

$$\frac{1}{a}, \frac{1}{H_1}, \dots, \frac{1}{H_n}, \frac{1}{c} \Rightarrow \frac{1}{H_1} = \frac{1}{a} + \frac{\frac{1}{c} - \frac{1}{a}}{n+1} = \frac{(n+1)c + (a-c)}{ac(n+1)}$$

$$\frac{ac(n+1)}{nc+a} - \frac{ac(n+1)}{na+c} = \frac{ac(n+1)(\cancel{n+1})(a-c)}{(1+n)ac + n(a^2+c^2)} = ac(a-c)$$

$$\frac{(n+1)(n+2)(n+3)(n+4)}{(n+1)(n+2)} - \dots - \frac{2 \cdot 1}{1 \cdot 2} = \frac{a_n}{a_1}$$

$$\therefore a_{n+1} = (n+1)ac + n(a^2+c^2)$$

$$\frac{\sqrt{a_n}}{a_{n+1}} = \frac{n+1}{n+2} \quad \frac{a_{n+1}}{a_{n+2}} = \frac{n+1}{n+2}$$

$$\frac{a_2}{a_1} = \frac{2}{3}$$

$9 \text{ min} \rightarrow 150 \times 9 = 1350$

$150, 148, 146, \dots, 10, -$

\downarrow

$$9(25a^2) + 9b^2 + 25c^2 \\ = 25 \times 3a^2 + 15b^2 + 15c^2 \\ = 25 \times 3 \times 150 = \frac{1}{2}(300 + (n-1)(-2))$$

$$r = 3b = 15a = 5c \quad n = ?$$

$$(a, b, c) = \left(\frac{1}{5}, \frac{1}{3}, \frac{1}{5}\right)$$

$n+9$

$G_1, G_2, G_3, G.M.S$

$$\left(\frac{6}{5}, \frac{1}{3}, \frac{1}{5}\right)$$

$$\frac{\left(1^2 + \dots + n^2\right) + \left(2^2 + 4^2 + \dots + n^2\right)}{2 \cdot n^2}$$

$$\frac{n(n+1)(2n+1)}{6} + \frac{\frac{1}{2}(n^2+1)(n+1)}{6}$$

~~$$\frac{n(n+1)^2}{2}$$~~

$$1^2 + 2^2 + 3^2 + \dots + (n-1)^2 + n^2$$

$$\frac{(n-1)n^2}{2} + n^2$$

1.

$$2 \sin\left(3x + \frac{\pi}{4}\right) = \sqrt{1 + 8 \sin 2x \cos 2x}$$

$$\rightarrow \pi$$

$$T = 2\pi$$

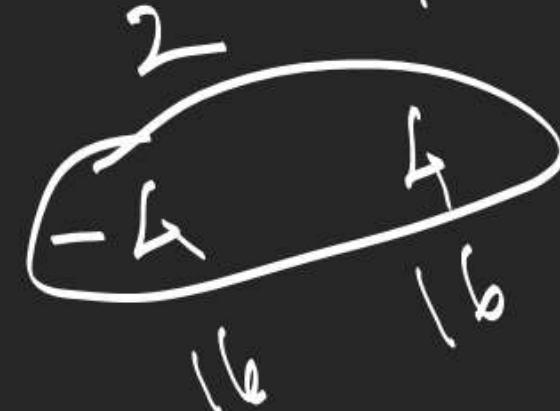
$$4 \sin^2\left(3x + \frac{\pi}{4}\right) = 1 + 4 \sin 4x \cos 2x$$

$$2 \left(1 - \cos\left(6x + \frac{\pi}{2}\right)\right) = 1 + 2(\cancel{\sin 6x} + \sin 2x) = 2 + 2 \sin 2x$$

sin

$$\sin\left(x + \frac{\pi}{4}\right)$$

$$x \in [0, 2\pi]$$



$$2x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}, \frac{17\pi}{6}$$

$$x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}$$

$$\sin 2x = \frac{1}{2}$$

$$x = 2n\pi + \frac{\pi}{12}, 2n\pi + \frac{17\pi}{12}$$

$$n \in \mathbb{Z}$$

Q:

$$\frac{1}{\sin^2 x} \geq 1 \quad \Rightarrow \quad \sqrt{y^2 - 2y + 2} \leq 2.$$

