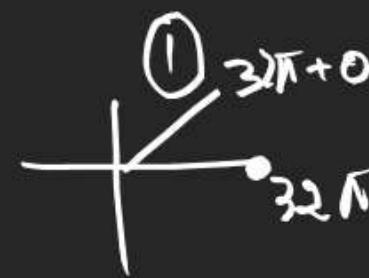


$$\sum \left(\frac{\pi}{2} - \theta \right) = + G_s \theta$$

$$\sin(\pi - \theta) = + \sin \theta$$

~~$$\sin\left(-\frac{7\pi}{2} + \theta\right) = - G_s \theta$$~~

$$\begin{aligned} \sin(32\pi + \theta) \\ = + \sin \theta \end{aligned}$$



$$\underline{\sec} \left(\frac{7\pi}{2} - \theta \right) = -\sec \theta$$



$$\underline{\tan} \left(\frac{7\pi}{2} - \theta \right) = +\cot \theta$$

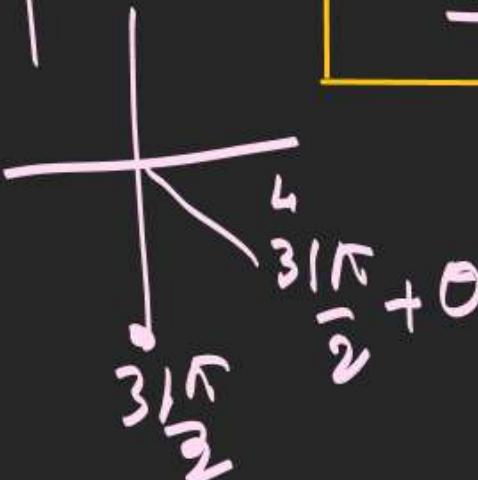
(3)

$$\underline{\sec} \left(31\pi - \theta \right) = +\csc \theta$$



$$\underline{\sec} \left(\frac{3\pi}{2} + \theta \right) = +\csc \theta$$

$$\frac{4\sqrt{31}}{2\sqrt{3}}$$



$$\begin{aligned} \underline{\tan} (\pi + \theta) &= \underline{\tan} \theta \\ &= +\tan \theta \end{aligned}$$

$$\begin{aligned} \underline{\tan} \left(\frac{3\pi}{2} - \theta \right) &= +\cot \theta \\ &= \frac{\cot \theta}{1} \end{aligned}$$

$$\begin{aligned} \underline{\cot} (17\pi + \theta) &= \underline{\cot} \theta \\ &= +\cot \theta \end{aligned}$$

$$\begin{aligned} \underline{\sin} \left(\frac{9\pi}{2} - \theta \right) &= +\sin \theta \\ &= \frac{\sin \theta}{\sqrt{2}} \end{aligned}$$

$$\begin{aligned} \underline{\sin} (3\pi + \theta) &= -\sin \theta \\ &= \frac{-\sin \theta}{\sqrt{2}} \end{aligned}$$

$$\text{Q } \sin(120^\circ) = \sin(90^\circ + 30^\circ)$$

$$= \sin\left(\frac{\pi}{2} + 30^\circ\right)$$

$$= + \underline{\cos 30^\circ}$$

$$= \frac{\sqrt{3}}{2}$$

$$\text{Q } \cos 120^\circ = \cos(90^\circ + 30^\circ)$$

$$= \cos\left(\frac{\pi}{2} + 30^\circ\right)$$

$$= - \sin 30^\circ$$

$$= - \frac{1}{2}$$

$$\text{Q } \tan 120^\circ = \tan(90^\circ + 30^\circ)$$

$$= \tan\left(\frac{\pi}{2} + 30^\circ\right)$$

$$= - \cot 30^\circ$$

$$= - \sqrt{3}$$

$$\text{Q } \cos 150^\circ = \cos(90^\circ + 60^\circ)$$

$$= \cos\left(\frac{\pi}{2} + 60^\circ\right)$$

$$= - \sin 60^\circ$$

$$= - \frac{\sqrt{3}}{2}$$

90°, 180°, 270°, 360°

$$\text{Q} \operatorname{tm} 300^\circ = \operatorname{tm}(360^\circ - 60^\circ)$$

$$\begin{aligned} &= \operatorname{tm}(2\pi - 60^\circ) \\ \frac{s}{t} \mid \begin{array}{c} A \\ T \\ \searrow \\ \angle 4 \\ 2\pi - 60^\circ \end{array} &= - \operatorname{tm} 60^\circ \\ &= -\sqrt{3} \end{aligned}$$

$$\text{Q} \operatorname{sec}(330^\circ)$$

$$\operatorname{sec}(360^\circ - 30^\circ)$$

$$\begin{aligned} &= \operatorname{sec}(2\pi - 30^\circ) \\ &\quad \frac{s}{t} \mid \begin{array}{c} A \\ T \\ \searrow \\ \angle 4 \\ 2\pi - 30^\circ \end{array} \end{aligned}$$

