

Doppler Effect

⇒ When source and observer moving parallel to each other

$$\underline{f_{app} = f_{real}}$$
 ✓



Along the line going  
 $v_s$  &  $v_o$  is zero.

Doppler Effect

(★)

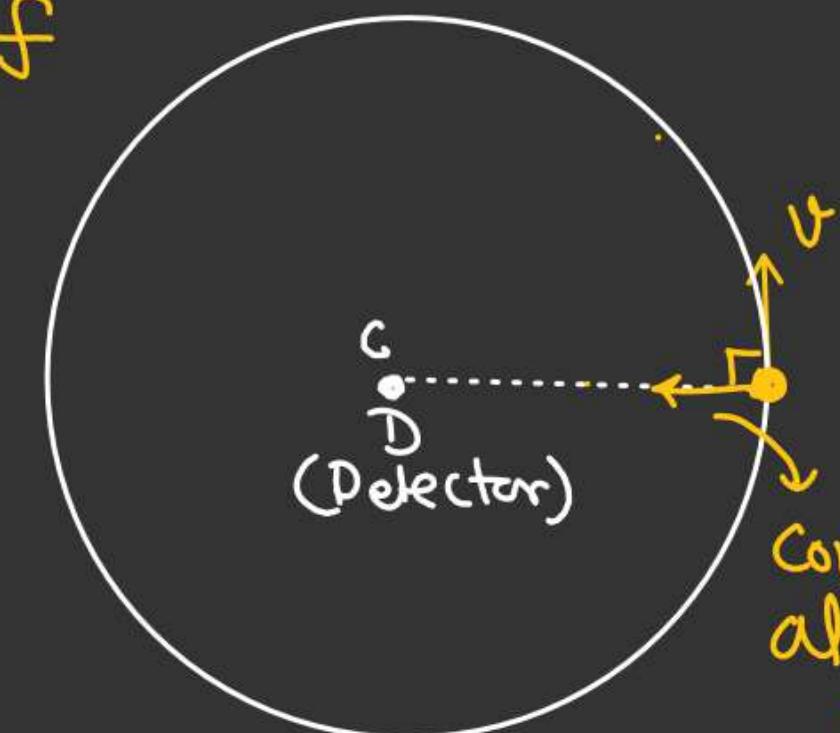
When Source moving in a CircleCase-1.Detector at the Center of the  
Circle on which Source is moving

