

$$Q \sin(-65^\circ) = -\sin 65^\circ$$

$$Q \cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$$

$$\begin{aligned} & \cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 63^\circ} \cdot \frac{\tan 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ \\ & \underline{\sin(90-63^\circ)} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\cos 63^\circ} \\ & + \underline{\cos 63^\circ} \times \frac{1}{\cos 63^\circ} = 1 \end{aligned}$$

$$\frac{6x0}{(+6x0)} + \frac{+8x0}{(+8x0)} T \frac{(+6x0)}{6x0}$$

$$1 + 1 + 1 = 3$$

$$Q \begin{cases} 3 \\ 3 \end{cases} \frac{60}{\sin(90+\theta)} + \frac{\sin(-\theta)}{\sin(180+\theta)} - \frac{\tan(90+\theta)}{\cot\theta} = 3$$

$$Q \frac{\sin 135^\circ - \sin 120^\circ}{\sin 135^\circ + \sin 120^\circ} = 3 + 2\sqrt{2}$$

$$\sin(90^\circ + 45^\circ) = +\cos 45^\circ$$

2 ②

$$Q \sin(-65^\circ) = -\sin 65^\circ$$

$$Q \cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$$

$$\cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 27^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$$



$$\frac{\sin(90^\circ - 63^\circ)}{\cos 63^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\sec 63^\circ}$$

$$+\cos 63^\circ \times \frac{1}{\sec 63^\circ} = 1$$

$$\frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ}$$

$$\frac{1}{\sqrt{2}} + \left(+\frac{1}{2}\right)$$

$$= \frac{\frac{1}{\sqrt{2}} + \left(-\frac{1}{2}\right)}{\frac{1}{\sqrt{2}}} = \frac{\frac{\sqrt{2}+1}{2\sqrt{2}}}{\frac{\sqrt{2}-1}{2\sqrt{2}}} = \frac{\sqrt{2}+1}{2\sqrt{2}}$$

Rat

$$= \frac{\sqrt{2}+1}{\sqrt{2}-1} \times \frac{\sqrt{2}+1}{\sqrt{2}+1}$$

$$= \frac{(\sqrt{2}+1)^2}{(\sqrt{2})^2 - 1^2} = \frac{2+1+2\sqrt{2}}{2-1} = \frac{3+2\sqrt{2}}{1} = 3+2\sqrt{2}$$

$$Q \frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ} = 3+2\sqrt{2}$$

$$\text{Q. } \tan(-65^\circ) = -\tan 65^\circ$$

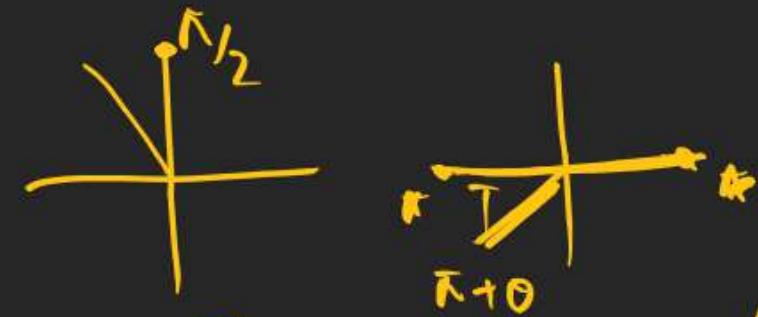
$$\text{Q. } \cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$$

$$\cos 27^\circ \cdot \frac{\tan 27^\circ}{\cos 27^\circ} \cdot \frac{\tan 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$$



$$\tan(90 - 63^\circ) \cdot \frac{\tan 63^\circ}{\cos 63^\circ} \times \frac{1}{\sec 63^\circ}$$

$$+ \cancel{\cos 63^\circ} \times \frac{1}{\cancel{\cos 63^\circ}} = 1$$



$$\text{Q. } \frac{\tan(90 + \theta) \cdot \sec(180 + \theta)}{\cancel{(\cos(180 + \theta))} (\sec(-\theta))} = \cancel{-1}$$

$$\frac{\cancel{\tan(\pi + \theta)} \cancel{\times} (-\sec(\theta)}}{\cancel{(\sec(\pi + \theta))} \cancel{+} \cancel{(-\sec(\theta))}} = -1$$

$$Q \cdot 4 \left(\text{ctg}^2 45^\circ - \sec^2 60^\circ + \sin^2 30^\circ \right) = \frac{1}{4}$$

$$Q \cdot \tan^2 \frac{\pi}{6} + \tan^2 \frac{\pi}{4} + \tan^2 \frac{\pi}{3} = \frac{13}{3}.$$

$$\theta_6 \cdot 4 \times \left(1 \right)^2 - \left(2 \right)^2 + \left(\frac{1}{2} \right)^2$$

$$4 - 4 + \frac{1}{4} = \frac{1}{4}$$

$$\theta_1 \quad \tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ$$

$$\left(\frac{1}{\sqrt{3}} \right)^2 + (1)^2 + (1)^2 = \frac{1}{3} + 1 + 3 = 4 + \frac{1}{3} = \frac{13}{3}$$

