

DPP 1-2, 4, 8.

$$Q \lim_{x \rightarrow 1} (1-x + [x-1] + [1-x]) = ?$$

LHL

$$\lim_{h \rightarrow 0} (x - (x-h) + [x-h-x] + [x-(x-h)])$$

$$\lim_{h \rightarrow 0} (h + [0-h] + [0+h])$$

$$\lim_{h \rightarrow 0} [h] + (-1) + 0 = 0 - 1 = -1$$

RHL

$$\lim_{h \rightarrow 0} (x - (x+h) + [x+h-x] + [x-(x+h)])$$

$$\lim_{h \rightarrow 0} (-h + [0+h] + [0-h])$$

$$\lim_{h \rightarrow 0} -h + 0 + -1$$

-1

$$\therefore \lim_{x \rightarrow 1} (1-x + [1-x] + [x-1]) = -1$$

LIMIT

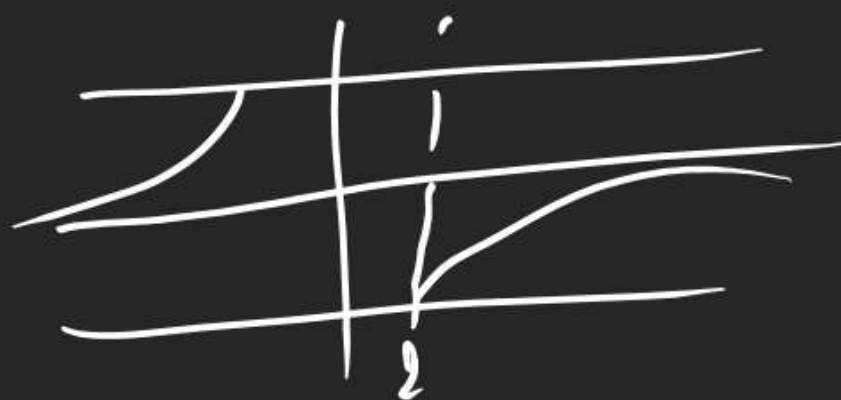
$$Q \lim_{x \rightarrow \infty} \sec^{-1}\left(\frac{x}{x+1}\right) = \text{Not Defined}$$

$$x < x+1$$

$$\frac{x}{x+1} < 1$$

$$\sec^{-1}(<1)$$

Not in Domain



$$Q \lim_{x \rightarrow 0^-} \frac{x([x] + |x|) \sin[x]}{|x|} \quad \begin{matrix} \text{Main} \\ \text{H.L. Demanded} \end{matrix} \quad \begin{matrix} -\sin 1 \\ \sin 1 \\ 0 \end{matrix}$$

$$x = -h$$

$$\lim_{h \rightarrow 0} \frac{-h([0-h] + |-h|) \sin[0-h]}{|-h|}$$

$$\lim_{h \rightarrow 0} \frac{-x(-1+h) \sin(-1)}{1}$$

$$\lim_{h \rightarrow 0} -(1-h) \cdot \sin(1) = -(1-0) \sin 1 = -\sin 1$$

LIMIT

Q $\lim_{x \rightarrow 1^+} \frac{(1 - |x| + \sin |1-x|) \sin\left(\frac{\pi}{2}[1-x]\right)}{|1-x| [1-x]}$

Main $x \rightarrow 1^+$

RHL Demanded

$$x = 1+h$$

$$\lim_{h \rightarrow 0} \frac{(1 - (1+h) + \sin |x - (x+h)|) \sin\left(\frac{\pi}{2}[x - (x+h)]\right)}{[x - (x+h)] [x - (x+h)]}$$

$$\lim_{h \rightarrow 0} \frac{(1 - (1+h) + \sin(h)) \sin\left(\frac{\pi}{2}[0-h]\right)}{[-h] [0-h]}$$

$$\lim_{h \rightarrow 0} \frac{(-h + \sin h) \sin\left(-\frac{\pi}{2}\right)}{h (-1)} = \frac{-1(-h + \sin h)}{-h} = \lim_{h \rightarrow 0} \frac{h - \sin h}{-h} = \lim_{h \rightarrow 0} \boxed{-1} + \cancel{\frac{\sin h}{h}}$$