$$f_{app} = \left( \frac{V \pm V_o}{V \mp V_s} \right) f$$

$$V_o = 0$$

$$(V_s) = 0$$

$$\underline{f_{app} = f}$$



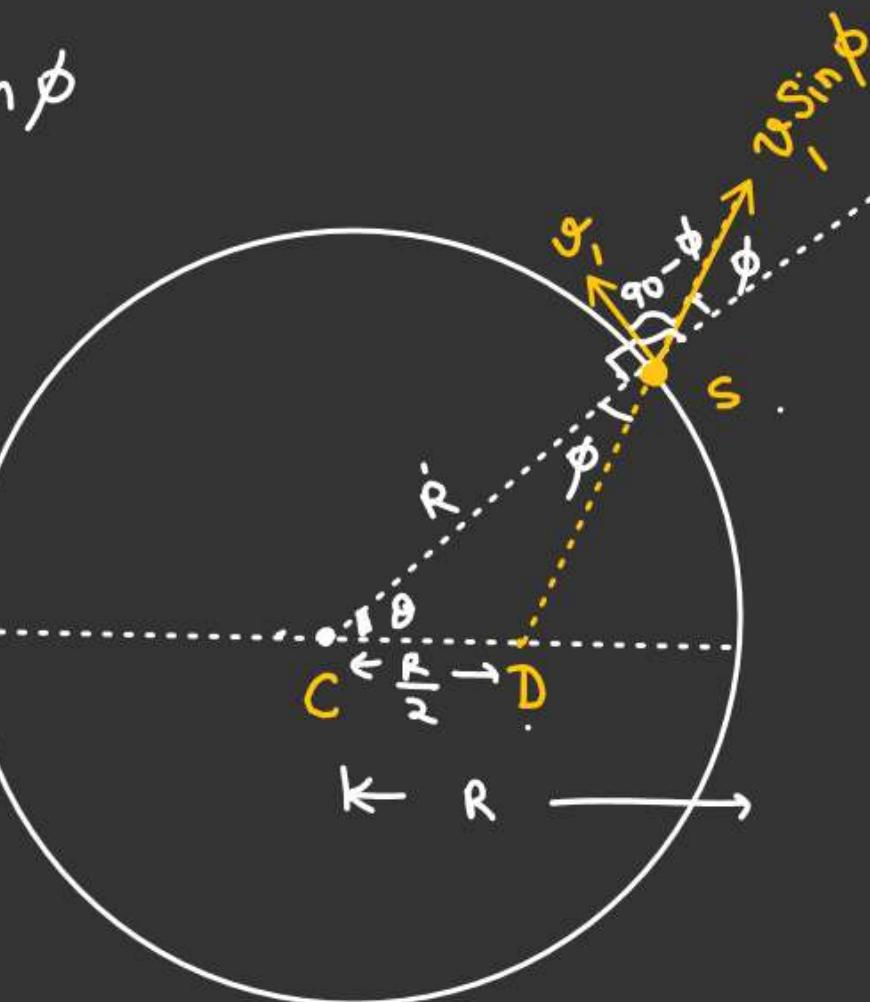
Component of  $V_s$   
along the line going  
is zero.

## Doppler Effect

## D → Detector

$$V_0 = 0, \quad V_S = V_1 \sin \phi$$

