

$$\left. \begin{aligned}
 & Q \sqrt{\sec^2 \theta + \csc^2 \theta} = \tan \theta + \cot \theta \\
 & \sqrt{1 + \tan^2 \theta + 1 + \cot^2 \theta} \\
 & \sqrt{\tan^2 \theta + \cot^2 \theta + 2 \cdot \tan \theta \cdot \cot \theta} \\
 & \sqrt{(\tan \theta + \cot \theta)^2} \\
 & = \tan \theta + \cot \theta = \text{RHS}
 \end{aligned} \right\}$$

$$\left. \begin{aligned}
 & Q (\sec \theta - \sin \theta) (\sec \theta - \csc \theta) (\tan \theta + \cot \theta) = 1 \\
 & \left(\frac{1}{s} - s \right) \left(\frac{1}{c} - c \right) \left(\frac{s}{c} + \frac{c}{s} \right) \\
 & \frac{1-s^2}{s} \times \frac{1-c^2}{c} \times \frac{s^2+c^2}{sc} \\
 & \frac{c^2}{s} \times \frac{s^2}{c} \times \frac{1}{sc} = 1 \quad \text{RHS}
 \end{aligned} \right\}$$

Q If $\tan \theta + \sec \theta = \frac{3}{2}$ then $\sin \theta = ?$

$$\sec \theta + \csc \theta = \frac{3}{2}$$

$$\sec \theta - \csc \theta = \frac{2}{3}$$

$$\underline{2 \sec \theta = \frac{3}{2} + \frac{2}{3} = \frac{9+4}{6}}$$

$$\sec \theta = \frac{13}{12} \Rightarrow \csc \theta = \frac{12}{13}$$

$$\begin{aligned}\sin \theta &= \sqrt{1 - \csc^2 \theta} \\ &= \sqrt{1 - \frac{144}{169}} = \sqrt{\frac{25}{169}} \\ &= \frac{5}{13}\end{aligned}$$

Q If $2 \sin \theta = 2 - \csc \theta$ then $\sin \theta = ?$

$$\csc \theta = 2 - 2 \sin \theta$$

$$\csc^2 \theta = 4 + 4 \sin^2 \theta - 8 \sin \theta$$

$$1 - \sin^2 \theta = 4 + 4 \sin^2 \theta - 8 \sin \theta$$

$$5 \sin^2 \theta - 8 \sin \theta + 3 = 0$$

$$5 \sin^2 \theta - 5 \sin \theta - 3 \sin \theta + 3 = 0$$

$$5 \sin \theta (\sin \theta - 1) - 3 (\sin \theta - 1) = 0$$

$$(\sin \theta - 1)(5 \sin \theta - 3) = 0$$

$$\sin \theta = 1, \frac{3}{5}$$

$\sin \theta \text{ & Q.E.D}$
Solve

Q 5 $3 \sec^4 \theta + 8 = 10 \sec^2 \theta$ then
 $\boxed{\sec^2 \theta = T}$
 $\frac{3T^2 + 8}{T} = 10T$

$$3T^2 + 8 = 10T$$

$$3T^2 - 10T + 8 = 0$$

$$3T^2 - 6T - 4T + 8 = 0$$

$$3T(T-2) - 4(T-2) = 0$$

$$T = \frac{4}{3}, 2$$

$$\begin{cases} \sec^2 \theta = \frac{4}{3} \\ 1 + \tan^2 \theta = \frac{4}{3} \end{cases} \Rightarrow \begin{cases} \sec^2 \theta = 2 \\ 1 + \tan^2 \theta = 2 \end{cases} \Rightarrow \tan \theta = \pm 1$$

