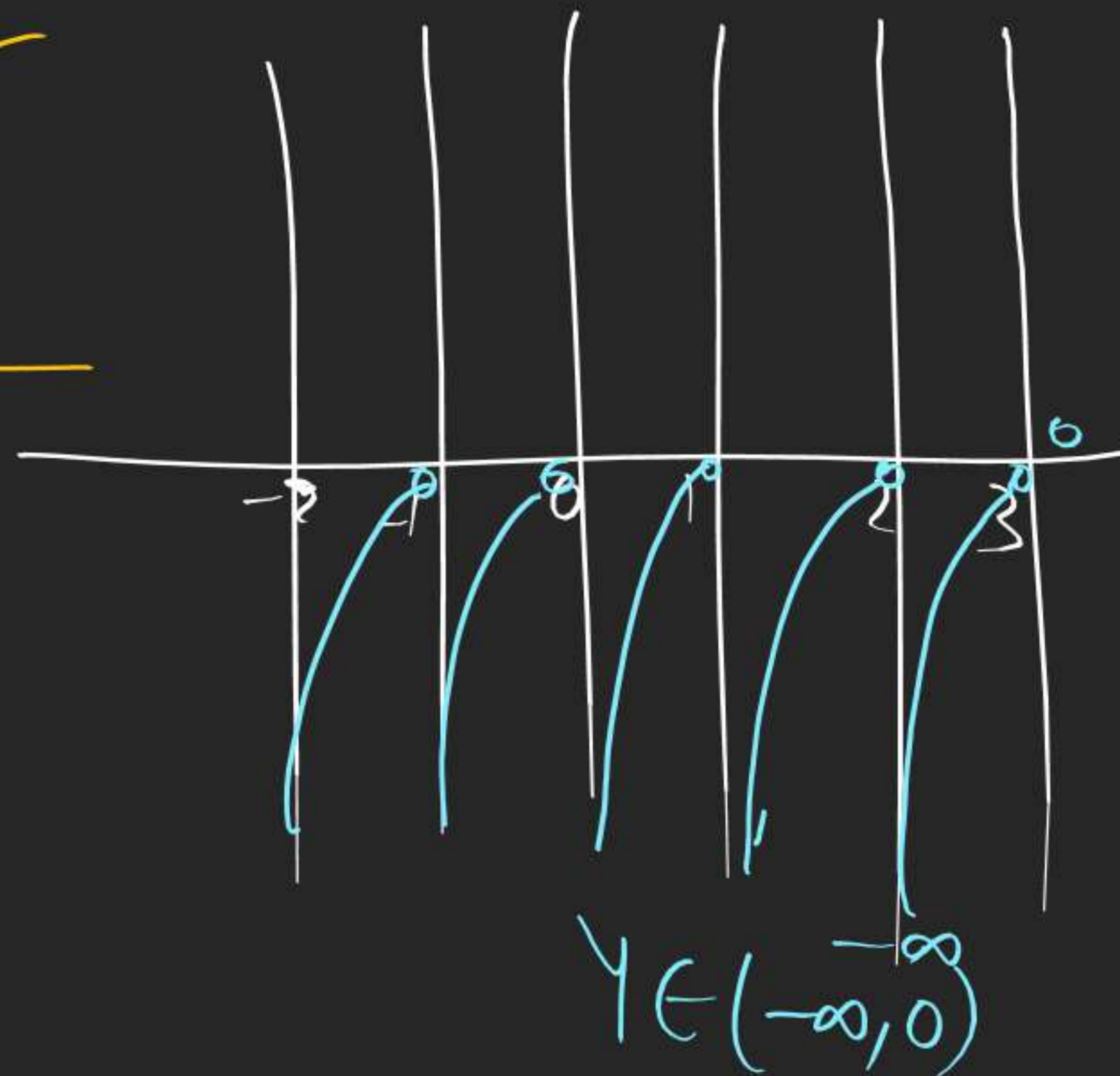
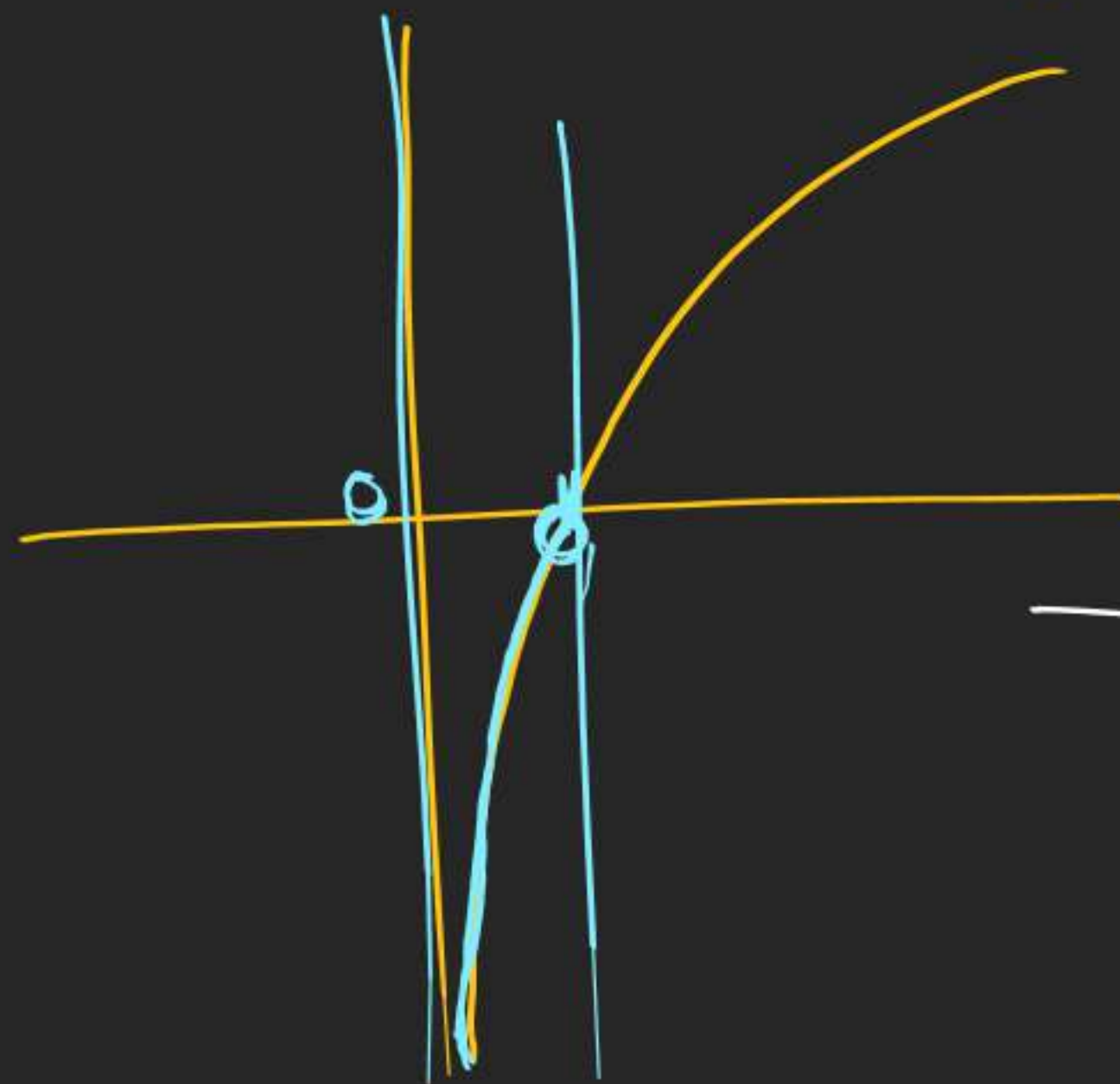
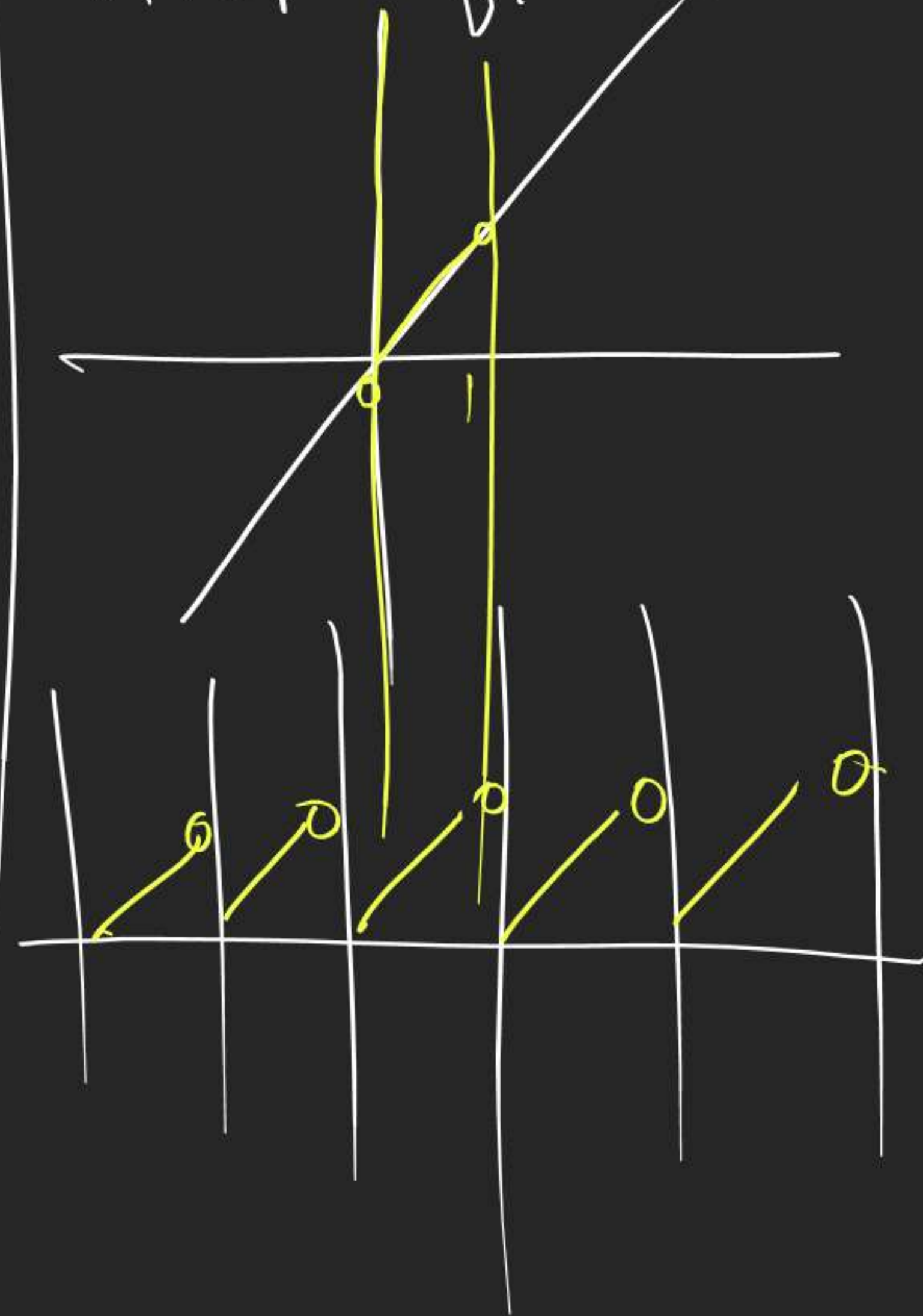


