

CURRENT ELECTRICITY

(8)

$$I = neAv_d \quad \text{--- (1)}$$

$$J = \frac{I}{A} = nev_d \quad \text{--- (2)}$$

$$v_d = \left(\frac{eE}{m} \tau \right) \quad \text{--- (3)}$$

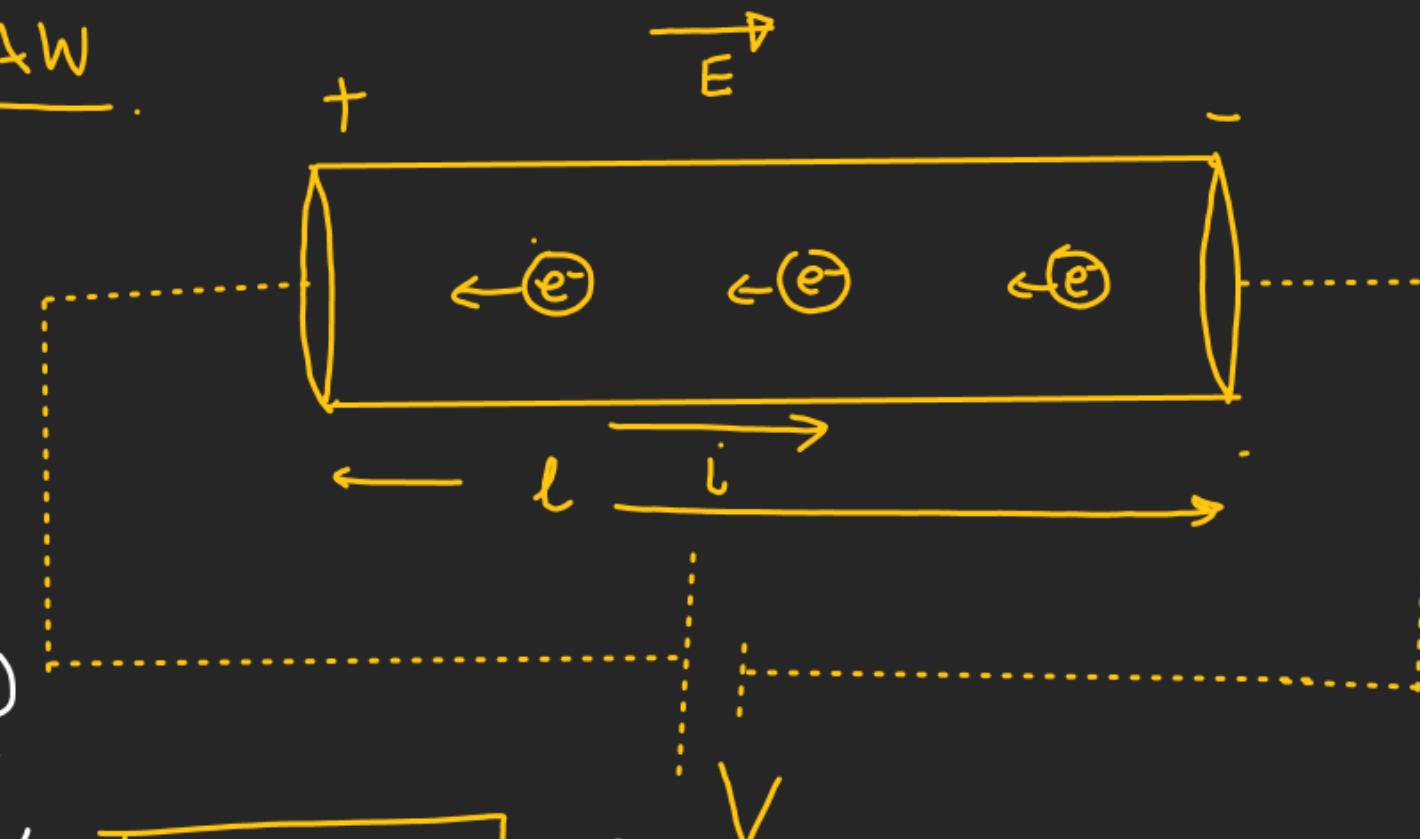
From (1) and (3)

