

CURRENT ELECTRICITY

(8)

$$I = neAv_d \quad \text{--- (1)}$$

OHM'S LAW

$$J = \frac{I}{A} = nev_d \quad \text{--- (2)}$$

$$v_d = \left(\frac{eE\tau}{m} \right) \quad \text{--- (3)}$$

From (1) and (3)

$$I = (neA) \left(\frac{e\tau}{m} \right) E$$

$$I = \left(\frac{ne^2\tau}{m} \right) AE \quad \text{--- (4) } (**)$$

$$\frac{I}{A} = \left(\frac{ne^2\tau}{m} \right) E \Rightarrow \vec{J} = \sigma \vec{E} \quad \rho = \frac{m}{ne^2\tau}, \quad \left(\sigma = \frac{1}{\rho} = \frac{ne^2\tau}{m} \right)$$

From (4) and (5)

$$I = \left(\frac{ne^2\tau}{m} \right) \left(\frac{A}{l} \right) V$$

$$V = El \quad \text{--- (5)}$$

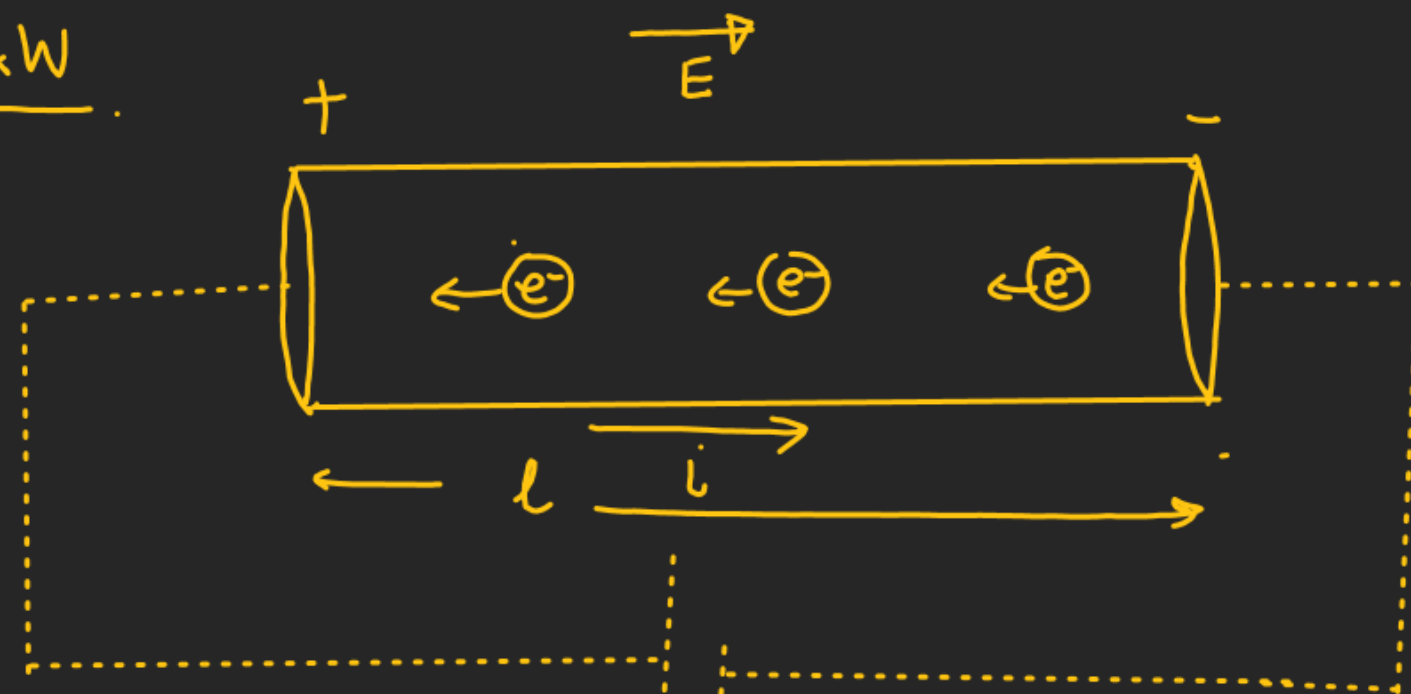
$$E = \left(\frac{V}{l} \right)$$

$$V = \left(\frac{\rho l}{A} \right) I$$

$$V = IR$$

Ohm's Law

R → Resistance



CURRENT ELECTRICITY

$$R = \frac{\rho l}{A}$$

$$G = \frac{1}{R}$$

$G \rightarrow$ Conductance $\rightarrow [mho] \rightarrow [\Omega^{-1}]$

$\alpha \Rightarrow$ Temperature coefficient of resistance