# RELATION FUNCTION

Q Graph of  $y = \log\{x\}$

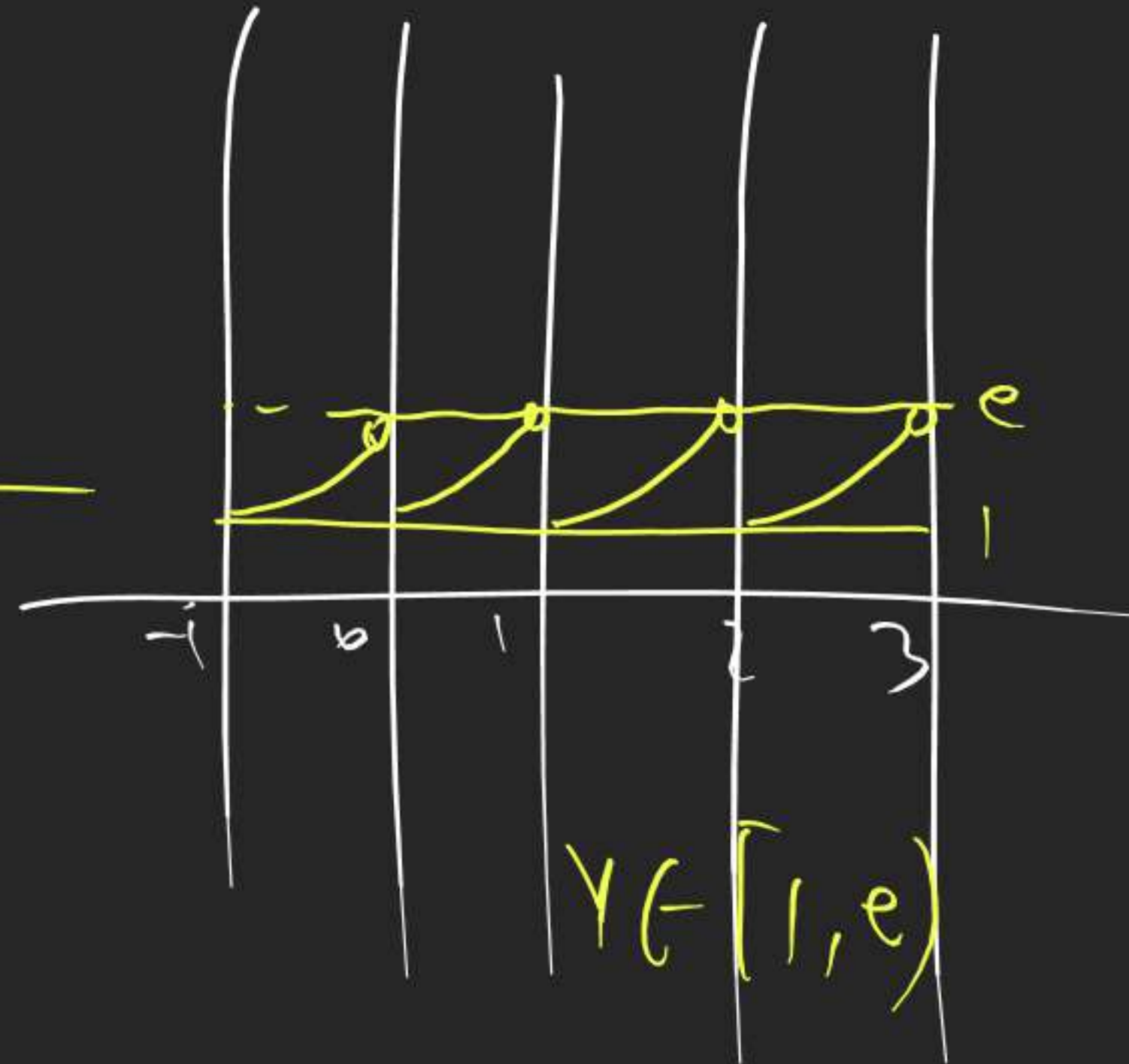
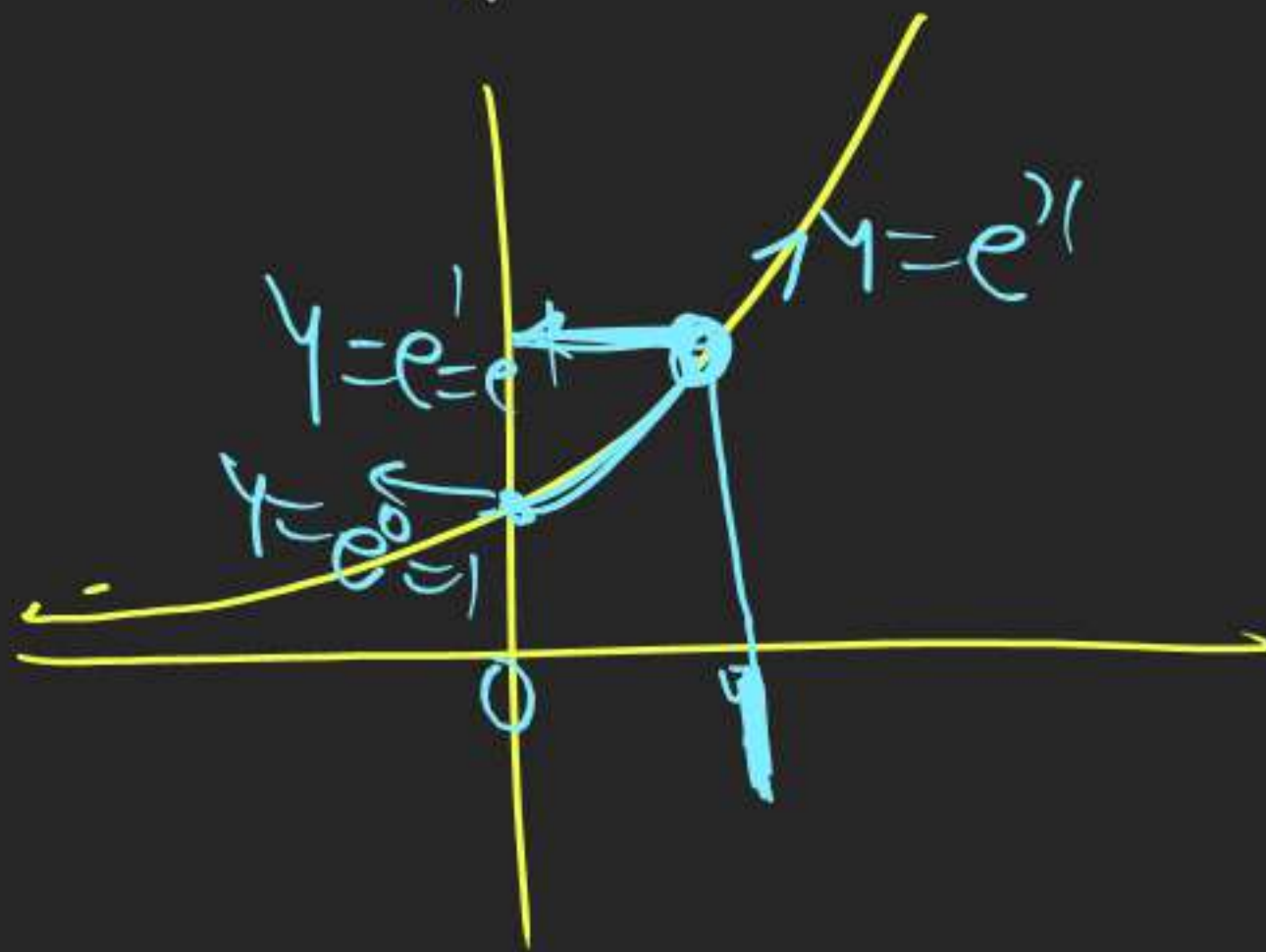
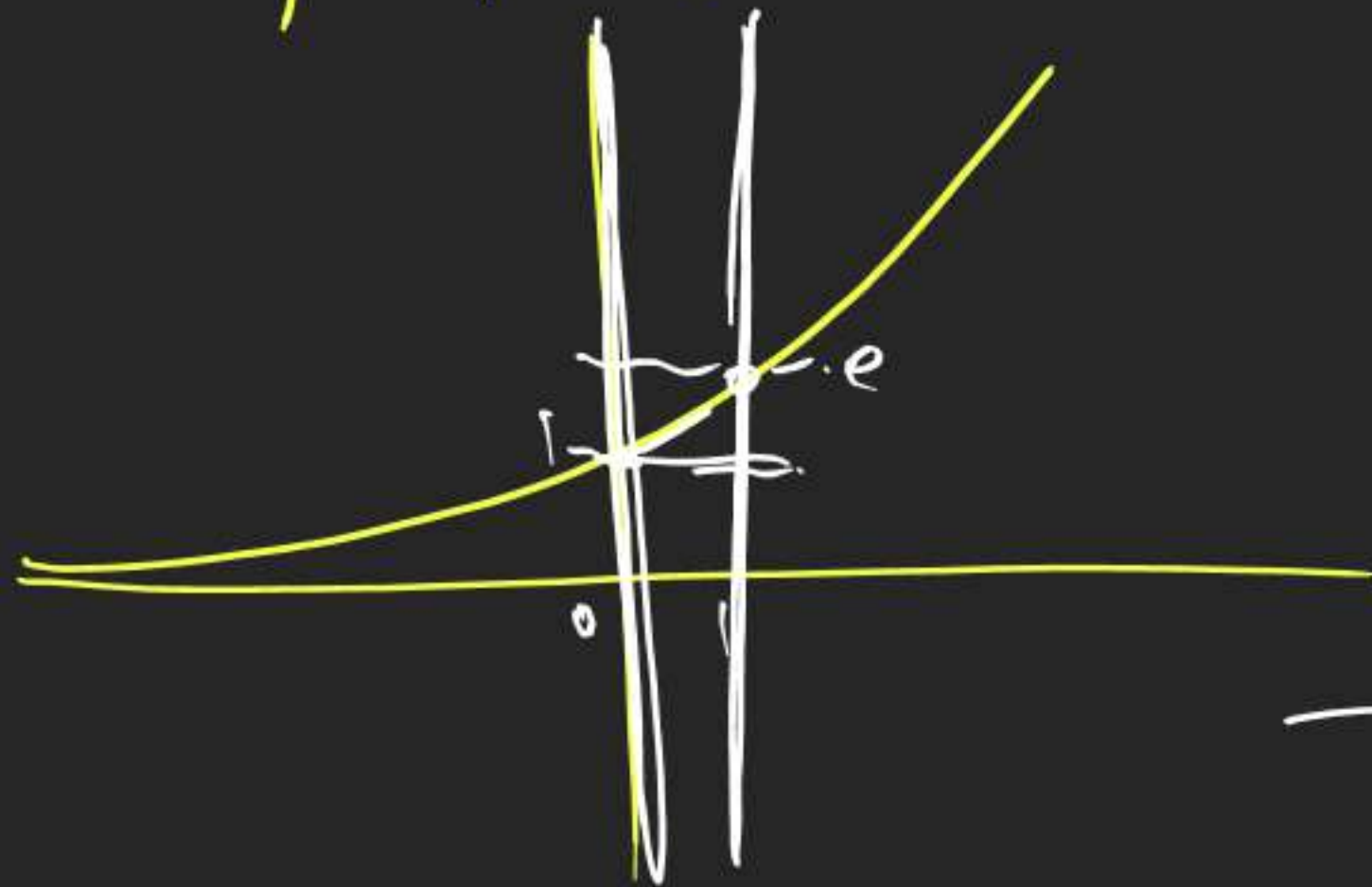


Graph of  $y = \{x\}$



# RELATION FUNCTION

$$Q \quad y = e^{\{x\}}$$



$$D_f \rightarrow x \in \mathbb{R}$$



# RELATION FUNCTION

Q find Domain & Range of  $y = \frac{x - [x]}{(-[x]) + x}$

$$y = \frac{\{x\}}{1 + \{x\}} = \{x\} \times \frac{1}{\{x\} + 1}$$

$x \in \mathbb{R}$

$$\{x\} + 1 \neq 0$$

$$\boxed{\{x\} \neq -1}$$

$$\underline{x \in \mathbb{R}}$$

$$y = 1 - \frac{1}{1 + \{x\}}$$

$$y \in \left[0, \frac{1}{2}\right)$$

$$0 \leq \{x\} < 1$$

$$1 \leq 1 + \{x\} < 2$$

$$\frac{1}{1} \geq \frac{1}{1 + \{x\}} > \frac{1}{2}$$

$$0 \leq \left(1 - \frac{1}{1 + \{x\}}\right) < \frac{1}{2} \leq -1 \leq \frac{-1}{1 + \{x\}} < -\frac{1}{2}$$

$$y = \frac{\{x\}}{1 + \{x\}}$$

$$= \frac{(\{x\} + 1) - 1}{(\{x\} + 1)}$$

$$y = 1 - \frac{1}{1 + \{x\}}$$

JUST H



## RELATION FUNCTION

$$y = \frac{\{x\}}{1+\{x\}} = \frac{(\{x\}+1)-1}{(\{x\}+1)} = 1 - \frac{1}{1+\{x\}}$$

$$\cancel{1} + \cancel{1} + \cancel{1} + \cancel{1}$$

$$0 \leq \{x\} < 1$$

$$1 \leq 1 + \{x\} < 2$$

$$1 > \frac{1}{1+\{x\}} > \frac{1}{2}$$

$$-1 \leq -\frac{1}{1+\{x\}} < -\frac{1}{2}$$

$$0 \leq 1 - \frac{1}{1+\{x\}} < \frac{1}{2}$$

$$0 \leq y < \frac{1}{2}$$

$$\text{R.A. } y \in \left(0, \frac{1}{2}\right)$$



# RELATION FUNCTION

$x, [x]$  &  $\{x\}$  Based Qs

Q If  $\{x\} = x + [x]$  find  $x = ?$

① Convert  $x$  into  $\{x\} + [x]$

$$\{x\} = \{x\} + [x] + [x]$$

$$3\{x\} = 2[x]$$

② find value of  $\{x\}$  & put it in  $[0, 1)$

$$\boxed{\{x\} = \frac{2[x]}{3}} \Rightarrow$$

$$0 \leq \frac{2[x]}{3} < 1$$

$$0 \leq [x] < \frac{3}{2}$$

3) Read it & find  $[x]$  then find  $\{x\}$ .

then add them.

$$0 \leq [x] < \frac{3}{2}$$

$$\begin{array}{l} [x] = 0 \\ \{x\} = \frac{2 \times 0}{3} \\ = 0 \end{array}$$

$$x = 0$$

$$x \in \left\{0, \frac{5}{8}\right\}$$

$$\begin{array}{l} [x] = 1 \\ \{x\} = \frac{2 \times 1}{3} \\ = \frac{2}{3} \end{array}$$

$$x = 1 + \frac{2}{3} = \frac{5}{3}$$



# RELATION FUNCTION

Q If  $2x + 3\{x\} = 4[x] - 2$  find  $x$ ?

$$\textcircled{1} \quad 2\{x\} + 2[x] + 3\{x\} = 4[x] - 2$$

$$5\{x\} = 2[x] - 2$$

$$\Rightarrow \boxed{\{x\} = \frac{2([x] - 1)}{5}}$$

$\textcircled{2}$

$$0 \leq \frac{2([x] - 1)}{5} < 1$$

$$0 \leq [x] - 1 < 5$$

$$1 \leq [x] < 7$$

$$1 \leq [x] < \frac{7}{2} \quad \begin{array}{|c|c|c|c|} \hline & & & \\ \hline 1 & & & 3.5 \\ \hline \end{array}$$

$$[x] = 1$$

$$\{x\} = \frac{2(1-1)}{5}$$

$$= 0$$

$$x = 1 + 0$$

$$= 1$$

$$x \in \left\{1, \frac{12}{5}, \frac{19}{5}\right\}$$

$$[x] = 2$$

$$\{x\} = \frac{2(2-1)}{5}$$

$$= \frac{2}{5}$$

$$x = 2 + \frac{2}{5}$$

$$= \frac{12}{5}$$

$$[x] = 3$$

$$\{x\} = \frac{2(3-1)}{5}$$

$$= \frac{4}{5}$$

$$x = 3 + \frac{4}{5}$$

$$= \frac{19}{5}$$



Q If  $\lceil x \rceil \{x\} = 1$  find sol. set?  $\rightarrow \{x\} = \frac{1}{\lceil x \rceil} = \frac{1}{\oplus}$

Ans  $\{x\} = \frac{1}{\lceil x \rceil}$

$$x - \lceil x \rceil = \frac{1}{\lceil x \rceil}$$

$$\lceil x \rceil + \frac{1}{\lceil x \rceil} = 1$$

$\downarrow$   $\{0, 1\}$   $\oplus$   $\oplus$

$\downarrow$   $\oplus$   $\oplus$   $\oplus$

$\downarrow$   $\oplus$   $\oplus$   $\oplus$

$$x = \lceil x \rceil + \frac{1}{\lceil x \rceil} > 2$$


Sol set:  $(2, \infty)$

$$\lceil x \rceil = \frac{1}{\lceil x \rceil}$$

$$\lceil x \rceil^2 = 1$$

$$\lceil x \rceil = 1$$

Q No of sol. of eqn  $e^{2x} + e^x - 2 = 0$   $\left[ \begin{matrix} \{x^2 + 10x + 11\} \\ \downarrow \\ [0, 1) \\ = \emptyset \end{matrix} \right] = ?$



$$e^{2x} + e^x - 2 = 0$$

$$(e^x)^2 + e^x - 2 = 0$$

$$(e^x + 2)(e^x - 1) = 0$$

$$\begin{matrix} e^x = -2 & \& e^x = 1 = e^0 \\ \textcircled{\times} & & x = 0 \end{matrix}$$

$$x = \underline{\underline{\{0\}}}$$



# 11) Signum fcn.

A) Rep by  $y = \text{sgn}(x)$

$$(B) \text{sgn}(x) = \begin{cases} \frac{|x|}{x} & x \neq 0 \\ 0 & x = 0 \end{cases}$$

Defined fcn

$$\text{sgn}(x) = \begin{cases} \frac{x}{x} = 1 & x > 0 \\ -\frac{x}{x} = -1 & x < 0 \\ 0 & x = 0 \end{cases}$$

$$y = \text{sgn}(x) = \begin{cases} 1 & x > 0 \\ -1 & x < 0 \\ 0 & x = 0 \end{cases}$$

$$\text{sgn}(3) = 1$$

$$\text{sgn}(-1.8) = -1$$

$$\text{sgn}(0) = 0$$



Q  $y = \text{Sgn}\{x\}$  Range? <sup>= Answer</sup>

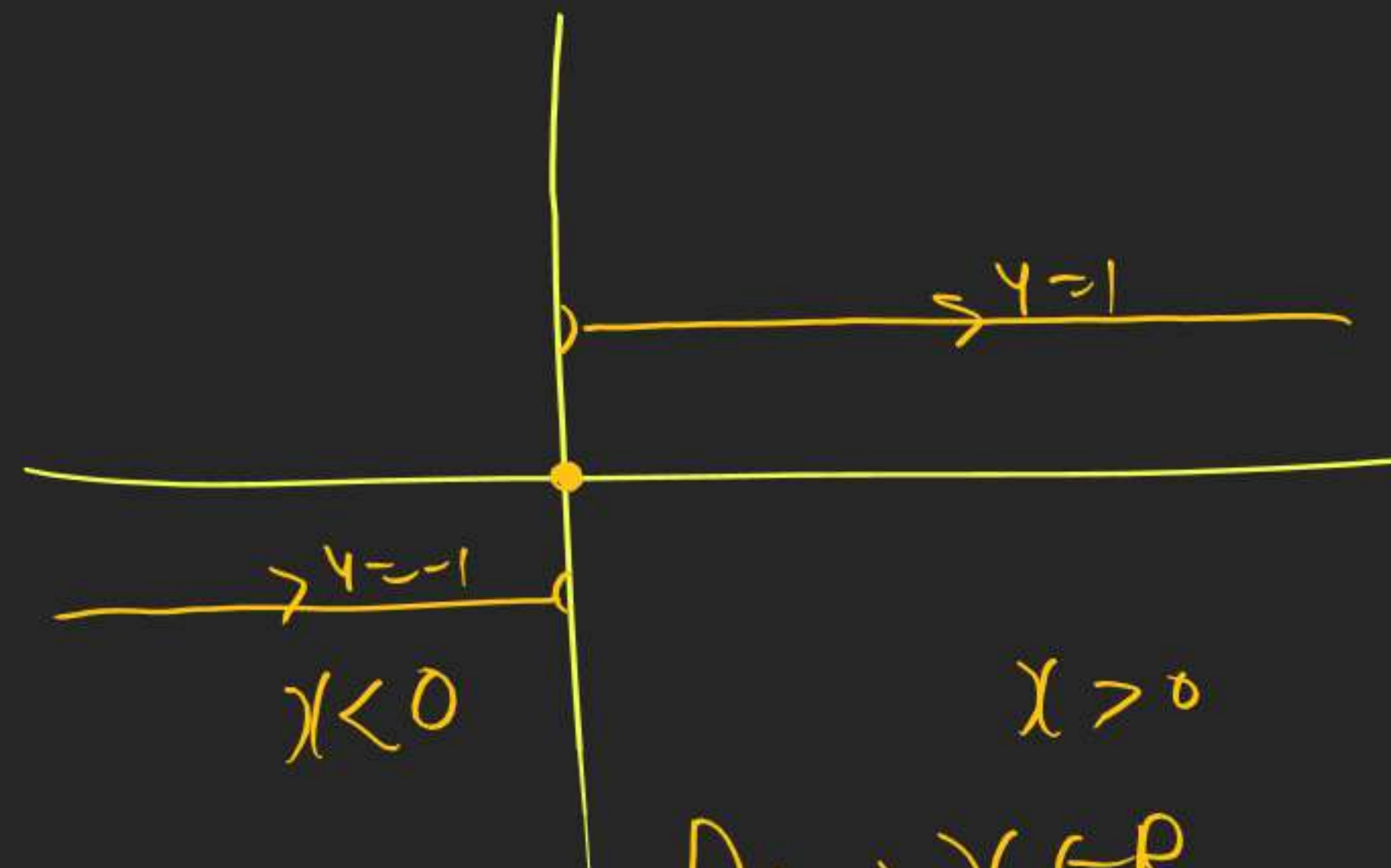
$= \text{Sgn}[0, 1)$



$= \text{Sgn } 0, \text{Sgn}(\underline{0, 1})^{\oplus}$

$R_f = y = \{0, 1\}$

$y = \text{Sgn } x = \begin{cases} 1 & x > 0 \\ 0 & x = 0 \\ -1 & x < 0 \end{cases}$



$D_f \rightarrow x \in \mathbb{R}$

$R_f \rightarrow \{-1, 0, 1\}$



Q  $y = \text{Sgn}(e^x)$  find  $R_f$ ?