$$I = (neA) \left(\frac{e\tau}{m} \right) E$$

$$\boxed{I = \left(\frac{ne^2\tau}{m} \right) A E \quad \text{--- (4)} \quad (***)}$$

$$\boxed{\frac{I}{A} = \left(\frac{ne^2\tau}{m} \right) E \Rightarrow J = \sigma E}$$

OHM'S LAW



From (4) and (5)

$$I = \left(\frac{ne^2\tau}{m} \right) \left(\frac{A}{l} \right) V$$

$$V = El \quad \text{--- (5)}$$

$$V = \left[\left(\frac{m}{ne^2\tau} \right) \left(\frac{l}{A} \right) \right] I \quad \epsilon = \left(\frac{V}{l} \right)$$

\Downarrow $\rho = \frac{m}{ne^2\tau}$ (Resistivity)

$$\rho = \frac{m}{ne^2\tau}, (\sigma = \frac{1}{\rho} = \frac{ne^2\tau}{m})$$

$$V = \left\{ \frac{\rho l}{A} \right\} I$$

$$V = IR$$

Ohm's Law

R → Resistance

CURRENT ELECTRICITY

$$R = \frac{\rho l}{A}$$

$$G = \frac{1}{R}$$

$G \rightarrow$ Conductance $\rightarrow [\text{mho}] \rightarrow [\Omega^{-1}]$

$\alpha \Rightarrow$ Temperature coefficient of resistance

Depends on :-
 1. geometrical Configuration ✓
 2. Temperature.

$$\left[\begin{array}{l} \rho \rightarrow \text{Resistivity} \\ \sigma = \frac{1}{\rho} \rightarrow \text{Conductivity.} \end{array} \right]$$

Depends only on
 → Nature of material
 → Temperature.

Temperature dependency
 for conductor

$$R = R_0(1 + \alpha \Delta T)$$

$$\rho = \rho_0(1 + \alpha \Delta T)$$

$R_0 \rightarrow$ Resistance at 0°C.

$R \rightarrow$ Resistance at any $t^\circ\text{C}$.
 $\alpha \rightarrow$

$$\left[\frac{dR}{dt} = R_0 \alpha \right]$$

$$\left[\frac{\Delta R}{\Delta t} = R_0 \alpha \right]$$



t (temperature)

CURRENT ELECTRICITY

AAK

Ohm's Law :- [$\vec{J} = \sigma \vec{E}$] $V = IR$

$$\boxed{f = \frac{mn e^2}{\tau}}$$

- ↳ ① Current density is directly proportional to applied electric field. provided temperature must be constant.

 - ↳ ② Current across any conductor is directly proportional to applied potential difference. provided temperature must be constant
- Note ⇒ If temperature increases →
- | | |
|---------------------------------|----------------------------|
| $T \rightarrow$ decreases. | $f \rightarrow$ increases. |
| $\sigma \rightarrow$ decreases. | |

CURRENT ELECTRICITY



K.V.L and K.C.L.

K.V.L : \rightarrow [Krichhoff's Voltage Law]

\Leftarrow (Depends on energy conservation).

\rightarrow Sum of all the potential drop across any closed loop is zero

Sign-convention:



direction
of movement
in the loop.

① $\left[\begin{array}{l} \text{Crossing the battery from} \\ -\text{ve terminal to +ve terminal} \\ \text{Considered as potential rise.} \end{array} \right]$

(+V)

②



←
direction of
movement in the
loop.

