



$$S_2 P - S_1 P = \frac{\lambda}{3} \text{ (given)}$$

Find resultant intensity at P.

$$S_2 P - S_1 P = \frac{\lambda}{3}$$

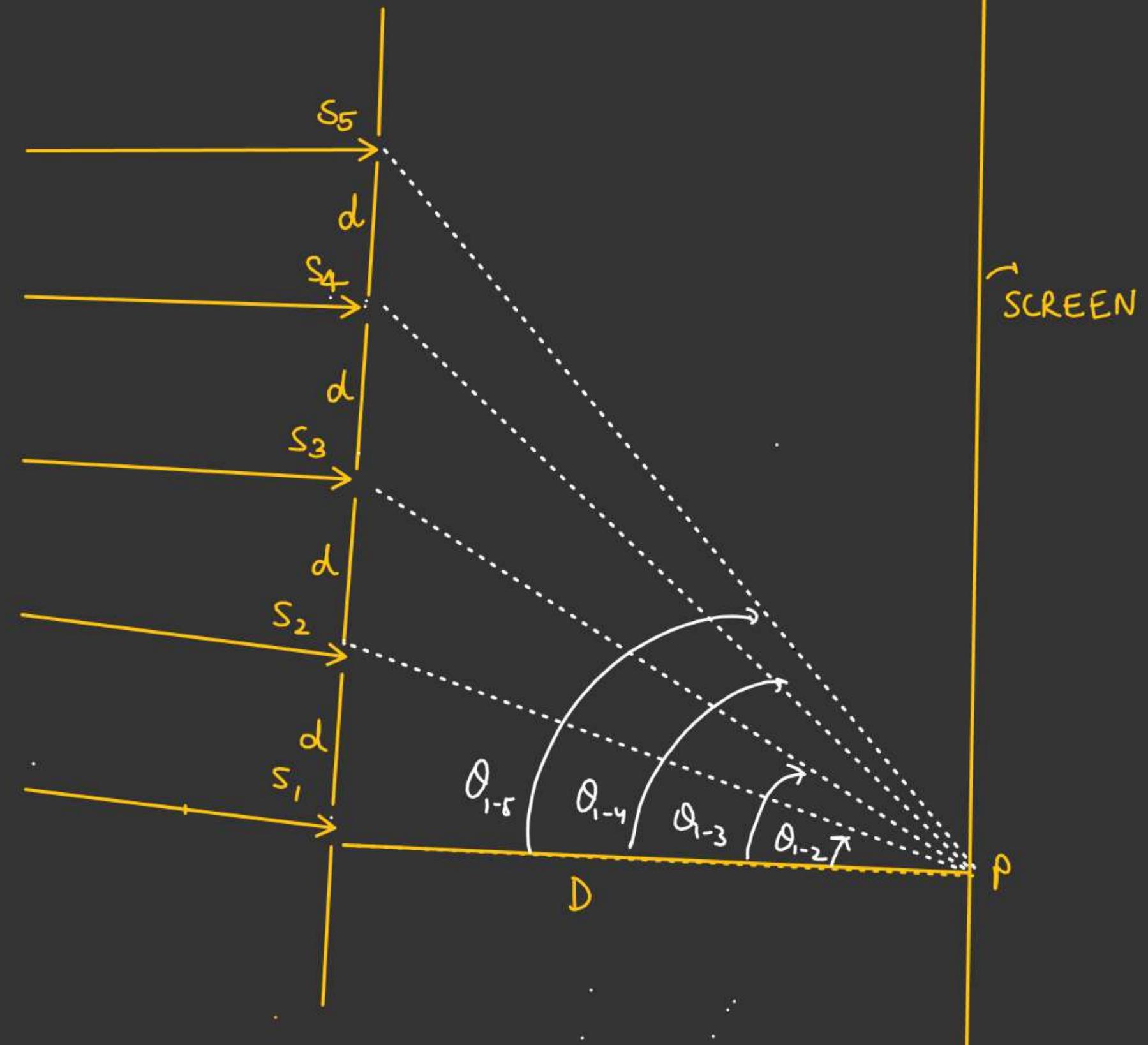
$$d \tan \theta_{1-2} = \frac{\lambda}{3}$$

$$d \left(\frac{d}{2D} \right) = \frac{\lambda}{3}$$

$$\boxed{\frac{d^2}{2D} = \frac{\lambda}{3}}$$

$$\Delta x_{1-2} = \frac{\lambda}{3}$$

$$\Delta \phi_{1-2} = \frac{2\pi}{\lambda} \times \frac{\lambda}{3} = \left(\frac{2\pi}{3} \right)$$

