

INTERFERENCE

$$I_R = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

$$\text{If } I_1 = I_2 = I$$

$$I_R = (2I + 2I \cos \phi)$$

$$I_R = 2I(1 + \cos \phi)$$

$$I_R = 2I(1 + 2\cos^2 \frac{\phi}{2} - 1)$$

$$I_R = 4I \cos^2(\phi/2)$$

$$(I_R)_{\max} = 4I$$

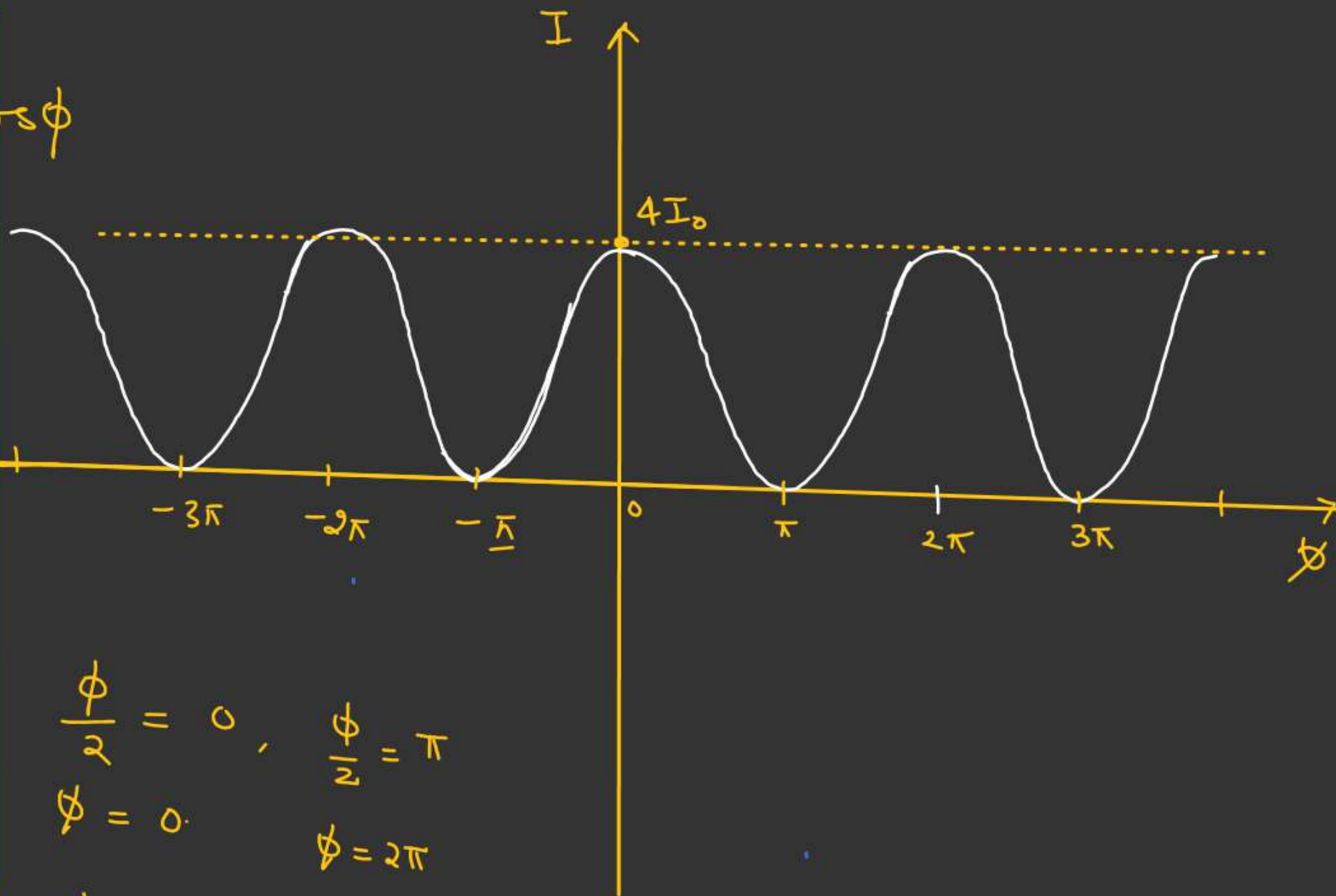
$$\Downarrow$$

$$\phi = 2n\pi$$

$$(I_R)_{\min} = 0$$

$$\Downarrow$$

$$\phi = (2n+1)\pi$$



