

$$\frac{1}{a}, \frac{1}{H_1}, \dots, \frac{1}{H_n}, \frac{1}{c} \Rightarrow \frac{1}{H_1} = \frac{1}{a} + \frac{\frac{1}{c} - \frac{1}{a}}{n+1} = \frac{(n+1)c + (a-c)}{ac(n+1)}$$

$$= \frac{nc+a}{ac(n+1)}$$

$$\frac{ac(n+1)}{nc+a} - \frac{ac(n+1)}{na+c} = \frac{ac(n+1)(n-1)(a-c)}{(1+n^2)ac + n(a^2+c^2)} = ac(a-c)$$

$$\left(\frac{n}{n+1}\right) \left(\frac{n}{n+2}\right) \left(\frac{n-1}{n+3}\right) \left(\frac{n-2}{n+4}\right) \dots = \frac{a}{a_{n-1}}$$

$$n^2 - 1 = (n^2 + 1)ac + n(a^2 + c^2)$$

$$\sqrt{\frac{a}{a_{n-1}}} = \frac{n}{n+1}$$

$$\frac{a_{n-1}}{a_{n-2}} = \frac{n-1}{n}$$

$$\sqrt{\frac{a}{a_1}} = \frac{1}{2}$$

$$9(25a^2) + 9b^2 + 25c^2 + 156c' \quad n$$

$$= 25 \times 3a^2 + 156(3a) = \frac{1}{2} (300 + (n-1)(-2))$$

$$k = 3b = 15a = 5c \quad n = ?$$

$$(a, b, c) = \left(\frac{k}{15}, \frac{k}{3}, \frac{k}{5} \right)$$

n

4x9

$$G_1, G_2, G_3 \cdot G.M.S$$

6/5 2, 7

$$(1^2 + \dots + n^2) + (2^2 + 4^2 + \dots + n^2)$$

$$\frac{n(n+1)(2n+1)}{6} + 4 \frac{\frac{n}{2}(\frac{n}{2}+1)(n+1)}{6}$$

$$\frac{n(n+1)^2}{2}$$

$$1^2 + 2 \cdot 2^2 + 3^2 + 2 \cdot 4^2 + \dots + 2 \cdot (n-1)^2 + n^2$$

$$\frac{(n-1)n^2}{2} + n^2$$

$$1. \quad 2 \sin\left(3x + \frac{\pi}{4}\right) = \sqrt{1 + 8 \sin 2x \cos^2 2x} \quad \xrightarrow{\pi}$$

$$T = 2\pi$$

$$4 \sin^2\left(3x + \frac{\pi}{4}\right) = 1 + 4 \sin 4x \cos 2x$$

$$2 \left(1 - \cos\left(6x + \frac{\pi}{2}\right)\right) = 1 + 2(\sin 6x + \sin 2x) = 2 + 2 \sin 6x$$

$$x = 2n\pi + \frac{\pi}{12}, 2n\pi + \frac{17\pi}{12} \\ n \in \mathbb{I}$$

$$\sin 2x = \frac{1}{2}$$

$$2x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}, \frac{17\pi}{6}$$

$$x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}$$

$$x \in [0, 2\pi)$$

$$\frac{2}{16} \quad \frac{4}{16}$$

$$\sin\left(x + \frac{\pi}{4}\right)$$

2.

$$\underbrace{\left(2 \cdot \underbrace{\frac{1}{\sin^2 x}}_{\geq 1}\right)}_{\geq 2} \underbrace{\sqrt{y^2 - 2y + 2}}_{\geq 1} \leq 2.$$

, find x, y .