$$\therefore + \operatorname{sec} 30^\circ$$

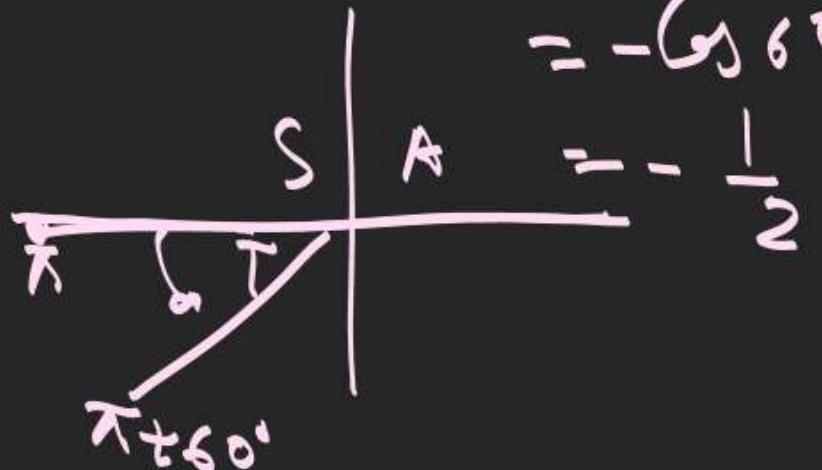
$$= \frac{1}{\cos 30^\circ} = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}}$$

$$Q \underset{\cancel{240^\circ}}{(240^\circ)}$$

$$= \text{cosec}(180^\circ + 60^\circ)$$

$$= \text{cosec}(\pi + 60^\circ)$$

$$= -\text{cosec} 60^\circ$$



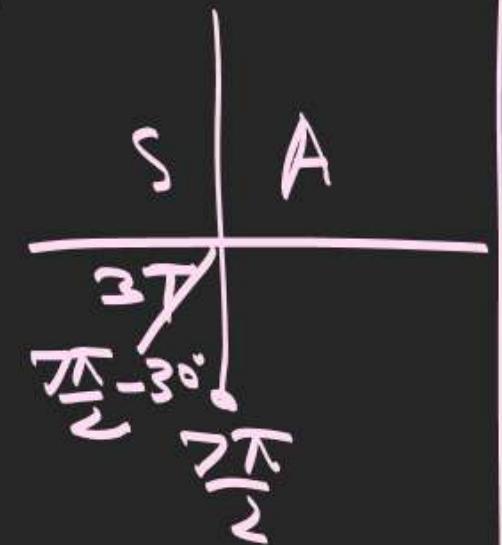
$$Q \underset{\cancel{60^\circ}}{(60^\circ)} \left| \begin{array}{l} \text{cosec}(60^\circ) \\ \text{cosec}(630^\circ - 30^\circ) \end{array} \right.$$

$$\text{cosec}\left(\frac{7\pi}{2} - 30^\circ\right)$$

$$= -\text{cosec} 30^\circ$$

$$= -\frac{1}{\sin 30^\circ}$$

$$= -\frac{1}{\frac{1}{2}} = -2$$



$$90^\circ, 180^\circ, 270^\circ, 310^\circ, 450^\circ, 540^\circ, \underline{630^\circ}$$

$$7 \times 90$$

$$\frac{7\pi}{2}$$

Yed

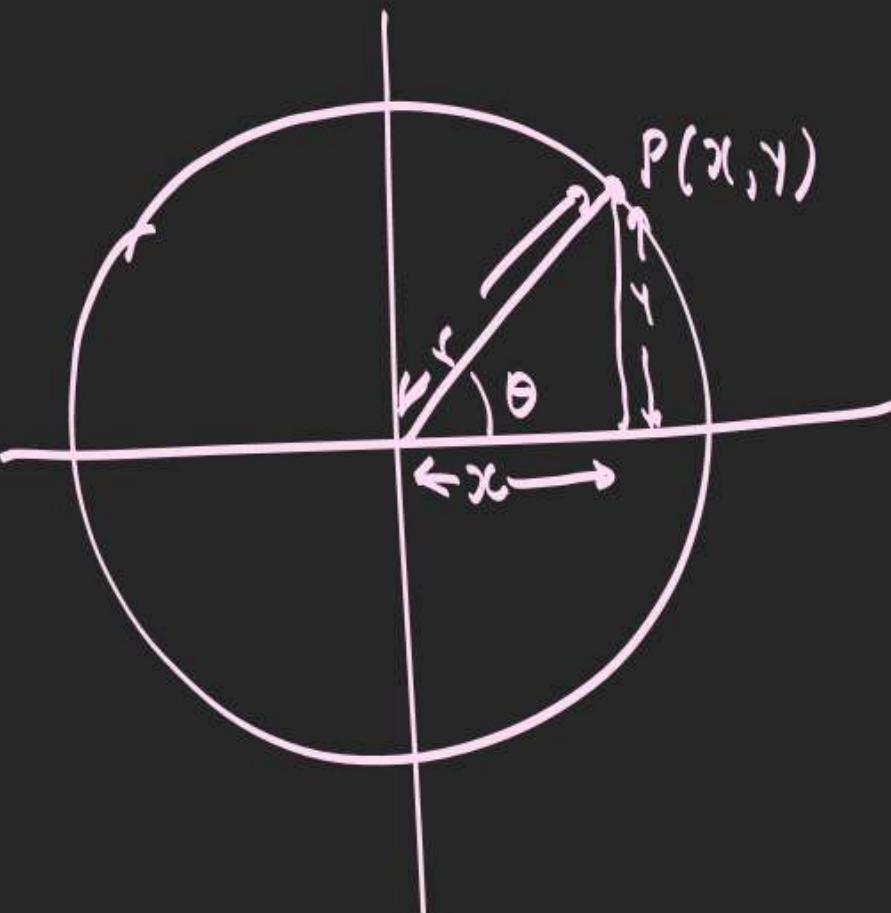
	0°	30°	45°	60°	90°	120°	135°	150°	180°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{\sqrt{3}}{2}$	-1
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞	$-\sqrt{3}$	-1	$-\frac{1}{\sqrt{3}}$	0
$\cot \theta$	∞	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0	$-\frac{1}{\sqrt{3}}$	-1	$-\sqrt{3}$	$-\infty$
$\sec \theta$	∞	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	8
$\csc \theta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	8	$-\frac{2}{\sqrt{3}}$	$-\sqrt{2}$	$-\frac{2}{\sqrt{3}}$	-1

