

$$3^a \cdot 3^c = 3^{2b}$$

$\underbrace{a + c}_{\downarrow \downarrow} = 2b$

$$7^{10} - \left[{}^7C_6 {}^{10} - {}^7C_2 {}^{10} + \dots \right]$$

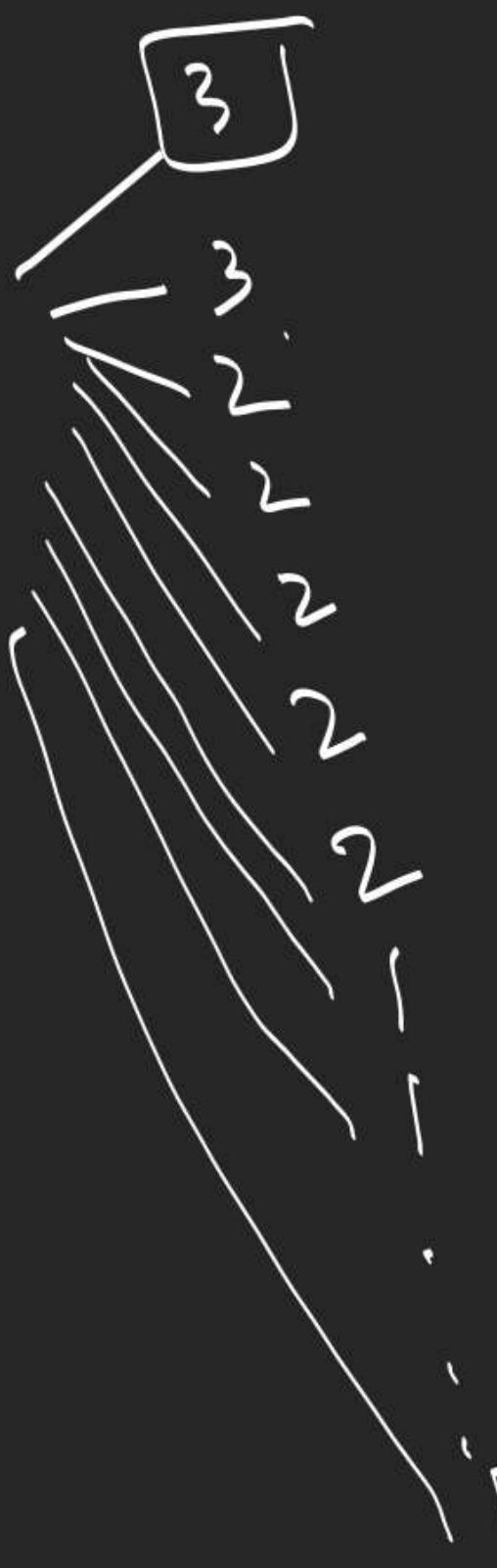
$$\begin{aligned}
 & 3A, 1D \rightarrow {}^6C_1 {}^5C_1 \leftarrow E + {}^{50}C_2 \\
 & 2A, 20A \rightarrow {}^6C_2 \\
 & 2A, 2D \rightarrow {}^6C_1 {}^5C_2 \quad | \quad | \quad | \quad | \quad | \quad | \quad 4 \longrightarrow {}^7C_1 \frac{10!}{4!} \\
 & \quad | \quad | \quad | \quad | \quad | \quad | \quad 2 \quad 3 \longrightarrow {}^7C_1 {}^6C_1 \frac{10!}{2! \cdot 3!} \\
 & \quad | \quad | \quad | \quad | \quad | \quad | \quad 2 \quad 2 \quad 2 \longrightarrow {}^7C_3 \frac{10!}{2! \cdot 2! \cdot 2!}
 \end{aligned}$$