\hookrightarrow Depends on :- 1. geometrical Configuration. ✓

2. Temperature.

S.I \rightarrow ohm $[\Omega]$.

$$\left[\begin{array}{l} \rho \rightarrow \text{Resistivity} \\ \sigma = \frac{1}{\rho} \rightarrow \text{Conductivity} \end{array} \right]$$

\rightarrow Depends only on
 \rightarrow Nature of material
 \rightarrow Temperature.

Temperature dependency for conductor.

$$R = R_0 (1 + \alpha \Delta T)$$

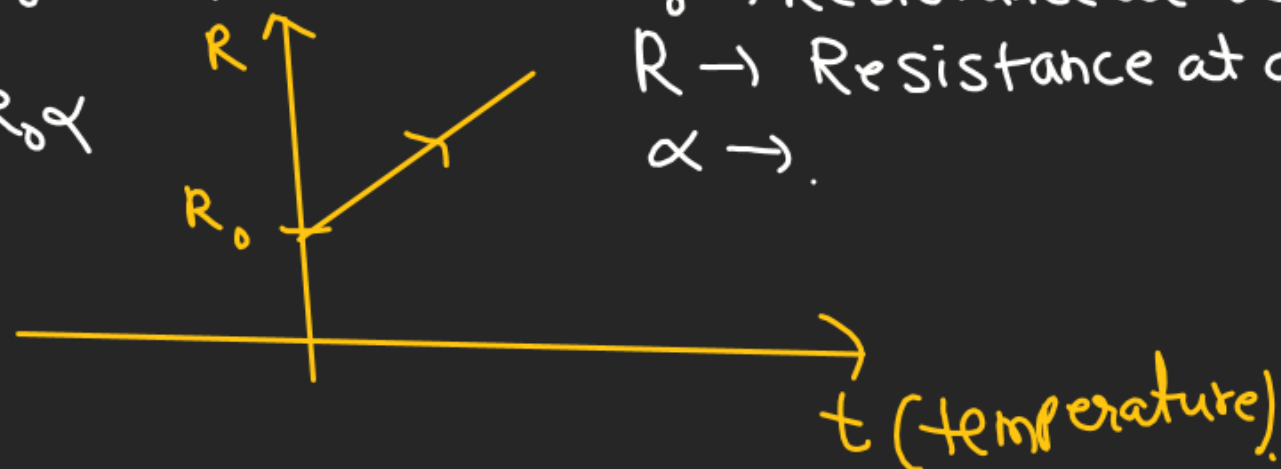
$$\rho = \rho_0 (1 + \alpha \Delta T)$$

$R_0 \rightarrow$ Resistance at $0^\circ C$.
 $R \rightarrow$ Resistance at any $t^\circ C$.
 $\alpha \rightarrow$

$$** \quad R - R_0 = R_0 \alpha \Delta T$$

$$\frac{\Delta R}{\Delta T} = R_0 \alpha$$

$$\frac{dR}{dt} = R_0 \alpha$$



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$$\rho = \frac{m n e^2}{\tau}$$

Ohm's Law :- $[\vec{J} = \sigma \vec{E}]$ $V = IR$

↳ ① [Current density is directly proportional to applied electric field. provided temperature must be Constant.]