$$\operatorname{cosec}^2 x = 1 \quad \sin^2 x = 1$$

$$y = 1$$

$$x = n\pi \pm \frac{\pi}{2}, n \in \mathbb{I}$$

$$\sin \theta \geq 1$$

$$\sin \theta = 1$$

3. Solve for x, y satisfying

$$\cos x \cos y = \frac{3}{4}$$

$$\text{and } \sin x \sin y = \frac{1}{4}$$

$$\cos(x-y) = 1$$

 \Rightarrow

$$x-y = 2n\pi$$

①

$$\cos(x+y) = \frac{1}{2}$$

 \Rightarrow

$$x+y = 2m\pi \pm \frac{\pi}{3}$$

②

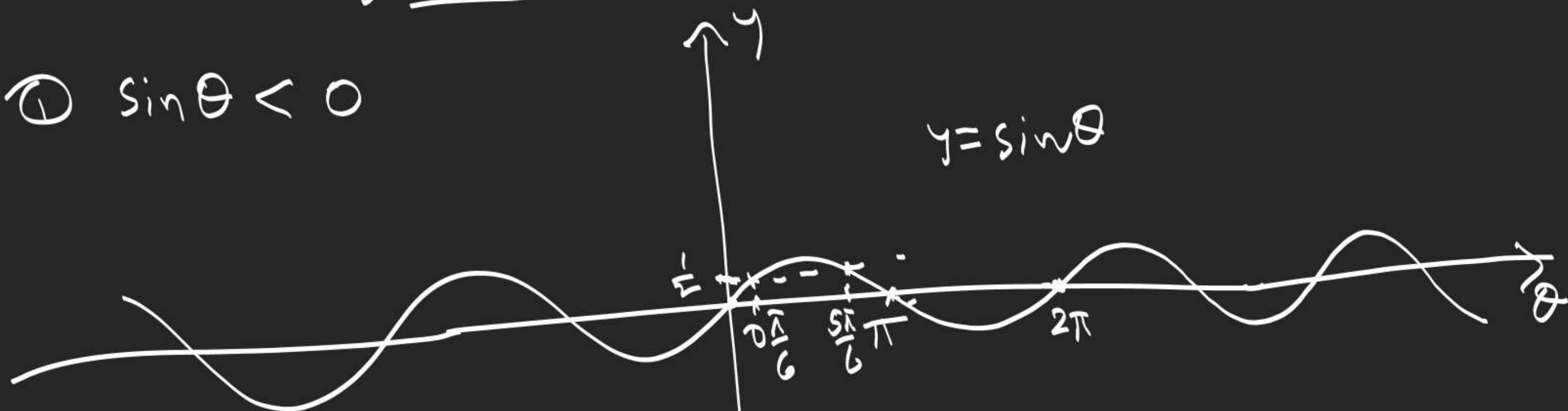
$$m, n \in \mathbb{I}$$

$$x = (n+m)\pi \pm \frac{\pi}{6}$$

$$y = (m-n)\pi \pm \frac{\pi}{6}$$

Inequality.

