

$$PV = nRT$$

$$n = \frac{PV}{RT}$$

For isothermal

Temp doesn't change

$$P_1 - P_{atm} = \frac{4S}{r_1}$$

$$P_2 - P_{atm} = \frac{4S}{r_2}$$

$$P - P_{atm} = \frac{4S}{R}$$

Soap bubble coalesce isothermally.
Isothermally \rightarrow Temp. Constant.
Initially both the bubble have same temp. Find expression for Surface tension 'S' = ??

No of moles conserved.

$$n_1 + n_2 = n \\ \Downarrow$$

$$P_1 \frac{4}{3}\pi r_1^3 + P_2 \frac{4}{3}\pi r_2^3 = \frac{P \frac{4}{3}\pi R^3}{}$$

$$\frac{4}{3}\pi(r_1^3 + r_2^3) = \frac{4}{3}\pi R^3$$

$$R^3 = r_1^3 + r_2^3$$

$$P_1 - P_{atm} = \frac{4S}{r_1}$$

$$P_2 - P_{atm} = \frac{4S}{r_2}$$

$$P - P_{atm} = \frac{4S}{R}$$

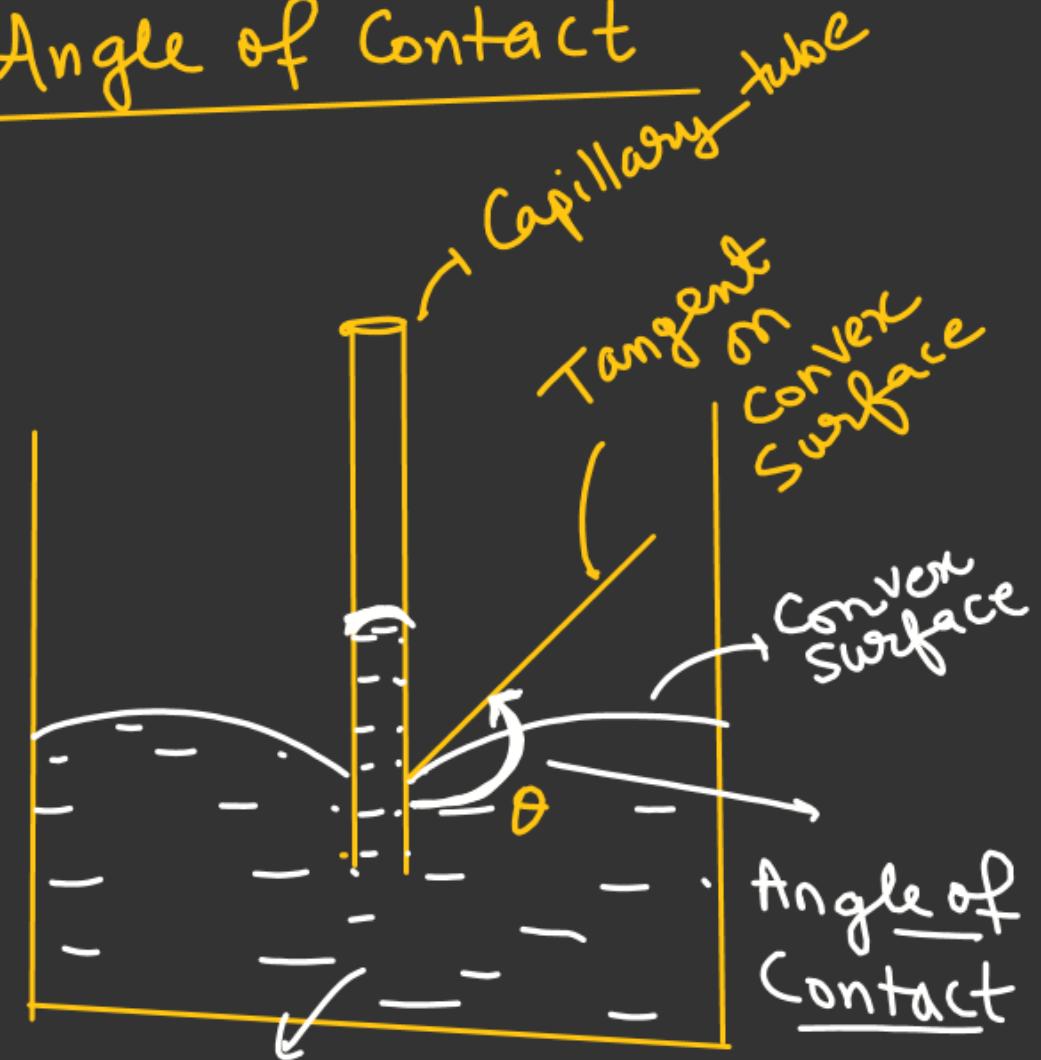
$$\downarrow P_1 \frac{4}{3}\pi r_1^3 + P_2 \frac{4}{3}\pi r_2^3 = \frac{P \frac{4}{3}\pi R^3}{}$$

