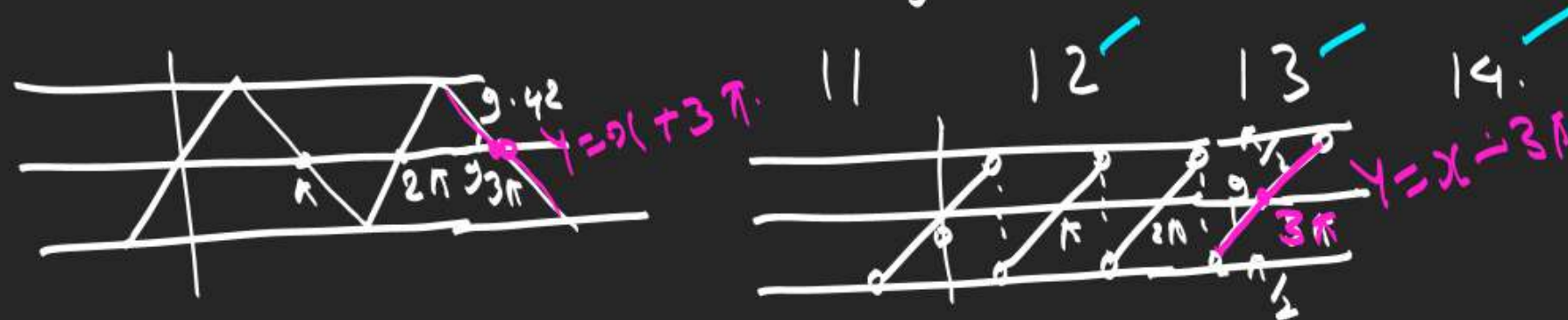


Q. If $x^2 + 2x + n > \sin^{-1}(\sin x) + \tan^{-1}(\tan x) + 10$ for all real x then n can be.



$$x^2 + 2x + n > -9 + 3\pi + 9 - 3\pi + 10$$

$$x^2 + 2x + n - 10 > 0 \rightarrow Q.E. > 0$$

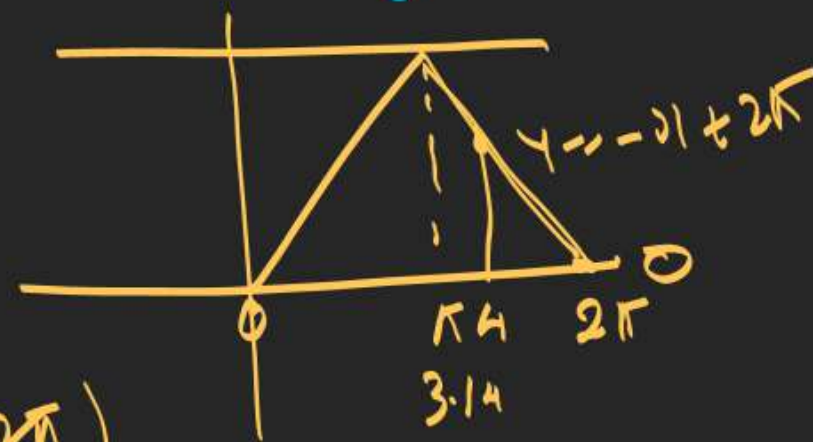
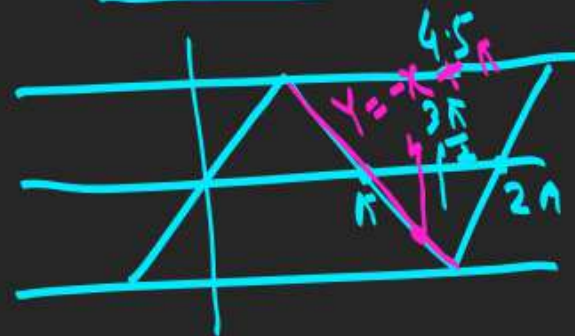
$$D < 0$$

$$(2)^2 - 4 \times 1 \times (n - 10) < 0$$

$$1 - n + 10 < 0$$

$$n > 11$$

Q $3x^2 + 8x < 2 \sin(\sin 4) - \cos(\cos 4)$ find Integral Sol.?