A) 0 Q-1
B) DNE D) 1

I hode Dintk yad Karlo

$$1) \lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

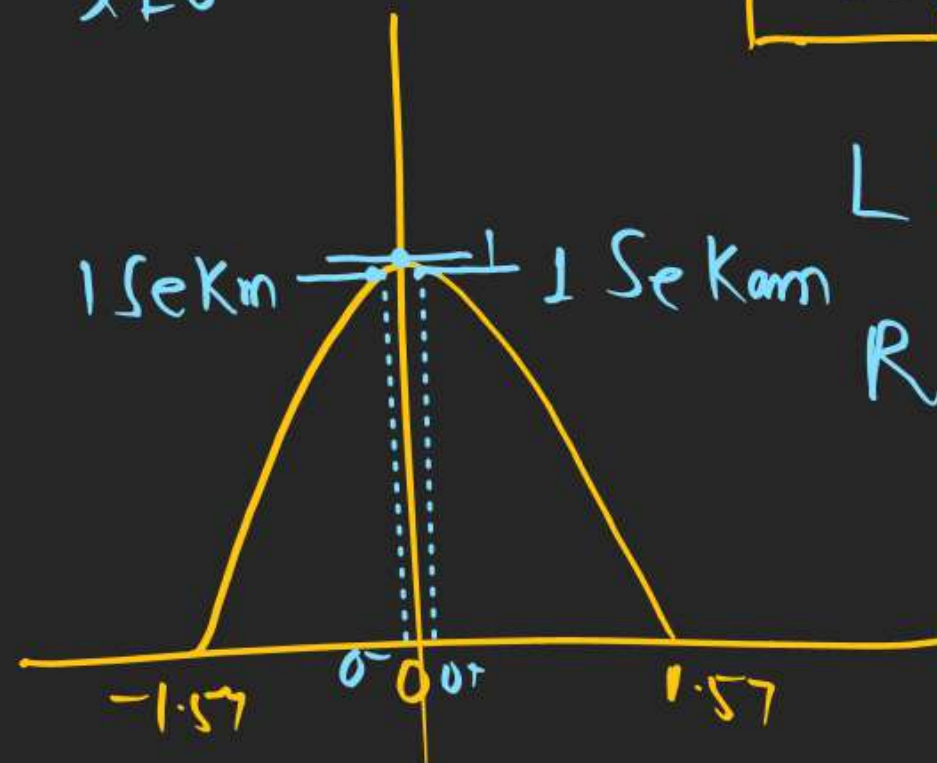
$$2) \lim_{x \rightarrow 0} \frac{\tan x}{x} = 1$$