\rightarrow $(-V) \rightarrow$ $\left[\begin{array}{l} \text{crossing the battery} \\ \text{from +ve terminal to} \\ -\text{ve terminal Considered} \\ \text{as potential drop.} \end{array} \right]$

CURRENT ELECTRICITY

For resistance

Sign-convention

direction of movement



$$V_A - IR = V_B$$

$$\boxed{V_A - V_B = IR}$$

- ① if direction of movement in the loop is along the current flow then potential drop.

$$\boxed{\Delta V = -IR}$$

direction of movement



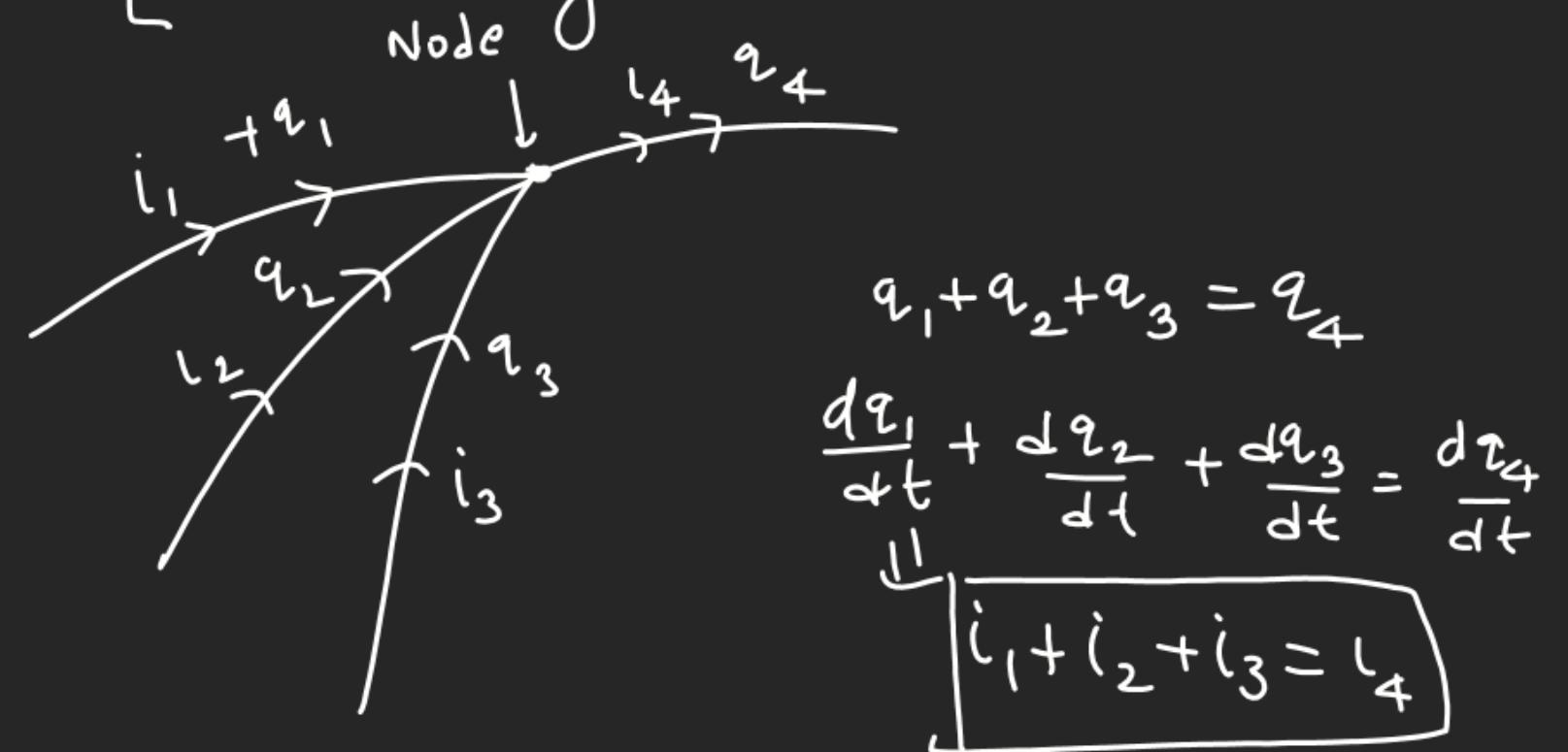
$$\boxed{V_B + IR = V_A}$$

while moving opposite to current flow in the resistance potential across the resistance considered as potential rise