$$3x^2 + 8x < 2(-4 + \pi) - (-4 + 2\pi)$$

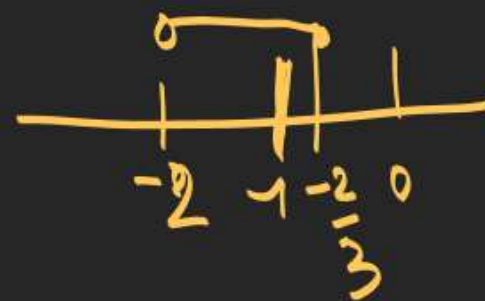
$$3x^2 + 8x < -4$$

$$3x^2 + 8x + 4 < 0$$

$$3x^2 + 6x + 2x + 4 < 0$$

$$(3x + 2)(x + 2) < 0$$

$$-\frac{2}{3} < x < -2 \Rightarrow x = -1 \text{ is the only Integer.}$$

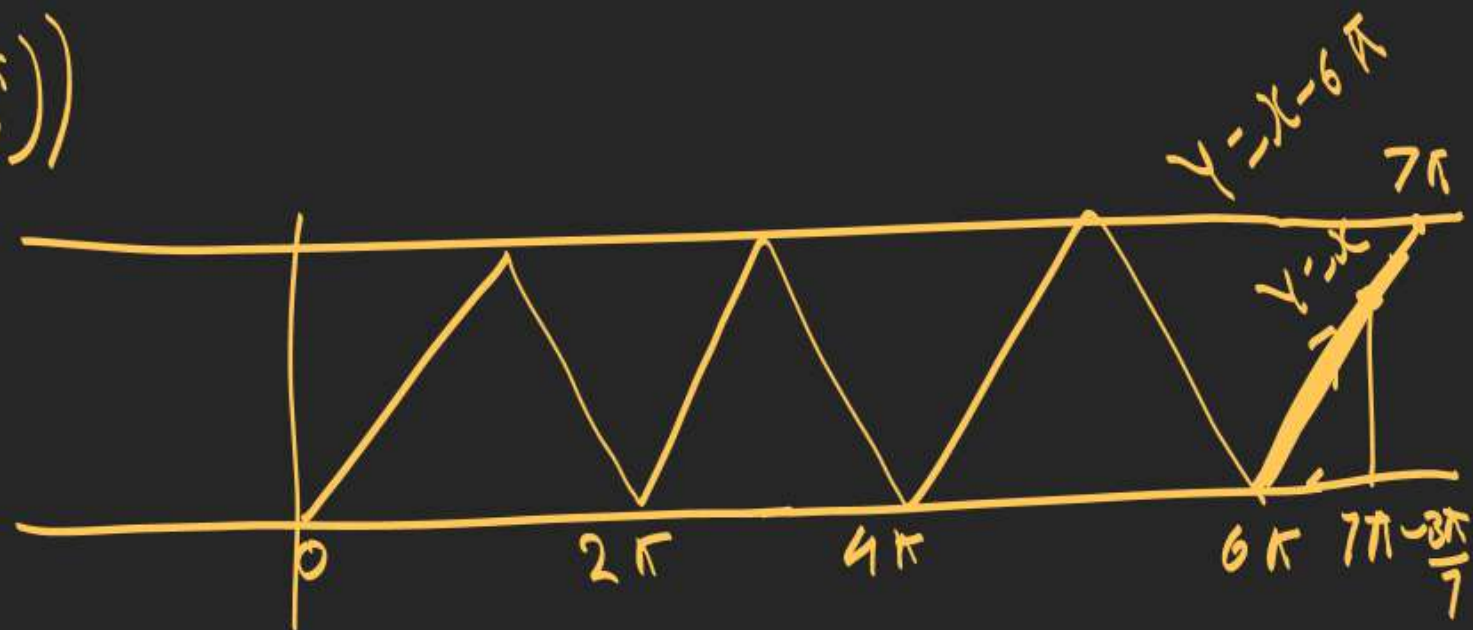
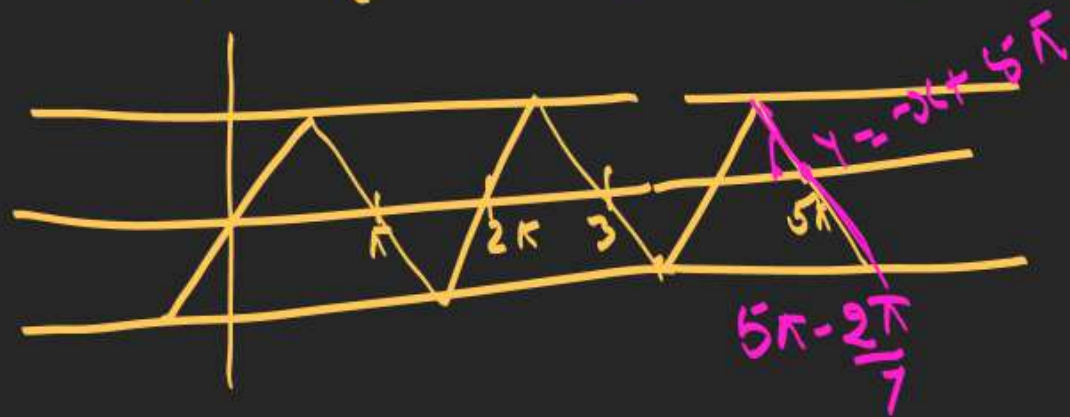