4 8

Actual Definition of $\sin \theta$ & $\cos \theta$

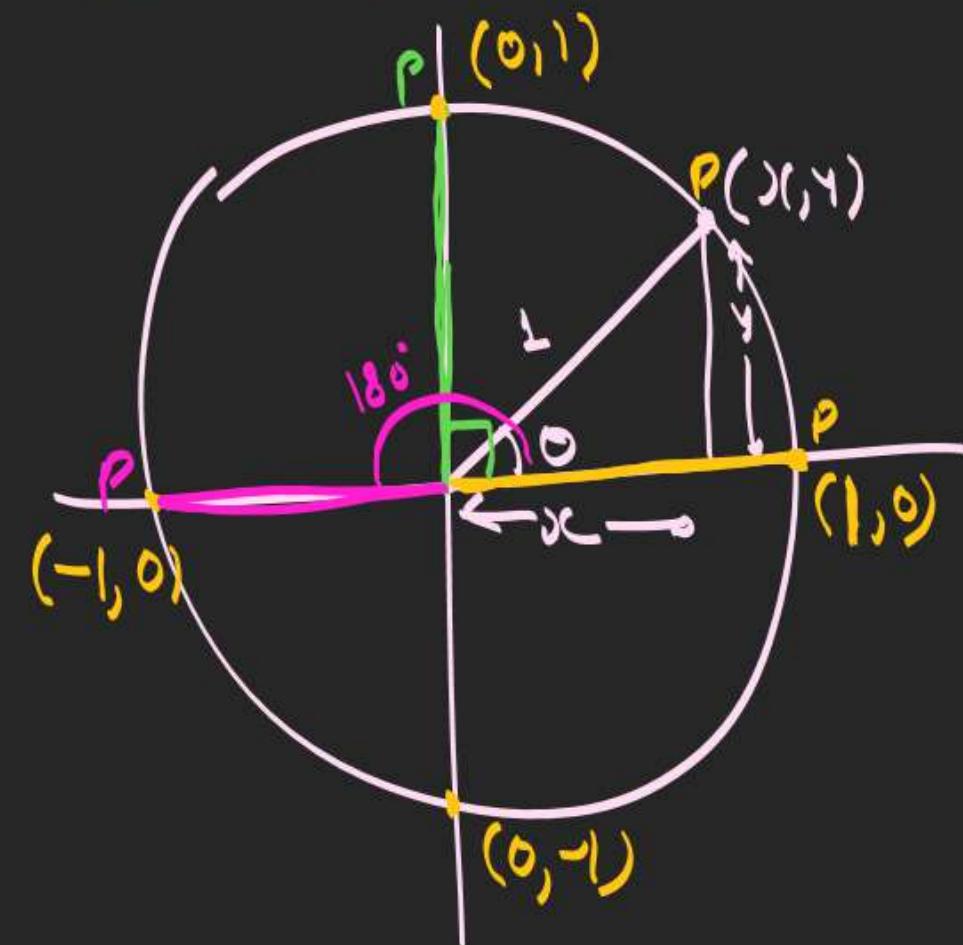
$$\sin \theta = \frac{\text{Ordinate of Pt. } P}{\text{rad.}} = \frac{Y \text{ coord.}}{\text{rad.}}$$

$$\cos \theta = \frac{\text{Abscissa of Pt. } P}{\text{rad.}} = \frac{X \text{ coord.}}{\text{rad.}}$$



