

LOCUS

A) Set of Pt. Which follow Q's (md<sup>m</sup>)

B) Steps.

A) first assumption In whose locus is to be known.  
let  $(h, k)$

(B) Now follow Q's (md<sup>m</sup>)

(C) after solving  $(h \rightarrow x, k \rightarrow y)$

$\left. \begin{array}{l} \text{Locus} \\ 61 \rightarrow 66 \\ 67-69 \end{array} \right\} \underline{\underline{\text{done}}}$

$$26) \frac{1}{2} \begin{vmatrix} 1 & 1 \\ 0 & \sec^2 \theta \\ \sec^2 \theta & 0 \\ 1 & 1 \end{vmatrix} = 0$$

$$27) \Delta = \frac{1}{2} \begin{vmatrix} 1 & 2 \\ -2 & 3 \\ -3 & -4 \\ 1 & 2 \end{vmatrix}$$

$$28) \Delta = \frac{1}{2} \begin{vmatrix} 2 & -1 \\ 4 & 3 \\ -1 & 2 \\ -3 & -2 \\ 2 & -1 \end{vmatrix}$$

$$31) \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}^2 = \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \\ x_3 & y_3 \end{vmatrix}$$

$$31) \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}^2 - \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \\ x_3 & y_3 \\ x_1 & y_1 \end{vmatrix}^2 = 4\Delta^2$$

$$= 4 \times \frac{3}{4} (a^2)^2$$

$$2\Delta = \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \\ x_3 & y_3 \\ x_1 & y_1 \end{vmatrix}$$

$$Eq \Delta = \frac{\sqrt{3}}{4} a^2$$

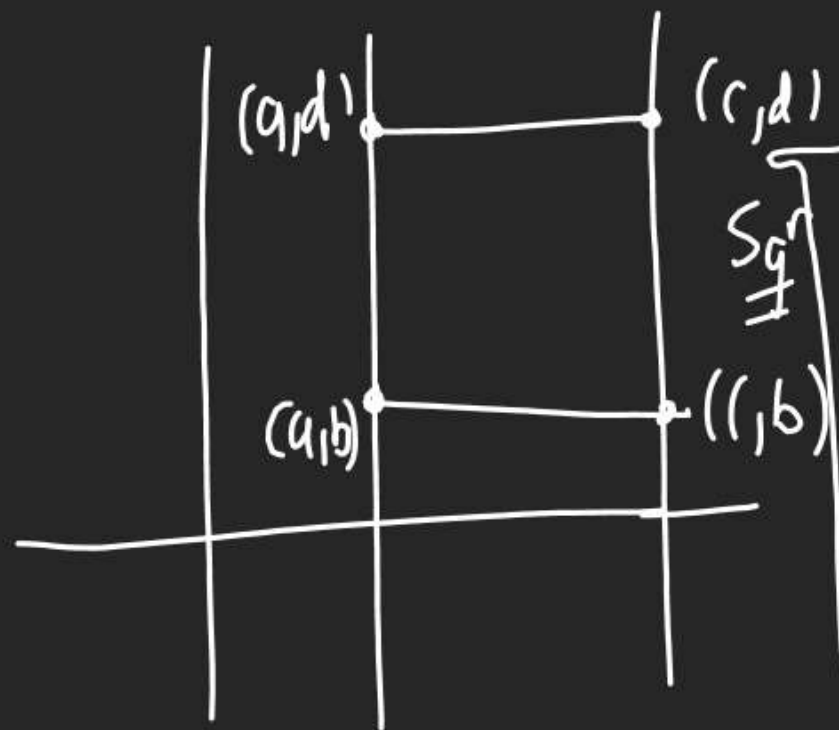
$$4\Delta = \sqrt{3} a^2$$

$$\begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = \begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \\ a_3 & b_3 \end{vmatrix}$$

