

FRICTION

Q.1 A block of mass 1 kg is placed on a rough inclined plane at angle $\theta = 30^\circ$ with horizontal. The block is connected with a string as shown in Fig. If $\mu_s = 3/4$, find the tension in string.

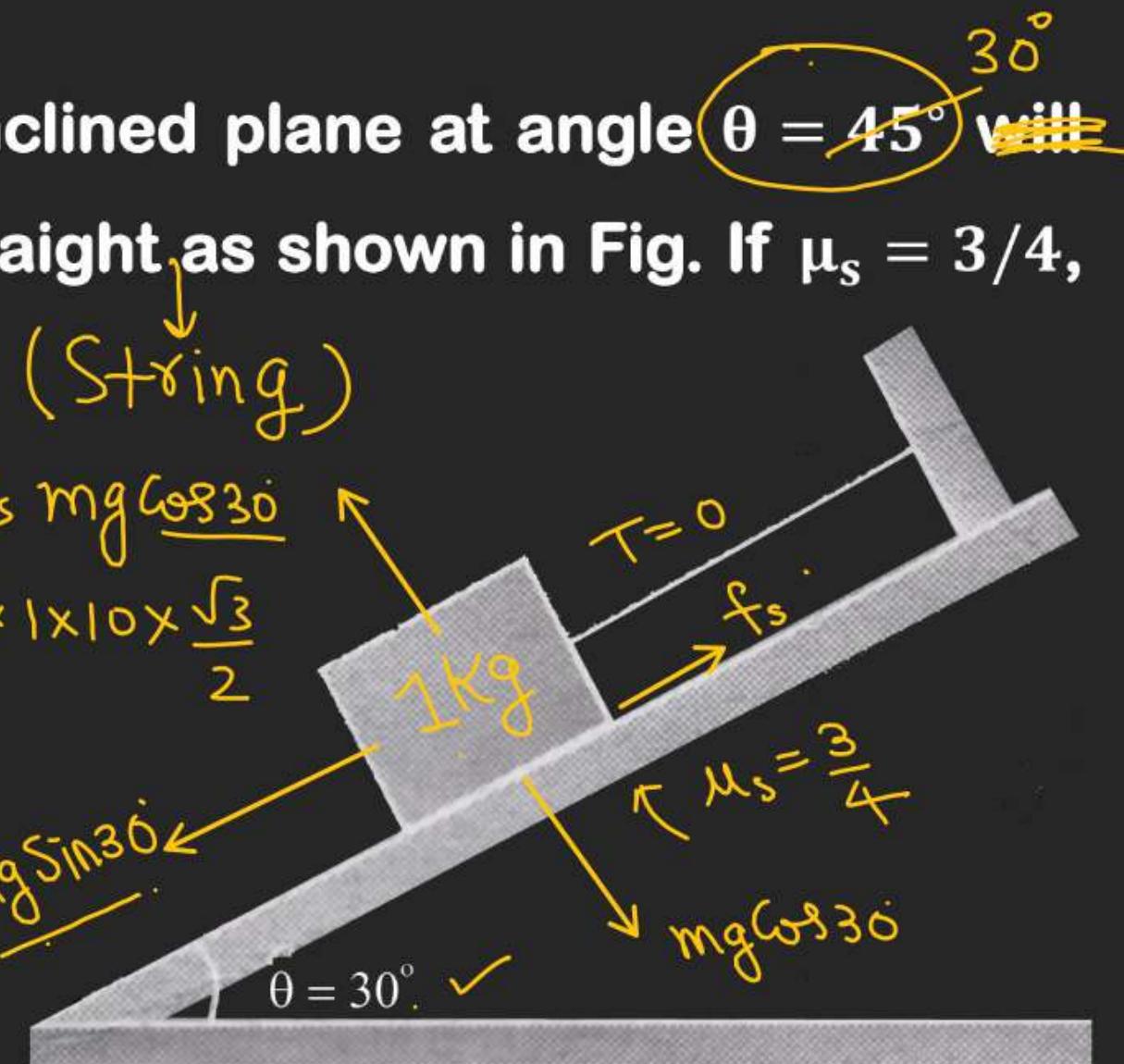
$$F_{ext} = mg \sin 30 = 1 \times 10 \times \frac{1}{2} \\ = \underline{\underline{5N}}$$

$$\underline{\underline{F_{ext}}} < \underline{\underline{(f_s)_{max}}}$$

$$f_s = F_{ext} = \underline{\underline{5N}} \quad \checkmark$$

$$(f_s)_{max} = \mu_s mg \cos 30 \\ = \frac{3}{4} \times 1 \times 10 \times \frac{\sqrt{3}}{2} \\ = \frac{15\sqrt{3}}{4}$$

