

$$\boxed{b^2 - ac > 0} \quad \stackrel{13}{\rightarrow} \quad (a(a+c) + 2(b^2 - ac))x^2 + 2b(a+c)x + (c(a+c) + 2(b^2 - ac))$$

$$D = 4 \left[ b^2(a+c)^2 - ac(a+c)^2 - 2(b^2 - ac)(a+c)^2 - 4(b^2 - ac)^2 \right] = 0$$

$$= 4 \left[ -b^2(a+c)^2 + ac(a+c)^2 - 4(b^2 - ac)^2 \right]$$

$$= 4 \left[ (b^2 - ac)(a+c)^2 - 4(b^2 - ac)^2 \right] < 0$$

$$y(bcx^2 - (ac+bd)x + ad) = adx^2 - (ac+bd)x + bc \cdot$$

$$(yb - ad)x^2 - (ac+bd)(y-1)x + (ad - bc) = 0 \cdot$$

$$(ac+bd)^2(y^2 - 2y + 1) - 4(ac+bd)y^2 - 4(b^2c^2 + a^2d^2) + abcd \geq 0$$

$$(ac-bd)y^2 + \left(2(b^2c^2 + a^2d^2) - (ac+bd)^2\right)2y + (ac-bd)^2 \geq 0 \quad \forall y \in \mathbb{R}.$$

$$\begin{aligned} D \leq 0 &\Rightarrow \left(2(b^2c^2 + a^2d^2) - (ac+bd)^2 - (ac-bd)^2\right) \left(2(b^2c^2 + a^2d^2) - (ac+bd)^2 + (ac-bd)^2\right) \leq 0 \\ &\Rightarrow 4 \left((b^2c^2 + a^2d^2) - (a^2c^2 + b^2d^2)\right) \left(\frac{b^2c^2 + a^2d^2}{(b^2 - a^2)(c^2)} - \frac{d^2}{(b^2 - a^2)(c^2)} (bc - ad)^2\right) \leq 0 \end{aligned}$$

$$lx^2 + mx + ny^2 = 0 \Rightarrow nt^2 + mt + l = 0 \quad \frac{y}{x} = k - \text{const} = \alpha \beta \cdot \\ y = \alpha x \quad y = \beta x$$

$$\frac{y}{x} = t$$

$$nt$$

$$l' x^2 + m' xy + n' y^2 = 0$$

$$n' t^2 + m' t + l' = 0$$

$$\frac{x^2 - 2x + 6}{1} = f(x)$$

$$\frac{t^2}{t^2} = \frac{t}{t} = \frac{1}{1}$$

$\nearrow$  Rational

$$f(x) = \frac{x^3 - x^2 + 2x - 1}{x^2 - 3x + 7}$$

Rational function

$f(x) = \frac{\text{Polynomial function}}{\text{Polynomial function}}$

1. Show that in equation  $x^2 - 3xy + 2y^2 - 2x - 3y - 35 = 0$ ,  
for every real value of  $x$  there is a real value of  $y$ ,

and for every real value of  $y$  there is a real  $x$ .