Q 6 $\frac{\sin x + 6x}{6^3 x} = \tan^3 x + \tan^2 x + \tan x + 1$

$$LHS = \frac{\sin x + 6x}{6^3 x}$$

$$= \left(\frac{1}{6^2 x} \right) \cdot \left(\frac{\sin x + 6x}{6x} \right)$$

$$= 1 \sec^2 x \times (\tan x + 1)$$

$$(1 + \tan^2 x)(\tan x + 1)$$

$$\tan^3 x + \tan^2 x + \tan x + 1 = RHS$$

Fundamentals of Mathematics

Q. $\underbrace{\sin \theta + \sin^3 \theta + \sin^5 \theta}_{=1}$

then $\underline{\sin^6 \theta - 4\sin^4 \theta + 8\sin^2 \theta} = ?$

Hint

$$\sin \theta + \sin^3 \theta = 1 - \sin^2 \theta$$

$$\sin \theta + \sin^3 \theta = \sin^2 \theta$$

$$\sin \theta (1 + \sin^2 \theta) = \sin^2 \theta$$

Sq:

$$\sin^2 \theta (1 + \sin^2 \theta)^2 = \sin^4 \theta$$

$$(1 - \sin^2 \theta) (1 + 1 - \sin^2 \theta)^2 = \sin^4 \theta$$

$$(1 - \sin^2 \theta) (2 - \sin^2 \theta)^2 = \sin^4 \theta$$

$$(1 - \sin^2 \theta) (4 + \sin^4 \theta - 4\sin^2 \theta) = \sin^4 \theta$$

$$4 + \sin^4 \theta - 4\sin^2 \theta - 4\sin^4 \theta - \sin^6 \theta + 4\sin^4 \theta - \sin^6 \theta$$

$$4\sin^4 \theta - \sin^6 \theta - 8\sin^2 \theta = -4$$

$$\underline{\sin^6 \theta + 8\sin^2 \theta - 4\sin^4 \theta} = 4$$

Q If $\frac{8m^4x}{2} + \frac{6m^2x}{3} = \frac{1}{5}$ then.

A) $\frac{8m^8x}{8} + \frac{6m^8x}{27} = \frac{1}{125}$ ✓

B) $tm^2x = \frac{1}{3}$

C) $tm^2x = \frac{2}{3}$.

D) $\frac{8m^8x}{8} + \frac{6m^8x}{27} = \frac{2}{125}$

E) $\frac{8m^8x}{8} + \frac{6m^8x}{27} = \left(\frac{2}{5}\right)^4 + \left(\frac{3}{5}\right)^4$

$$\frac{16^2}{625x^8} + \frac{81^3}{625x^27} = \frac{5}{625} = \frac{1}{125}$$

$$\frac{8m^4x}{2} + \frac{(1-8m^2x)^2}{3} = \frac{1}{5}$$

$$\frac{8m^4x}{2} + \frac{8m^4x - 2(8m^2x) + 1}{3} = \frac{1}{5}$$

$$3(8m^4x + 2(8m^4)(-4(8m^2)x + 2) = \frac{6}{5}$$

$$5(8m^4x - 4(8m^2)x + 2) = \frac{6}{5}$$

$$25(8m^4x - 20(8m^2)x + 4) = 0$$

$$(5(8m^2x - 2))^2 = 0$$

$$5(8m^2x - 2) = 0$$

$$8m^2x - \frac{2}{5} \Rightarrow 64x - 1 - 6m^2x = 1 - \frac{2}{5} = \frac{3}{5}$$

$$tm^2x = \frac{\sin^2x}{6^2x} = \frac{2}{\frac{3}{5}} = \frac{2}{3}$$

$$\textcircled{1} \quad 81^{\sin^2\theta} + 81^{\cos^2\theta} = 30$$

from dθ - 1

$$81^{\sin^2\theta} + 81^{1-\sin^2\theta} = 30$$

$$81^{\sin^2\theta} + \frac{81}{81^{\sin^2\theta}} = 30$$

$$t + \frac{81}{t} = 30$$

$$t^2 - 30t + 81 = 0$$

$$t^2 - 27t - 3t + 81 = 0$$

$$t(t-27) - 3(t-27) = 0$$

$$t=3, 27$$

\rightarrow $\textcircled{2} \quad 81^{\sin^2\theta} = 3 \quad \& \quad 81^{\cos^2\theta} = 27$