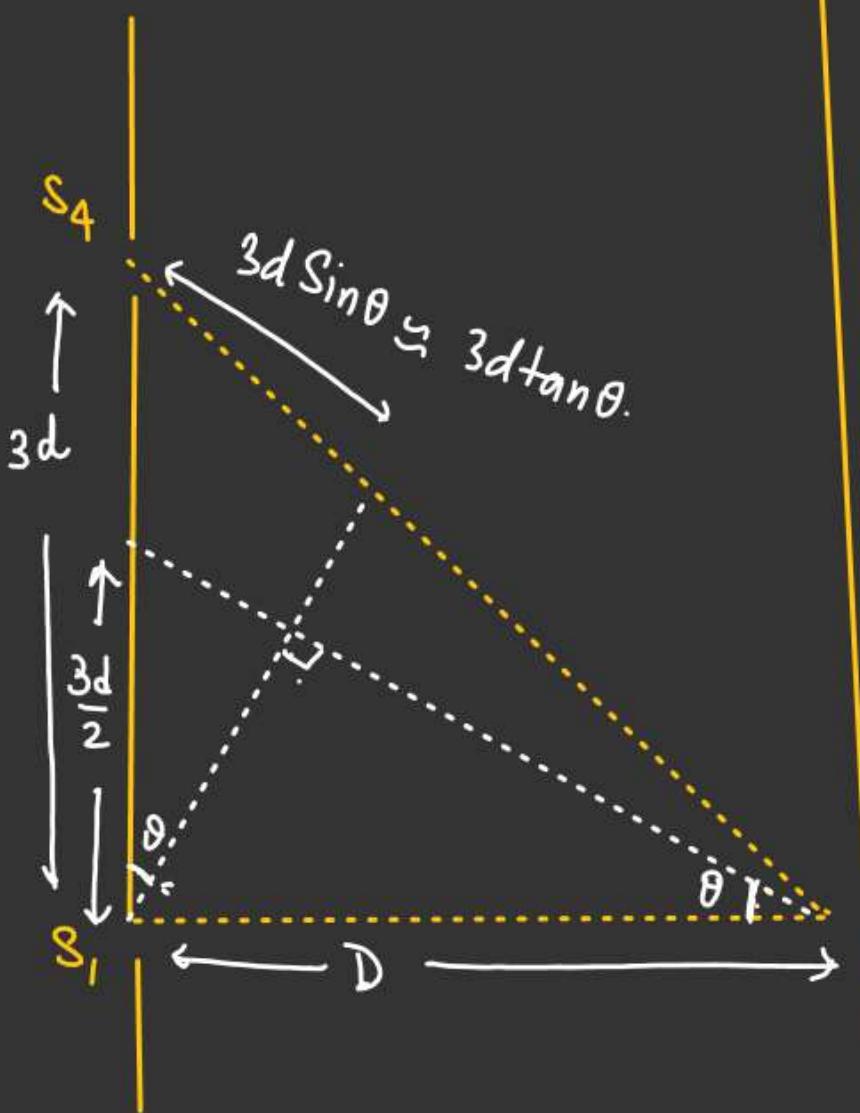


$$\begin{aligned}\Delta \chi_{1-4} &= 3d \tan(\theta_{1-4}) \\ &= 3d \left(\frac{3d}{2D} \right) \\ &= 9 \left(\frac{d^2}{2D} \right) \\ &= 9 \frac{\lambda}{3} = 3\lambda\end{aligned}$$

$$\Delta \phi_{1-4} = \frac{2\pi}{\lambda} \times 3\lambda = \frac{6\pi}{\lambda}$$

$$\begin{aligned}\Delta \chi_{1-5} &= 4d \tan(\theta_{1-5}) \\ &= 4d \left(\frac{2d}{D} \right) \\ &= 8 \left(\frac{d^2}{D} \right) = 8 \times \frac{2\lambda}{3}\end{aligned}$$

$$\begin{aligned}\Delta \phi_{1-5} &= \frac{2\pi}{\lambda} \times \frac{16\lambda}{3} \\ &= \frac{32\pi}{3} = (11\pi - \pi_3)\end{aligned}$$