Q $\sin^{-1}(\sin(\frac{33\pi}{7})) + \cos^{-1}(\cos(\frac{46\pi}{7})) = \frac{a\pi}{b}$ find $|a-b| = ?$ $a=6, b=7$
 $|6-7|=1$

$\frac{49\pi-3\pi}{7} = 7\pi - \frac{3\pi}{7}$

$$\sin^{-1}(\sin(\frac{35\pi-2\pi}{7})) + \cos^{-1}(\cos(\frac{42\pi+4\pi}{7}))$$

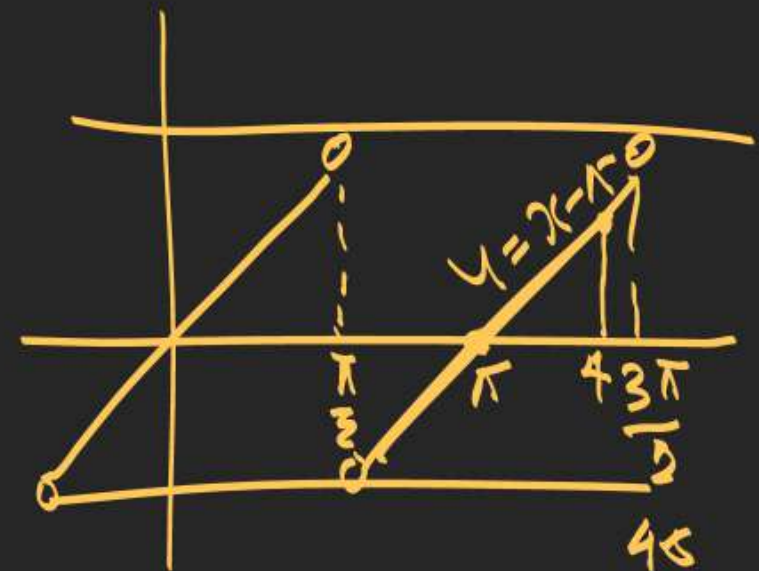
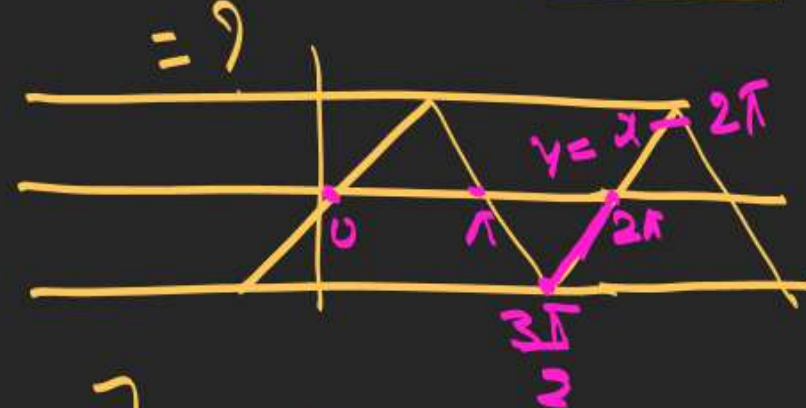
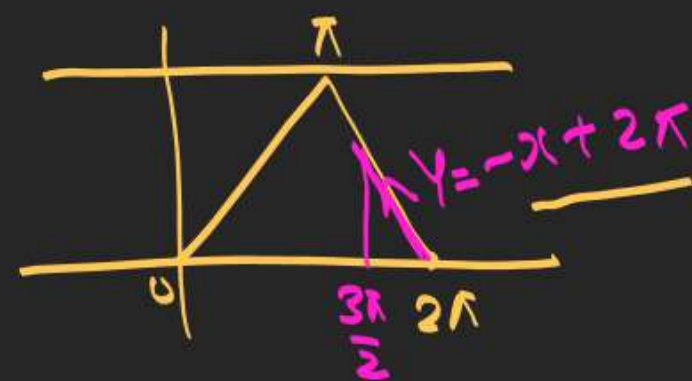
$$\sin^{-1}(\sin(5\pi - \frac{2\pi}{7})) + \cos^{-1}(\cos(7\pi - \frac{3\pi}{7}))$$



$$-\frac{33\pi}{7} + 5\pi + \frac{46\pi}{7} - 6\pi$$

$$-\pi - \frac{33\pi}{7} + \frac{46\pi}{7} = -\pi + \frac{13\pi}{7} = \frac{-7\pi + 13\pi}{7} = \frac{6\pi}{7} = \frac{a\pi}{b}$$