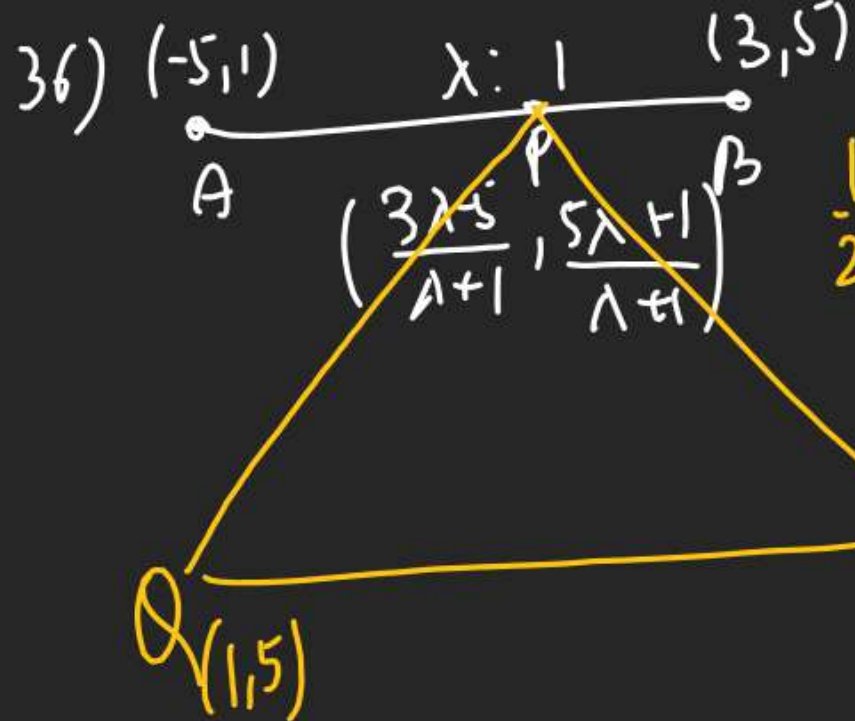
$$\frac{1}{2} \begin{vmatrix} x_1 & y_1 \\ x_2 & y_2 \\ x_3 & y_3 \\ x_1 & y_1 \end{vmatrix} = \frac{1}{2} \begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \\ a_3 & b_3 \\ a_1 & b_1 \end{vmatrix}$$

$$= \frac{3}{4} a^4$$

$$33) (a,b), (a,d), (c,d), (c,b)$$

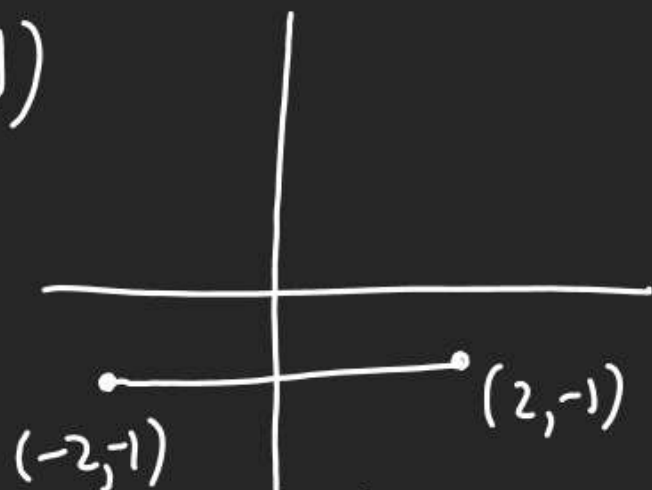


$$\Delta_1 = 42$$



$$\frac{1}{2} \begin{vmatrix} \frac{3\lambda-5}{\lambda+1} & \frac{5\lambda+1}{\lambda+1} \\ 1 & 5 \\ 7 & 2 \\ \frac{3\lambda-5}{\lambda+1} & \frac{5\lambda+1}{\lambda+1} \end{vmatrix} = 42$$

61)



	-2	-1
X	$2 \cos 45^\circ$	$1 \cos 45^\circ$
Y	$-2 \sin 45^\circ$	$-1 \sin 45^\circ$

$$X = -2 \cos 45^\circ - 1 \sin 45^\circ$$

$$Y = -2 \sin 45^\circ - 1 \cos 45^\circ$$

62)  $(h, k) = (2, -1)$

$$X = x - 2, Y = y + 1$$

$$x_{\text{old}} = X + 2, y_{\text{old}} = Y - 1$$

$$(X+2)^2 + (Y-1)^2 - 4(X+2) + 2(Y-1) + 1 = 0$$

63)  $x = 4 - 1, y = 5 - (-2)$

$$(3, 7)$$

	x	y
4	$4 \cos 135^\circ$	$4 \sin 135^\circ$
-3	$-3 \cos 135^\circ$	$3 \sin 135^\circ$

$$x = 4 \cos 135^\circ + (-3) (-\sin 135^\circ)$$

$$y = 4 \sin 135^\circ + (-3) \cos 135^\circ$$



L.O.C.S.