(String)



FRICTION

Q.3 Two blocks M and m are arranged as shown in Fig. If $M = 50 \text{ kg}$, then determine the minimum and maximum values of mass of block m to keep the heavy block M stationary.

$$\begin{aligned} \text{Soln} - & \\ & (f_s)_{\max} = \mu_s N \\ & = 0.60 \times 400 \\ & = 240 \text{ N} \end{aligned}$$

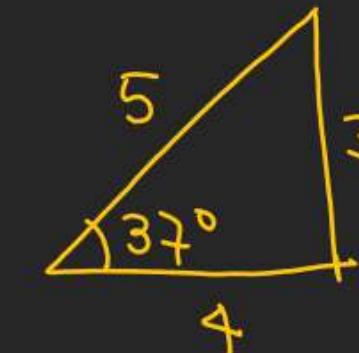
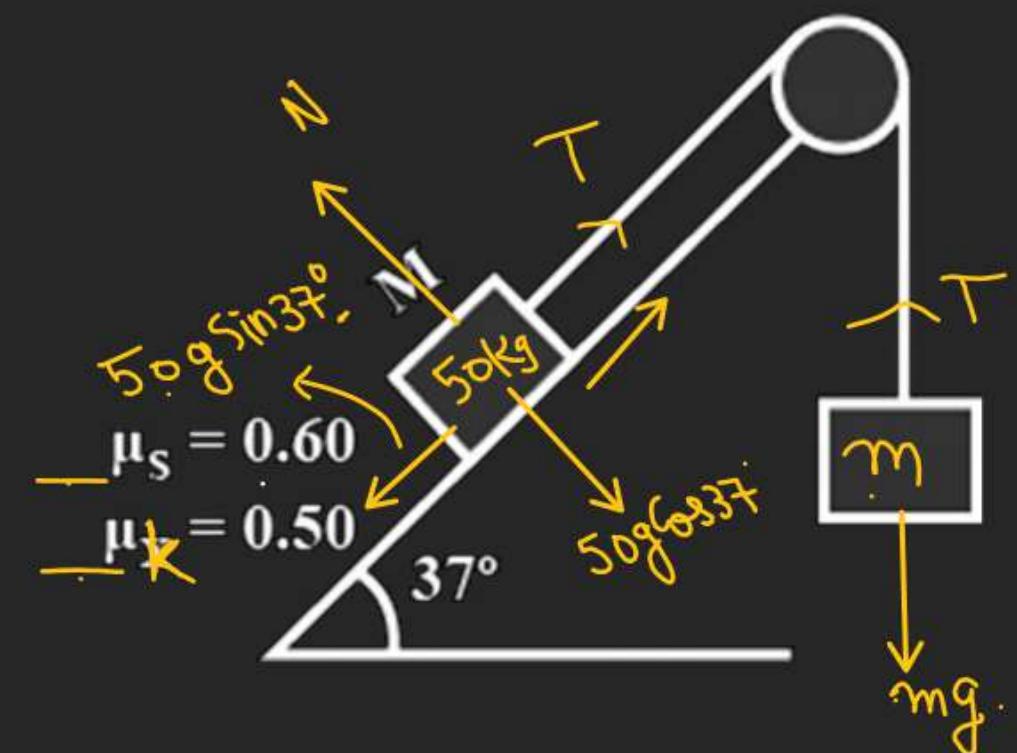
Minimum For block not to slide.

$$300 = 240 + T$$

$$mg = T = 60 \text{ N}$$

$$m = 6 \text{ Kg} \quad (\text{minimum value})$$

$$\begin{aligned} N &= 50 \times 10 \times \frac{4}{5} \\ N &= 400 \text{ Newton} \quad \checkmark \\ 50g \sin 37^\circ &= 50 \times 10 \times \frac{3}{5} \\ &= 50 \times 6 \\ &= 300 \text{ Newton} \end{aligned}$$

