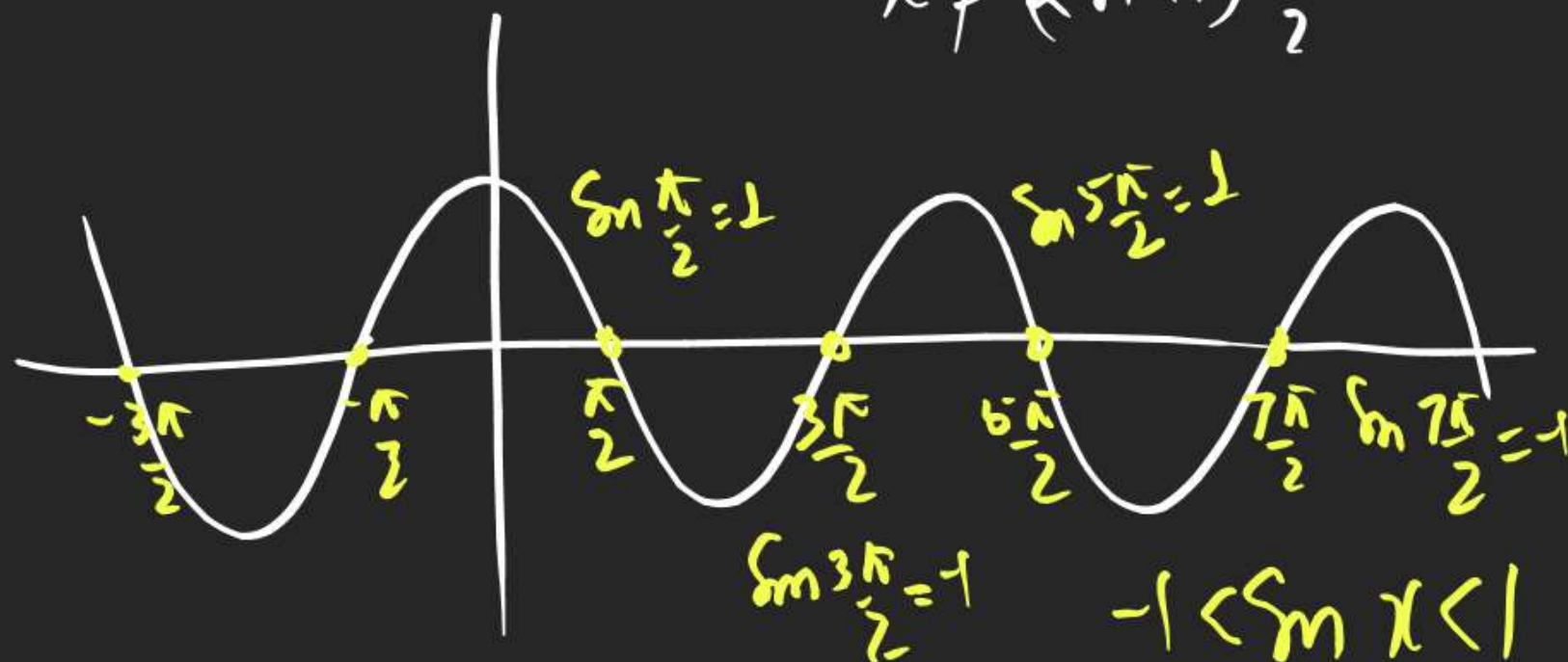


RELATION FUNCTION

Q.25 $y = 4 \tan x \cdot \sec x.$

$$= 4 \frac{\sin x}{\cos x} \times \frac{1}{\cos x} \quad \cos x \neq 0$$

$$x \neq (2n+1)\frac{\pi}{2}$$



$$-1 < \sin x < 1$$

$$\underline{-4 < 4 \sin x < 4}$$

$$f(x) = 4 \sin x \in [-4, 4] \times \mathbb{Q}$$

$$\in (-4, 4)$$

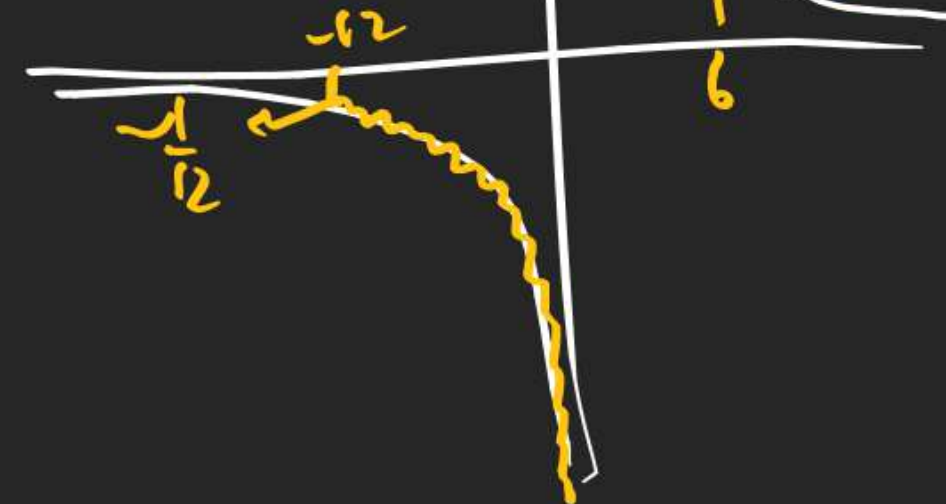
(correction)