$\geq 2 \qquad \qquad \geq 1$

≥ 2

, find x, y .

$$\csc^2 x = 1 \quad \sin^2 x = 1$$

$y = 1$
 $x = n\pi \pm \frac{\pi}{2}, n \in \mathbb{Z}$

$$\sin \theta \geq 1$$

$$\sin \theta = 1$$

3. Solve for x, y satisfying

$$\cos x \cos y = \frac{3}{4} \quad \text{and} \quad \sin x \sin y = \frac{1}{4}$$

$$\cos(x-y) = 1$$

$$\Rightarrow x-y = 2n\pi$$

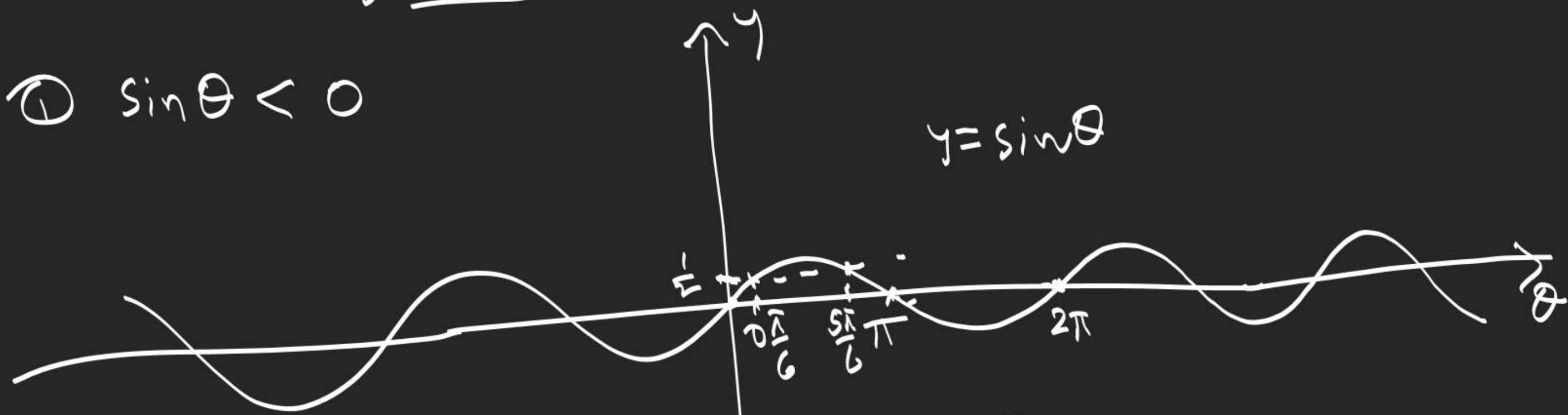
$$\cos(x+y) = \frac{1}{2}$$

$$\Rightarrow x+y = 2m\pi \pm \frac{\pi}{3}$$

$$\boxed{m, n \in \mathbb{Z}} \quad \begin{aligned} x &= (n+m)\pi \pm \frac{\pi}{6} \\ y &= (m-n)\pi \pm \frac{\pi}{6} \end{aligned}$$

Inequality.