↳ ② [Current across any conductor is directly proportional to applied potential difference. provided temperature must be Constant]

Note

⇒

If temperature increases →

- $\tau \rightarrow \text{decreases.}$
- $\rho \rightarrow \text{increases.}$
- $\sigma \rightarrow \text{decreases.}$

CURRENT ELECTRICITY

★★

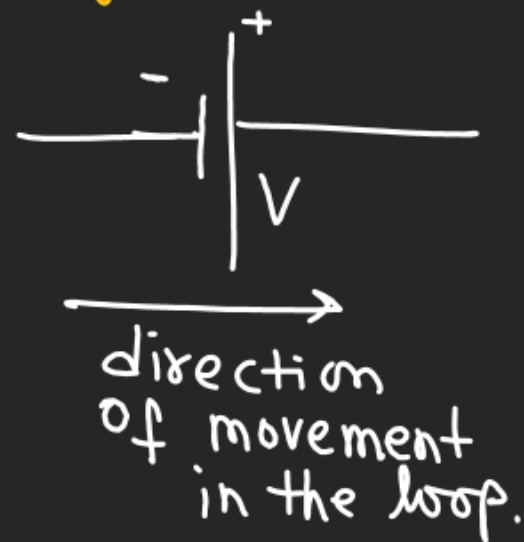
K.V.L and K.C.L.

K.V.L :→ [Krichhoff's Voltage Law]

↳ (Depends on energy conservation)

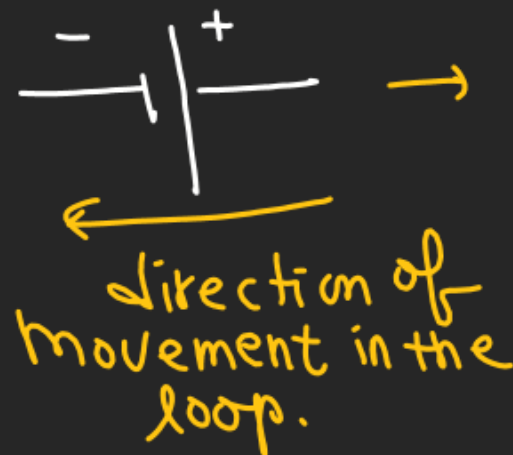
↳ Sum of all the potential drop across any closed loop is zero

Sign-convention.



① Crossing the battery from -ve terminal to +ve terminal Considered as potential rise. (+V)

②



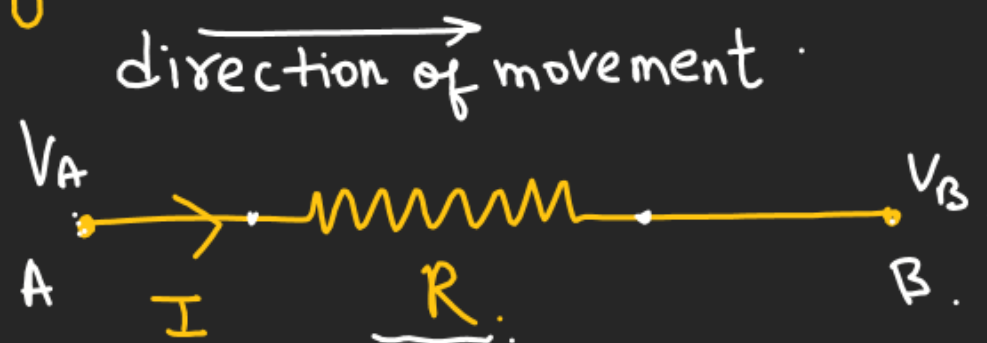
→ (-V)

→ Crossing the battery from +ve terminal to -ve terminal Considered as potential drop.