$$-9 \leq 9 \sin x \leq 9$$

$$-12 \leq 9 \sin x - 3 \leq 6$$

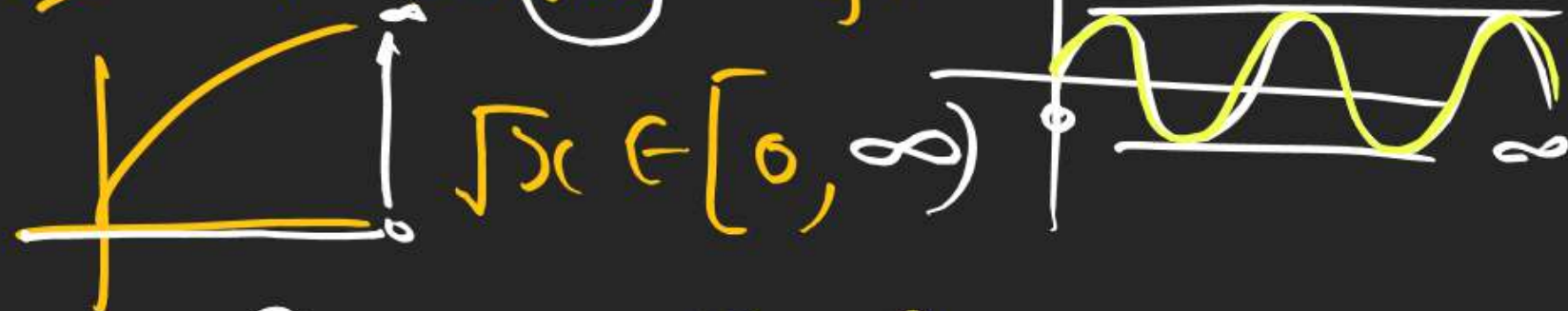
Behave Zero

$$\frac{1}{9 \sin x - 3} \in (-\infty, -\frac{1}{12}] \cup [\frac{1}{6}, \infty)$$



RELATION FUNCTION

Q26 $y = \sin(\sqrt{x})$ is Rf?



$\sin \sqrt{x} \in [-1, 1]$

Q27 $y = 3 - 2^x$ Rf?

$0 < 2^x < \infty$

$0 > -2^x > -\infty$

$3 > 3 - 2^x > -\infty \Rightarrow y \in (-\infty, 3)$



Q28 $y = 4^x + 2^x + 1$ Rf?

$2^x = t \Rightarrow$

$y = t^2 + t + 1, t = 2^x \in (0, \infty)$

Q Eqn ka graph Banao.