$$\textcircled{1} \quad \sin \theta < 0$$

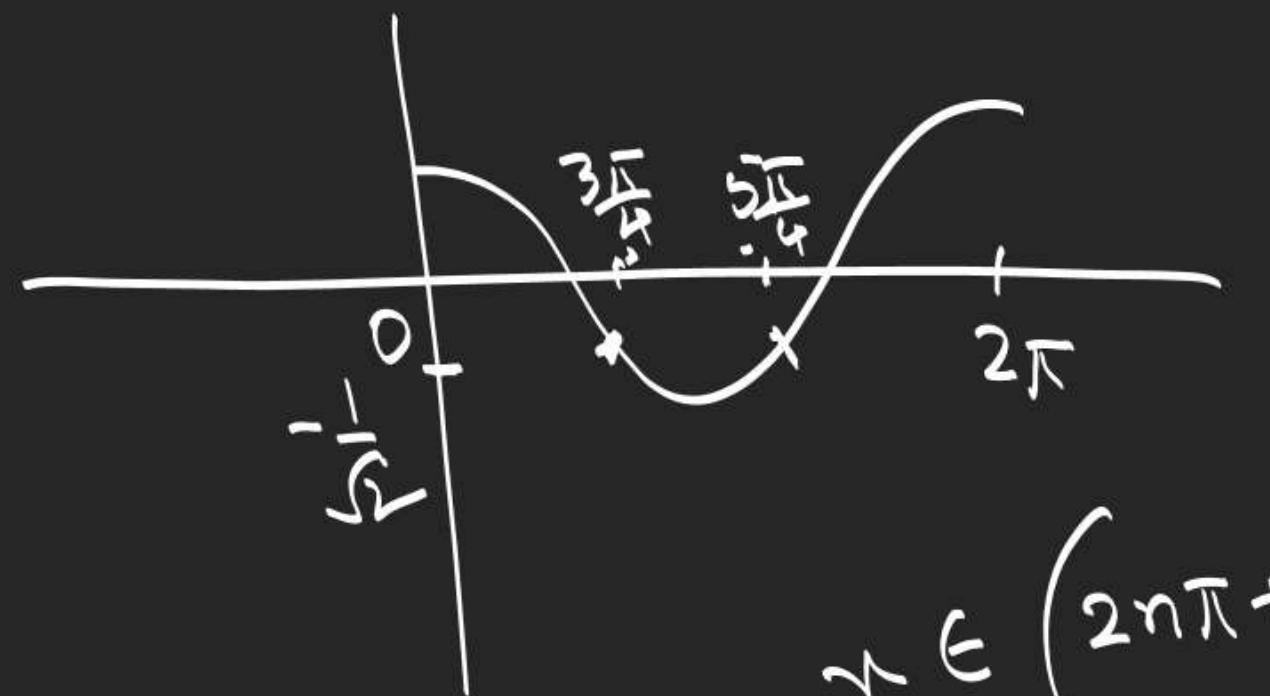


$$\boxed{\theta \in (2n\pi + \pi, 2n\pi + 2\pi) , n \in \mathbb{I}}$$

$$\textcircled{2} \quad \sin \theta > \frac{1}{2}$$

$$\boxed{\theta \in \left(2n\pi + \frac{\pi}{6}, 2n\pi + \frac{5\pi}{6}\right) , n \in \mathbb{I}}$$

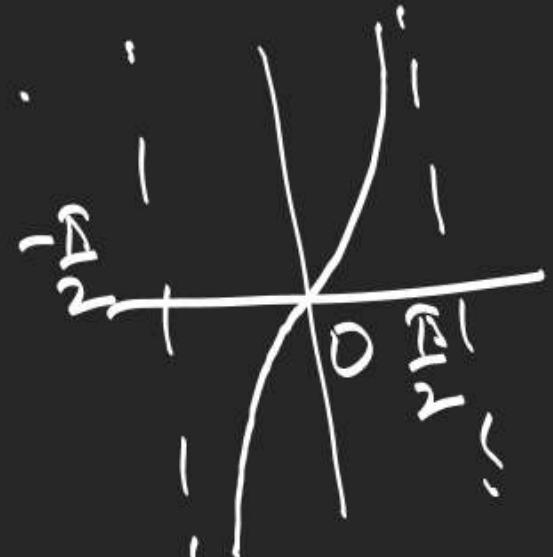
$$\underline{3} : \cos x < -\frac{1}{\sqrt{2}}$$



$$x \in \left(2n\pi + \frac{3\pi}{4}, 2n\pi + \frac{5\pi}{4}\right), n \in \mathbb{I} .$$

4.

$$\tan x > 0$$



$$x \in \left(n\pi + 0, n\pi + \frac{\pi}{2}\right), n \in \mathbb{I}$$

5.