$$\frac{\phi}{2} = 0, \quad \frac{\phi}{2} = \pi$$

$$\phi = 0$$

$$\phi = 2\pi$$

$$\frac{\phi}{2} = 2\pi$$

$$\phi = 4\pi$$

(*) Coherent Sources:-

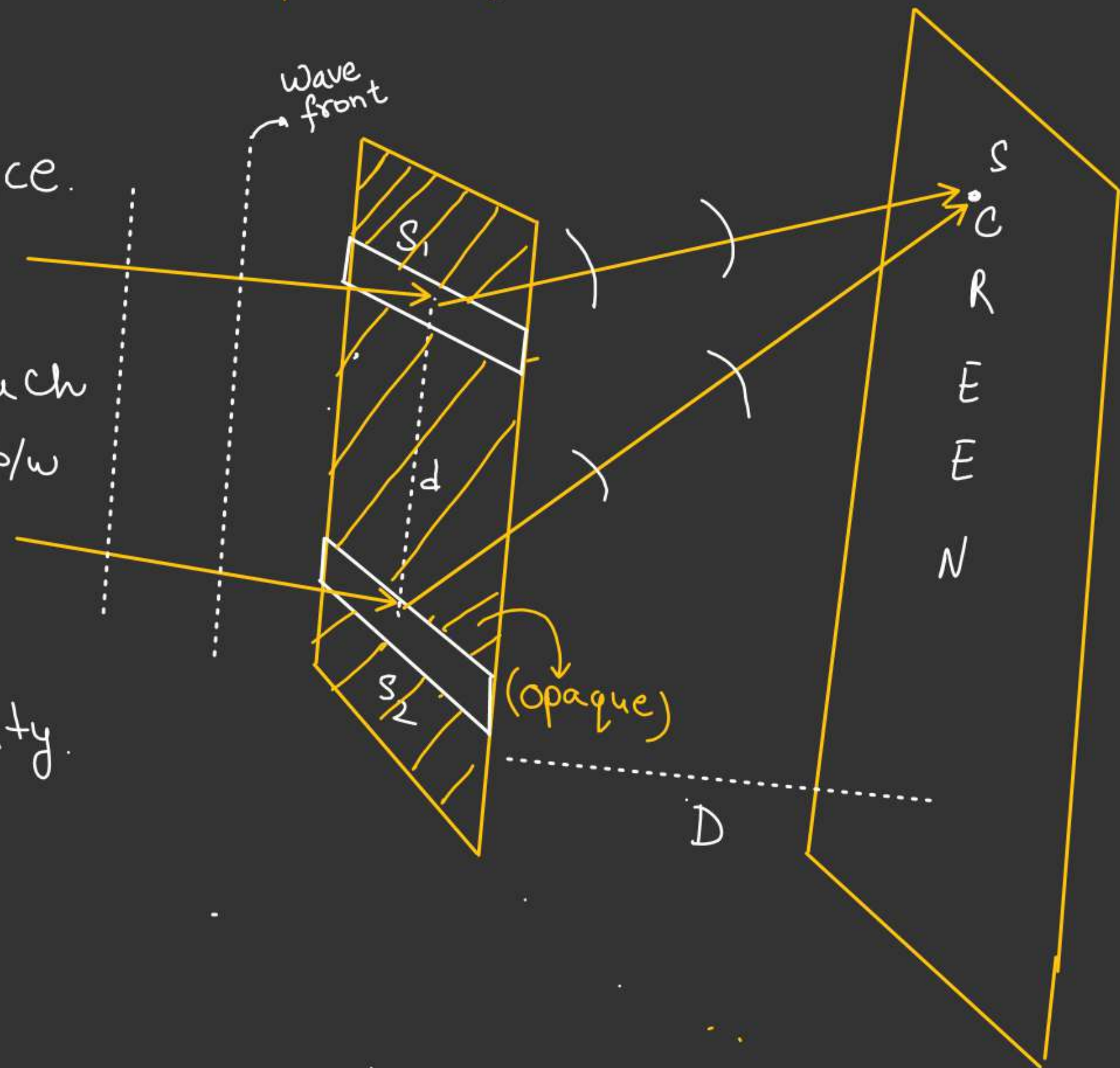
- ↳ Sources which have constant phase difference are called coherent sources.
- ↳ Two Independent light sources never be coherent.
- ↳ From a single light source if we generate two secondary light sources then these light sources are coherent in nature.