$\frac{dy}{dt} = 2t + 1 = 0 \Rightarrow t = -\frac{1}{2}$

$y = (-\frac{1}{2})^2 + \frac{1}{2} + 1 = \frac{3}{4}$



$y = 0^2 + 0 + 1 = 1$

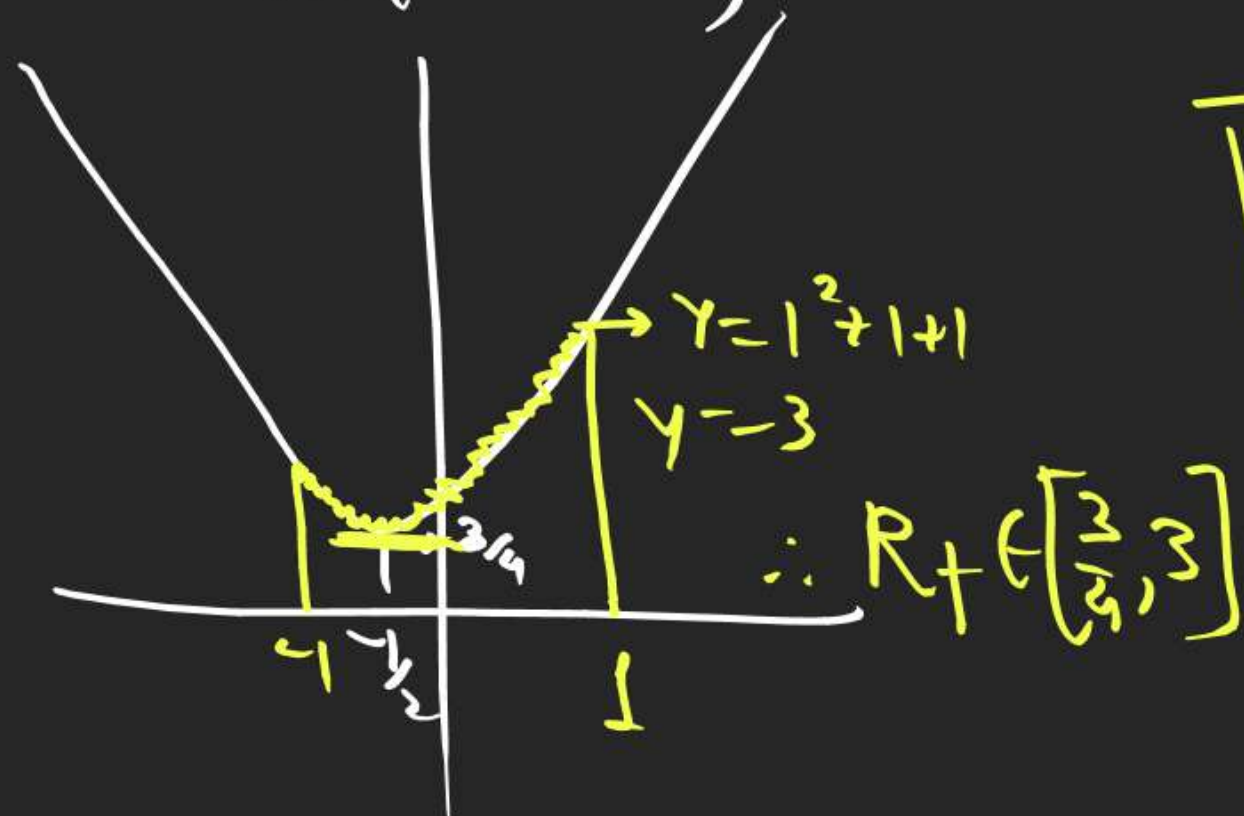
$\therefore y \in (1, \infty)$

RELATION FUNCTION

$$Q29 \quad y = 8m^2x + 8mx + 1$$

$$8mx = t$$

$$y = t^2 + t + 1; \quad t = 8mx \in [-1, 1]$$



$$Q \quad y = -(6m^2x)^2 + 8m^2x + 1 \rightarrow 6m^2x \in [-1, 1]$$

$$Q30 \quad y = \frac{2x-3}{3x+4} \text{ find } R_f? \quad y = \frac{\text{Linear}}{\text{Linear}}$$

$$y = \frac{ax+b}{(cx+d)}$$

$$R_f \rightarrow y \in \mathbb{R} - \left\{ \frac{a}{c} \right\}$$

$$D_f \rightarrow x \in \mathbb{R} - \left\{ -\frac{d}{c} \right\}$$

$$3xy + 4y = 2x - 3$$

$$3xy - 2x = -3 - 4y$$

$$x(3y - 2) = -3 - 4y$$

$$x = \frac{4y+3}{2-3y} \quad \& \text{ Iska dom.}$$

$$2 - 3y \neq 0 \Rightarrow y \neq \frac{2}{3}$$

$$y \in \mathbb{R} - \left\{ \frac{2}{3} \right\}$$

RELATION FUNCTION

Q $y = \frac{x^2 - 5x + 4}{x^2 + 2x - 3}$ find R_f ?

factorise \rightarrow

$$y = \frac{(x-1)(x-4)}{(x+3)(x-1)} \quad \begin{matrix} x \neq 1 \\ x-1 \neq 0 \end{matrix}$$

$\hookrightarrow D_f \rightarrow R - \{-3, 1\}$

Df me $x=1$ Nahi hai \therefore
($x-1$) cancel kr diya.

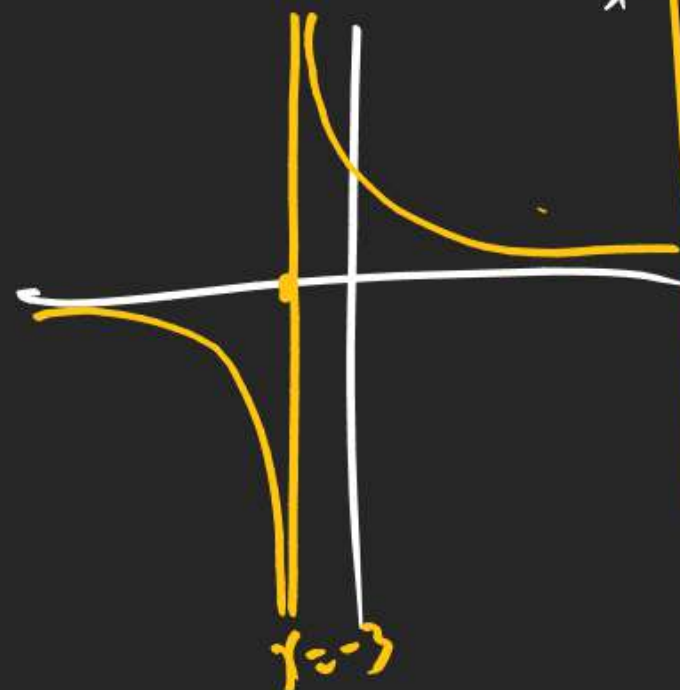
$$y = \frac{x-4}{x+3} \rightarrow R = \left\{1, -\frac{3}{4}\right\}$$