① $\sin \theta < 0$



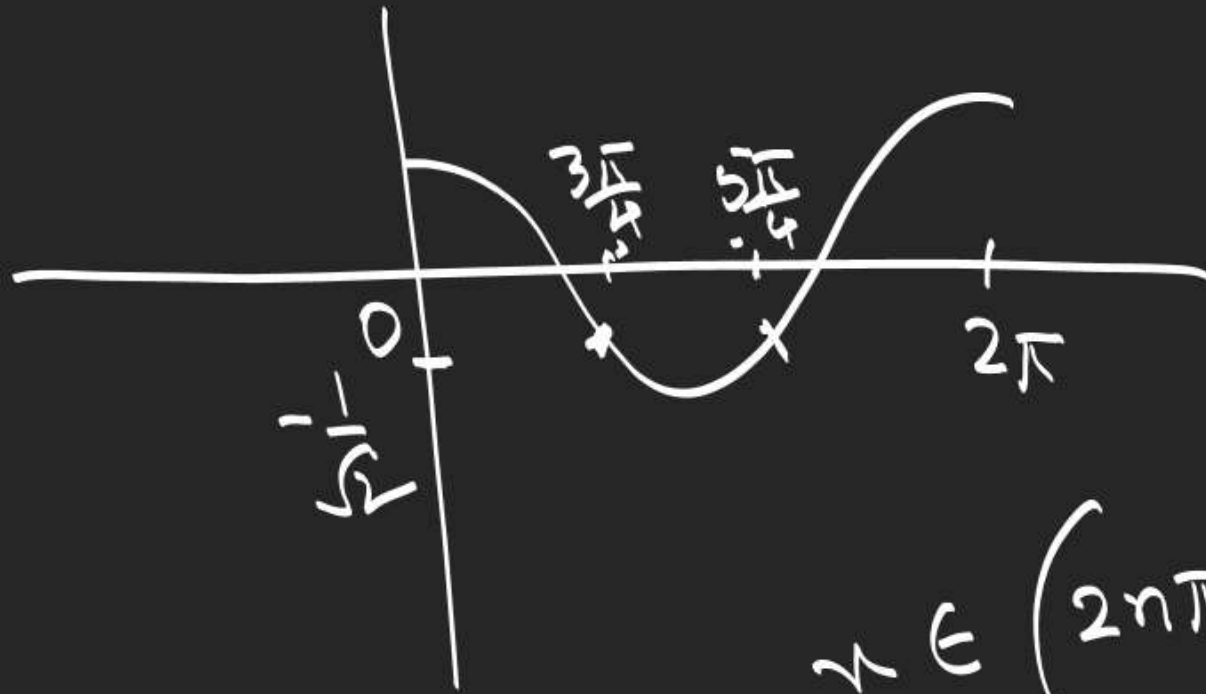
② $\sin \theta > \frac{1}{2}$

$$\theta \in (2n\pi + \pi, 2n\pi + 2\pi), n \in \mathbb{I}$$

$$\theta \in \left(2n\pi + \frac{\pi}{6}, 2n\pi + \frac{5\pi}{6}\right), n \in \mathbb{I}$$

3.

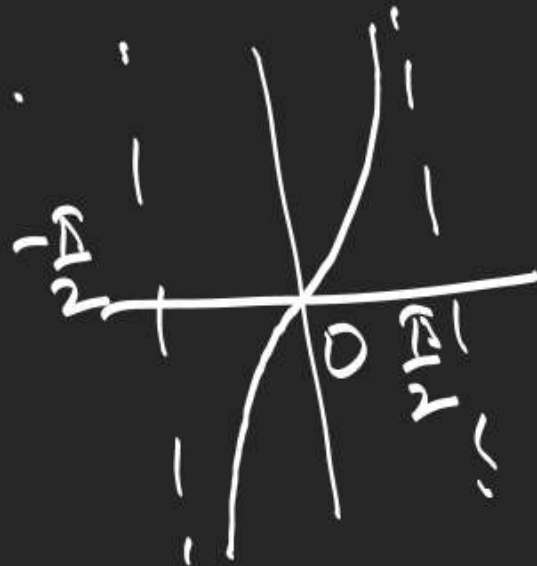
$$\cos x < -\frac{1}{\sqrt{2}}$$



$$x \in \left(2n\pi + \frac{3\pi}{4}, 2n\pi + \frac{5\pi}{4}\right), n \in \mathbb{I}.$$

4.

$$\tan x > 0$$



$$x \in \left(n\pi, n\pi + \frac{\pi}{2}\right), n \in \mathbb{I}$$

5.