When Circle is Unit Circle

Unit Circle is circle with rad=1



$$\sin \theta = \frac{Y \text{ coord}}{\text{radius}} = y$$

$$\cos \theta = \frac{X \text{ coord}}{\text{radius}} = x$$

$$\cos 0^\circ = \frac{1}{1} = 1$$

$$\sin 0^\circ = \frac{0}{1} = 0$$

$$\sin\left(\frac{\pi}{2} - \theta\right) = +\cos \theta \text{ Kyo?}$$

$$\sin\left(\frac{\pi}{2} - \theta\right) = +\sin \theta \text{ Kyo}$$

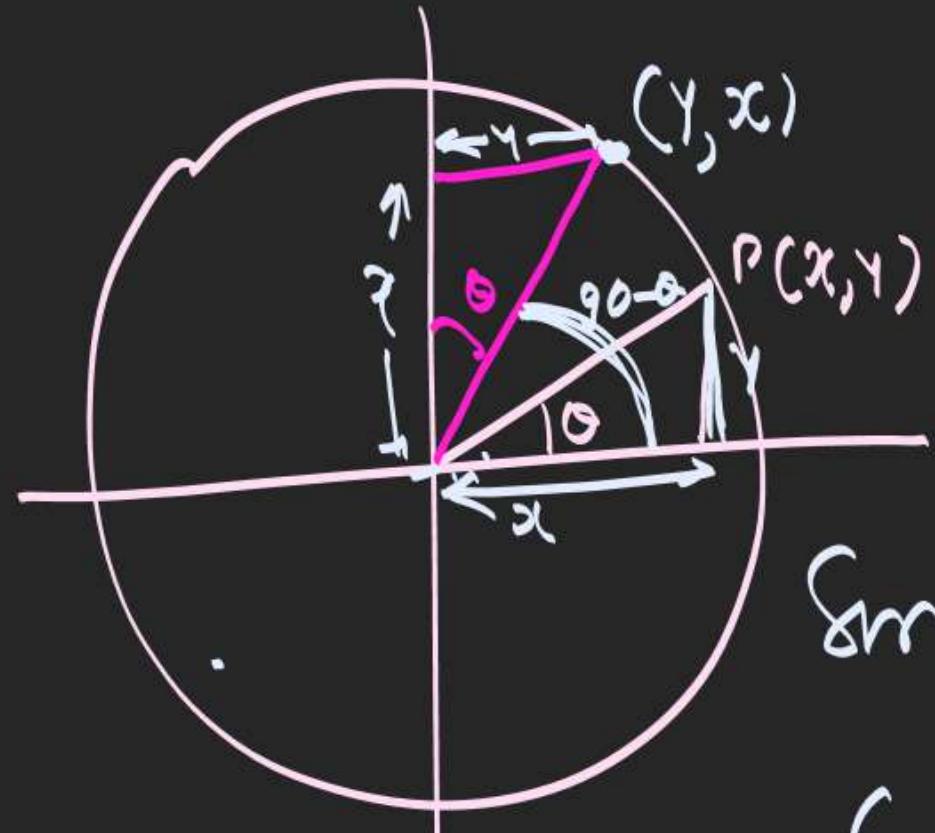
Logic Adv Level

$$\cos 90^\circ = \frac{0}{1} = 0$$

$$\sin 90^\circ = \frac{1}{1} = 1$$

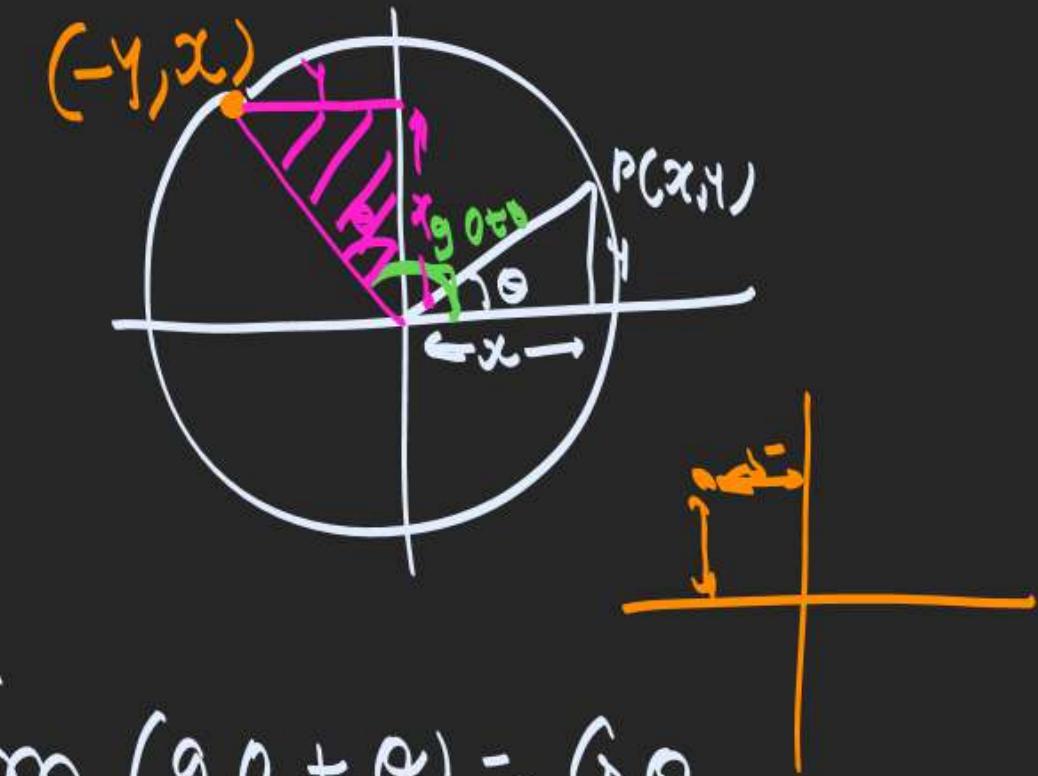
$$\cos 180^\circ = \frac{-1}{1} = -1$$

$$\sin 180^\circ = \frac{0}{1} = 0$$



