

Orthocentre

$$AH = 2R \cos A$$

$$BH = 2R \cos B$$

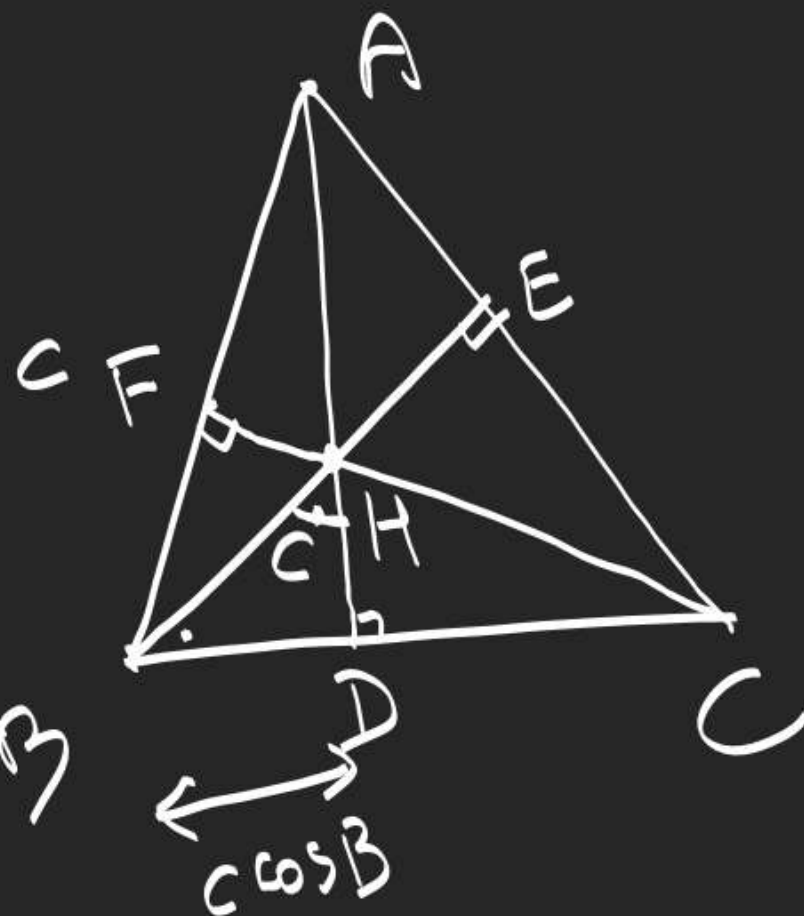
$$CH = 2R \cos C$$

$$HF = 2R \cos A \cos B$$

$$HD = 2R \cos B \cos C$$

$$HE = 2R \cos A \cos C$$

$$2R \cos B \cos C = \frac{c \cos B \cos C}{\sin C}$$



