

$$\Delta^2 = \begin{vmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{vmatrix} \begin{vmatrix} ax_1 & ay_1 & az_1 \\ bx_2 & by_2 & bz_2 \\ cx_3 & cy_3 & cz_3 \end{vmatrix} \frac{1}{abc} = \frac{1}{abc} \begin{vmatrix} d & f & f \\ f & d & f \\ f & f & d \end{vmatrix}$$

$\downarrow R_1 \rightarrow R_1 + R_2 + R_3$

$$= \begin{vmatrix} 1+1+1 & \alpha^1 + \beta^1 + \gamma^1 & \alpha^2 + \beta^2 + \gamma^2 \\ \alpha^1 + \beta^1 + \gamma^1 & \alpha^2 + \beta^2 + \gamma^2 & \alpha^3 + \beta^3 + \gamma^3 \end{vmatrix} \frac{d+2f}{abc}$$

$$= \begin{vmatrix} 1 & 1 & 1 \\ \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \end{vmatrix} \begin{vmatrix} 1 & \alpha & \alpha^2 \\ 1 & \beta & \beta^2 \\ 1 & \gamma & \gamma^2 \end{vmatrix}$$

$$\left| \begin{array}{ccc} y^2 & -xy & x^2 \\ a & b & c \\ a' & b' & c' \end{array} \right| \xrightarrow{\begin{array}{l} C_2 \rightarrow yC_2 + xC_1 \\ C_3 \rightarrow yC_3 + xC_2 \end{array}}$$

$$= \frac{1}{y^2} \left| \begin{array}{ccc} y^2 & 0 & 0 \\ a & by+ax & cy+bx \\ a' & b'y+a'x & c'y+b'x \end{array} \right| = \left| \begin{array}{cc} by+ax & cy+bx \\ b'y+a'x & c'y+b'x \end{array} \right|$$

$\downarrow C_2 \rightarrow yC_2 + xC_1$

$$\frac{1}{y} \left| \begin{array}{cc} a_{11}+b_1y & u \\ a'_{11}+b'_1y & u' \end{array} \right|$$

$$\textcircled{3} - \cos^2 \textcircled{1} + \sin^2 \textcircled{2}$$

$$z(1 - \cos^2 \textcircled{1} + \sin^2 \textcircled{2}) = 2 - \frac{\cos^2 \textcircled{1} - \cos^2 \textcircled{2} + \sin^2 \textcircled{2} - \sin^2 \textcircled{1}}{2}$$

$$\boxed{z = 1}$$

$$\boxed{\begin{matrix} c=2 \\ D= \end{matrix}}$$

$$\begin{matrix} -3x = 0 \\ x = 0 \end{matrix}$$

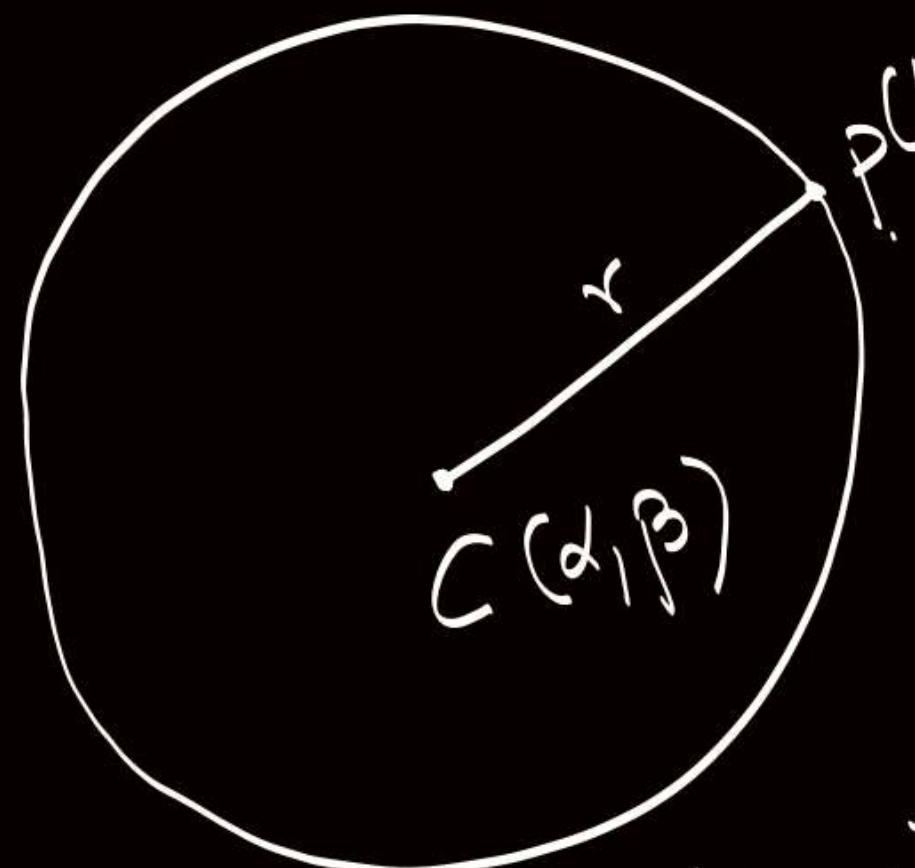
$$(x, y, z) = \left( 1, \frac{1}{2}, -\frac{1}{2}, 0 \right) \cdot \begin{matrix} 2x+2y-2z=1 \\ 4x+4y-z=2 \\ 6x+6y+2z=3 \end{matrix}$$