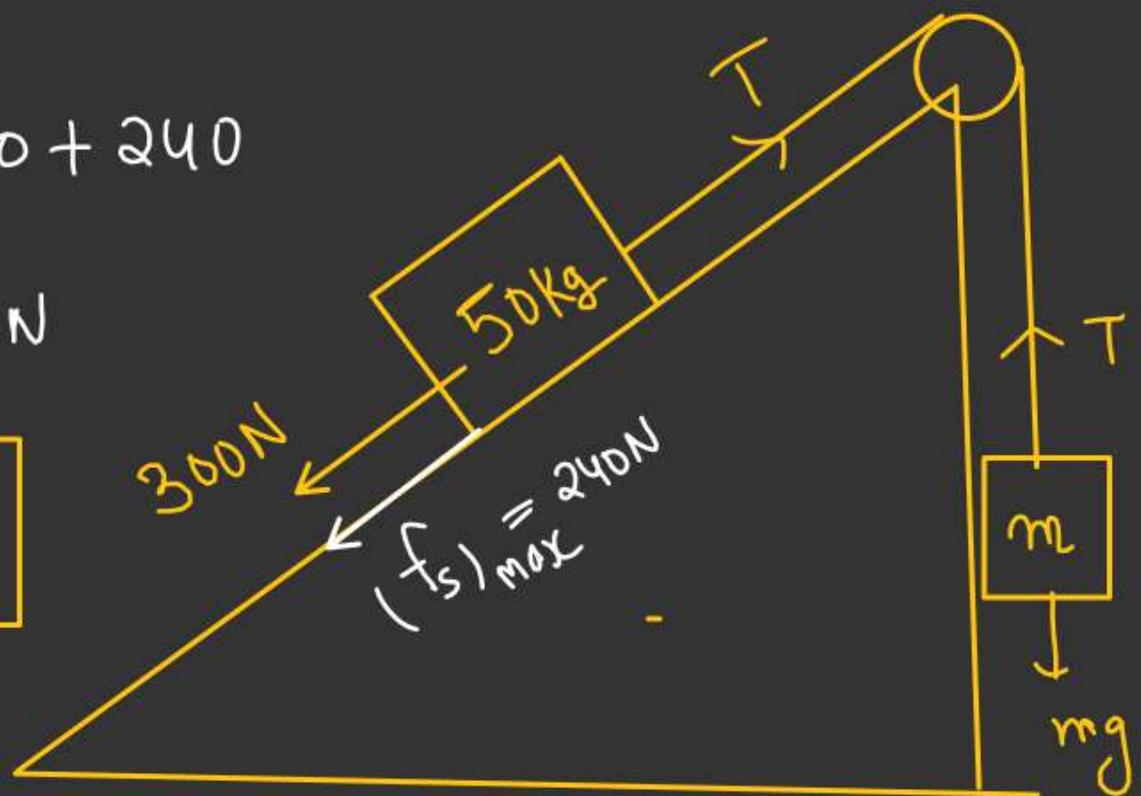


For $m \rightarrow \text{maximum}$

$$mg = 300 + 240$$

$$mg = 540 \text{ N}$$

$$m = 54 \text{ Kg}$$



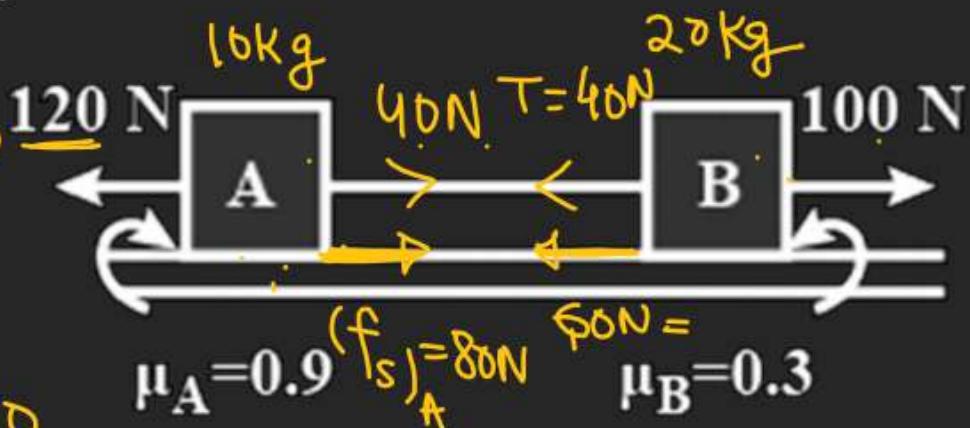
FRICTION

Q.4 Two blocks A and B of mass $m_A = 10 \text{ kg}$ and $m_B = 20 \text{ kg}$ are placed on rough horizontal surface. The blocks are connected with a string. If the coefficient of friction between block A and ground is $\mu_A = 0.9$ and between block B and ground is $\mu_B = 0.3$, find Fig. the tension in the string in situation as shown in Fig. Forces 120 N and 100 N start acting when the system is at rest?