$\theta \tan \theta + \tan(\pi - \theta) + \tan(\frac{\pi}{2} + \theta) - \tan(2\pi - \theta)$

 $\tan \theta + (-\tan \theta) + (-\tan \theta) + (\tan \theta) = 0$

Complementary Angles

When Sum of 2 angles = $\frac{\pi}{2}$

$$30^\circ \& 60^\circ$$

$$-30^\circ \& 120^\circ$$

$$\sin(90^\circ - \theta) = \cos\theta$$

$$\csc(90^\circ - \theta) = \sec\theta$$

$$\tan(90^\circ - \theta) = \cot\theta$$

$$\cot(90^\circ - \theta) = \tan\theta$$

$$\sec(90^\circ - \theta) = \csc\theta$$

$$\csc(90^\circ - \theta) = \sec\theta$$

(θ & $90^\circ - \theta$)

sin, cos

tan, cot

sec, cosec

Supplementary Angle

When Sum of 2 angles are 180°

$$30^\circ, 150^\circ$$

$$90^\circ, 90^\circ$$

$$60^\circ, 120^\circ$$

$$-30^\circ, 210^\circ$$

Q2

$$\sin(\pi - \theta) = + \sin\theta$$

$$\csc(\pi - \theta) = - \csc\theta$$

$$\tan(\pi - \theta) = - \tan\theta$$

$$\cot(\pi - \theta) = - \cot\theta$$

$$\sec(\pi - \theta) = - \sec\theta$$

$$\sin(\pi - \theta) = + \sin\theta$$

Trigo Fxn

Q If ABCD is cyclic Quad. then S.T.

$$G_A + G_B + \underline{G_C} + G_D = 0$$

$$A+C=\pi, \quad B+D=\pi$$

$$G_A + G_B + G_{\pi-A}^2 + G_{\pi-B}^2$$

$$G_A + G_B - G_{\pi-A} - G_{\pi-B}$$

$$= 0$$

| | | |
|--------------------|-----------|-------------|
| $\delta m_1^r > 0$ | $b_1 > 0$ | $t m_1 > 0$ |
| $\delta m_2^r > 0$ | $b_2 < 0$ | $t m_2 < 0$ |
| $\delta m_3^r > 0$ | $b_3 < 0$ | $t m_3 < 0$ |
| $\delta m_4^r < 0$ | $b_4 < 0$ | $t m_4 > 0$ |
| $\delta m_5^r < 0$ | $b_5 > 0$ | $t m_5 < 0$ |
| $\delta m_6^r < 0$ | $b_6 > 0$ | $t m_6 < 0$ |
| $\delta m_7^r > 0$ | $b_7 > 0$ | $t m_7 > 0$ |

- $1^\circ \approx 57^\circ \rightarrow 1^{\text{st}}$
 $2^\circ \approx 114^\circ \rightarrow 2^{\text{nd}}$
 $3^\circ \approx 171^\circ \rightarrow 2^{\text{nd}} \frac{180^\circ}{180^\circ} \pi$
 $4^\circ = 228^\circ = 3^{\text{rd}}$
 $5^\circ = 285^\circ = 4^{\text{th}}$
 $6^\circ = 342^\circ = 4^{\text{th}}$
 $7^\circ = 399^\circ = 1^{\text{st}}$
-

$$Q = 27^\circ - 63^\circ \quad [11F]$$

Comp. Sum = 90

$$\tan 27^\circ = \tan(90^\circ - 63^\circ) = \cot 63^\circ$$

$$Q. \frac{\text{Gt } 54^\circ}{\text{fm } 36^\circ} + \frac{\text{fm } 20^\circ}{\text{Gt } 70^\circ} = ?$$

$20^\circ + 70^\circ = 90^\circ$

$$64 + 36^\circ = 90^\circ$$

$$\frac{64 \cancel{36^\circ}}{\cancel{64}36^\circ} + \frac{\cancel{64}20^\circ}{\cancel{64}70^\circ} = 1 + 1 = 2$$

$$\begin{aligned} \text{At } 54^\circ &= \text{At } (90 - 36^\circ) = \text{Am } 36^\circ \\ \text{Am } 20^\circ &= \text{Am } (90 - \underline{70^\circ}) = \text{At } 70^\circ \end{aligned}$$