Y.D.S.E (Young's Double Slit experiment)

Assumption:-

1. Monochromatic light source.
(Single wavelength)
2. Distance b/w slits is much smaller than distance b/w screen. ($d \ll D$)
3. light source at infinity.



Since $D \gg d$.

S_1P , OP & S_2P assumed to be parallel.

In ΔS_1S_2M .

$$\sin \theta = \frac{S_2M}{S_1S_2}$$

$$S_2M = S_1S_2 \sin \theta$$

$$\underline{\Delta x} = d \sin \theta = d \tan \theta \quad \text{--- (1)}$$

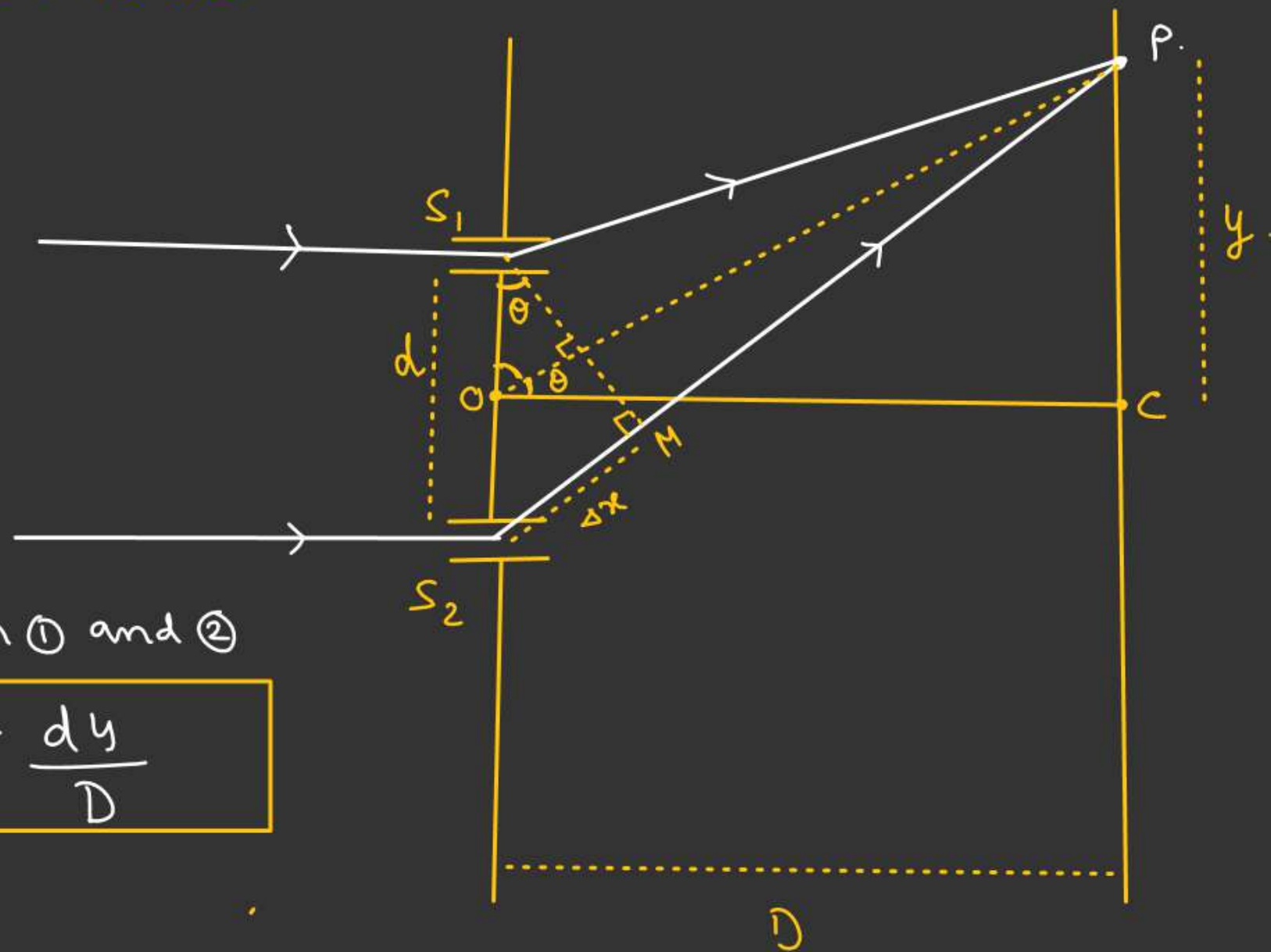
θ very small.
 $\sin \theta \approx \tan \theta$.