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For resistance

Sign-Convention:



$$V_A - IR = V_B$$

$$\boxed{V_A - V_B = IR}$$

① If direction of movement in the loop is along the Current flow then potential drop.

$$\boxed{\Delta V = -IR}$$

direction of movement



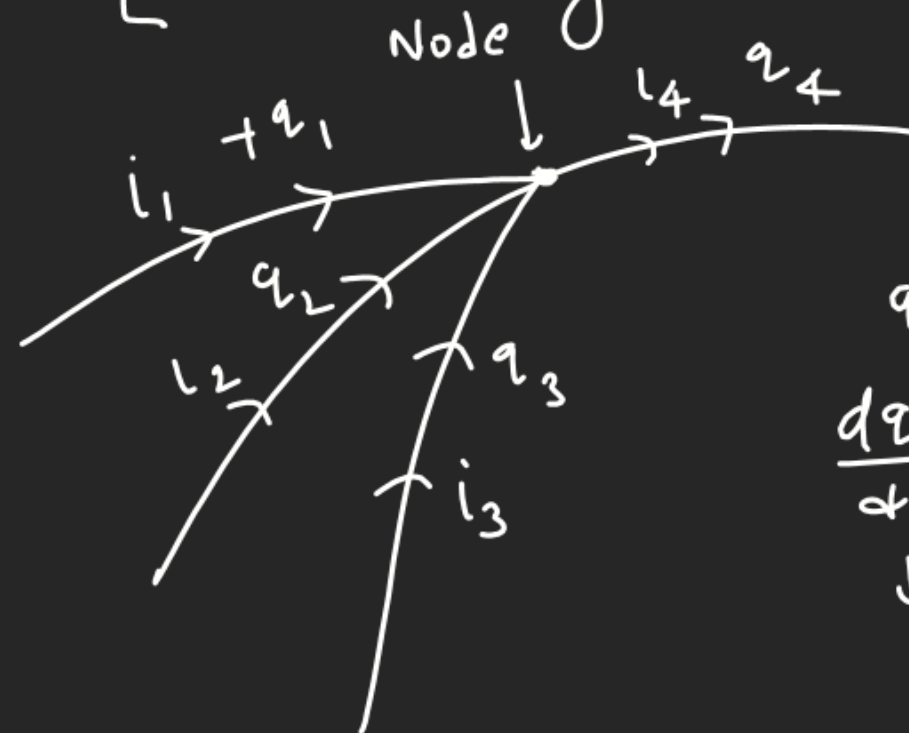
$$\boxed{V_B + IR = V_A}$$

While moving opposite to Current flow in the resistance potential across the resistance considered as potential rise

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K.C.L \rightarrow Krichhoff's Current Law [Conservation of Charge]

\rightarrow Sum of incoming current is equal to sum of outgoing current across any node or junction