$$\lim_{x \rightarrow 1} \frac{x-4}{x+3} = \frac{1-4}{1+3} = -\frac{3}{4}$$

Q Form Graph of $y = \frac{x-4}{x+3}$
32

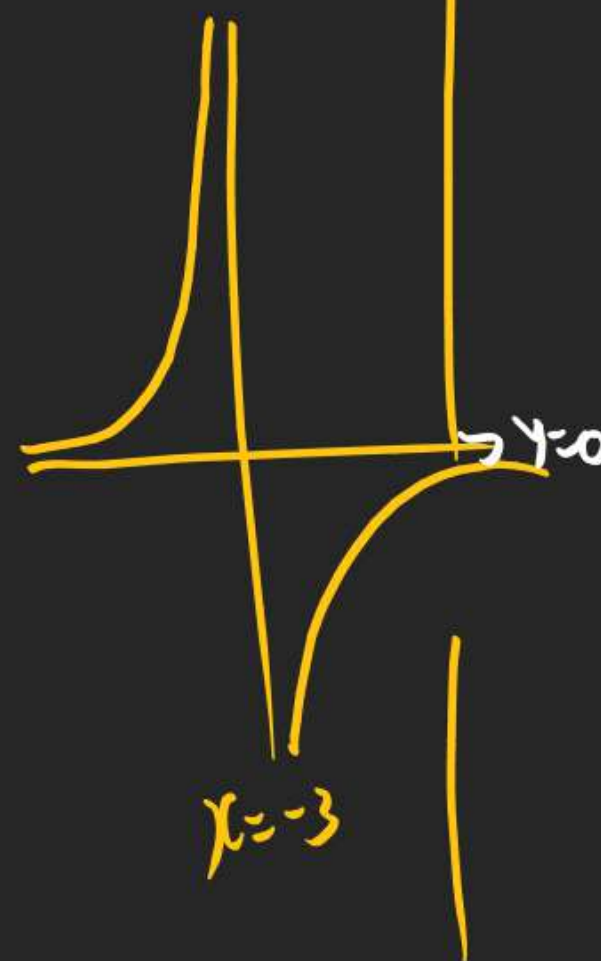
$$y = \frac{(x+3)-7}{(x+3)} = 1 - \frac{7}{(x+3)}$$