$$(P_{atm} + \frac{4S}{r_1})r_1^3 + (\frac{4S}{r_2} + P_{atm})r_2^3 = (P_{atm} + \frac{4S}{R})R^3$$

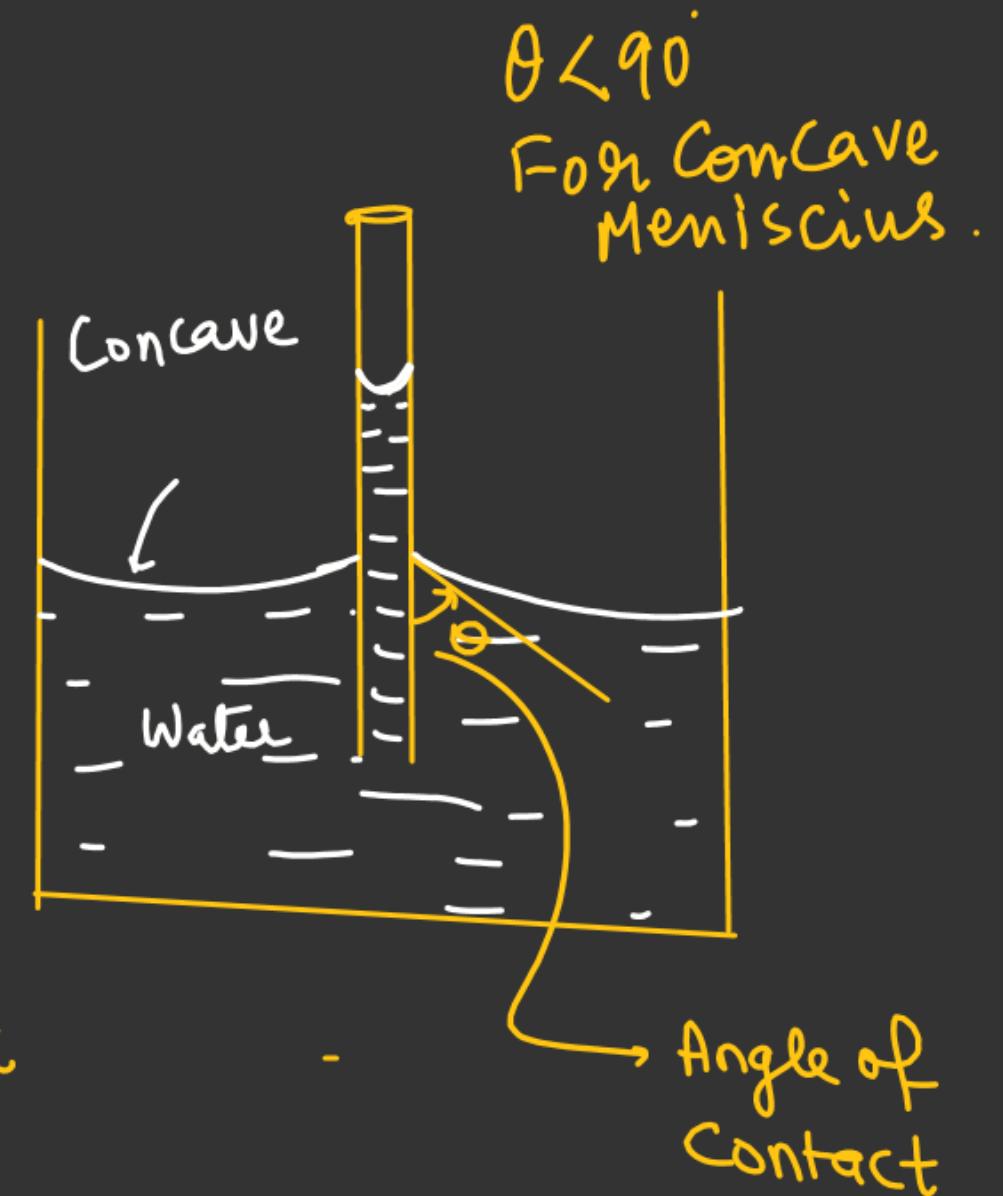
$$P_{atm} (\underbrace{r_1^3 + r_2^3 - R^3}_{\cdot}) = 4S (R^2 - (r_1^2 + r_2^2))$$