$$\sin(90 - \theta) = \frac{y}{r} = \cos\theta$$

$$\cos(90 - \theta) = \frac{x}{r} = \sin\theta$$

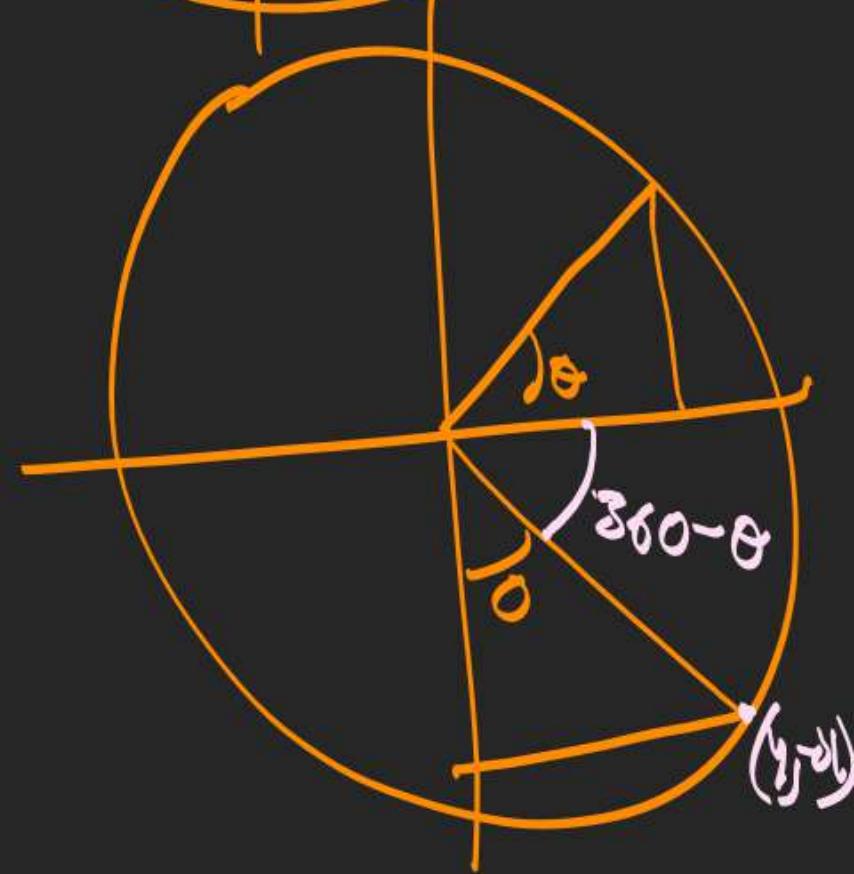
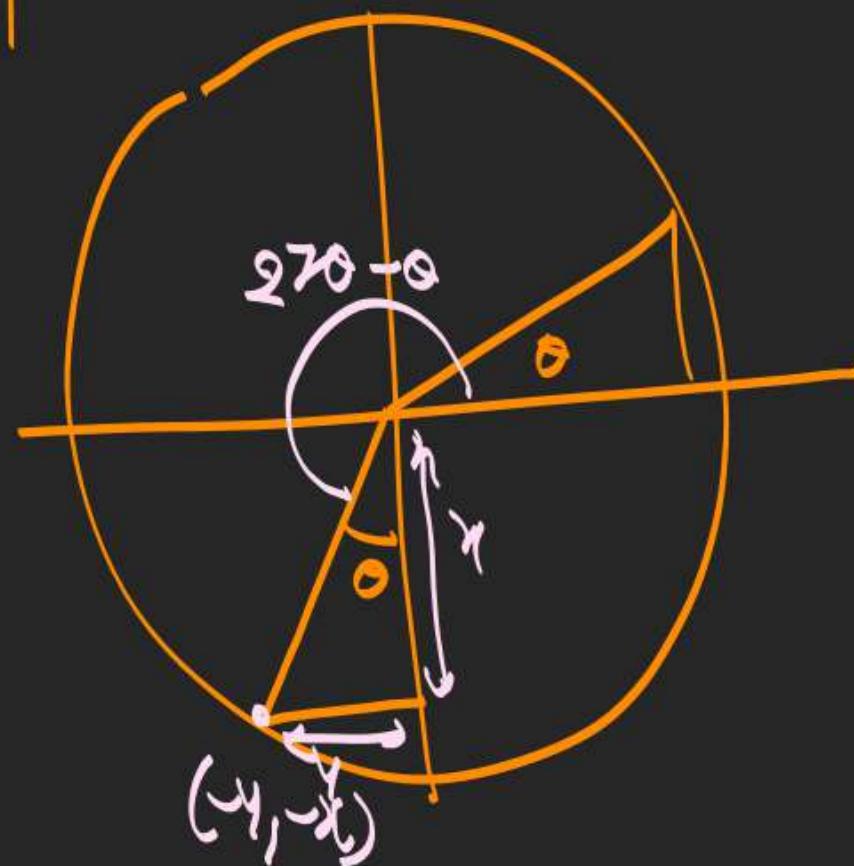
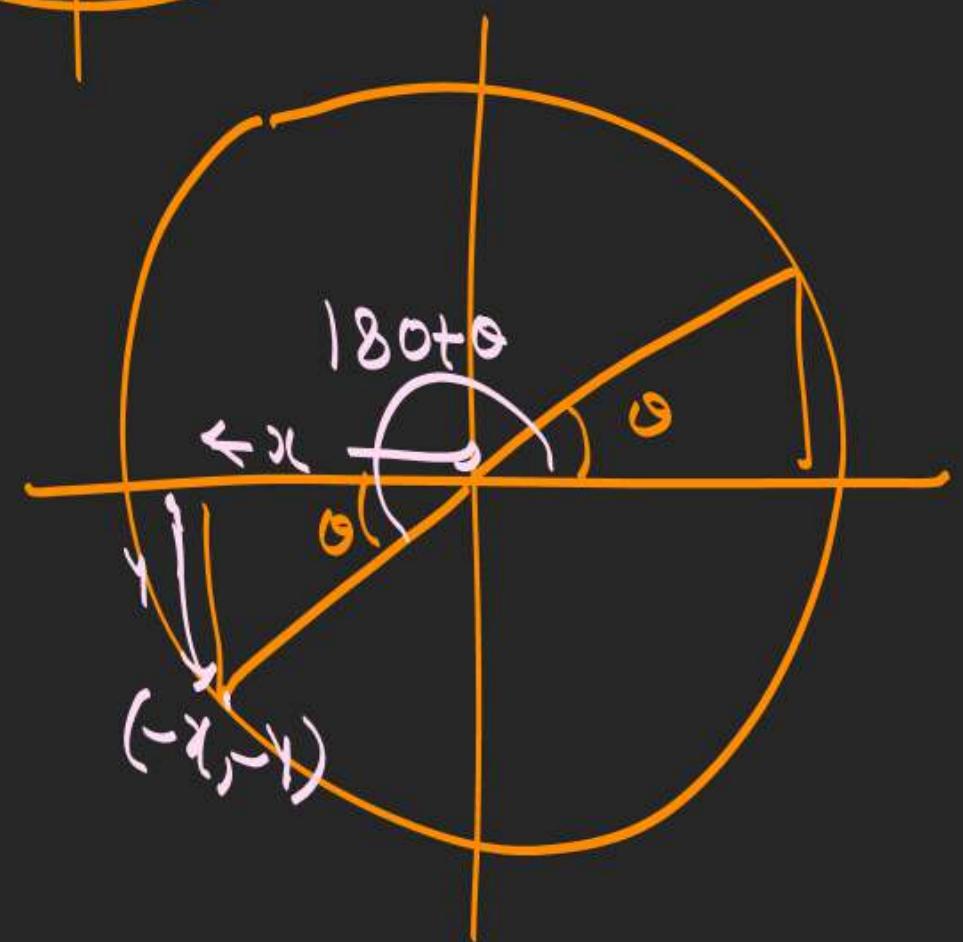
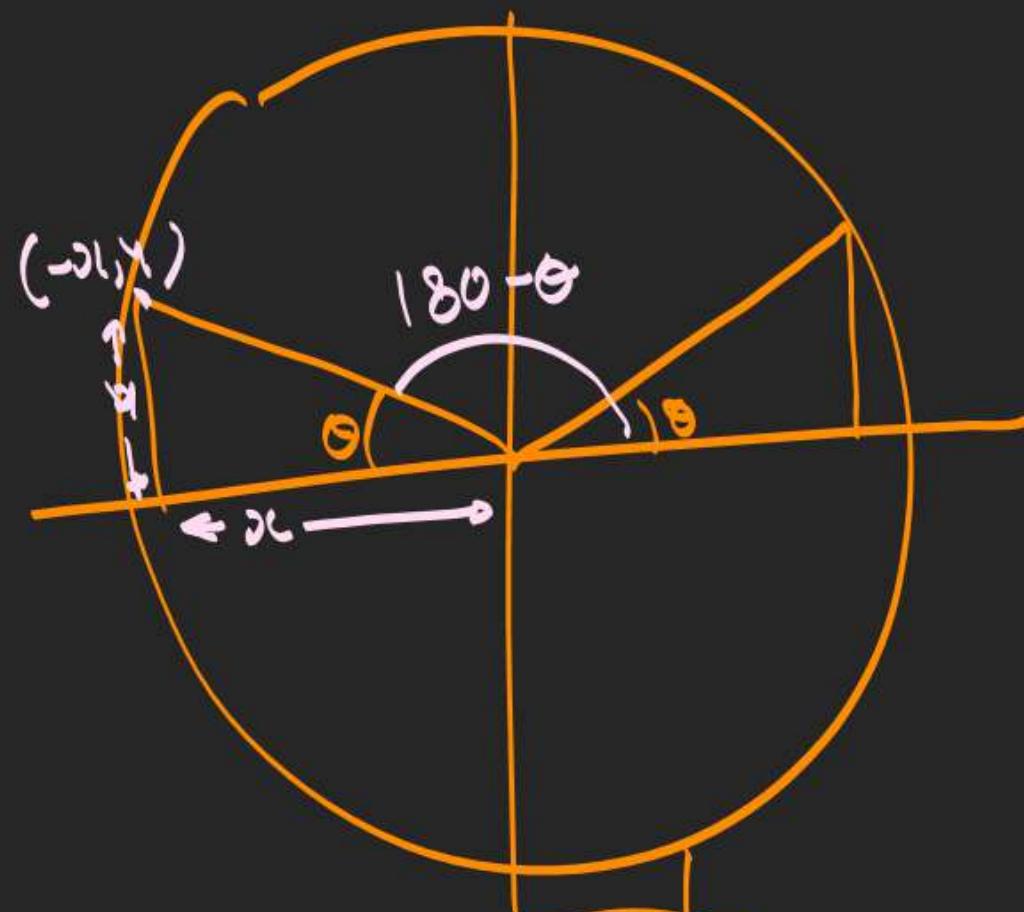
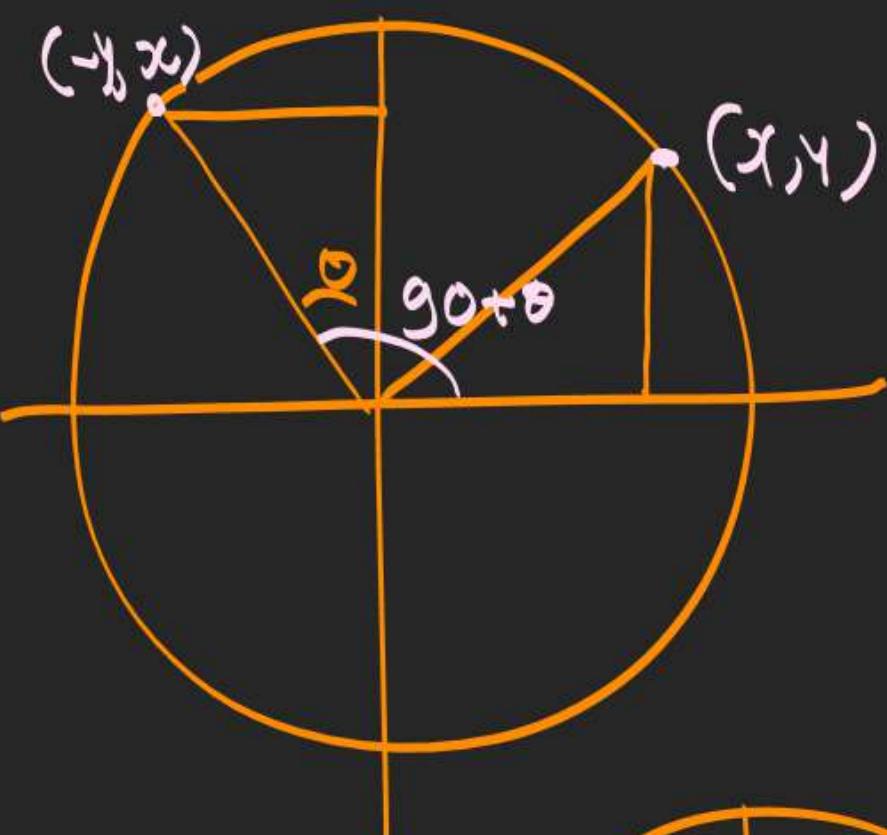
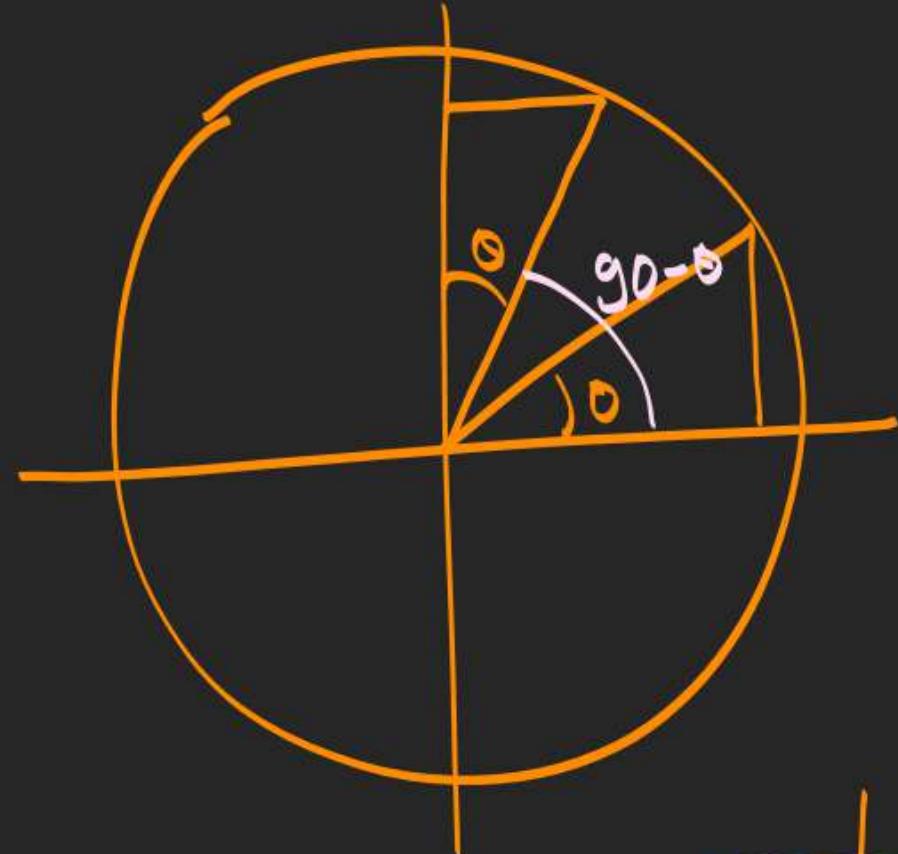