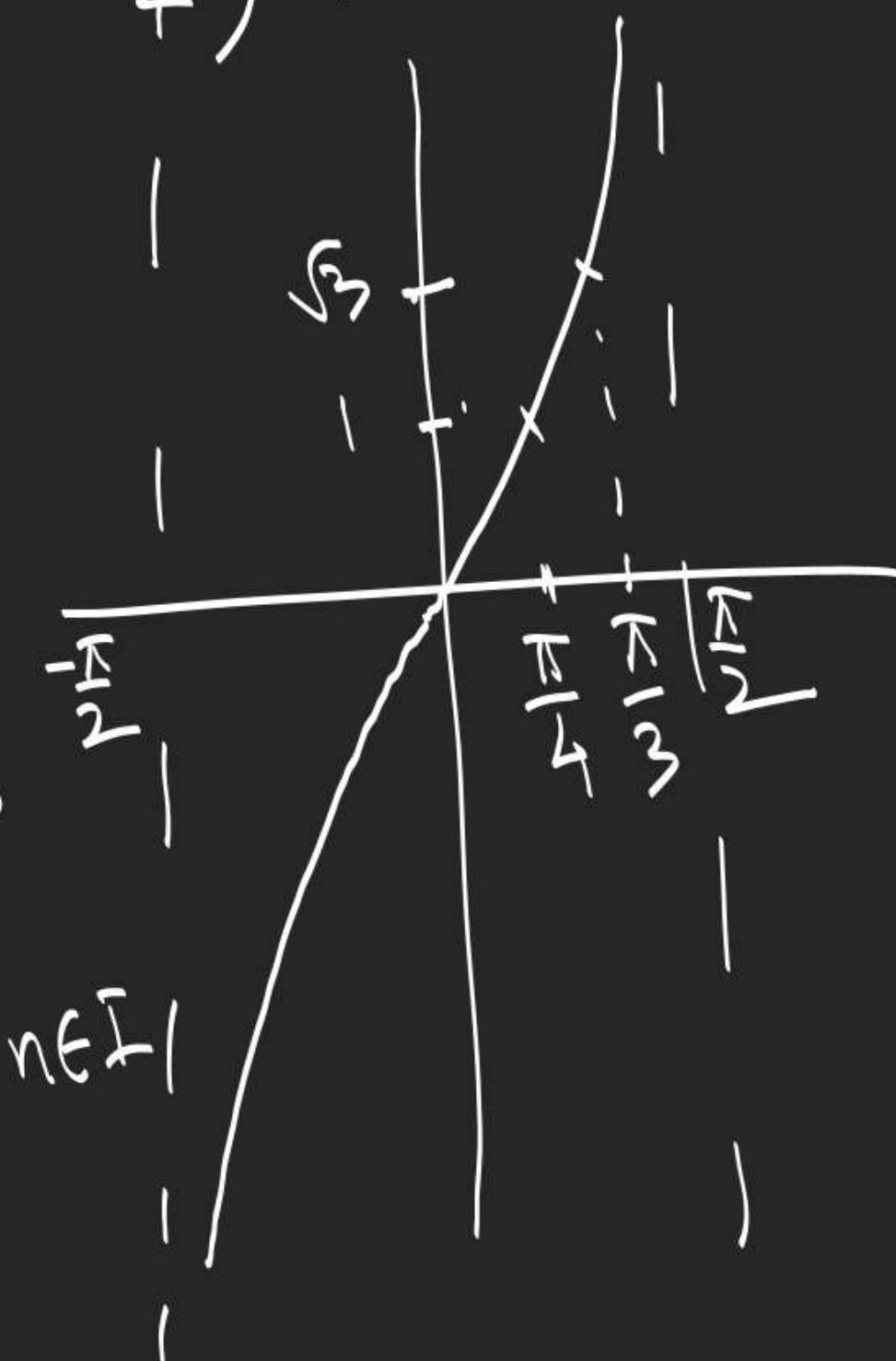
$$\tan^2 x - (\sqrt{3} + 1) \tan x + \sqrt{3} < 0$$

$$(\tan x - \sqrt{3})(\tan x - 1) < 0$$



$$1 < \tan x < \sqrt{3}$$

$$x \in \left(n\pi + \frac{\pi}{4}, n\pi + \frac{\pi}{3}\right), n \in \mathbb{I}$$