$$y = \frac{3(x+1) \pm \sqrt{(x+1)^2 - 4}}{4} = x+5, \frac{x-7}{2}$$

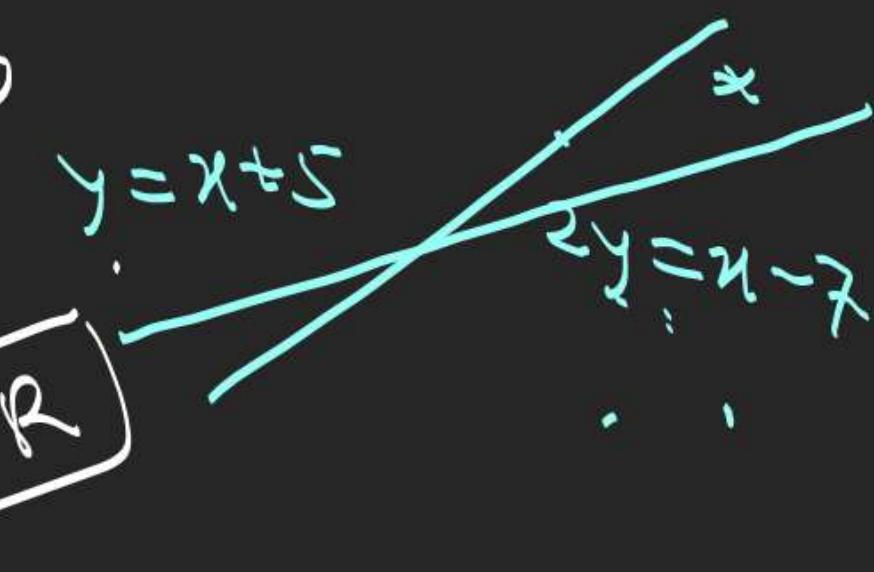
for what  $x$ ? there is a real  $y$

$$\frac{2y - x + 7}{=0}, \frac{y - x - 5}{=0}$$

$$2y^2 - (3x+3)y + x^2 - 2x - 35 = 0$$

$$\Delta \geq 0 \Rightarrow 9(x+1)^2 - 8(x^2 - 2x - 35) \geq 0$$

$$x^2 + 34x + 289 \geq 0 \Rightarrow (x+17)^2 \geq 0 \quad \boxed{x \in \mathbb{R}}$$