$$\begin{aligned}
 & Q \quad \delta m^2 5^\circ + \delta m^2 10^\circ + \delta m^2 15^\circ \quad + \text{break} \quad \boxed{\delta m^2 75^\circ} \quad \boxed{\delta m 80^\circ} \quad \boxed{\delta m^2 85^\circ} \quad + \quad \delta m^2 90^\circ \\
 & \frac{\delta m^2}{\boxed{5^\circ}} \rightarrow \underline{\delta m^2 10^\circ} + \underline{\delta m^2 15^\circ} \quad \underline{\delta^2 15^\circ + \delta^2 10^\circ + \delta^2 5^\circ + L^2} \\
 & 85^\circ \quad \frac{1 + L + 1 + \dots + 1 + \delta m^2 45^\circ + \frac{1}{2}}{8 \text{ Pairs}} \\
 & 17 \text{ Pairs} \\
 & 8 + 1 + \frac{1}{2} = 9 + \frac{1}{2} = \frac{19}{2} \\
 & \delta m 85^\circ = 675^\circ \\
 & \delta m 80^\circ = 6710^\circ \\
 & 70^\circ = 50^\circ
 \end{aligned}$$

$$\sum m^2 5 + \sum m^2 10^\circ + \sum m^2 15^\circ + \sum m^2 20^\circ + \sum m^2 25^\circ + \sum m^2 30^\circ + \sum m^2 35^\circ + \sum m^2 40^\circ + \sum_{i=1}^{55} G_i^2 35^\circ + \sum_{i=35}^{60} G_i^2 30^\circ + \sum_{i=30}^{65} G_i^2 25^\circ + \sum_{i=25}^{70} G_i^2 20^\circ + \sum_{i=20}^{75} G_i^2 15^\circ + \sum_{i=15}^{80} G_i^2 10^\circ + \sum_{i=10}^{85} G_i^2 5^\circ + L$$

$$1 + 1 + 1 + 1 + 1 + 1 + 1 + \frac{1}{2} + L = 9.5$$

$$Q = \sum_{r=1}^{89^\circ} \log_{10} (\tan r^\circ)$$

$$\log_{10} \tan 1^\circ + \log \tan 2^\circ + \log \tan 3^\circ + \dots - \log \tan 87^\circ + \log \tan 88^\circ + \log \tan 89^\circ$$