3 वाला

$$3^{4\sin^2\theta} = 3^1$$

$$4\sin^2\theta = 1$$

$$\sin^2\theta = \frac{1}{4}$$

$$\sin\theta = \frac{1}{2}, -\frac{1}{2}$$

$$\theta = 30^\circ, -30^\circ$$

$$\frac{\pi}{6}, -\frac{\pi}{6}$$

$$3^{4\cos^2\theta} = 3^3$$

$$4\cos^2\theta = 3$$

$$\cos^2\theta = \frac{3}{4}$$

$$\sin\theta = \frac{\sqrt{3}}{2}, -\frac{\sqrt{3}}{2}$$

$$\theta = 60^\circ, -60^\circ$$

$$\theta = \frac{\pi}{3}, -\frac{\pi}{3}$$

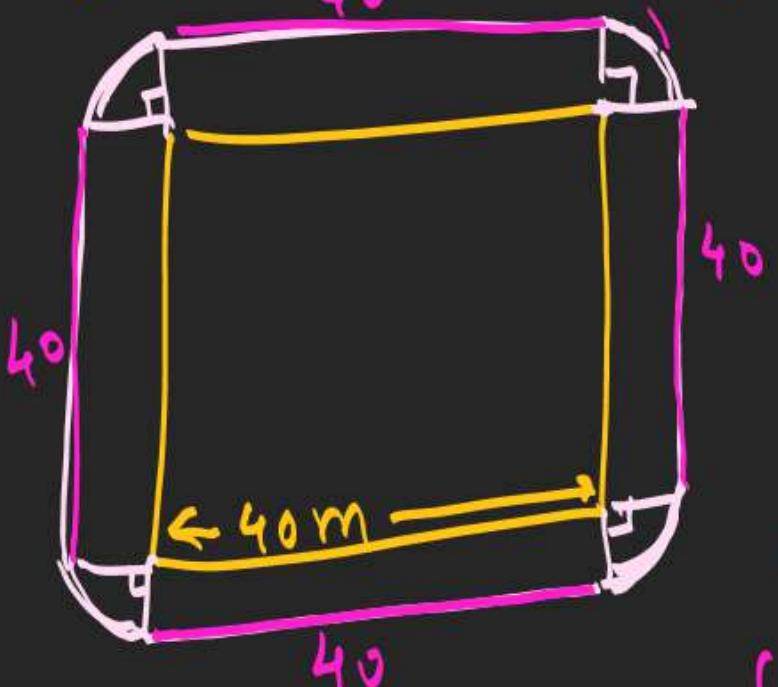
Q Let $f_R(\theta) = \sin^k \theta + \cos^k \theta$

then find value of $\frac{1}{6}f_6(\theta) - \frac{1}{4}f_4(\theta)$

Q $\int m \theta + \ln \theta = m$, $\int m \theta - \ln \theta = n$

then P.T. $m^2 - n^2 = 4\sqrt{mn}$

Q A garden is in shape of a sq^r of side length 40m. Now if a man runs around the garden in such a way that his distance from side of sq^r in L meter. How much distance will he travel after L