$$S = \frac{P_{atm}}{4} \left[\frac{(r_1^3 + r_2^3) - R^3}{R^2 - (r_1^2 + r_2^2)} \right]$$

Angle of Contact



Hg: $\theta > 90^\circ$ for Convex Meniscus

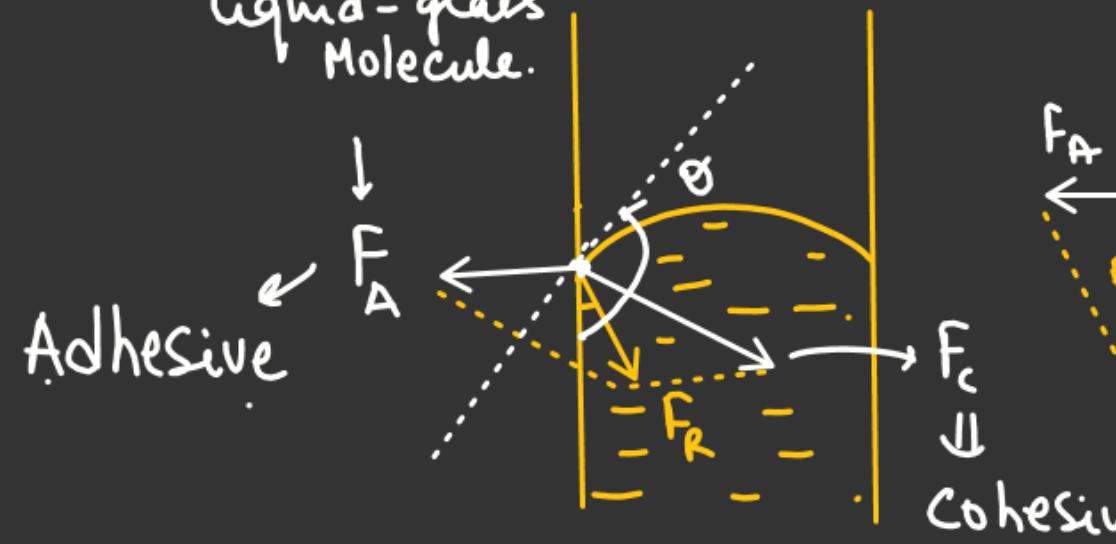


$\theta < 90^\circ$
For Concave Meniscus.

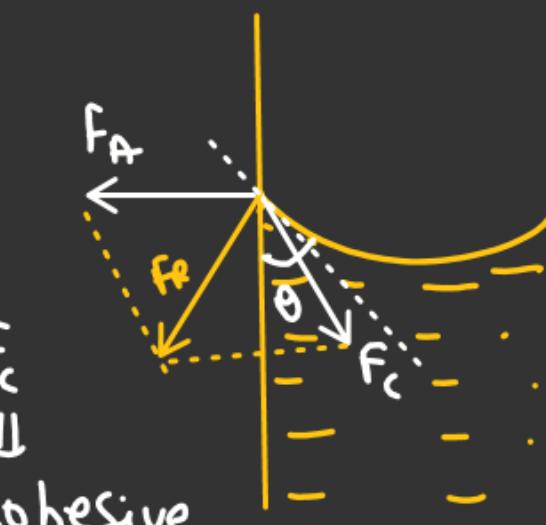
(*) For pure water and clean glass
angle of contact is zero

Shape of liquid Meniscus \rightarrow (Shape of liquid Surface)

Liquid-glass
Molecule.