① find Locus of a Pt. whose abscissa & Ordinate are equal.

A) Let Pt.  $(h, k)$

B)  $\left. \begin{array}{l} \text{abs} = h \\ \text{ord.} = k \end{array} \right\}$

C) Acc. to Qs  $\rightarrow h = k$   
 $x = y$   
 $\Rightarrow y - x = 0$  is locus.

Q<sub>2</sub> find Locus of a Pt.

whose dist. from X Axis is equal to dist. from Y Axis?

① let Pt.  $(h, k)$

② dist. of  $(h, k)$  from X Axis



dist of  $(h, k)$  from Y Axis  $= |h|$

(3) Acc. to Qs  $|h| = |k|$

$$\Rightarrow h^2 = k^2 \Rightarrow x^2 - y^2 = 0$$

A

Q<sub>3</sub> find Locus of Pt. whose dist. from origin is thrice of its dist. from X Axis

① let Pt  $(h, k)$

②  $(h, k)$ 's  $(0, 0)$  distance  $= \sqrt{(h-0)^2 + (k-0)^2}$   
 $= \sqrt{h^2 + k^2}$

(3) dist from origin  $= 3$  (dist. from X Axis)

$$\sqrt{h^2 + k^2} = 3|k|$$

$$h^2 + k^2 = 9k^2$$

$$h^2 - 8k^2 = 0$$

$$x^2 - 8y^2 = 0$$

A



Q Find Locus of a Pt. whose distance from  $P(2,3)$  remains 5 units always.

① Let  $Pt = (h, k)$

② dist. of  $(h, k)$  from  $(2, 3) = 5$

$$\Rightarrow \sqrt{(h-2)^2 + (k-3)^2} = 5$$

$$(h-2)^2 + (k-3)^2 = 25$$

$$(x-2)^2 + (y-3)^2 = 25$$



Q5 Find Locus of a Pt. whose distance from  $A(2,3)$  &  $B(5,7)$  Remains Same/Equal.

① Let  $Pt. = (h, k)$

② dist. of  $(h, k)$  from  $(2, 3)$  = dist. of  $(h, k)$  from  $(5, 7)$

$$\Rightarrow \sqrt{(h-2)^2 + (k-3)^2} = \sqrt{(h-5)^2 + (k-7)^2}$$

$$\Rightarrow h^2 + k^2 - 4h - 6k + 13 = h^2 + k^2 - 10h - 14k + 74$$

$$6h + 8k = 61$$

$$6x + 8y = 61 \text{ is locus.}$$

Extra Note

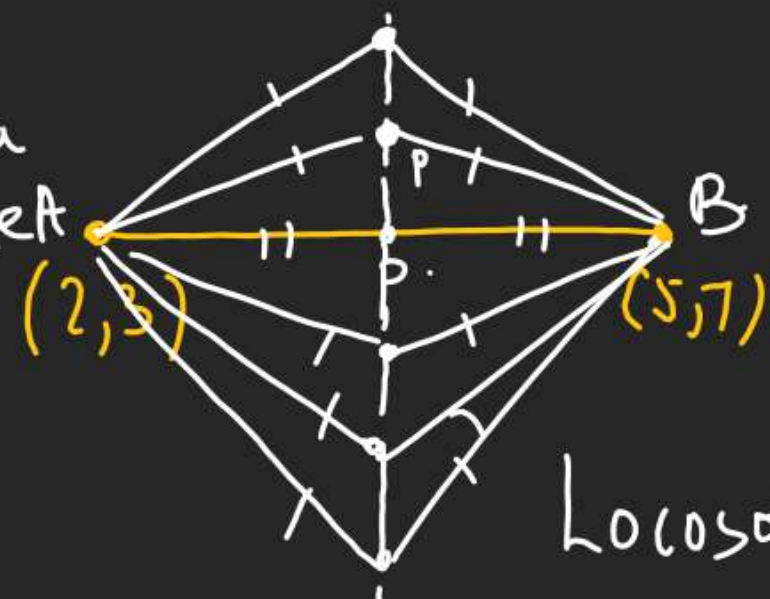


diagram.  
Locus of P is  $\perp$  Bisector of Line AB

Q6 Find locus of a Pt. whose Sum of distances from 2  $\perp^r$  lines is 1 Unit.