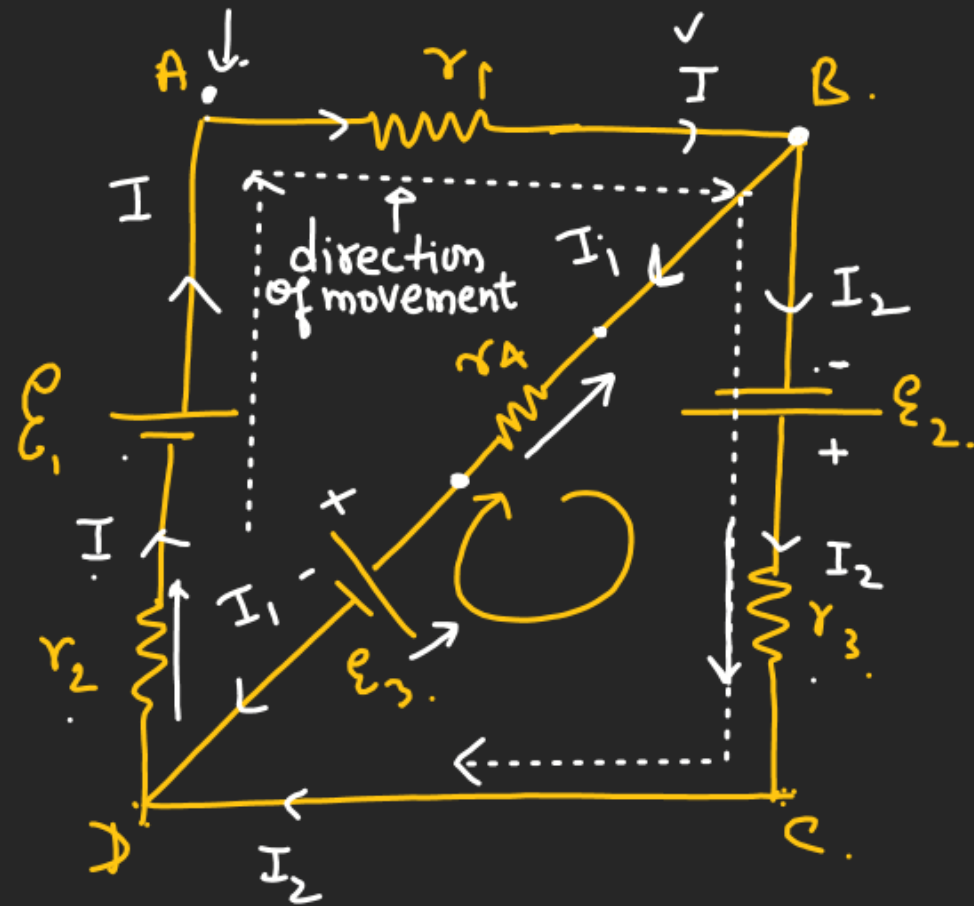
$$q_1 + q_2 + q_3 = q_4$$

$$\frac{dq_1}{dt} + \frac{dq_2}{dt} + \frac{dq_3}{dt} = \frac{dq_4}{dt}$$

$$\boxed{i_1 + i_2 + i_3 = i_4}$$

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K.V.L in the loop ABCDA

$$[-I r_1 + \varepsilon_2 - I_2 r_3 - I r_2 + \varepsilon_1 = 0]$$