$$\boxed{x+y = \frac{1}{2}}$$

$$\text{Circumcentre} = \left( \frac{(\sin 2A)x_1 + (\sin 2B)x_2 + (\sin 2C)x_3}{\sin 2A + \sin 2B + \sin 2C}, - \right)$$

$$\begin{aligned}
 \frac{OA}{OD} &= \frac{\Delta AOB}{\Delta BOD} = \frac{\Delta AOC}{\Delta COD} \quad A(x_1, y_1) \\
 &= \frac{\Delta AOB + \Delta AOC}{\Delta BOD + \Delta COD} \quad \text{sin } 2C + \sin 2B \\
 &= \frac{\Delta AOB + \Delta AOC}{\Delta BOC} \quad \text{sin } 2C \quad D(x_3, y_3) \\
 &= \frac{\frac{1}{2}(OA)(OB)\sin 2C + \frac{1}{2}R \times R \sin 2B}{\frac{1}{2}R \times R \sin 2A} \\
 &= \frac{(\sin 2B)x_2 + (\sin 2C)x_3}{\sin 2B + \sin 2C}
 \end{aligned}$$

$$\begin{aligned}
 \frac{BD}{DC} &= \frac{\Delta BOD}{\Delta COD} = \frac{\frac{1}{2}(OB)(OD)\sin(\pi - 2B)}{\frac{1}{2}(OC)(OD)\sin(\pi - 2C)} \\
 &= \frac{\sin 2C}{\sin 2B}
 \end{aligned}$$

Locus

find locus of  $P$  moving in plane  
so that its distance from  
 $C$  is constant =  $r$ .