$$\underline{T=40 \text{ N}} \quad \checkmark$$

$$(f_s)_{\max \text{ of } A} = 0.9 \times 10 \times 10 = 90 \text{ N}$$

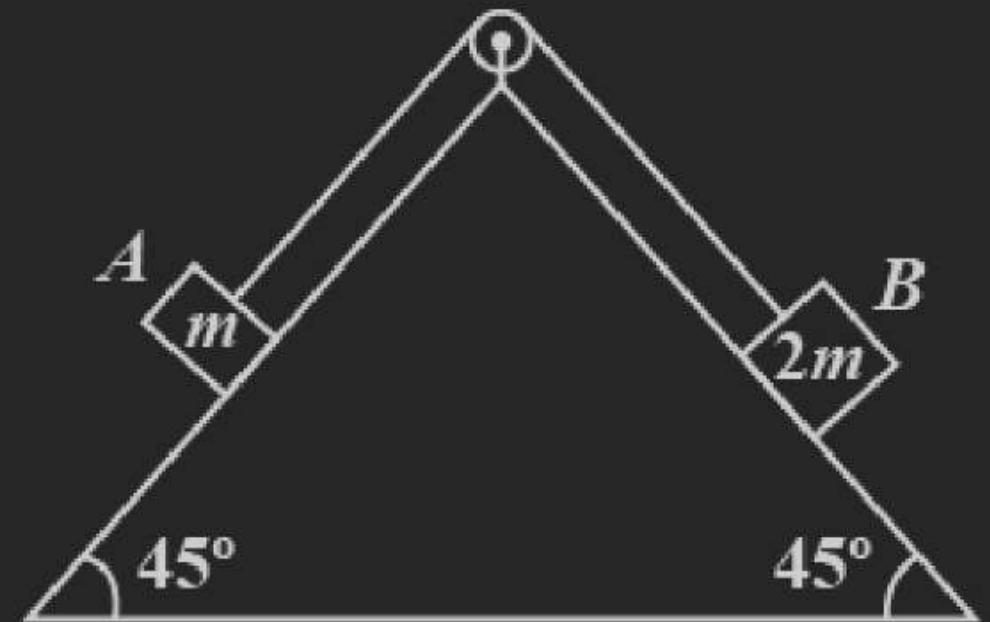
$$(f_s)_{\max \text{ of } B} = 0.3 \times 20 \times 10 = 60 \text{ N}$$



FRICTION

H.W.