CURRENT ELECTRICITY

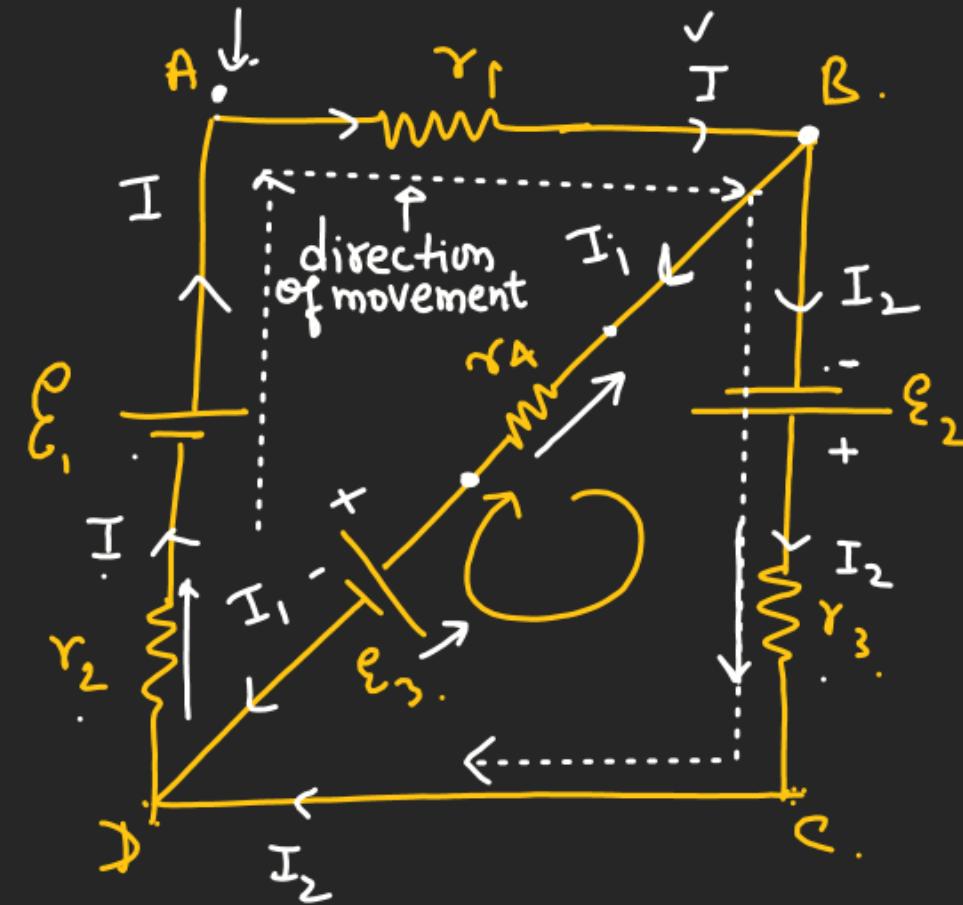
K.C.L :- Krichhoff's Current Law [Conservation of Charge].

↳ Sum of incoming Current is equal to Sum of outgoing Current across any node or junction.



