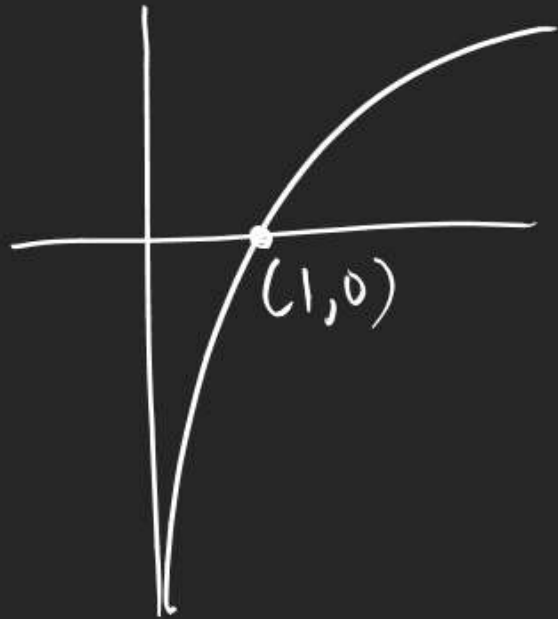
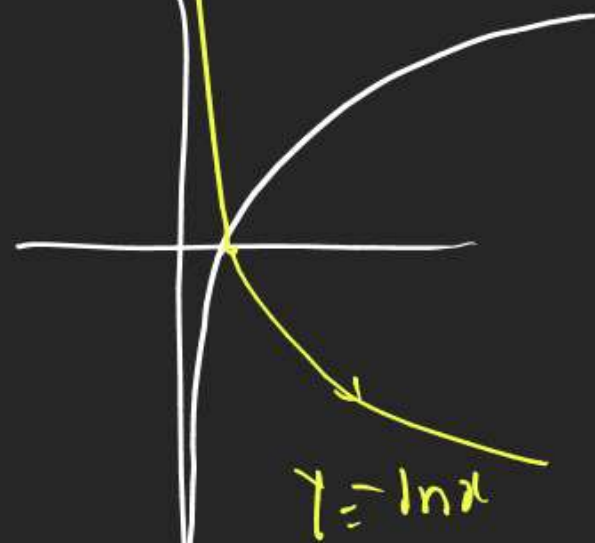


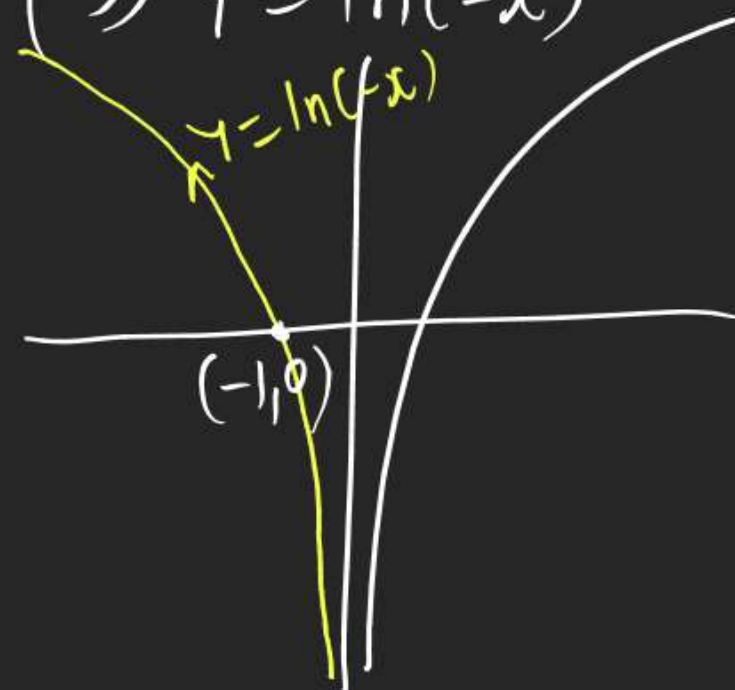
① $y = \ln x$



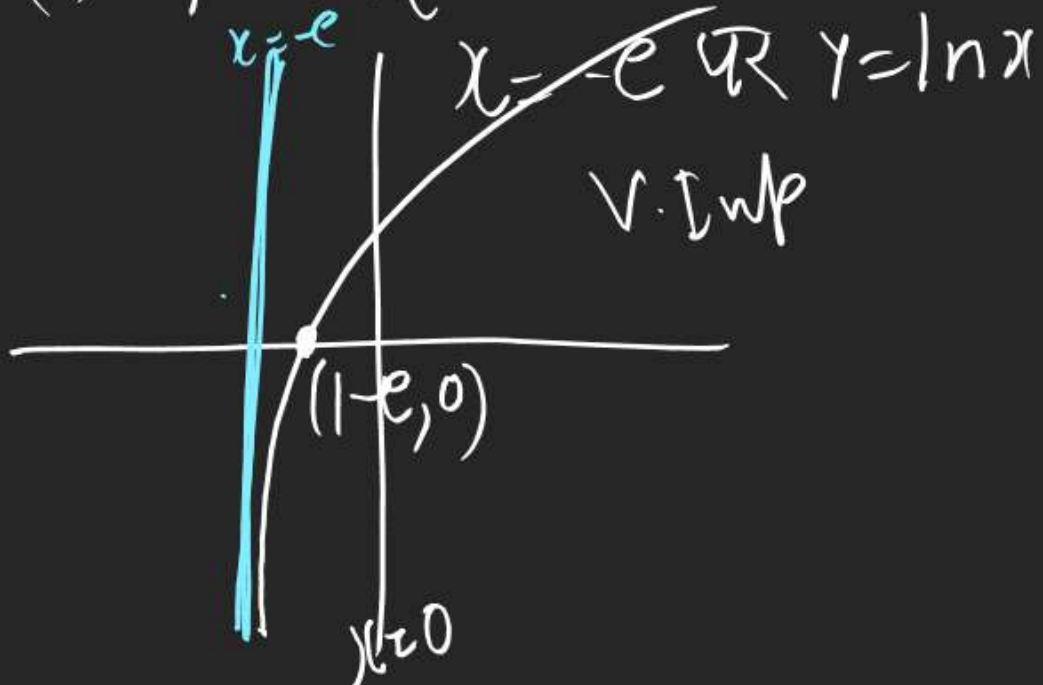
② $y = -\ln x$



③ $y = \ln(-x)$



④ $y = \ln(x + e)$ $f(x) + K$ $f(x + K)$



\propto Speed

Accuracy

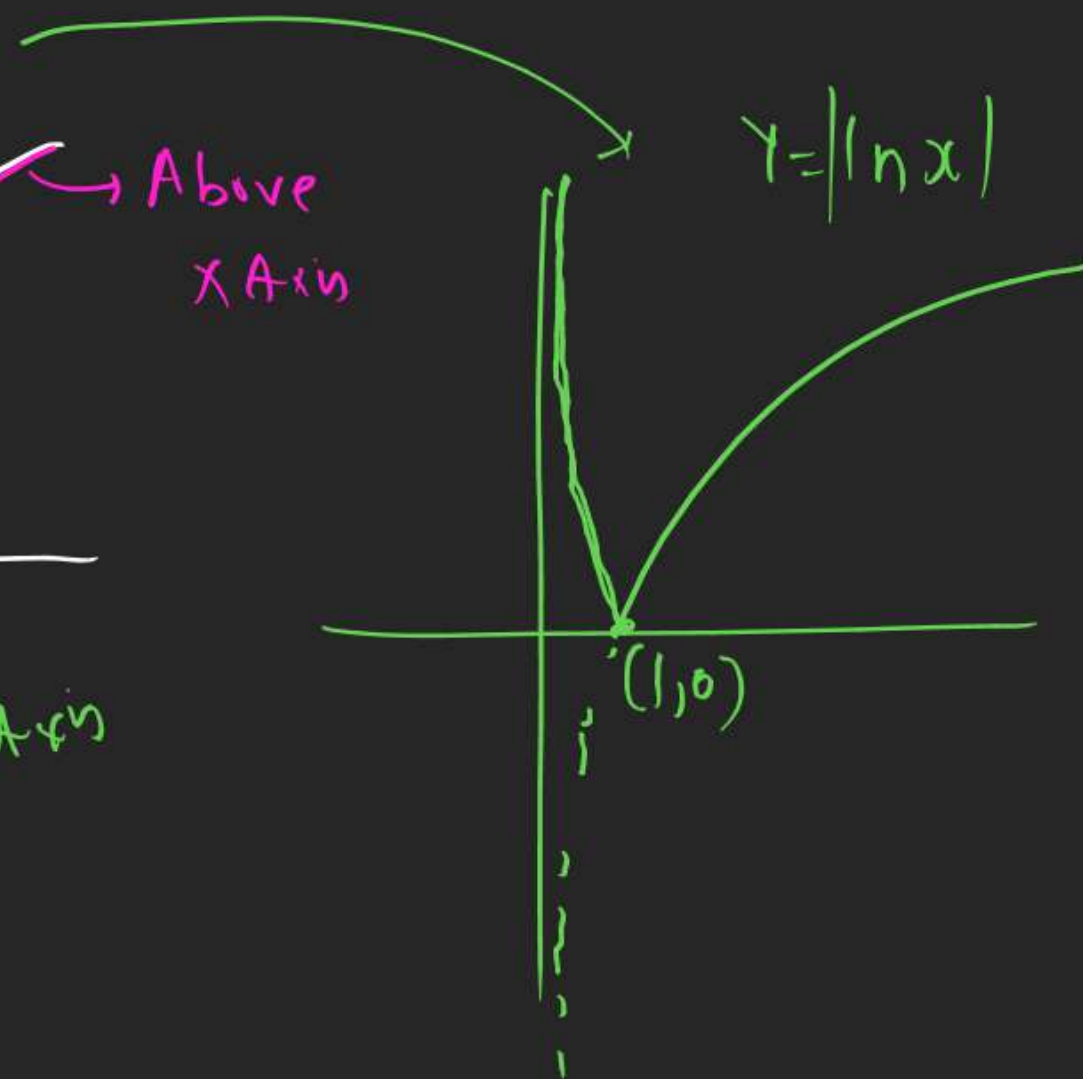
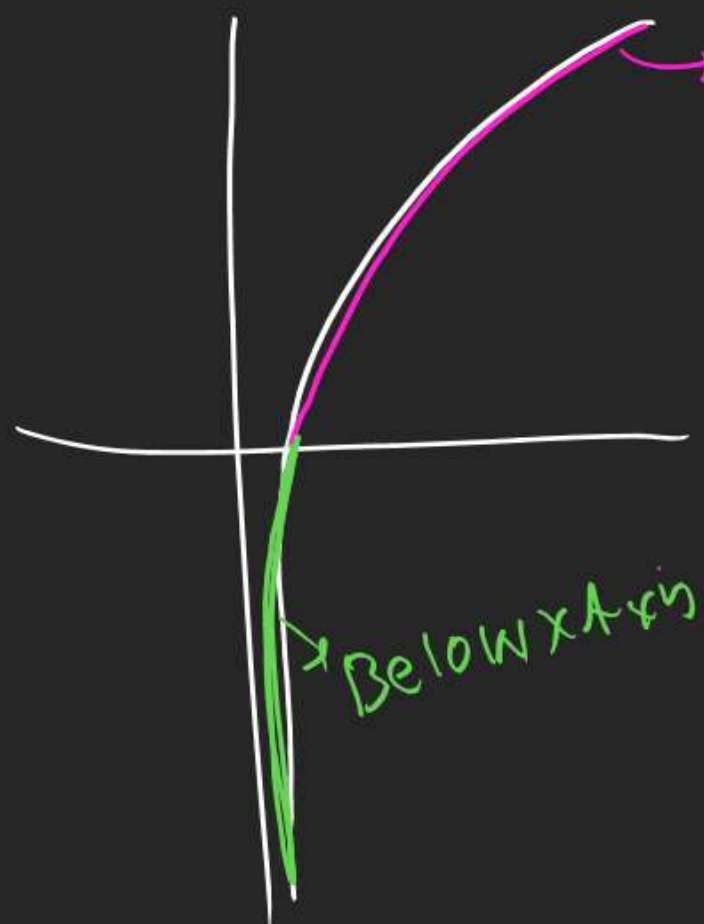
Time Spent

School ✓

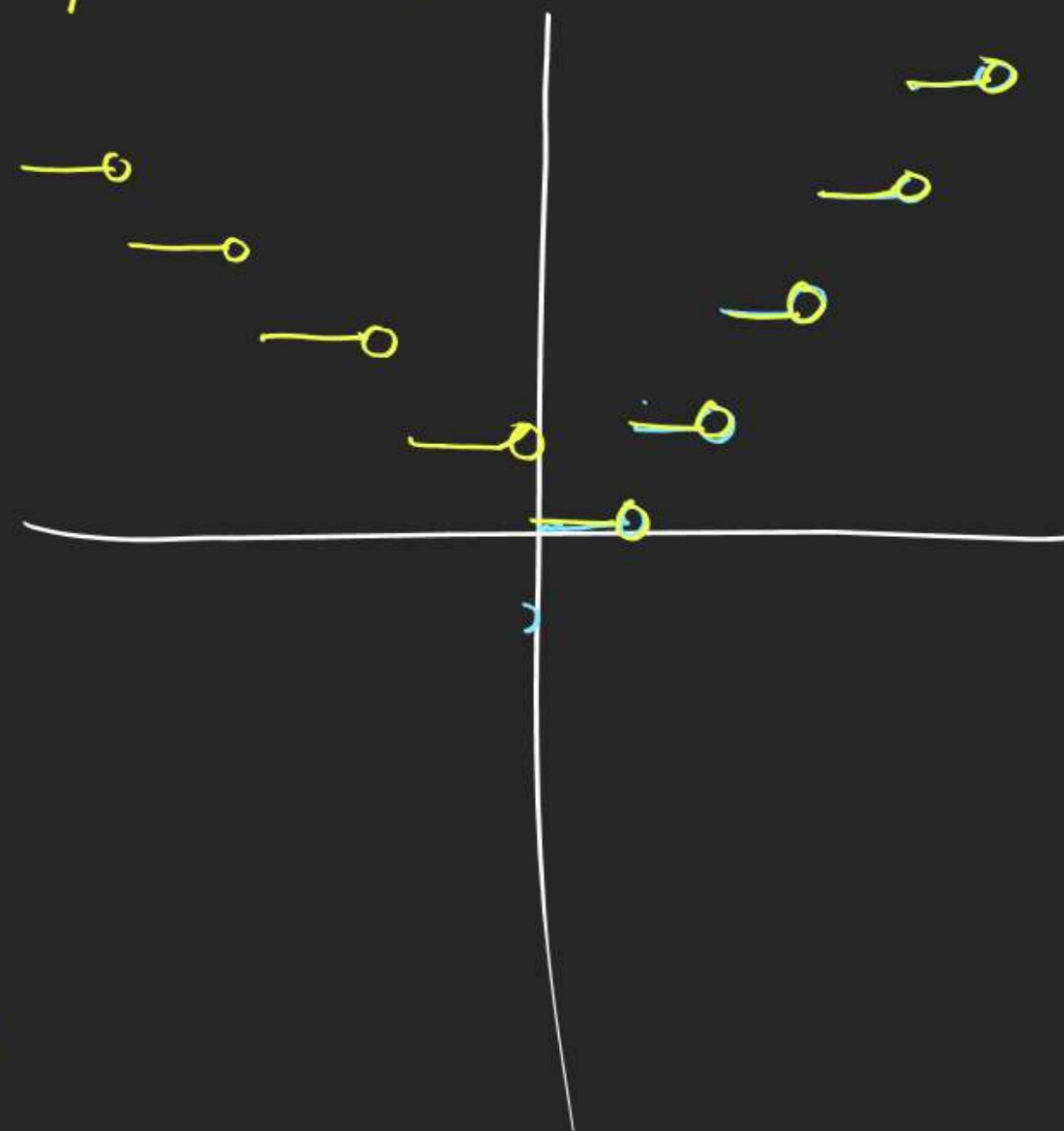
$$y = |f(x)| = \begin{cases} f(x) & f(x) \geq 0 \\ -f(x) & f(x) < 0 \end{cases}$$

$f(x) \geq 0 \rightarrow$ Jha $f(x)$ y Axis k above hai
 $f(x) < 0 \rightarrow$ $f(x)$ y Axis k Below.