$$-1 + 1 = 0$$

LIMIT

$$\textcircled{Q} \lim_{\substack{x \rightarrow 0 \\ x \neq 0}} [\cos x]$$

[Trigo] then use graph at given Limit

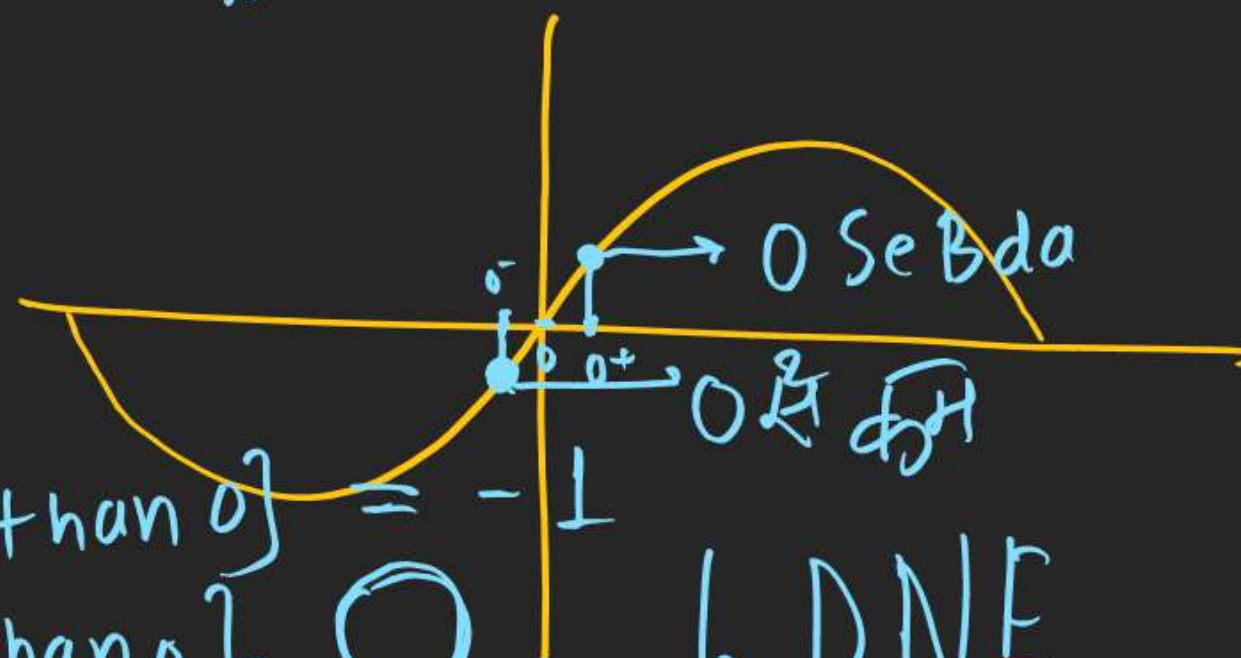


$$LHL = [\cos(0-h)] = [\text{less than } 1] = 0$$

$$RHL = [\cos(0+h)] = [\text{less than } 1] = 0$$

$$\therefore \lim_{x \rightarrow 0} [\cos x] = 0$$

$$\textcircled{Q} \lim_{\substack{x \rightarrow 0 \\ x \neq 0}} [\sin x]$$



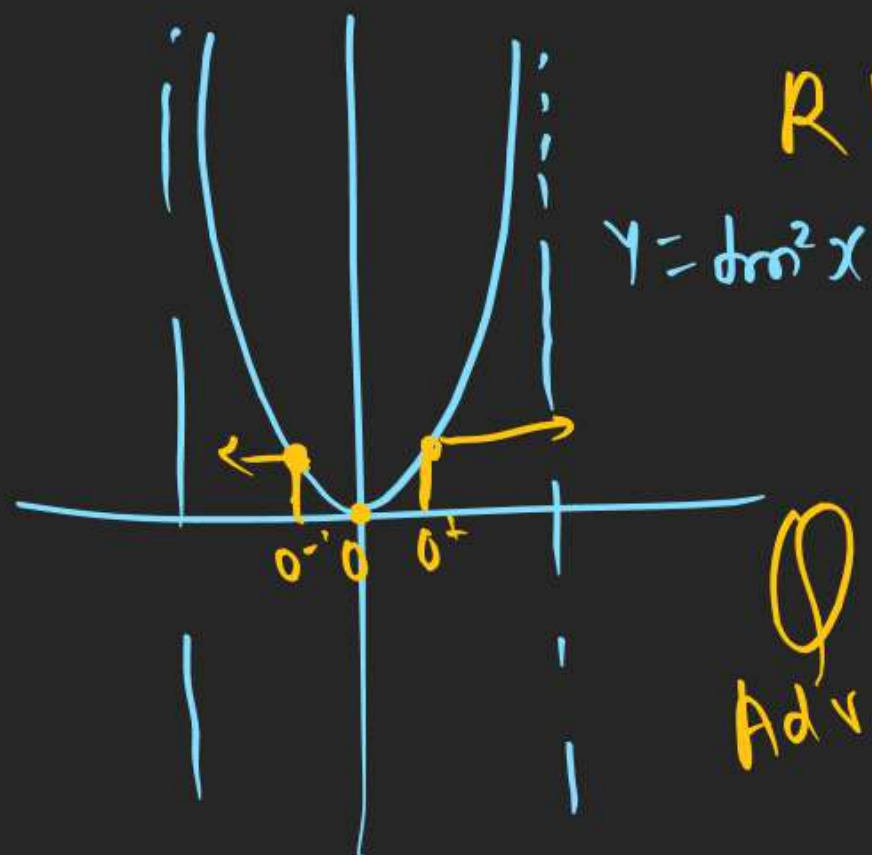
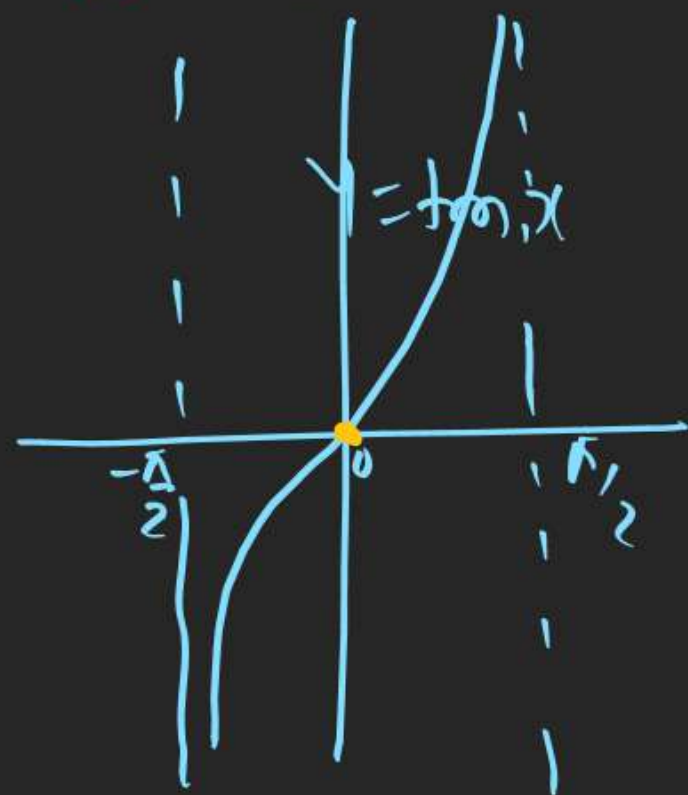
$$LHL = [\sin(0-h)] = [\text{less than } 0] = -1$$