① $y = \frac{7}{(x+3)}$
 $x = -3$ or $y = \frac{1}{x}$

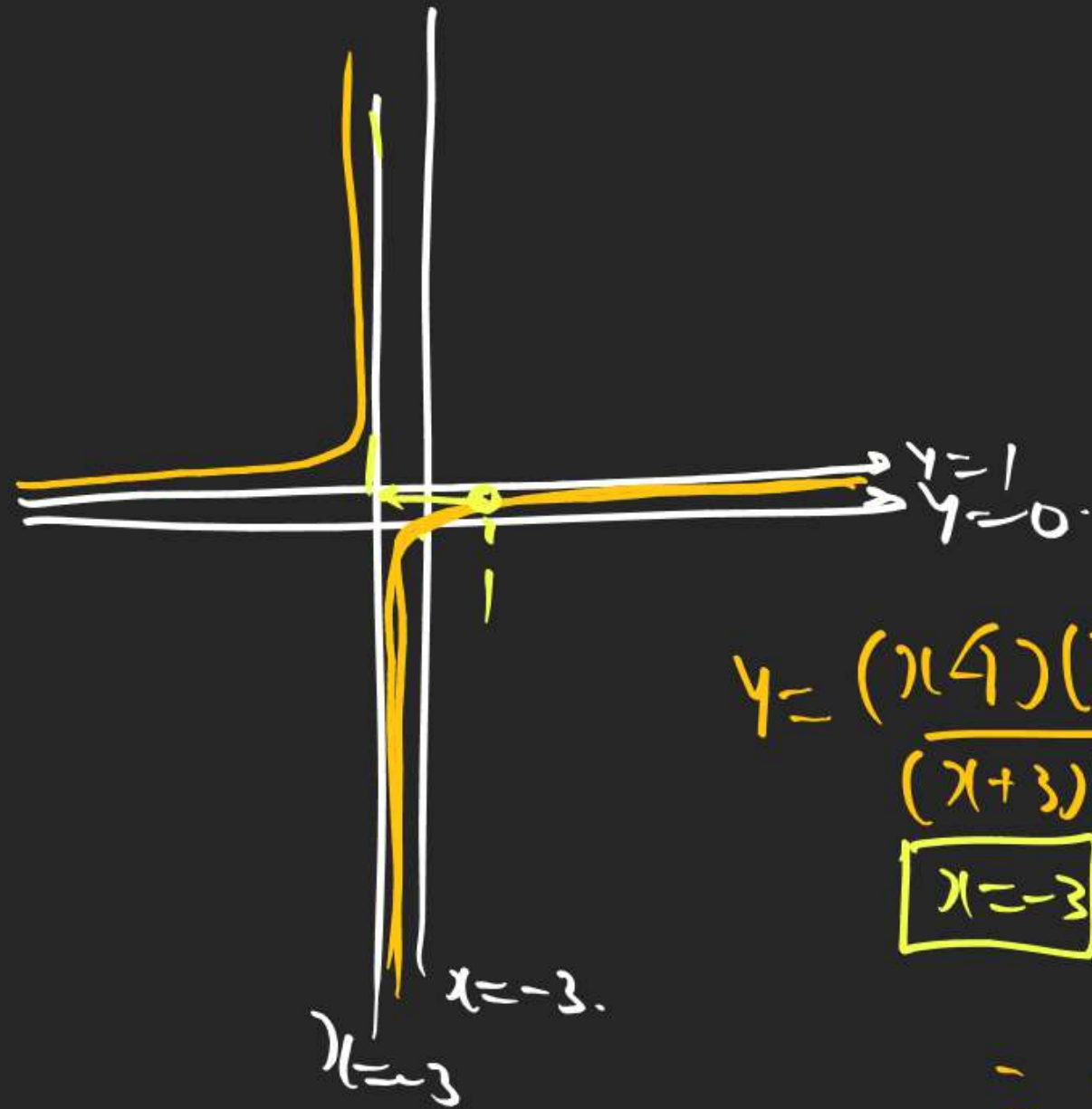


② $y = \frac{-7}{x+3}$

$$y = \frac{-7}{x+3} + 1$$



RELATION FUNCTION

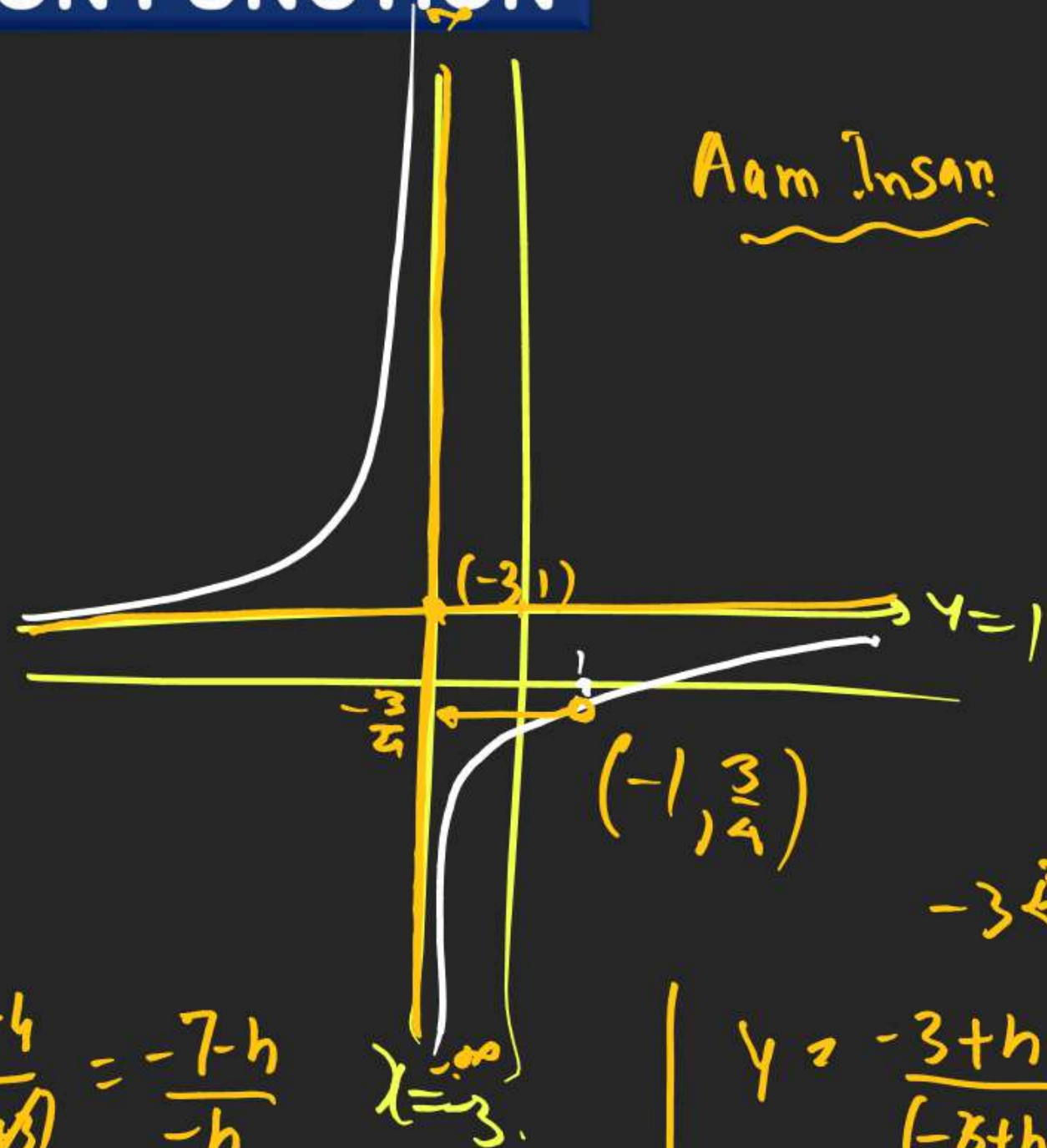


$$y = \frac{(x+4)(x-4)}{(x+3)(x-4)}$$

$$\boxed{x = -3}$$

$$= \frac{-3-h-4}{(-\beta-h+\beta)} = \frac{-7-h}{-h}$$

$$= \frac{7+h}{h} \rightarrow \infty$$



Aam Insan

-3 < x < -1

$$y = \frac{-3+h-4}{(-\beta+h+\beta)} = \frac{-7+h}{h} \rightarrow \infty$$

RELATION FUNCTION

$$Q_{33} \quad y = \frac{x^2 - x + 1}{x^2 + x + 1} \text{ find } R_f$$

factorise try $\frac{1}{2}$ aur $\frac{1}{3}$
 $\frac{1}{2} \in \mathbb{R} \rightarrow \underline{\text{C.M.}}$

$$x^2 y + x(y+1) = x^2 - x + 1$$

$$x^2(y-1) + x(y+1) + (y-1) = 0 \rightarrow \text{Now it is a Quad. Exp}$$

$y \neq 1$

$$D \geq 0$$

$$(y+1)^2 - 4(y-1)(y-1) \geq 0$$

$$A^2 - B^2 \leftarrow (y+1)^2 - (2(y-1))^2 \geq 0$$

$$\{(y+1) + 2(y-1)\} \{(y+1) - 2(y-1)\} \geq 0$$

$$(3y-1)(-y+3) \geq 0$$

$$(3y-1)(y-3) \leq 0$$

$$\frac{1}{3} \leq y \leq 3$$

$$y \in \left[\frac{1}{3}, 3\right] - \{1\}$$

$$1 = \frac{y(y^2 - y + 1)}{y^2 + y + 1}$$

$$y^2 + y + y = y^2 - y + 1$$

$$2y = 1$$

$$y = \frac{1}{2}$$

\Rightarrow Jinda Rhna
 Chahata hanta
 $D \geq 0$ aur

RELATION FUNCTION

$$y = \sqrt{x} \Rightarrow \frac{dy}{dx} = \frac{1}{2\sqrt{x}} \cdot 1$$

$$y = \sqrt{5-x} \Rightarrow \frac{dy}{dx} = \frac{1}{2\sqrt{5-x}} \cdot (-1)$$

Q34) Let $y = \sqrt{x-3} + \sqrt{5-x}$ find \mathbb{R}_+

Dx

$x-3 > 0 \Rightarrow x > 3$