Q $\sin^{-1} \left[\cos \left(\boxed{\sin^{-1}(\cos x)} + \sin^{-1}(\sin x) \right) \right] ; x \in \left(\frac{3\pi}{2}, 2\pi \right)$



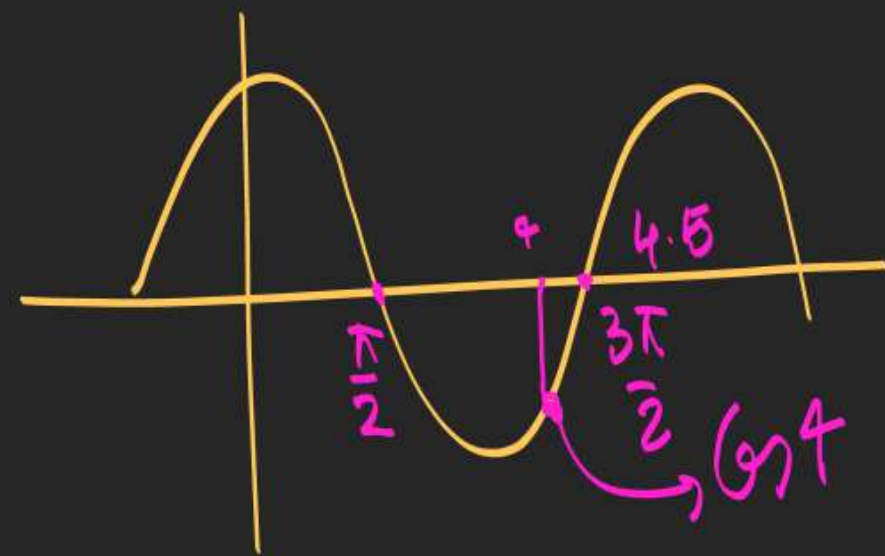
Kham
Nashta

$$\sin^{-1} \left[\cos \left(-x + 2\pi + x - 2\pi \right) \right] = \sin^{-1}(\cos 0) = \sin^{-1} 1 = \frac{\pi}{2}$$

Q $\cos(\sin^{-1}(\tan 4))$ is +ve or -ve?

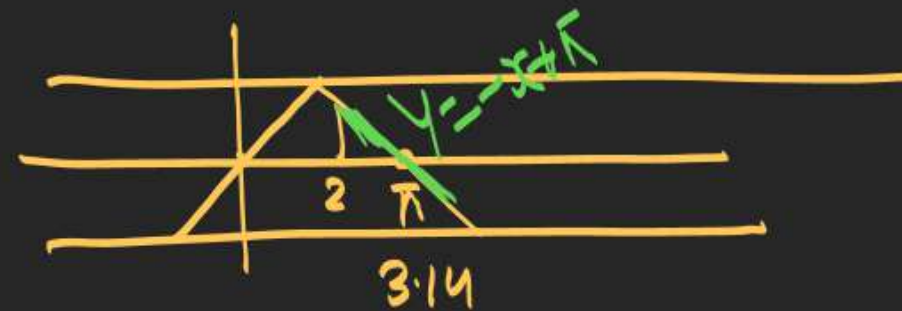
40%

$$\begin{aligned} \cos(\pi - 4) &= \cos(\pi - 4) = -\cos 4 \\ &= -(-ve) \\ &= +ve \end{aligned}$$



$$x \in (-1, 1)$$

$$Q \text{ Solve } \sin\left(\tan\left(\frac{2x^2+4}{1+x^2}\right)\right) < \pi-3$$



Kai Bar $T^{-1}(T(\cdot))$ me Andar se Nahi dia Jata. Kabhi Kabhi fcn de dete hain tab fcn ki Range Nikale aur $T^{-1}(T(\cdot))$ ki value find Karen.