$$f_{app} = \left[ \frac{V}{V + v_1 \sin \phi} \right] f.$$



Doppler Effect

$$(f_{app})_{max} = ??$$

$$f_{app} = \left( \frac{v \pm v_o}{v \mp v_s} \right) f$$

$v_o = 0$

$$(f_{app})_{min} = ??$$

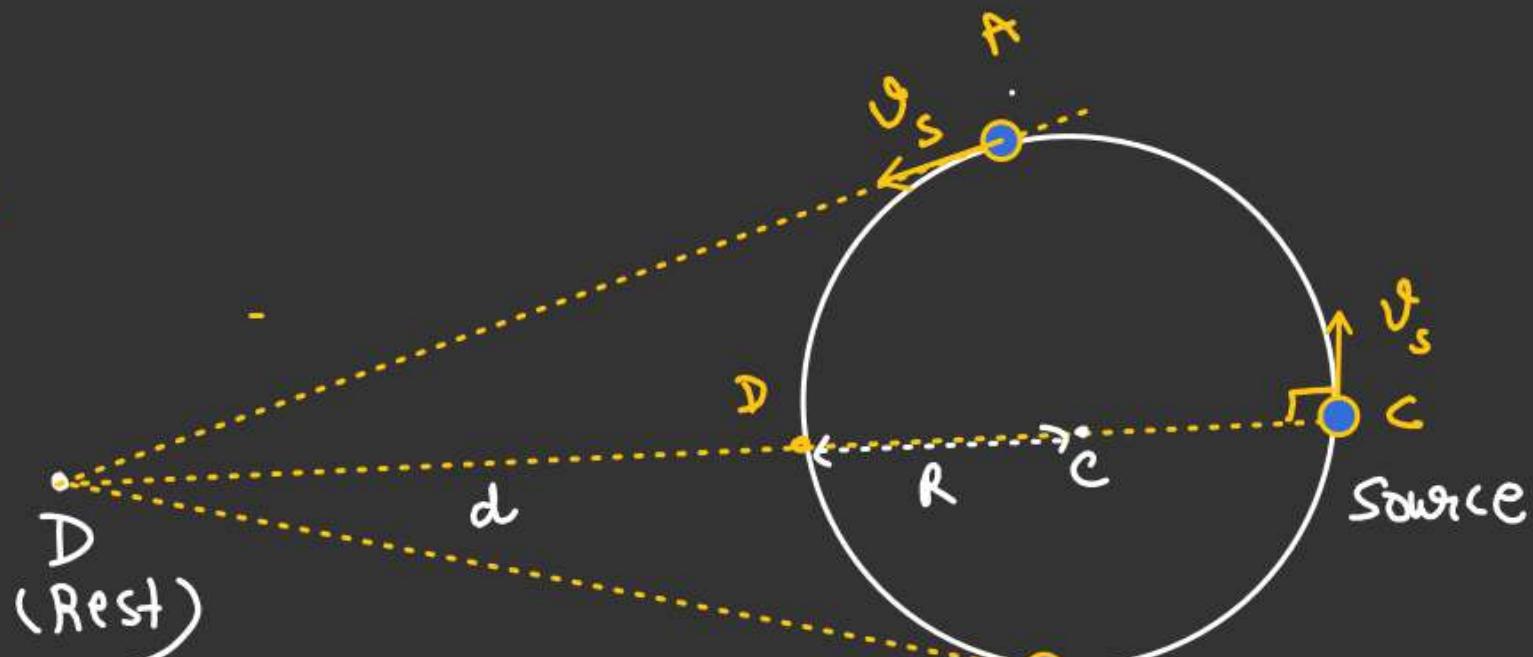
$$f_{app} = \left( \frac{v}{v \mp v_s} \right) f$$