$$2^4 C_2 - \left(3 \times 4 C_2 + 2 \right)$$

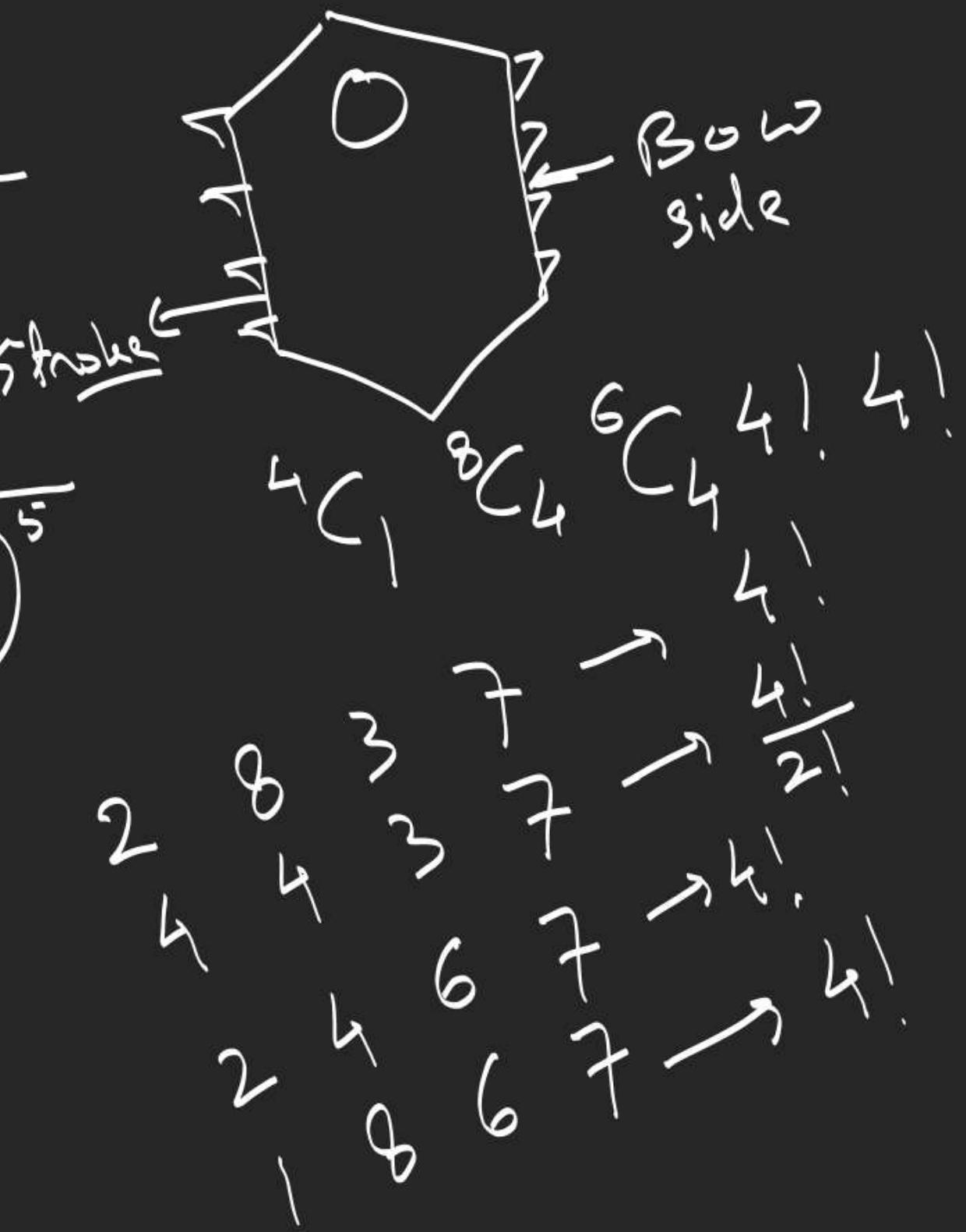
$$\left(\dots \frac{B \text{ or } C}{K B^1 S} \frac{15-K}{15-K} C^5 \right) \left(- \frac{C^5 \text{ or } A}{K C^5 S} \frac{5-K}{5-K} A^5 \right) \left(- \frac{K A^5}{K A^5} \frac{3}{5-K B^1 S} \right)$$