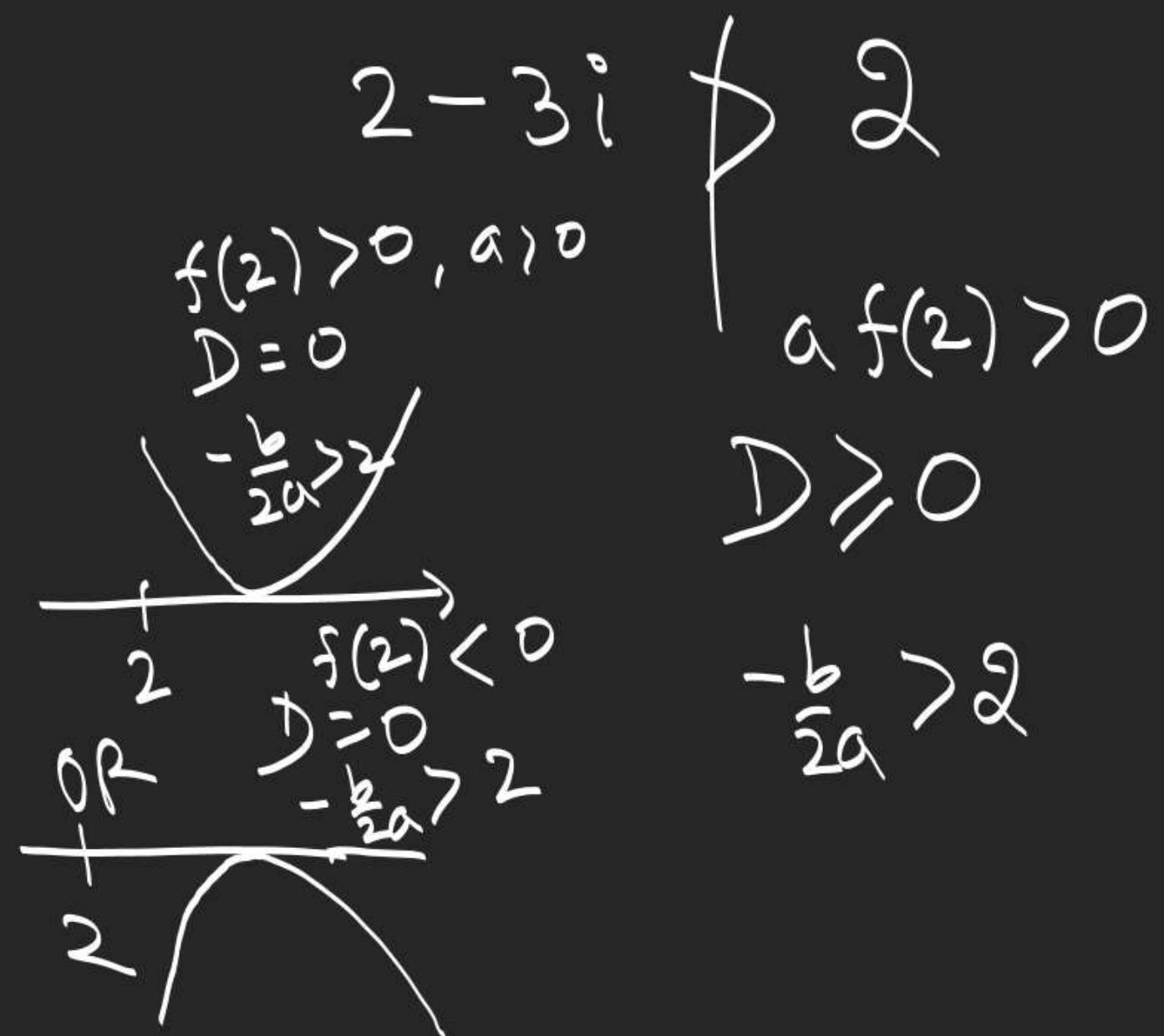
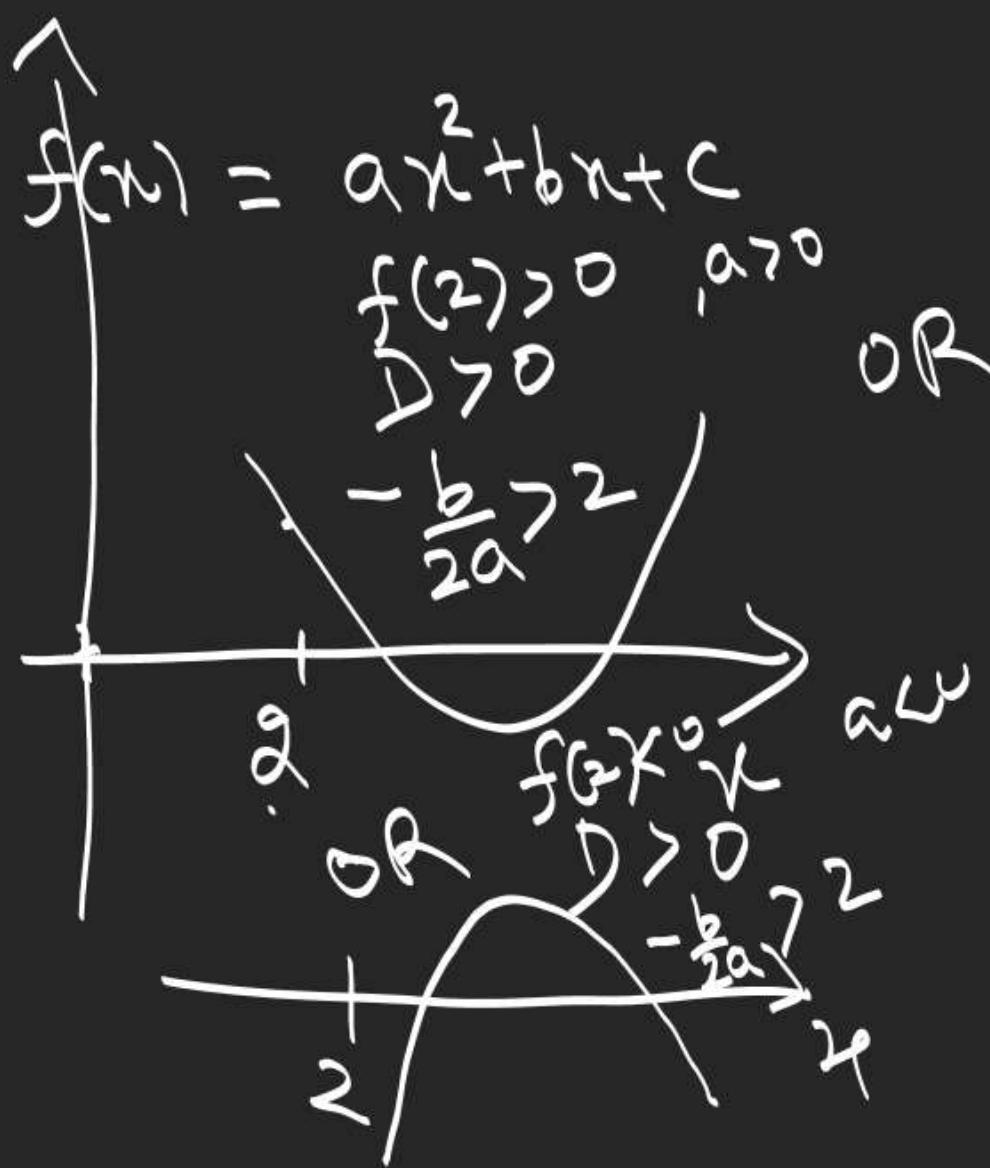


Condition for both roots of quadratic eqn.

