

Total Probability Theorem.

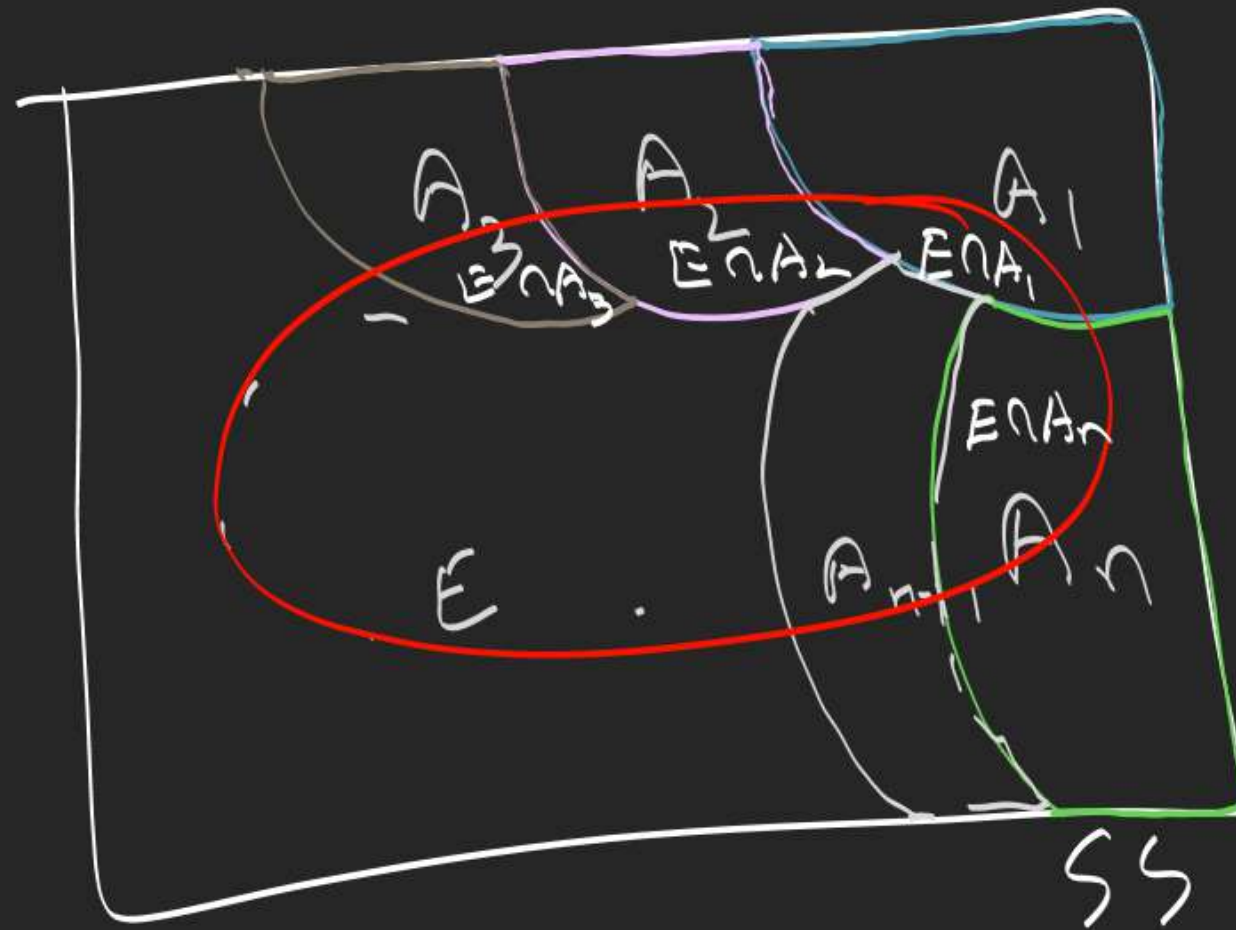
Let an event E can only occur with one of the ' n ' mutually exclusive and exhaustive events $A_1, A_2, A_3, \dots, A_n$, then

$$P(E) = \sum_{i=1}^n P(A_i) P(E/A_i)$$

✓

$$\frac{\text{Baye's theorem}}{P(A_3/E)} =$$

$$\frac{P(A_3 \cap E)}{P(E)} = \frac{P(A_3)P(E/A_3)}{\sum_{i=1}^n P(A_i)P(E/A_i)}$$



$$P(E) = P(E \cap A_1) + P(E \cap A_2) + P(E \cap A_3) + \dots + P(E \cap A_n)$$

$$P(E) = P(A_1)P(E/A_1) + P(A_2)P(E/A_2) + P(A_3)P(E/A_3) + \dots + P(A_n)P(E/A_n)$$