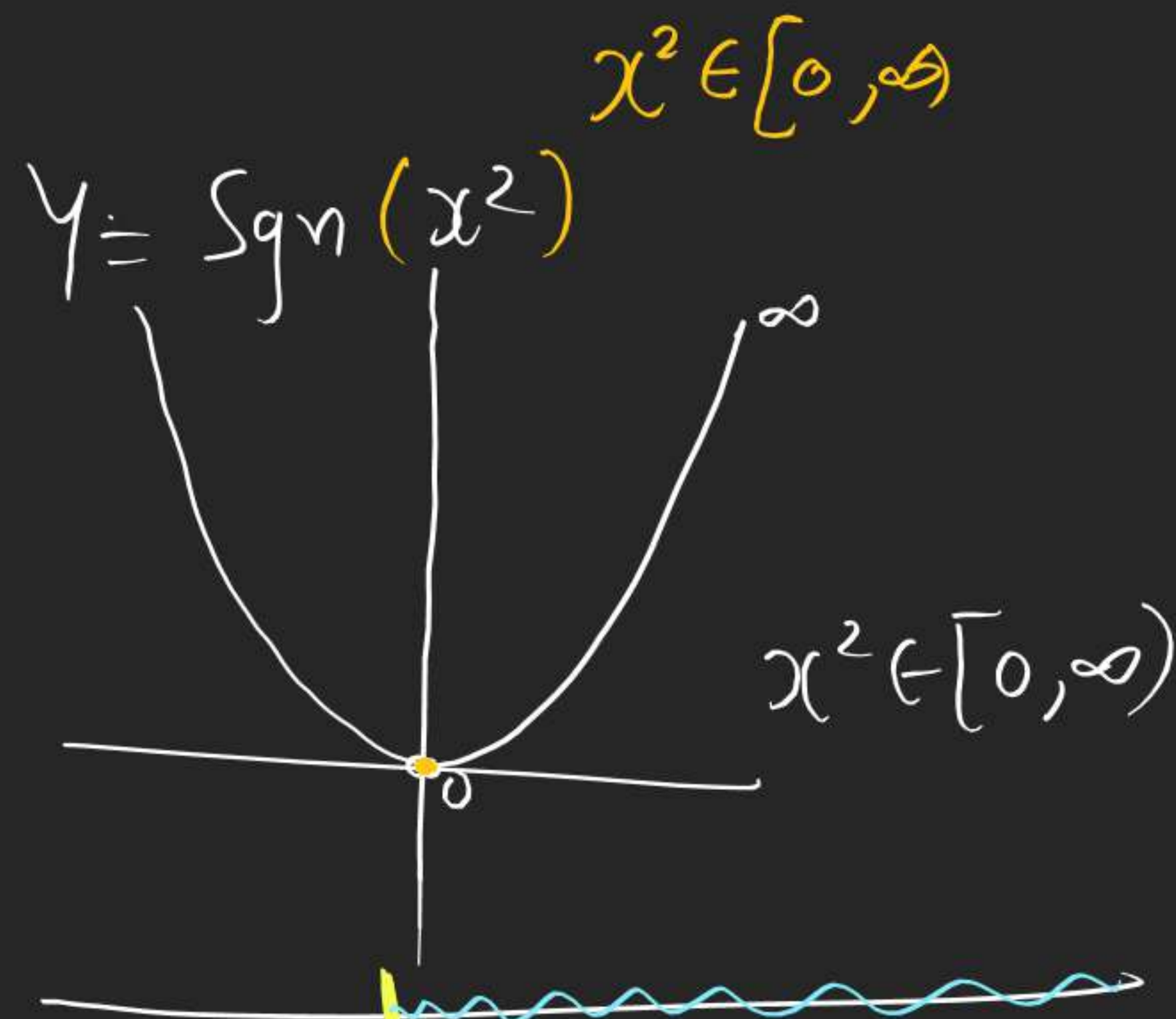
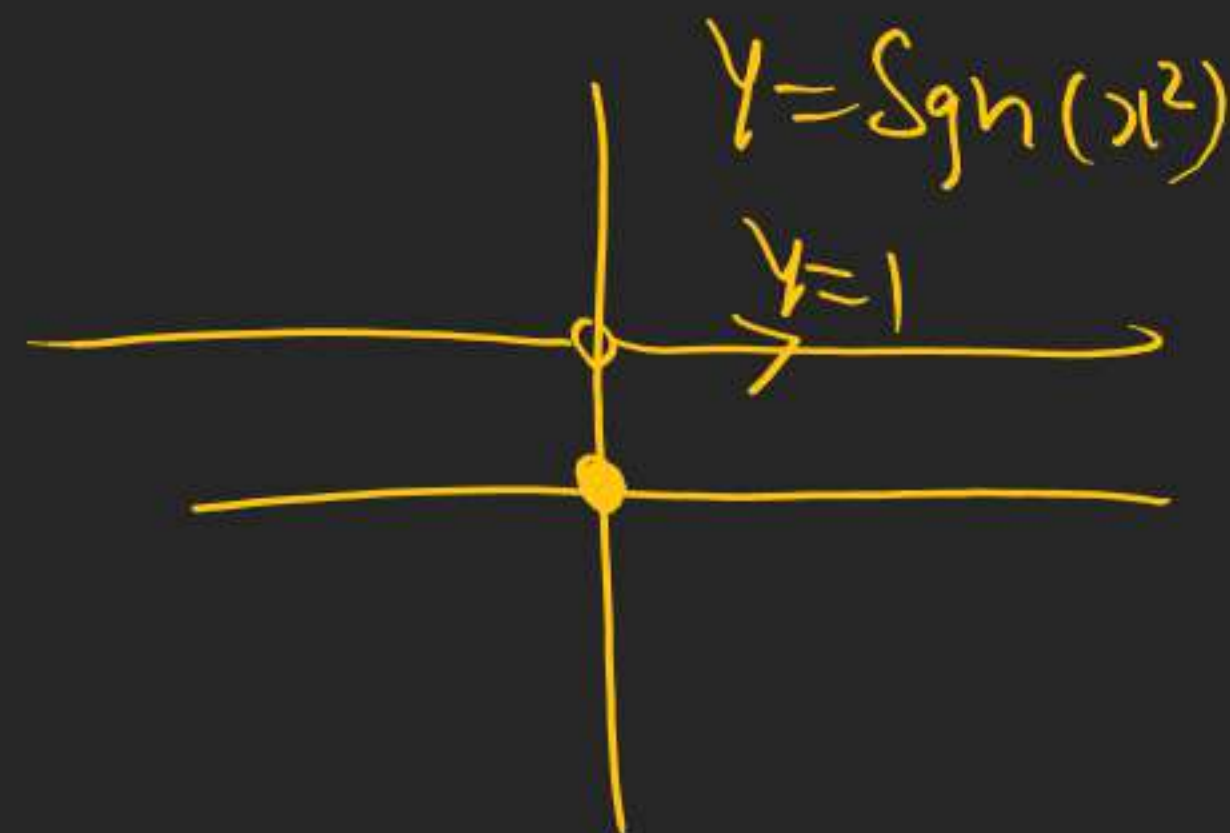
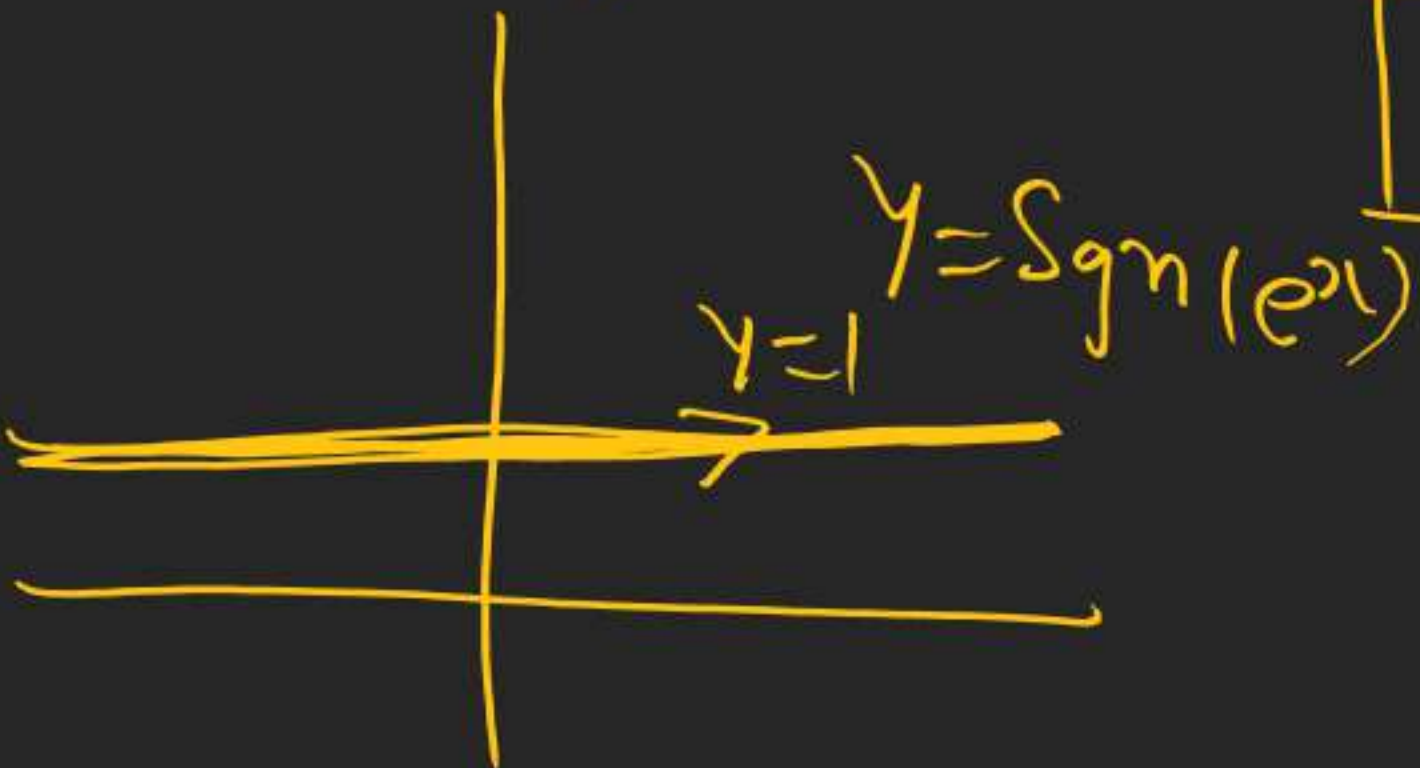
$$e^x > 0$$

$$e^x \in (0, \infty)$$

$$y = \text{Sgn}(0 \oplus)$$

$$y = 1$$

$$R_f \ni y \in \{1\}$$



$$\begin{aligned} y &= \text{Sgn}[0, \infty) \\ &= \text{Sgn } 0, \text{Sgn}(0, \infty) \\ &= 0, 1 \\ \therefore R_f &\in \{0, 1\} \end{aligned}$$



# RELATION FUNCTION

17Qs

Basic  
+  
SrDrd

3, 10, 12, 15, 16

DPP 1

Tough / Adv

Q17

Domain

$$\textcircled{1} f(x) = \frac{x^2 - 5x + 3}{x^2 - 1} = x^3 - 5x + 3 \times \frac{1}{x^2 - 1}$$

Poly  
 $x \in \mathbb{R}$

$$x^2 - 1 \neq 0$$

$$x^2 \neq 1$$

$$x \neq \pm 1$$

$$x \in \mathbb{R} - \{-1, 1\}$$



$$x \in \mathbb{R} - \{-1, 1\}$$

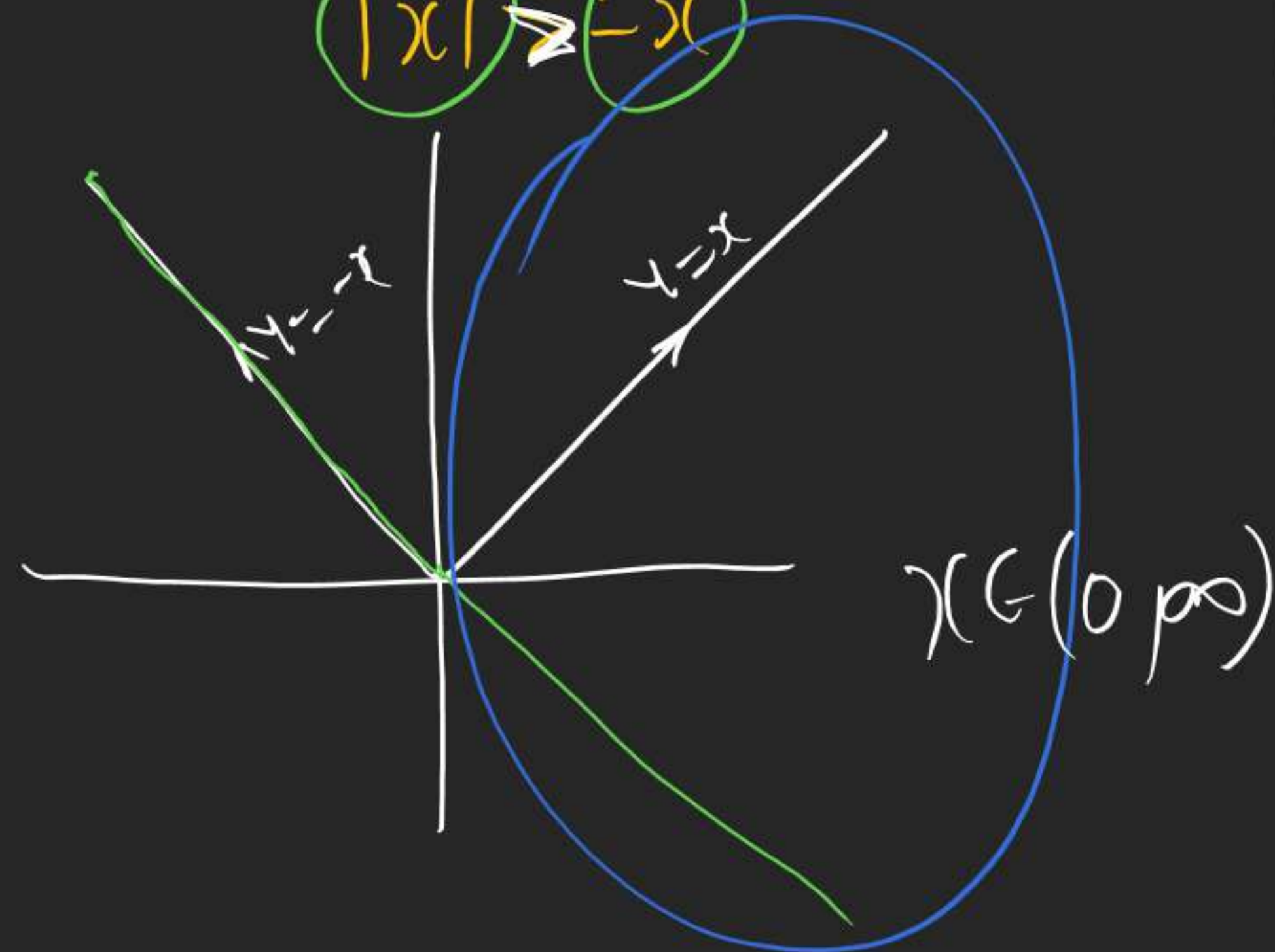


# RELATION FUNCTION


Q (ii)  $y = \frac{1}{\sqrt{x+|x|}}$  Mains.