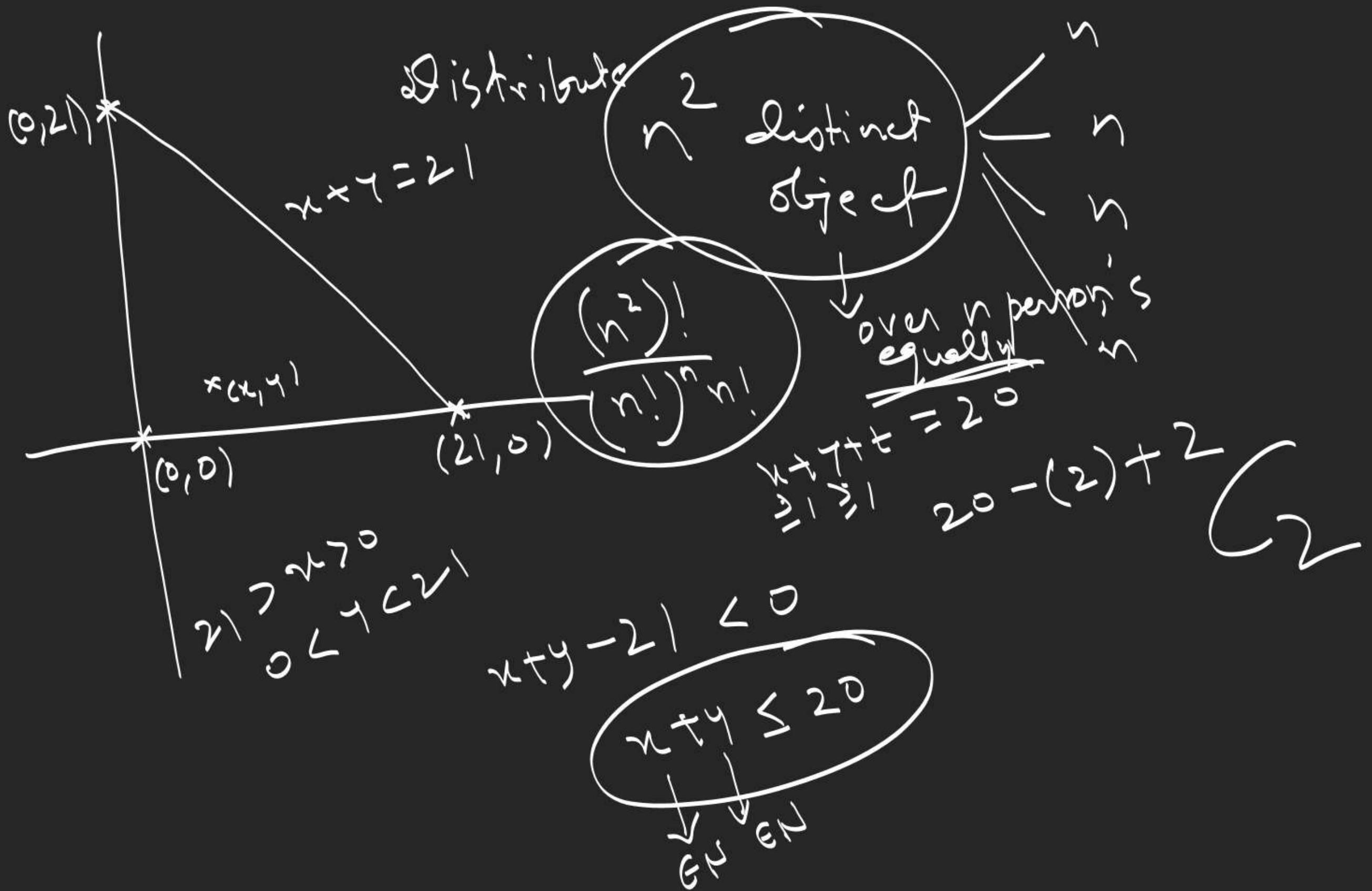
$$\sum_{k=0}^{15} 5^3 C_k - 15 \cdot 2^3 C_3 - 15 \cdot (6+2) \cdot 3^3 C_3$$