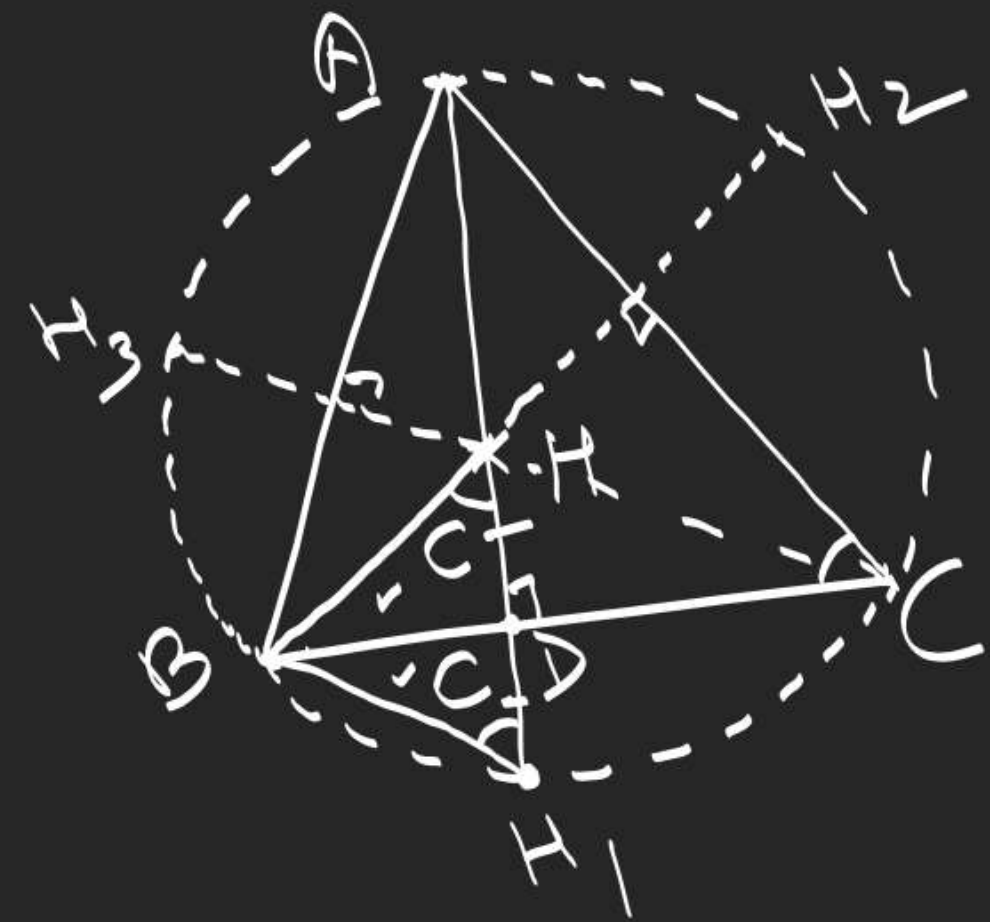
HA, HB, HC

HD, HE, HF

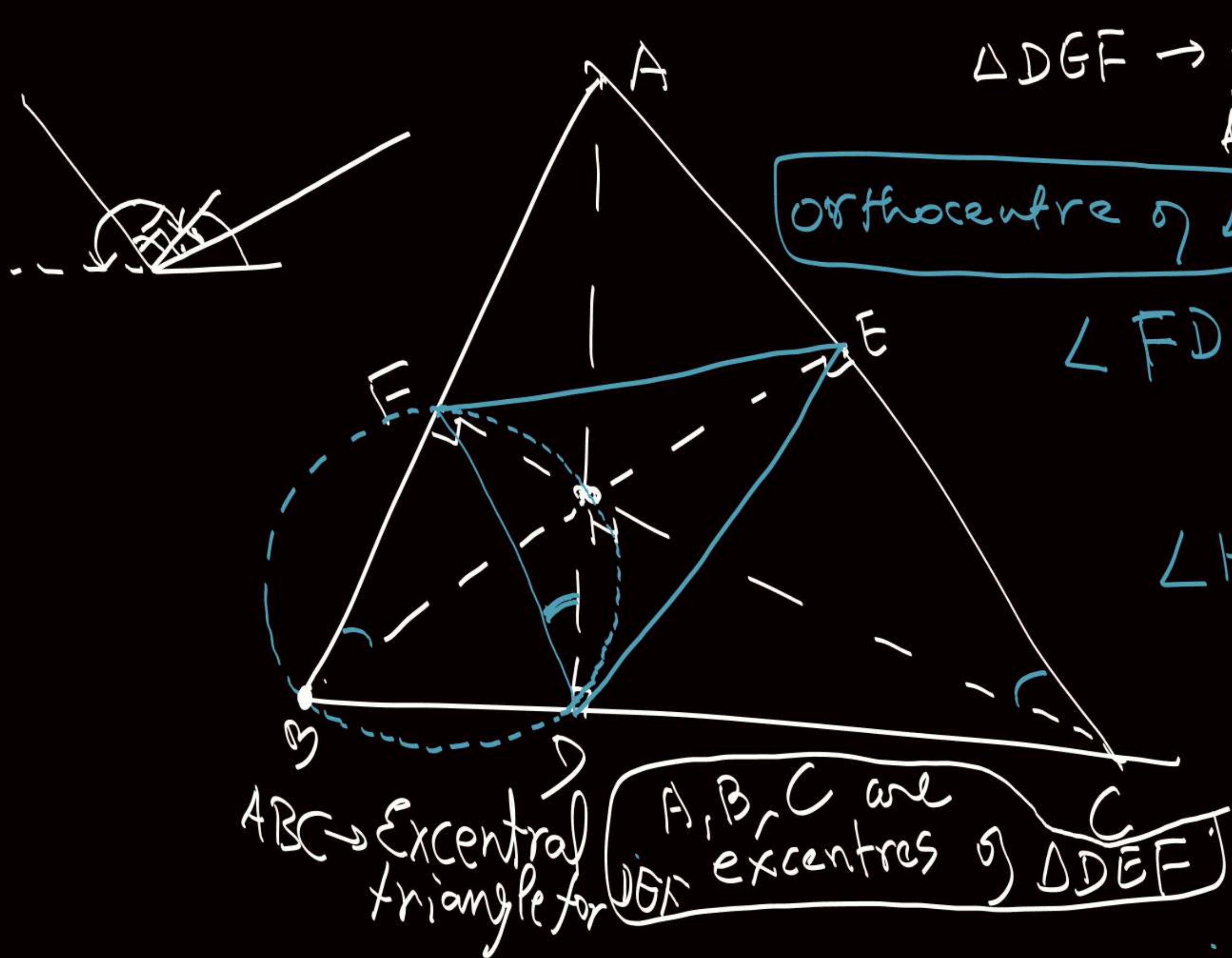
$\triangle BHD$

$$\begin{aligned} BH &= \frac{BD}{\sin C} \\ &= \frac{c \cos B}{\sin C} \\ &= 2R \cos B \end{aligned}$$