$$|x| + x > 0$$

$$|x| \Rightarrow -x$$



(iii)  $y = e^{\underbrace{x + \sin x}_{\substack{\text{Constant} \\ x \in \mathbb{R}}}}$  Q5) Df

2  $x + \sin x \in \mathbb{R}$  Df  
 $\downarrow$    
 $\mathbb{R} \cap \mathbb{R}$   
 $x \in \mathbb{R}$



$$(iv) \quad y = \frac{1}{\log_{10} \frac{1}{1-x}} + \sqrt{x+2}$$

$$= \log_{10} 10 + \sqrt{x+2}$$

$$1-x > 0 \Rightarrow x < 1$$

$$1-x \neq 1 \Rightarrow x \neq 0$$

$$10 > 0 \checkmark$$

$$x \in (-\infty, 0) \cup (0, 1)$$

$$x+2 \geq 0$$

$$x \geq -2$$

$$x \in (-2, 1) - \{0\}$$

$$(v) \quad y = \log_x \left( \log_2 \left( \frac{1}{x - 1/2} \right) \right) \quad \text{---} \textcircled{+} \textcircled{+}$$

$$x > 0$$

$$x \neq 1$$

$$\log_2 \left( \frac{1}{x - 1/2} \right) > 0$$

$$\frac{1}{x - 1/2} > 1$$

$$2 > 0$$

$$2 \neq 1$$

$$\frac{1}{x - 1/2} - 1 > 0$$

$$1 - (x - 1/2) > 0$$

$$\frac{1}{(x - 1/2)} > 0$$

Solve



## RELATION FUNCTION

$$(VI) \quad y = \sqrt{3 - 2^x - 2^{1-x}}$$

$$3 - 2^x - \frac{2}{2^x} \geq 0$$

$$3 \cdot 2^x - (2^x)^2 - 2 \geq 0$$

$$3t - t^2 - 2 \geq 0$$

$$t^2 - 3t + 2 \leq 0$$

$$(t-1)(t-2) \leq 0$$

$$1 \leq t \leq 2$$

$$1 \leq 2^x \leq 2^1$$

$$2^0 \leq 2^x \leq 2^1$$

$$0 \leq x \leq 1$$

$$(VII) \quad y = \sqrt{1 - \sqrt{1-x^2}}$$

$$1 - \sqrt{1-x^2} \geq 0$$

$$1 \geq \sqrt{1-x^2}$$

$$\text{sq}^n$$

$$1 \geq 1 - x^2$$

$$x^2 \geq 0$$

$$x \in \mathbb{R}$$

$$1 - x^2 \geq 0$$

$$x^2 - 1 \leq 0$$

$$(x-1)(x+1) \leq 0$$

BHALLA

$$-1 \leq x \leq 1$$

$$x \in [-1, 1]$$



## RELATION FUNCTION

$$(VIII) y = (x^2 + x + 1)^{3/2} \quad \boxed{a^{3/2} = a\sqrt{a}}$$

$$= \frac{1}{(x^2 + x + 1)^{3/2}}$$

$$= \frac{1}{(x^2 + x + 1)\sqrt{x^2 + x + 1}} = \frac{1}{(x^2 + x + 1)} \times \frac{1}{\sqrt{x^2 + x + 1}}$$

$$x^2 + x + 1 \neq 0$$

$$D = -3 \quad a = 1$$

True for all  $x \in \mathbb{R}$

$$x^2 + x + 1 > 0$$

$$D = -3 \quad a = 1$$

$x^2 + x + 1$  is +ve for all  $x$

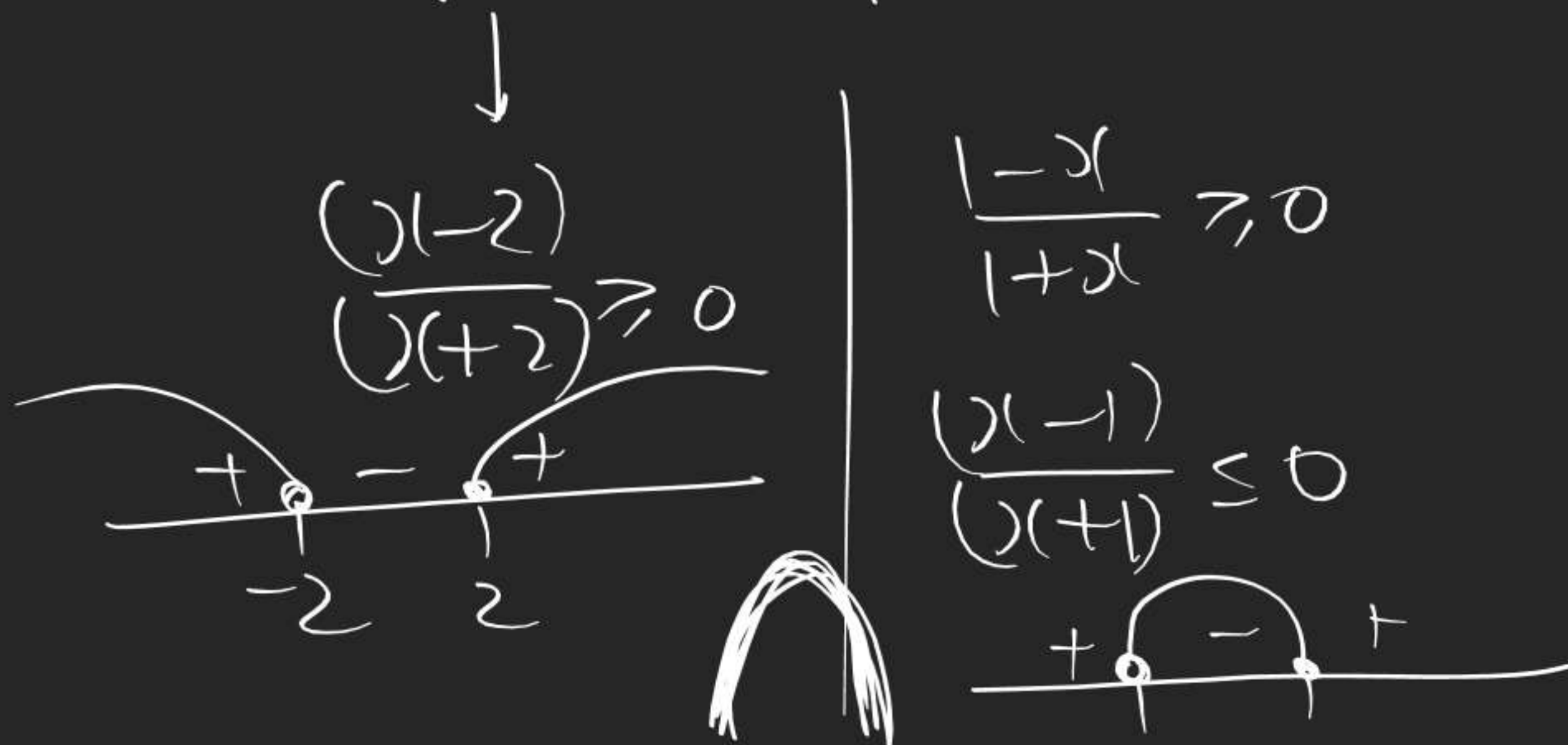
$$\mathbb{R} \quad \underline{\underline{x \in \mathbb{R}}}$$



# RELATION FUNCTION

$$(1x) \quad y = \sqrt{\frac{x-2}{x+2}} + \sqrt{\frac{1-x}{1+x}}$$

$$(x) \quad y = \sqrt{\tan x - \tan^2 x}$$



$$\tan x - \tan^2 x \geq 0$$

$$\Rightarrow \tan^2 x - \tan x \leq 0$$

$$\Rightarrow (\tan x)(\tan x - 1) \leq 0$$

$$0 \leq \tan x \leq 1$$

$$\tan 0 \leq \tan x \leq \tan \frac{\pi}{4}$$

Trigo  $0 \leq x \leq \frac{\pi}{4}$

$$x \in \left[ n\pi + 0, n\pi + \frac{\pi}{4} \right]$$



# RELATION FUNCTION

$$x1) y = \frac{1}{\sqrt{1-\cos x}}$$



$$1 - \cos x > 0$$

$$\cos x \neq 1$$

$$x \neq 2n\pi$$

$$x \in \mathbb{R} - \{2n\pi\}$$

$$\begin{aligned} \cos x &= 1 \\ x &= \text{even } n\pi \\ x &= 2n\pi \end{aligned}$$

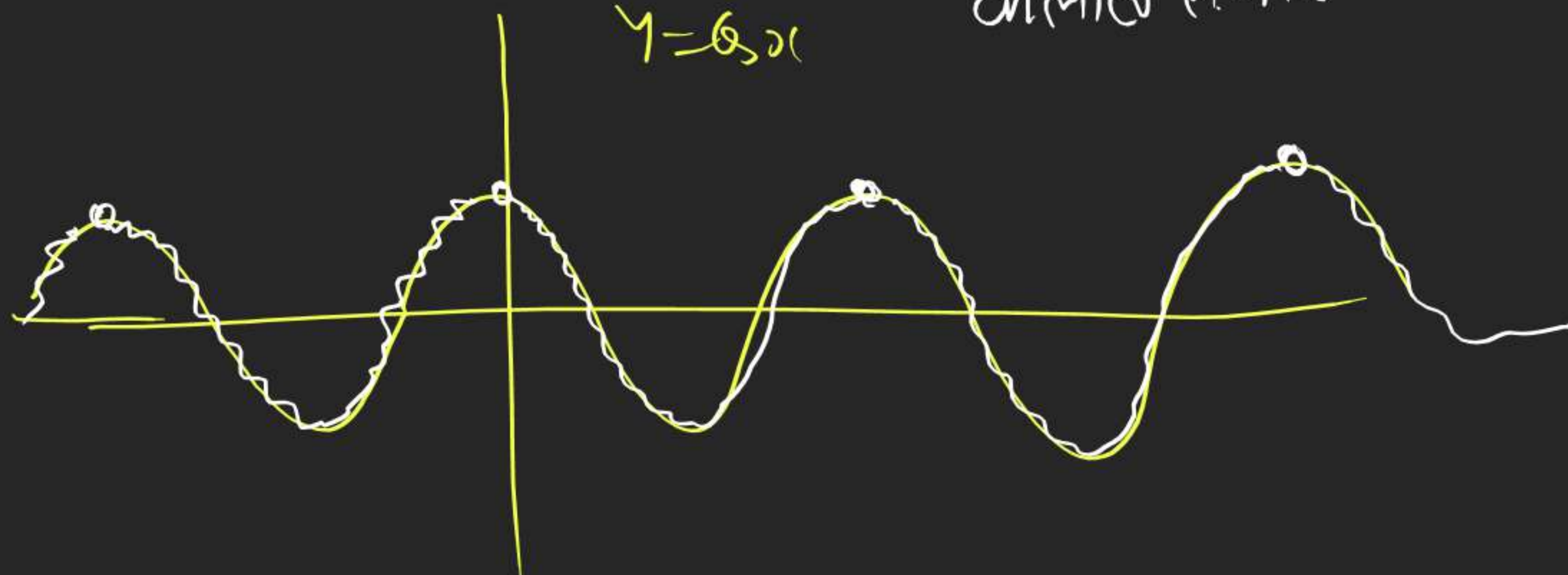
$$12) \rightarrow (0, 1] \cup [4, 5)$$

$$13) (2, 3)$$

$$\cos x < 1 \rightarrow \cos x, 1 \text{ है कम}$$

आलावा लेना है

$$y = \cos x$$





# RELATION FUNCTION

in  $y = \sin x$  का graph

$$= n\pi + (-1)^n x$$

$$0\pi + (-1)^0 x \Rightarrow y = x$$

$$\pi + (-1)^1 x = \pi - x$$

$$2\pi + (-1)^2 x = \boxed{2\pi + x}$$

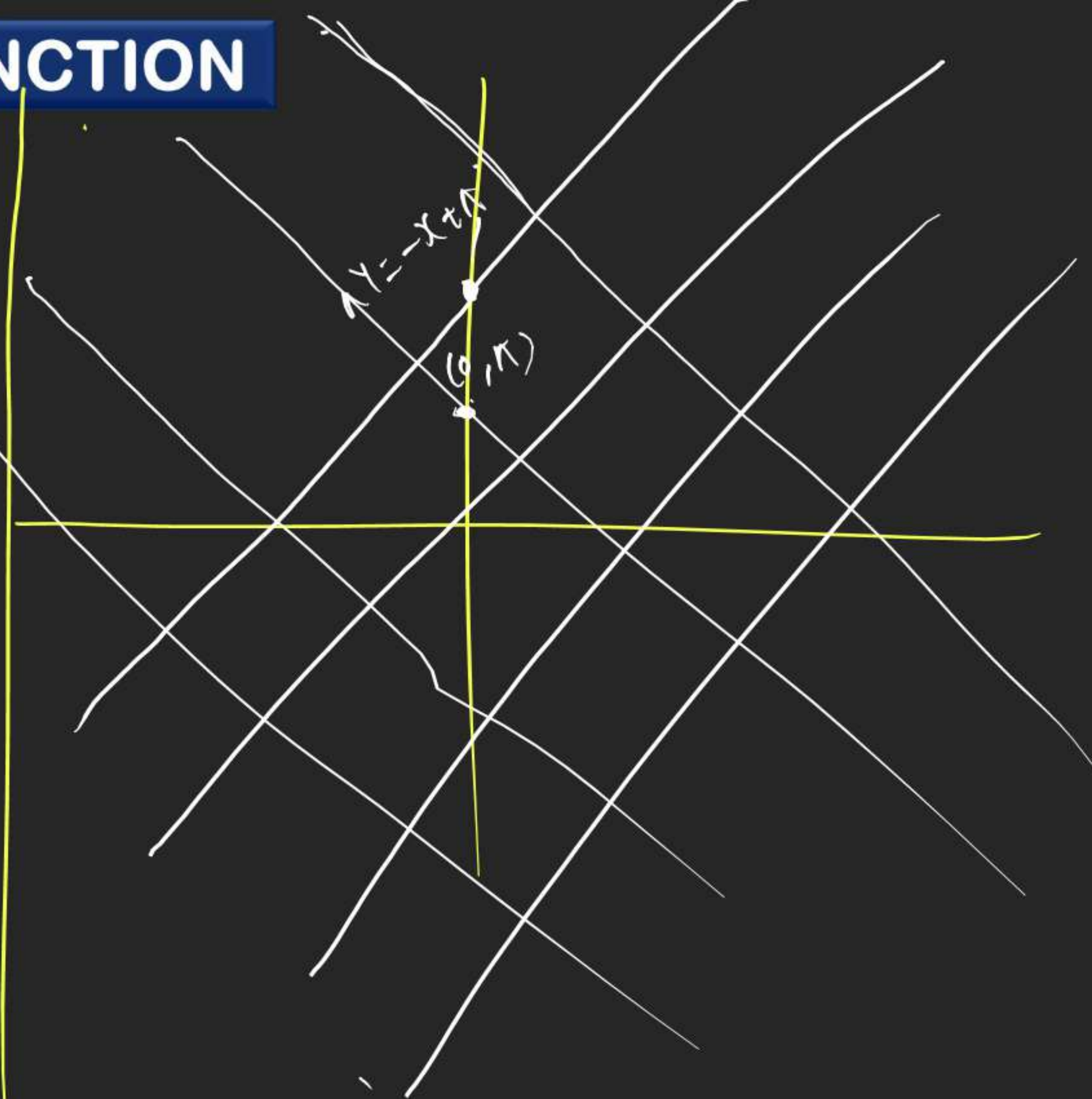
$$= 3\pi - x$$

(Trig के graph में कहा था)  
 1<sup>st</sup> कोप्य दिखाती  
 11<sup>th</sup> कोaching दी गी  
 रहे ले-1