$$RHL = [\sin(0+h)] = [\text{greater than } 0] = 0$$

L DNE

LIMIT

$$Q \lim_{x \rightarrow 0} [\tan^2 x]$$



$$LHL = [\tan^2(0-h)] = [\tan^2(-h)] = 0$$

$$RHL = [\tan^2(0+h)] = [\tan^2(h)] = 0$$

$$\lim_{x \rightarrow 0} [\tan^2 x] = 0$$

Q
Adv.

(check cont^y of $y = [\tan^2 x]$ at $x=0$)
Next chapter

$$\left. \begin{array}{l} LHL = [\tan^2(0-h)] = 0 \\ RHL = [\tan^2(0+h)] = 0 \\ f(0) = [0] = 0 \end{array} \right\} \begin{array}{l} \text{fxn is} \\ \text{cont} \end{array}$$

LIMIT

Q $\lim_{x \rightarrow 0} \frac{\sin(\cos x)}{1 + [\cos x]}$

Sheets $x \rightarrow 0$

$$\lim_{x \rightarrow 0} [\cos x] = 0$$

$$\frac{\sin 0}{1+0} = \frac{0}{1} = 0$$

HW Q $\lim_{x \rightarrow 2^-} [2-x] + [x-2] - x$

(-3)

Ans of L is Normal one \Rightarrow L D E

$$\Rightarrow \text{LHL} = \text{RHL} \Rightarrow \left| \frac{1}{\lambda} \right| = \left| \frac{1}{\lambda-1} \right| \Rightarrow |\lambda| = |\lambda-1|$$

$$\begin{aligned} \lambda &= \lambda-1 \\ 0 &= -1 \end{aligned}$$

$$\begin{aligned} \lambda &= -(\lambda-1) \\ 2\lambda &= 1 \Rightarrow \lambda = \frac{1}{2} \end{aligned}$$

Q [] If \forall for some $\lambda \in \mathbb{R} - \{0, 1\}$

Main $\lim_{x \rightarrow 0} \left| \frac{1-x+|x|}{\lambda-x+[\bar{x}]} \right| = L$ then $L = ?$

$\frac{1}{2}$
0
2
1

LHL $\lim_{h \rightarrow 0} \left| \frac{1-(-h)+|-h|}{\lambda-(-h)+[-h]} \right| = L$

$$\lim_{h \rightarrow 0} \left| \frac{1+h+h}{\lambda+h-1} \right| = L \Rightarrow \left| \frac{1}{\lambda-1} \right| = L \rightarrow 2$$

RHL $\lim_{h \rightarrow 0} \left| \frac{1-h+|h|}{\lambda-h+[\bar{h}]} \right| = L$

$$\lim_{h \rightarrow 0} \left| \frac{1-h+h}{\lambda-h+0} \right| = L \Rightarrow \left| \frac{1}{\lambda} \right| = L$$