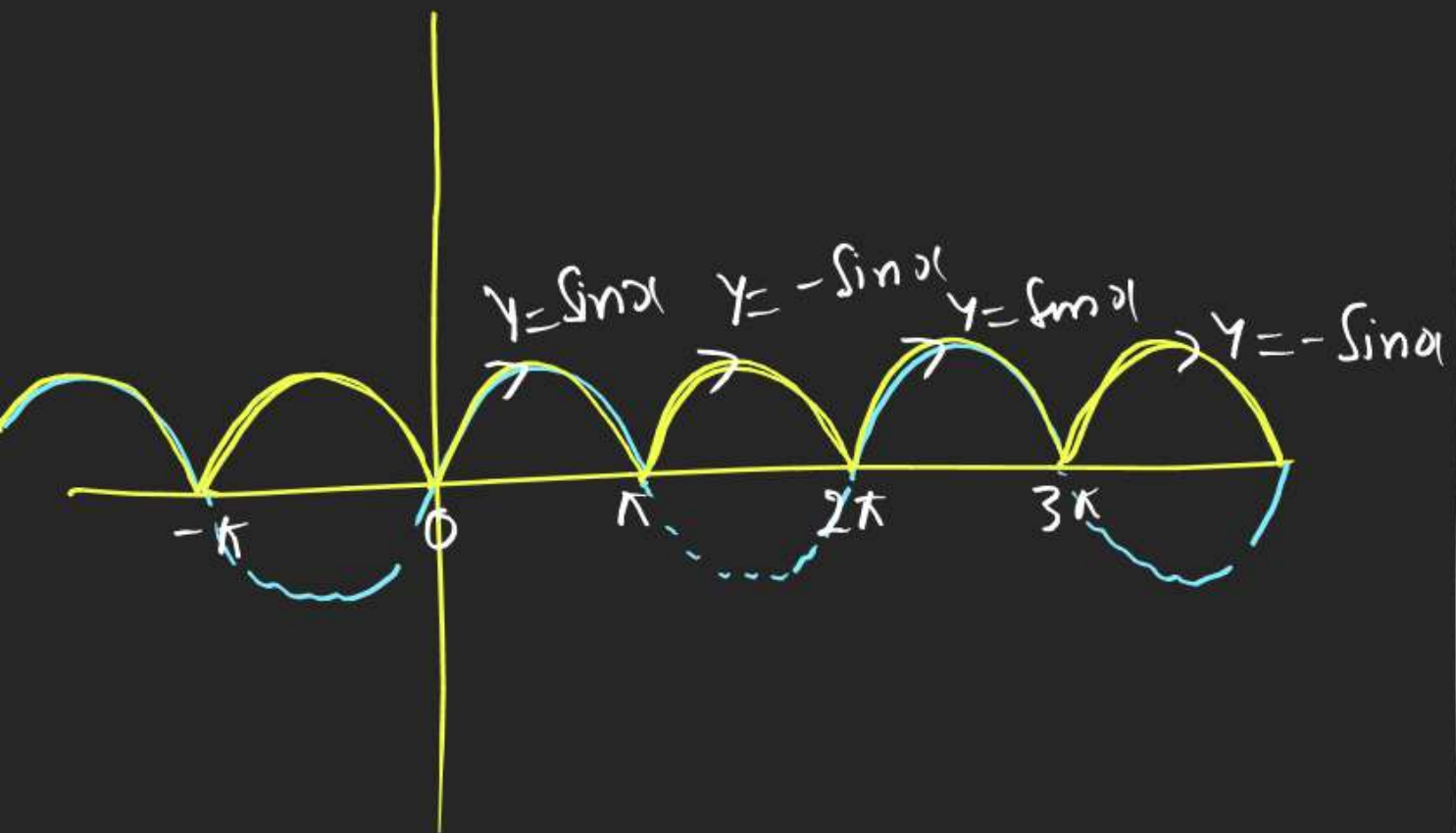
$$y = |\ln x|$$



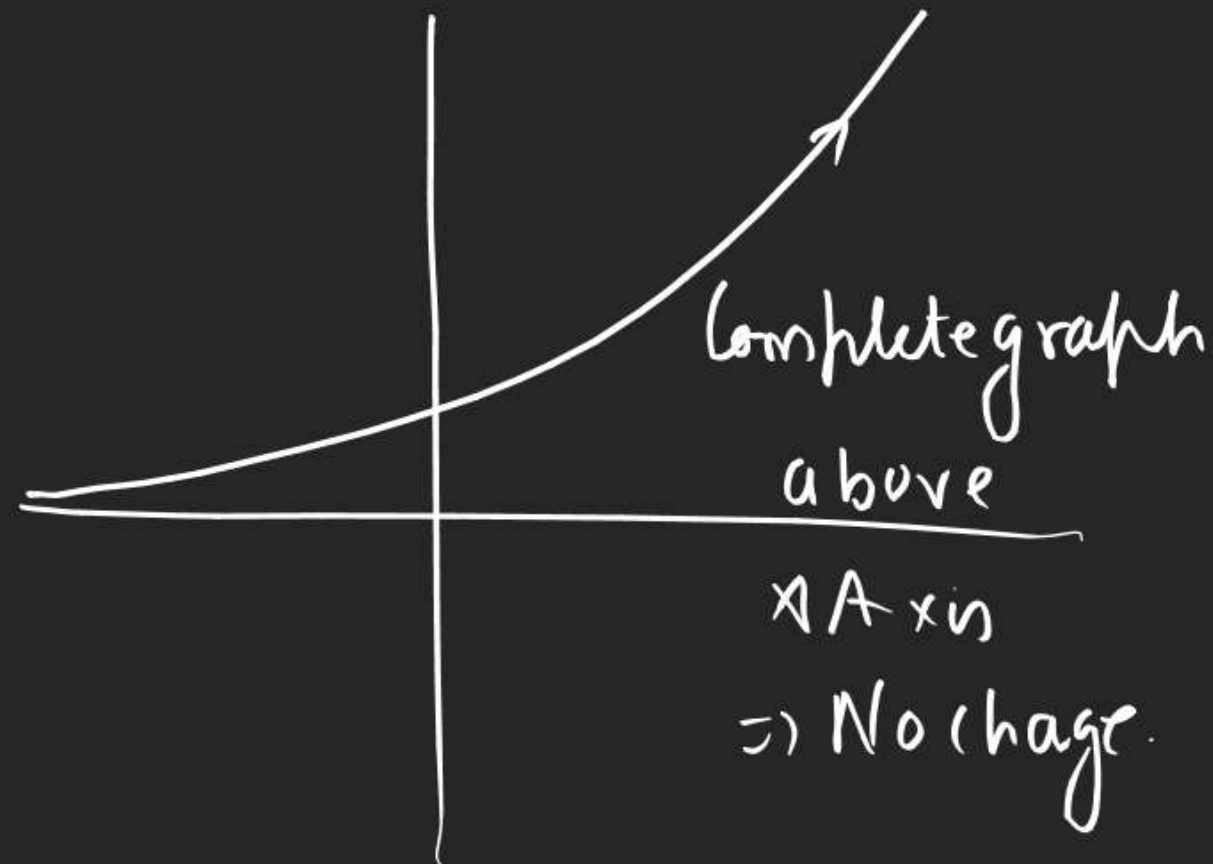
$$y = |\lceil x \rceil|$$



$$y = |\sin x|$$

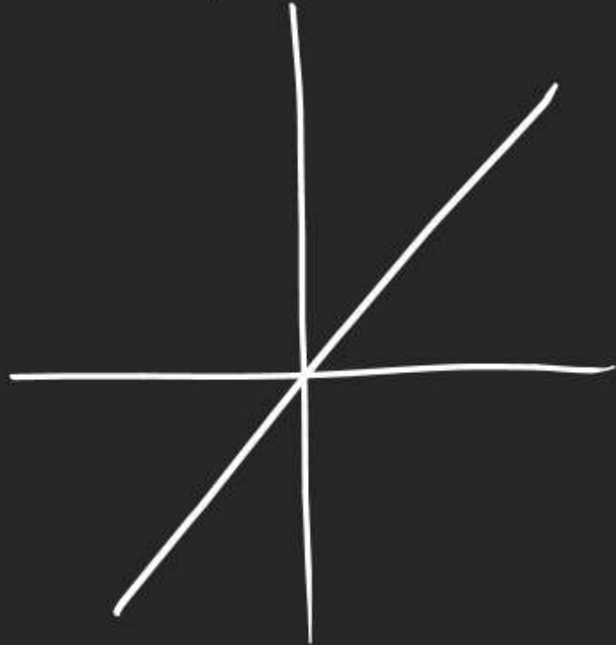


$$y = |e^x|$$



9 Basic graphs

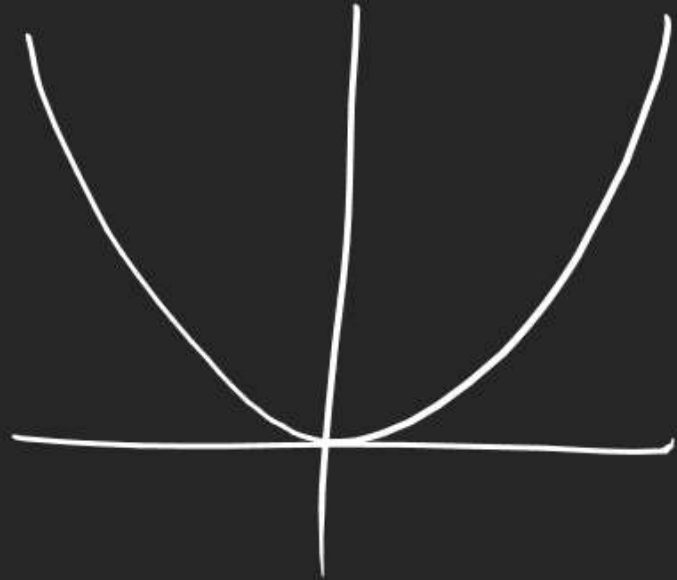
(1) $y = x$



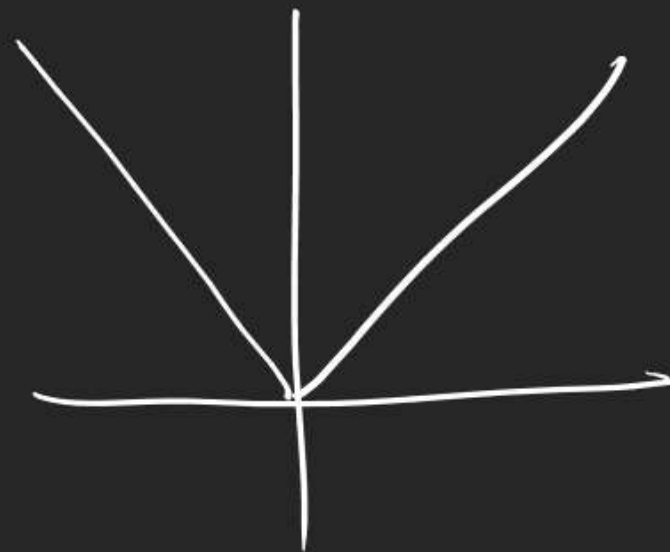
(2) $y = -x$



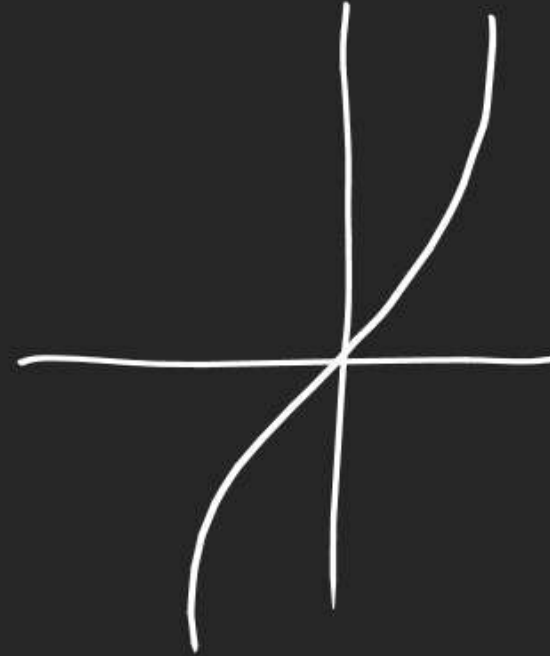
(3) $y = x^2$



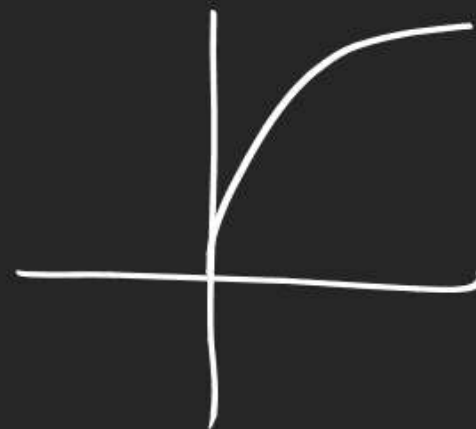
(4) $y = |x|$



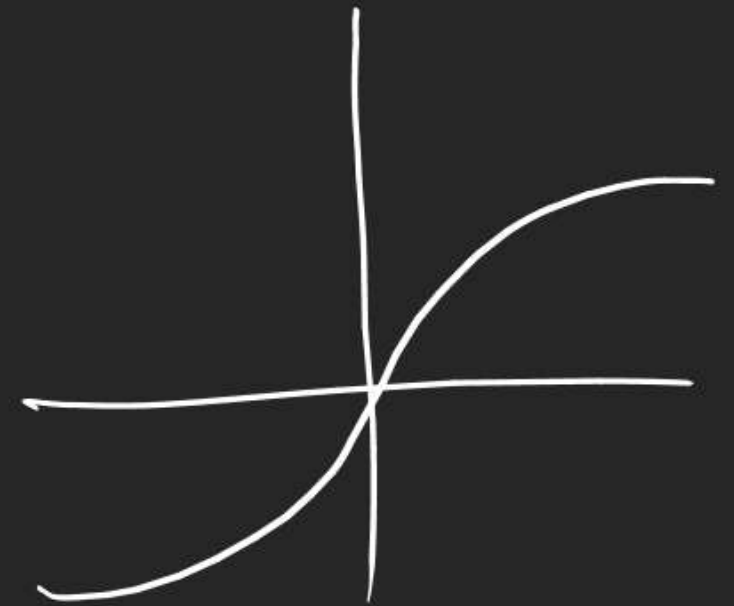
(5) $y = x^3$



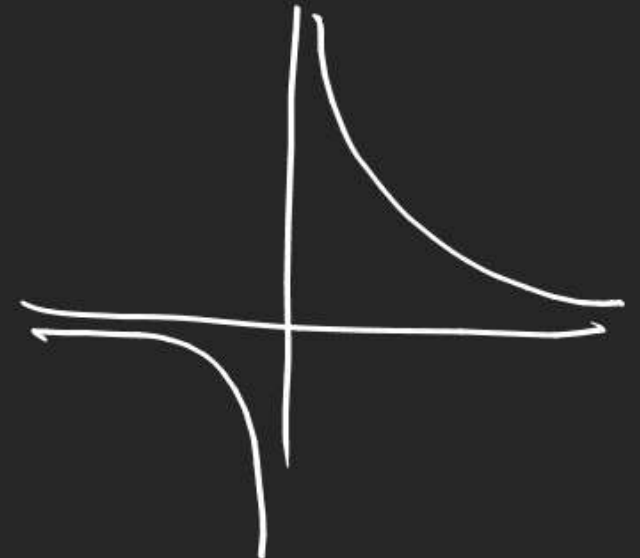
(6) $y = \sqrt{x}$



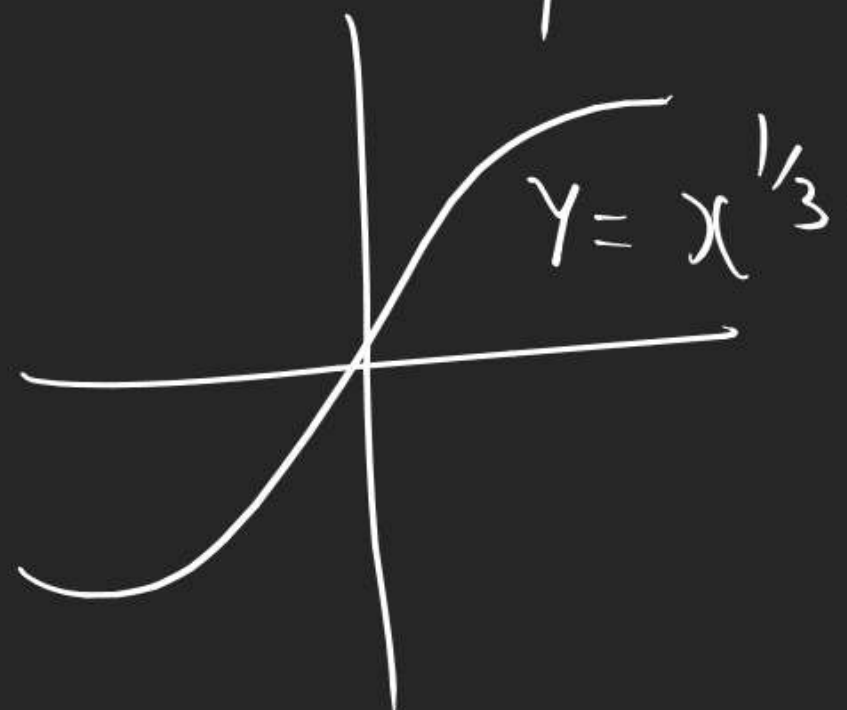
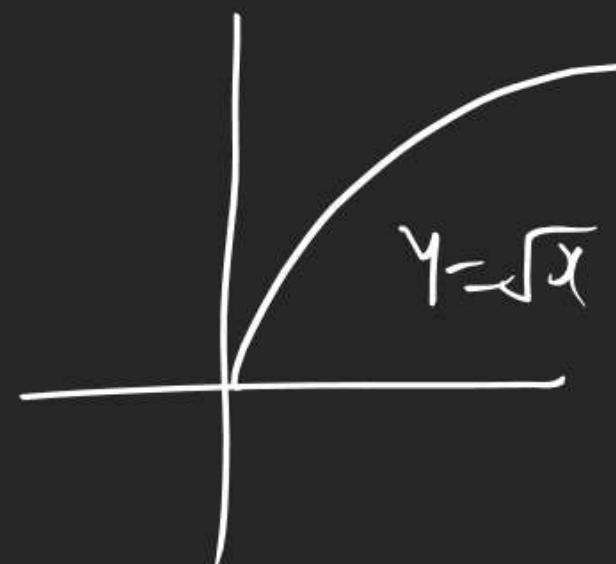
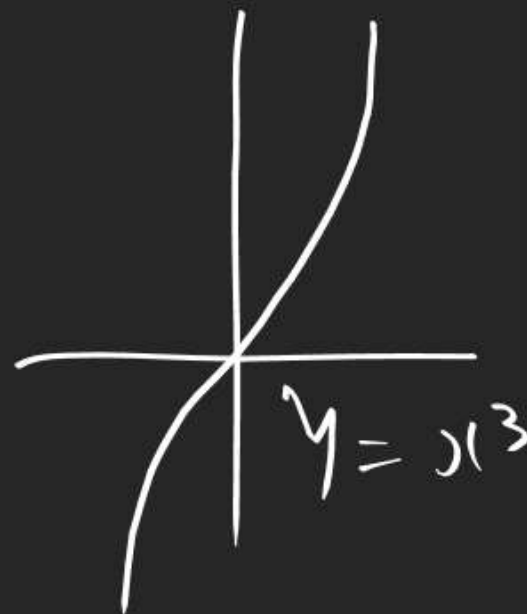
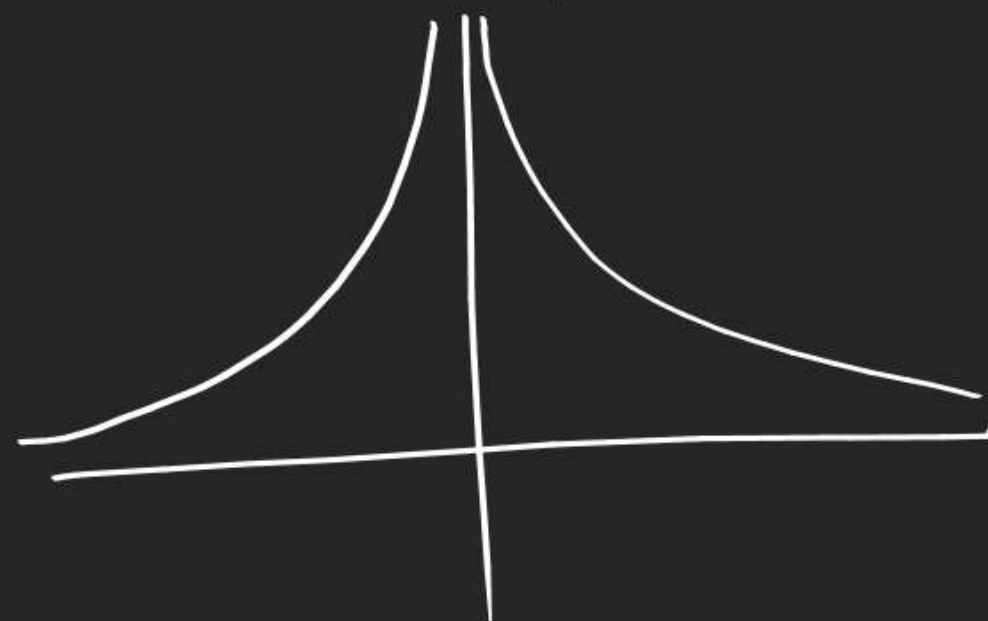
(7) $y = x^{1/3}$