$$y = -x + \pi$$

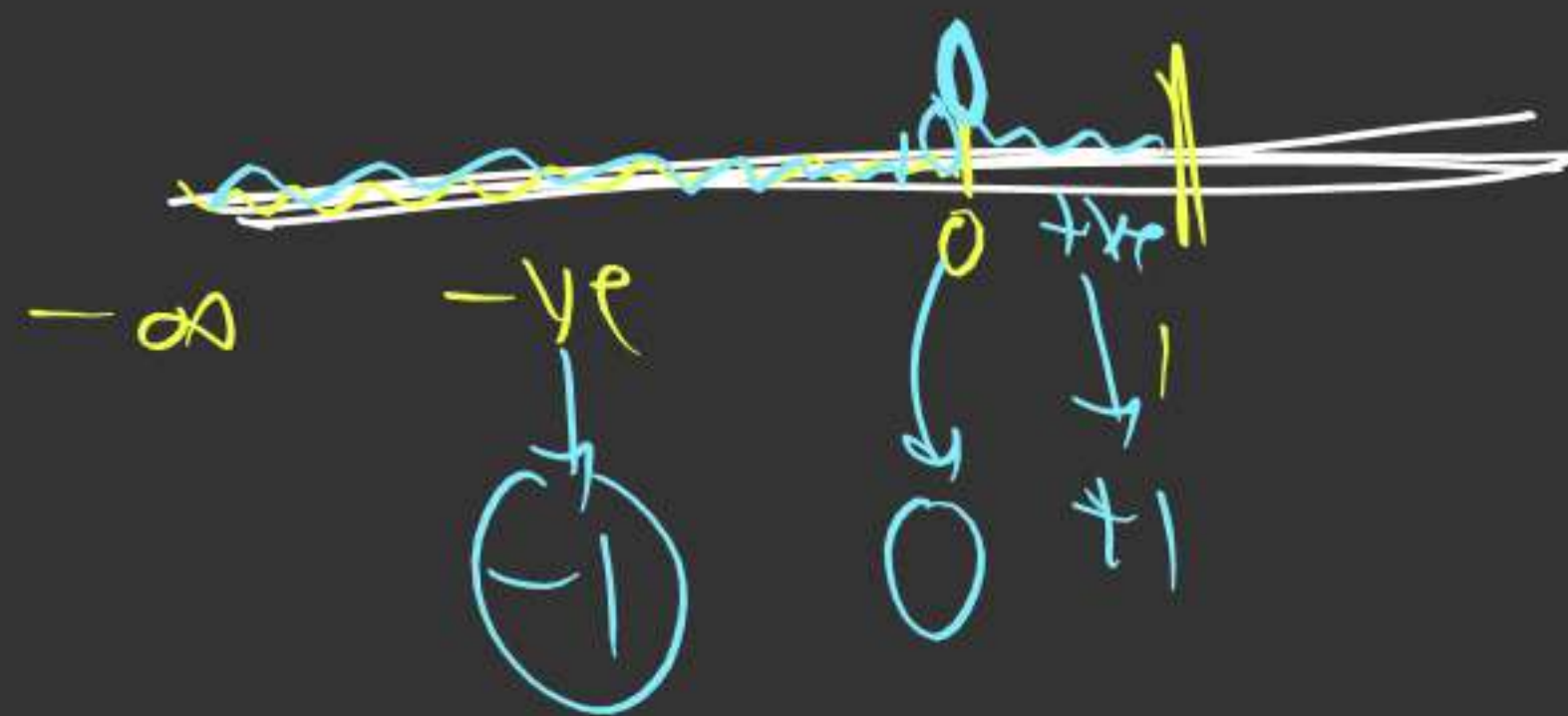
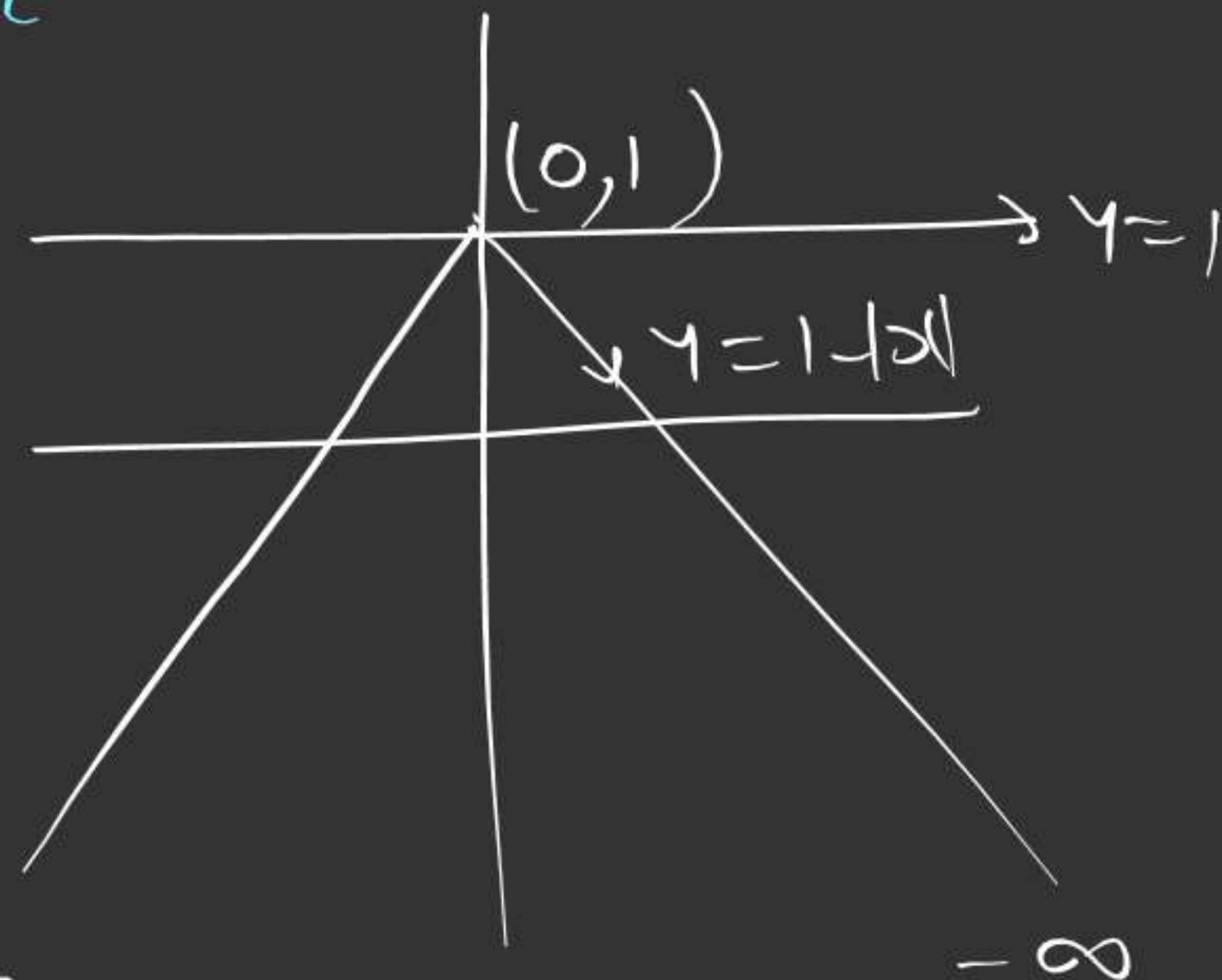
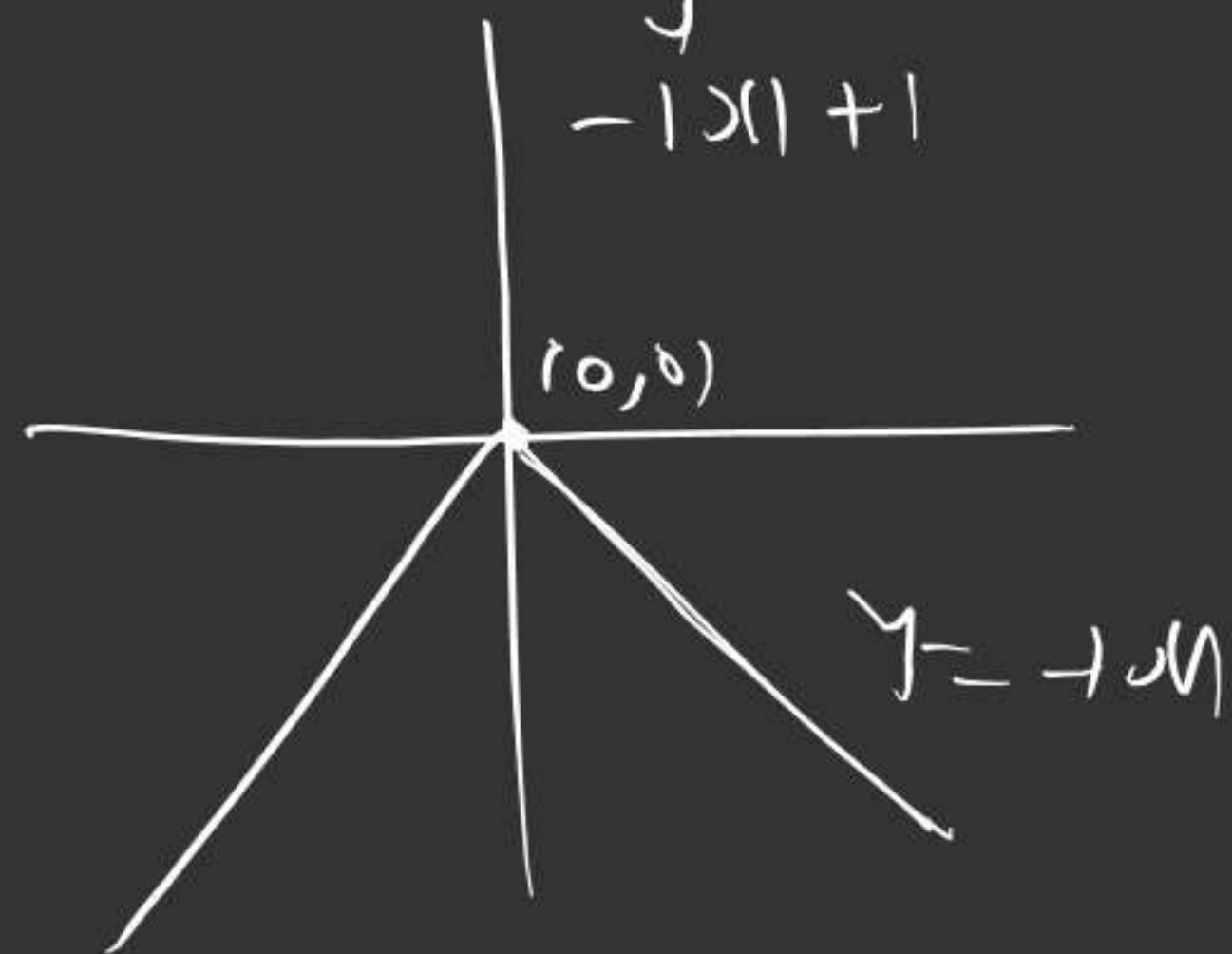
$$y = x + 2\pi$$

$$y = -x + 3\pi$$





$$15) \quad y = \text{Sgn}(\underbrace{1 - |x|}_{(-\infty, 0), \{0\}, (0, 1]}) = \{-1, 0, 1\}$$



$$R_f = (-\infty, 1] \rightarrow 3 \text{ Tokde.}$$



$$\frac{1}{\log_a b} = \log_b a$$

$$\frac{x^2 - 8x + 23}{8} < \phi$$

Do it

(4)  $y = \log_e \left\{ \log_{|\sin x|} (x^2 - 8x + 23) - \frac{3}{\log_2 |\sin x|} \right\}$  Df.

$$y = \log_e \left\{ \log_{|\sin x|} (x^2 - 8x + 23) - \log_{|\sin x|} 2^3 \right\}$$