$$\tan 1^\circ \times \tan 1^\circ$$

$$\tan 0^\circ \times \tan 0^\circ$$

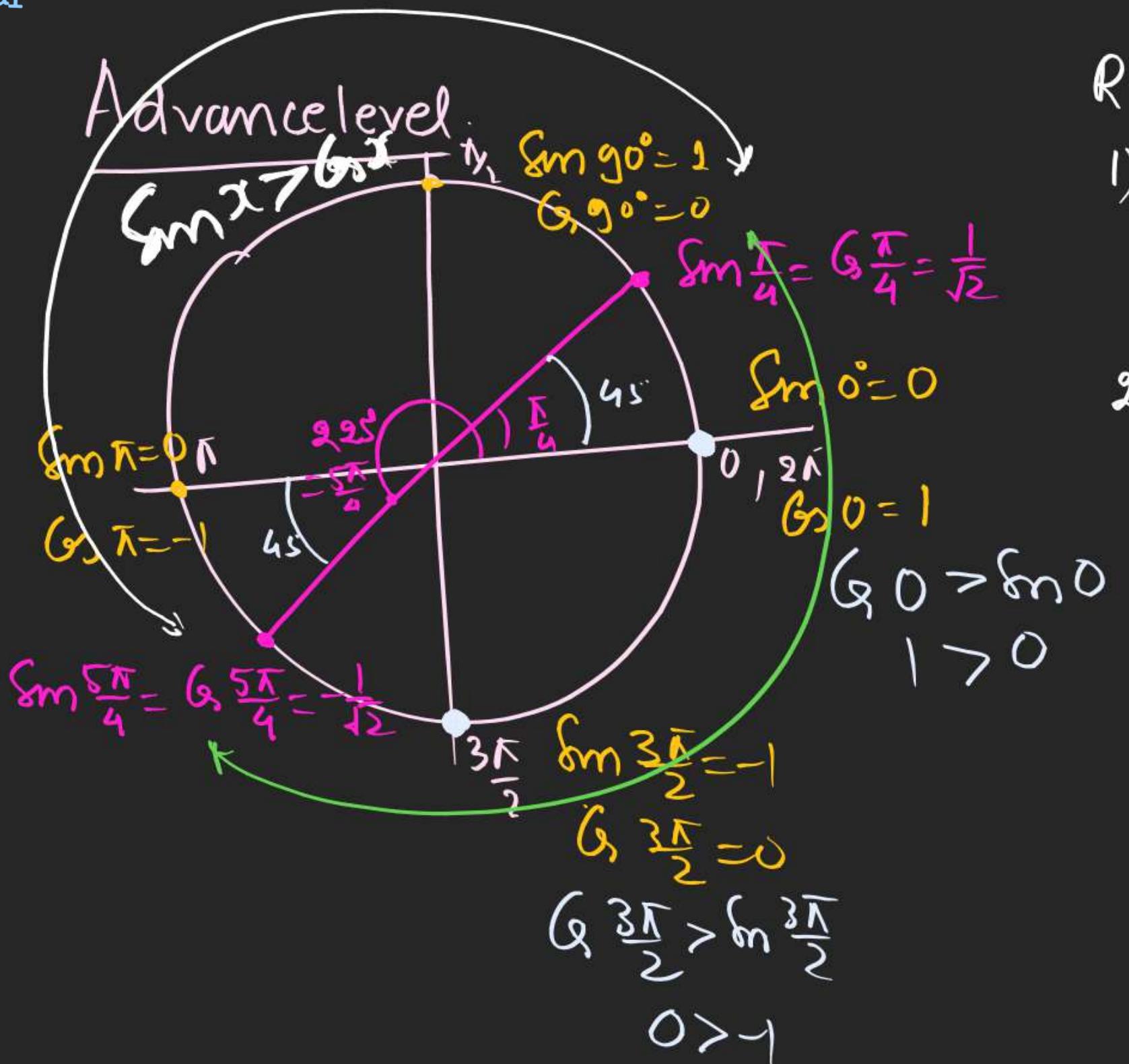
$$= L$$

$$= \log \left\{ \tan 1^\circ + \tan 2^\circ + \tan 3^\circ + \dots - \boxed{\tan 45^\circ} + \tan 87^\circ + \tan 88^\circ + \tan 89^\circ \right\}$$

↑ ↓

$$= \log \left\{ \underbrace{\tan 1^\circ}_{\text{44 Pairs}} + \underbrace{\tan 2^\circ}_{\text{44 Pairs}} + \underbrace{\tan 3^\circ}_{\text{44 Pairs}} + \dots + \tan 87^\circ + \tan 88^\circ + \tan 89^\circ \right\}$$