CURRENT ELECTRICITY

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K.V.L in the loop ABCDA

$$[-I r_1 + E_2 - I_2 r_3 - I r_2 + E_1 = 0]$$

K.V.L in the loop BCDB

$$[+E_2 - I_2 r_3 + E_3 + I_1 r_4 = 0]$$

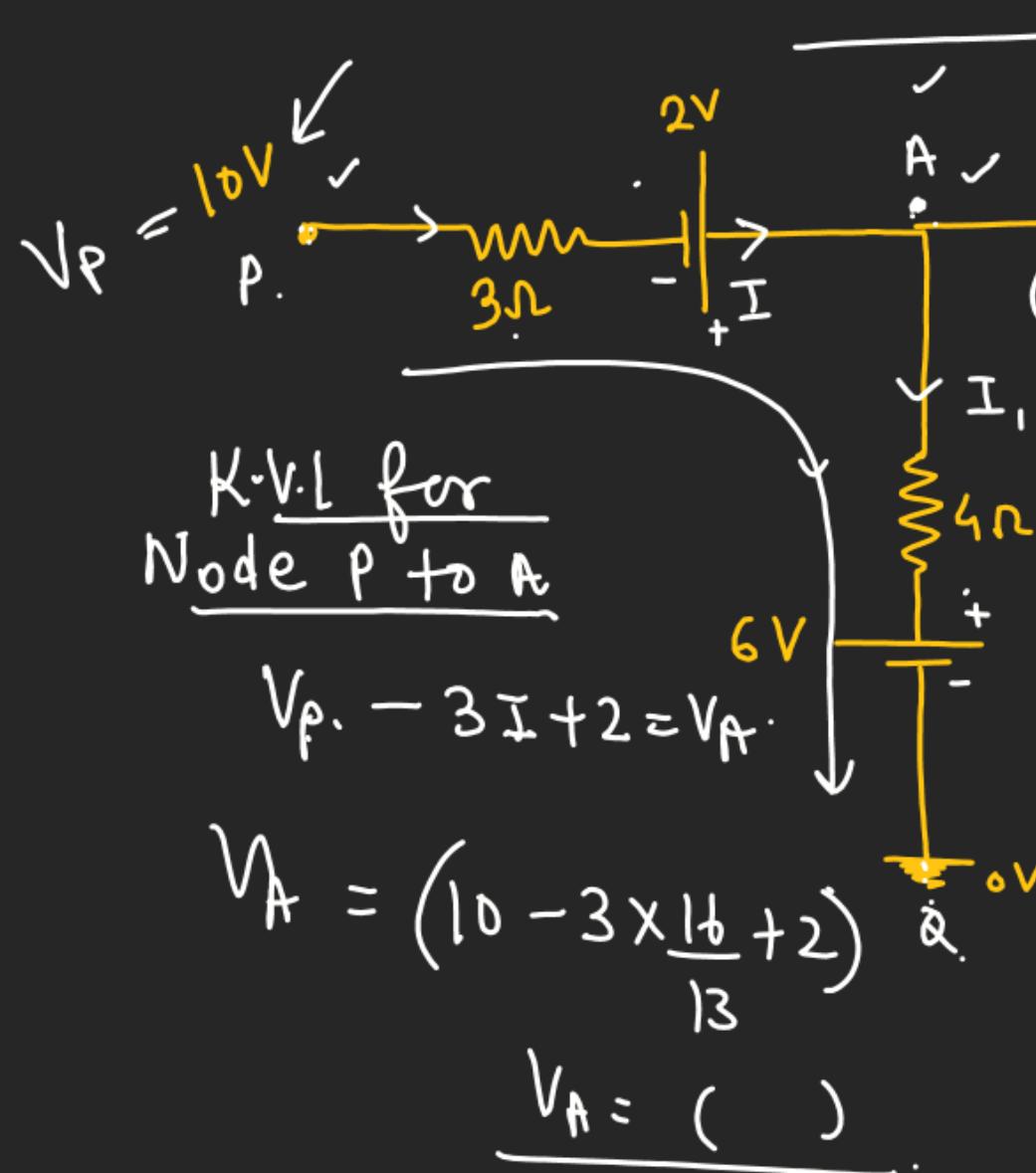
K.C.L at B

$$[I = I_1 + I_2]$$

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Find, $V_A = ?$, $V_B = ?$



$$I = I_1 + I_2$$

K.V.L from Node P to Q.