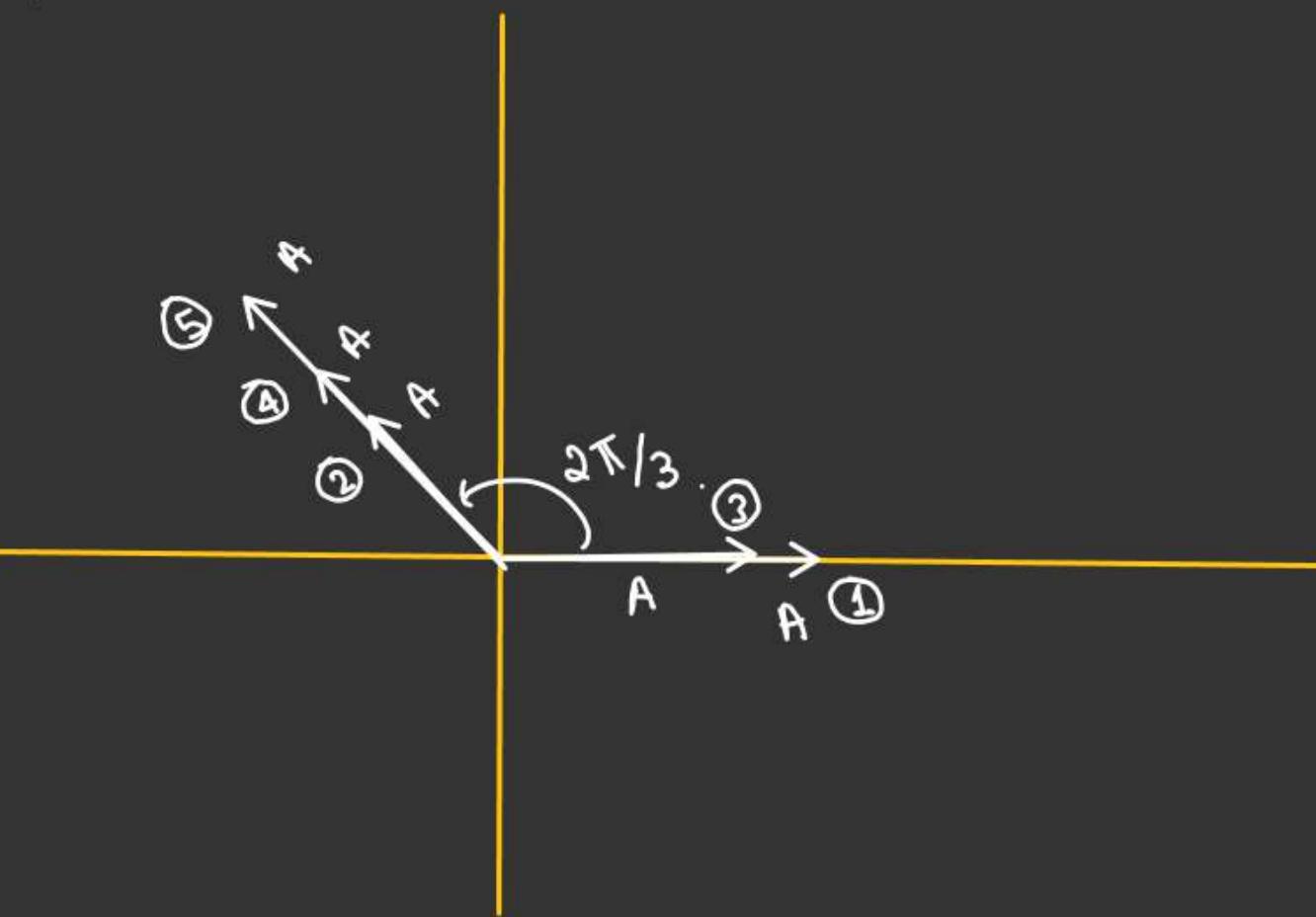
$$\begin{aligned}\Delta \chi_{1-3} &= 2d \tan(\theta_{1-3}) \\ &= 2d \left(\frac{d}{D} \right) \\ &= \frac{2d^2}{D} \quad \left(\frac{d^2}{2D} = \frac{\lambda}{3} \right) \\ &= 2 \left(\frac{2\lambda}{3} \right) = \frac{4\lambda}{3} \\ \Delta \phi_{1-3} &= \frac{2\pi}{\lambda} \times \frac{4\lambda}{3} = \frac{8\pi}{3} \\ &= \left(2\pi + \frac{2\pi}{3} \right) \checkmark\end{aligned}$$