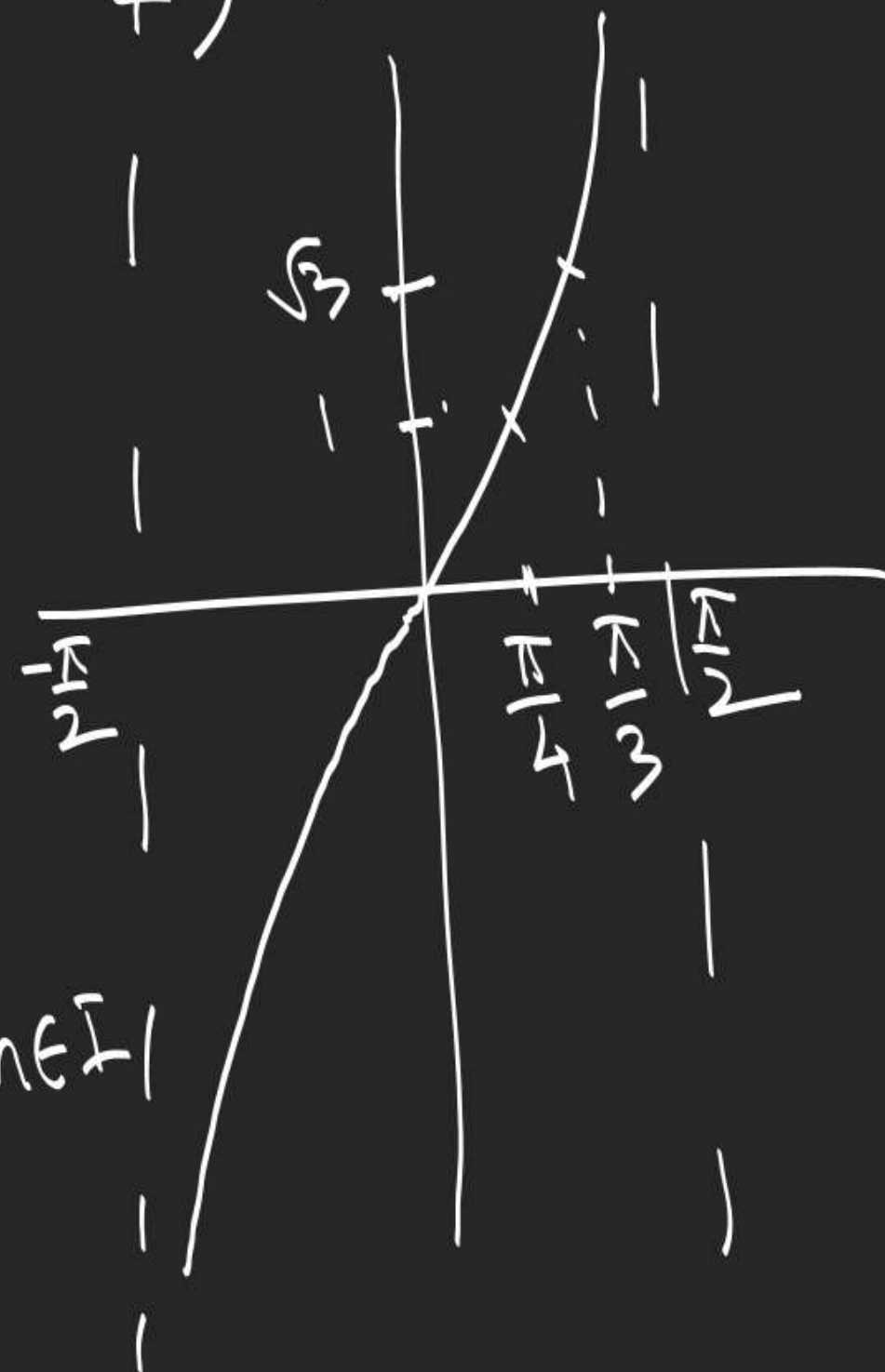
$$\tan^2 x - (\sqrt{3} + 1)\tan x + \sqrt{3} < 0$$

$$(\tan x - \sqrt{3})(\tan x - 1) < 0$$



$$1 < \tan x < \sqrt{3}$$

$$x \in \left(n\pi + \frac{\pi}{4}, n\pi + \frac{\pi}{3}\right), n \in \mathbb{I}$$



6. $\sin x \geq \cos 2x = 1 - 2\sin^2 x$

$$2\sin^2 x + \sin x - 1 \geq 0$$

$2s^2 - s - 1$

$$(2\sin x - 1)(\sin x + 1) \geq 0$$



$$\sin x \in \{-1\} \cup \left[\frac{1}{2}, 1\right]$$

$$x \in \left[2n\pi + \frac{\pi}{6}, 2n\pi + \frac{5\pi}{6}\right] \cup \left\{2n\pi + \frac{3\pi}{2}\right\}$$

$n \in \mathbb{I}$



PT-1, 2, 3

↓
Trig. Egn.

Find no. of solutions
 $\sin x + 2\sin 2x = 3 + \sin 3x$ in $[0, \pi]$.

$$\underline{\sin x - \sin 3x + 2\sin 2x = 3}$$

$$-2\sin x \cos 2x + 4\sin x \cos x = 3$$

$$\underbrace{2\sin x}_{\leq 2} \left(\underbrace{2\cos x - 2\cos^2 x + 1}_{\leq 2\left(\frac{1}{2}\right) - 2\left(\frac{1}{4}\right) + 1 = \frac{3}{2}} \right) = 3$$

$$\leq 2\left(\frac{1}{2}\right) - 2\left(\frac{1}{4}\right) + 1 = \frac{3}{2}$$

$$\underbrace{\hspace{10em}}_{\leq 3}$$