$$L = \left| \frac{1}{\frac{1}{2}} \right| = 2$$

LIMIT

Q $\lim_{x \rightarrow 8} \{x\}$ Aakashan

LHL
 $x \rightarrow 8^-$

$\lim_{h \rightarrow 0} \{8-h\}$

$\{-h\}$

$\lim_{h \rightarrow 0} 1-h$

$1-0$
 $= 1$

RHL
 $x \rightarrow 8^+$

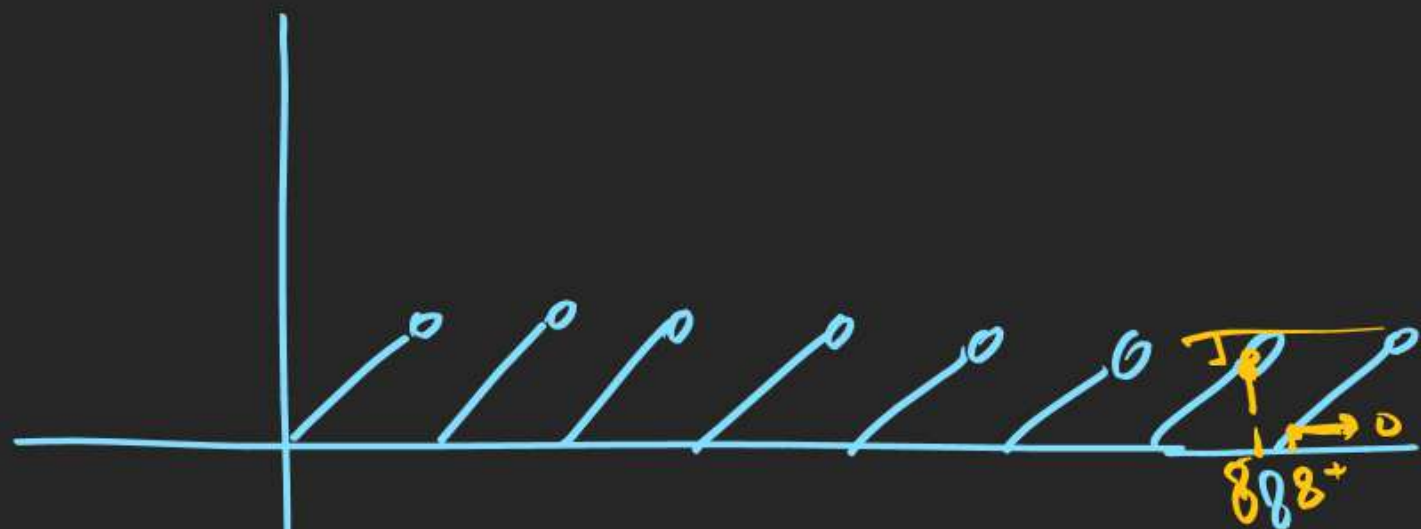
$\lim_{h \rightarrow 0} \{8+h\}$

$\{h\}$

$= \lim_{h \rightarrow 0} h$

$= 0$

$\therefore \text{LHL} = \text{RHL}$
LDNE



Q $\lim_{x \rightarrow 2^+} \frac{\{x\} \ln(x-2)}{(x-2)^2} = ?$

RHL Demanded
 $x = 2+h$

$\lim_{h \rightarrow 0} \frac{\{2+h\} \ln(x+h-x)}{(x+h-x)^2} = \lim_{h \rightarrow 0} \frac{\{h\} \ln h}{h^2}$

$\lim_{h \rightarrow 0} \frac{h/x \ln h}{h^2} = 1$

LIMIT

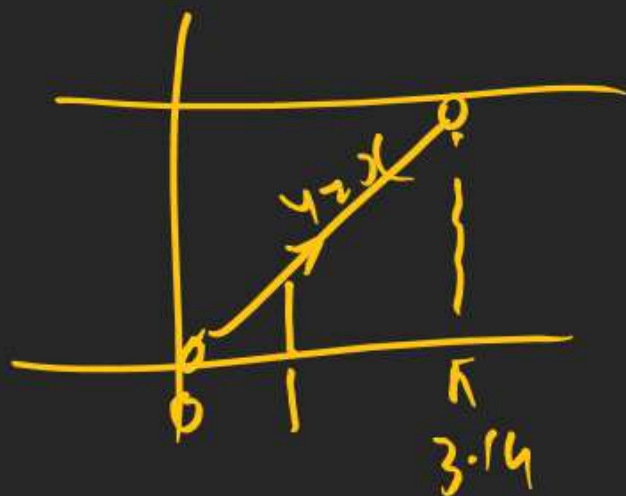
$$Q \lim_{x \rightarrow 0^-} (\cot^{-1}(\{x\}) (\cot \{x\})) = ?$$