for  $(f_{app})_{max}$  denominator

Should be min ie  $(v - v_s)$

so, At point A  $(f_{app})_{max}$

For  $(f_{app})_{min}$ , denominator should be maximum  
ie  $(v + v_s)$ . So, at point B  $(f_{app})_{min}$ .



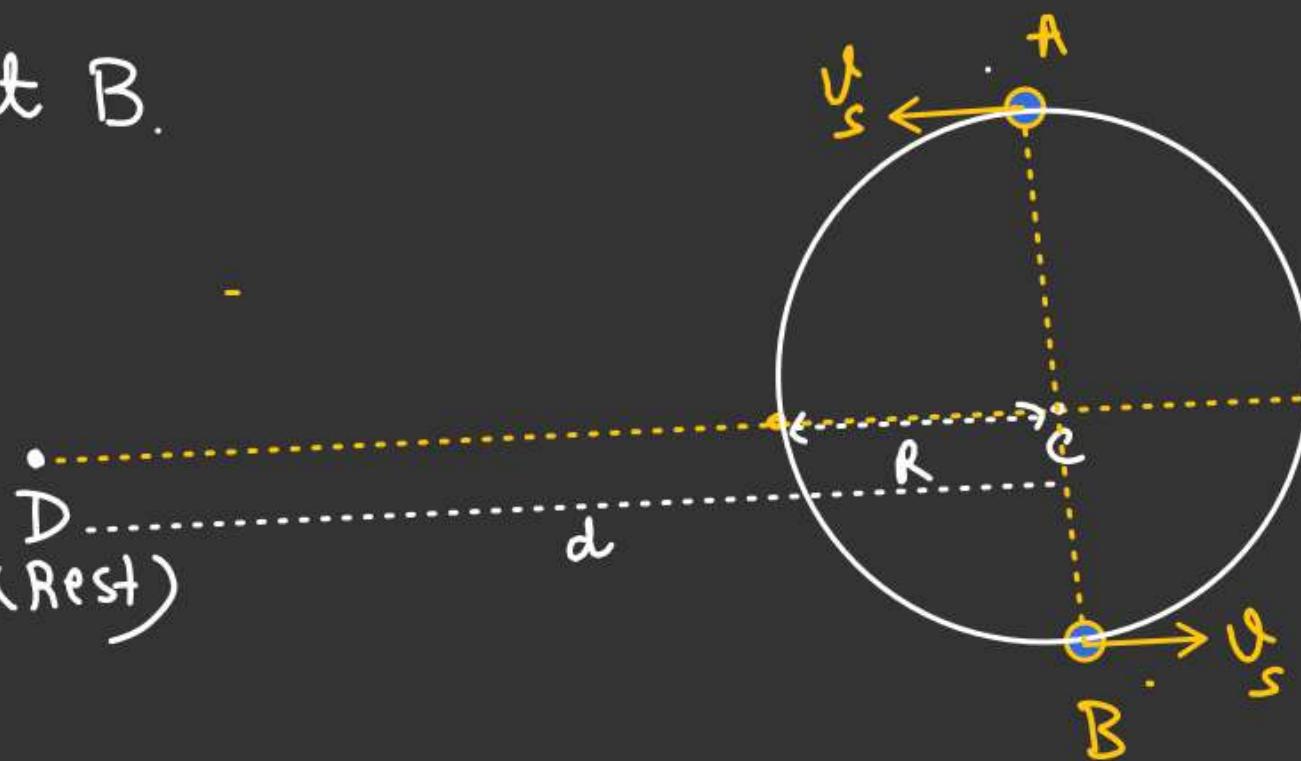
When Source's at C & D

$$f_{app} = (f_{real})$$

Doppler Effect

$(R \ll d)$ ,  $(f_{app})_{\max}$  at A

$(f_{app})_{\min}$  at B.