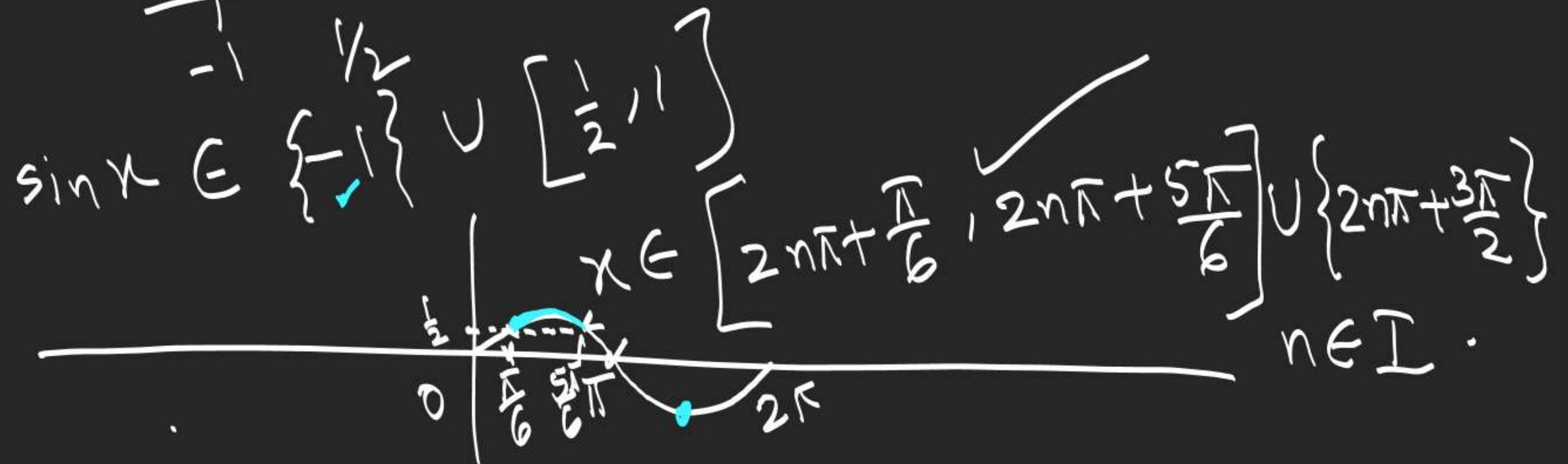
$$\underline{6:} \quad \sin x \geq \underline{\cos 2x} = 1 - 2\sin^2 x$$

$$2\sin^2 x + \sin x - 1 \geq 0$$

$$2\sin x - \sin x$$

$$(2\sin x - 1)(\sin x + 1) \geq 0$$

$$\begin{array}{c} x \\ + - + \end{array}$$



PT-1, 2, 3

Trig. Eqn.

Find no. of solutions
 $\sin x + 2 \sin 2x = 3 + \sin 3x$ in $[0, \pi]$

$$\underbrace{\sin x - \sin 3x}_{\leq 2} + 2 \sin 2x = 3$$



$$-2 \sin x \cos 2x + 4 \sin x \cos x = 3$$

$$2 \underbrace{\sin x}_{\leq 2} \left(2 \cos x - 2 \cos^2 x + 1 \right) = 3$$

$$\leq 2\left(\frac{1}{2}\right) - 2\left(\frac{1}{4}\right) + 1 \geq \frac{3}{2}$$

$$\leq 3$$