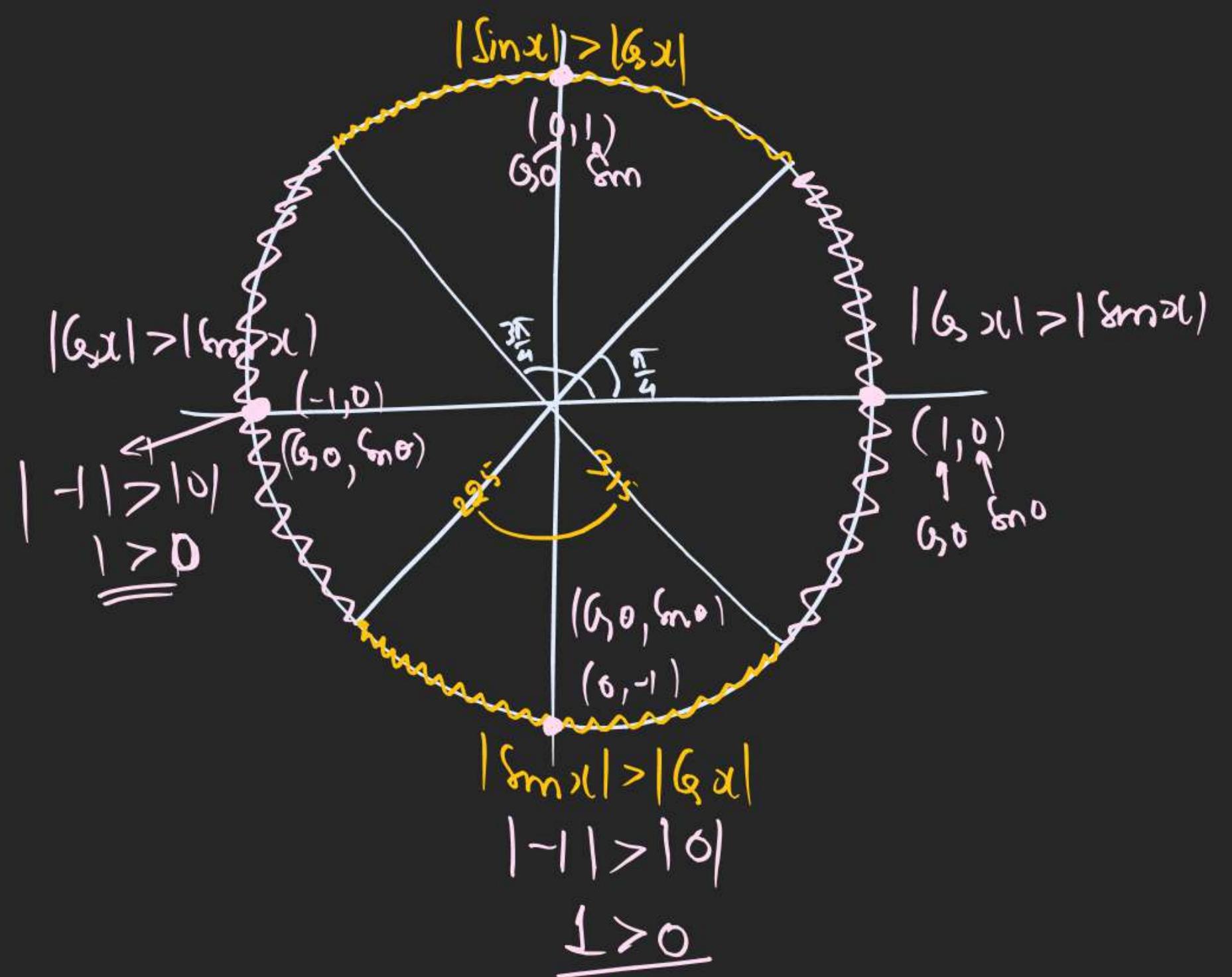
$$= \log \{ 1 \} = 0$$

 R_K

$$1) \theta \in (45^\circ - 225^\circ)$$

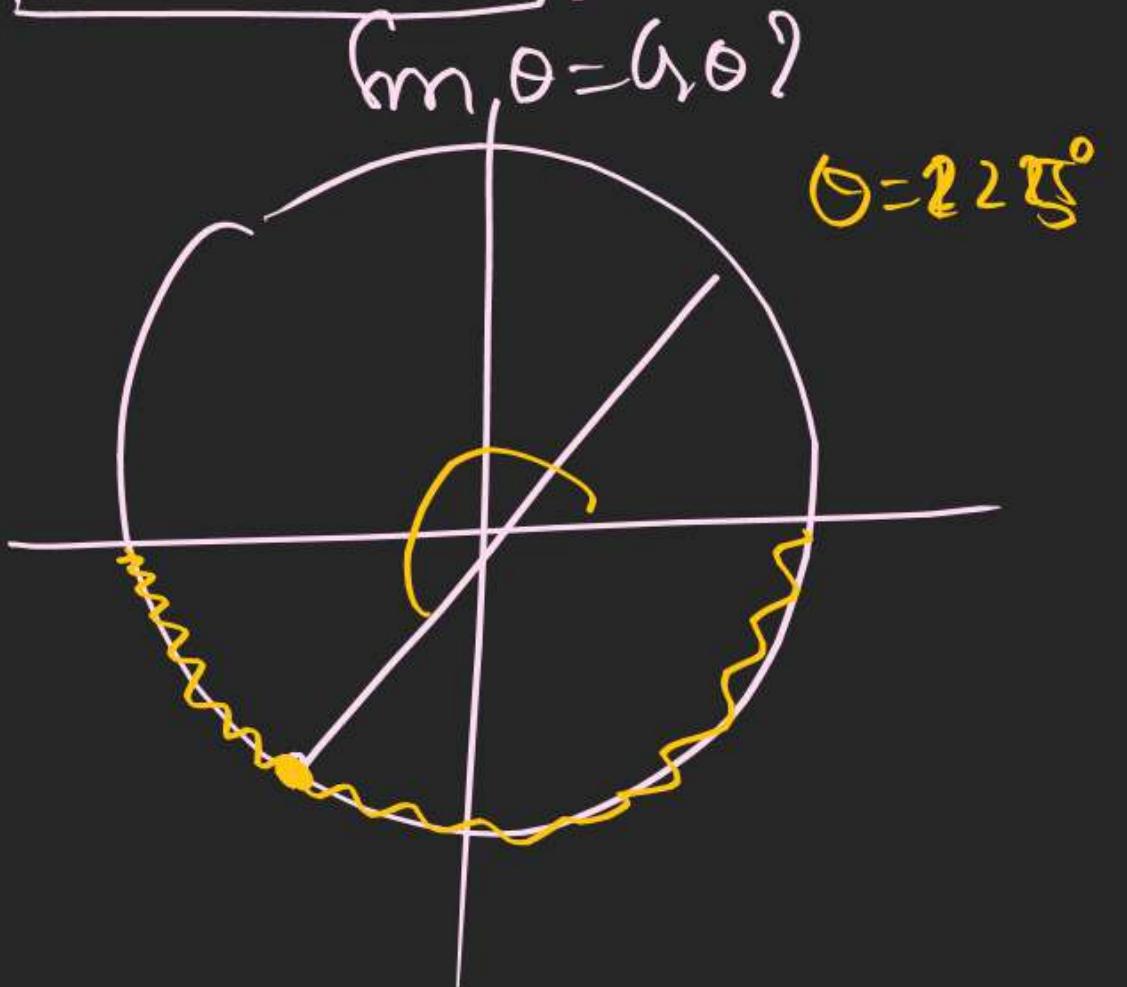
$$\theta \in \left(\frac{\pi}{4}, \frac{5\pi}{4}\right) \rightarrow \text{Sm } 0 > \text{Sm } \theta$$

$$2) \theta \in \left(\frac{5\pi}{4}, \frac{7\pi}{4}\right) \rightarrow \text{Sm } \theta > \text{Sm } 0$$