K.V.L in the loop BCDB

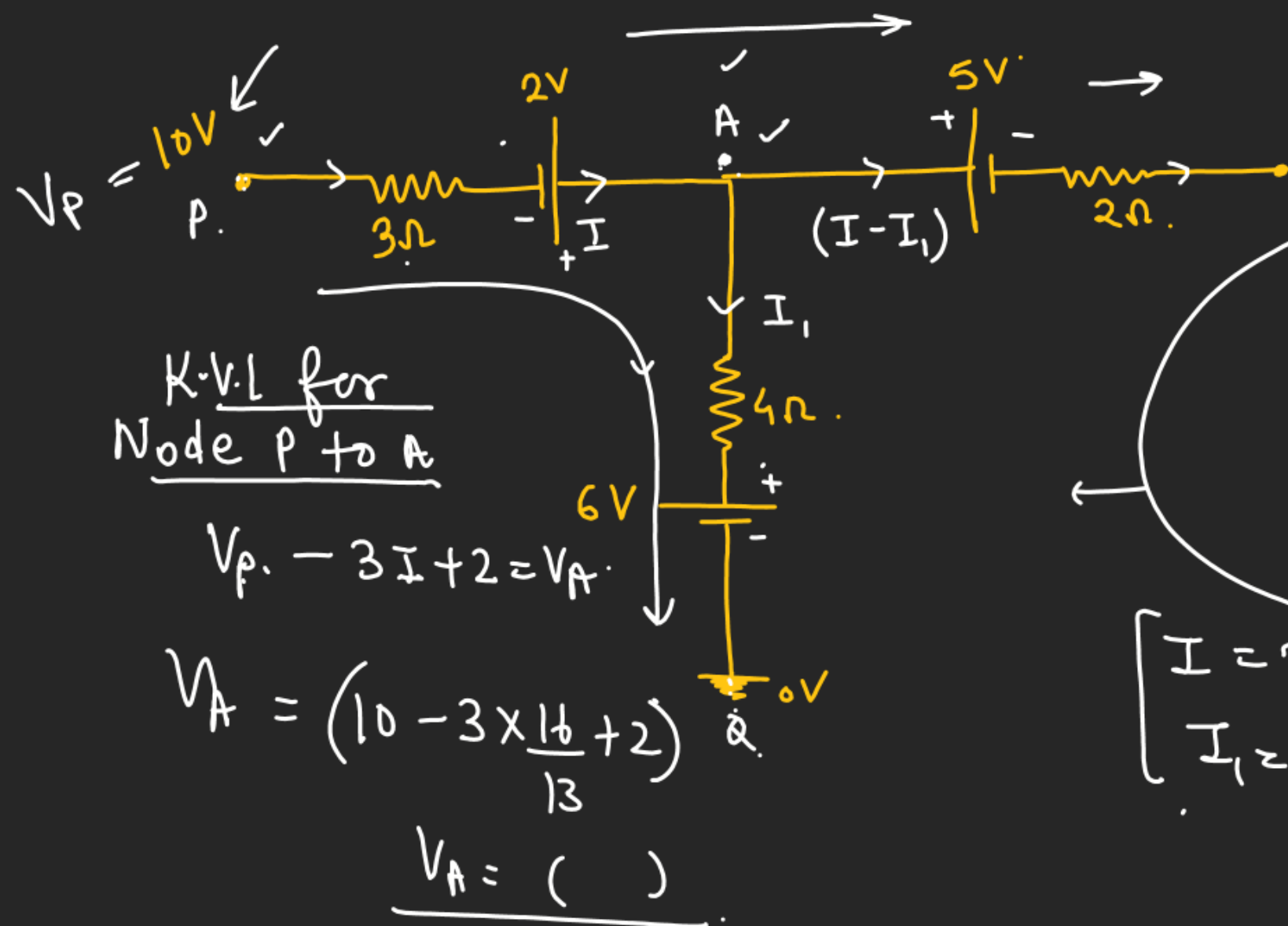
$$[+\varepsilon_2 - I_2 r_3 + \varepsilon_3 + I_1 r_4 = 0]$$

K.C.L at B

$$[I = I_1 + I_2]$$

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Find, $V_A = ?$, $V_B = ?$ 

$$I = I_1 + I_2$$

K.V.L from Node P to Q.