 $5-x > 0 \Rightarrow x < 5$

$x > 3$ $x < 5$

$x \in (3, 5)$

$x \in [3, 5] \leftarrow \text{Domain}$
 Bounded

$$2) \frac{dy}{dx} = \frac{1}{2\sqrt{x-3}} + \frac{1}{2\sqrt{5-x}} \cdot (-1)$$

$$\frac{1}{2\sqrt{x-3}} - \frac{1}{2\sqrt{5-x}} = 0$$

$$y = \sqrt{x^2-3} + \sqrt{5-x^2}$$

$$\frac{1}{2\sqrt{x-3}} = \frac{1}{2\sqrt{5-x}} \Rightarrow \sqrt{x-3} = \sqrt{5-x}$$

$$2) x-3 = 5-x \Rightarrow 2x = 8$$

$$x = 4$$

$$f(3) = \sqrt{3-3} + \sqrt{5-3} = \sqrt{2}$$

$$f(5) = \sqrt{5-3} + \sqrt{5-5} = \sqrt{2}$$

$$f(4) = \sqrt{4-3} + \sqrt{5-4} = 1+1 = 2$$

$$\therefore R \in [1, 2]$$

RELATION FUNCTION

★ Equal & Identical fxn.

$y = f(x)$ & $y = g(x)$ are Identical.

fxn if

A) $D_f = D_g$

B) $R_f = R_g$

C) Socially Eq.
 $f(x) = g(x)$

Q $f(x) = \frac{1}{x}$, $g(x) = \frac{x}{x^2}$ is Eq or not?

\downarrow
 $x \neq 0$

$x \in \mathbb{R} - \{0\}$

$= x \times \frac{1}{x^2}$

$\mathbb{R} \quad \downarrow$
 $x^2 \neq 0$

$\cap x \neq 0$

$x \in \mathbb{R} - \{0\}$

$x \in \mathbb{R} - \{0\}$

$D_f = D_g$

(3) $f(x) = \frac{1}{x} = \frac{x}{x^2} = g(x)$

Graphically $f(x)$ & $g(x)$ are same
 \therefore fxn is Identical

RELATION FUNCTION

Q₂ $f(x) = e^{\ln x}$ & $g(x) = \ln e^x$
 $\xrightarrow{\mathbb{R}}$ $\xrightarrow{\mathbb{R}}$
 $x > 0$
 $x \in (0, \infty)$

$e^x > 0$
 Always
 $x \in \mathbb{R}$
 $x \in (-\infty, \infty)$

$D_f \neq D_g$
 \Rightarrow Not Eqⁿ fun

Q₃ $f(x) = \text{sgn}\{x\}$, $g(x) = \text{sgn}(x^2 - 4x + 5)$
 $\xrightarrow{\mathbb{R}}$ $\xrightarrow{\mathbb{R}}$ Poly

