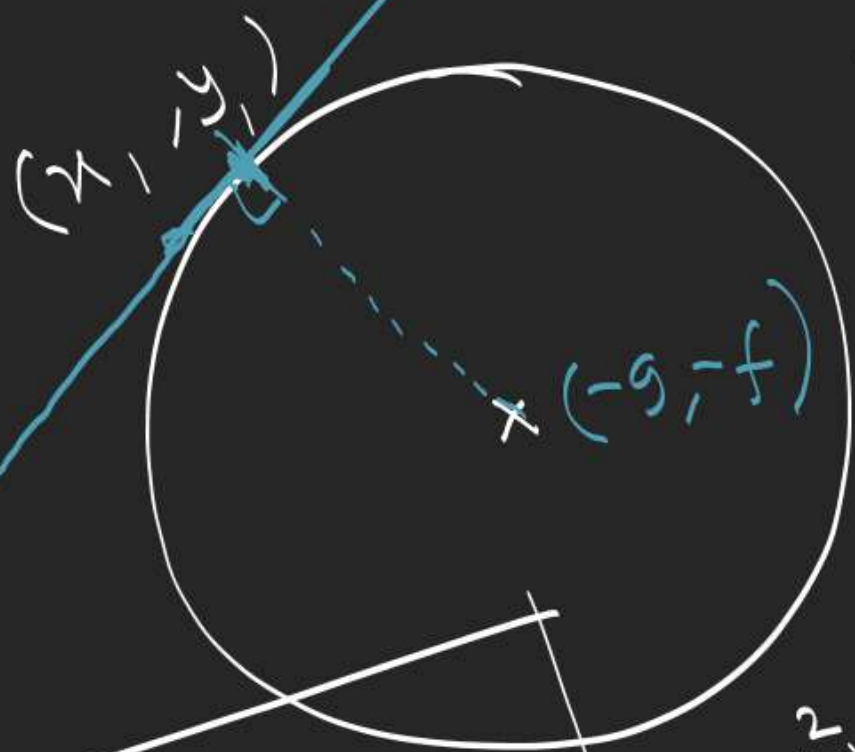


Tangent



$$ax^2 + by^2 + 2hxy + 2gx + 2fy + c = 0$$

$\times (x_1, y_1)$

$$\begin{aligned} x^2 &\rightarrow xx_1 \\ y^2 &\rightarrow yy_1 \\ x &\rightarrow \frac{x+x_1}{2} \\ y &\rightarrow \frac{y+y_1}{2} \\ c &\rightarrow c \end{aligned}$$

$$\begin{aligned} x &\rightarrow \frac{x+y_1}{2} \\ xy &\rightarrow \frac{xy_1 + yx_1}{2} \\ c &\rightarrow c \end{aligned}$$

$$-\frac{x_1+g}{y_1+f}(x-x_1) = y-y_1$$

$$-xx_1 + x_1^2 - gx + gx_1 = y_1^2 - y_1^2 + fy - fy_1$$

$$xx_1 + yy_1 + gx + fy = x_1^2 + y_1^2 + gx_1 + fy_1$$

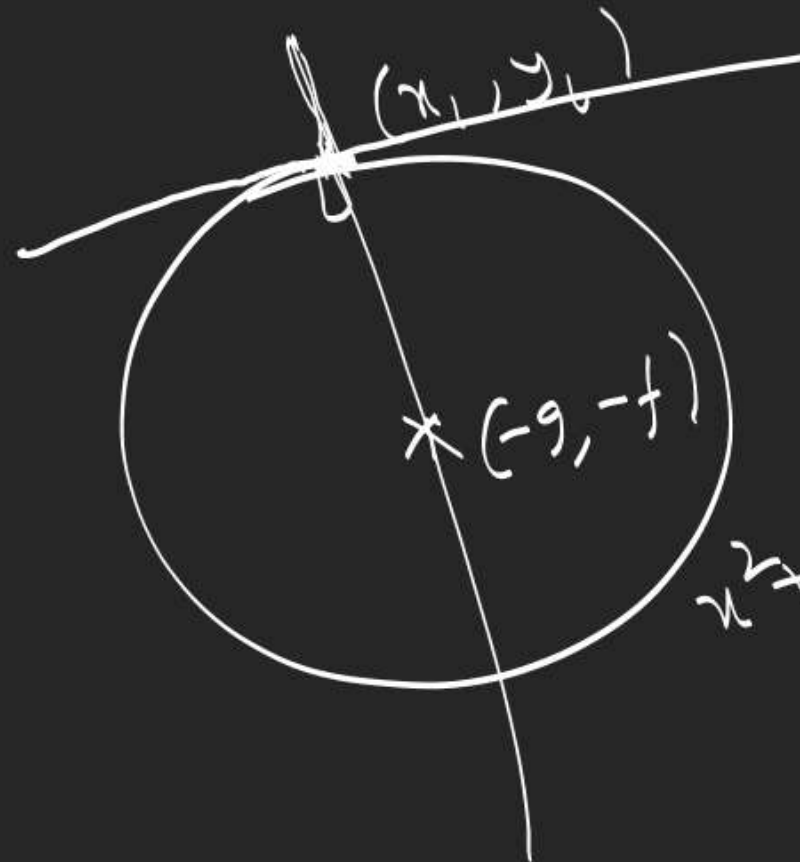
$$xx_1 + yy_1 + g(x+x_1) + f(y+y_1) + c$$