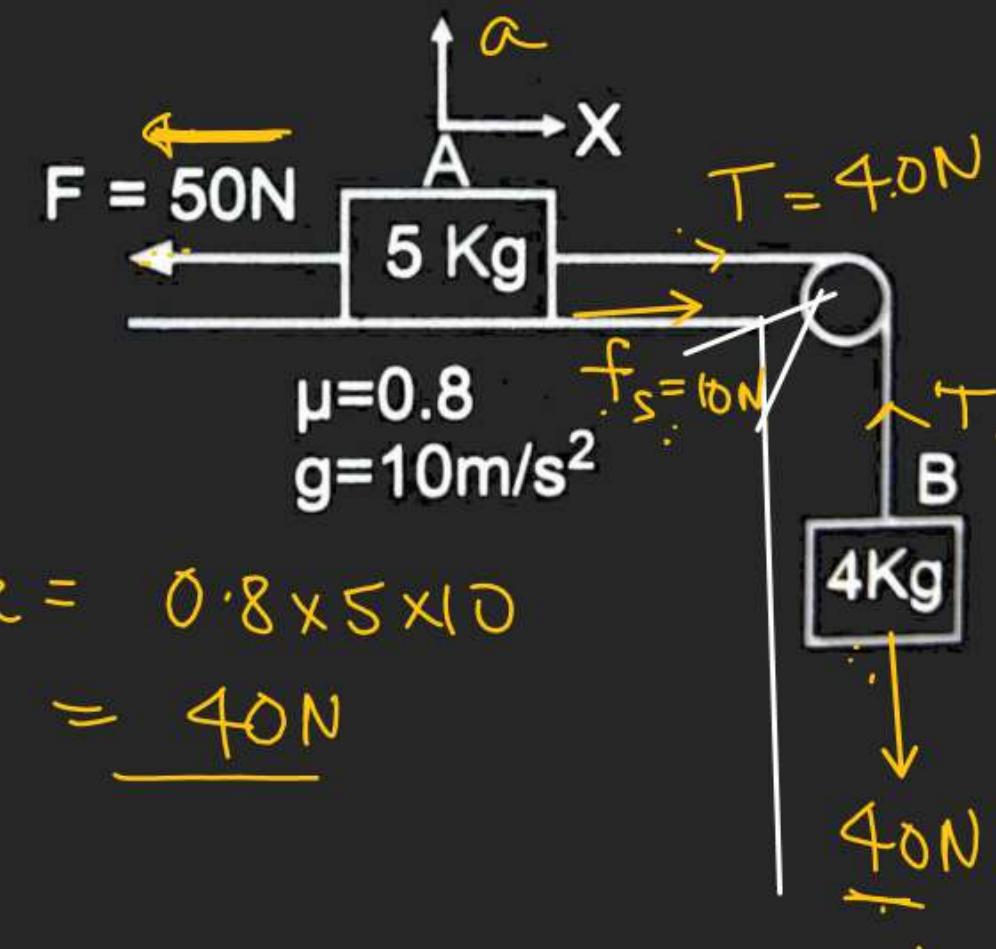
- Q.5** Block A of mass m and block B of mass $2m$ are placed on a fixed triangular wedge by means of a light and inextensible string and a frictionless pulley as shown in Fig. The wedge is inclined at 45° to the horizontal on both sides. The coefficient of friction between the block A and the wedge is $2/3$ and that between the block B and the wedge is $1/3$. If the system of A and B is released from rest, then find,
- the acceleration of A
 - tension in the string
 - the magnitude and direction of the frictional force acting on A



FRICTION

Q.1 Find the acceleration of the block and magnitude and direction of frictional force between block A and table, if block A is pulled towards left with a force of 50 N.

$$\left[\begin{array}{l} a = 0 \\ f_s = 10 \text{ N} \end{array} \right]$$



$$\begin{aligned} (f_s)_{\max} &= 0.8 \times 5 \times 10 \\ &= \underline{\underline{40 \text{ N}}} \end{aligned}$$

FRICTION

Q.2 The 10 kg block is resting on the horizontal surface when the force ' F ' is applied to it for 7 second. The variation of ' F ' with time is shown. Calculate the maximum velocity reached by the block and the total time ' t ' during which the block is in motion. The coefficient of static and kinetic friction are both 0.50.

$$F = \begin{cases} \frac{25t}{2}, & 0 < t \leq 4 \\ 40, & 4 < t \leq 7 \end{cases}$$