$$A_R = \sqrt{4A^2 + 9A^2 + 2 \cdot (2A)(3A) \cos \frac{2\pi}{3}}$$

$$A_R = \sqrt{13A^2 - 6A^2}$$

$$A_R = \sqrt{7A^2}$$

$$\bar{I}_R = 7 I_0$$



O & O' Symmetrically located.

to Center of Screen. $\lambda \rightarrow$ wavelength of light.

I_0 = Intensity of light.

Path difference at S_3 b/w light ray from S_1 & S_2

$$\Delta x_{1-2} = d_1 \sin \theta \approx d_1 \tan \theta.$$

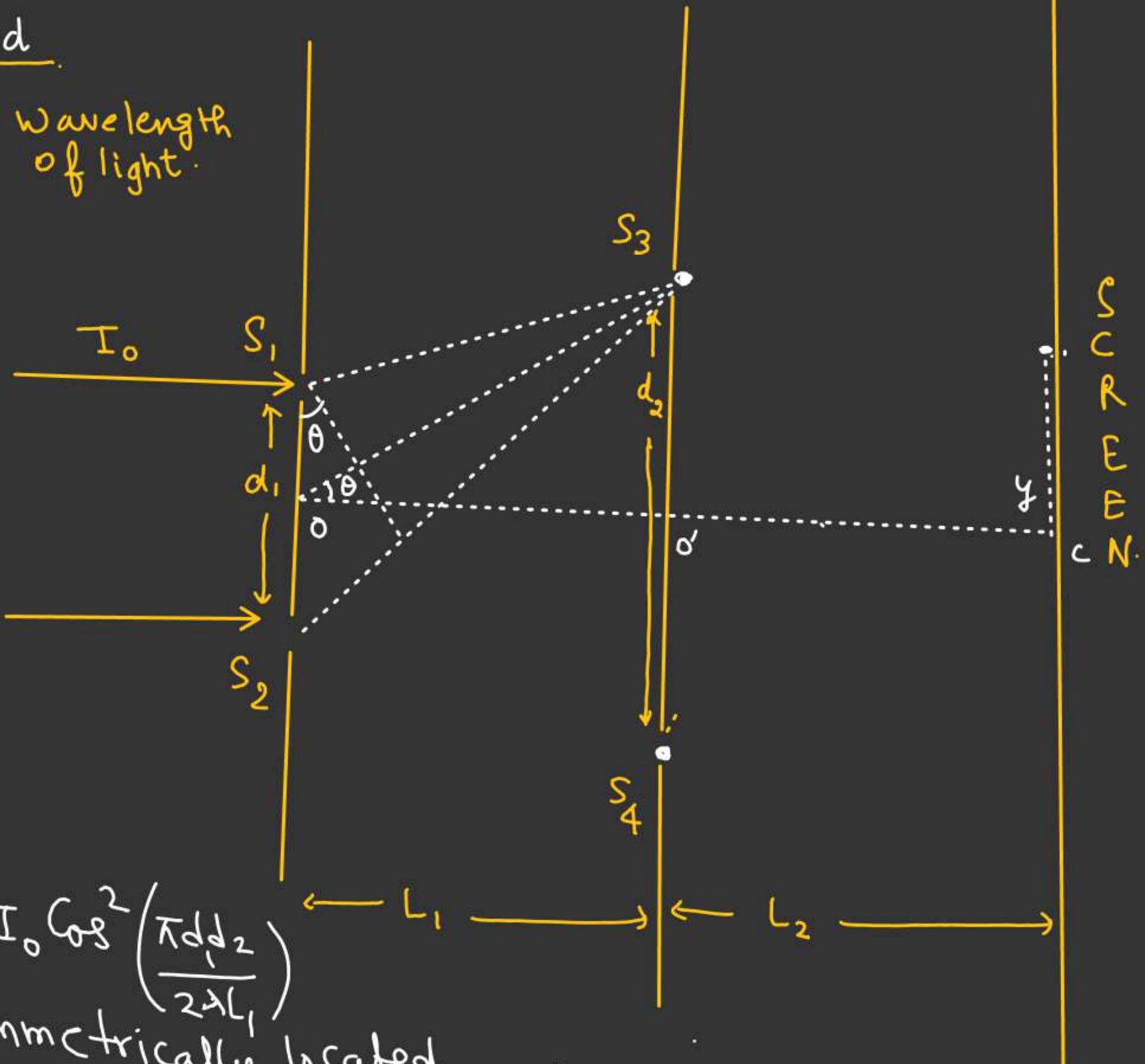
$$\Delta x_{1-2} = d_1 \left(\frac{d_2}{2L_1} \right)$$