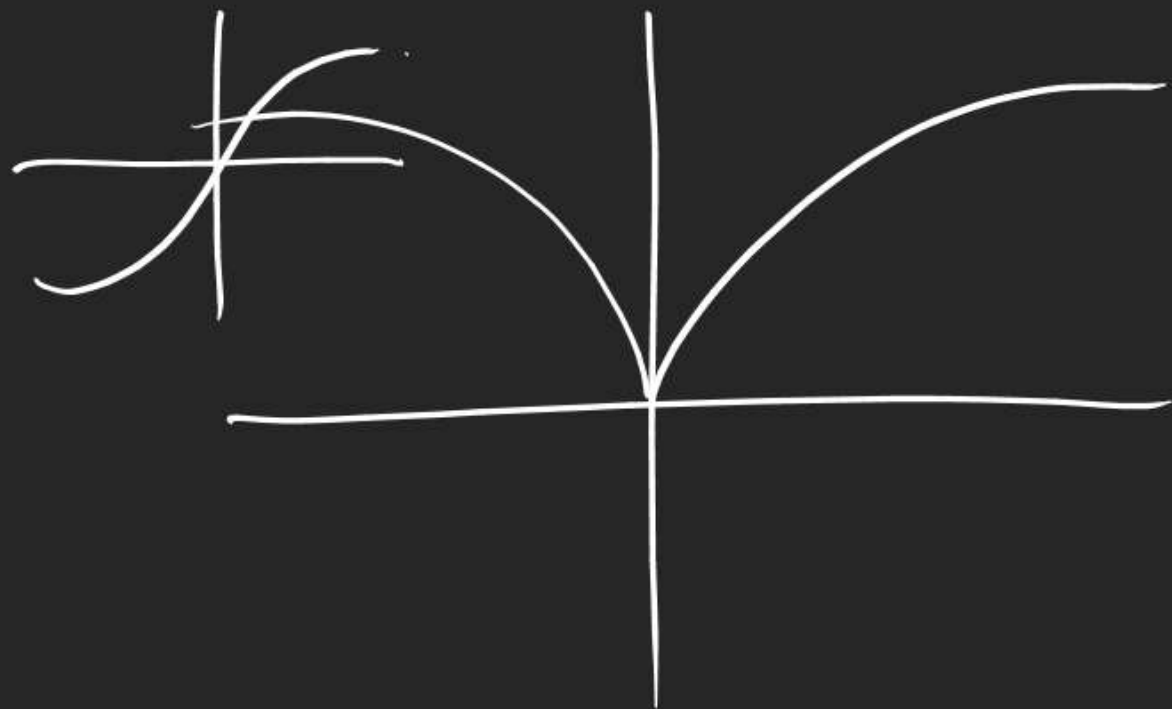
(8) $y = \frac{1}{x}$



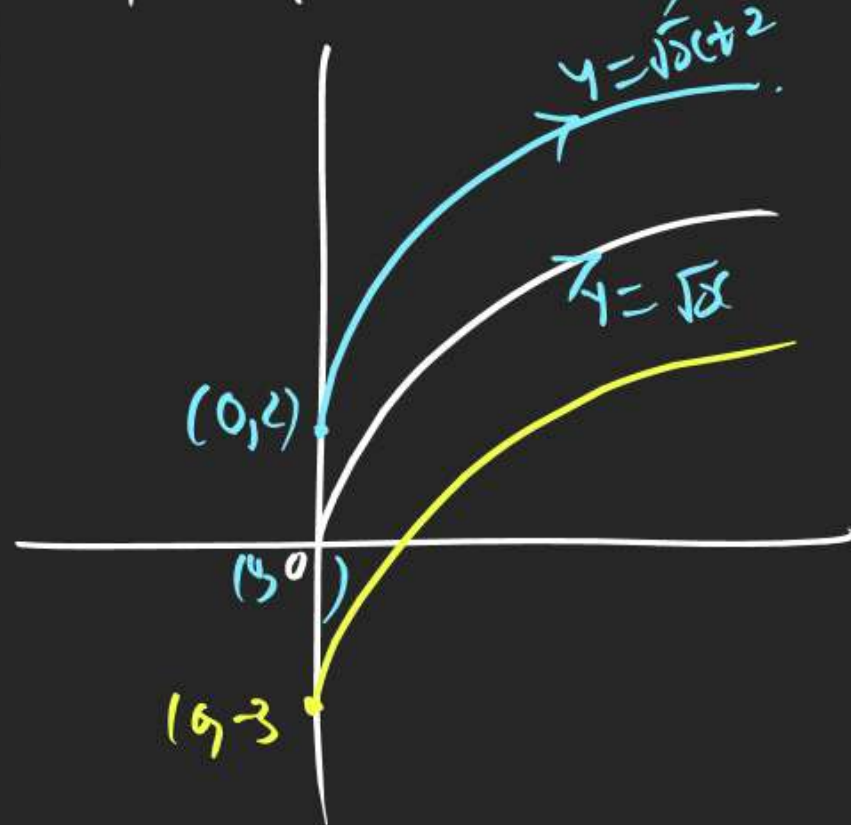
(9) $y = \frac{1}{|x|}$



$$Q \ y = |x|^{1/3}$$

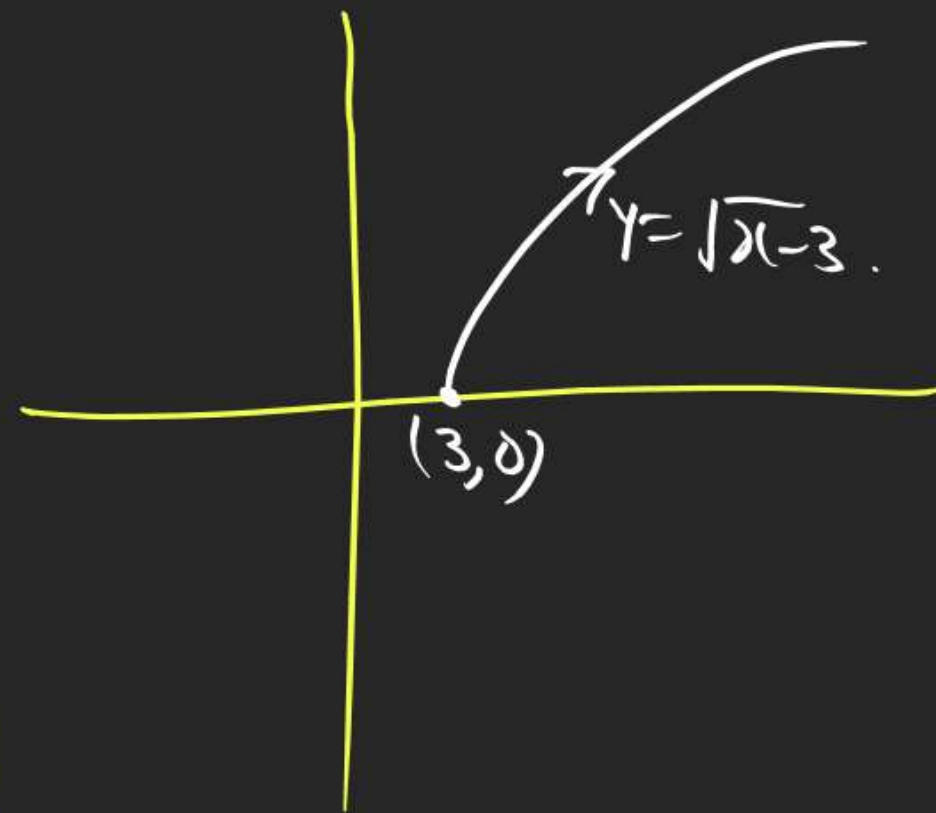


$$y = \sqrt{x} + 2 \quad / \quad y = \sqrt{x} - 3$$



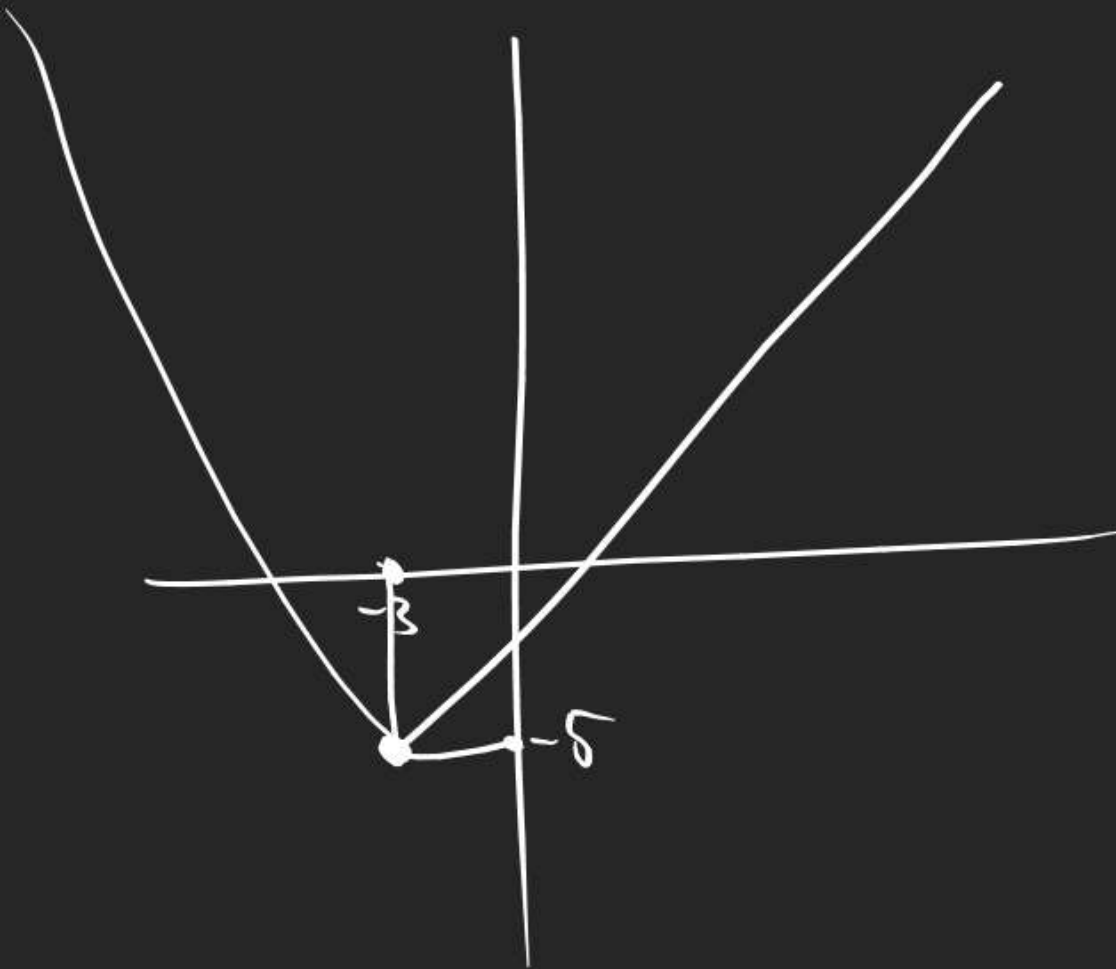
$$y = \sqrt{x-3} \quad f(x+k)$$

$$x = 3 \quad y = \sqrt{x}$$



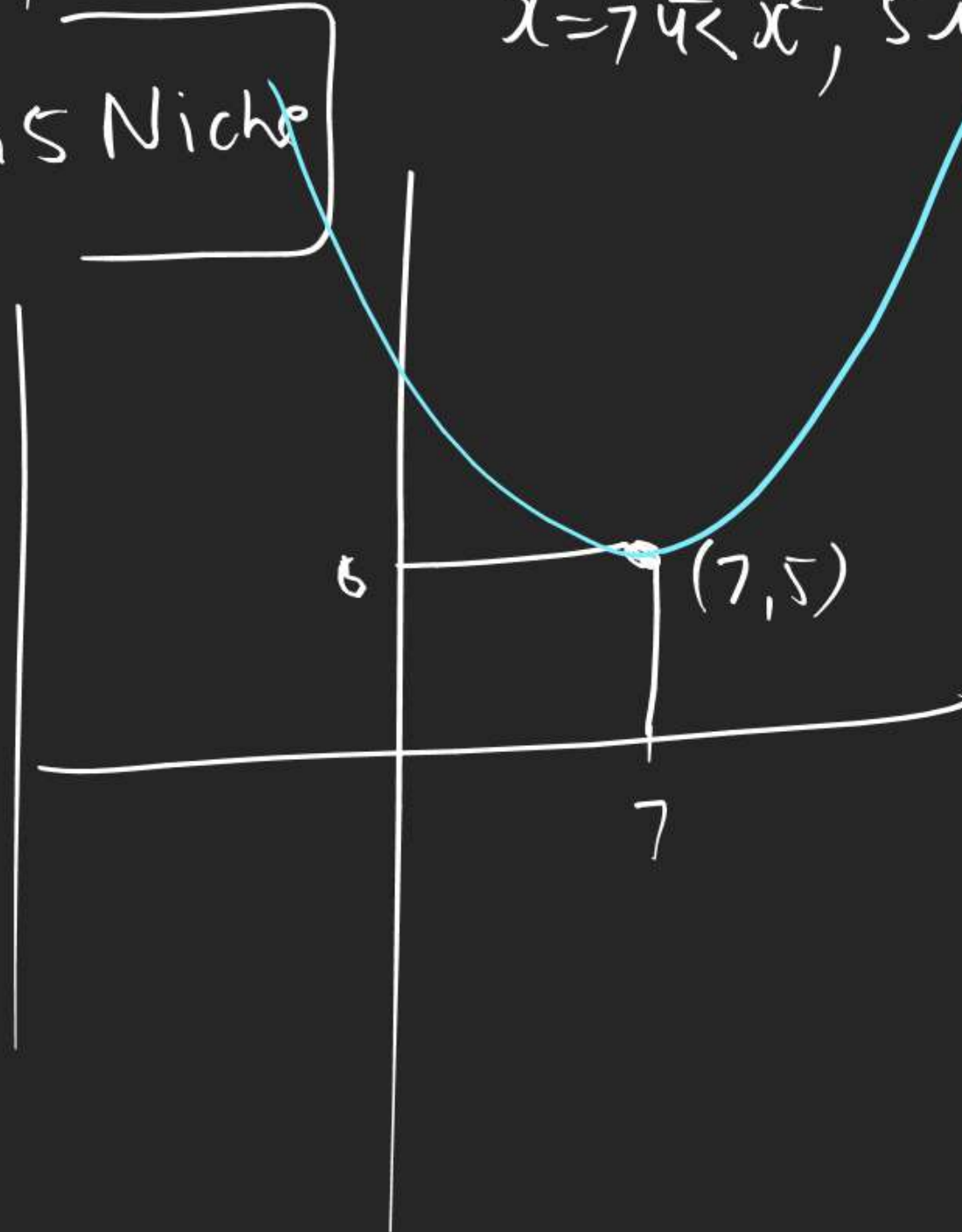
$$y = |x+3| - 5$$

$x = -3$ is a local minimum

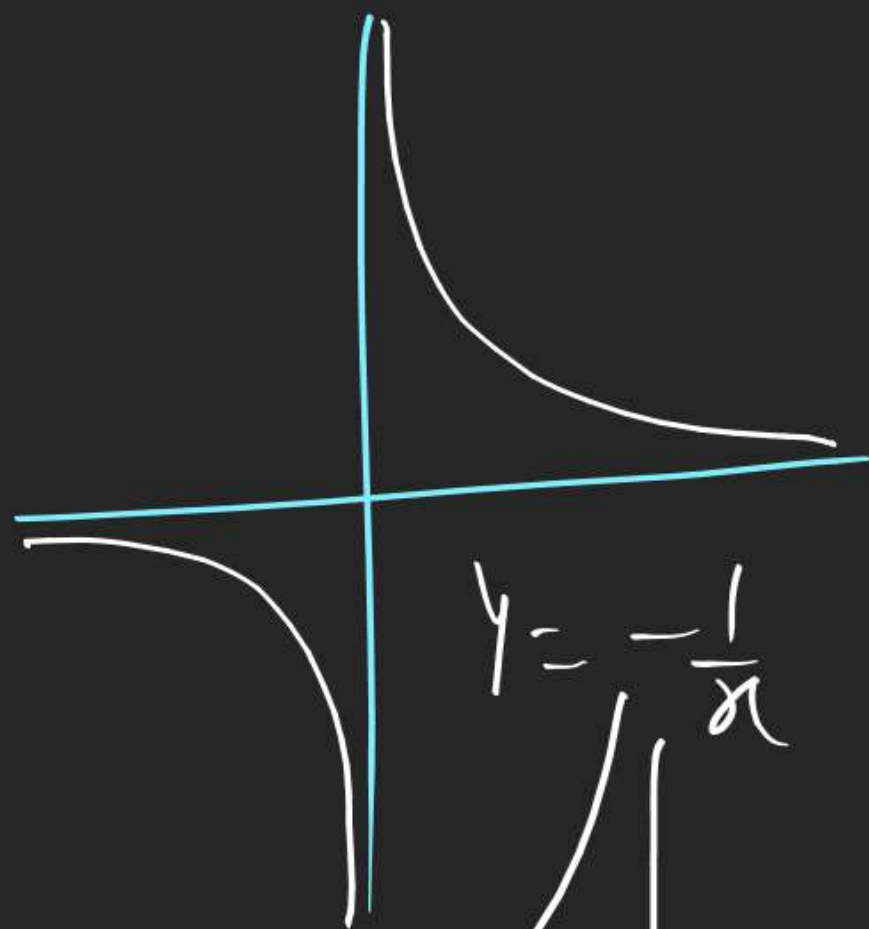


$$\textcircled{Q} y = (x-7)^2 + 5$$

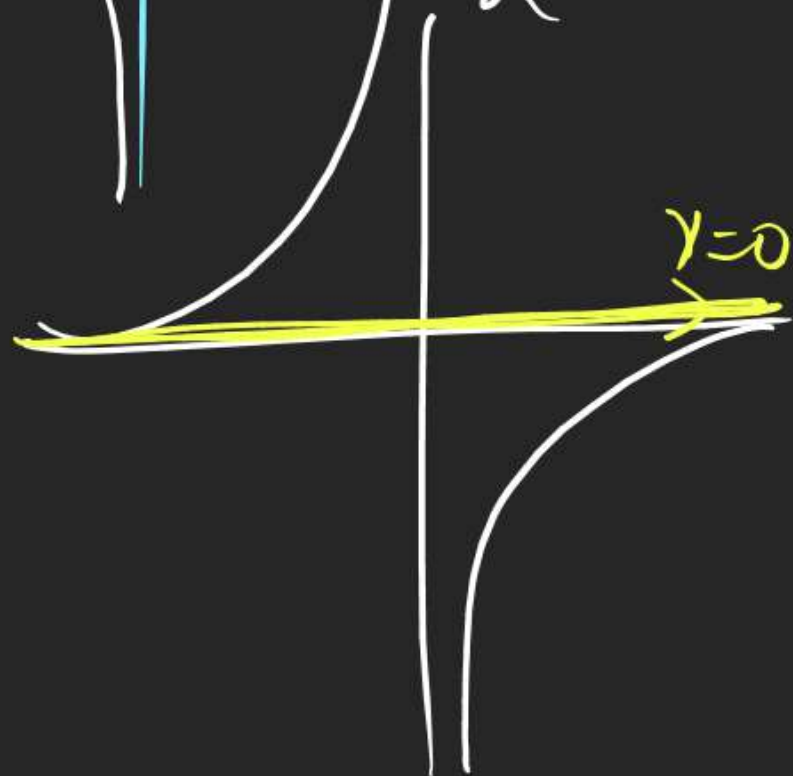
$x = 7$ is a local minimum



$$y = \frac{1}{x}$$

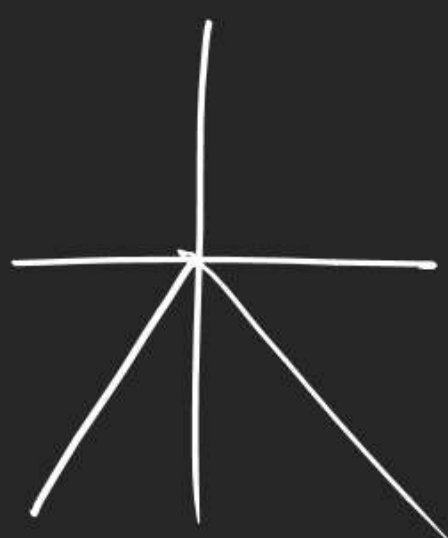


$$y = -\frac{1}{x}$$

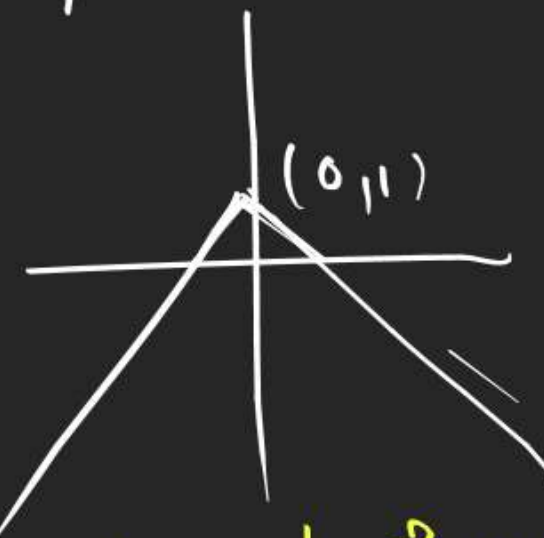


$$y = 1 - |x| = -|x| + 1$$

① $y = -|x|$ then ② \perp up.