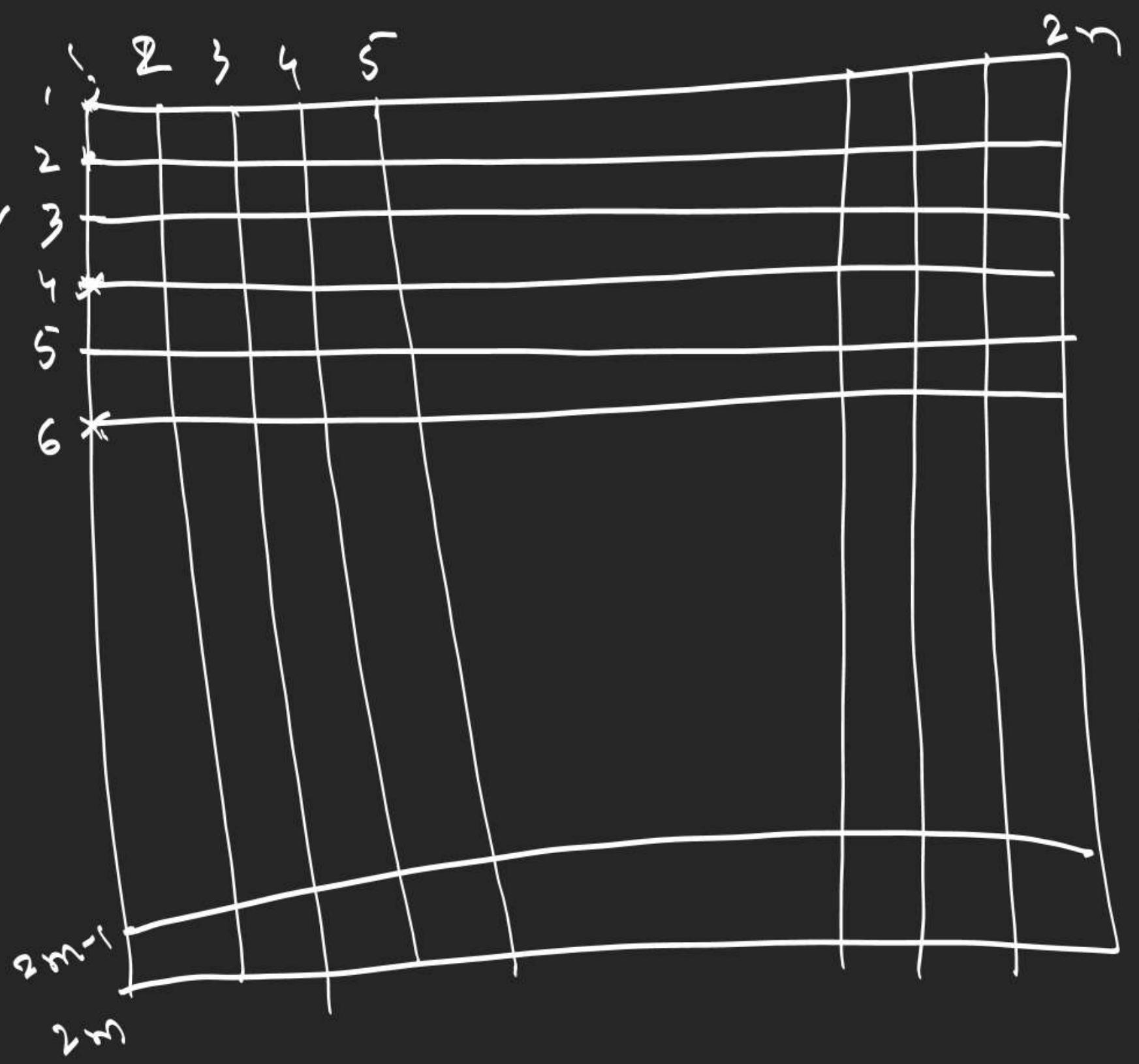


$$\frac{24!}{3! \cdot 3! \cdot (2!)^5}$$

$$8! \cdot \frac{23!}{(3!)^2 \cdot (2!)^5}$$







$$\left(\begin{matrix} x \\ 1 \\ 2 \\ \vdots \\ n \end{matrix} \right)$$

$$1 \times 1, 1 \times 3, 1 \times 5, \dots 1 \times 2n-1$$

$$3 \times 1, 3 \times 3, 3 \times 5, \dots$$

$$5 \times 1, 5 \times 3, \dots$$

$$\left(\begin{matrix} m \\ 1 \\ 2 \\ \vdots \\ n \end{matrix} \right) \left(\begin{matrix} n \\ 1 \\ 2 \\ \vdots \\ 1 \end{matrix} \right)$$