$$x = 0 - h \lim_{h \rightarrow 0} (\cot^{-1}(\{-h\}) (\cot \{-h\}))$$

$$\lim_{h \rightarrow 0} \cot^{-1}(1-h) (\cot(1-h))$$

$$(\cot^{-1}(1-0) (\cot(1-0)))$$

$$(\cot^{-1}(\cot 1)) = 1$$



$$\{-h\} = 1-h$$

$$\{-.2\} = 1-.2$$

$$\{.2\} = .2$$

$$Q \lim_{x \rightarrow 0^+} \frac{\tan^2 \{x\}}{x^2 - [x]^2}$$

$$x = 0 + h$$

$$\lim_{h \rightarrow 0} \frac{\tan^2 \{h\}}{h^2 - [0+h]^2}$$

$$\lim_{h \rightarrow 0} \frac{\tan^2 h}{h^2 - 0}$$

$$= \lim_{h \rightarrow 0} \left(\frac{\tan h}{h} \right)^2 = 1^2 = 1$$

LIMIT

Q If

Defined
fxn.

$$f(x) = \begin{cases} \frac{\tan^2\{x\}}{x^2 - [x]^2} & x > 0 \\ 1 & x = 0 \\ \cot^{-1}(\{x\}) \cot(\{x\}) & x < 0 \end{cases}$$

(Note: The first case is labeled RHL, the second case is labeled 1, and the third case is labeled LHL.)

Next Chapter Aise Qs Se Bhra

Pda Rahega

$$\left. \begin{array}{l} LHL = 1 \\ RHL = 1 \\ f(0) = 1 \end{array} \right\} \text{Cont's at } x=0$$
LHL
RHLthen find $\lim_{x \rightarrow 0} f(x) = ?$ LHL $\boxed{x = 0 - h} \rightarrow x < 0$

$$\lim_{x \rightarrow 0^-} \cot^{-1}(\{x\}) \cot(\{x\}) = 1$$

RHL $\boxed{x = 0 + h} \rightarrow x > 0$

$$\lim_{x \rightarrow 0^+} \frac{\tan^2\{x\}}{x^2 - [x]^2} = 1$$

$$LHL = RHL$$

$$\lim_{x \rightarrow 0} f(x) = 1$$

$$Q \quad f(x) = \begin{cases} x-1 & x \geq 1 \\ 2x^2-2 & x < 1 \end{cases}, \quad g(x) = \begin{cases} x+1 & x > 0 \\ -x^2+1 & x \leq 0 \end{cases} \quad \& \quad r(x) = |x|$$

$$r(0-h) = |-h|$$

$$\therefore \lim_{x \rightarrow 0} f(g(r(x))) \quad \text{find} \quad \lim_{x \rightarrow 0} f(g(|r(x)|))$$

$$\text{LHL} \quad \lim_{x \rightarrow 0^-} f(g(r(0-h)))$$

$$\lim_{h \rightarrow 0} f(g(|-h|))$$

$$\lim_{h \rightarrow 0} f(g(|h|)) \quad \begin{matrix} \nearrow 0 \notin \text{Bda.} \\ \nearrow f \nmid 1 \notin \text{Bda} \end{matrix}$$

$$\lim_{h \rightarrow 0} f(h+1) = (h+1) - 1 = 0$$

$$\text{RHL} \quad \lim_{x \rightarrow 0^+} f(g(r(0+h)))$$

$$\lim_{h \rightarrow 0} f(g(|h|))$$

$$\lim_{h \rightarrow 0} f(g(h)) \quad \begin{matrix} \nearrow 0 \notin \text{Bda} \end{matrix}$$

$$\lim_{h \rightarrow 0} f(h+1) = \lim_{h \rightarrow 0} (h+1) - 1$$

$$= 0$$

LIMIT

$$Q \lim_{x \rightarrow 1} \left[x \left[\frac{1}{x} \right] \right]$$

$$LHL \ x = 1 - h$$

$$\lim_{h \rightarrow 0} \left[(1-h) \left[\frac{1}{1-h} \right] \right]$$

\swarrow
1 is Bda

$$[(1-h) \times 1]$$

$$[1-h] = 0$$

$$RHL \ x = 1 + h$$

$$\lim_{h \rightarrow 0} \left[(1+h) \left[\frac{1}{1+h} \right] \right]$$

\swarrow
1 is Karm

$$[(1+h) \times 0]$$

$$[0] = 0$$

$$\therefore \lim_{x \rightarrow 1} \left[x \left[\frac{1}{x} \right] \right] = 0$$

Concept

$$\frac{1}{9} = 1 \text{ is Bda.}$$

$$\frac{10}{9} = "$$

$$\frac{1}{1.1} = 1 \text{ is Karm}$$

$$\frac{10}{11} = "$$

$$\lim_{t \rightarrow 0} \left(\frac{23}{t^2} \right) \rightarrow \infty$$

Q Difficult Make graph of f(x).