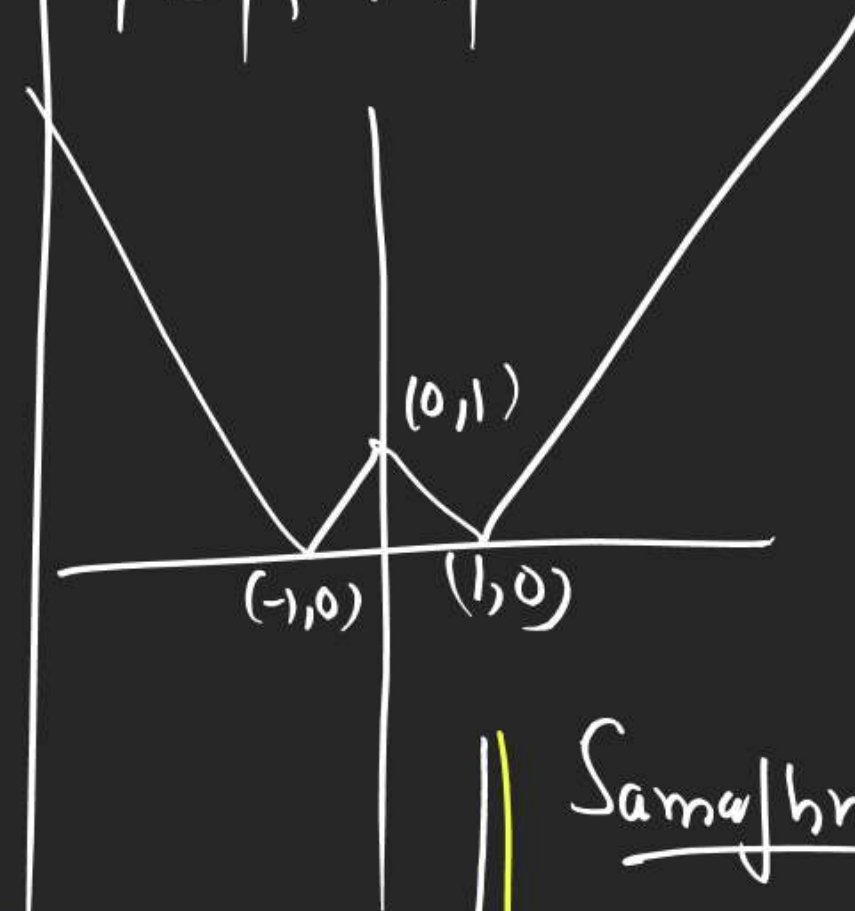
$$y = -|x| + 1$$



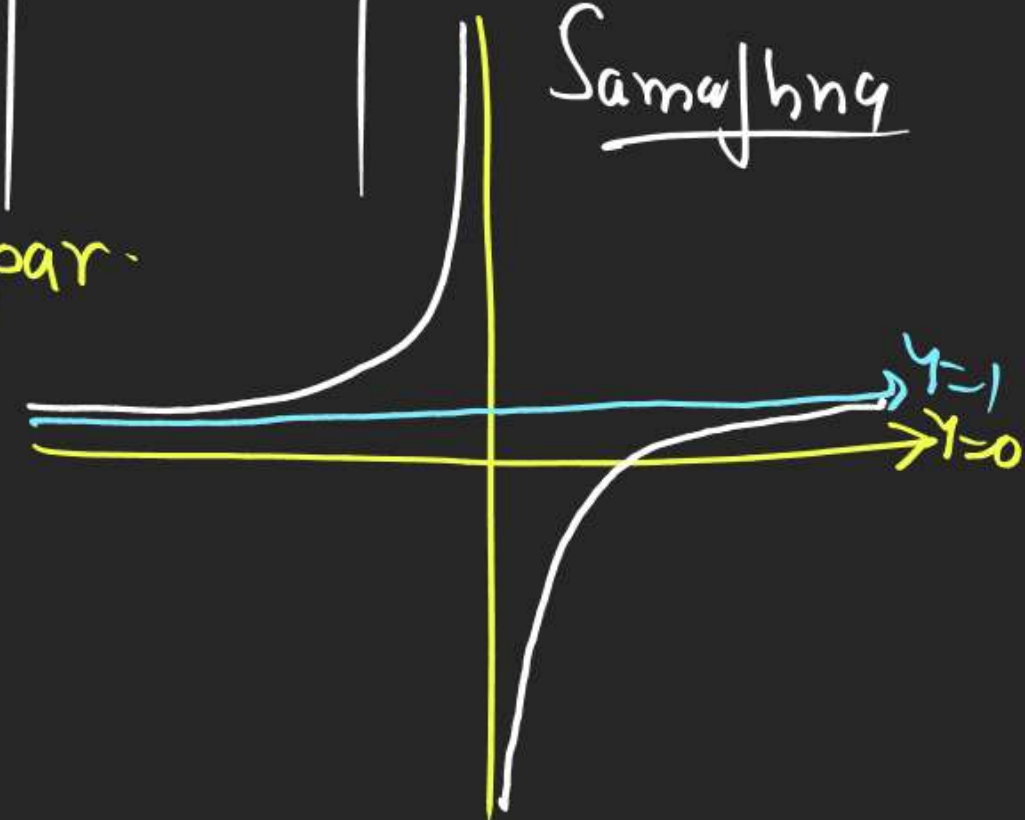
$$y = \left(1 - \frac{1}{x}\right) - \frac{1}{x} \text{ } \frac{2}{x} \text{ } \perp \text{ up.}$$

$$y = \frac{1(-1)}{(x)}$$

$$y = |1 - |x||$$



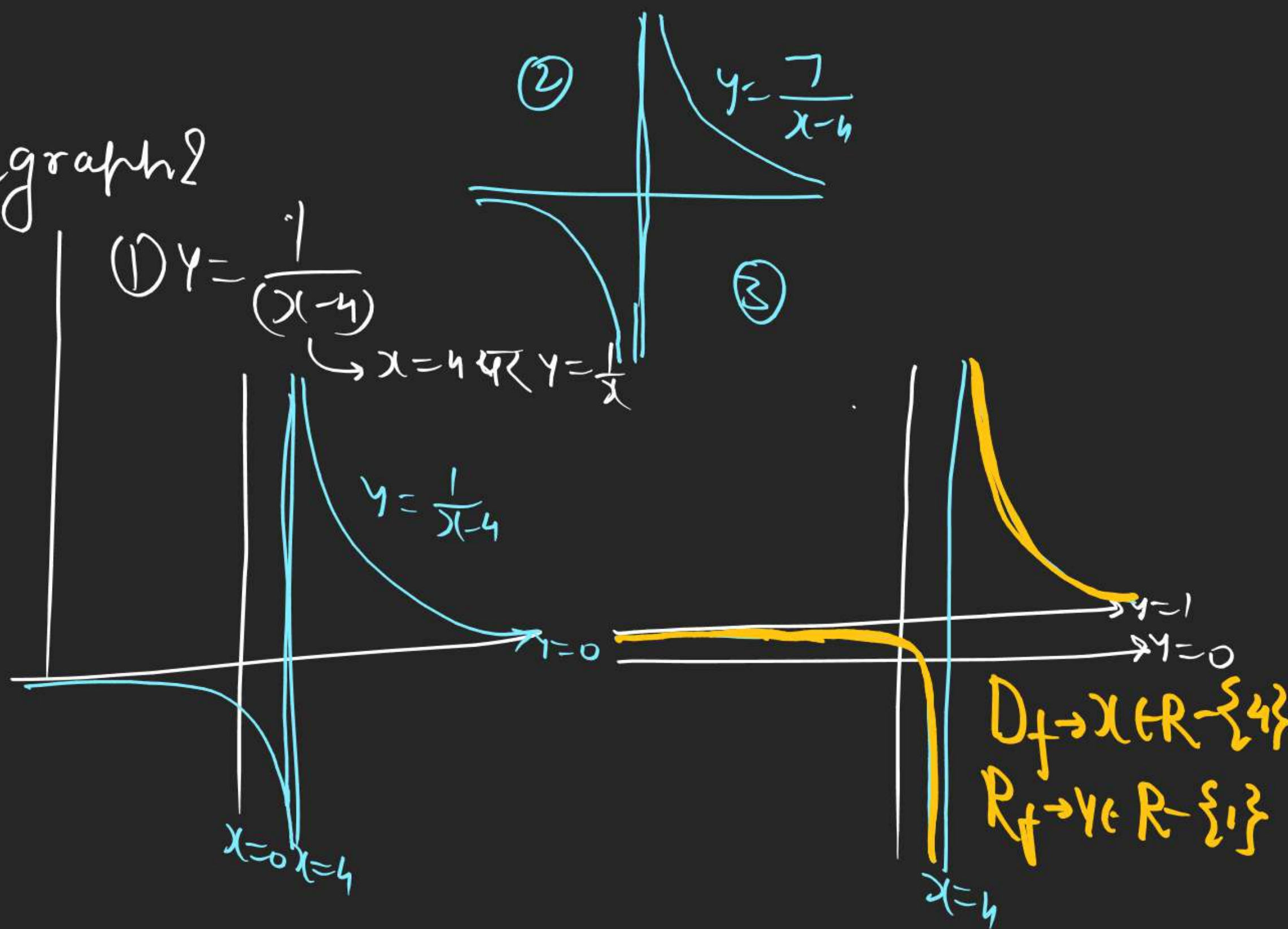
Samajhna



$$\textcircled{Q} \quad y = \frac{x+3}{x-4} \quad \text{Kagrapth 2}$$

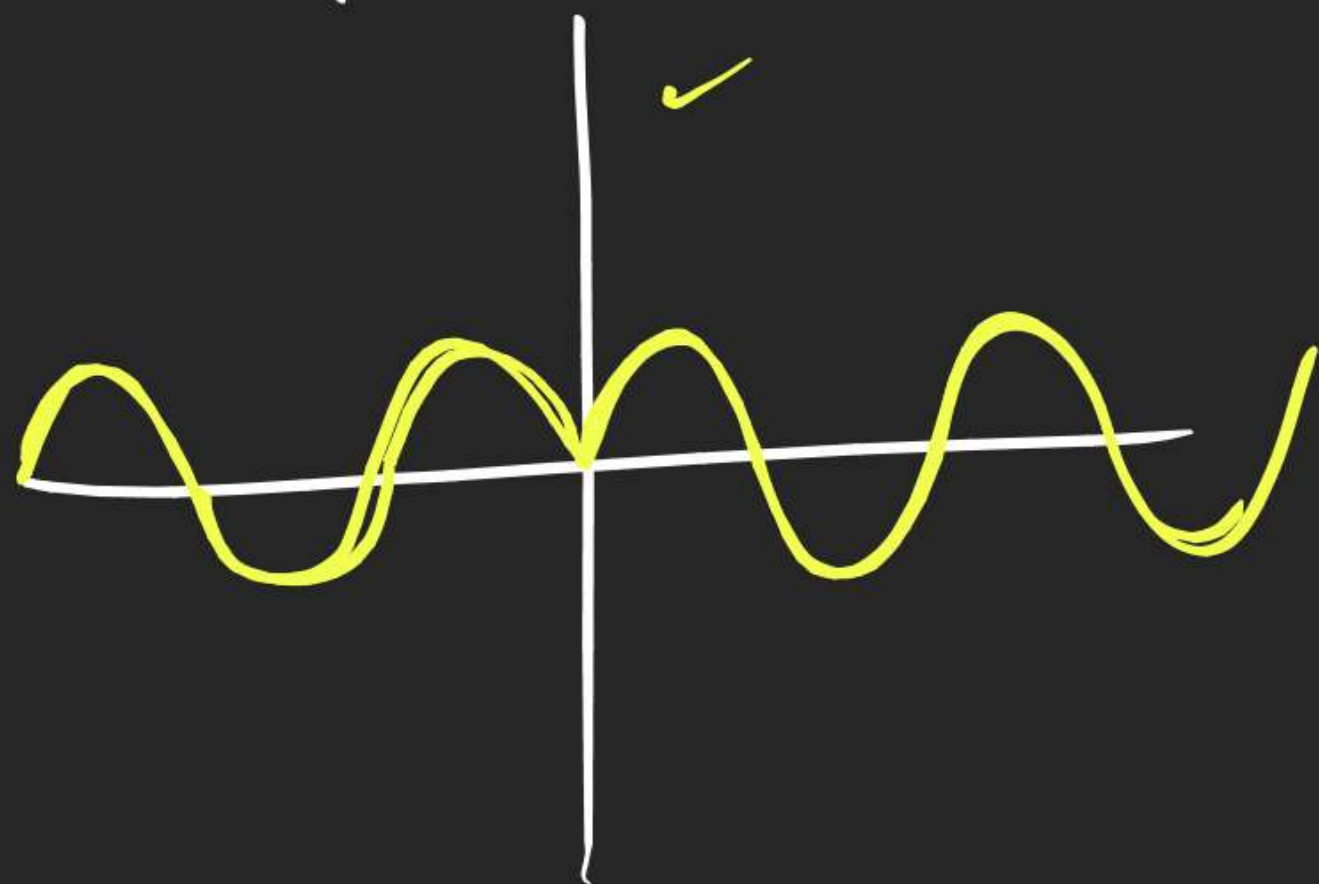
$$= \frac{(x-4)+7}{(x-4)}$$

$$= \textcircled{1} + \frac{7}{(x-4)}$$



$$8) y = f(|x|) = \begin{cases} f(x) \\ f(-x) \end{cases}$$

$$y = \sin|x|$$



$$x \geq 0$$

$$x < 0$$

$$x < 0$$

$$x \geq 0$$

RHS Pr fxn as it is Banega.

