

$$\lim_{x \rightarrow 0} \frac{x^4 - \frac{ax^2}{2} - \frac{x^2}{2}}{\left(\left(a - \frac{x^2}{4} \right) + \sqrt{a^2 - x^2} \right)^2}$$

$\lim_{x \rightarrow 1} \left(\frac{-a + \frac{\sin(x-1)}{x-1}}{1 + \frac{\sin(x-1)}{x-1}} \right)^{1+\sqrt{x}}$
 $\lim_{n \rightarrow \infty} \left(\frac{2}{\pi} \cos^{-1} \frac{1}{n} + \frac{1}{\pi} \left(\cos^{-1} \frac{1}{n} - \frac{\pi}{2} \right) \right)^{\frac{1-a}{2}}$
 $\left(\frac{1-a}{2} \right)^2 = \frac{1}{4}$
 $\frac{1-a}{2} = \frac{1}{2}$

$\lim_{x \rightarrow 0} \frac{f(x)}{g(x)}$
 $f(x) > 0$
 $g(x) > 0$
 $\frac{1}{32a}$
 $\frac{1}{b} + \frac{1}{b} = 2 \sin^2 \theta$

$\frac{2}{\pi} \cos^{-1} \frac{1}{n}$
 $\frac{\sin^{-1} \frac{1}{n}}{\frac{1}{n}} = 1 - \frac{2}{\pi}$

5.

$$\frac{1 - \cos\left(\frac{\pi}{2} - \pi x\right)}{\left(\frac{\pi}{2}(1-2x)\right)^2} \cdot \frac{1}{4}$$

$$\frac{1 - \cos(\pi - 2\pi x)}{(\pi(1-2x))^2}$$

4.

$$f(x) = \begin{cases} x^2 & x \in [0, 1] \\ 2x - x^2 & x \in [-1, 0] \end{cases}$$

$$x - x^2$$

$$4(2^x - 4)$$

$x = 1$

$a=1, 2$

$$LHL = \lim_{x \rightarrow 1} \underbrace{f(f(x))}_{=1+x} = 3$$

$$RHL = \lim_{n \rightarrow 1^+} f(f(n)) = 1$$

3-4 \leftarrow f \rightarrow 5 \downarrow 2+

$$x = a \quad \checkmark$$
$$x = f(a)$$
$$g\left(\frac{1}{f(x)}\right)$$

$$n-a$$

$$\frac{f}{g}(u) = (f \circ g)(u)$$

• $\alpha = 2$

$$a = 2$$
$$f(a) = 2 = 1 + a, 3 - a$$
$$a = 1, 1$$

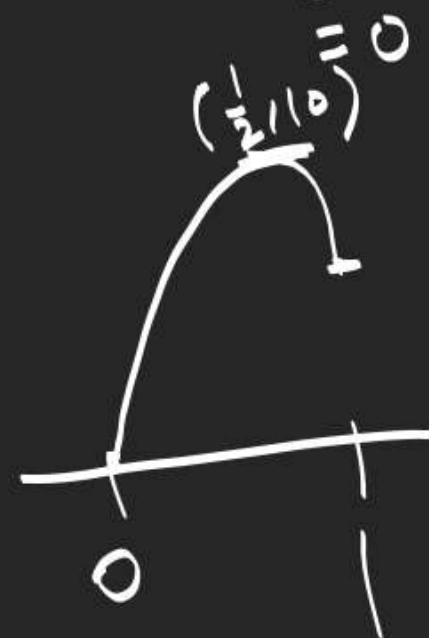
$$\lim_{x \rightarrow 1^-} [f(f(x))] = 2.$$

$$f^{-1} = G^{-1} \circ f$$

$$\lim_{x \rightarrow 1^+} [f(f(x))] = 0$$

$$\lim_{x \rightarrow 1} \left(\lim_{n \rightarrow \infty} \frac{1}{1 + n \sin^2 \pi x} \right) = \lim_{x \rightarrow 1} 0 = 0.$$

$$f(1) = \lim_{n \rightarrow \infty} \frac{1}{1 + n \sin^2 \pi} = 1$$





$\lim_{x \rightarrow a} f(x) = \begin{cases} a \\ -a \end{cases}$

$a = -a \Rightarrow \boxed{a = 0}$

$f(x)$ is discont $\forall x \in \mathbb{R} - \{0\}$

Cont. at $x=0$
 $\lim_{x \rightarrow 0} f(x) = 0$
 $x \in \mathbb{Q} \quad f(0) = 0$
 $x \notin \mathbb{Q}$
 $\Rightarrow f(x)$ is cont. at $x=0$

\therefore Let $f(x) = \begin{cases} x^2 + ax + 1 & x \in \mathbb{Q} \\ ax^2 + 2x + b & x \notin \mathbb{Q} \end{cases}$ is cont. at $x=1, e$
 find a, b .

$$x^2 + ax + 1 = ax^2 + 2x + b$$

$$(a-1)x^2 + (2-a)x + b-1 = 0 \quad \begin{matrix} 1 \\ e \end{matrix}$$

$$\left(\frac{b-1}{a-1} \right) = \frac{1}{1} = 1 \Rightarrow$$

$$\boxed{b=0}$$

$$\frac{a-2}{a-1}$$

$$= 1+e = 1 - \frac{1}{e}$$

$$a-1 = -\frac{1}{e} \Rightarrow a = 1 - \frac{1}{e}$$

$$f(x) = \begin{cases} [x] & x \in \mathbb{Q} \\ x & x \notin \mathbb{Q} \end{cases}$$

$$[\cdot] = G \cdot I \cdot F$$

$$[x] = x \Rightarrow x \in \mathbb{I}$$

$$\text{RHL} = \lim_{x \rightarrow a^+} [x] \text{ or } \lim_{x \rightarrow a^+} x$$

$$\underline{x=a}, a \in \mathbb{I}$$

$$\text{LHL} = \lim_{x \rightarrow a^-} [x] \text{ or } \lim_{x \rightarrow a^-} x$$

$$= a-1 \text{ or } a$$

$f(x)$ is discontin.
 $\forall x \in \mathbb{R}$

Differentiability ✓

Limits $\rightarrow \mathbb{R} - \{14, 15, 16\}$
Continuity $\rightarrow \mathbb{R} - \mathbb{I}$