$$10 - 3I + 2 - 4I_1 - 6 = V_Q = 0$$

K.V.L for the path P to B

$$10 - 3I + 2 - 5 - 2(I - I_1) = V_B = 2V$$

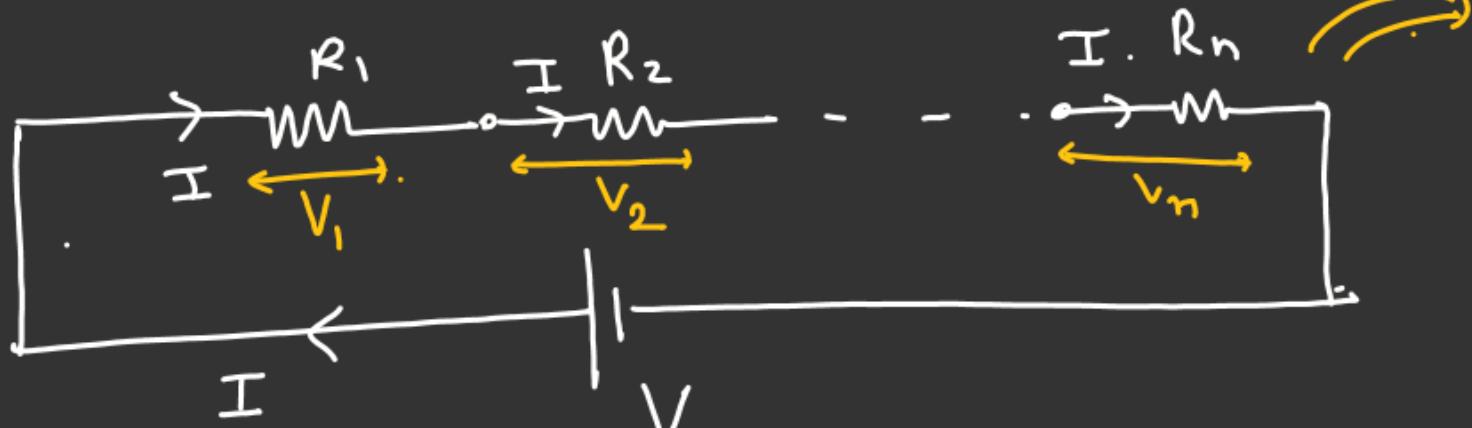
$$10 - 3I - 5 - 2I + 2I_1 = 0$$

$$\begin{cases} I = ? \left(\frac{16}{13}\right) ?? \\ I_1 = ? = \left(\frac{15}{26}\right) ?? \end{cases}$$

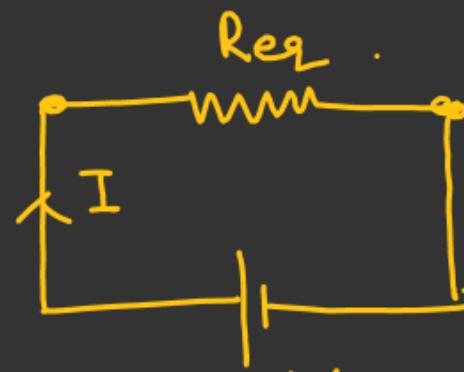
Series and parallel combination

Series combination

⇒ Current in all resistance is Same.



$$R_{eq} = ??$$



$$V = I R_{eq}$$

$$\begin{cases} V_1 = I R_1 \\ V_2 = I R_2 \\ \vdots \\ V_n = I R_n \end{cases} \quad V_1 + V_2 + \dots + V_n = V$$