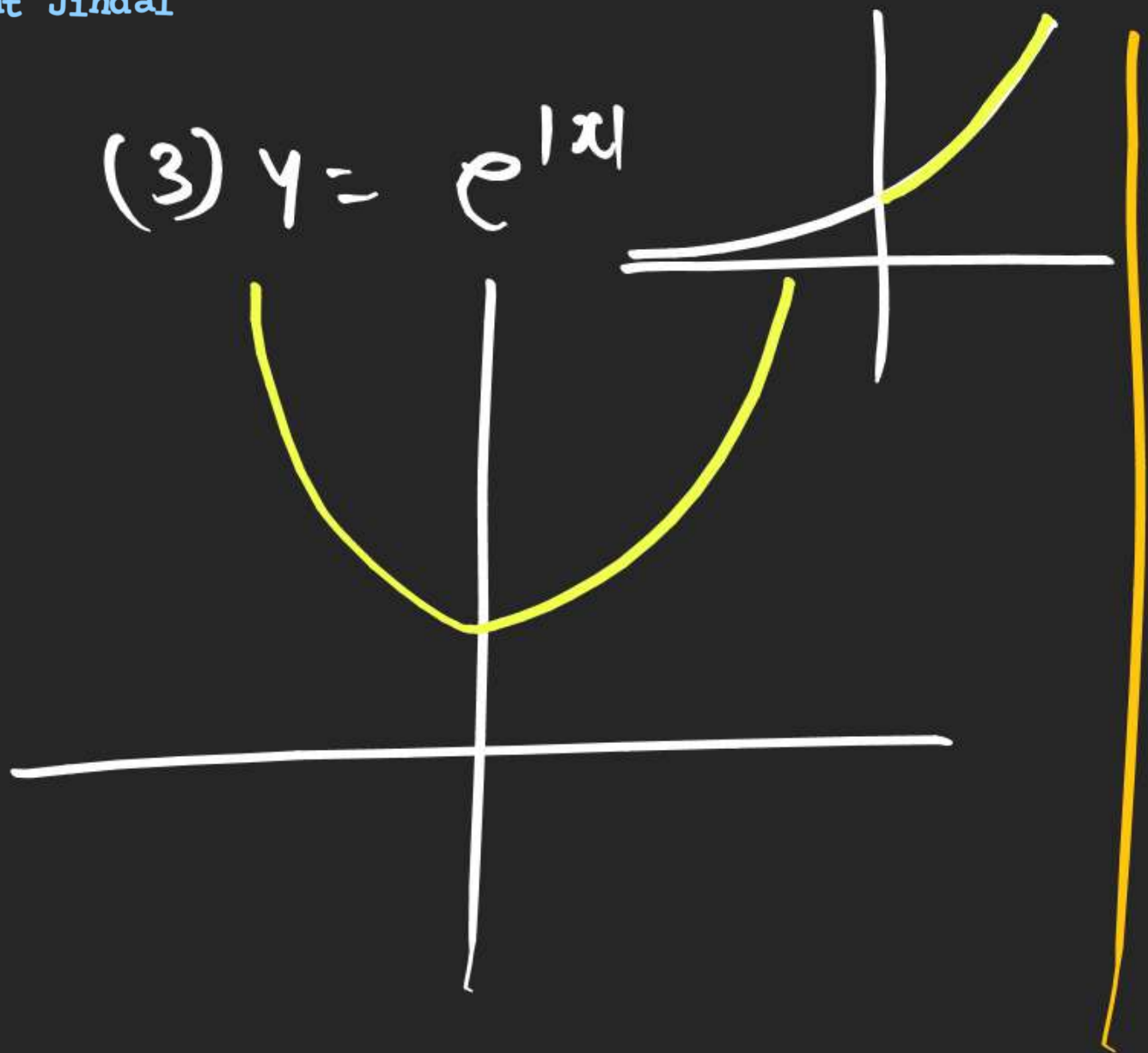
Left side

fxn Ki Image
Banegi

$$y = \cos|x| = \cos x$$



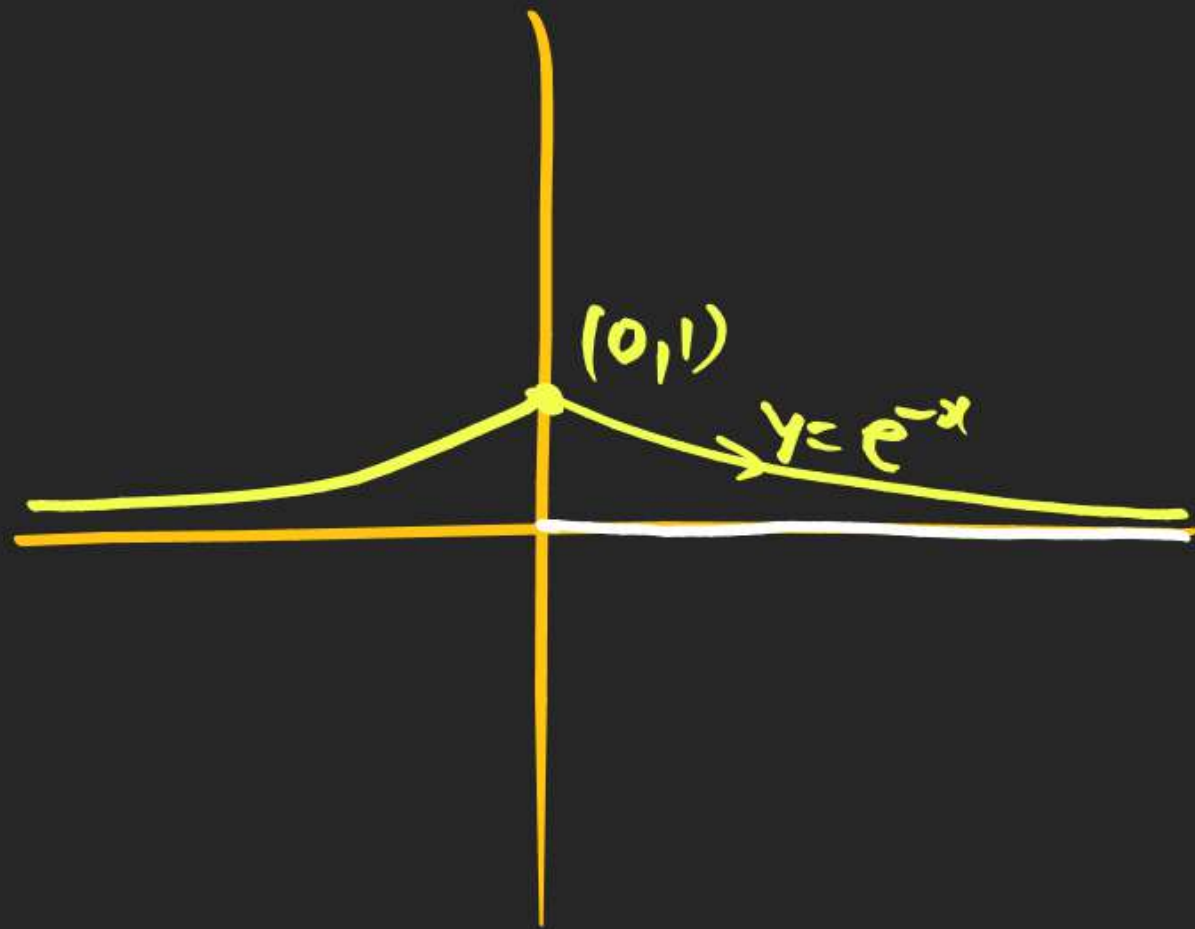
(3) $y = e^{|x|}$



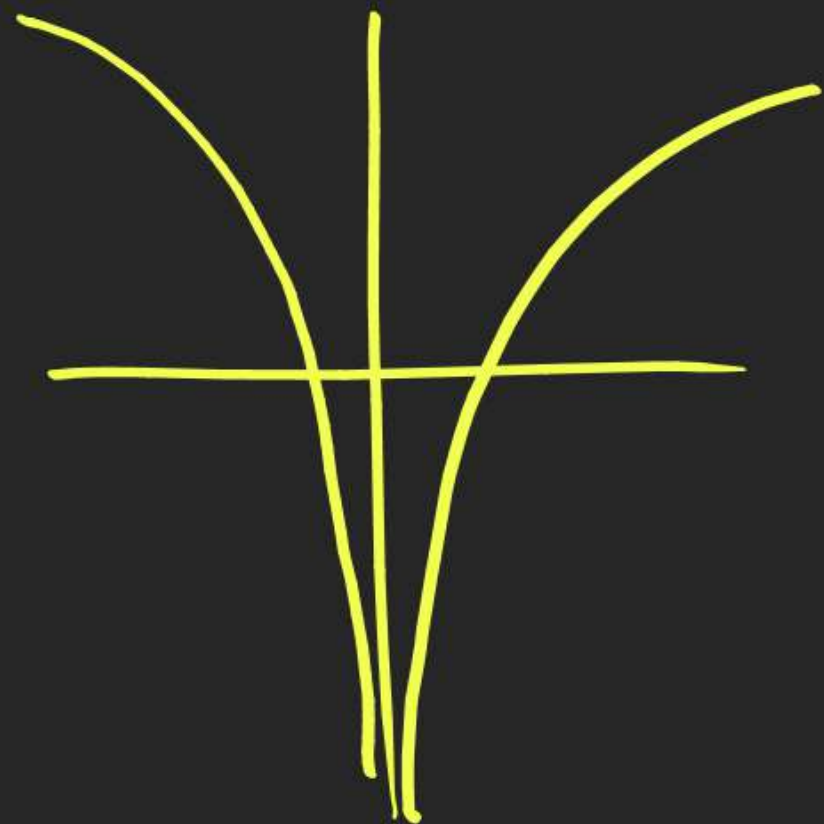
$$y = e^{-|x|} = \begin{cases} e^{-x} & x \geq 0 \\ e^{+(-x)} & x < 0 \end{cases}$$

$x \geq 0$

$x < 0$

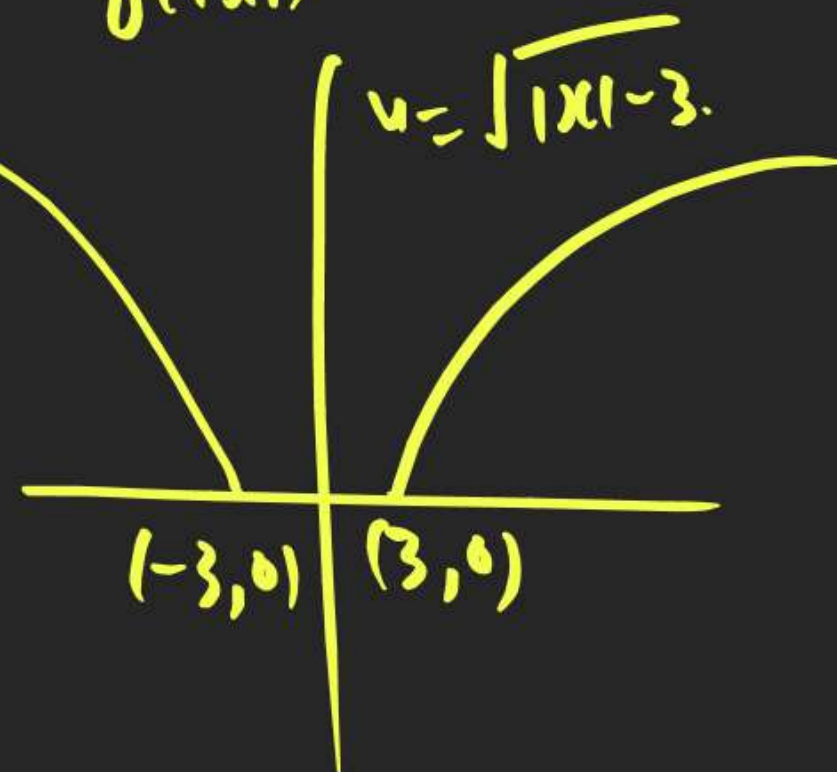
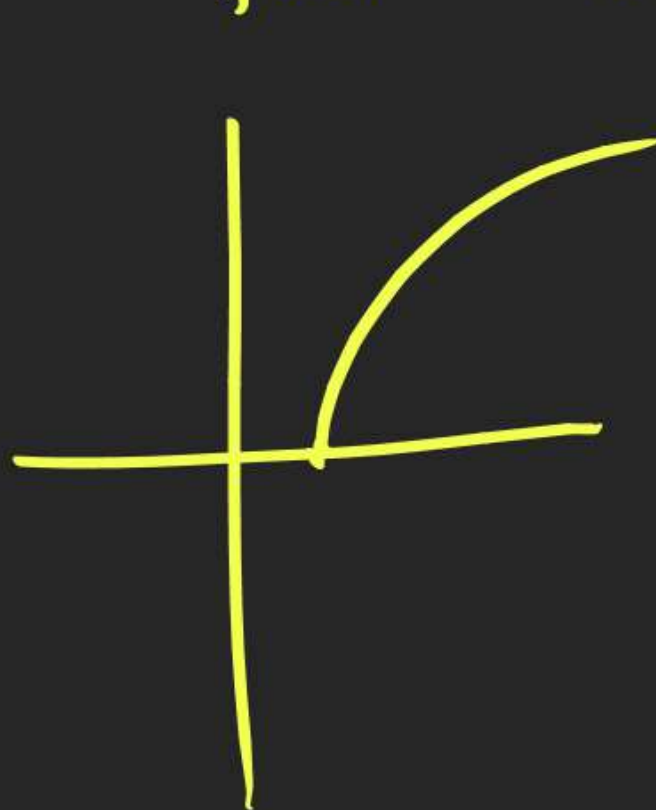


$$Q \ y = \ln|x|$$



$$y = \sqrt{|x|-3}$$

$$\textcircled{1} \ y = \sqrt{x-3} \xrightarrow{f(x) \rightarrow x=3} \textcircled{2} \ y = \sqrt{|x|-3}$$