$$\Delta \phi_{1-2} = \left(\frac{2\pi}{\lambda} \frac{d_1 d_2}{2L_1} \right) = \left(\frac{\pi d_1 d_2}{\lambda L_1} \right)$$

Let, Intensity at 3 be I

$$I = 4I_0 \cos^2 \left(\frac{\Delta \phi_{1-2}}{2} \right) = 4I_0 \cos^2 \left(\frac{\pi d_1 d_2}{2\lambda L_1} \right)$$

Intensity at S_4 is also I , as symmetrically located.



Interference at screen at a distance y from center of screen:—

Light ray coming from S_3 and S_4 having intensity I interfere at y .

$$\Delta \alpha_{3-4} = \left(\frac{d_2 y}{L_2} \right)$$

$$I = 4I_0 \cos^2 \left(\frac{\pi d_1 d_2}{2\lambda L_1} \right)$$

$$\Delta \phi_{3-4} = \frac{2\pi}{\lambda} \left(\frac{dy}{L_2} \right)$$

$$I_R = 16I_0 \cos^2 \left(\frac{\pi d_1 d_2}{2\lambda L_1} \right) \cdot \cos^2 \left(\frac{2\pi dy}{\lambda L_2} \right)$$

$$I_R = 4I \cos^2 \left(\frac{\Delta \phi_{1-3}}{2} \right) = 4I \cos^2 \left(\frac{2\pi dy}{\lambda L_2} \right)$$

S_1 & S_2 Equidistance from O

S_3 & S_4 Equal distance from O'