$$\log_m A - \log_m B = \log \frac{A}{B}$$

Defn



$$y = \log_e \left\{ \log_{|\sin x|} \frac{x^2 - 8x + 23}{8} \right\}$$

$y = |\sin x|$

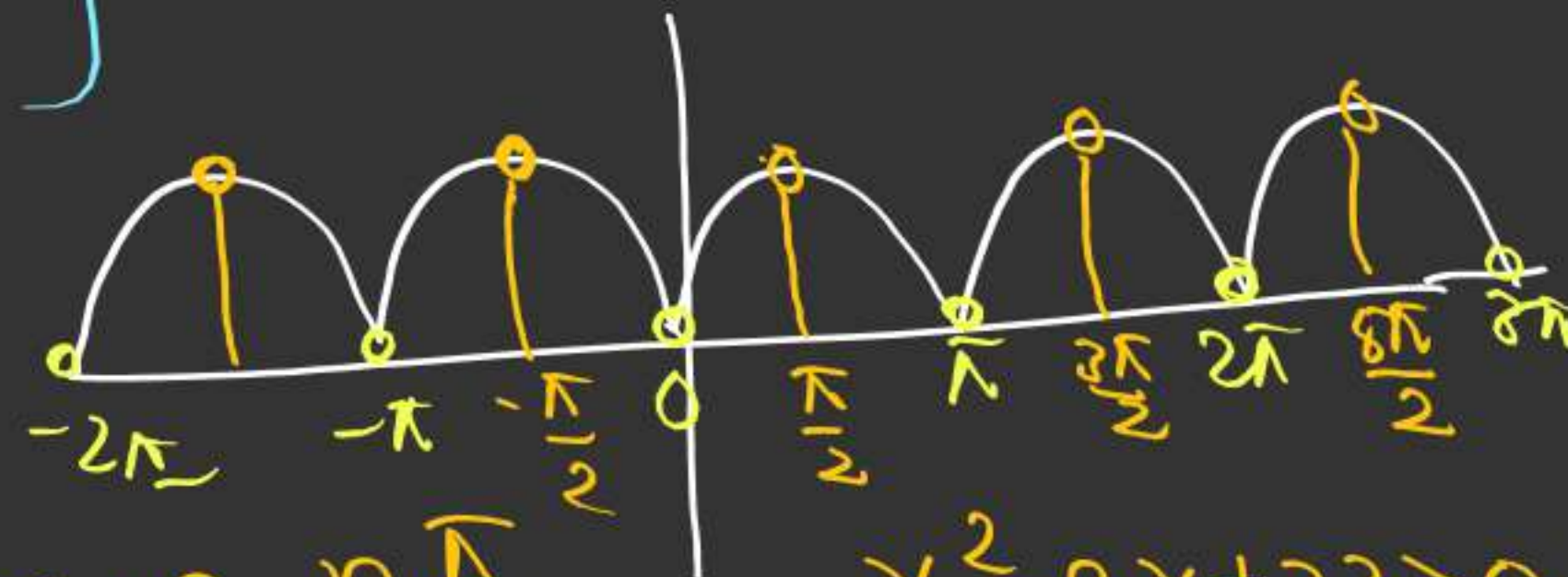
$$e > 0$$

$$e \neq 1$$

$$\frac{x^2 - 8x + 23}{8} > 0$$

~~$\log_{|\sin x|}$~~  Base  $\in (0, 1)$

$$|\sin x| \neq 1$$



$$x \in \mathbb{R} - n\frac{\pi}{2}$$

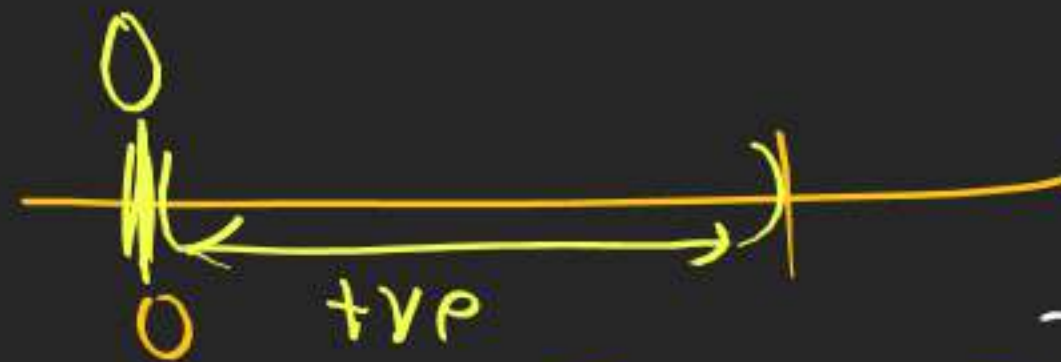
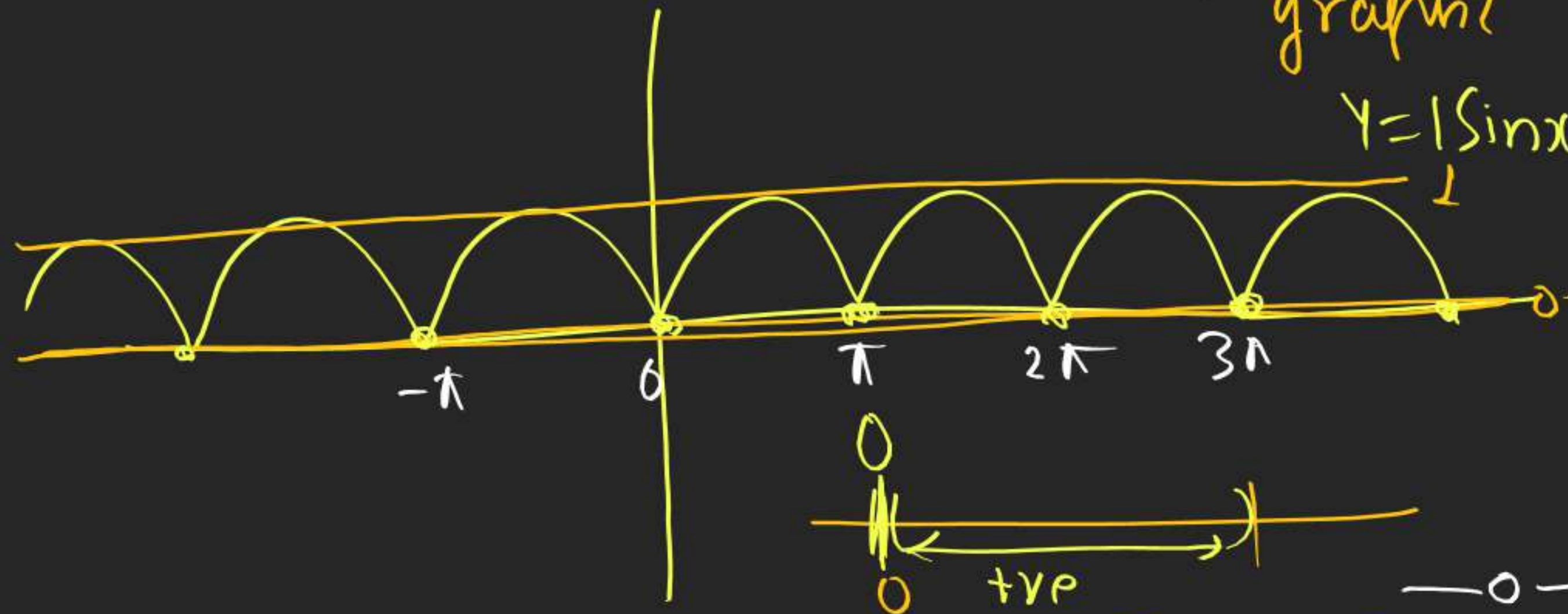
$$\frac{x^2 - 8x + 23}{8} > 0$$



# RELATION FUNCTION

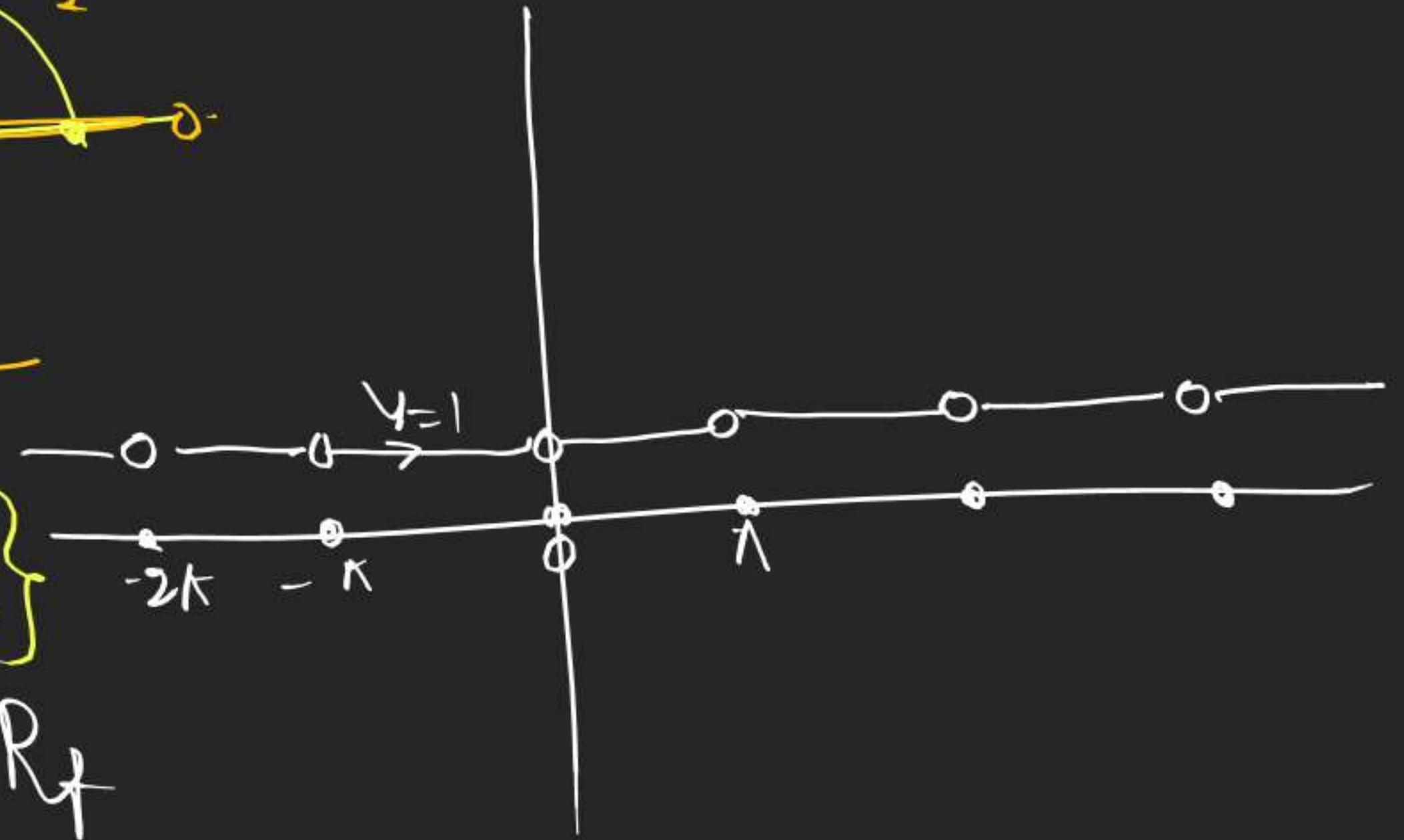
Note DPP  
QS ← Backward  
form

Q  $y = \text{Sgn}(|\sin x|)$  find Range & make graph?



$$y = \text{Sgn}(|\sin x|) = \{0, 1\}$$

$\nwarrow$   
 $\mathbb{R}_+$



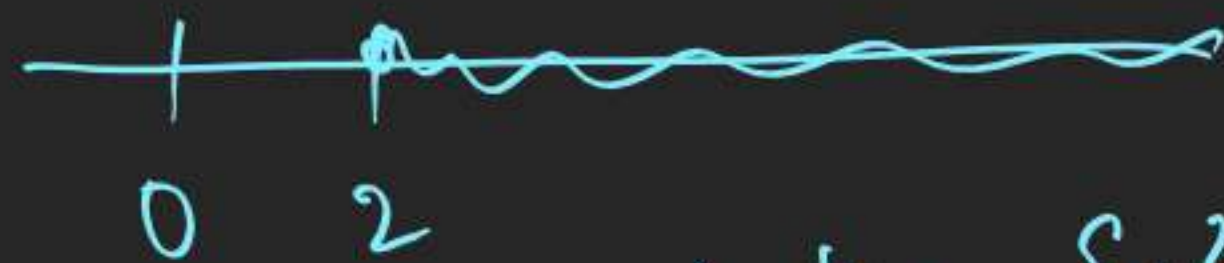


# RELATION FUNCTION

Q  $y = \text{Sgn}(x^2 - 2x + 3) \text{ } R_+$ ?

$$(x^2 - 2x + 1) + 2$$

$$y = \text{Sgn}\left(\underbrace{(x-1)^2 + 2}_{\substack{\geq 0 + 2 \\ \geq 2}}\right) = 1 \quad \text{+ve \&gt; 0}$$



$$\therefore K_f = \{1\}$$

$$y = 1$$

(M2)

$$a=1, b=-1, c=3.$$

$$D = (-1)^2 - 4 \times 1 \times 3$$

$$= -11 = -ve$$

$$a > 0, D < 0$$

$$x^2 - 2x + 3 > 0 \text{ for all } x$$

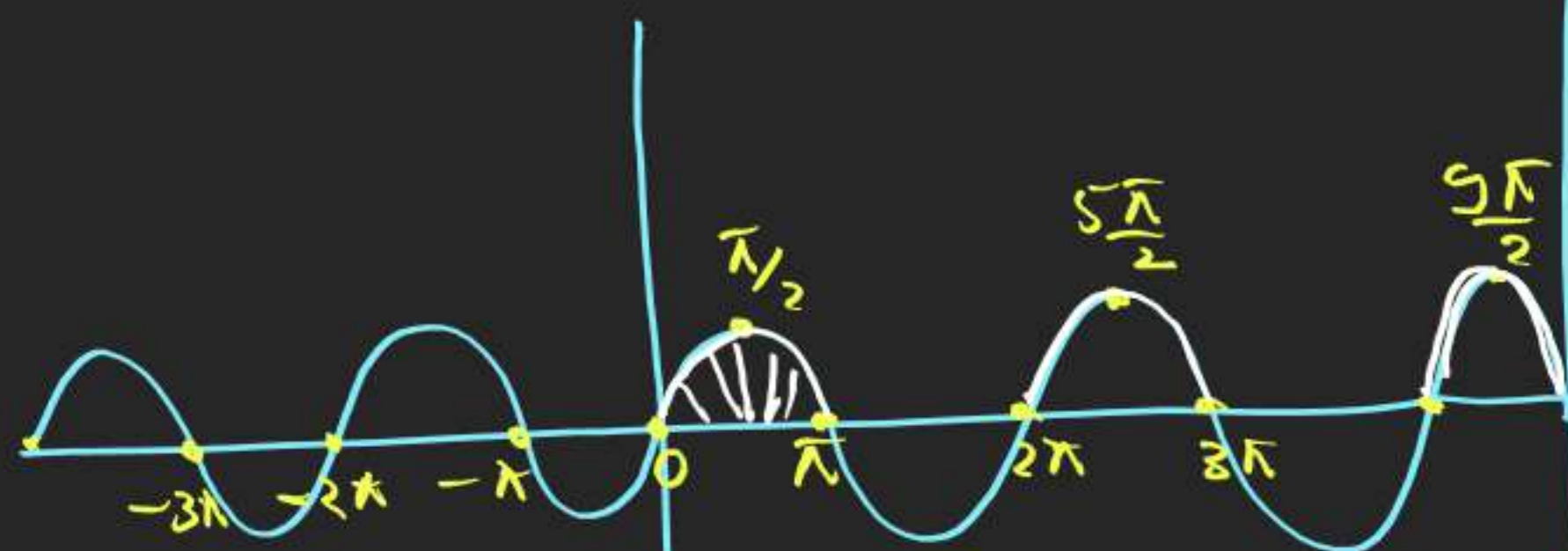
$$y = \text{Sgn}(x^2 - 2x + 3) = 1.$$



## RELATION FUNCTION

 $(2n\pi, (2n+1)\pi)$ Trig of  $x$ .

①  $y = \sin x$



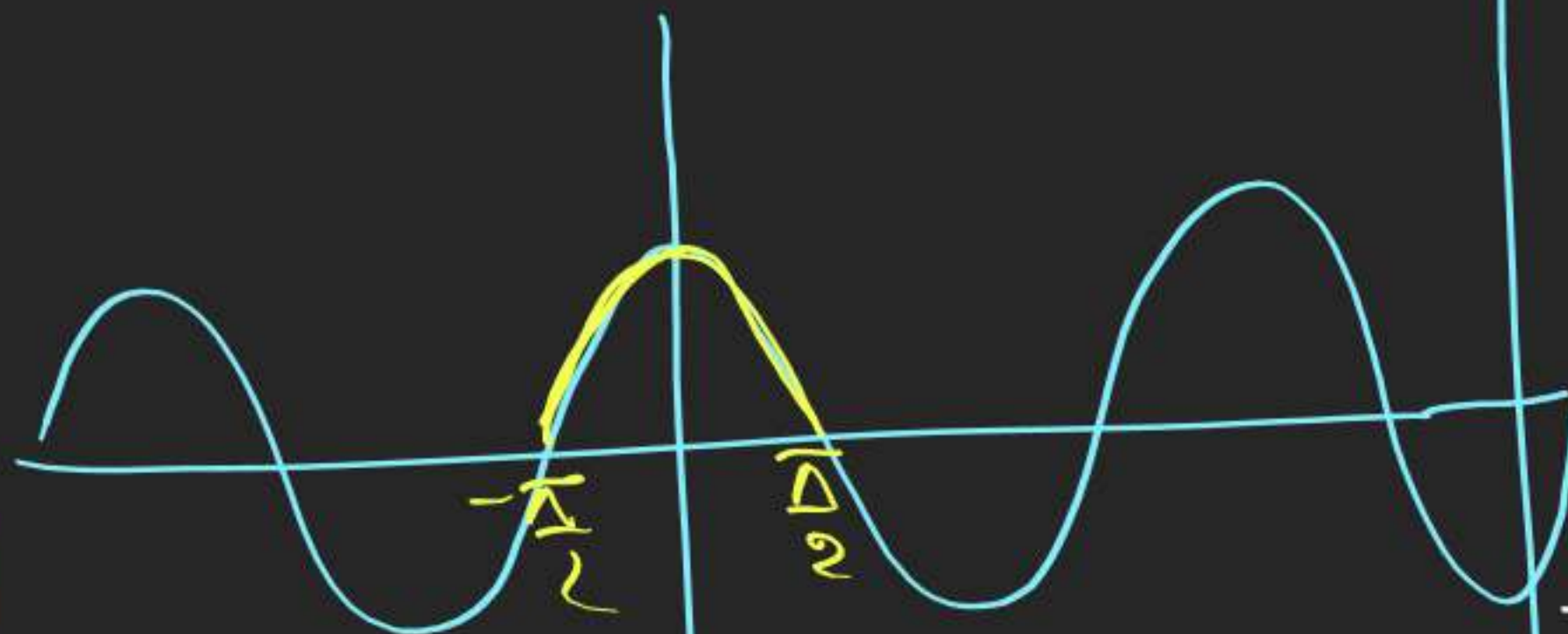
$$\begin{aligned} \text{A) } \sin x &= 0 \\ x &= n\pi \end{aligned}$$