Adhesive



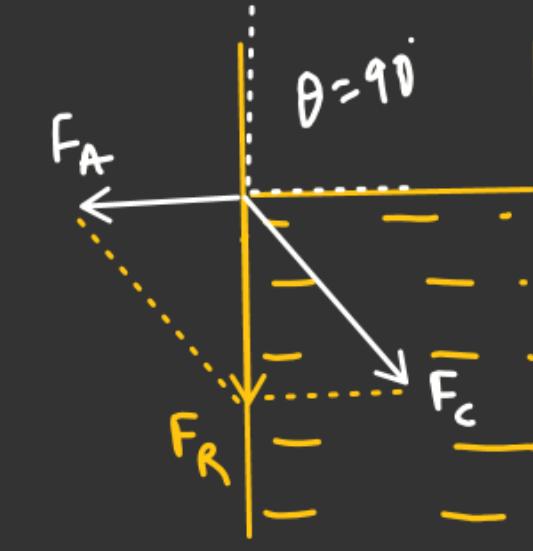
Cohesive

$$\frac{F_c > F_A}{\downarrow} \Rightarrow \text{Convex Meniscus}$$

Such liquid is called
(Non-Wetting)

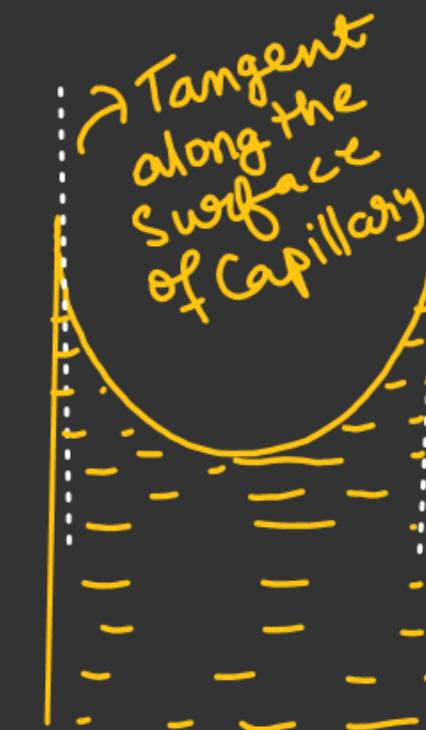
Ex:- Hg

$F_A > F_c$
Concave
Meniscus
 ↳ Wetting liquid
 ↳ Ex:- Water.



