

$$C_r = \boxed{\begin{matrix} S_3 & S_1 & S_6 & S_7 & S_5 \\ S_1 & S_3 & S_5 & S_6 & S_7 \end{matrix}}$$

Arrange persons in r seats n $0 \leq r \leq n$

$$\frac{P_1 P_2 \cdots P_r}{P_1 P_2 \cdots P_n} \cdot r!$$

$$\frac{P_1 P_2 \cdots P_r}{P_1 P_2 \cdots P_{r+1}} \rightarrow r!$$

$$P_r =$$

30 students
↓
select S

$$\text{arrange 30 students in chains} \rightarrow 30P_5 = \frac{30!}{25!}$$

$$= 30C_5 \cdot 5!$$

$$= 30C_5 = \frac{30!}{25!5!} = \frac{30 \times 29 \times 28 \times 27 \times 26}{5!}$$

$$= 30 \times 29 \times 28 \times 27 \times 26 \times 25 \times 24 \times 23 \times 22 \times 21 \times 20 \times 19 \times 18 \times 17 \times 16 \times 15 \times 14 \times 13 \times 12 \times 11 \times 10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2$$

$$nC_r = \frac{nPr}{r!} = \frac{n!}{(n-r)!r!}$$

$$\binom{n}{r} = \binom{n}{n-r} \rightarrow \text{Pascal's mirror formula}$$

$\frac{n!}{(n-r)!(n-(n-r))!} = \frac{n!}{(n-r)!r!}$

$$\binom{n}{r} = \binom{n-1}{r} + \binom{n-1}{r-1} \rightarrow \text{Pascal's triangle formula}$$

$$r \binom{n}{r} = n \binom{n-1}{r-1}$$

$$\frac{\binom{n}{r}}{r+1} = \frac{\binom{n+1}{r+1}}{n+1}$$

r objects
 n
 n-r

Select 'r' persons out of 'n' given persons.

$$0 \leq r \leq n$$

$$= {}^n C_r$$

$$P_1 P_2 P_3 \dots P_n$$

$= P_1$ is present in the selection + P_1 is not present
in selection.

$$= 1 \times {}^{n-1} C_{r-1} + {}^{n-1} C_r$$

↓
 select P_1 ↓
 select $r-1$ persons

P.T.

$${}^n P_r = {}^{n-1} P_{r-1} + {}^{n-1} P_r$$

arranging n person
in r seats = P_1 is there + P_1 is not there

$$= \cancel{x} \times {}^{n-1} P_{r-1} + {}^{n-1} P_r$$

arrange P_1
arranging remaining persons

— . . P_1 . . —

$${}^n C_r = n {}^{n-1} C_{r-1}$$

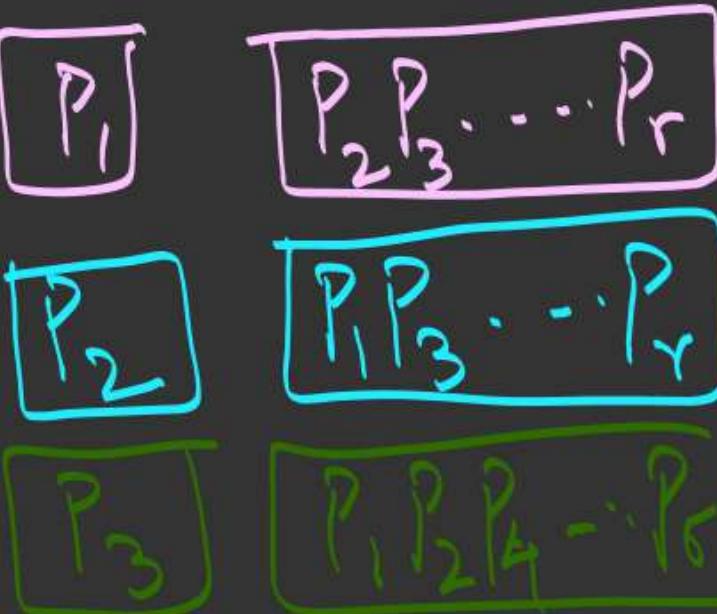
Select 'r' person out of 'n' persons

$$= {}^n C_r$$

$$= \cancel{n} \times {}^{n-1} C_{r-1}$$

Select 1st person

*Selecting remaining
persons*



$$\therefore \textcircled{2} {}^{10}C_3 - {}^4C_3 \text{ or } 0 + {}^4C_2 \times {}^6C_1 + {}^4C_1 \times {}^6C_2 + {}^6C_3 \quad \left(\text{no 3 are collinear} \right)$$

$$\text{Find no. of } \textcircled{3} {}^{10}C_4 - \left({}^4C_4 + {}^4C_3 \times {}^6C_1 \right)$$

$\textcircled{1}$ no. of straight lines ${}^4C_2 \times {}^6C_2 + {}^4C_1 \times {}^6C_3 + {}^6C_4$

$\textcircled{2}$ triangles
using 4 collinear points

$\textcircled{3}$ quadrilaterals

using these points.

$$\begin{aligned} & {}^{10}C_2 - {}^4C_2 + 1 \\ & 1 + {}^4C_1 \times {}^6C_1 + {}^6C_2 \\ & \frac{10!}{8!2!} - \frac{4!}{2!2!} + 1 \end{aligned}$$

$$= \frac{10 \times 9}{2 \times 1} - \frac{4 \times 3}{2 \times 1} + 1$$

$$= 45 - 6 + 1$$

$\boxed{40}$

Match the Columns (St. line) + Test (1-20)