$$\frac{2x^2+4}{1+x^2} = \frac{2x^2+2+2}{1+x^2} = \frac{2(1+x^2)+2}{1+x^2} = 2\frac{(1+x^2)}{1+x^2} + \frac{2}{1+x^2} = 2 + \frac{2}{1+x^2}$$

$$-\frac{2x^2+4}{1+x^2} + \pi < \pi - 3$$

$$\frac{2x^2+4}{1+x^2} > 3 \Rightarrow 2x^2+4 > 3+3x^2$$

$$x^2-1 < 0$$

$$(x-1)(x+1) < 0$$

$$-1 < x < 1$$

$$0 \leq x^2 < \infty$$

$$1 \leq 1+x^2 < \infty$$

$$1 \geq \frac{1}{1+x^2} > 0$$

$$2 \geq \frac{2}{1+x^2} > 0$$

$$4 \geq 2 + \frac{2}{1+x^2} > 2$$

$$\frac{2x^2+4}{1+x^2} \in (2, 4]$$

Q Adv $\sin^{-1}\left(\cos\left(\frac{2x^2+10|x|+6}{x^2+5|x|+3}\right)\right) = \cancel{\cos^{-1}}\left(\cancel{\cos^{-1}}\left(\frac{2-18|x|}{9|x|}\right)\right) + \frac{\pi}{2}$ find x ? $\cos^{-1}(\cos^{-1}(x)) = x$

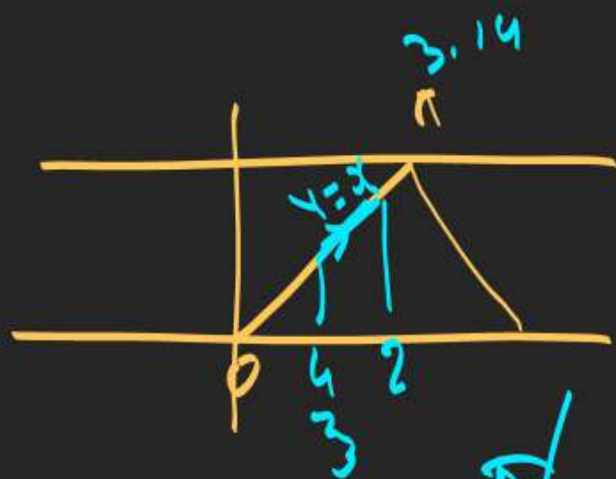
$\left[\frac{4}{3}, 2\right)$ \uparrow Trigo (Inverse Trigo)

$$\frac{\pi}{2} - \cos^{-1}\left(\cos\left(\frac{2(x^2+5|x|+3)}{x^2+5|x|+3} - \frac{2}{x^2+5|x|+3}\right)\right)$$

$$\frac{\pi}{2} - \cos^{-1}\left(2 - \frac{2}{x^2+5|x|+3}\right)$$

$$\geq 0 + \geq 0 + 3$$

$$\geq 3$$



$$\frac{\pi}{2} - \left(2 - \frac{2}{x^2+5|x|+3}\right) = \frac{\pi}{9|x|} - 2 + \frac{\pi}{2}$$

$$x^2+5|x|+3=9|x| \Rightarrow x^2-4|x|+3=0$$

$$(x-3)(x-1)=0$$

JUSTIFY

$$\infty \Rightarrow x^2+5|x|+3 \geq 3$$

$$0 < \frac{2}{x^2+5|x|+3} \leq \frac{2}{3}$$

$$0 > \frac{-2}{x^2+5|x|+3} \geq -\frac{2}{3}$$

$$2 > 2 - \frac{2}{x^2+5|x|+3} \geq \frac{4}{3}$$

$$\begin{cases} |x|=1, |x|=3 \\ x = +1, -1, 3, -3 \end{cases}$$

Adv
Material.When $T^{-1}(T)$ has algebraic Expression Inside.

Q. $G^{-1}(2x^2-1) = \begin{cases} 2\boxed{G^{-1}x} & \boxed{0 \leq x \leq 1} \\ 2\pi - 2G^{-1}x & \boxed{-1 \leq x < 0} \end{cases}$ P.T.