$$10 - 3I + 2 - 4I_1 - 6 = V_Q = 0$$

$$6 - 3I - 4I_1 = 0 \quad \text{--- (1)}$$

K.V.L for the path P → B

$$10 - 3I + 2 - 5 - 2(I - I_1) = V_B = 2V$$

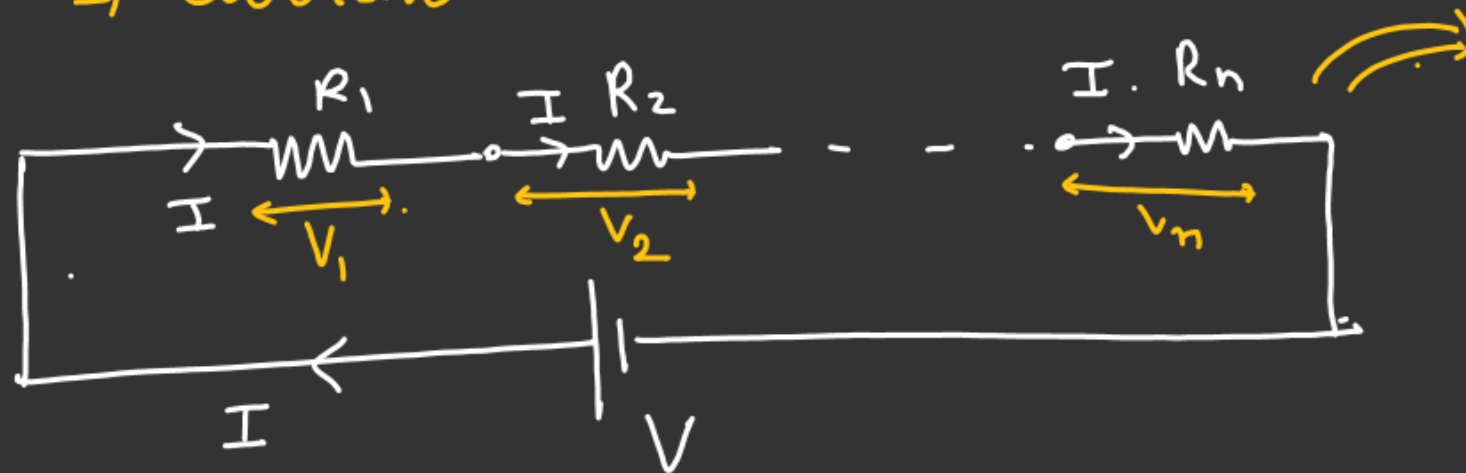
$$10 - 3I - 5 - 2I + 2I_1 = 0$$

$$\begin{cases} I = ? \left(\frac{16}{13}\right) ?? \\ I_1 = ? = \left(\frac{15}{26}\right) ?? \end{cases}$$

Series and parallel combination

Series combination

↳ Current in all resistance is same.



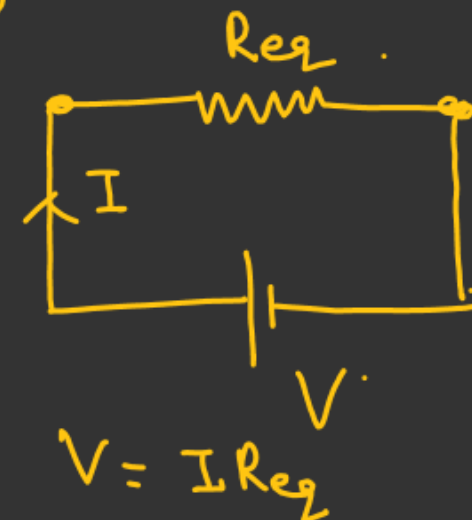
$$\begin{cases} V_1 = IR_1 \\ V_2 = IR_2 \\ \vdots \\ V_n = IR_n \end{cases}$$