(1) $x \in \mathbb{R}$ | $x \in \mathbb{R}$
 $D_f = D_g$

(2) $\{x\} \in [0, 1]$ | $x^2 - 4x + 5$
 $D = 16 - 20 = -4 < 0$
 $x^2 - 4x + 5 = +ve$

$\hookrightarrow 0 \rightarrow (0, 1)$
 $y = \text{sgn} 0 = 0$ | $y = \text{sgn}(+) = 1$ | $y = \text{sgn}(+ve) = 1$
 $y \in \{0, 1\}$ | $y \in \{1\}$

Not Eqⁿ

RELATION FUNCTION

$$Q \cos^2 x \cdot \cos^2 x = \cos^2 x - \cos^2 x$$

$$Q \tan^2 x \cdot \tan^2 x = \tan^2 x - \tan^2 x$$

$$Q_4 f(x) = \cos^2 x \cdot \cos^2 x \quad g(x) = \cos^2 x - \cos^2 x$$

$$① = \frac{\cos^2 x}{\sin^2 x} \times \cos^2 x$$

$$\begin{array}{c|c} R & R \\ \hline \sin^2 x \neq 0 \\ \sin x \neq 0 \\ x \neq n\pi \end{array}$$

$$x \in \mathbb{R} - \{n\pi\}$$

$$= \frac{\cos^2 x}{(\sin^2 x)} - \cos^2 x$$

$$\sin^2 x \neq 0$$

$$\sin x \neq 0$$

$$x \neq n\pi$$

$$x \in \mathbb{R} - \{n\pi\}$$

$$D_f = D_g$$

② graphically same
 \Rightarrow Eq of x

$$Q_5 f(x) = \sqrt{\frac{1 - \cos 2x}{2}}, g(x) = \sin x$$

$$① \frac{1 - \cos 2x}{2} \geq 0$$

$$1 - \cos 2x \geq 0$$

$$\cos 2x \leq 1$$

Always True
 $x \in \mathbb{R}$

Not Eql.

$$D_f = D_g$$

$$② f(x) = \sqrt{\frac{2 \sin^2 x}{2}} = |\sin x| \quad g(x) = \sin x$$

$$(3) R_f \neq R_g$$

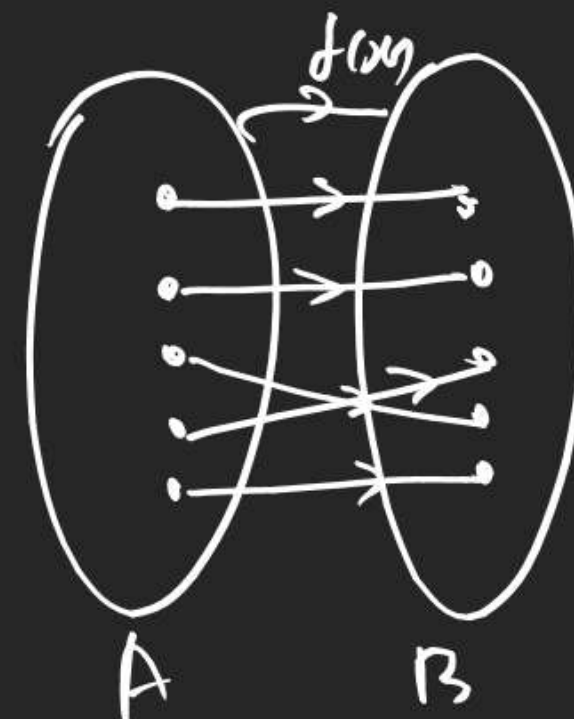
graphically same
Identical

One to one + Onto = Bijection.

RELATION FUNCTION

A) One to One

If each element of A is associated with single element of B then 1-2-1
 $\{1 \text{ teen } 1 \text{ ko Lage}\}$



(B) Many to One

If 2 or more elements of A are associated with single element of B then it is M21
 $\{2 \text{ ya } 4 \text{ adhik teen } 1 \text{ ko Lageyenge}\}$