$$\text{B) } \sin x = 1 \Rightarrow x = (4n+1)\frac{\pi}{2}$$

$$\text{C) } \sin x > 0 \text{ कहाँ?}$$

$$0 < x < \pi \Rightarrow x \in (2n\pi, 2n\pi + \pi)$$

②  $y = \cos x$

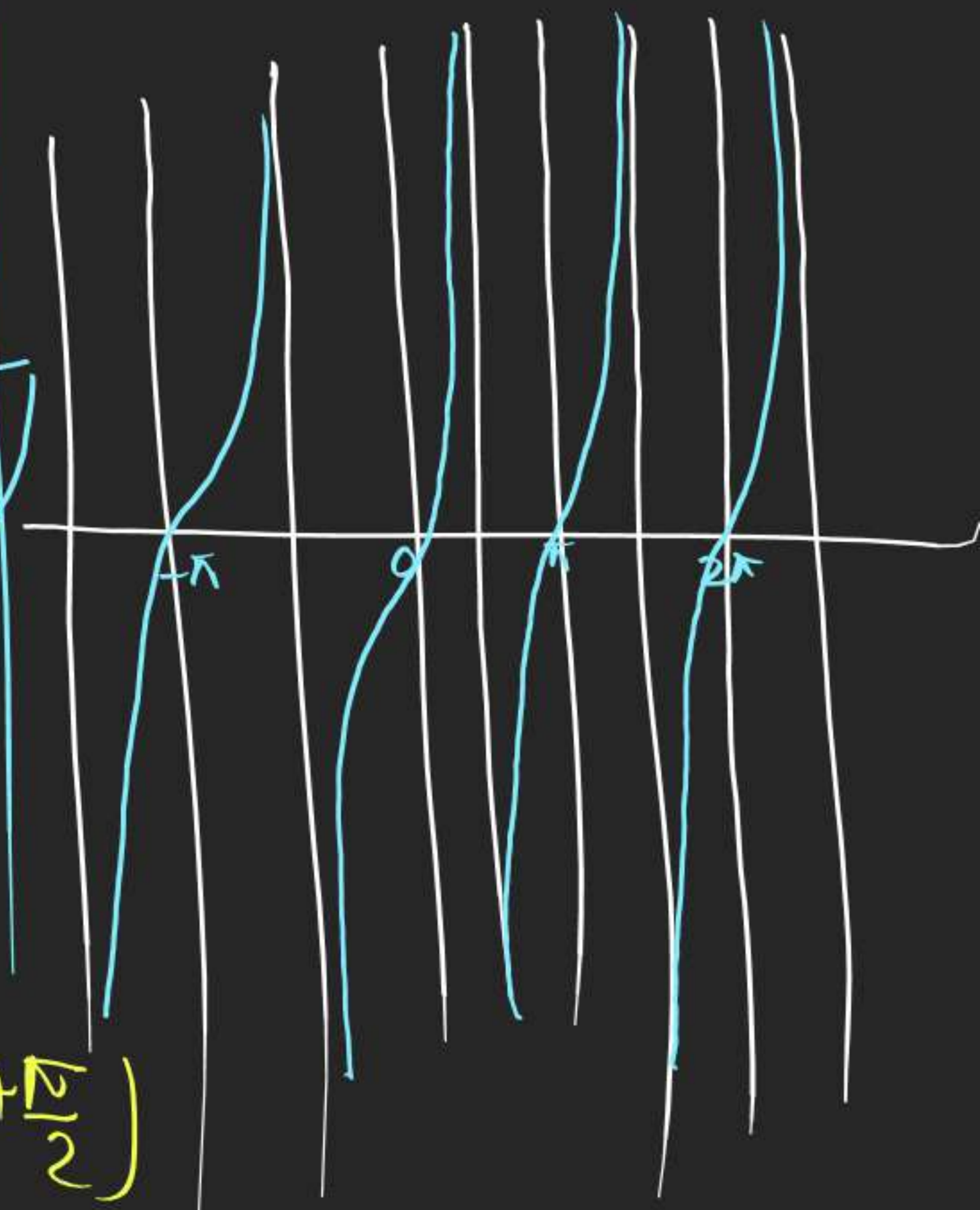


$$\text{D) } \cos x > 0 \text{ कहाँ?}$$

$$-\frac{\pi}{2} < x < \frac{\pi}{2}$$

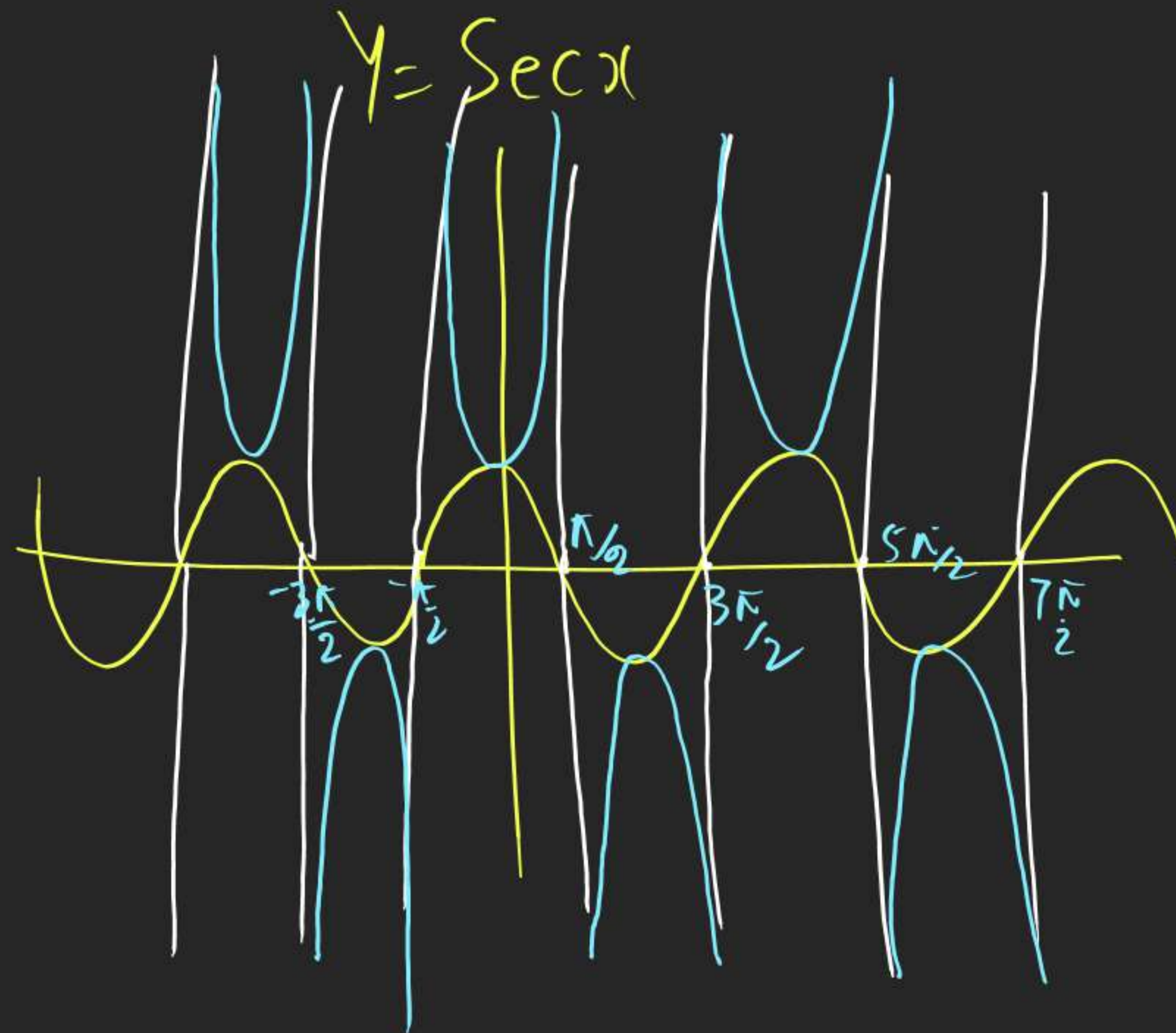
$$x \in \left(2n\pi - \frac{\pi}{2}, 2n\pi + \frac{\pi}{2}\right)$$

③  $y = \tan x$





# RELATION FUNCTION



Q  $f(x) = \frac{1}{\sqrt{|\sin x| + \sin x}}$  find D<sub>f</sub>?

$|\sin x| + \sin x > 0$

$\swarrow$   
 $\sin x > 0$   
 $\sin x + \sin x > 0$   
 $2 \sin x > 0$   
 $\sin x > 0$   
 $x \in (2n\pi, (2n+1)\pi)$

$\searrow$   
 $\text{let } \sin x = -ve$   
 $-\sin x + \sin x > 0$   
 $0 > 0$   
 Not Possible



# Transformation of Graph.

$f(x)$  Ki image X Axis me

$f(x)$  Ki image Y Axis

Part of graph Below.

X Axis will be converted above X Axis

K Pt. Up or down Kar k.

$x = -k$  or  $f(x)$  Ka graph Bnado.