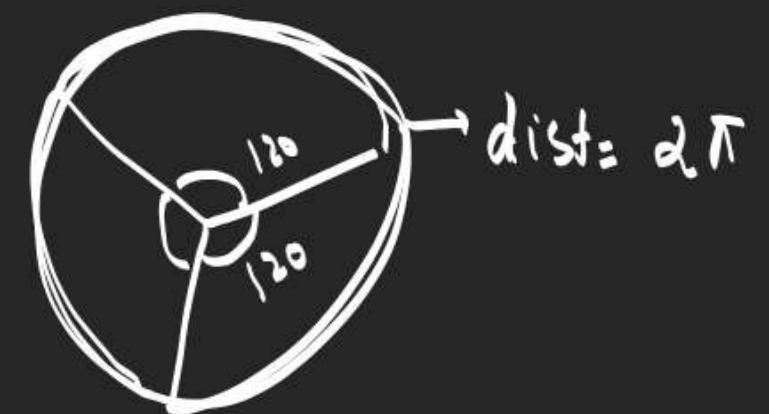
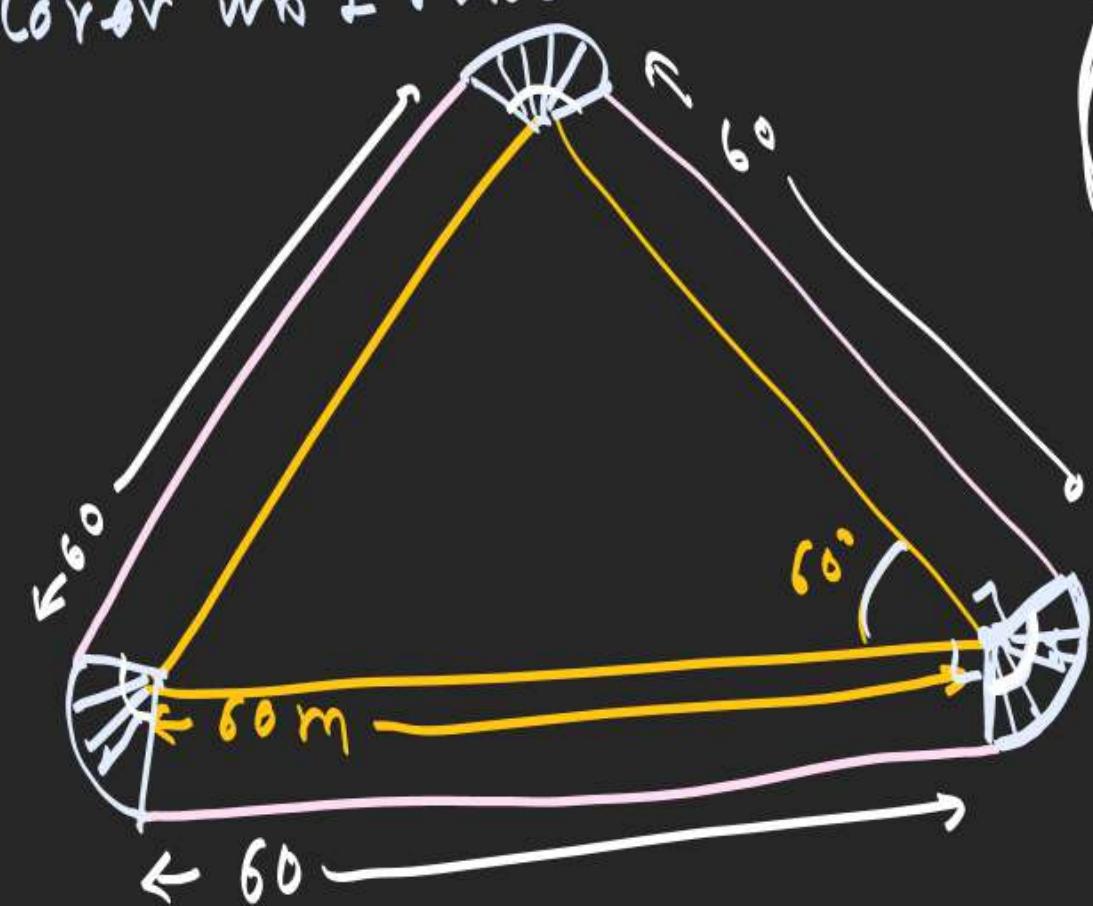
$$\text{dist} = 2\pi$$

$$\begin{aligned} & 40 + 40 + 40 + 40 + 2\pi \\ & 160 + 2\pi \end{aligned}$$

Q An equilateral triangle of sides 60m is in the shape of a garden. Now if a man runs in such a way that his distance from the sides of \triangle is always 10m. How much distance he will cover in 2 rounds.

$$\text{Total} = 180 + 2\pi$$

Cover in 2 rounds



$$\begin{aligned} x + 90 + 90 + 60 &= 360 \\ x &\approx 120^\circ \end{aligned}$$

Q If $\theta \in (0, \frac{\pi}{4})$ then .