Note →



$$HD = DH_1$$



Orthocentre of $\triangle ABC =$ Circumcentre of $\triangle DEF$

$$\angle FDH = \frac{\pi}{2} - A$$

$$\angle HDE = \frac{\pi}{2} - A$$

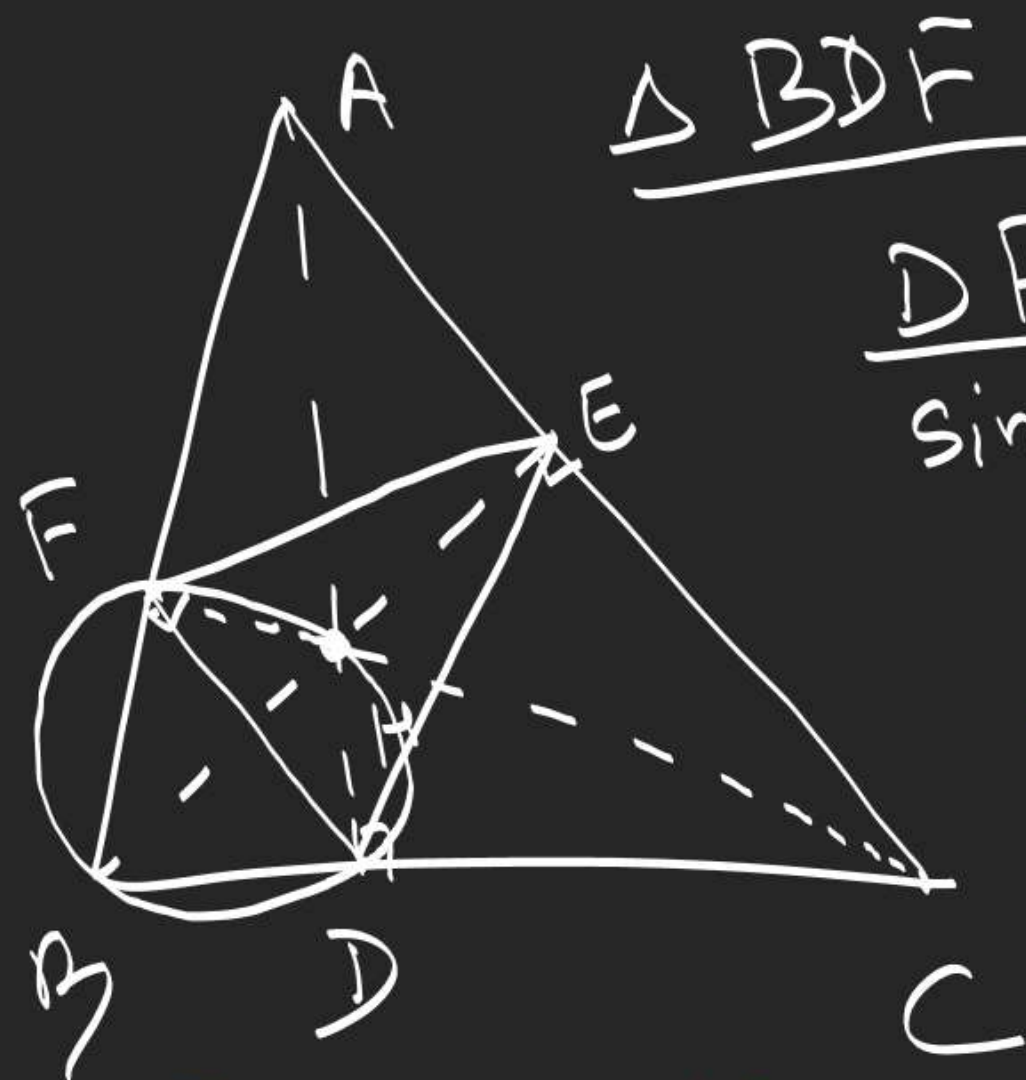
$$\angle D = \pi - 2A$$

$$\angle E = \pi - 2B$$

$$\angle F = \pi - 2C$$

A, B, C are excentres of $\triangle DEF$

$ABC \rightarrow$ Excentral triangle for $\triangle DEF$



$\triangle BDF$

$$\frac{DF}{\sin B} = 2R_{BDF} = BH$$

$$= 2R \cos B$$

$$DF = R \sin 2B$$

$$DE = R \sin 2C$$

$$EF = R \sin 2A$$

$$2R_{DEF} = \frac{DF}{\sin E} = \frac{R \sin 2B}{\sin(\pi - 2B)} = R$$

$$R_{DEF} = \frac{1}{2} R$$

$$\underline{\Sigma x \rightarrow 37}$$

1, 2, 18, 20, 21, 23,
24, 25

S \rightarrow area of ABC

$$\Sigma x = 36 \rightarrow 1, 3, 5, 8, 6$$