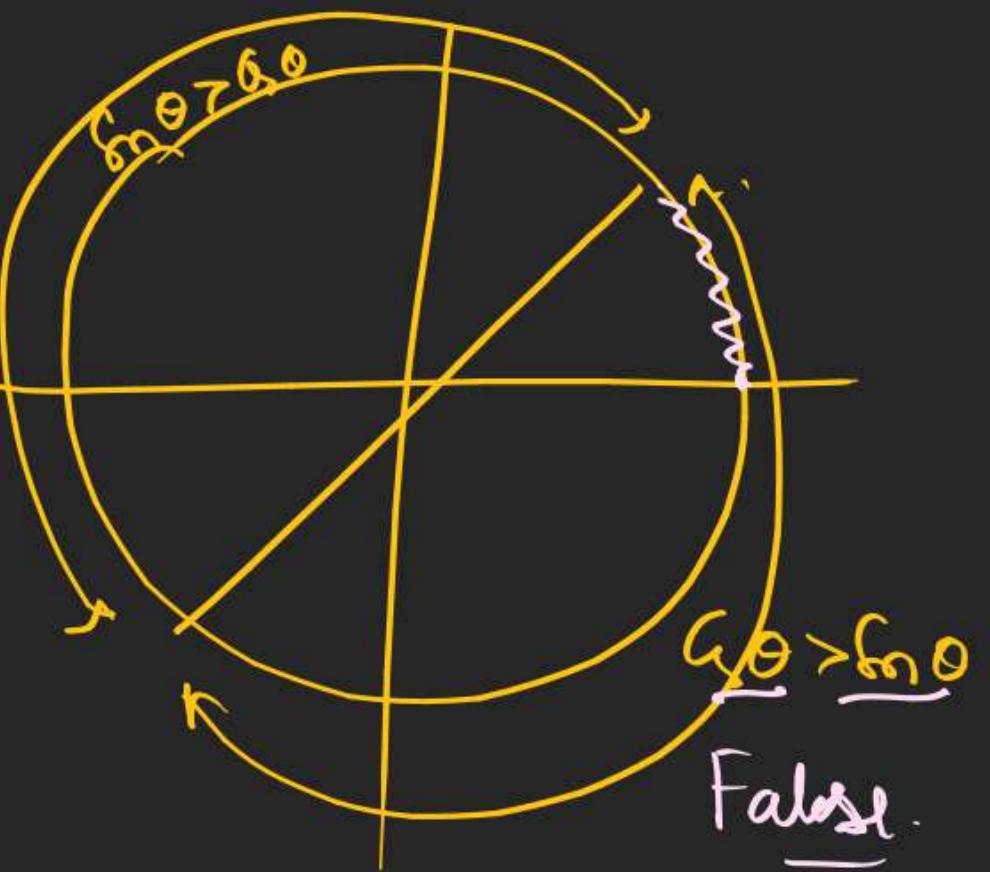


$$\begin{aligned} 6\sin \theta &= 4(600\pi) \\ 6\theta &= x(600\pi) \end{aligned}$$