$$I (R_1 + R_2 + \dots + R_n) = I R_{eq}$$

$$R_{eq} = R_1 + R_2 + \dots + R_n$$

Parallel Combination

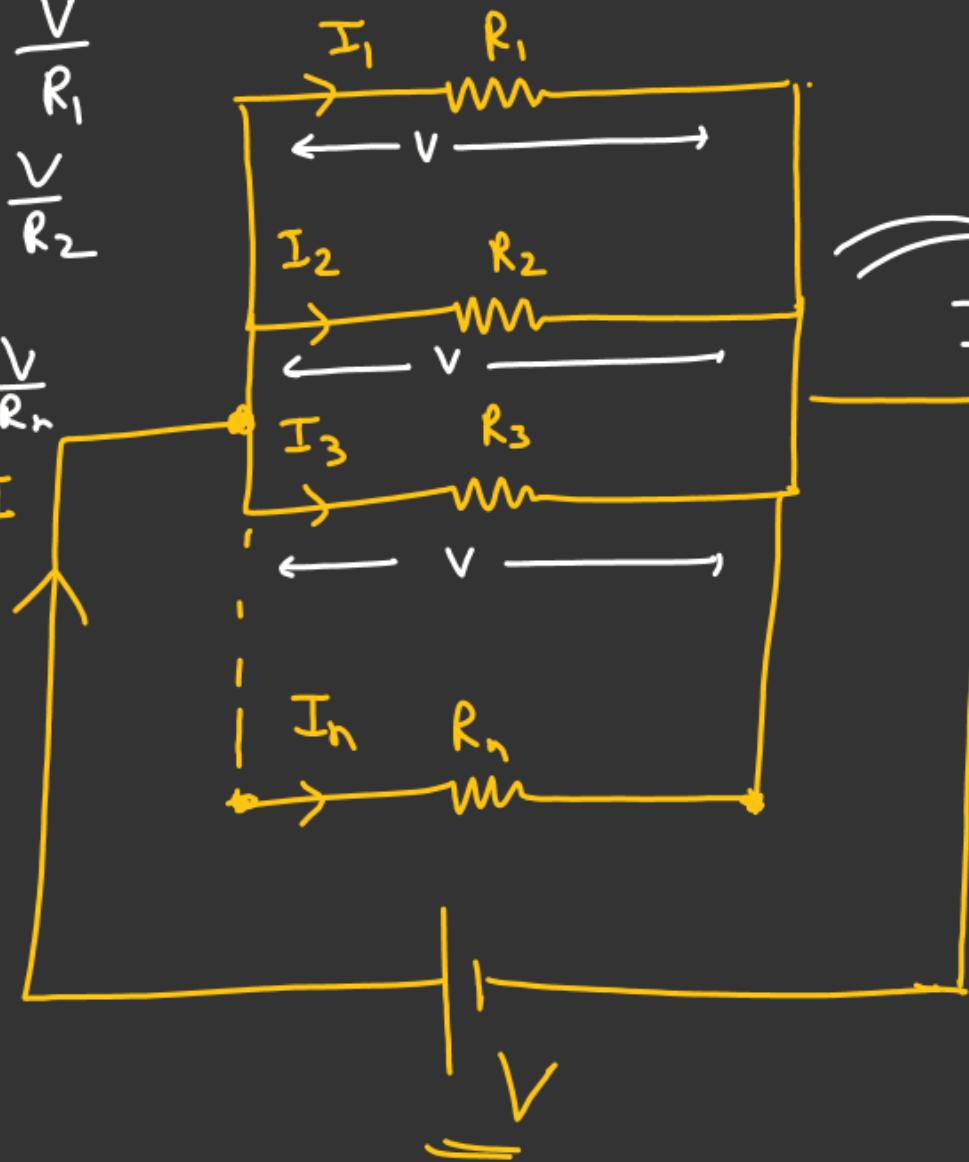
↪ Potential drop across each Capacitor is Same.

$$I_1 = \frac{V}{R_1}$$

$$I_2 = \frac{V}{R_2}$$

$$I_n = \frac{V}{R_n}$$

$$I$$



$$I = I_1 + I_2 + \dots + I_n$$

$$I = \frac{V}{R_{eq}}$$

$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2} + \dots + \frac{V}{R_n}$$

$$\boxed{\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}} \quad **$$