$$f(x) = \lim_{t \rightarrow 0} \frac{2x}{\pi} \cot^{-1} \frac{x}{t^2} = ?$$

$$\lim_{t \rightarrow 0} \left(\frac{-23}{t^2} \right) \rightarrow -\infty$$

$$x = -ve$$

$$\lim_{t \rightarrow 0} \frac{2x}{\pi} \cot^{-1} \left(\frac{x}{t^2} \right)$$

$$\frac{2x}{\pi} \cdot \cot^{-1}(-\infty)$$

$$y = \frac{2x}{\pi} \times \frac{\pi}{2} \quad \boxed{y = -2x}$$

$$x = +ve$$

$$y = \lim_{t \rightarrow 0} \frac{2x}{\pi} \cot^{-1} \left(\frac{x}{t^2} \right)$$

$$\frac{2x}{\pi} \cdot \cot^{-1}(\infty)$$

$$y = \frac{2x}{\pi} \times 0 \Rightarrow y = 0$$

$$x = 0$$

$$y = \frac{2x}{\pi} \cot^{-1} \left(\frac{0}{t^2} \right)$$

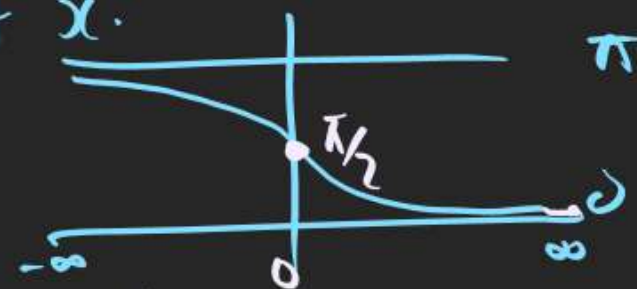
$$\lim_{t \rightarrow 0} \frac{2x}{\pi} \cot^{-1}(0)$$

$$\frac{2x}{\pi} \cdot \frac{\pi}{2} = x = 0$$

thought \rightarrow here we have 2 variables. x & t

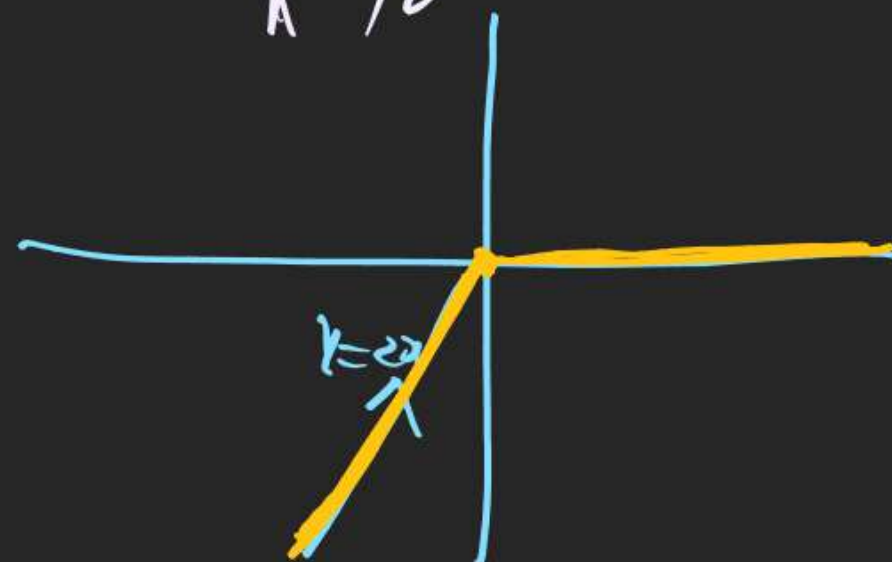
2) $t \rightarrow 0$ given But we do not have.

Idea about x .



3)

$x = -ve$
 $x = +ve$
 \rightarrow



Q $\lim_{x \rightarrow 0^+} \frac{x}{a} \left[\frac{b}{x} \right] \quad a, b \neq 0$

$\lim_{h \rightarrow 0} \frac{h}{a} \left[\frac{b}{h} \right] \quad 0 \times \infty$
 $[x] = x - \{x\}$
 $\{x\} \in [0, 1)$

(M1) $\lim_{h \rightarrow 0} \frac{h}{a} \left(\frac{b}{h} - \left\{ \frac{b}{h} \right\} \right)$

$\frac{b}{a} - \lim_{h \rightarrow 0} \frac{h}{a} \left\{ \frac{b}{h} \right\}$

$\frac{b}{a} - \lim_{h \rightarrow 0} \frac{h}{a} \times (\text{any value bet}^n 0 \text{ to } 1)$

$\frac{b}{a} - \frac{0}{a} \times (0 \text{ to } 1) = \frac{b}{a} - 0 = \frac{b}{a}$

M2 funda.