2 x 4
 M21
 Samey
 Value

RELATION FUNCTION

(C) On to fxn

lathen

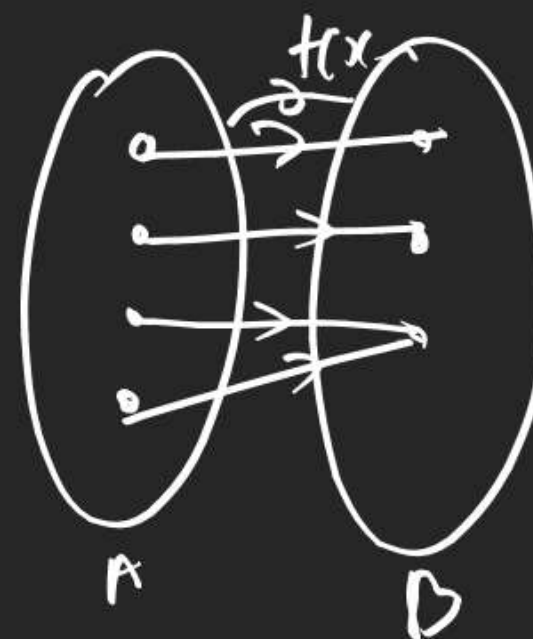
onto \leftarrow Range = Codomain

{ B me Sab ko Teer Lga ho }

(D) Into fxn lathen

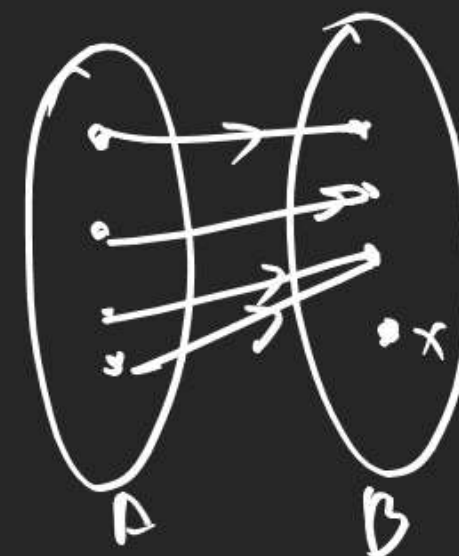
Into \leftarrow Range $<$ Codomain

{ B me Sab ko Teer nahi Lga }



4×2

M21 + Onto



M21 + Into

RELATION FUNCTION

How to check kinds of f.xn.

M1

Using Mapping

When f.xn has following nature

A) $f: \mathbb{N} \rightarrow \mathbb{N}$

B) $f: \mathbb{N} \rightarrow \mathbb{I}$

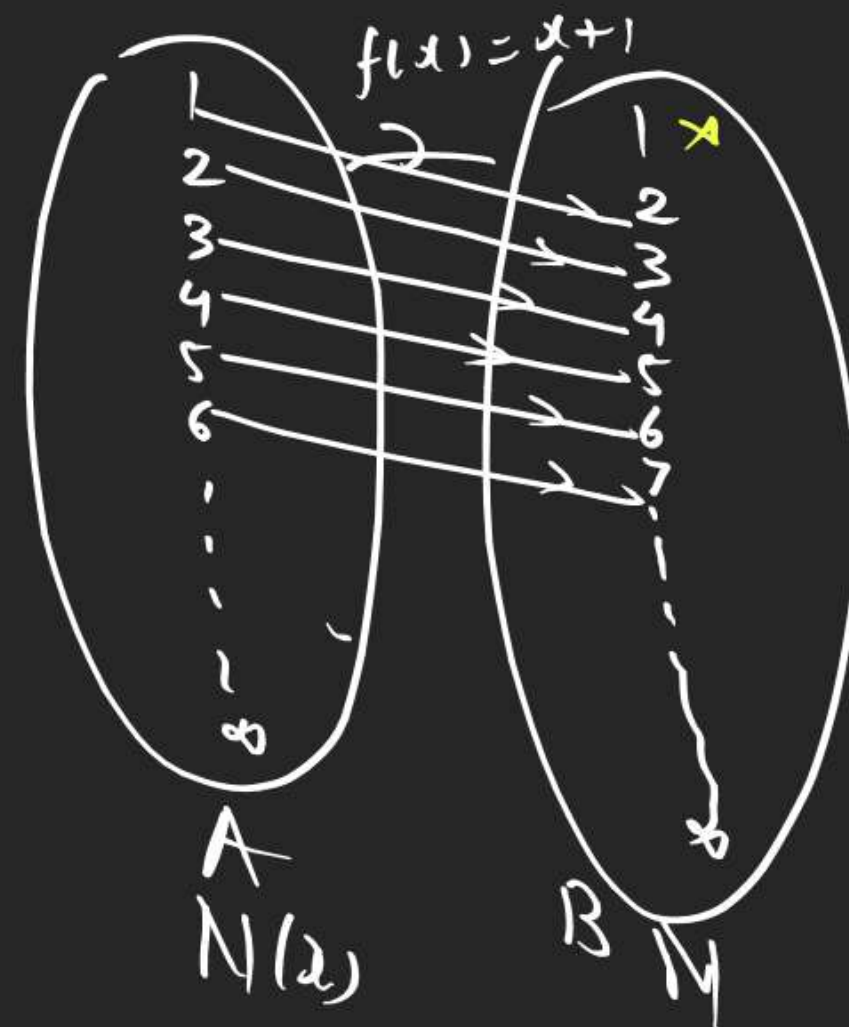
C) $f: \mathbb{I} \rightarrow \mathbb{I}$

D) $f: \mathbb{R} \rightarrow \mathbb{R}$ (difficult)
Qs

$$f: A \rightarrow B, y = f(x)$$

Raja.

Q $f: \overset{\text{Dom}}{\mathbb{N}} \rightarrow \overset{\text{Cod}}{\mathbb{N}} f(x) = x+1$ Nature?



1 2 1
+
Into