$$\begin{array}{c} P \quad Q \\ r^2 \quad r^0, r^1, r^2 \\ r^0, r^1 \\ r^4 \quad r^0, r^1, r^2, r^3, r^4 \\ r^0, r^1, r^2, r^3, r^4 \\ \{ \quad \{ \quad \{ \quad \{ \quad \{ \\ 5 \text{ ways} \quad 9 \end{array}$$

$$5 \times 9 \times 5$$

$$A \rightarrow \{1\} \checkmark$$

$$B \rightarrow \{2\}$$

$$\{2\}$$

$$\{1\}$$

only A
only B
none

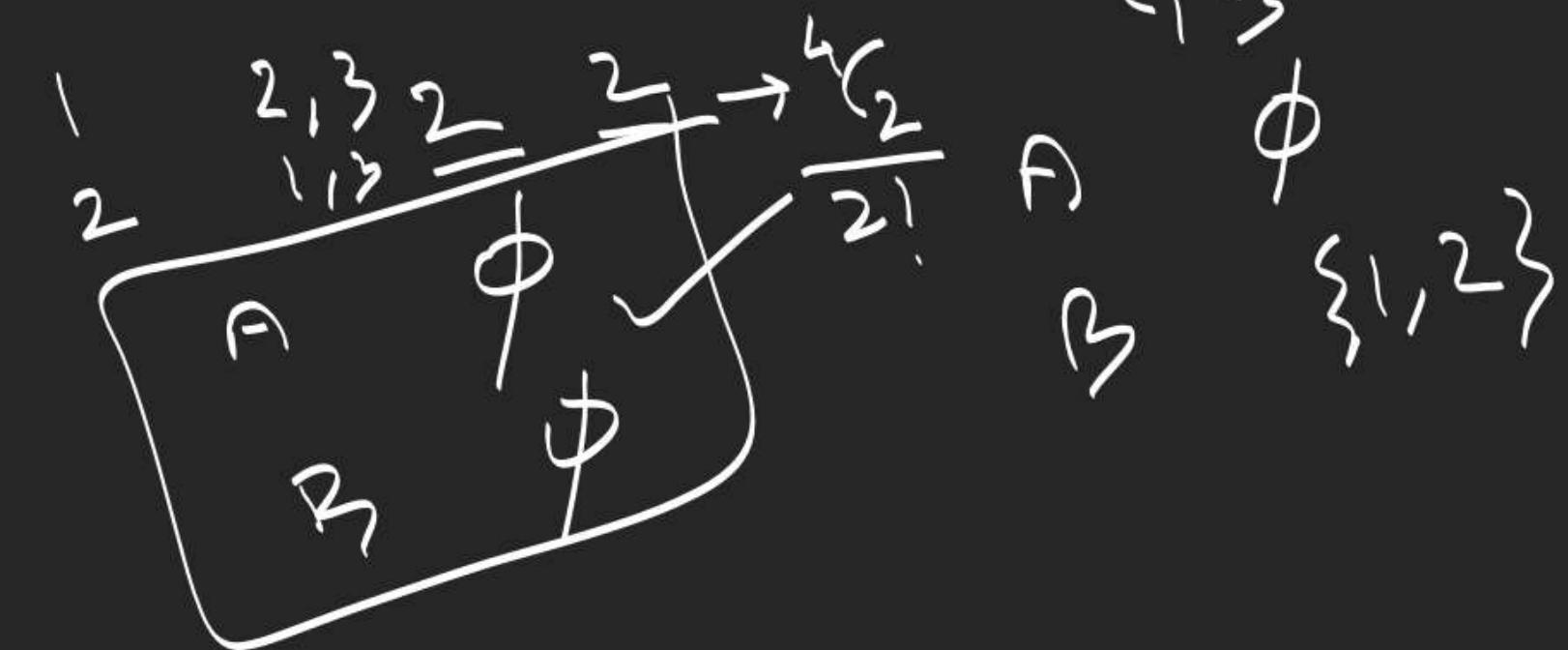
Remaining P&C
 $\{x-1\}$ (Binomial)

$$1, 2, 3, 4$$

$$\frac{3^4 - 1}{2} + 1$$

$$0 \quad 0, 1, 2, 3, 4 \rightarrow 2^4$$

$$! \quad 1, 2, 3 \rightarrow 4C_2 + 4C_1 C_3$$



$$A \quad \phi$$

$$B \quad \{1, 2\}$$