$\lim_{x \rightarrow \infty} [x] = x$

$\lim_{h \rightarrow 0} \frac{h}{a} \left[\frac{b}{h} \right] \rightarrow \text{Indicate to } \infty$

$\lim_{h \rightarrow 0} \frac{K}{a} \times \frac{b}{K}$

Main

Q $\lim_{x \rightarrow 0^+} x \left(\left[\frac{1}{x} \right] + \left[\frac{2}{x} \right] + \dots + \left[\frac{15}{x} \right] \right)$

$\Rightarrow x \left(\frac{1}{x} + \frac{2}{x} + \frac{3}{x} + \dots + \frac{15}{x} \right) = 1 + 2 + 3 + \dots + 15$
 $= \frac{(15)(16)}{2} = 120$

DPP2

Sur \rightarrow Onto ✓
 \times Inj \rightarrow 1-2-1

$$f(x) = \tan^{-1} x$$

$$f'(x) = \frac{1}{1+x^2}$$

$$1) f: \mathbb{R} \rightarrow \left[\frac{\pi}{6}, \frac{\pi}{4} \right) \quad f(x) = \tan^{-1} \left(\frac{x^2+1}{x^2+\sqrt{3}} \right)$$

$$y = \frac{x^2+1}{x^2+\sqrt{3}} \rightarrow \frac{\phi}{\phi}$$

$$x^2 y + \sqrt{3} y = x^2 + 1$$

$$x^2 (y-1) = 1 - \sqrt{3} y$$

$$\textcircled{x^2} = \frac{1 - \sqrt{3} y}{y-1} \geq 0$$

$$\frac{(\sqrt{3} y - 1)}{(y-1)} \leq 0$$

+	-	+
1	1	
$\frac{1}{\sqrt{3}}$		

$$f'(x) = \frac{1}{1 + \left(\frac{x^2+1}{x^2+\sqrt{3}} \right)^2} \times \frac{(x^2+\sqrt{3})2x - (x^2+1)2x}{(x^2+\sqrt{3})^2}$$

$$= \frac{1}{1 + \left(\frac{x^2+1}{x^2+\sqrt{3}} \right)^2} \times \frac{2x^3 + 2\sqrt{3}x - 2x^3 - 2x}{(x^2+\sqrt{3})^2}$$

$$f'(x) = \frac{1 +}{+ \textcircled{+}} \times \left(\frac{\textcircled{+} 2x(\sqrt{3}-1)}{(x^2+\sqrt{3})^2 \textcircled{+}} \right)$$

$$f'(x) \begin{cases} \nearrow +ve \\ \searrow -ve \end{cases}$$

N/2

$$y \in \left[\frac{1}{\sqrt{3}}, 1 \right)$$

$$\frac{x^2+1}{x^2+\sqrt{3}} \in \left[\frac{1}{\sqrt{3}}, 1 \right)$$

$$\tan^{-1} \left(\frac{x^2+1}{x^2+\sqrt{3}} \right) \in \left[\tan^{-1} \frac{1}{\sqrt{3}}, \tan^{-1} 1 \right)$$

$$\in \left[\frac{\pi}{6}, \frac{\pi}{4} \right)$$

$$Q4 \text{ } \ln \left(\underbrace{(\log x)^2 - 2\log x + 2}_{(1^2 - 2 \cdot 1 + 2)} \right) + \ln \left(\underbrace{(\log x)^2 - 2\log x + 2}_{(1^2 - 2 \cdot 1 + 2)} \right) + \ln \left(\underbrace{(\log x)^2 - 2\log x + 2}_{(1^2 - 2 \cdot 1 + 2)} \right)$$

$$\ln(1) + \ln(1) + \ln(1)$$

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{4} = 1$$

$$P = \frac{7}{4}$$

$$-1 \leq (\log x)^2 - 2\log x + 2 \leq 1$$

$$-1 \leq (\log_{10} x - 1)^2 + 1 \leq 1$$

$$\log_{10} x - 1 = 0$$

$$\log_{10} x = 1$$

$$\underline{x = 10}$$