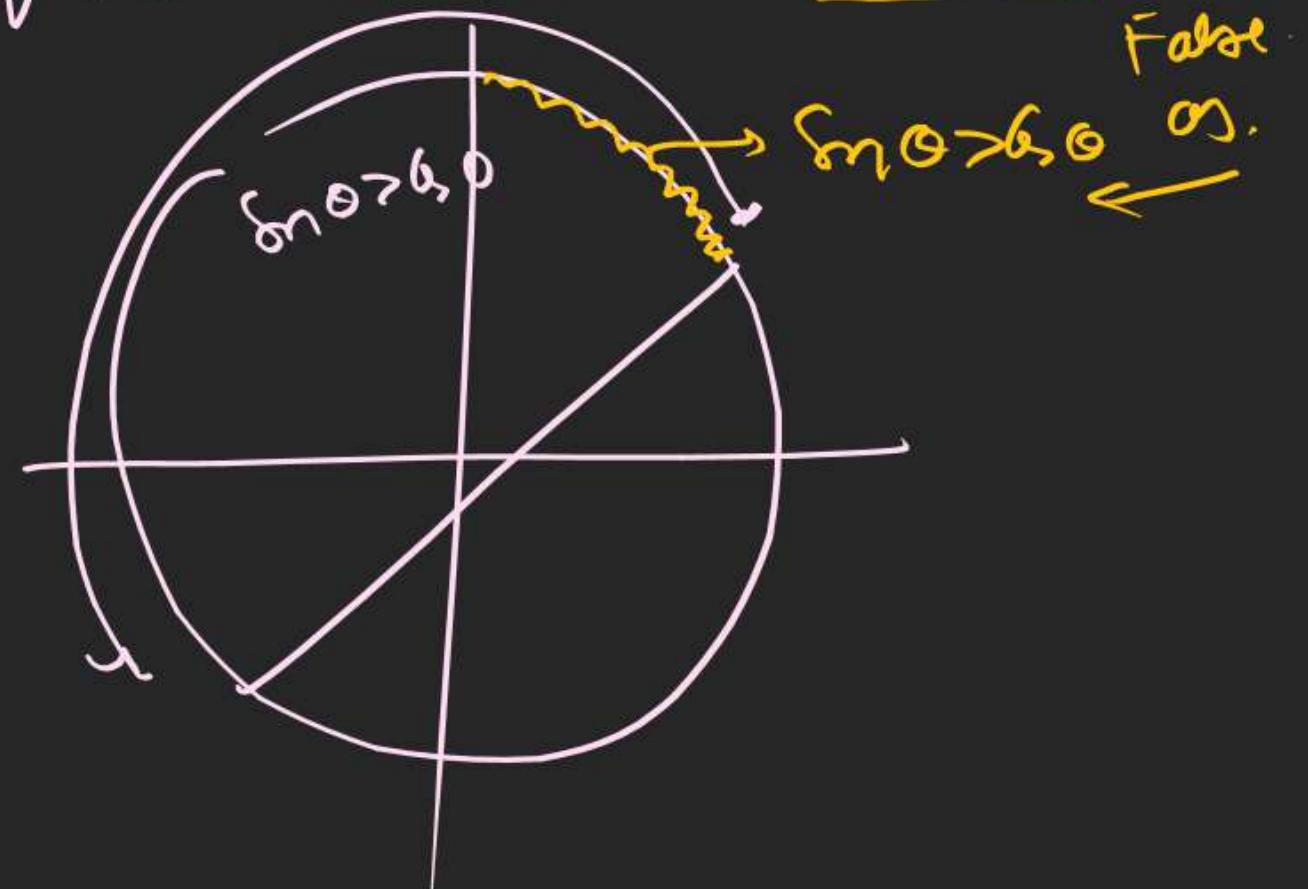
Q angle $180^\circ < \theta < 360^\circ$ for what value



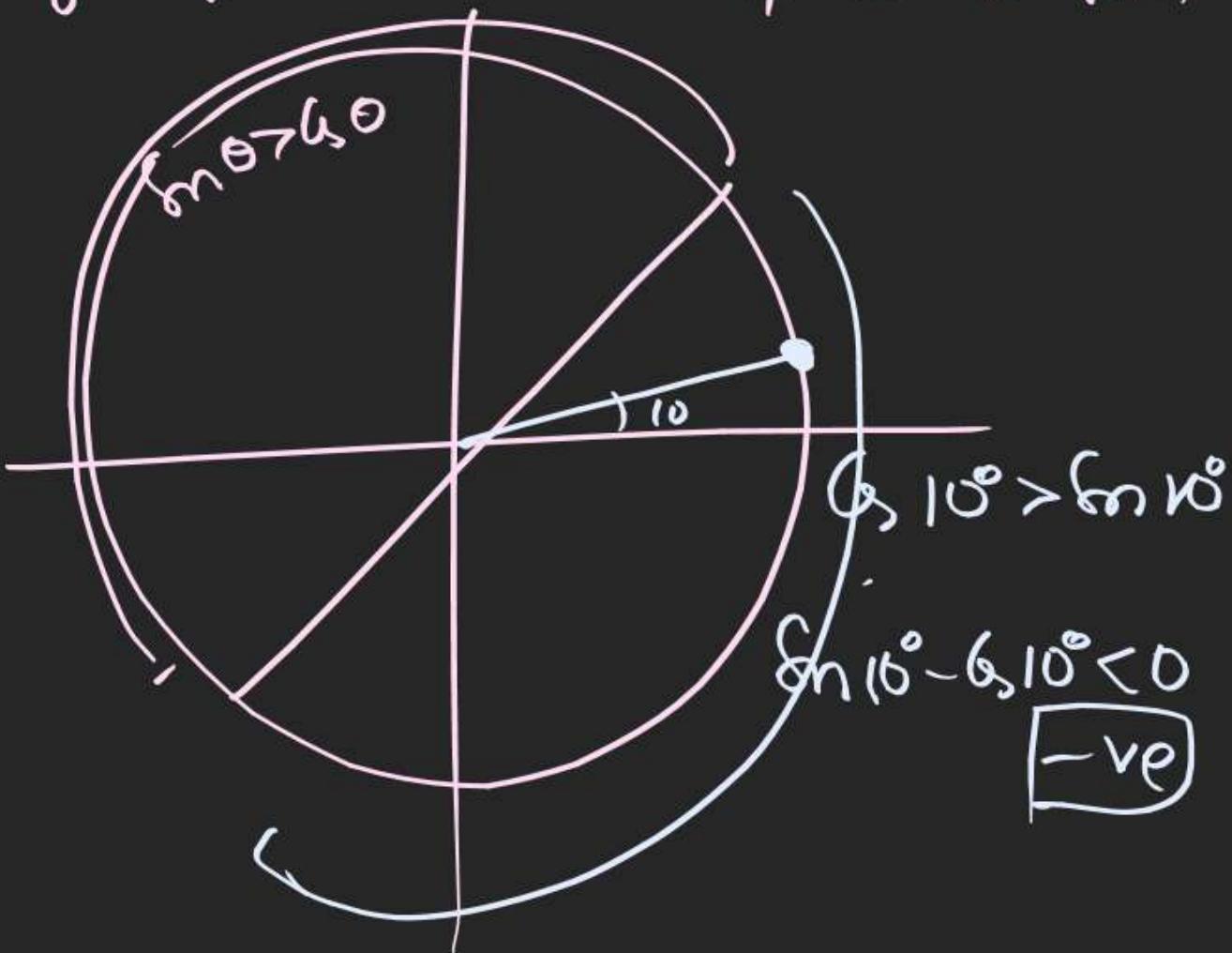
Q If $\theta \in [0, 45^\circ]$ then $\text{Co } \theta < \text{En } \theta$ [T/F] ?



