considered to be a standing wave.

$$\left[ \frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + \frac{\partial^2 \psi}{\partial z^2} + \frac{8\pi^2m(E-V)}{h^2} \psi = 0 \right]$$

$\psi = \Psi$  = amplitude of  
wave  
or wave function

$E$  = Total Energy  
 $V$  = Potential energy

$$\frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z} = \nabla = \text{nabla operator}$$

$$\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} = \nabla^2 = \text{Laplacian operator}$$

$$\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + \frac{\partial^2 \psi}{\partial z^2} = \nabla^2 \psi$$

$$\nabla^2 \psi + \frac{8\pi^2 m (E - V)}{h^2} \psi = 0$$

$$(E - V) \psi = -\frac{h^2}{8\pi^2 m} \nabla^2 \psi$$

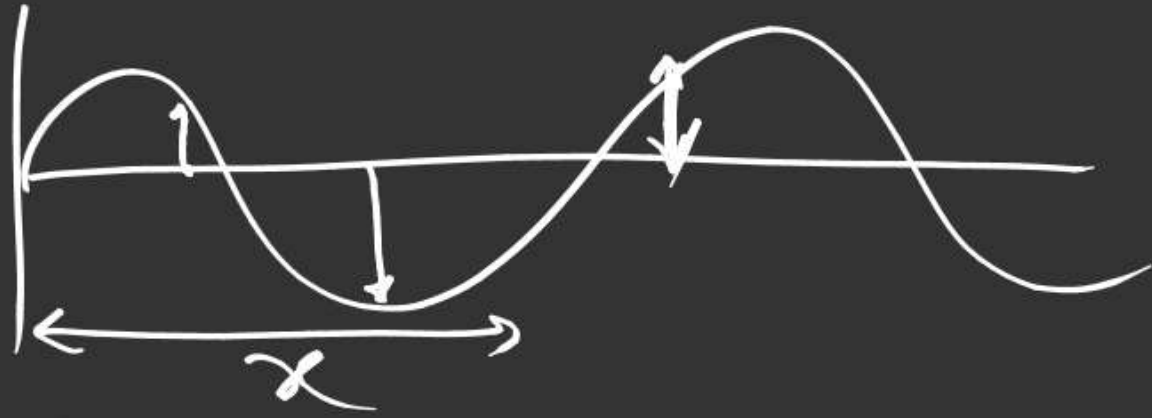
$$E \psi = -\frac{h^2}{8\pi^2 m} \nabla^2 \psi + V \psi$$

$$E \psi = \left( -\frac{h^2}{8\pi^2 m} \nabla^2 + V \right) \psi$$

$$E \psi = H \psi$$

↑  
Hamiltonian operator





$$\textcircled{y} = A \sin(\omega \underset{\uparrow}{t} - k \underset{\downarrow}{x})$$

displacement

$$\frac{\partial^2 y}{\partial t^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial x^2}$$

O-I 45 — 54

S-I 41 — 53