$$y = x^2 - 2x + 3 \rightarrow \frac{dy}{dx} = 2x - 2 = 0$$

$$x = 1$$

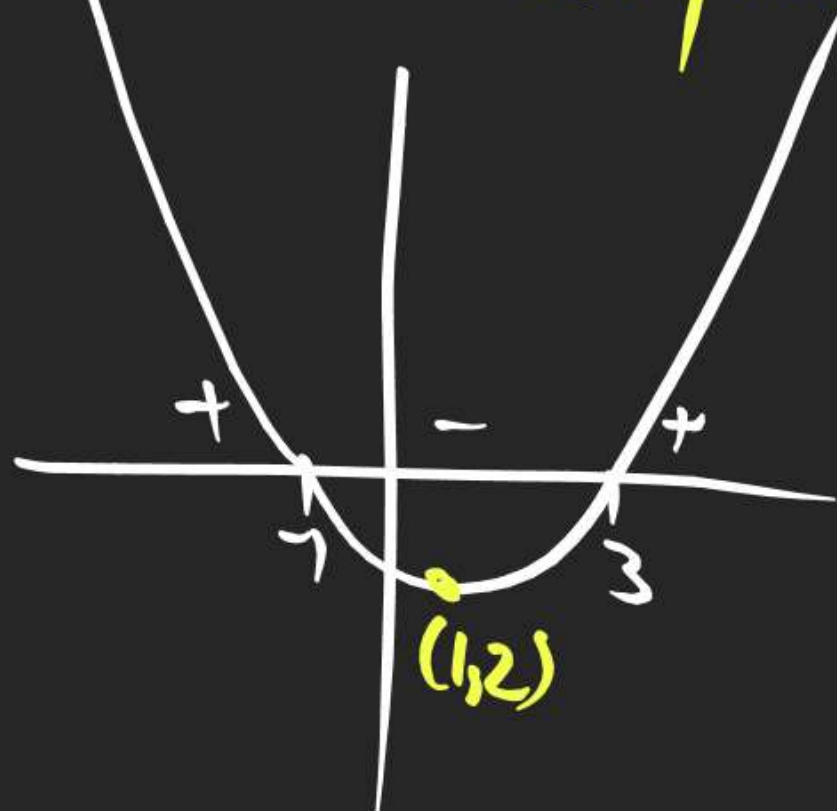
$$y = 1^2 - 2 \cdot 1 + 3 = 2$$

$$\textcircled{1} y = x^2 - 2x + 3 \quad \textcircled{2} y = x^2 - 2|x| + 3$$

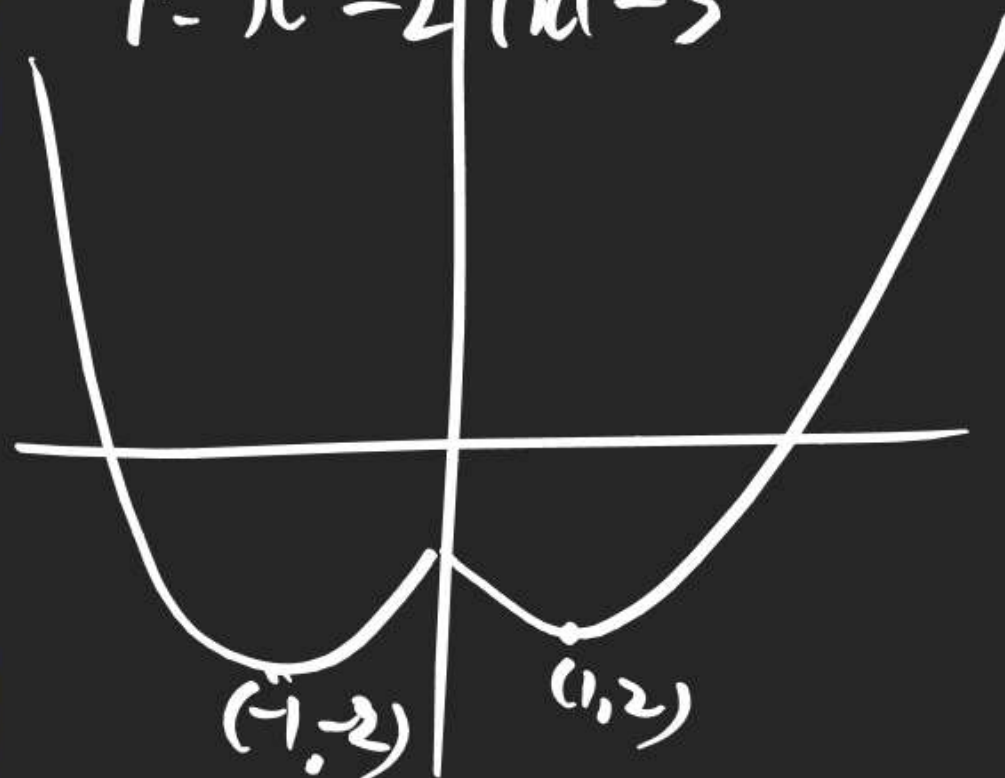
$$= (x-3)(x+1)$$

key curve

4 Lec



$$y = x^2 - 2|x| + 3$$

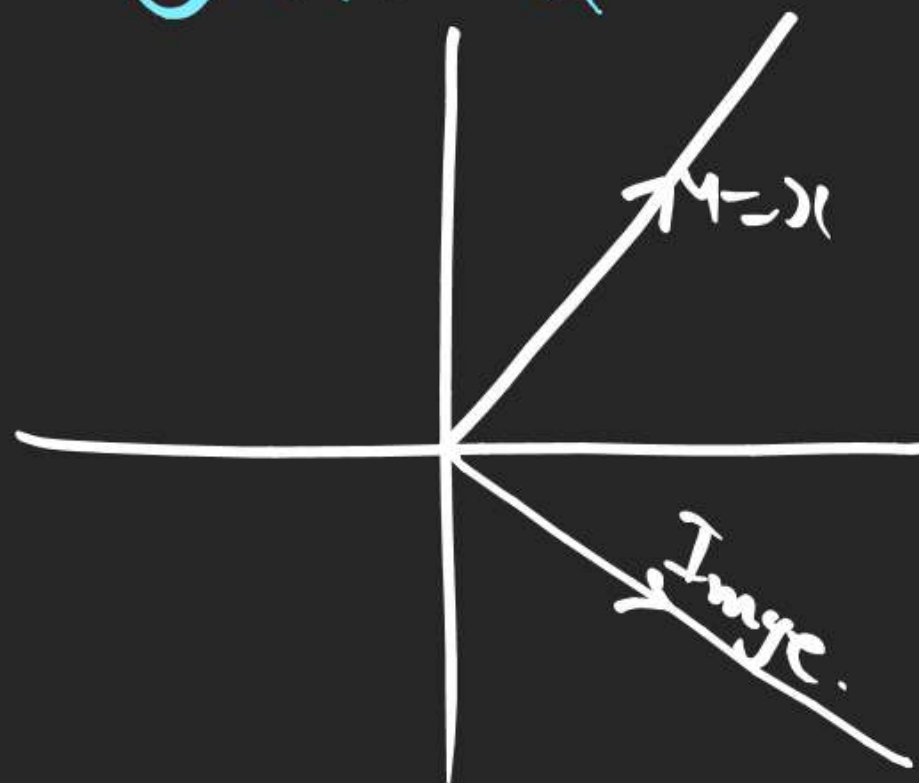


$$|y| = f(x)$$

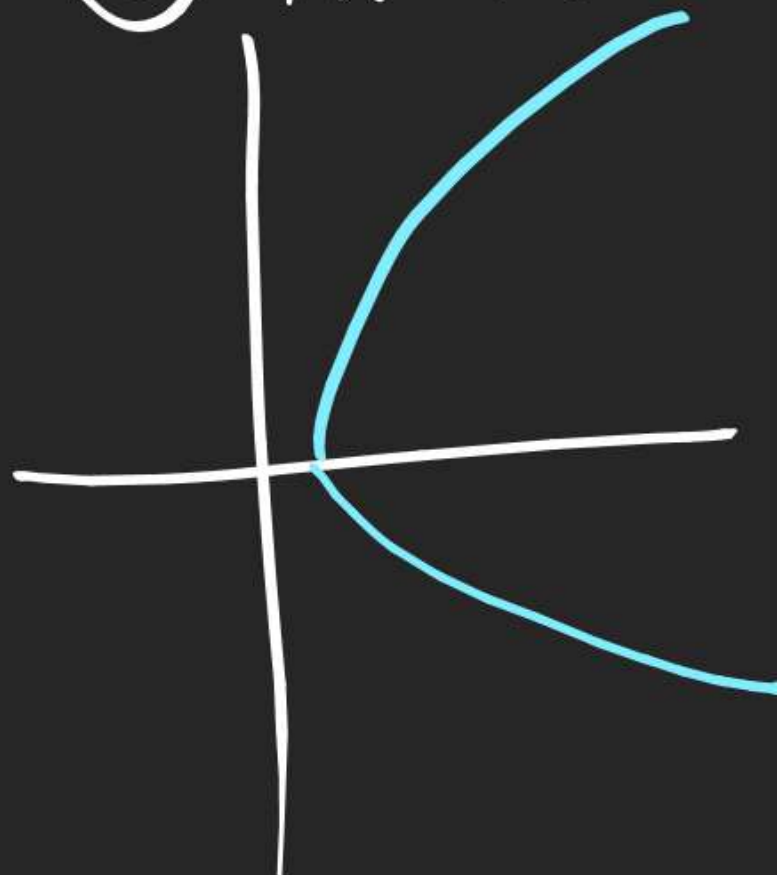
① Make graph Above X Axis only.