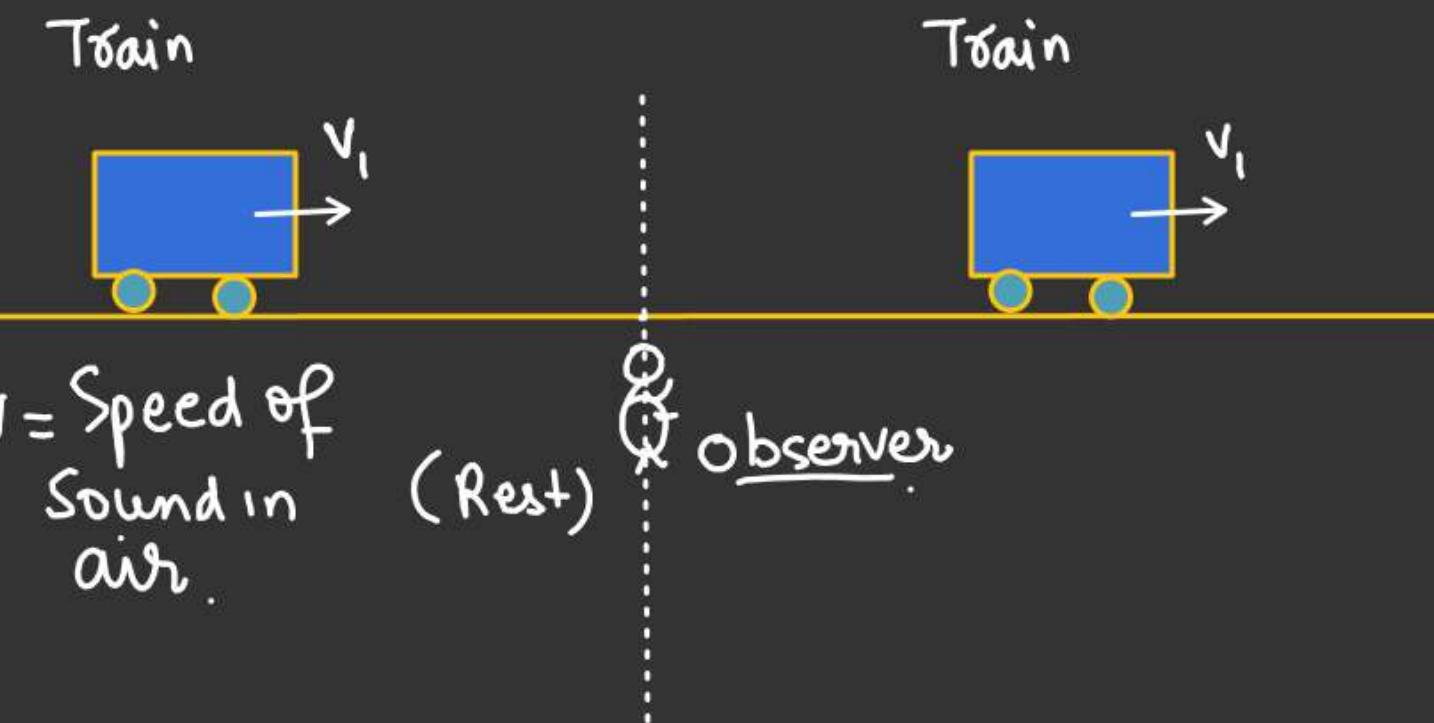


Doppler Effect

No of beats heard by  
Observer. ??

When train approaching  
the observer.

$$(f_{app})_1 = \left( \frac{v}{v - v_i} \right) f$$



When train moving away from observer

$$(f_{app})_2 = \left( \frac{v}{v + v_i} \right) f$$

$$\begin{aligned} \text{Beats} &= |(f_{app})_1 - (f_{app})_2| \\ &= vf \left[ \frac{1}{v-v_i} - \frac{1}{v+v_i} \right] \\ &= vf \left[ \frac{2v_i}{v^2 - v_i^2} \right] = \left( \frac{2vv_i}{v^2 - v_i^2} \right) f. \end{aligned}$$

Doppler EffectCase of perfect reflector

App frequency detect by detector.

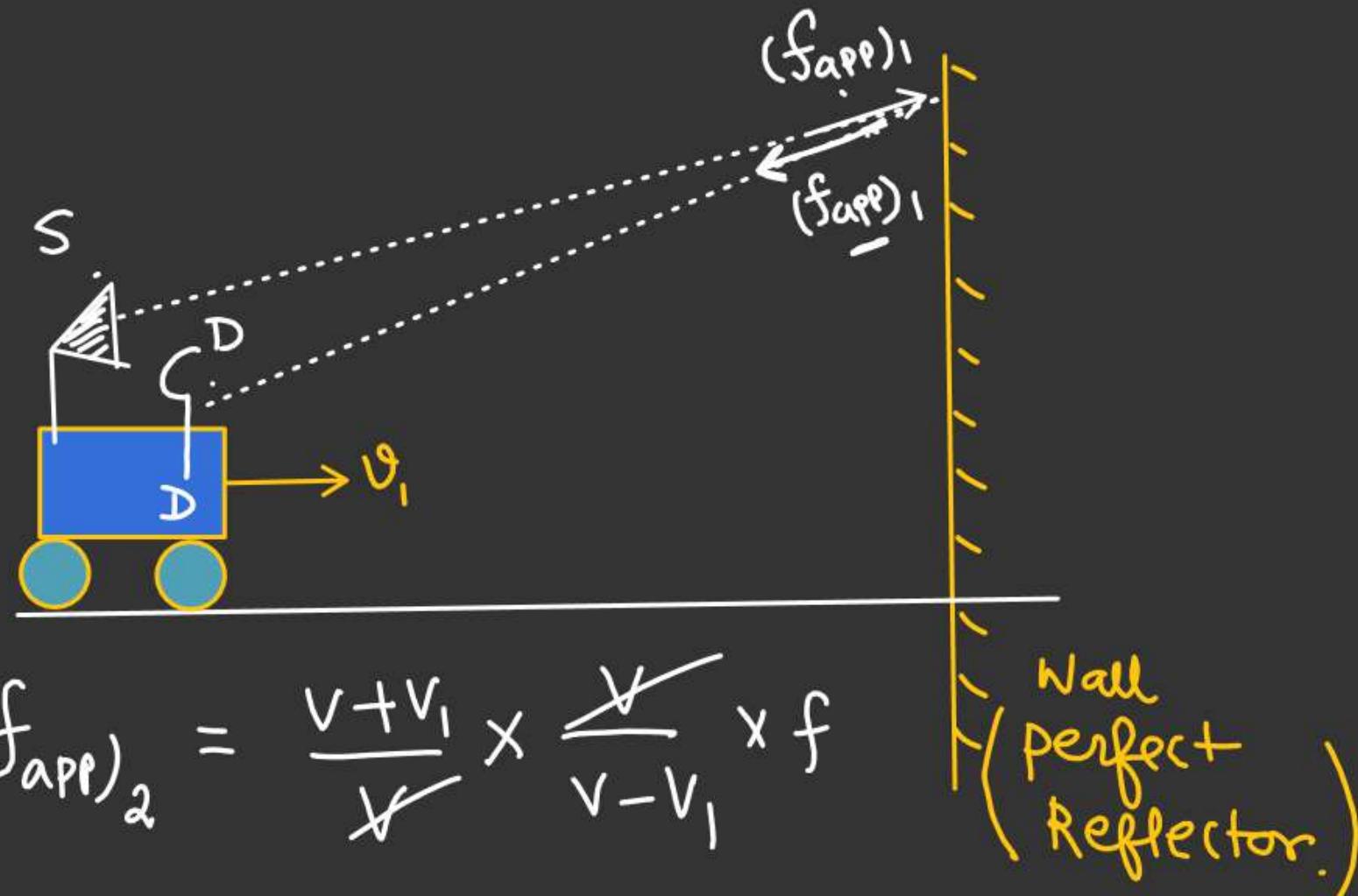
Wall as a observer ( $v_o = 0$ )  
Let,  $(f_{app})_1$  be the frequency received by wall.