\downarrow
Algebraic Exp \rightarrow feel $\rightarrow \underline{\theta = G^{-1}x} \Rightarrow \theta = G^{-1}x \rightarrow \boxed{0 \leq \theta \leq \pi}$

$\boxed{[0, \frac{\pi}{2}]} = \boxed{(\theta, \frac{\pi}{2})} \rightarrow 1 \text{ } 0$

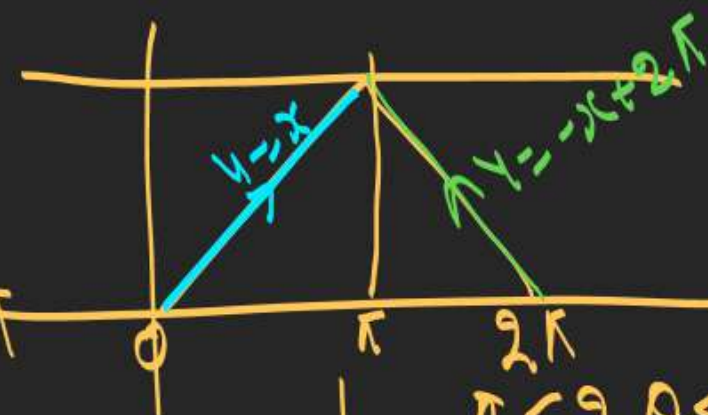
$$\text{LHS} = G^{-1}(2x^2-1)$$

$$= G^{-1}(2G^2\theta-1)$$

$$= G^{-1}(G(2\theta))$$

$$0 \leq \theta \leq \pi$$

$$0 \leq 2\theta \leq 2\pi$$



$$\boxed{0 > x \geq -1}$$

$$0 \leq 2\theta \leq \pi$$

$$0 \leq \theta \leq \frac{\pi}{2}$$

$$0 \leq G^{-1}x \leq \frac{\pi}{2}$$

$$\Rightarrow x \geq 0$$

$$y = 2\theta$$

$$y = 2G^{-1}x$$

$$y = -2\theta + 2\pi$$


$$y = -2G^{-1}x + 2\pi$$

$$\pi < 2\theta \leq 2\pi$$

$$\frac{\pi}{2} < \theta \leq \pi$$

$$\frac{\pi}{2} < G^{-1}x \leq \pi$$

Q $\sin^{-1}\left(\frac{2x}{1+x^2}\right) = \begin{cases} -\pi - 2\tan^{-1}x & x < -1 \\ 2\tan^{-1}x & -1 \leq x \leq 1 \\ \pi - 2\tan^{-1}x & x > 1 \end{cases}$ P.T.



$$-\frac{\pi}{4} \leq \tan^{-1}x \leq \frac{\pi}{4} \quad -1 \leq x \leq 1$$

ITF me Algebraic

$\frac{2x}{1+x^2} \rightarrow$ 1) $x = \tan \theta \Rightarrow \theta = \tan^{-1}x \in -\frac{\pi}{2} < \theta < \frac{\pi}{2}$

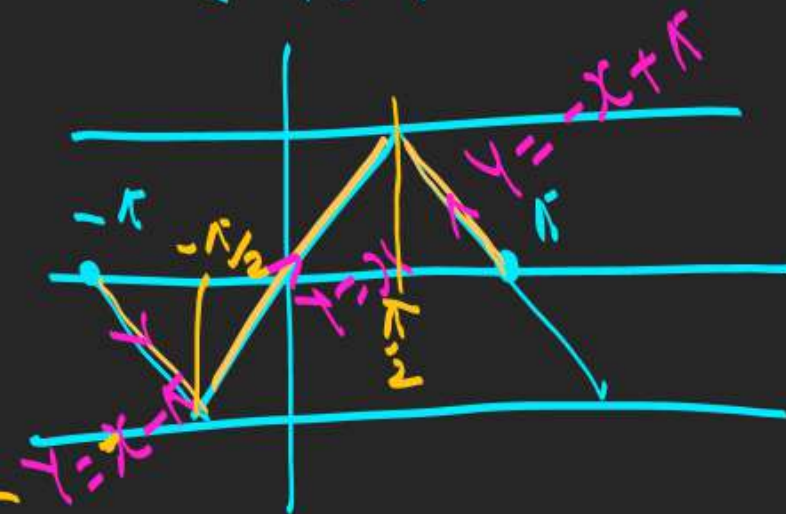
2) $y = \sin^{-1}\left(\frac{2x}{1+x^2}\right) = \sin^{-1}\left(\frac{2\tan\theta}{1+\tan^2\theta}\right)$

$$= \sin^{-1}(\sin 2\theta)$$

$$-\frac{\pi}{2} < \theta < \frac{\pi}{2}$$

$$-\pi < 2\theta < \pi$$

$y = -2\theta - \pi$	$y = 2\theta$	$y = -2\theta + \pi$
$y = -\pi - 2\tan^{-1}x$	$y = 2\tan^{-1}x$	$y = -2\tan^{-1}x + \pi$
$-\pi < 2\theta < -\frac{\pi}{2}$ $-\frac{\pi}{2} < \theta < -\frac{\pi}{4}$ $x < -1$	$-\frac{\pi}{2} < 2\theta < \frac{\pi}{2}$ $-\frac{\pi}{4} < \theta < \frac{\pi}{4}$ $-1 \leq x \leq 1$	$\frac{\pi}{2} < 2\theta < \pi$ $\frac{\pi}{4} < \theta < \frac{\pi}{2}$ $x > 1$