## RELATION FUNCTION

①  $y = |x|$



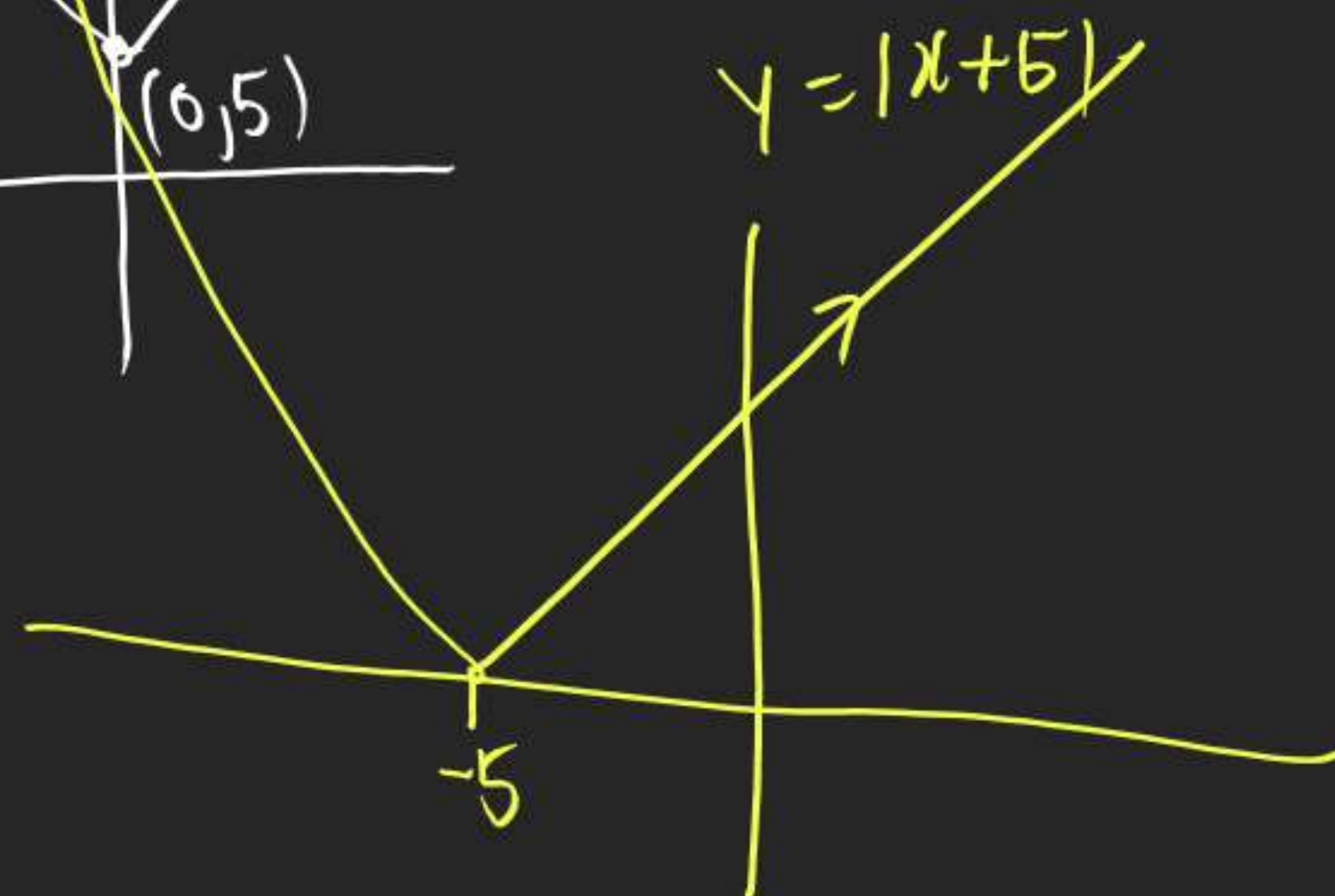
②  $y = -|x|$



③  $y = |x| + 5$



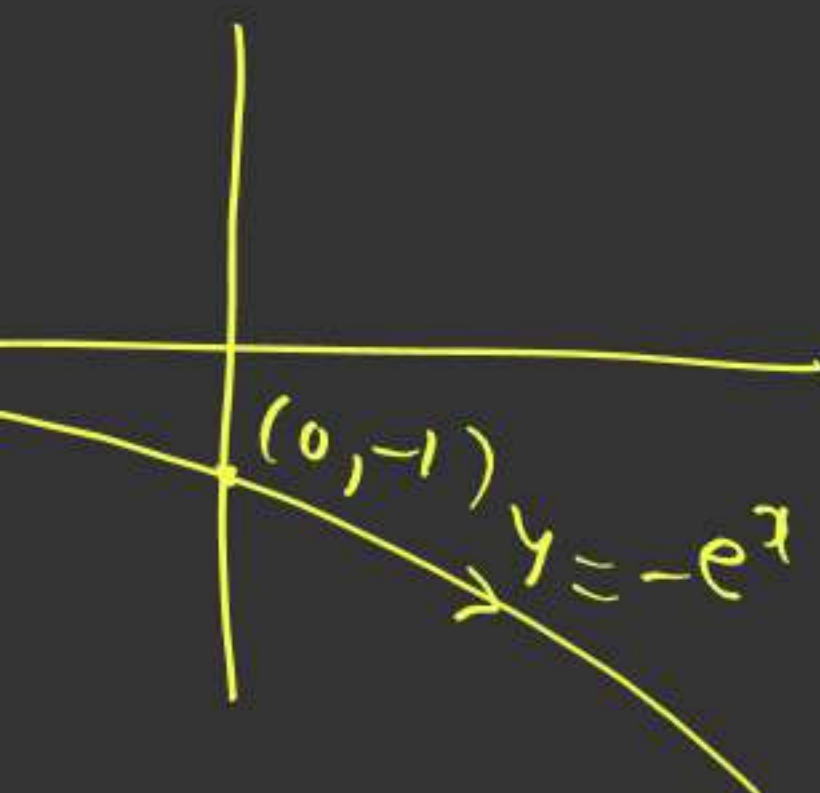
④  $y = |x + 5|$



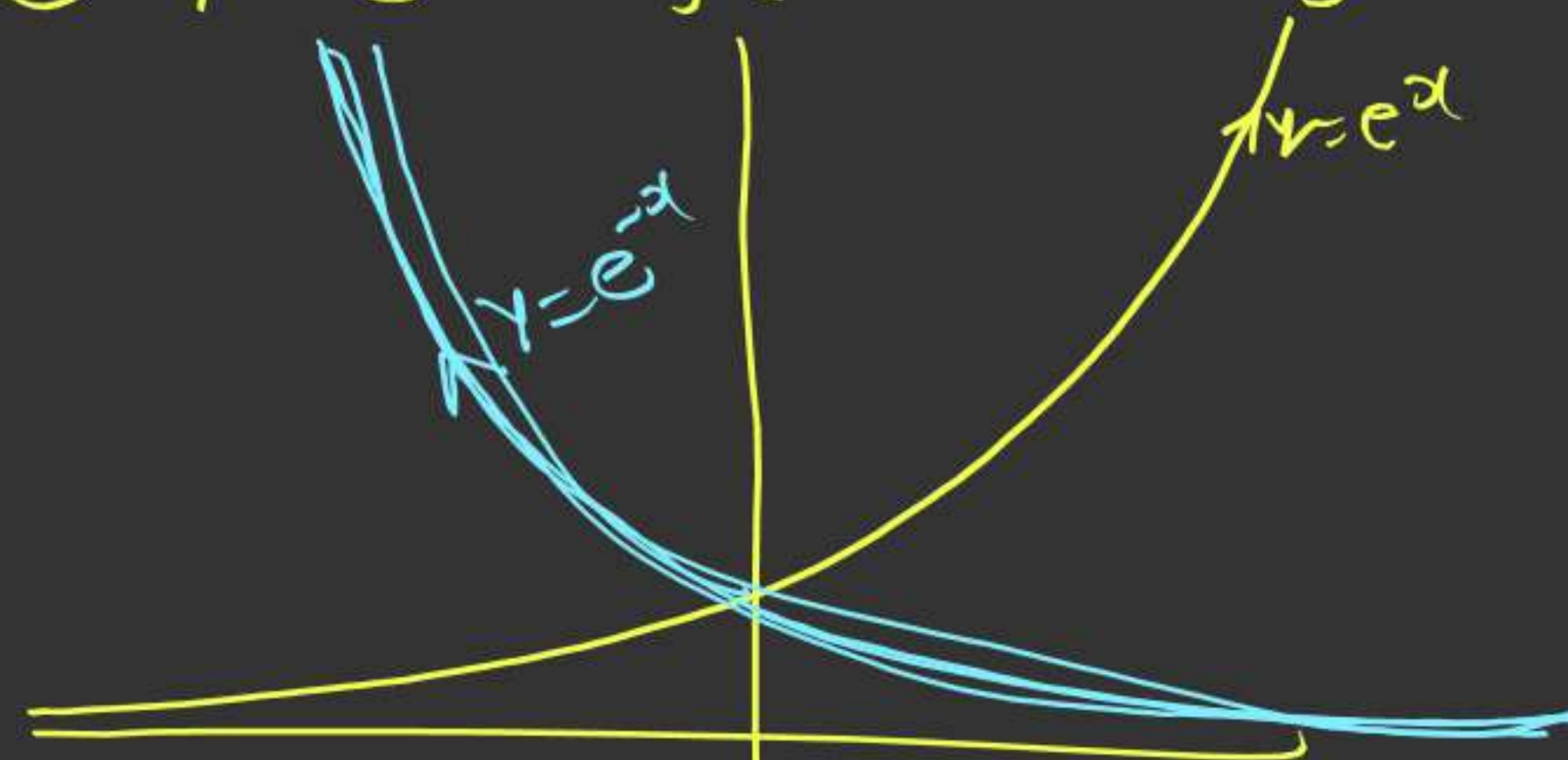




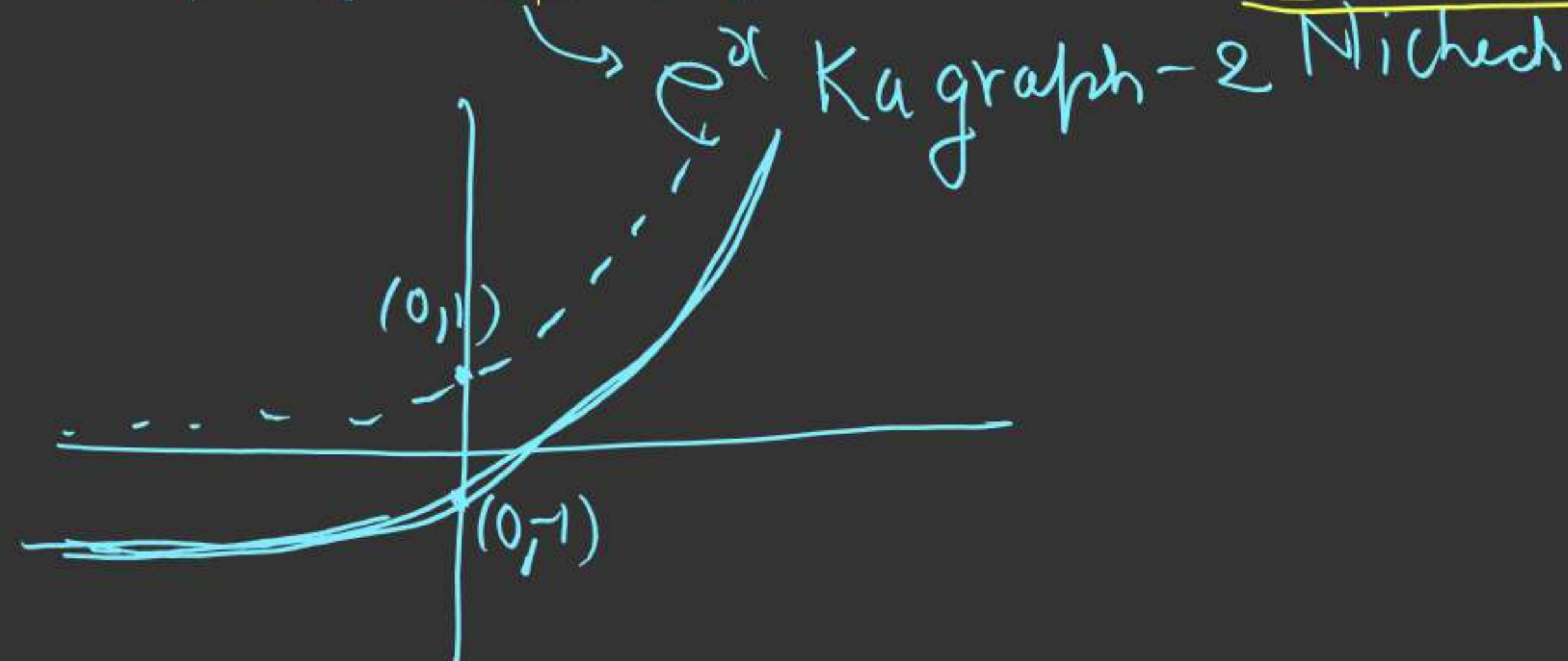
$$e^x \rightarrow -f(x)$$



(3)  $y = e^{-x} \rightarrow f(-x) \rightarrow \text{Image y Axis}$

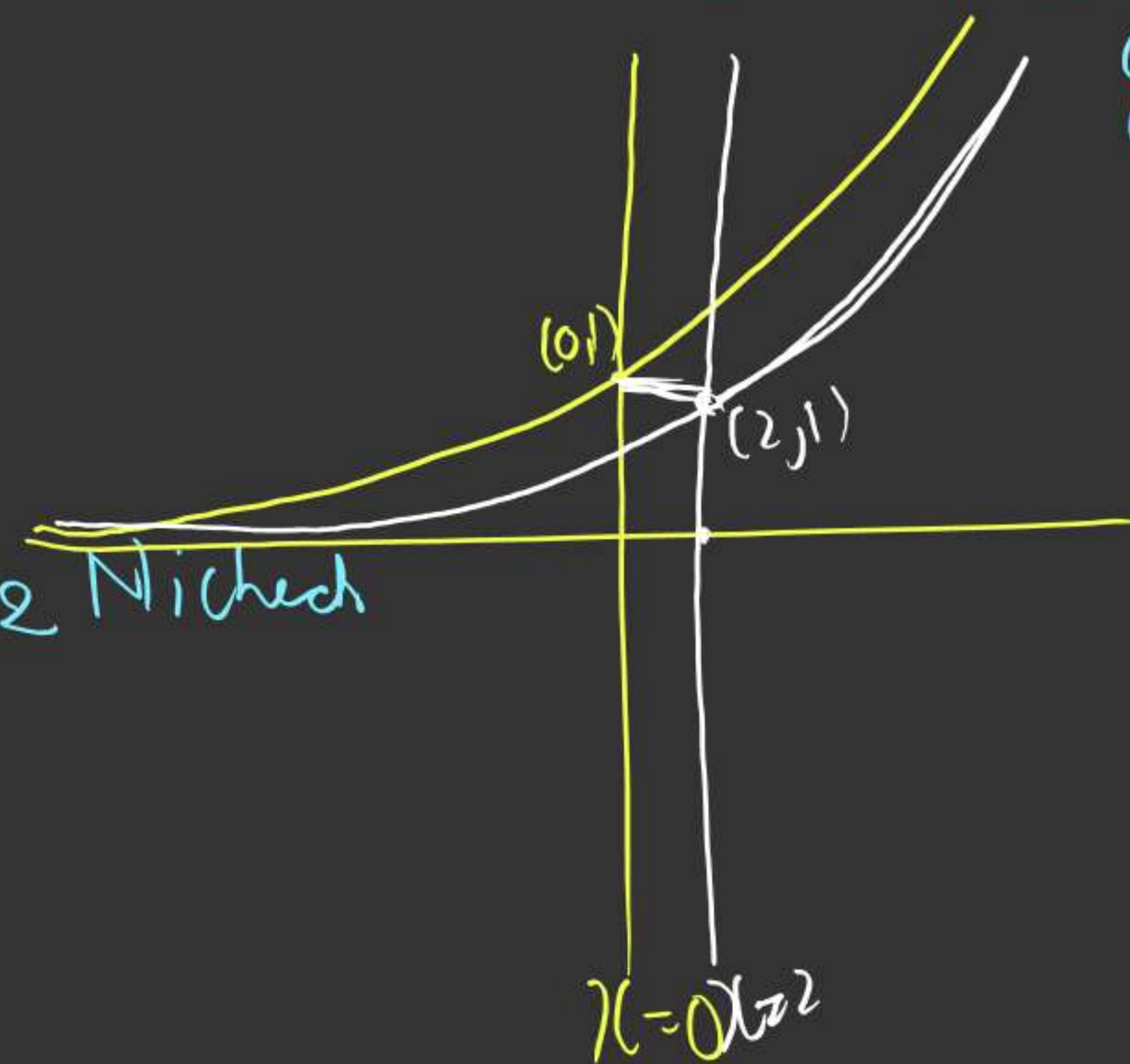


(4)  $y = e^x - 2 \rightarrow f(x) + K$



(5)  $y = e^{(x-2)} \rightarrow f(x+K)$

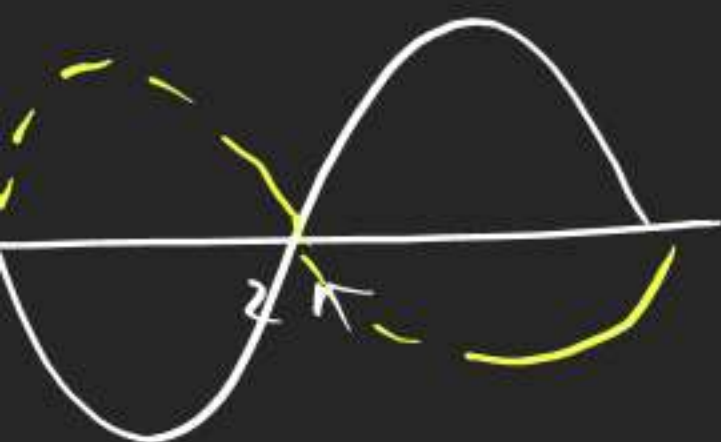
$x = 2 \quad K = y = e^x \quad \text{graph}$



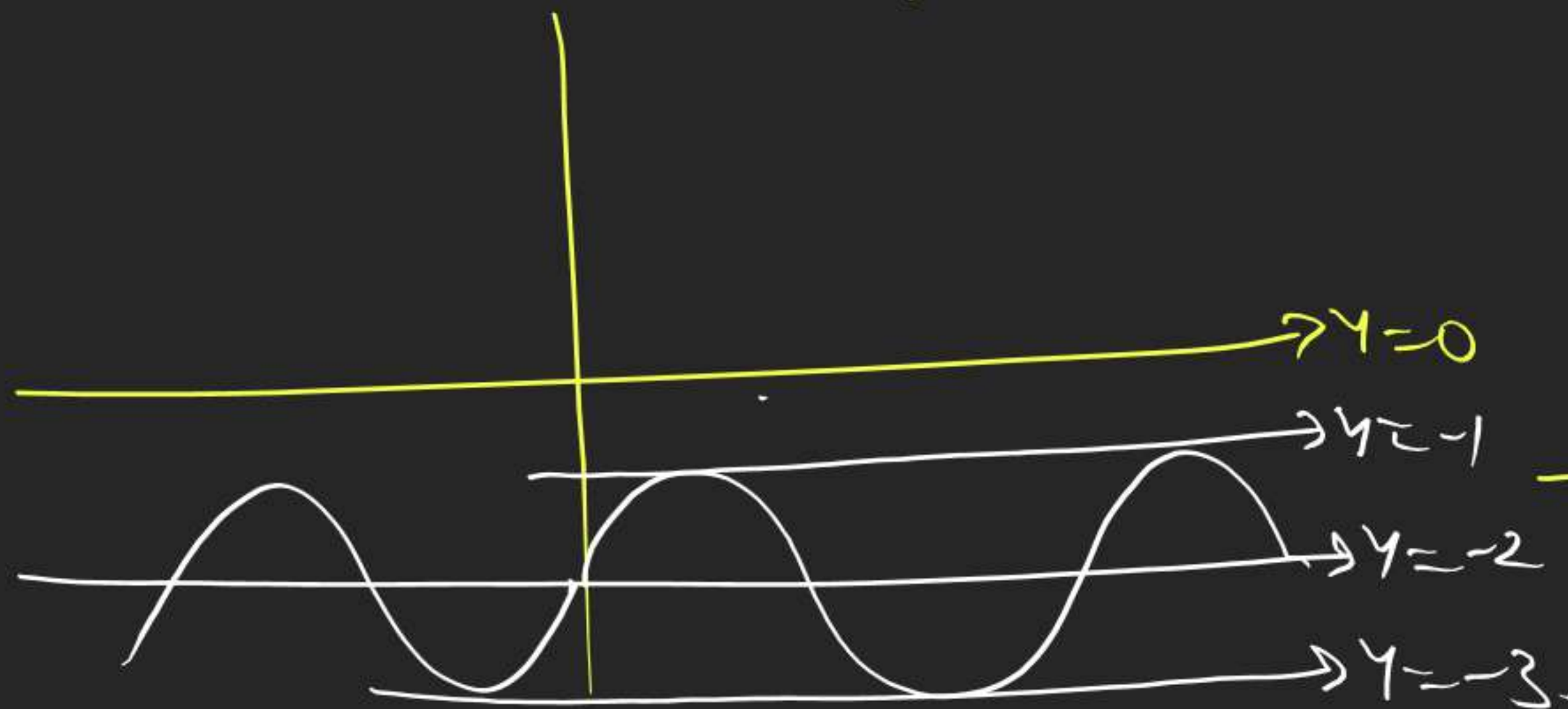
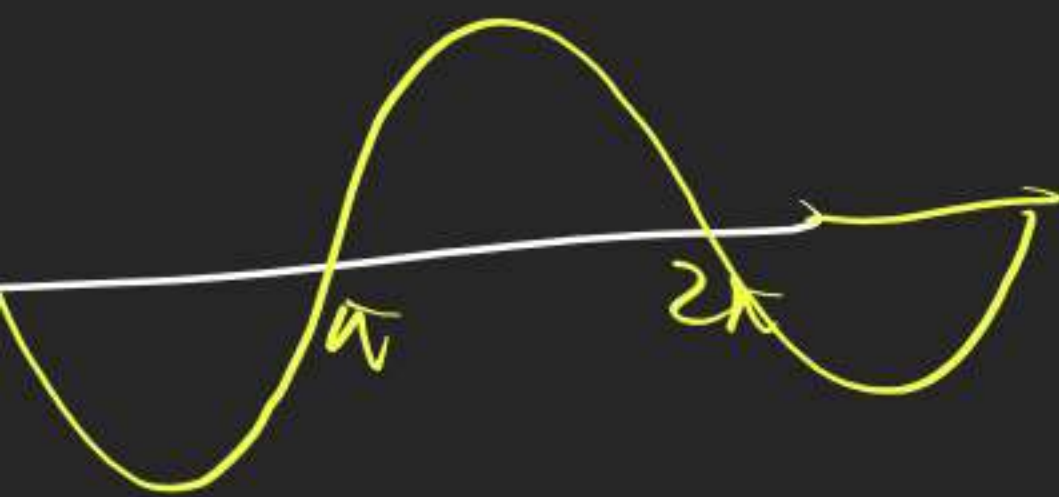


# RELATION FUNCTION

(3)  $y = \sin x - 2$   
 $R_f \in [-3, -1]$   
 $D_f \rightarrow x \in \mathbb{R}$   
 $\hookrightarrow 2 \text{ pt down.}$



$-\sin x$



(4)  $y = \sin(x-2)$

$x = 2 \text{ } \forall x, y = \sin x$

$DPP \rightarrow x = 1$