$$\theta = 90^\circ$$

$$(F_A = F_c)$$



$$\theta = 0^\circ$$

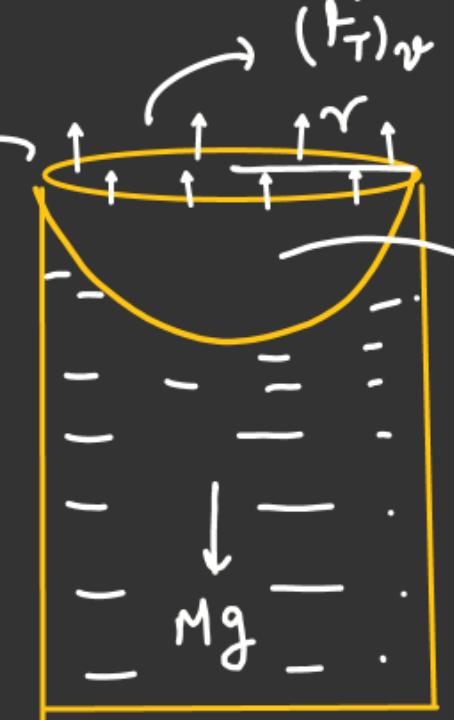
Ex:- Pure water
on
clean glass

~~Ans.~~

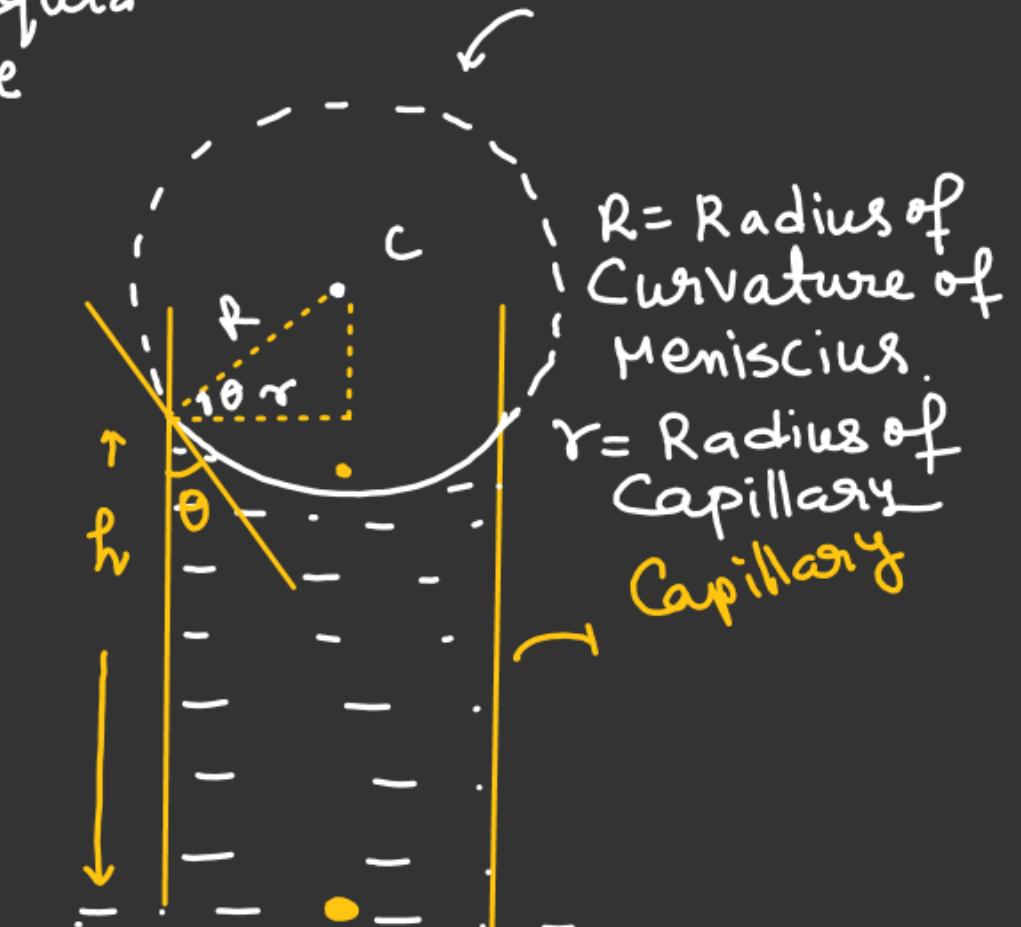
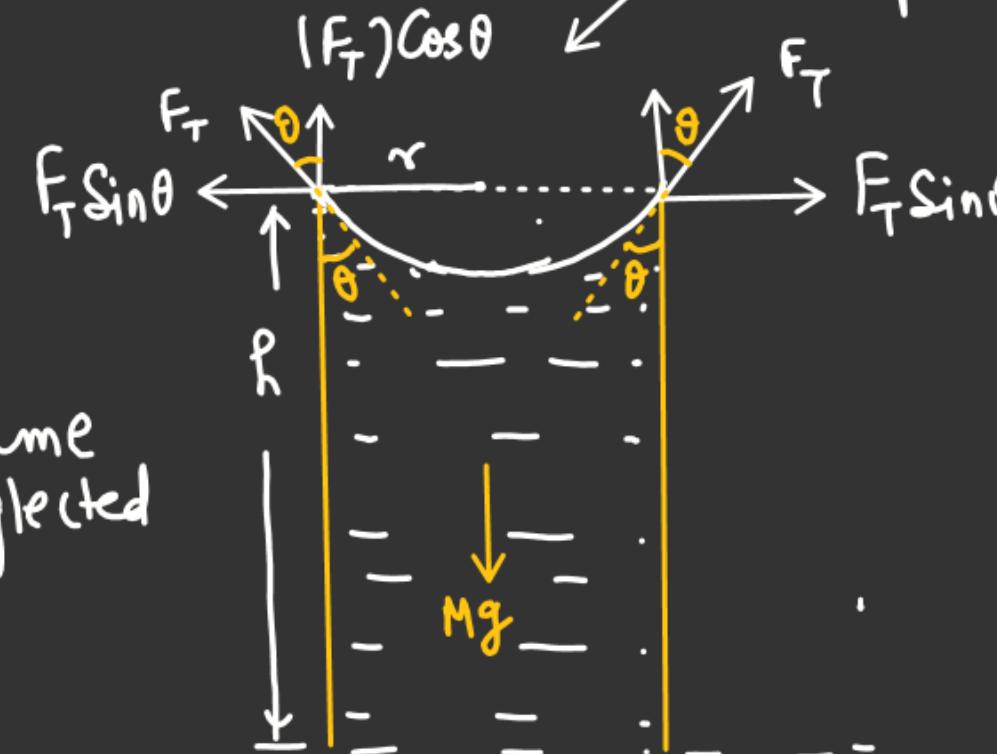
Capillary Rise.