$$\sin(90 + \theta) = \frac{y}{r} = \cos\theta$$

$$\cos(90 + \theta) = \frac{x}{r} = -\sin\theta$$

$$\sin(90 + \theta) = \frac{y(\text{opp})}{r} = \frac{y}{r} = \cos\theta$$

$$\cos(90 + \theta) = \frac{x(\text{opp})}{r} = \frac{-x}{r} = -\sin\theta$$





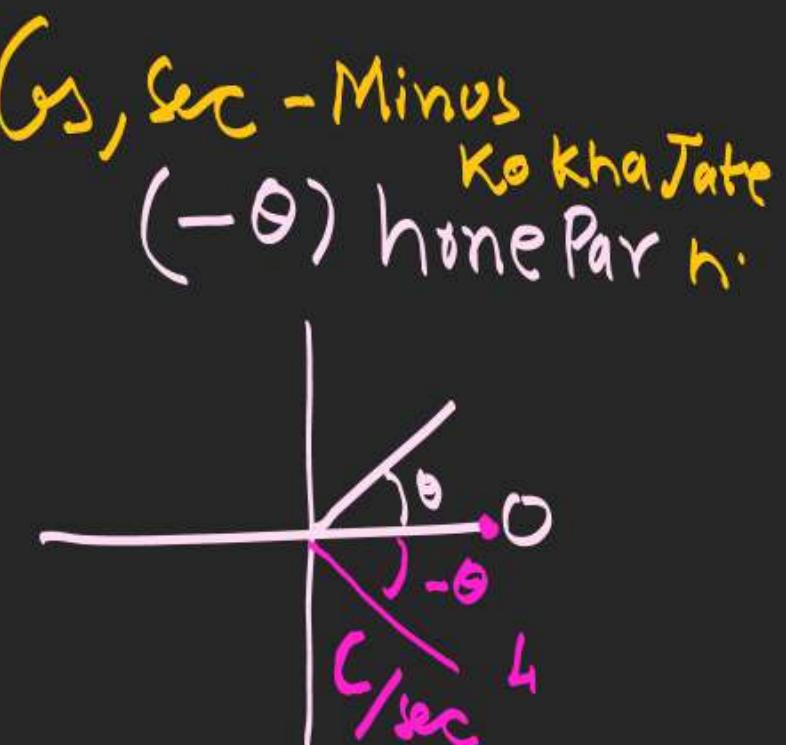
$$\sin\left(\frac{31\pi}{2} + \theta\right) \cdot \csc\left(13\pi + \theta\right) \cdot \tan\left(\frac{13}{2}\pi - \theta\right) \cdot \cot\left(\theta - \frac{57\pi}{2}\right)$$