$$t_1 = (tm\theta)^{tan\theta}$$

$$t_2 = (tm\theta)^{cot\theta}$$

$$t_3 = (gt\theta)^{tan\theta}$$

$$t_4 = (gt\theta)^{cot\theta}$$

$$t_1 > t_2 > t_3 > t_4$$

$$\boxed{t_4 > t_3 > t_2 > t_1}$$

$$t_3 > t_1 > t_2 > t_4$$

$$t_2 > t_3 > t_1 > t_4$$

$$\theta = (0, 45^\circ)$$

$$\theta = 30^\circ \text{ Assume}$$

$$t_1 = (tm 30^\circ)^{tan 30^\circ} = \left(\frac{1}{\sqrt{3}}\right)^{\frac{1}{\sqrt{3}}}$$

$$t_2 = (tm 30^\circ)^{cot 30^\circ} = \left(\frac{1}{\sqrt{3}}\right)^{\sqrt{3}} = \left(\frac{1}{\sqrt{3}}\right)^{1.7} = (1.21\sqrt{3})^{1.7} = \text{Archimedes}$$

$$t_3 = (gt 30^\circ)^{tan 30^\circ} = (\sqrt{3})^{1/\sqrt{3}}$$

$$x_4 = (gt 30^\circ)^{cot 30^\circ} = (\sqrt{3})^{\sqrt{3}} = \text{Saber Beta}$$

Conversion from Radian to degree.

$$\frac{5\pi}{12} \rightarrow \frac{5\pi}{12} \times \frac{180^\circ}{\pi} = 75^\circ$$

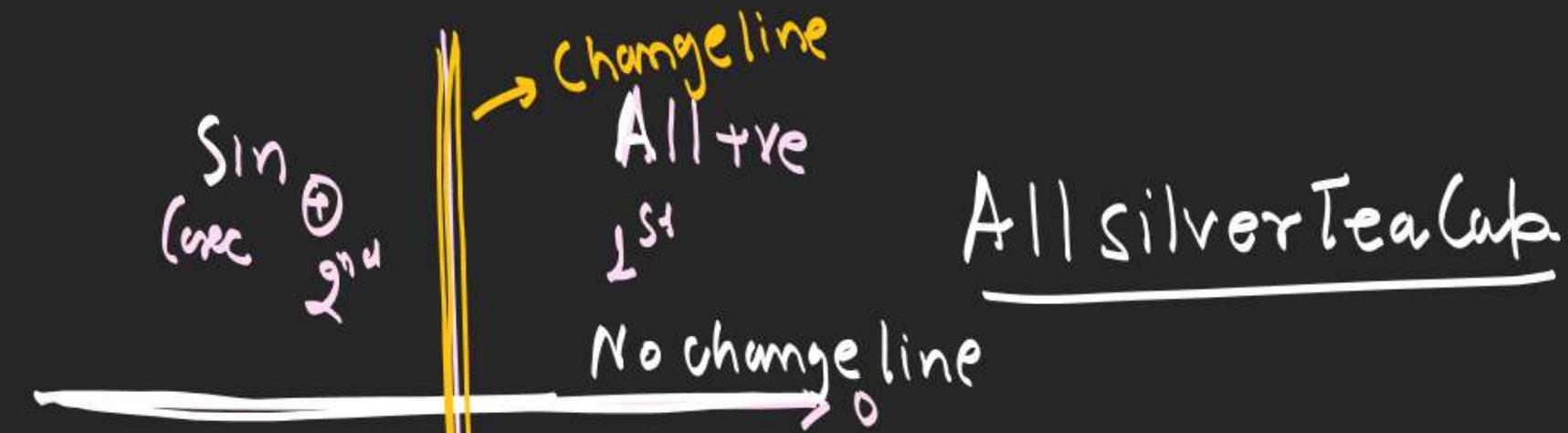
$$\frac{\pi}{10} \rightarrow \frac{\pi}{10} \times \frac{180^\circ}{\pi} = 18^\circ$$

$$\frac{2\pi}{3} \rightarrow \frac{2\pi}{3} \times \frac{180^\circ}{\pi} = 120^\circ$$

$$\frac{4\pi}{5} \rightarrow \frac{4\pi}{5} \times \frac{180^\circ}{\pi} = 144^\circ$$

$$\frac{\pi}{5} \rightarrow \frac{\pi}{5} \times \frac{180^\circ}{\pi} = 36^\circ$$

Quadrant system.