Baye's theorem

$$P(A_k/E) = \frac{P(A_k)P(E/A_k)}{\sum_{i=1}^n P(A_i)P(E/A_i)}$$

$$k=1, 2, \dots, n$$

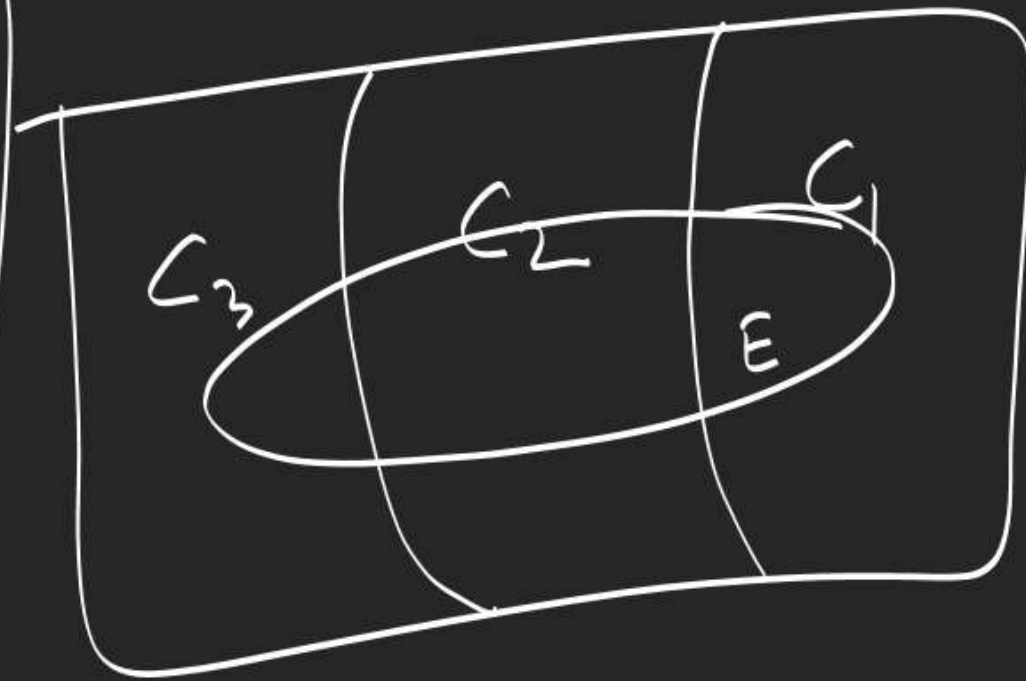
$$P(E) = \frac{1}{3} \times \left(\frac{1}{3} + \frac{2}{5} + \frac{3}{7} \right)$$

\downarrow
 $P(E/C_1)$

 E/C_2
 E/C_3

$$P(C_1) = P(C_2) = P(C_3) = \frac{1}{3}$$

 $C_i \rightarrow$ comp i selected.

 $E \rightarrow$ drawn coin is 10 Re.


2. $(0.4) \left(\frac{{}^{11}C_1 \times 1}{{}^{20}C_2} \right) + (0.6) \left(\frac{{}^{11}C_2 \times 1}{{}^{20}C_3} \right)$



$0.4 \left(\frac{{}^2C_1 {}^{18}C_{10}}{{}^{20}C_{11}} \times \frac{1}{9} \right) + 0.6 \left(\frac{{}^3C_2 {}^{17}C_9}{{}^{20}C_{11}} \times \frac{1}{9} \right)$

$0.4 \left(\frac{2}{20} \times \frac{18}{19} \times \frac{17}{18} \times \dots \times \frac{9}{10} \times \frac{1}{9} \times {}^{11}C_1 \right) + 0.6 \left(\frac{3}{20} \times \frac{2}{19} \times \frac{17}{18} \times \frac{16}{17} \times \dots \times \frac{9}{10} \times \frac{1}{9} \times {}^{11}C_2 \right)$

DNN...ND
NDN...ND

DDNNN...ND

Binomial Probability