In ΔPOC

$$\tan \theta = \frac{y}{D} \quad \text{--- (2)}$$

From (1) and (2)

$$\Delta x = \frac{dy}{D}$$



For Constructive interference.

$$\Delta x = n\lambda$$

$$\frac{dy}{D} = n\lambda$$

$$y = \frac{n\lambda D}{d}$$

For $n=0$, $y=0 \Rightarrow$ Central bright fringe } OR Central Maxima

$n=1$, $y = \frac{D\lambda}{d} \Rightarrow$ 1st bright fringe } OR { 1st Maxima

$n=2$, $y = \frac{2D\lambda}{d} \Rightarrow$ 2nd bright fringe } OR { 2nd Maxima

For destructive Interference

$$\Delta x = (2n+1)\frac{\lambda}{2} \quad (n=0,1,2,3,\dots)$$

$$\frac{dy}{D} = (2n+1)\frac{\lambda}{2}$$

$$y = (2n+1)\frac{D\lambda}{2d}$$

$n=0$, $y = \frac{D\lambda}{2d} \Rightarrow$ 1st Minima.

$n=1$, $y = \frac{3D\lambda}{2d} \Rightarrow$ 2nd Minima

$n=2$, $y = \frac{5D\lambda}{2d} \Rightarrow$ 3rd Minima

FRINGE WIDTH

⇒ Distance b/w two consecutive Maxima or two consecutive minima called Fringe Width.