$D \rightarrow$ Mid point of distance b/w S_3 & S_4

$O' \rightarrow$ Center of Screen

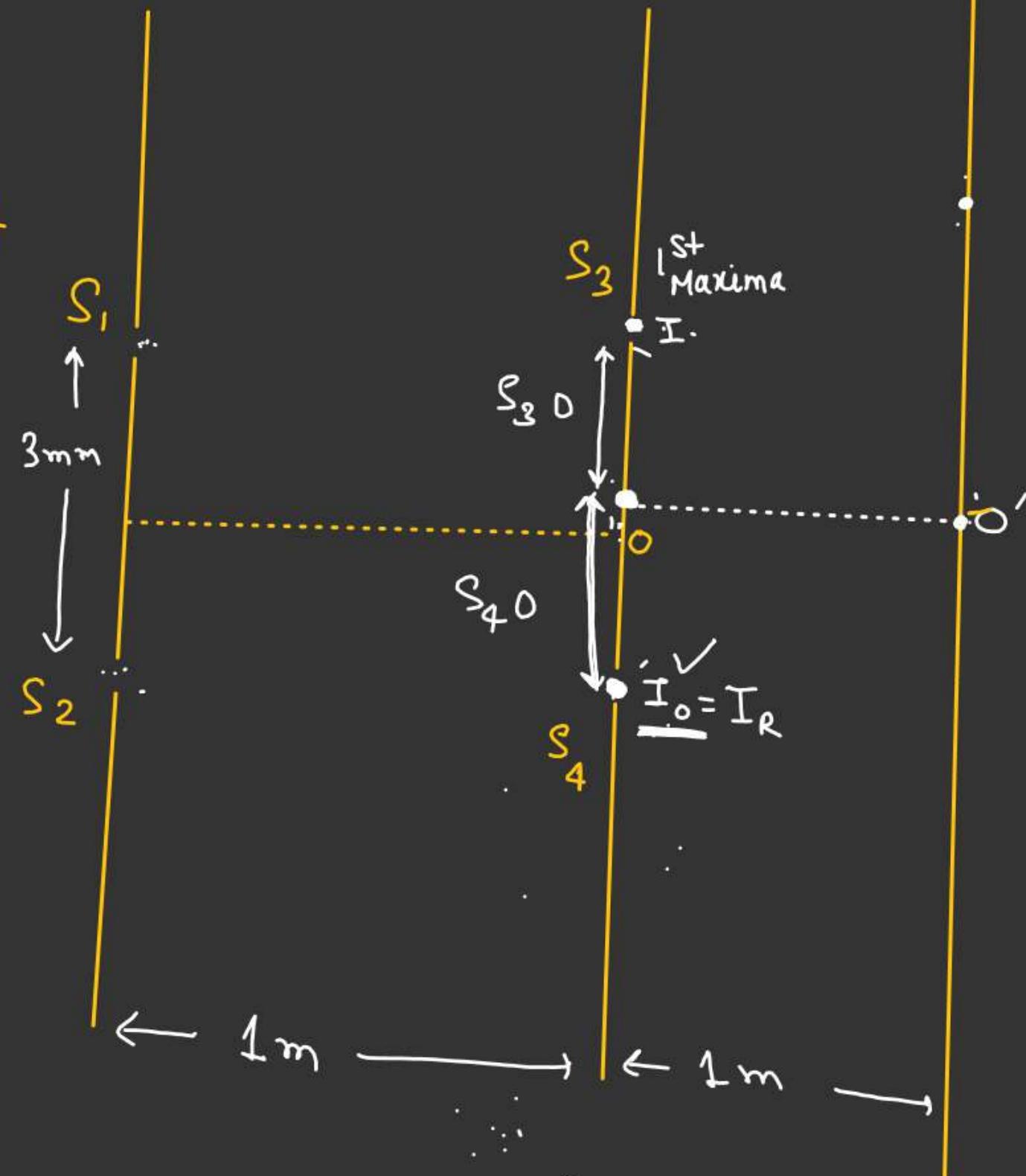
$$\lambda = 6000 \text{ Å}$$

① Find the Intensity at O' ✓

② Find the Intensity of bright fringe.

S_3 is the position of 1st Maxima

At S_4 Intensity is same as of light source. ✓



For 1st Maxima at S_3 .

$$\frac{dy}{D} = \textcircled{1} \lambda$$

1.

$$y = \left(\frac{D\lambda}{d} \right) = \frac{1 \times 6000 \times 10^{-10}}{3 \times 10^{-3}}$$

$$OS_3 = y = (2 \times 10^{-4}) \text{ m. } \checkmark$$

$$\Delta\phi = \frac{2\pi}{\lambda} \cdot (\Delta x)$$

$$\Delta\phi = \frac{2\pi}{\lambda}$$

$$I_R = 4I_0 \cos^2 \left(\frac{\Delta\phi}{2} \right)$$

$$I_R = (4I_0) \checkmark$$

$$(At 4). I_R = I_0.$$

$$I_0 = \frac{4I_0 \cos^2 \left(\frac{\phi}{2} \right)}{2}$$

$$\frac{1}{4} = \cos^2 \left(\frac{\phi}{2} \right)$$

$$\cos \left(\frac{\phi}{2} \right) = \frac{1}{2}$$

$$\frac{\phi}{2} = \frac{\pi}{3}$$

$$\phi = \underline{\underline{\left(\frac{2\pi}{3} \right)}} \checkmark \Rightarrow \frac{2\pi}{\lambda} \cdot \Delta x = \frac{2\pi}{3}$$

$$\frac{(OS_4)d}{D} = \left(\frac{\lambda}{3} \right)$$

$$OS_4 = \left(\frac{D\lambda}{3d} \right) = \frac{1 \times 6000 \times 10^{-10}}{3 \times 3 \times 10^{-3}} \\ = \frac{2}{3} \times 10^{-4}$$

Slit Separation b/w S_3 and S_4

$$= 0S_3 + 0S_4$$

$$= \underline{2 \times 10^{-4} + \frac{2}{3} \times 10^{-4}}$$

$$= \frac{8}{3} \times 10^{-3} \checkmark$$