Q If $\theta \in (45^\circ, 90^\circ]$ then $\sin \theta < \cos \theta$ [T/F]



Q Sign of $\sin 10^\circ - \cos 10^\circ$



Q For a Pentagon angles are

$$\theta_1 < \theta_2 < \theta_3 < \theta_4 < \theta_5$$

from d value of

$$\frac{\sin(\theta_1 + \theta_2)}{\sin(\theta_3 + \theta_4 + \theta_5)} + \frac{\sin(\theta_1 + \theta_2 + \theta_3)}{\sin(\theta_4 + \theta_5)}$$

$$\begin{aligned} \text{Sum of all Interior Angle, } &= (n-2)\pi \\ &= (5-2)\pi \end{aligned}$$

$$\boxed{\theta_1 + \theta_2 + \theta_3 + \theta_4 + \theta_5 = 3\pi}$$

$$\theta_3 + \theta_4 + \theta_5 = 3\pi - (\theta_1 + \theta_2)$$

$$\theta_1 + \theta_2 + \theta_3 = 3\pi - (\theta_4 + \theta_5)$$

$$\frac{\sin(\theta_1 + \theta_2)}{\sin(3\pi - (\theta_1 + \theta_2))} + \frac{\sin(3\pi - (\theta_4 + \theta_5))}{\sin(\theta_4 + \theta_5)}$$

$$\frac{\sin(\theta_1 + \theta_2)}{\sin(\theta_1 + \theta_2)} + \frac{\sin(\theta_4 + \theta_5)}{\sin(\theta_4 + \theta_5)} = 1 + 1 = 2$$

* $\frac{\sin(3\pi - \theta)}{\sin \theta} = +\sin \theta$



Adhe Se Kam / Aadhe Se Jayada

$$\varphi \left(1 + G \frac{\pi}{6} \right) \left(1 + G \frac{\pi}{3} \right) \left(1 + G \frac{2\pi}{3} \right) \left(1 + G \frac{5\pi}{6} \right)$$

$$\left(1 + G \frac{\pi}{6} \right) \left(1 + G \frac{2\pi}{6} \right) \left(1 + G \sqrt{\frac{4\pi}{6}} \right) \left(1 + G \frac{5\pi}{6} \right)$$

" " $\left(1 + G \left(\pi - \frac{2\pi}{6} \right) \right) \left(1 + G \left(\pi - \frac{\pi}{6} \right) \right)$

$$\left(1 + G \frac{\pi}{6} \right) \left(1 + G \frac{2\pi}{6} \right) \left(1 - G \frac{2\pi}{6} \right) \left(1 - G \frac{\pi}{6} \right)$$

$$\left(R - G^2 \left(\frac{\pi}{6} \right) \right) \left(1^2 - G^2 \left(\frac{2\pi}{6} \right) \right)$$

$$\sin^2 \left(\frac{\pi}{6} \right) \cdot \sin^2 \left(\frac{2\pi}{6} \right)$$

$$\sin^2 30^\circ \times \sin^2 60^\circ = \left(\frac{1}{2} \right)^2 \times \left(\frac{\sqrt{3}}{2} \right)^2 = \frac{1}{4} \times \frac{3}{4} = \frac{3}{16}$$

Qs जब नहीं Series में हो

(1) Last के 2, 3 Dekho

(2) 3 के Angle के Nr > half of Dr

हीं तो $(\pi - \theta)$ Ki tarah treat
Karo

(4) $\overrightarrow{4\pi/6}$ Nr = 4
Dr = 6 और half = 3

$Nr > Dr$ K half
4 > 3

$$4\frac{\pi}{6} = \frac{6\pi - 2\pi}{6} = \frac{\pi - 2\pi}{6}$$

$$5\frac{\pi}{6} = \frac{6\pi - \pi}{6} = \frac{\pi - \pi}{6}$$