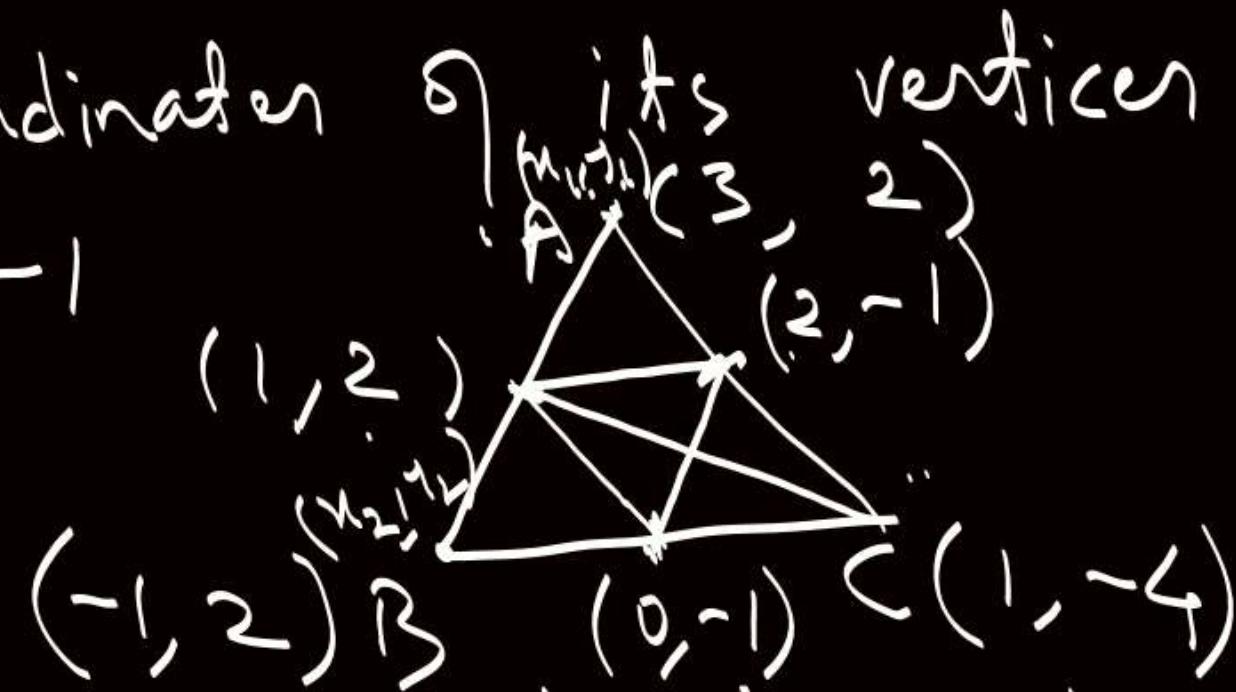
$$(h-\alpha)^2 + (k-\beta)^2 = r^2$$

$$(x-\alpha)^2 + (y-\beta)^2 = r^2$$

1. The midpoints of the sides of a triangle are  $(1, 2)$ ,  $(0, -1)$  and  $(2, -1)$ . Find the coordinates of its vertices.

$$x_1 + x_2 = 2 \quad x_1 + x_2 + x_3 = 3$$

$$2-1 = y-1$$



$$x_2 + x_3 = 0$$

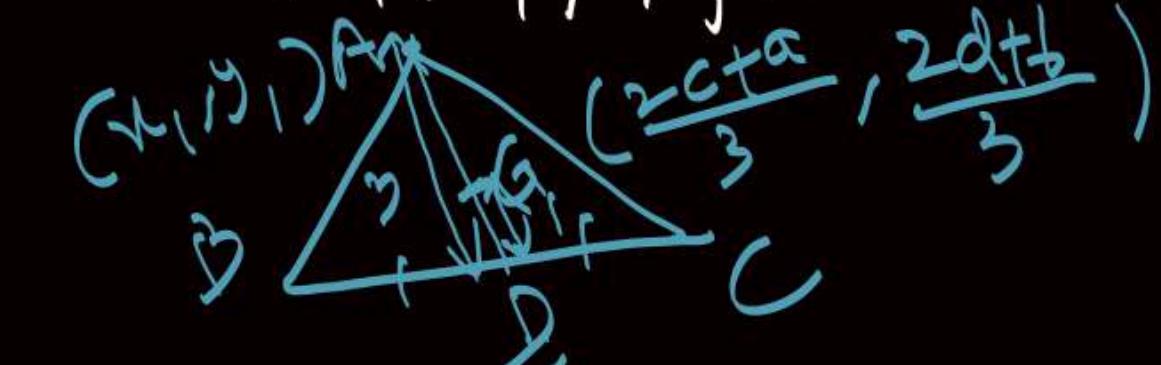
$$x_3 + x_1 = 4$$

$$x_1 = 2 + 0$$

$$D = \frac{3G - 1A}{3-1}$$

2. Orthocentre and circumcentre of  $\triangle ABC$  are  $(a, b)$  &  $(c, d)$  respectively. If coordinates of A is  $(x_1, y_1)$ , find the coordinate of middle point of BC.

$$\left( \frac{2c+a}{3}, \frac{2d+b}{3} \right)$$

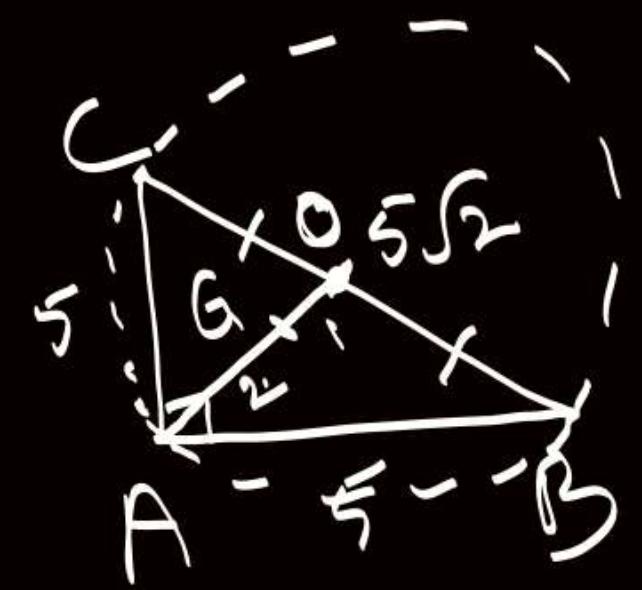


3: If the vertices of triangle are  $A(2, -2)$ ,  $B(-2, 1)$  and  $C(5, 2)$ . Find the distance b/w circumcentre and centroid.

