

Khushiyan

HW1

hi

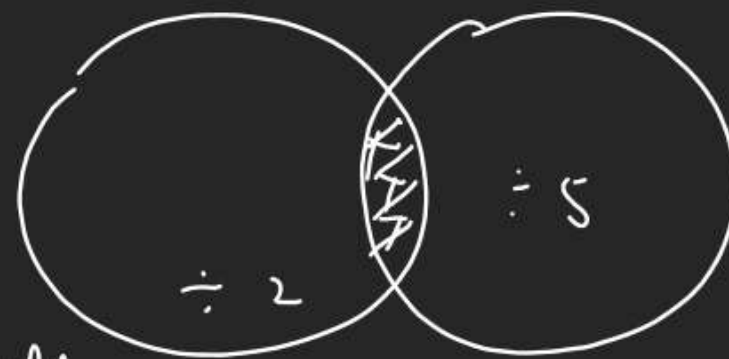
Khushiyan

Module

Flipkart → Amazon → 379

Q5

F Moduli



$$\{2+4+6+\dots+100\} + \{5+10+\dots+100\}$$

$$- 2\{10+20+\dots+100\}$$

$$Q3 \quad \log_4 2 + \log_4 4 + \log_4 8 + \dots + \log_4 2^n$$

Q4 ✓

$$= \log_4 \{2 \times 4 \times 8 \times \dots \times 2^n\}$$

Q5 ✓

$$= \log_4 \{2^1 \cdot 2^2 \cdot 2^3 \cdot \dots \cdot 2^n\}$$

Q6 ✓

$$= \log_4 \{2^{(1+2+3+\dots+n)}\}$$

Q7 ✓

$$= \frac{(1+2+3+\dots+n)}{2} \left( \frac{\log_4 2}{\log_4 4} \right) = \frac{(n)(n+1)}{4}$$

Q 8 If  $1, 2, 3, \dots$  are  $1^{\text{st}}$  terms,  $1, 3, 5, \dots$  are com. diff

&  $S_1, S_2, S_3, \dots$  are sum of  $n$  terms of  $P$  APs

then  $S_1 + S_2 + S_3 + \dots + S_p = ?$

$S_1 =$  Sum of  $n$  term of an AP whose  $1^{\text{st}}$  term  $= 1$  &  $d = 1$

$S_2 =$  \_\_\_\_\_  $= 2$  &  $d = 3$

$S_3 =$  \_\_\_\_\_  $= 3$  &  $d = 5$

$\vdots$

$S_p =$  \_\_\_\_\_  $= p$  &  $d = (2p-1)$

$$S_1 = \frac{n}{2} [2 \times 1 + (n-1) \times 1]$$

$$S_2 = \frac{n}{2} [2 \times 2 + (n-1) \times 3]$$

$$S_3 = \frac{n}{2} [2 \times 3 + (n-1) \times 5]$$

$\vdots$

$$S_p = \frac{n}{2} [2 \times p + (n-1) \times (2p-1)]$$

$$S_1 + S_2 + \dots + S_p = \frac{n}{2} [2 \times (1+2+3+\dots+p) + (n-1)(1+3+5+\dots+(2p-1))]$$

$$= \frac{n}{2} \left[ 2 \times \frac{p(p+1)}{2} + (n-1)p^2 \right]$$

$$= \frac{n}{2} [p^2 + p + np^2 - p^2] = \frac{np}{2} [n+1] \text{ Ans}$$

Q9 If  $a_1, a_2, a_3, \dots$  are in AP with C.D.  $= d \neq 0$  then the sum of series.

$$\underline{\sin d} \left[ \underline{\csc a_1 \cdot \csc a_2} + \csc a_2 \cdot \csc a_3 + \dots + \csc a_{n-1} \cdot \csc a_n \right]$$