② Make Image of made graph in X Axis

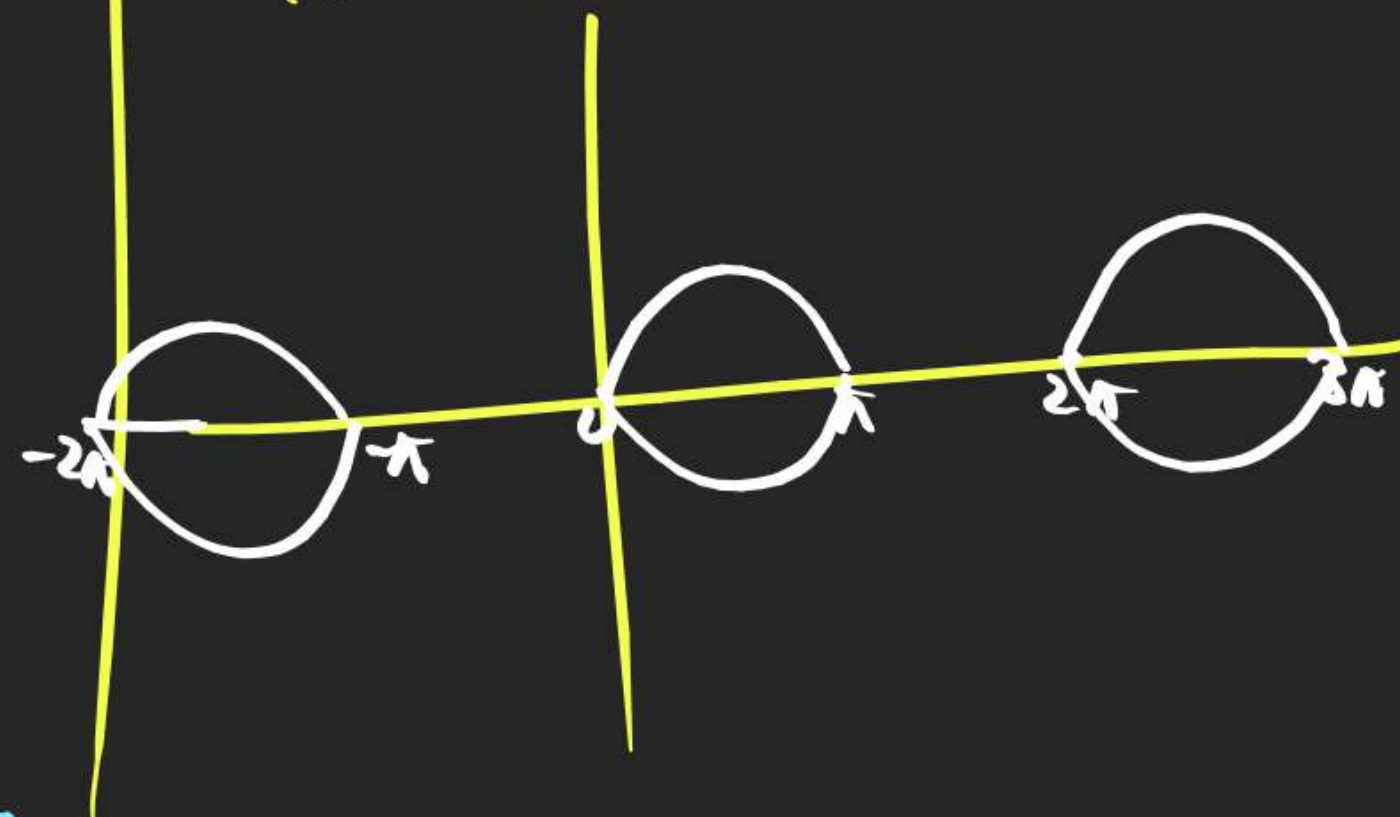
① $|y| = x$



② $|y| = \ln x$



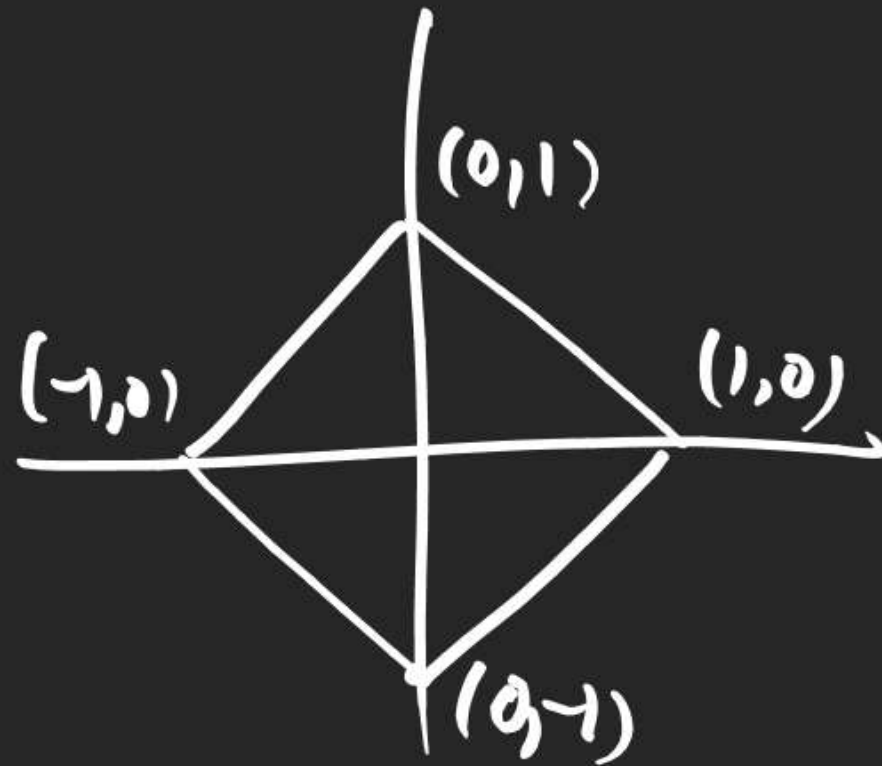
③ $|y| = \sin x$



$$y = 1 - |x|$$



$$|y| = 1 - |x|$$



Q

$$|x| + |y| = 1$$

$$|y| = 1 - |x|$$

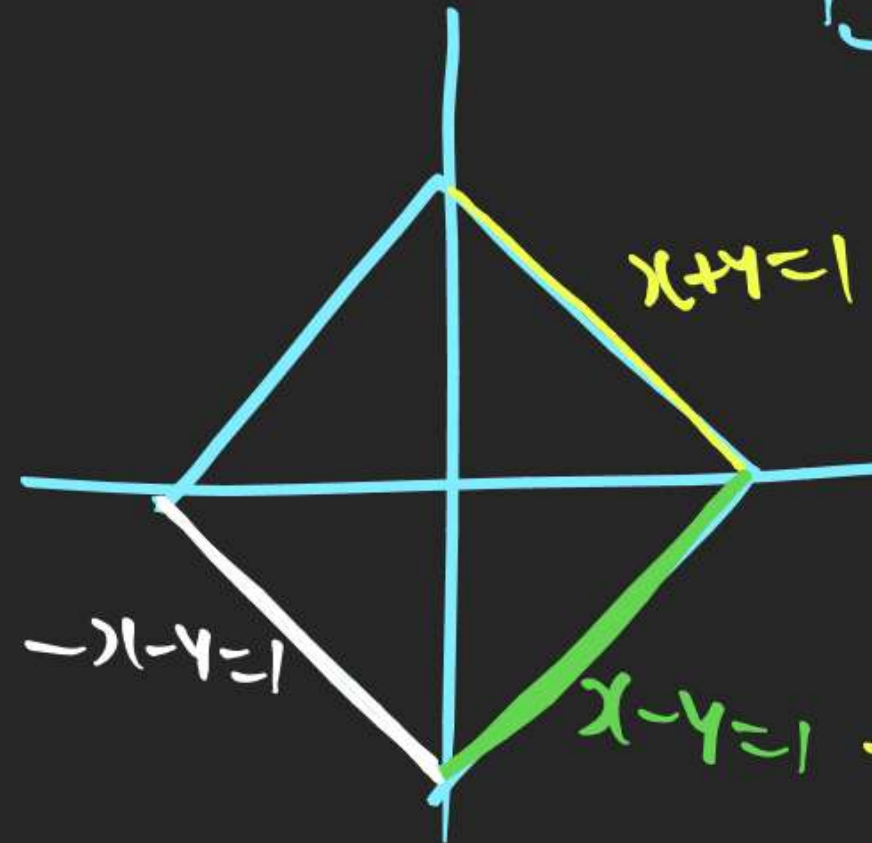
$$\rightarrow x + y = 1 \quad (+ +)$$

$$\rightarrow x - y = 1 \quad (+ -)$$

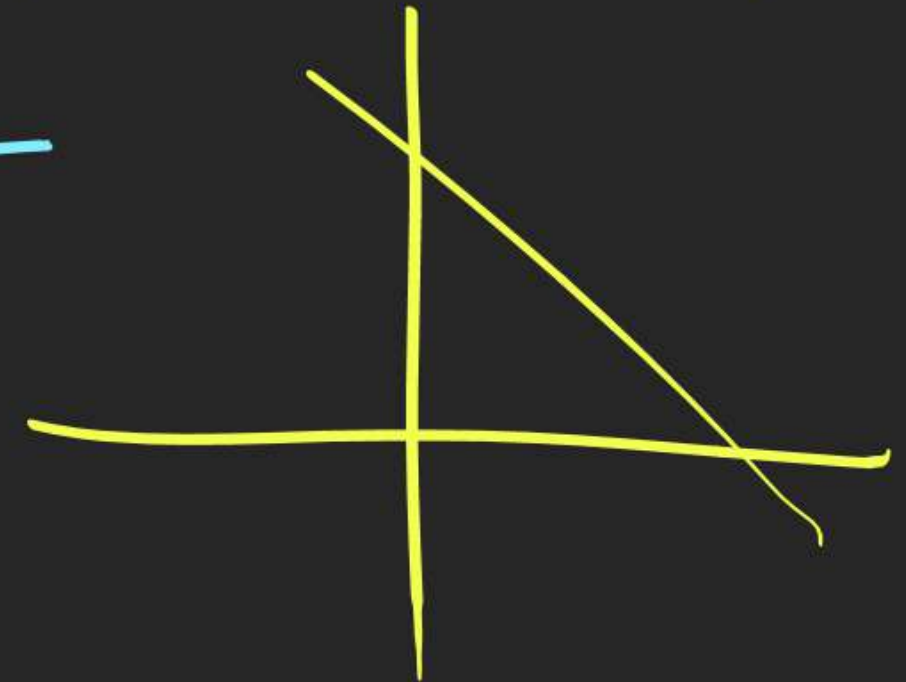
$$\rightarrow -x + y = 1 \quad (- +)$$

$$\rightarrow -x - y = 1 \quad (- -)$$

$$\rightarrow (-, -) \quad (3)$$

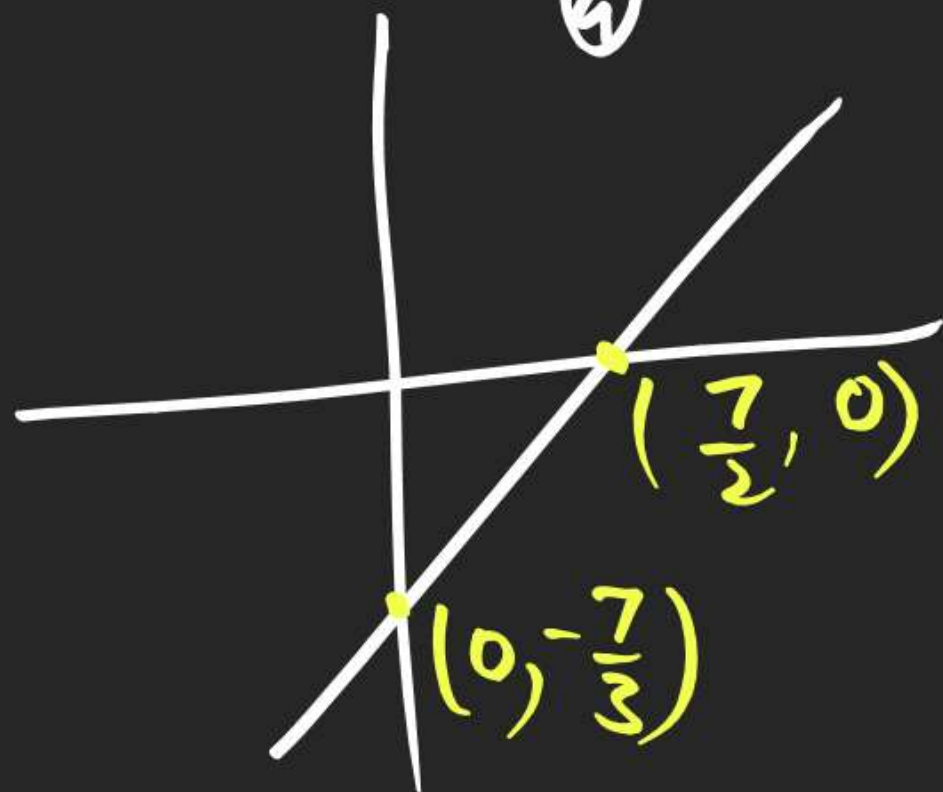


$$2x + 3y = 1$$

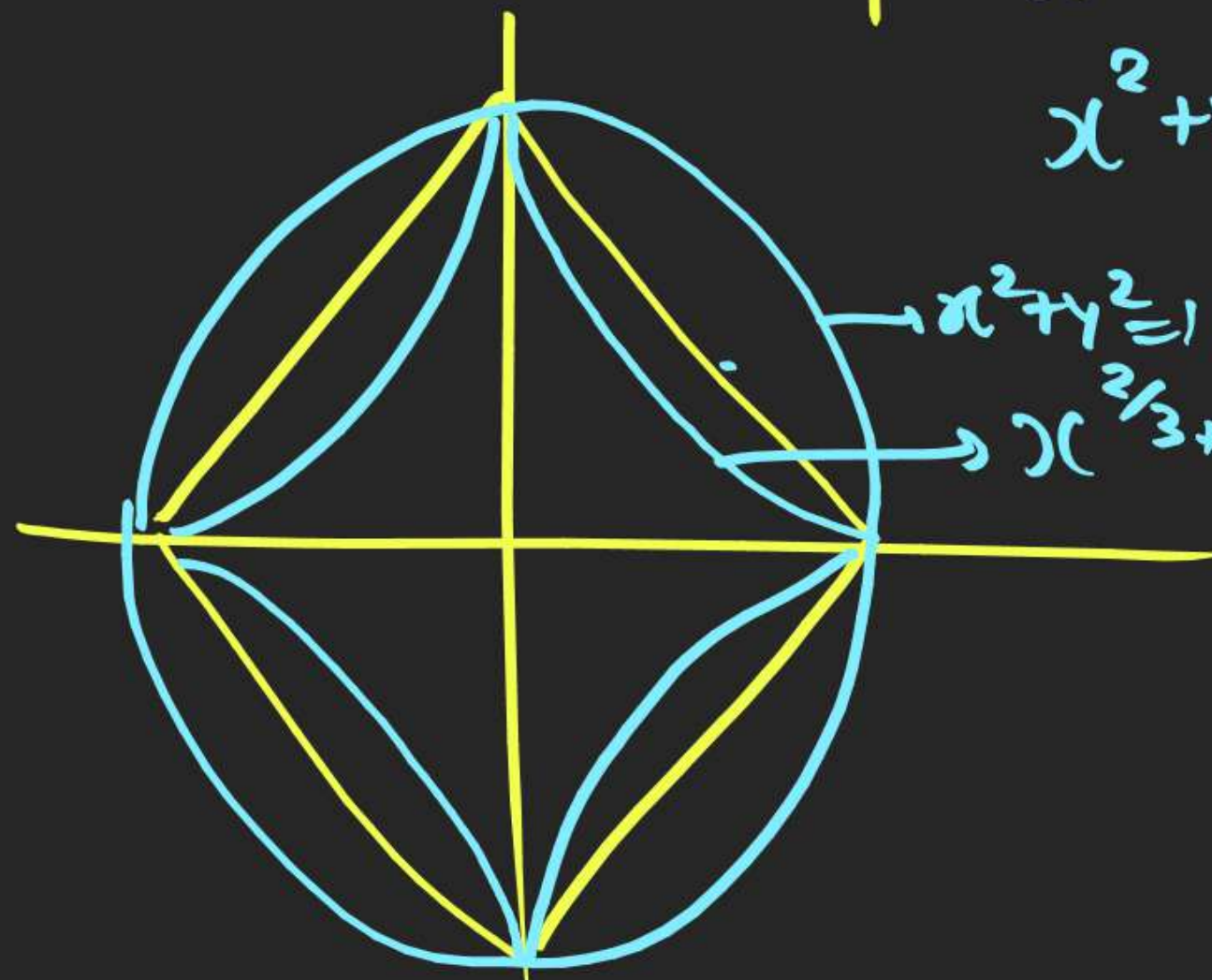


$$2x - 3y = 7$$

\oplus \ominus \ominus



$$|x| + |y| = 1$$



$\rightarrow x' + y' = 1$ deg 1 \rightarrow Km

$$x^{2/3} + y^{2/3} = 1$$

$$x^2 + y^2 = 1$$

$$x^2 + y^2 = 1$$

$$x^{2/3} + y^{2/3} = 1$$

Domain

Concept

$$y = f(g(x))$$

If Dom of $f = \mathbb{R}$ then

$$\text{Dom of } f(g(x)) = \text{Dom of } g(x)$$

$$Q \quad y = \sin(\ln(x-3)) \text{ find } D_f$$

$$D_f = \mathbb{R}$$

$$\text{Dom of } \sin(\ln(x-3))$$

$$= \text{Dom of } \ln(x-3)$$

$$x-3 > 0$$

$$x > 3$$

$$x \in (3, \infty)$$

$$(1) y = |x| \quad \text{Dom} = \mathbb{R}$$


$$(2) y = (x)^2 \quad \text{Dom} = \mathbb{R}$$


$$(3) y = x^2 - 2x + 3 \quad \text{Dom} = \mathbb{R}$$

Poly

$$(4) y = [x] \rightarrow x \in \mathbb{R}$$

$$(5) y = \{x\} \rightarrow x \in \mathbb{R}$$

$$(6) y = e^x \rightarrow \text{Graph} \rightarrow \mathbb{R}$$


$$(7) y = \ln x \rightarrow x > 0 \rightarrow x \in (0, \infty)$$

$$(8) y = \sin x \rightarrow x \in \mathbb{R}$$