$$AB = 5$$

$$BC = 5\sqrt{2}$$

$$CA = 5$$



$$\begin{aligned} OG &= \frac{1}{3} \left( \frac{5\sqrt{2}}{2} \right) \\ &= \frac{5\sqrt{2}}{6} \end{aligned}$$

4. If the area of triangle formed by points

$(1, 2), (2, 3), (x, 4)$  is  $40$  , find  $x$  .

$$\frac{1}{2} \begin{vmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ x & 4 & 1 \end{vmatrix} = \pm 40 \Rightarrow x = 83, -77$$

5. If points  $(a, 0), (0, b)$  and  $(1, 1)$  are collinear, find

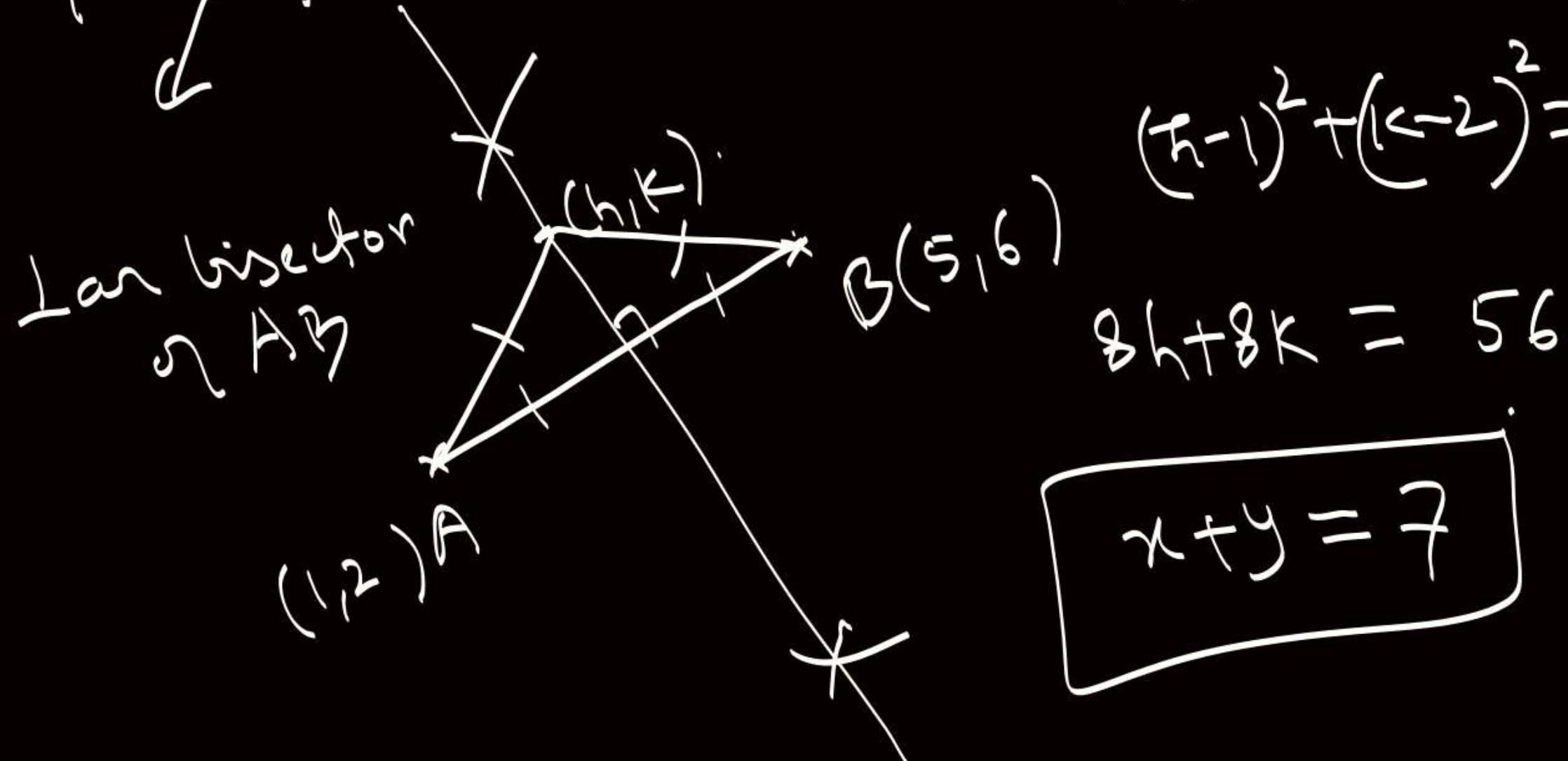
$$\frac{1}{a} + \frac{1}{b} = 1 \cdot \begin{vmatrix} a & 0 & 1 \\ 0 & b & 1 \\ 1 & 1 & 1 \end{vmatrix} = 0 = a(b-1) - b = 0$$