Sol  $d = a_2 - a_1 = a_3 - a_2 = a_4 - a_3 = \dots$

$$\frac{\sin d}{\sin a_1 \cdot \sin a_2} + \frac{\sin d}{\sin a_2 \cdot \sin a_3} + \frac{\sin d}{\sin a_3 \cdot \sin a_4} + \dots + \frac{\sin d}{\sin a_{n-1} \cdot \sin a_n}$$

$$\frac{\sin(a_2 - a_1)}{\sin a_1 \cdot \sin a_2} + \frac{\sin(a_3 - a_2)}{\sin a_2 \cdot \sin a_3} + \frac{\sin(a_4 - a_3)}{\sin a_3 \cdot \sin a_4} + \dots + \frac{\sin(a_n - a_{n-1})}{\sin a_{n-1} \cdot \sin a_n}$$

$$\frac{\sin a_2 \cdot \cos a_1 - \cos a_2 \cdot \sin a_1}{\sin a_1 \cdot \sin a_2} + \frac{\sin a_3 \cdot \cos a_2 - \cos a_3 \cdot \sin a_2}{\sin a_2 \cdot \sin a_3} + \dots + \frac{\sin a_n \cdot \cos a_{n-1} - \cos a_n \cdot \sin a_{n-1}}{\sin a_{n-1} \cdot \sin a_n}$$

$$(\cancel{\cot a_1} - \cancel{\cot a_2}) + (\cancel{\cot a_2} - \cancel{\cot a_3}) + \dots + (\cancel{\cot a_{n-1}} - \cot a_n) = \cot a_1 - \cot a_n$$



let  
(1)  $a^2(b+c), b^2(c+a), c^2(a+b)$  AP

Q16 ✓  $b^2(c+a) - a^2(b+c) = c^2(a+b) - b^2(c+a)$

$$b^2c + b^2a - a^2b - a^2c = c^2a + c^2b - b^2c - b^2a$$

$$(b^2 - a^2) + ba(b-a) = a(c^2 - b^2) + b(c-c^2)$$

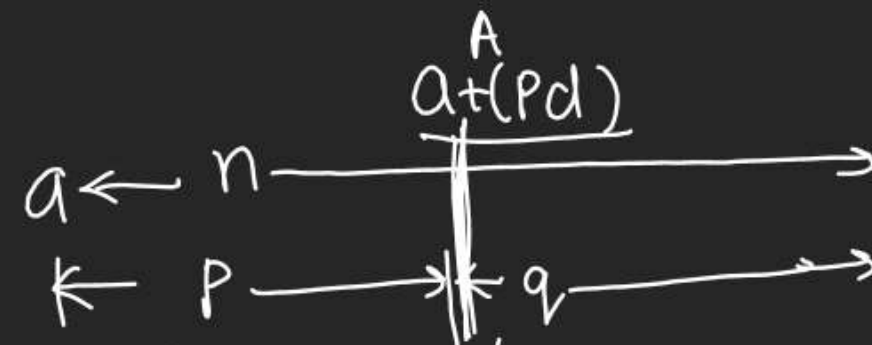
$$(b-a) \{ \cancel{b+ac+ba} \} = (c-b) \{ \cancel{ac+ab+bc} \}$$

$$b-a = c-b$$

$$2b = a+c$$

$$a, b, c \rightarrow AP$$

Q15



$$\leftarrow SP = 0 \rightarrow 0$$

$$\frac{p}{2} [2a + (p-1)d] = 0$$

$$d = \frac{-2a}{(p-1)}$$

$$Sq = \frac{q}{2} [2 \times (a+pd) + (q-1)d]$$

$$\begin{array}{c} \leftarrow 3000 \longrightarrow \\ \leftarrow 1500 \longrightarrow \bigg| 148 + 146 + 144 \dots \end{array}$$

$$148 + 146 + 144 + 142 + \dots - n = \underline{3000}$$

$$\frac{n}{2} [296 + (n-1)(-2)] = 3000$$

Q.E.g  $\rightarrow n = ?$

L-5

Q Supp that all term of AP are Natural No. C.D = Natural

Adv 2015 If Ratio of 1<sup>st</sup> 7 terms to sum of 1<sup>st</sup> 11 terms.