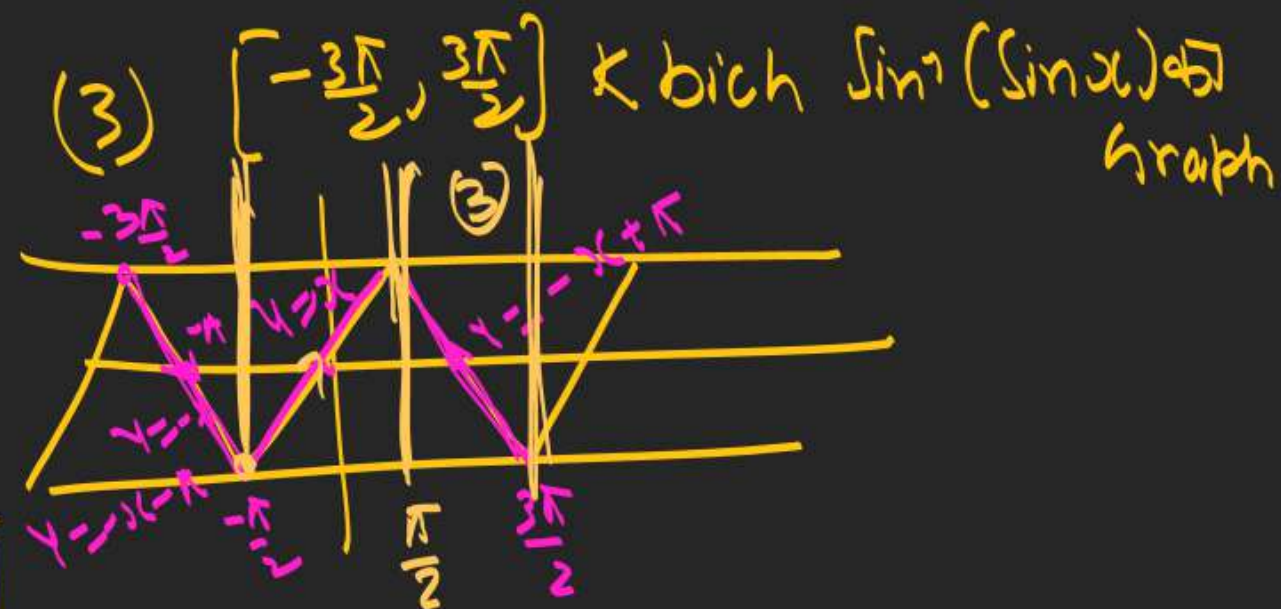
$$Q. \sin(3x-4x^3) = \begin{cases} -\pi-3\sin x & -1 \leq x \leq -\frac{1}{2} \\ 3\sin^{-1} x & -\frac{1}{2} \leq x \leq \frac{1}{2} \\ \pi-3\sin x & \frac{1}{2} \leq x \leq 1 \end{cases}$$



① $x = \sin \theta \rightarrow \theta = \sin^{-1} x \rightarrow -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$

② $y = \sin(3\sin \theta - 4\sin^3 \theta)$
 $= \sin(\sin 3\theta)$

$-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$
 $-3\frac{\pi}{2} \leq 3\theta \leq 3\frac{\pi}{2}$



④

$$y = -3\theta - \pi$$

$$y = -3\sin^{-1} x - \pi$$

$$y = 3\theta$$

$$y = 3\sin^{-1} x$$

$$y = -3\theta + \pi$$

$$y = \pi - 3\sin^{-1} x$$

5)

$$-\frac{3\pi}{2} \leq 3\theta \leq -\frac{\pi}{2}$$

$$-\frac{\pi}{2} \leq \theta \leq -\frac{\pi}{6}$$

$$-\frac{1}{2} \leq x \leq -\frac{1}{2}$$

$$-\frac{\pi}{2} \leq 3\theta \leq \frac{\pi}{2}$$

$$-\frac{\pi}{6} \leq \theta \leq \frac{\pi}{6}$$

$$-\frac{1}{2} \leq x \leq \frac{1}{2}$$

$$\frac{\pi}{2} \leq 3\theta \leq \frac{3\pi}{2}$$

$$\frac{\pi}{6} \leq \theta \leq \frac{\pi}{2}$$

$$\frac{1}{2} \leq x \leq 1$$

4

Q a, b find out of $\arccos\left[-1, -\frac{1}{2}\right]$ s.t. $\sin(\underline{3x-4x^3}) + \cos(\underline{4x^3-3x}) = \underline{a \cos x + b}$.