$\rightarrow a$

$10\text{kg} \rightarrow 25t$

$50\text{N} = f_k$

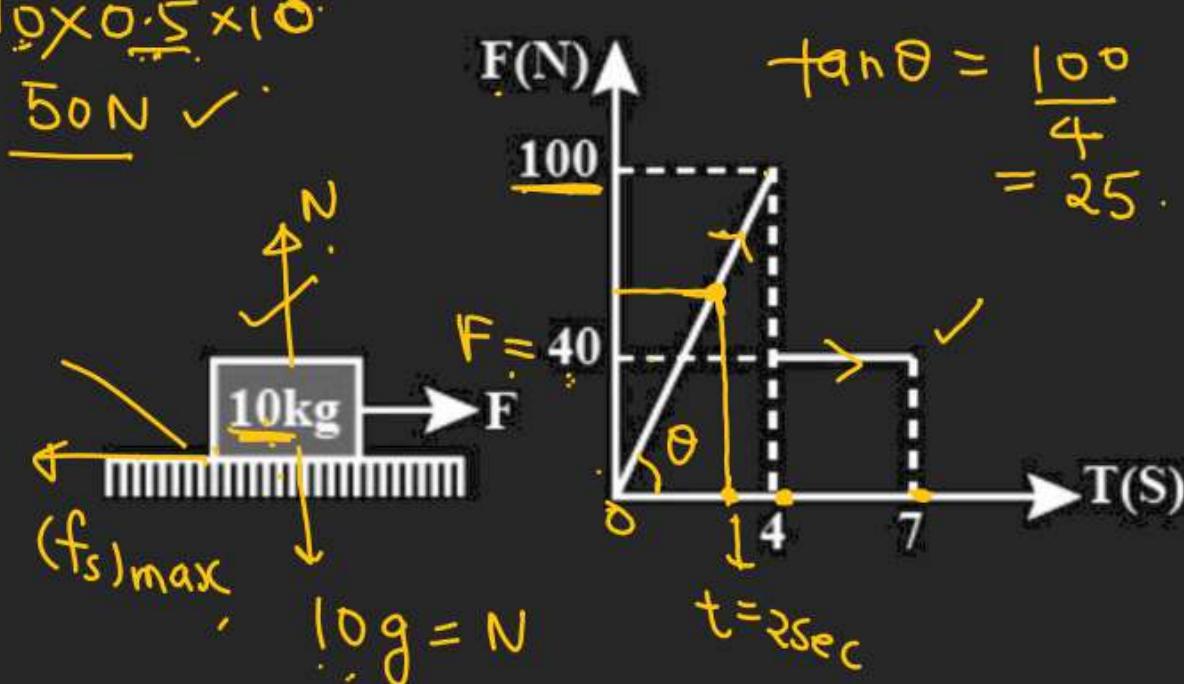
$$(f_s)_{\max} = 10 \times 0.5 \times 10 = 50\text{N} \checkmark$$