in 6:11 & 7<sup>th</sup> term lies bet<sup>n</sup> 130 to 140

then C.D. = ?

$$\frac{S_7}{S_{11}} = \frac{6}{11} \Rightarrow \frac{\frac{7}{2}[2a+6d]}{\frac{11}{2}[2a+10d]} = \frac{6}{11}$$

$$\Rightarrow 14a + 42d = 12a + 60d$$

$$2a = 18d \Rightarrow \underline{a = 9d}$$

$$130 < T_7 < 140$$

$$130 < a + 6d < 140$$

$$130 < 15d < 140$$

$$8.\dots < d < 9.\dots$$

$$\boxed{d = 9}$$

$$1 \text{ Br} = 1 \rightarrow 1^3 \quad 2 = 8 = (2)^3 \quad 3 \rightarrow 27 = (3)^3$$

Q Show that Sum of all terms of  $n^{\text{th}}$  Bracket of  $(1), (3, 5), (7, 9, 11) \dots$  is?

Sum  $\rightarrow 1^{\text{st}}$  term  
 $\hookrightarrow$  No of term  $= n$   
 $\hookrightarrow$  Com diff  $= 2$

$\uparrow$  1<sup>st</sup> Br  
 $\uparrow$  2<sup>nd</sup> Br  
 $\uparrow$  3<sup>rd</sup> Br

1<sup>st</sup> term = 1

2<sup>nd</sup> Br = 3

3<sup>rd</sup> Br = 7

4<sup>th</sup> Br = 13

5<sup>th</sup> Br = 21

$$S = 1 + 3 + 7 + 13 + 21 \dots T_n$$

$$S = 1 + 3 + 7 + 13 \dots T_{n-1} + T_n$$

$$0 = 1 + 2 + 4 + 6 + 8 + \dots + 2(n-1) - T_n$$

$$T_n = 1 + 2\{1 + 2 + 3 + 4 \dots (n-1)\} \Rightarrow T_n = 1 + 2 \left( \frac{(n-1)(n-1+1)}{2} \right) = 1 + n^2 - n = n^2 - n + 1$$

$(1), (3, 5), (7, 9, 11), (13, 15, 17, 19) \dots$   
 $\leftarrow 3 \quad \leftarrow 4 \text{ terms} \quad \leftarrow n \text{ term}$   
 $(n^2 - n + 1), n^2 - n + 3 \dots$

$$\text{Sum} = \frac{n}{2} [2(n^2 - n + 1) + (n-1) \cdot 2]$$

$$= n[n^2 - n + 1 + n - 1] = n^3$$

Sum =  $n^3$

1  
 3 5  
 7 9 11  
 13 15 17 19  
 !

Video Dubara Dekhna





Q If Ratio of sum of  $n$  terms of 2 different

AP is  $\frac{3n-1}{5n+21}$  find Ratio of 24<sup>th</sup> terms?

$$\frac{S_n}{S_n'} = \frac{3n-1}{5n+21}$$

$$\frac{T_n}{T_n'} = \frac{3(2n-1)-1}{5(2n-1)+21}$$

$$\frac{T_n}{T_n'} = \frac{6n-14}{10n+16}$$

$$\frac{T_{24}}{T_{24}'} = \frac{6 \times 24 - 14}{10 \times 24 + 16} = \frac{130}{256} = \frac{65}{128}$$

Q. Suppose  $a_1, a_2, a_3, \dots, a_n$  are in AP &  $S_K$  denotes

Sum of 1<sup>st</sup>  $K$  terms. If  $\frac{S_m}{S_n} = \frac{m^4}{n^4}$  find  $\frac{a_{m+1}}{a_{n+1}}$

$$\frac{S_m}{S_n} = \frac{m^4}{n^4} \Rightarrow \frac{a_m}{a_n} = \frac{(2m-1)^3}{(2n-1)^3}$$

$$\begin{aligned} \frac{a_{m+1}}{a_{n+1}} &= \frac{(2(m+1)-1)^3}{(2(n+1)-1)^3} \\ &= \left( \frac{2m+1}{2n+1} \right)^3 \underline{\underline{A}} \end{aligned}$$



