

$$f(n) < f(2n) < f(3n)$$

$$\boxed{\lim_{n \rightarrow \infty} \frac{f(2n)}{f(n)} = 1}$$

$$\frac{f(n)}{f(n)} < \frac{f(2n)}{f(n)} < \frac{f(3n)}{f(n)}$$

$$\lim_{n \rightarrow \infty} \frac{f(cn)}{f(n)} = ? \quad c > 0$$

$$\frac{f(n)}{f(n)} < \frac{f(2^n n)}{f(n)} < \frac{f(3^n n)}{f(n)}$$

$\lim_{n \rightarrow \infty} \frac{f(2^n n)}{f(n)} = 1$ $\lim_{n \rightarrow \infty} \frac{f(3^n n)}{f(n)} = 1$

$$\frac{1}{2^n} < c < \frac{1}{2^{n-1}}$$

Let $c > 1 \Rightarrow 2^{n-1} < c < 2^n$

$$f(2^{n-1}n) < f(cn) < f(2^n n)$$

$$\lim_{n \rightarrow \infty} \frac{f(2^n n)}{f(2^n n)} = 1$$

$$\lim_{n \rightarrow \infty} \frac{f(2^3 n)}{f(2^2 n)} = 1$$

$$\begin{aligned}
 & \sum_{k=1}^{15} k \\
 & \chi \left[\frac{1}{\chi} \right] \\
 & \lim_{n \rightarrow 0} \left(\frac{\chi}{\chi} \right) - \left(\frac{\chi}{\chi} \right) \\
 & \cot \pi \left(1 - \sin \pi \right) \\
 & \tan \left(\frac{\pi}{2} - \pi \right) \left(1 - \cos \left(\frac{\pi}{2} - \pi \right) \right) \\
 & 2^3 \left(\frac{\pi}{2} - \pi \right) \left(\frac{\pi}{2} - \pi \right)^2 \\
 & \cot \pi - \cos \pi
 \end{aligned}$$

1:12:

$$[-2, 0] \cup [k, \infty) \quad k > 0.$$

3:

$$\phi: \begin{cases} k \in [-2, 2] \\ x > 0 \text{ and } k \in \mathbb{R} \end{cases}$$

$$f(w) =$$

$$\sqrt{w^2 + kw + 1}$$

$$\lim_{w \rightarrow 0} f(w) = \lim_{w \rightarrow 0} \sqrt{w^2 + kw + 1} = \sqrt{k+1}$$

$$k = ?$$

3: $\lim_{x \rightarrow 0}$

$$\frac{e^x(e^x + e^{-x}) - (x+1)(e^x + e^{-x})}{x^2}$$

$$\frac{x^2}{(e^x - 1)} = \frac{x^2}{\frac{x^2}{2}} = 1$$

$$e^x - x - 1$$

$$\frac{e^x - 1}{x}$$

$$\text{Q: } g(x) = \csc(2x) + \csc^2(2x) + \csc^3(2x) + \dots + \csc^{n-1}(2x) + \csc^n(2x) + \cot(2x)$$

$\vdash \cot x$

$$\text{RHL} = \lim_{x \rightarrow 0^+} \left((\cos x)^{\cot x} + (\sec x)^{\csc x} + 1 \right) = 2 + 1 = 3$$

$$\rho = \phi$$

$$\text{LHL} = \lim_{x \rightarrow 0^-} \frac{e^x + e^{-x} - 2 + 2(1 - \cos x)}{x^2 \sin x} = 2$$

Let $f(x) = \lim_{n \rightarrow \infty} \frac{x^{2n-1} + ax^2 + bx}{x^{2n} + 1}$ = $\begin{cases} n \in \mathbb{N} \\ ax^2 + bx, |x| < 1 \\ \frac{1}{x}, |x| > 1 \end{cases}$

is continuous $\forall x \in \mathbb{R}$, find a, b .

Cont. At $x=1$

$$\text{LHL} = \lim_{x \rightarrow 1^-} \frac{ax^2 + bx}{1} = a+b$$

$$a=0, b=1$$

$$\text{RHL} = \lim_{x \rightarrow 1^+} \frac{1}{x} = 1$$

$$f(x) = \frac{1+a+b}{2}$$

$$\text{At } x=-1$$

$$\text{LHL} = \lim_{x \rightarrow -1^-} \frac{1+a+b}{2}$$

$$\text{at } x=-1$$

$$\text{RHL} = \lim_{x \rightarrow -1^+} \frac{-1+a-b}{2}$$

Cont. $x=-1$

$$\begin{aligned} a+b &= 1 \\ a-b &= -1 \end{aligned}$$

$$\text{LHL} = -1$$

$$\begin{aligned} \text{RHL} &\approx 0 \\ f(-1) &= \frac{a-b-1}{2} \end{aligned}$$

Q. Let $f(x) = \begin{cases} \frac{(a^x - 1)}{\sin x} \left(\frac{b \sin x - \sin bx}{x(\cos x - \cos bx)} \right)^n & , x > 0 \\ \frac{b(b^x - 1) + (bx - \sin bx)^3}{((\cos x - 1) + (1 - \frac{\sin bx}{bx}) b^2)^3} & , x < 0 \end{cases}$

LHL = $\frac{b-a}{b-a} = 1$

is continuous at $x=0$. Obtain $f(0)$ and a relation

between a, b & n :

$$\ln a \left(\frac{-\frac{b}{b} + \frac{b}{b}}{-\frac{1}{2} + \frac{b^2}{2}} \right)^n$$

$$f(0) = \lim_{x \rightarrow 0} f(x) = \ln a \left(\frac{b}{3} \right)^n$$

At $5:45 \text{ pm}$

L. Let $f(x+y) = f(x)f(y)$ $\forall x, y \in \mathbb{R}$ and

$f(x) = 1 + g(x)G(x)$, where $\lim_{x \rightarrow 0} g(x) = 0$ &

$\lim_{x \rightarrow 0} G(x)$ exists. P.T. $f(x)$ is continuous

$\forall x \in \mathbb{R}$:

cont. at $x=a$

$a \in \mathbb{R}$

$LHL = RHL = f(a)$

cont. at $x=a$.

$$LHL = \lim_{h \rightarrow 0} f(a-h) = f(a) \lim_{h \rightarrow 0} f(-h) = f(a) \lim_{h \rightarrow 0} (1 + g(-h)G(h))$$

$$RHL = \lim_{h \rightarrow 0} f(a+h) = f(a) \lim_{h \rightarrow 0} f(h) = f(a) \lim_{h \rightarrow 0} (1 + g(h)G(h))$$