$$(f_{app})_1 = \left( \frac{v}{v - v_i} \right) f \quad \text{--- ①}$$

Wall as a source ( $v_s = 0$ )

Let detector detects  $(f_{app})_2$

$$(f_{app})_2 = \left( \frac{v + v_i}{v} \right) \times (f_{app})_1 \quad \text{--- ②}$$



$$(f_{app})_2 = \left( \frac{v + v_i}{v - v_i} \right) f$$

Doppler Effect

$$(f_{app})_2 = \left( \frac{v+v_1}{v-v_1} \right) f$$

No of beats as detect by detector

$$= |(f_{app})_2 - f|$$

$$= \left| \frac{v+v_1}{v-v_1} - 1 \right| f$$

$$\therefore \left( \frac{2v_1}{v-v_1} \right) f$$

## Doppler Effect

When plane just above the observer

$$(f_{app}) = ??$$

When sound emitted by aeroplane at A reaches to C with velocity  $v$  then aeroplane is at position B.

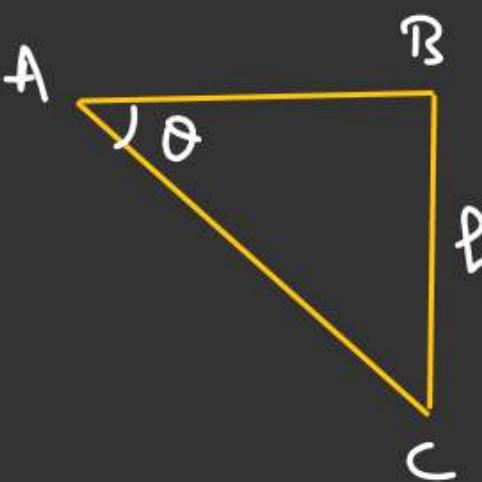
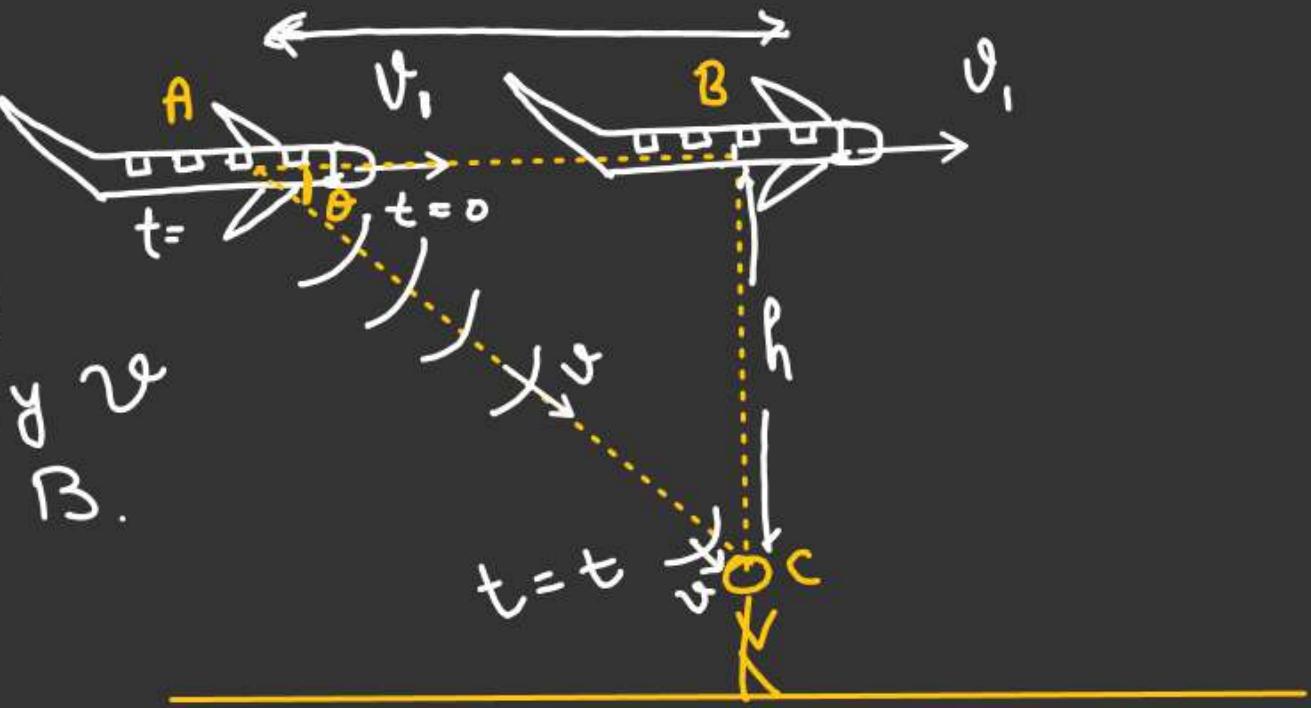
$$\frac{AB}{v_1} = \frac{AC}{v}$$

time taken by aeroplane to reach from A to B

time taken by sound wave to reach from A to C.