$$\begin{aligned} F &= 25t \\ F &= (f_s)_{\max} \end{aligned}$$

$$\begin{aligned} 25t &= 50 \\ t &= 2\text{sec} \end{aligned}$$

$$25t - 50 = 10a$$

$$a = \left(\frac{25t}{10} - 5 \right) = \left(\frac{5}{2}t - 5 \right)$$



$$0 < t \leq 4 \text{ sec}$$

$$\boxed{a = \frac{5}{2}t - 5}$$

$$\int_0^4 \frac{dv}{dt} = \left(\frac{5}{2}t - 5 \right)$$

$$\int_0^4 dv = \int_0^4 \left(\frac{5}{2}t - 5 \right) dt$$

$$v = \frac{5}{2} \int_2^4 t dt - 5 \int_2^4 dt$$

$$v = \frac{5}{2} \left[\frac{t^2}{2} \right]_2^4 - 5 [t]_2^4$$

$$v = \frac{5}{2} (16 - 4) - 5 (4 - 2)$$

$$v = (5 \times 3 - 10) = \underline{5 \text{ m/s}}$$

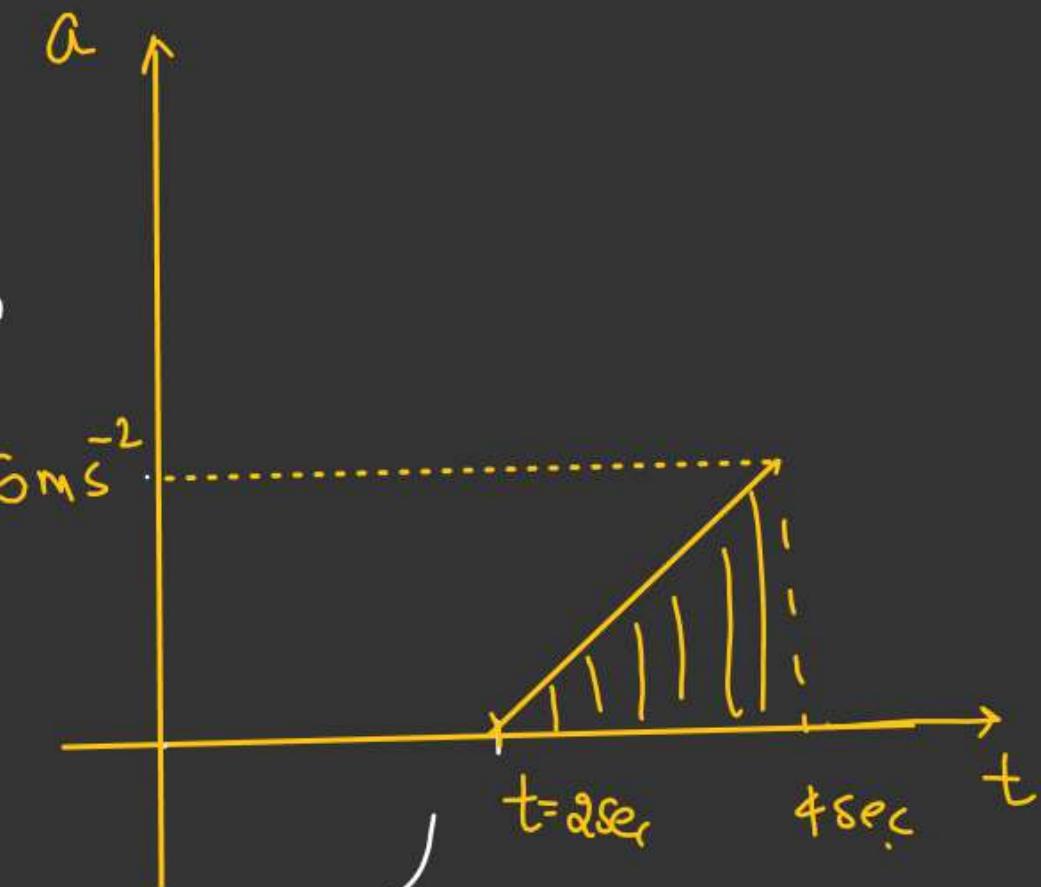
 M^{-2} Area of trapezium

$$= \Delta v \\ = v - 0$$

$$\frac{1}{2} [5 + 10] \times 2 = \underline{v}$$

$$\Delta v = \frac{1}{2} \times 2 \times 5 \quad \begin{array}{l} \text{[Area under]} \\ \text{a vs t} \end{array}$$

$$\underline{\Delta v = 5 \text{ m/s}^2}$$



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Q.6 What is the maximum value of the force F such that the block shown in the arrangement, does not move question:

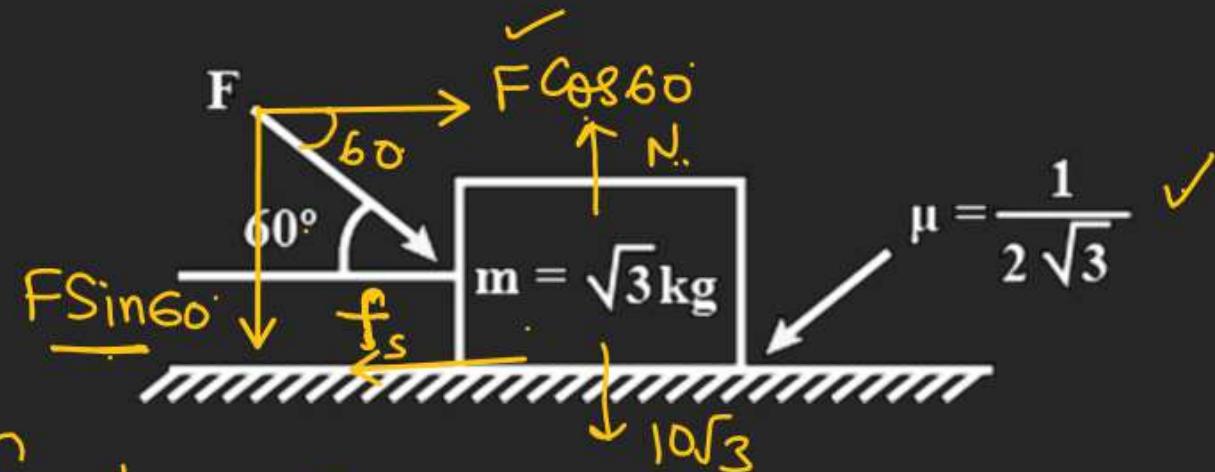
- (a) 20 N
- (b) 10 N
- (c) 12 N
- (d) 15 N

For block
not to move.

$$F \cos 60^\circ = f_s$$

$$\frac{F}{2} = f_s$$

$$F_{\max} = 20 \text{ N}$$



$$(f_s) \leq (f_s)_{\max}$$

$$\frac{F}{2} \leq \frac{1}{2\sqrt{3}} \left[10\sqrt{3} + \frac{F\sqrt{3}}{2} \right]$$

$$\frac{F}{2} \leq 5 + \frac{F}{4}$$

$$\frac{F}{4} \leq 5$$

$$F \leq 20 \text{ N}$$