Locus  $\rightarrow |x| + |y| = 1$

$\uparrow$  Axes  
Hint  
C1



Q If  $P(1,0), Q(-1,0), R(2,0)$

then find locus of a pt  $S$ , such.

that  $SQ^2 + SR^2 = 2SP^2$

A) Line  $\perp$  to x Axis

B) Line  $\perp$  to y Axis

C) Circle (D) NOT.

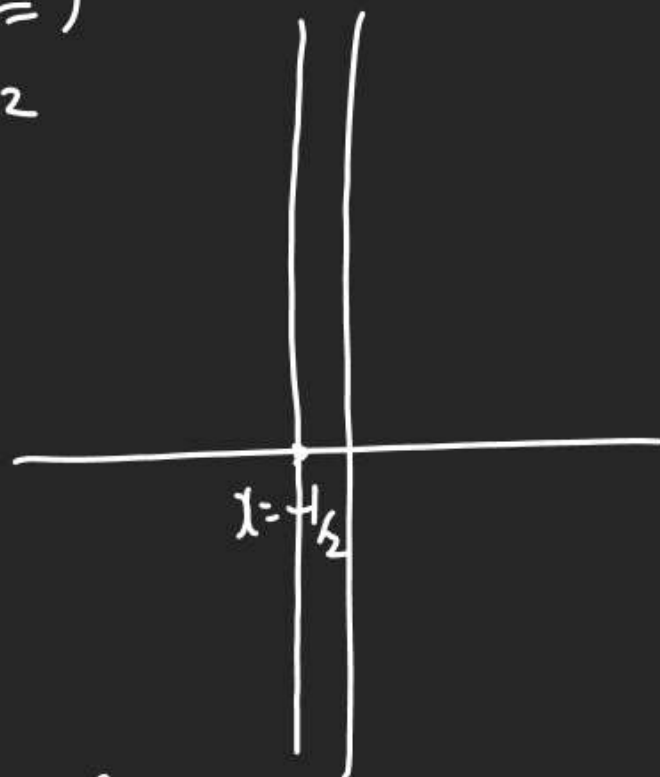
① Let  $S = (h, k)$

$$(SQ)^2 + (SR)^2 = 2(SP)^2$$

$$(h+1)^2 + (k-0)^2 + (h-2)^2 + (k-0)^2 = 2\{(h-1)^2 + (k-0)^2\}$$

$$h^2 + 2h + 1 + k^2 + h^2 - 4h + 4 + k^2 = 2h^2 - 4h + 4 + 2k^2$$

$$2h + 5 = 4 \Rightarrow h = -\frac{1}{2} \Rightarrow \text{Line } x = -\frac{1}{2}$$



Q Find locus of a pt.

Such that sum of its distance from  $(0, 2)$  &  $(0, -2)$  is 6.

① Let  $P = (h, k)$

$$\sqrt{(h-0)^2 + (k-2)^2} + \sqrt{(h-0)^2 + (k+2)^2} = 6$$

$$\sqrt{h^2 + (k-2)^2} = 6 - \sqrt{h^2 + (k+2)^2}$$

$$h^2 + (k-2)^2 = 36 + h^2 + (k+2)^2 - 12\sqrt{h^2 + (k+2)^2}$$

$$k^2 - 4k + 4 = 36 + k^2 + 4k + 4 - 12\sqrt{h^2 + (k+2)^2}$$

$$3\sqrt{h^2 + (k+2)^2} = 2k + 36$$

$$9(h^2 + k^2 + 4k + 4) = 4k^2 + 81 + 36k$$