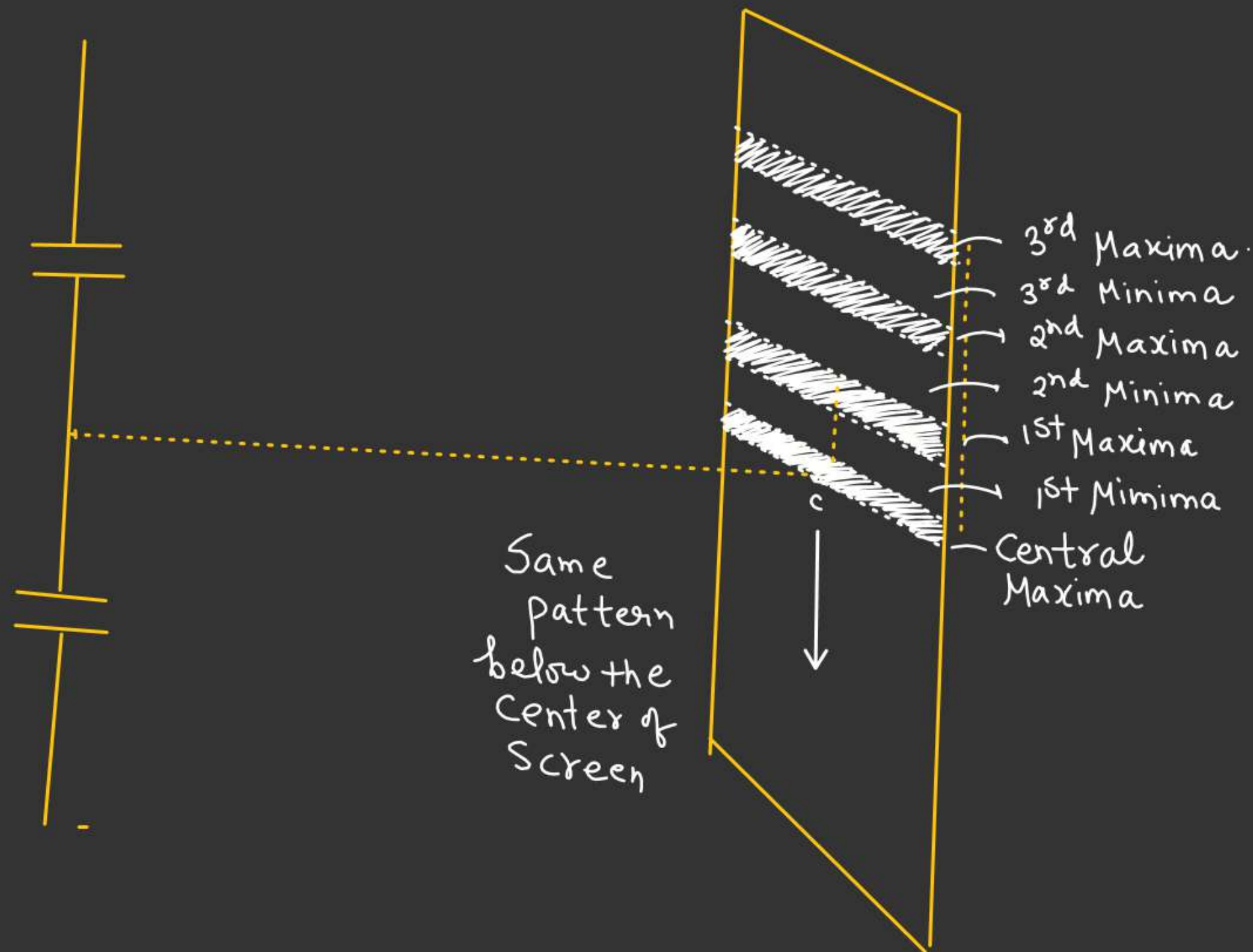
For Maxima

$$y_n = \frac{nD\lambda}{d}$$

$$y_{n-1} = (n-1) \frac{D\lambda}{d}$$

$$W = y_n - y_{n-1}$$

$$W = \frac{D\lambda}{d}$$



QAAngular fringe width

$$\tan \beta = \frac{w}{D}$$

$$\tan \beta \approx \beta = \left(\frac{w}{D} \right)$$

$$\beta = \frac{\cancel{D} \lambda}{d \cdot \cancel{D}}$$

$$\beta = \frac{\lambda}{d}$$

QA

$$w = \frac{D \lambda}{d}$$

 S_1 