$$S = x^2 + y^2 + 2gx + 2fy + c = 0 \quad = x_1^2 + y_1^2 + 2gx_1 + 2fy_1 + c$$

$$xx_1 + yy_1 + g(x+x_1) + f(y+y_1) + c = 0$$

$$T = 0$$

Normal



$$x^2 + y^2 + 2gx + 2fy + c = 0$$

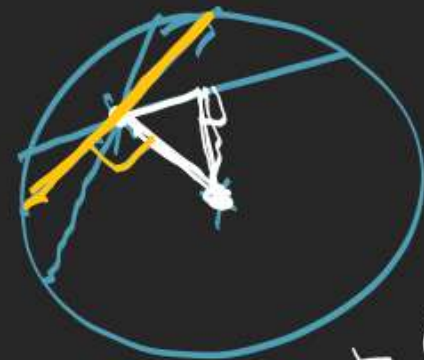
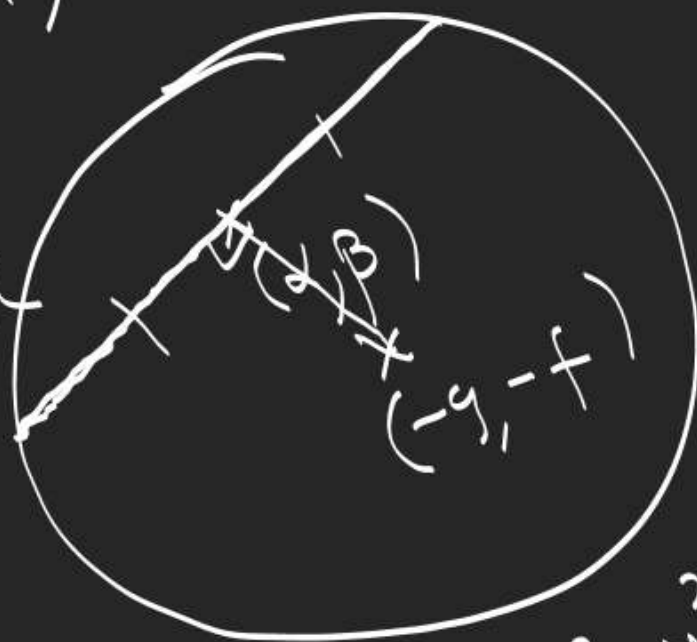
$$y - y_1 = \left(\frac{y_1 + f}{x_1 + g} \right) (x - x_1)$$

Chord whose midpoint is given / Chord

passing thru (α, β) situated
at max. distance from centre

$$y - \beta = -\left(\frac{\alpha + g}{\beta + f}\right)(x - \alpha)$$

$$y\beta - \beta^2 + fy - \beta f = -\alpha x + \alpha^2 - g\alpha + g\alpha$$



Shortest chord
thru (α, β)

$$x^2 + y^2 + 2gx + 2fy + c = 0$$

$$T = S_1$$

$$\alpha x + \beta y + g(\alpha + x) + f(\beta + y) + c = \alpha^2 + \beta^2 + 2g\alpha + 2f\beta + c$$

$$2\sqrt{r^2 - p^2} = L$$

Chord of Contact of a point w.r.t Circle