$$\sin\left(\frac{37\pi}{2} + \theta\right) \csc\left(13\pi + \theta\right) \tan\left(13\pi - \theta\right) \{-\cot\left(\frac{57\pi}{2} - \theta\right)\}$$

$$(+\csc\theta) (-\csc\theta) (+\tan\theta) \{+(-\tan\theta)\}$$

$$-\csc^2\theta \times \tan^2\theta$$

~~$$-\csc^2\theta \times \frac{\sin^2\theta}{\csc^2\theta} = -\sin^2\theta$$~~



$$\sin(-\theta) = \sin(0 - \theta)$$

$$= -\sin\theta$$

$$\csc(-\theta) = +\csc\theta$$

$$\sec(-\theta) = -\sec\theta$$

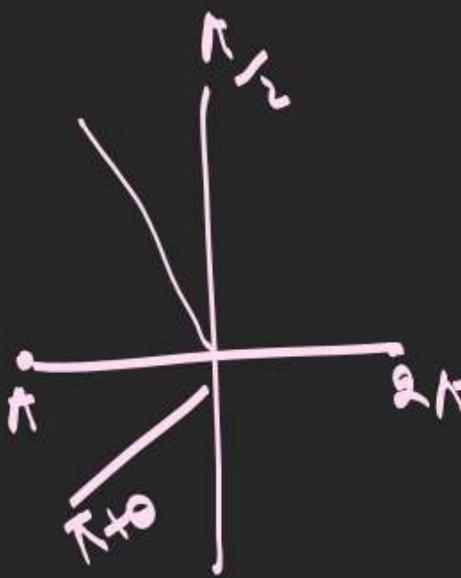
$$\cot(-\theta) = -\cot\theta$$

$$\tan(-\theta) = +\tan\theta$$

$$\varphi = \sin(x - \frac{\pi}{2}) \cdot (\cos(\frac{3\pi}{2} + x), \sin^3(\frac{\pi}{2} - x))$$

$$\begin{aligned} & \frac{\sin(x - \frac{\pi}{2}) \cdot (\cos(\frac{3\pi}{2} + x), \sin^3(\frac{\pi}{2} - x))}{\sin(x - \frac{\pi}{2}) \cdot \sin(\frac{3\pi}{2} + x)} = ? \\ & \frac{\sin(-(\frac{\pi}{2} - x)) \cos(\frac{3\pi}{2} + x) (\sin(\frac{7\pi}{2} - x))^3}{\sin(+(\frac{\pi}{2} - x)) \sin(\frac{3\pi}{2} + x)} \\ & + \frac{(\cancel{+ \sin x}) (\cancel{+ \sin x}) (\cancel{+ \sin x})^3}{(\cancel{+ \sin x}) (\cancel{- \sin x})} = -\cos^3 x \end{aligned}$$

$$\text{Q} \quad \frac{\operatorname{cosec}(90+\theta) \sec(-\theta) \tan(180+\theta)}{\sec(360-\theta) \sin(180+\theta) \cot(90-\theta)} = ?$$



$$\frac{\operatorname{cosec}(\frac{\pi}{2}+\theta) \cdot \sec \theta \cdot \tan(\pi+\theta)}{\sec(2\pi-\theta) \sin(\pi+\theta) \cot(\frac{\pi}{2}-\theta)}$$

$$\frac{(+\operatorname{cosec}\theta) \sec\theta \times (+\tan\theta)}{(+\sec\theta) (-\sin\theta) (+\cot\theta)} = 1$$

$$\frac{-\operatorname{cosec}\theta \sec\theta + \tan\theta}{\sec\theta - \sin\theta \tan\theta} = 1$$

$$Q \quad \sin(-65^\circ) = -\sin 65^\circ$$

$$Q \quad \cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$$

$$\cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 27^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$$

$$\begin{aligned} & \frac{\sin(90-63^\circ)}{\cos 63^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\sec 63^\circ} \\ & + \cos 63^\circ \times \frac{1}{\sec 63^\circ} = 1 \end{aligned}$$

P.T.

$$\begin{cases} Q \quad \tan \theta + \tan(\pi - \theta) + \cot\left(\frac{\pi}{2} + \theta\right) - \tan(2\pi - \theta) \\ = 0 \end{cases}$$

$$Q. \quad \frac{\tan(90+\theta) \cdot \cot(180+\theta)}{\cos(180+\theta) \cdot \cot(-\theta)} = -1$$

$$Q. \quad \frac{\cos \theta}{\sin(90+\theta)} + \frac{\sin(-\theta)}{\sin(180+\theta)} - \frac{\tan(90+\theta)}{\cot \theta} = 3$$

$$Q. \quad \frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ} = 3 + 2\sqrt{2}$$

$$Q \ 4(\cot^2 45^\circ - \sec^2 60^\circ + \csc^2 30^\circ) = \frac{1}{4}$$

$$Q \ \tan^2 \frac{\pi}{6} + \tan^2 \frac{\pi}{4} + \tan^2 \frac{\pi}{3} = \frac{13}{3}.$$