$$\frac{AC \cot \theta}{v_1} = \frac{AC \sec \theta}{v}$$

$$\cot \theta = \left( \frac{v_1}{v} \right)$$



$$\tan \theta = \frac{BC}{AB}$$

$$AB = \frac{h \cot \theta}{\sin \theta}$$

$$\sin \theta = \frac{h}{AC}$$

$$AC = \frac{h \csc \theta}{\cot \theta}$$

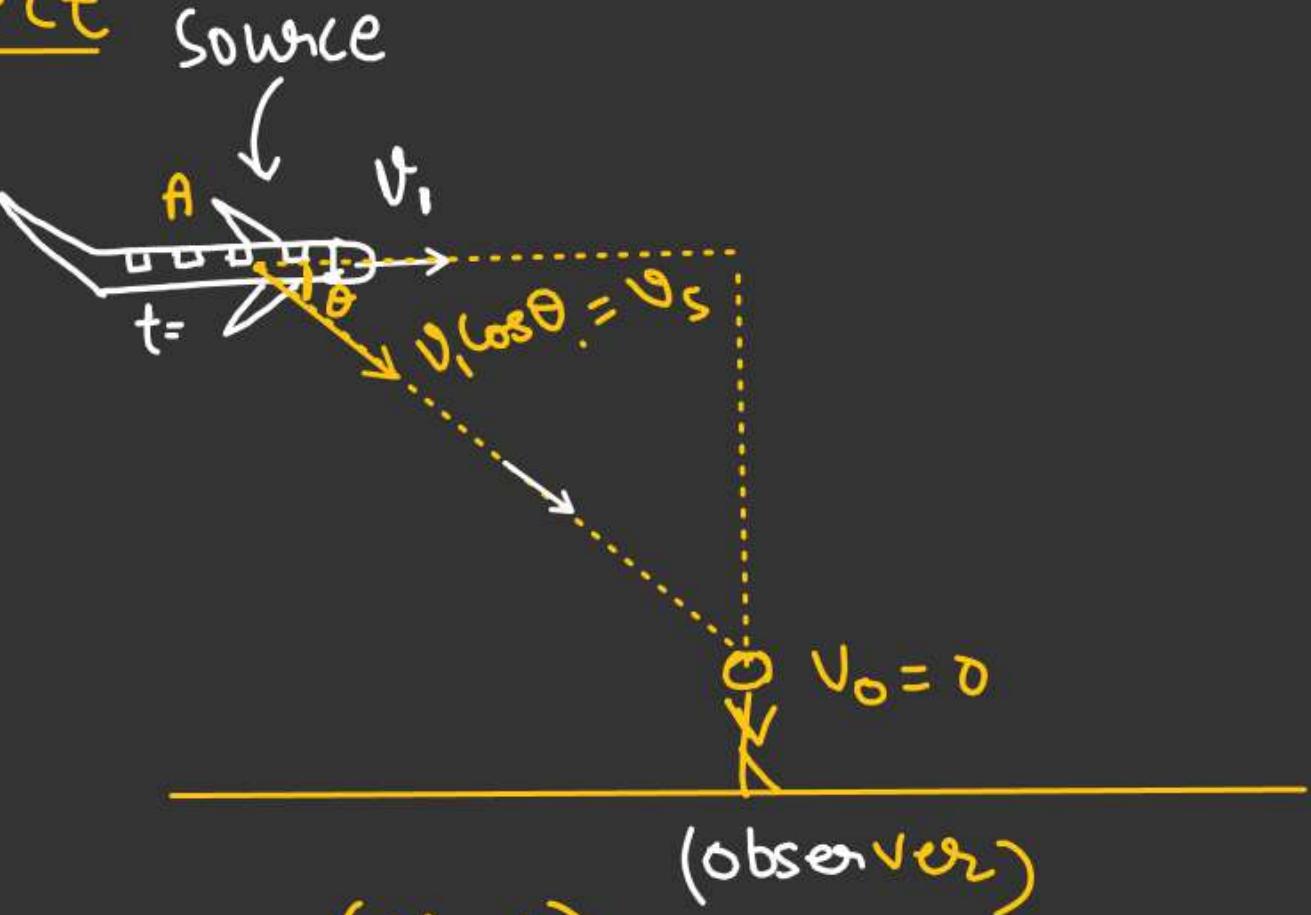
$$\cos\theta = \left(\frac{v_1}{v}\right)$$

$$f_{app} = \left( \frac{v}{v - v_1 \cos\theta} \right) \times f$$

$$f_{app} = \left( \frac{v}{v - v_1 \times \frac{v_1}{v}} \right) \times f$$

$$f_{app} = \left( \frac{v^2}{v^2 - v_1^2} \right) \times f$$

## Doppler Effect



**Doppler (H-W)**  
 → H-C Verma  
 Sound wave