$\cos(-x) = \pi - \cos x$. 1) When 2 diff. algebraic fcn are given try to make them 1.

$$\frac{\pi}{2} = \cos(3x-4x^3) + \cos(4x^3-3x)$$

$$\frac{\pi}{2} = \cos(-(4x^3-3x)) + \cos(4x^3-3x)$$

$$\frac{\pi}{2} = (\pi - \cos(4x^3-3x)) + \cos(4x^3-3x)$$

$$-\frac{\pi}{2} + 2\cos(4x^3-3x)$$

Qs me

2) $x = \cos \theta \Rightarrow \boxed{\theta = \arccos x} \rightarrow 0 \leq \theta \leq \pi$

3) $y = -\frac{\pi}{2} + 2\cos(4(\cos^3 \theta - 3\cos \theta))$

$$= -\frac{\pi}{2} + 2\boxed{\cos(\cos 3\theta)}$$

$$= -\frac{\pi}{2} + 2(3\theta - 2\pi)$$

$$\underline{6\arccos x - \frac{9\pi}{2}}$$

$$a=6, b=-\frac{9\pi}{2}$$

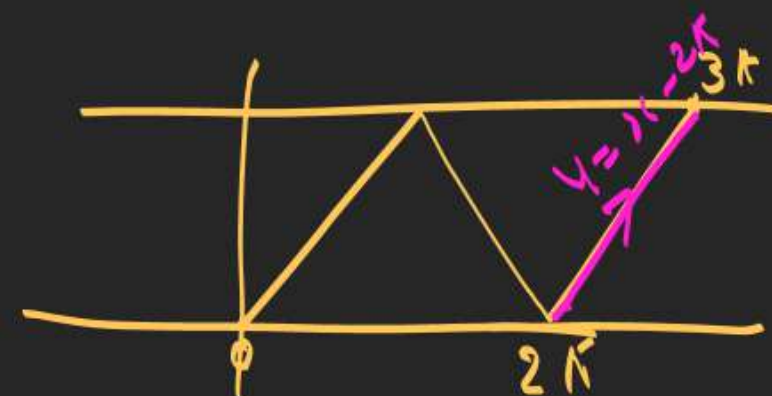
Adv

$$-1 \leq x \leq -\frac{1}{2}$$

$$-1 \leq \cos \theta \leq -\frac{1}{2}$$

$$\pi \leq \theta \leq \frac{2\pi}{3}$$

$$3\pi \leq 3\theta \leq 2\pi$$



$$Q \alpha = 2 \tan^{-1} \left(\frac{1+x}{1-x} \right) \text{ \& } \beta = \sin^{-1} \left(\frac{1-x^2}{1+x^2} \right)$$

Adv

then S.T. $\alpha + \beta = \pi$ if $0 < x < 1$

α के लिए

$$x = \tan \theta$$

$$\alpha = 2 \tan^{-1} \left(\frac{1 + \tan \theta}{1 - \tan \theta} \right)$$

$$= 2 \left(\tan^{-1} \left(\tan \left(\frac{\pi}{4} + \theta \right) \right) \right)$$

$$0 < \theta < \frac{\pi}{4}$$

$$\frac{\pi}{4} < \frac{\pi}{4} + \theta < \frac{\pi}{2}$$

$$\alpha = 2 \left(\frac{\pi}{4} + \theta \right) = \frac{\pi}{2} + 2\theta$$

β के लिए

$$x = \tan \theta$$

$$\beta = \sin^{-1} \left(\frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} \right)$$

$$= \sin^{-1} (\cos 2\theta)$$

$$\beta = \frac{\pi}{2} - \sin^{-1} (\cos 2\theta)$$

$$0 < \theta < \frac{\pi}{4}$$

$$0 < 2\theta < \frac{\pi}{2}$$

$$\beta = \frac{\pi}{2} - 2\theta$$

$$\alpha = \frac{\pi}{2} + 2\theta$$

$$\beta = \frac{\pi}{2} - 2\theta$$

$$\alpha + \beta = \pi$$

②

$$0 < x < 1$$

$$0 < \tan \theta < 1$$

$$0 < \theta < \frac{\pi}{4}$$

Sub

Limit
35 Min