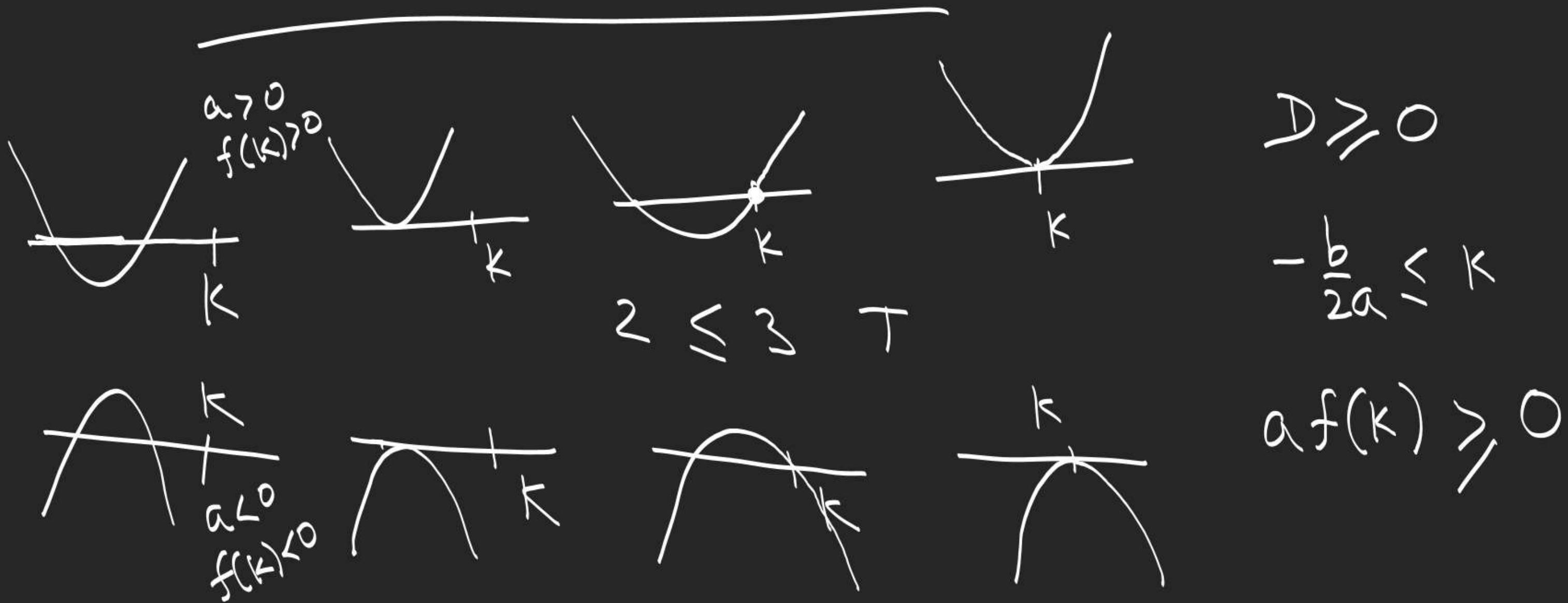
$$ax^2 + bx + c = 0$$

,  $a, b, c \in \mathbb{R}$ ,  $a \neq 0$  to be more than

$|z|$



Condition for  $ax^2+bx+c=0$ ,  $a, b, c \in \mathbb{R}$ ,  $a \neq 0$   
 to have both roots  $\leq k$



\* Condition for  $a^2+b^2+c=0$ ,  $a, b, c \in \mathbb{R}$ ,  $a \neq 0$   
to have both roots in interval  $[k_1, k_2]$

\* If  
one root  $< k_1$  & other root  $> k_2$ ,  $k_1 < k_2$

Ex- 9(c) 7, 8, 9, 10.

