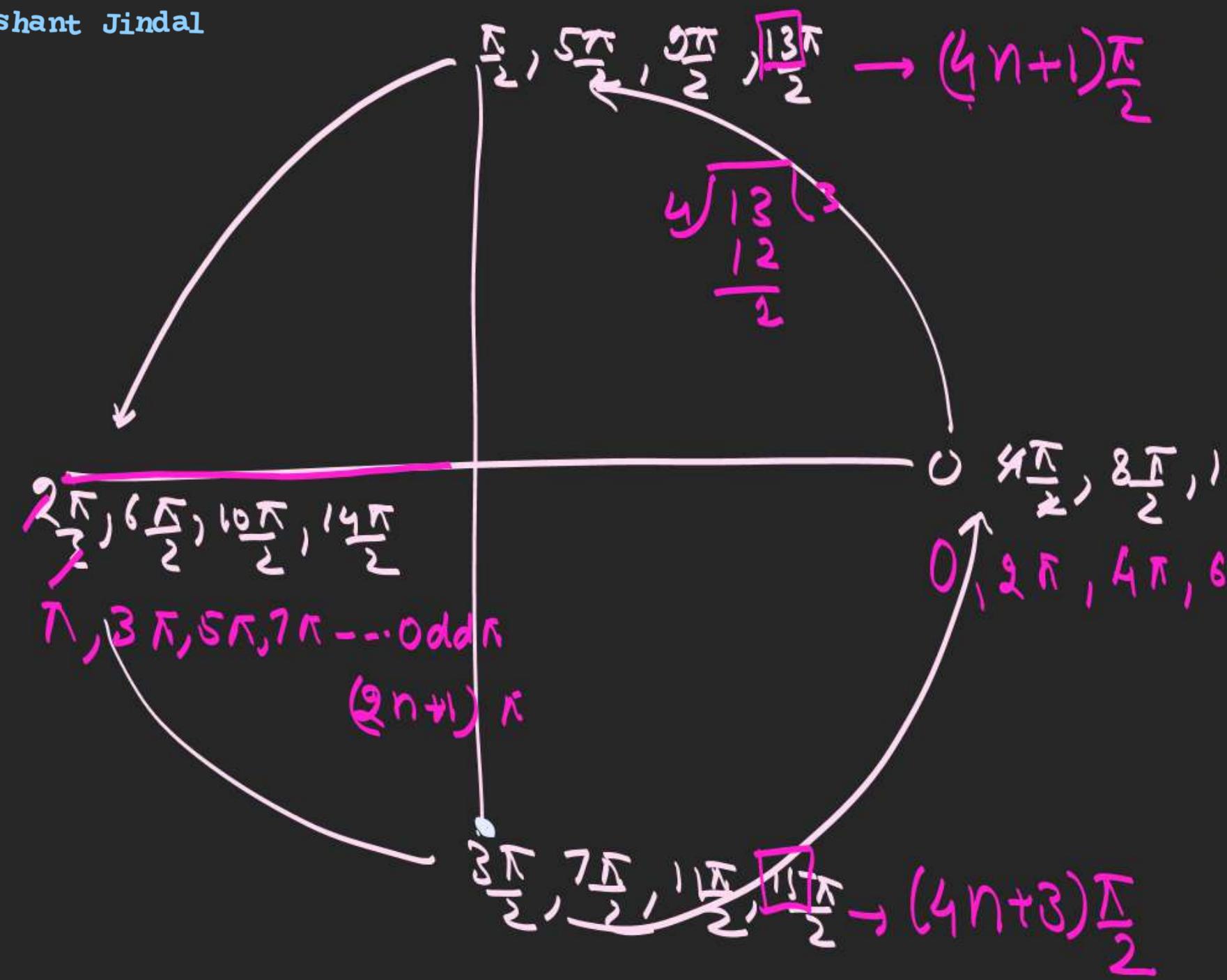


Tan 3rd
6th

4th Sec +

Change

$\sin \Rightarrow 6^{\text{th}}$
 $\tan \Rightarrow 6^{\text{th}}$
 $\sec \Rightarrow 6^{\text{th}}$



$$\sec\left(\frac{31\pi}{2} - \theta\right) = -\csc\theta$$

$$\sec\left(\frac{17\pi}{2} + \theta\right)$$

$$\sec(82\pi - \theta)$$

$$\tan\left(\frac{7\pi}{2} - \theta\right)$$

$$\cot\left(\frac{3\pi}{2} + \theta\right)$$