$$V_1 + V_2 + \dots + V_n = V$$

$$I(R_1 + R_2 + \dots + R_n) = IR_{eq}$$

$$\boxed{R_{eq} = R_1 + R_2 + \dots + R_n}$$

$R_{eq} = ??$



$$V = IR_{eq}$$

Parallel Combination

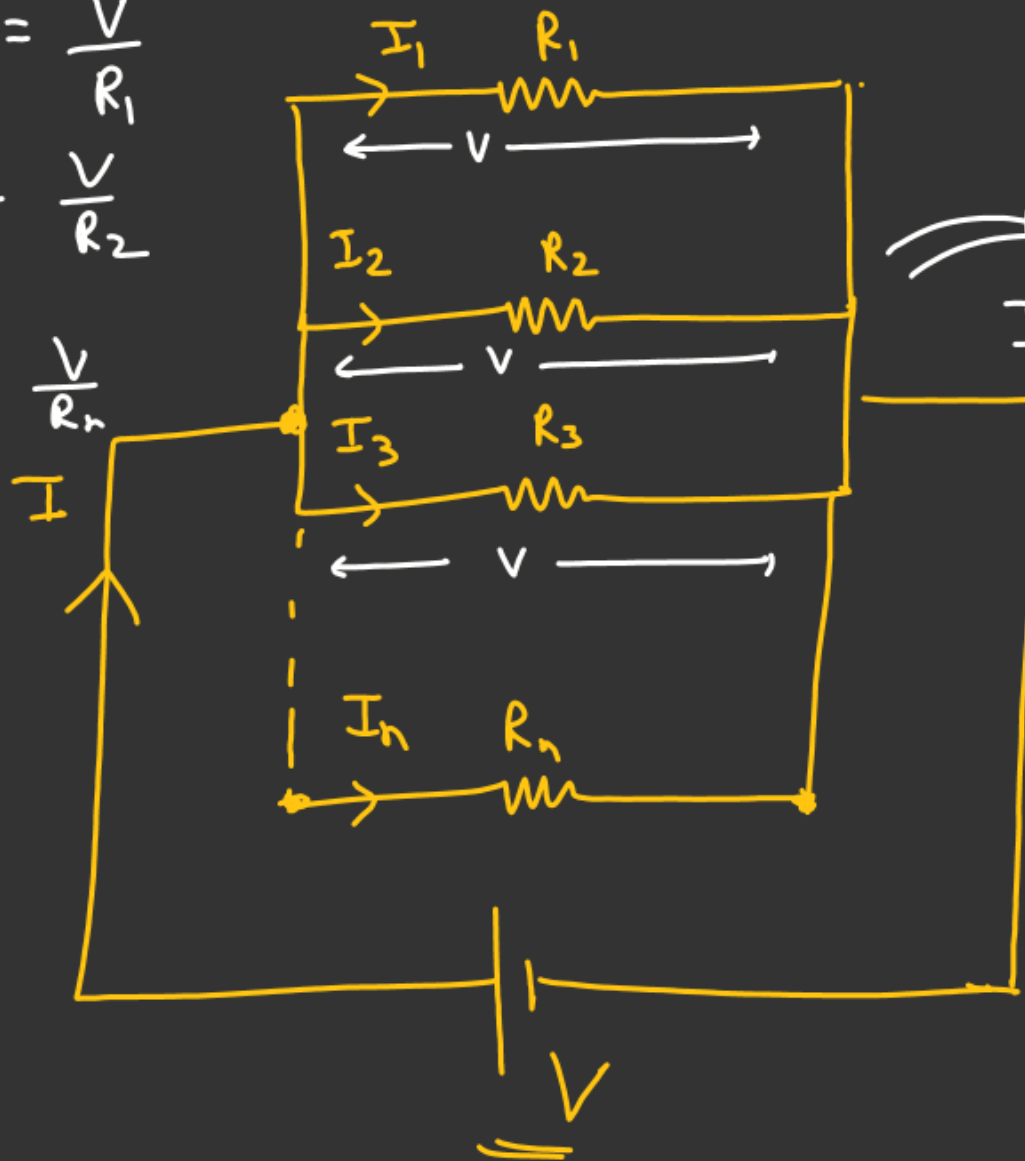
⇒ Potential drop across each Capacitor is Same.

$$I_1 = \frac{V}{R_1}$$

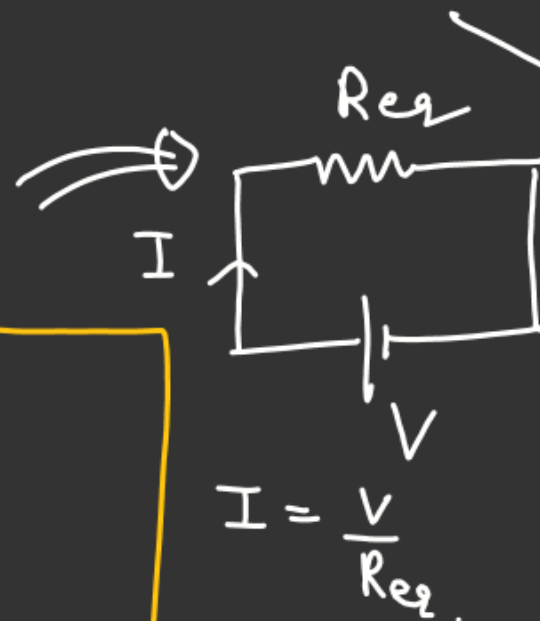
$$I_2 = \frac{V}{R_2}$$

$$\vdots$$

$$I_n = \frac{V}{R_n}$$



$$I = I_1 + I_2 + \dots + I_n$$



$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2} + \dots + \frac{V}{R_n}$$

$$\boxed{\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}} \quad **$$