# Geometric Progression. [G.P.]

It is a Seq<sup>n</sup> of non Zero No. in which  
ratio of any term to the term Preceding  
is always constant & this Constant Ratio is known  
as Com. Ratio of this G.P.

$$\begin{array}{c}
 \overset{2}{\curvearrowright} \overset{2}{\curvearrowright} \overset{2}{\curvearrowright} \overset{2}{\curvearrowright} \\
 2, 4, 8, 16, 32, \dots \\
 \\
 \begin{array}{ccccccc}
 2 & 1 & 1 & \frac{1}{2} & \frac{1}{4} & \frac{1}{8} & \dots \\
 \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \\
 2 & 2 & 2 & 2 & 2 & 2 & \dots
 \end{array} \\
 \\
 \rightarrow \frac{4}{2} = \frac{8}{4} = \frac{16}{8} = \frac{32}{16}
 \end{array}$$

1) If  $a_1, a_2, a_3, a_4, \dots, a_n$  G.P.

$$\frac{a_2}{a_1} = \frac{a_3}{a_2} = \frac{a_4}{a_3} = \dots = \frac{a_n}{a_{n-1}} = (C.R. = r)$$

2) G.P. when  $(C.R. = r)$

$$a, ar, \boxed{ar^2}, \boxed{ar^3}, \dots, \boxed{ar^{n-1}}$$

$T_3 \quad T_4 \quad T_n$

3)  $n^{\text{th}}$  term =  $T_n = a \cdot r^{n-1}$

Q Let  $a_1, a_2, a_3, \dots, a_{10}$  are in HP. If  $\frac{a_3}{a_1} = 25$

Main then  $\frac{a_9}{a_5} = ?$

$$\frac{a_3}{a_1} = \frac{ar^2}{a} = 25 \Rightarrow r^2 = 25$$

$$r = 5, -5$$

Demand  $\frac{a_9}{a_5} = \frac{ar^8}{ar^4} = r^4$   
 $= (25)^2$   
 $= 625$

① The 4<sup>th</sup>, 7<sup>th</sup>, Last term of HP are 10, 80, 2560

Find 1<sup>st</sup> term & No. of terms?

$$1) \begin{array}{l} T_4 = \boxed{ar^3 = 10} \\ T_7 = \boxed{ar^6 = 80} \end{array} \quad \left| \quad \begin{array}{l} T_7 = \frac{ar^6}{ar^3} = \frac{80}{10} = 8 \Rightarrow \boxed{r=2} \end{array} \right.$$

$\searrow a \cdot 2^3 = 10$

$$a = \frac{10}{8} = \frac{5}{4}$$

No of terms = 12

2) Last term =  $n^{\text{th}}$  term =  $ar^{n-1}$

$$\frac{5}{4} \cdot (2)^{n-1} = \frac{512}{2560}$$

$$(2)^{n-1} = 2^9 \times 2^2$$

$$(2)^{n-1} = 2^{11}$$

$$n-1 = 11 \Rightarrow \boxed{n=12}$$

Q If 5<sup>th</sup> term of HP is 2, then Prod of 1<sup>st</sup> 9 terms?

$$T_5 = ar^4 = 2$$

$$\text{Prod of 1<sup>st</sup> 9 terms} = T_1 \times T_2 \times T_3 \times \dots \times T_9$$

$$= a \times ar \times ar^2 \times ar^3 \times \dots \times ar^8$$

$$= a^9 (r)^{1+2+3+\dots+8}$$

$$= a^9 (r)^{\frac{8 \times 9}{2}}$$

$$= a^9 \cdot r^{36} = (ar^4)^9$$

$$= 2^9 = \underline{\underline{512}}$$

Q Let  $\{a_n\}$  be in HP Such that  $\frac{a_4}{a_6} = \frac{1}{4}$

$$\& a_2 + a_5 = 216 \text{ then } a_1 = ?$$

3'