$$ab = a+b$$

$$\frac{1}{a} + \frac{1}{b} = 1 \cdot$$

Q.  $A = (1, 2)$ ,  $B = (5, 6)$ , find locus of

point  $P$  such that  $PA = PB$ .



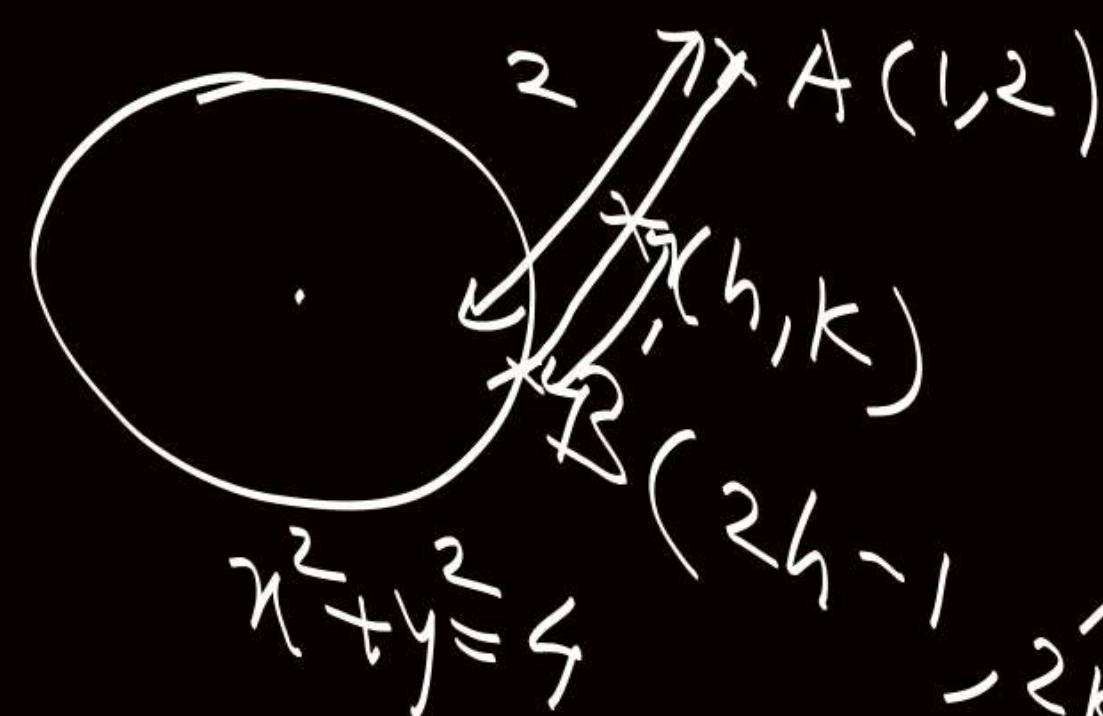
$$(h-1)^2 + (k-2)^2 = (h-5)^2 + (k-6)^2$$

$$8h + 8k = 56$$

$$x + y = 7$$

$\exists$ : A(1,2) is a fixed point. A variable point B lies on curve whose equation is  $x^2+y^2=4$ .

Find the locus of midpoint Q AB.



$$x^2+y^2=4$$

$$\begin{aligned} (2h-1)^2 + (2k-2)^2 &= 4 \\ 4h^2 + 4k^2 - 4h - 8k + 1 &= 0 \end{aligned}$$

Determinants

$$\begin{vmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 2h-1 & 2k-2 & 2h-1 & 2k-2 \\ 2h-1 & 2k-2 & 2h-1 & 2k-2 \end{vmatrix}$$