$$(1) y = \left[\sin \ln(x-3) \right] \quad \text{Dom} = ?$$

$\mathbb{R} \quad \mathbb{R} \quad \mathbb{R}$

$$x-3 > 0$$

$$x > 3 \Rightarrow x \in (3, \infty)$$

\neq

$$(2) y = e^{\left[\sin \ln(x-3) \right]} \quad \text{Dom} = ?$$

$\mathbb{R} \quad \mathbb{R} \quad \mathbb{R} \quad \mathbb{R}$

$$x-3 > 0$$

$$x > 3$$

$$x \in (3, \infty)$$

Q $f(x) = [x] \cdot \sin\left(\frac{1}{[x+3]}\right)$ find D_f?

See

$x \in \mathbb{R}$

$[x+3] \neq 0$

$[x] + 3 \neq 0$

$[x] \neq -3$

$x \notin [-3, -2)$

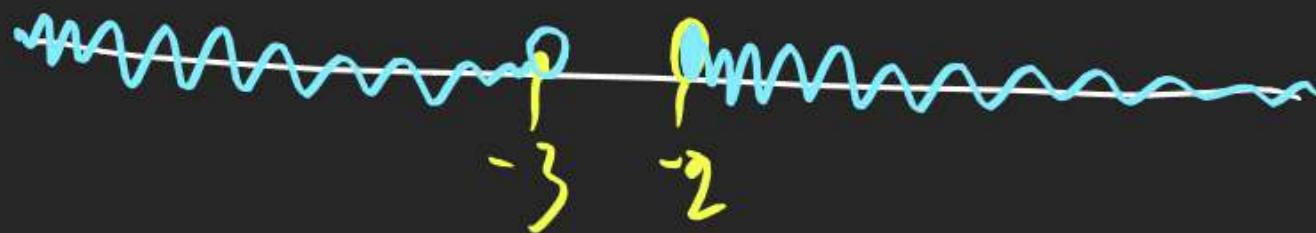
$x \in (-\infty, -3) \cup [-2, \infty)$

$[x] = -3$



$x \in [-3, -2)$

Memo



Q $y = \log_{2\{x\}-3} (x^2 - 5x + 13) + \frac{1}{\sqrt{\sin x}}$

$2\{x\} - 3 > 0$

$\{x\} > \frac{3}{2}$

$\{x\} \in [0, 1)$

Not Possible

$x \in \emptyset$



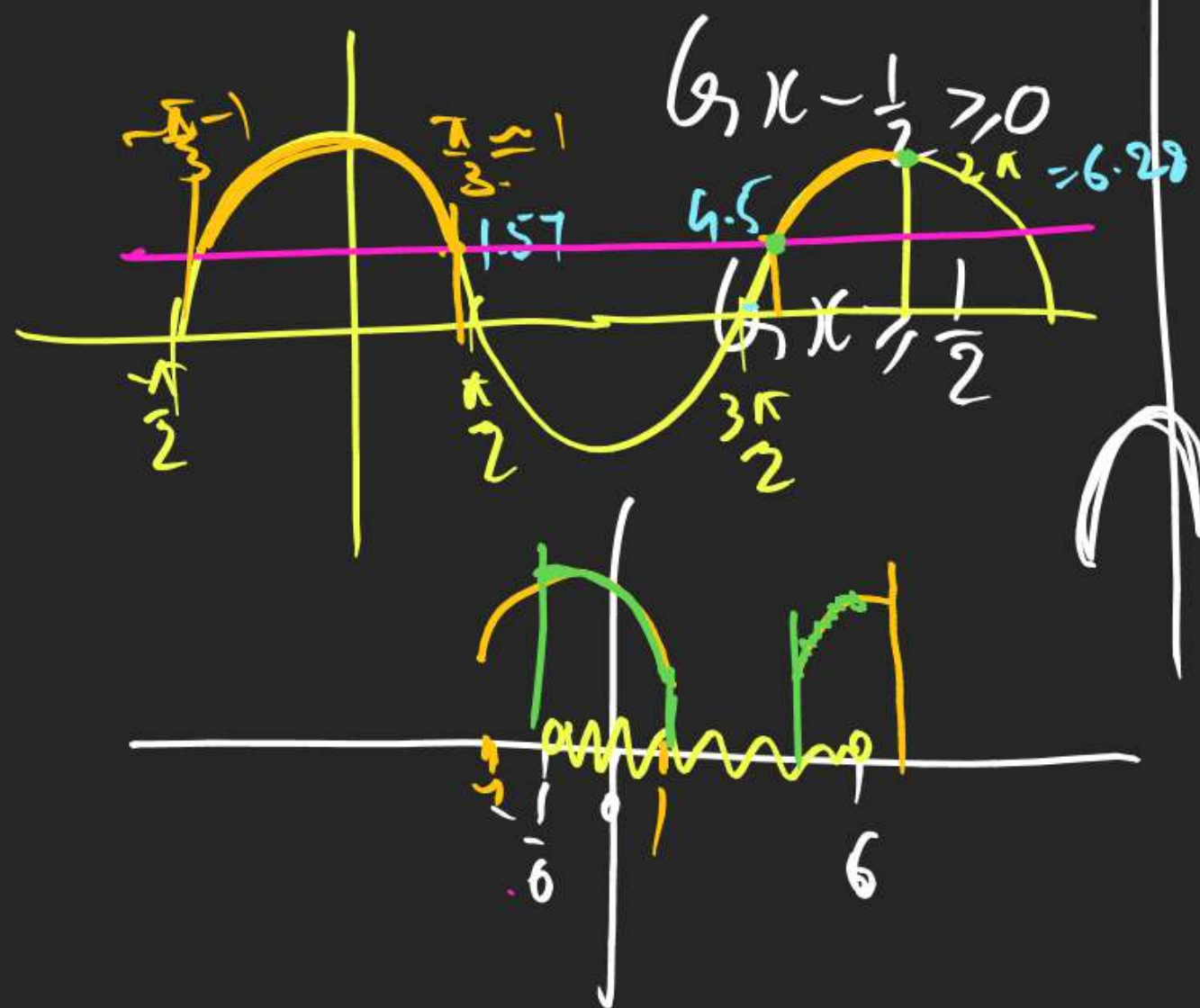
Dom.

$$\frac{\pi}{3} = \frac{3.14}{3} = 1.047$$

$$y = \frac{\sqrt{6x - \frac{1}{2}}}{\sqrt{6 + 35x - 6x^2}} = \sqrt{6x - \frac{1}{2}} \times \frac{1}{\sqrt{6 + 35x - 6x^2}}$$

$$300 = 5\pi \frac{\pi}{3}$$

$$x \in \left(-\frac{1}{6}, \frac{\pi}{3}\right] \cup \left[\frac{5\pi}{3}, 6\right)$$



$$6 + 35x - 6x^2 > 0$$

$$6x^2 - 35x - 6 < 0$$

$$6x^2 - 36x + x - 6 < 0$$

$$(6x + 1)(x - 6) < 0$$

$$-\frac{1}{6} < x < 6$$

$$\textcircled{1} \quad y = \frac{\sqrt{8mx - \frac{1}{2}}}{\sqrt{6 + 35x - 6x^2}} = \sqrt{8mx - \frac{1}{2}} \times \frac{1}{\sqrt{6 + 35x - 6x^2}}$$

$$= \quad 8mx \geq \frac{1}{2}$$

$$6 + 35x - 6x^2 > 0$$

$$(6x+1)(x-6) < 0$$

$$-\frac{1}{6} < x < 6$$

$$x \in \left[\frac{1}{6}, \frac{5\pi}{6} \right]$$