(Due to excess pressure)

$$\text{effective contact} = 2\pi r$$



F.B.D of liquid
Rise in the
Capillary



$$\underbrace{\rho(\pi r^2 h)g}_{M} = (F_T)_v$$

$$= F_T \cos \theta$$

$$\cancel{\rho \pi r^2 h g} = T \cdot 2 \cancel{\pi r} \cdot \cos \theta \Rightarrow$$

$$h = \frac{2T \cos \theta}{\rho g r}$$

θ = angle of contact
 r = radius of capillary
 T = surface tension



If height of Capillary is insufficient

$$\cos\theta = \frac{r}{R} \Rightarrow \frac{r}{\cos\theta} = R.$$

$$h = \frac{2T \cos\theta}{\rho g r}$$

$$h = \frac{2T}{\rho g R}$$

$$hR = \left(\frac{2T}{\rho g} \right)$$

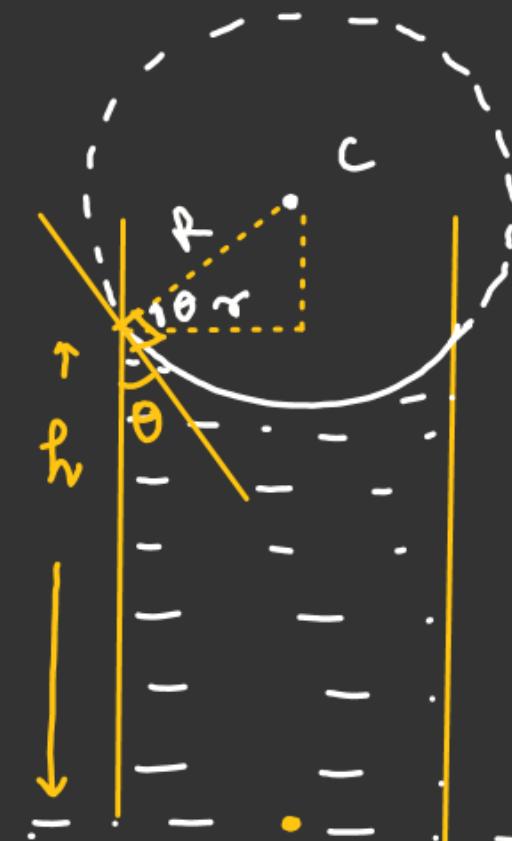
(constant)

R = Radius of
Curvature of
liquid meniscus

$$h_1 R_1 = h_2 R_2$$

$$R_2 = \left(\frac{h_1 R_1}{h_2} \right) \quad \text{if } h_1 > h_2$$

$$\frac{R_2}{R_1} = \frac{h_1}{h_2} \Rightarrow R_2 > R_1$$



Capillary Rise

$$P_1 = P_4 = P_{atm.} \text{ (open to atmosphere)}$$

$$\underline{P_4 = P_3} \quad (\text{Points on the same horizontal level})$$

$$P_4 = P_3 = P_{atm.}$$

$$P_1 - P_2 = \frac{2T}{R} \Rightarrow P_2 = \left(P_1 - \frac{2T}{R} \right)$$

•1

•2

$$P_3 = \underline{\underline{P_2 + \rho gh}}$$

$$P_3 = \left(P_1 - \frac{2T}{R} \right) + \rho gh$$

$$\underline{P_1 = P_3}$$

$$\frac{2T}{R} = \rho gh \quad R = \frac{\gamma}{\cos \theta}$$

$$h = \left(\frac{2T}{\rho g R} \right) \Rightarrow \left(h = \frac{2T \cos \theta}{\rho g R} \right)$$

