

Ideal Gas



1 atm - x $\frac{3x}{2}$ x

= 0.8

0.3

0.2

= 1.3 atm

0.3 x 76 cm

$\frac{r_A}{r_B}$

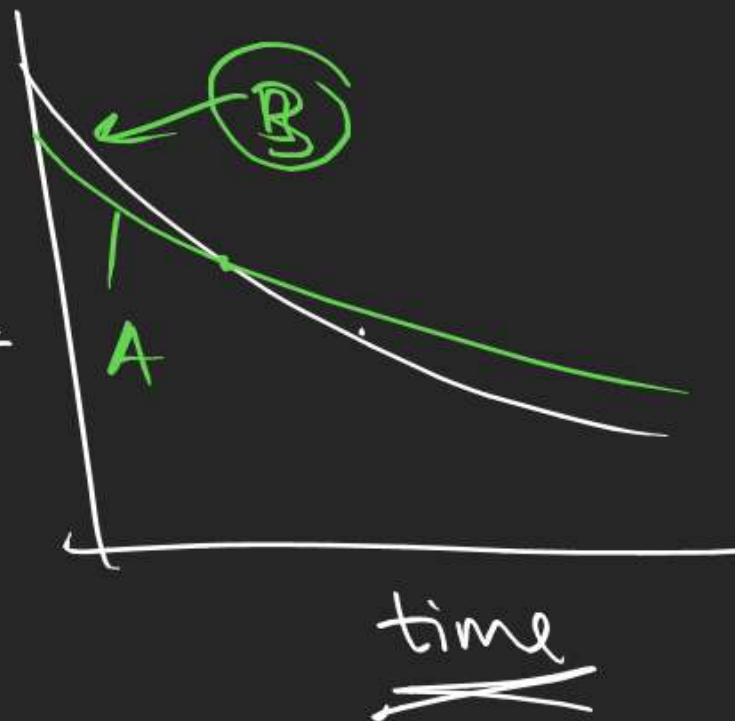
$\frac{r_A}{r_B}$

④

$M_A > M_B$



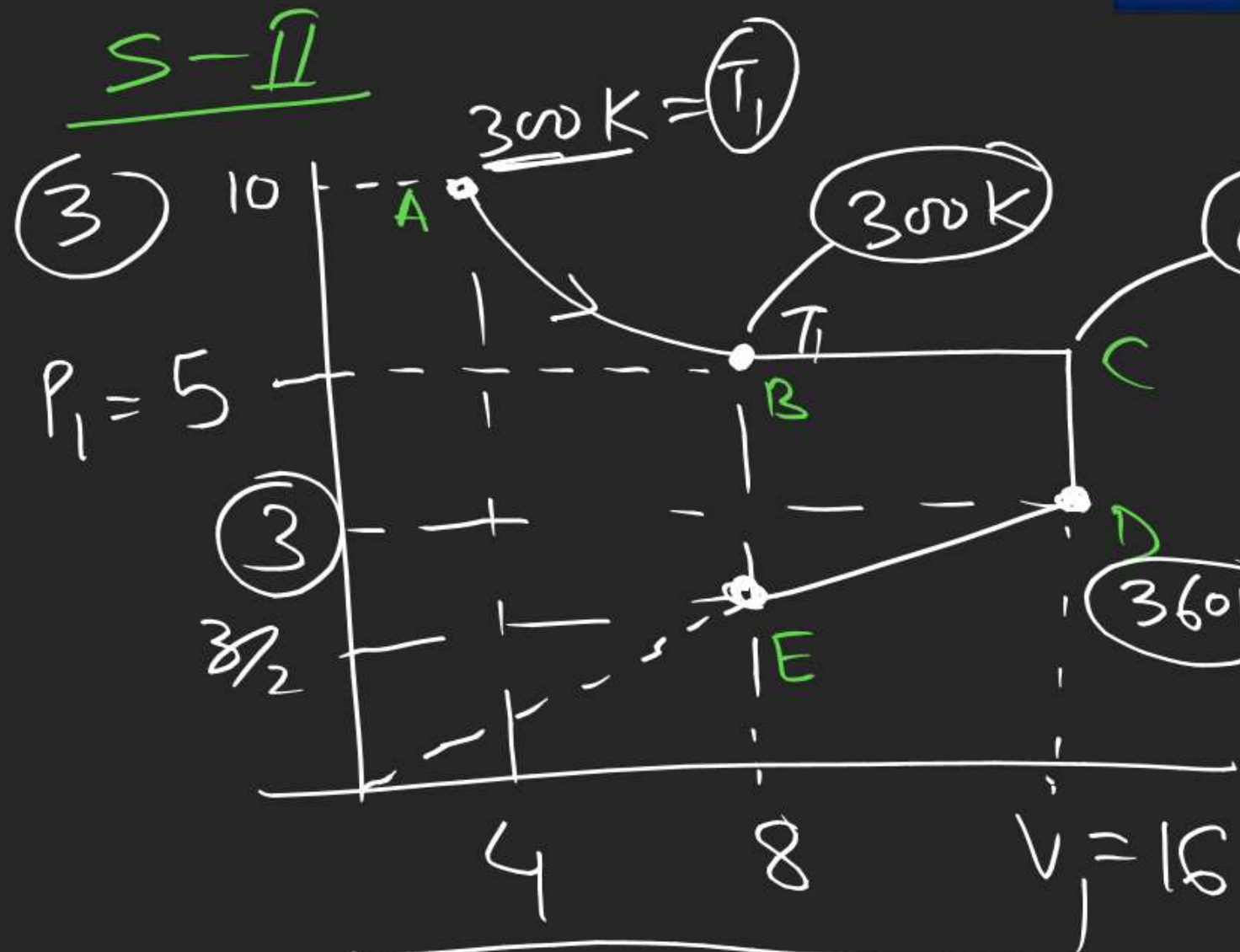
rate



$n_t = n_0 e^{-ct}$

$-\frac{dn_t}{dt} = n_0 c e^{-ct}$

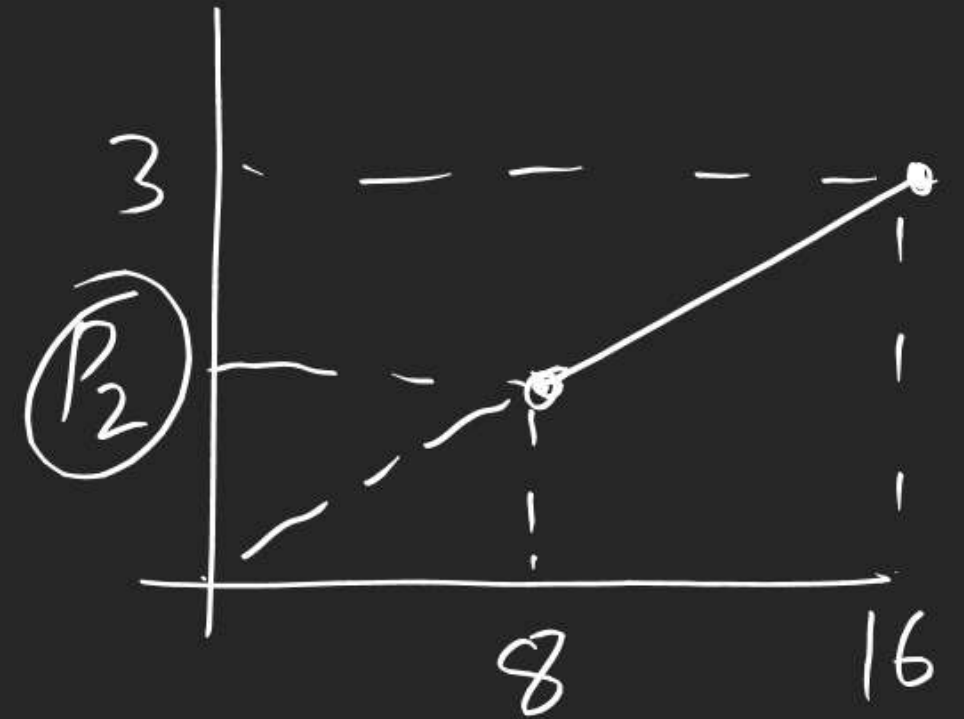
Ideal Gas



$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$\frac{5}{600} = \frac{3}{T}$$

$$T = 360$$



$$P = mV$$

$$\frac{P_1}{P_2} = \frac{V_1}{V_2}$$

$$P \propto V$$

$$\frac{P_1}{V_1} = \frac{P_2}{V_2}$$

$$\frac{3}{16} = \frac{P_2}{8}$$

Ideal Gas

$$P \propto d$$

$$P = k d$$

$$1 = k \cdot 1$$

$$P = d$$

$$\frac{4}{3} \pi \left(\frac{d}{2}\right)^3$$

$$= \frac{1}{6} \pi d^3$$

$$\frac{P_1 V_1}{n_1} = \frac{P_2 V_2}{n_2}$$

$$\frac{1 \times \cancel{\frac{4}{3}} \pi \times 1}{1} = \frac{3 \times \cancel{\frac{4}{3}} \pi \times 3^3}{n_2}$$

$$n_2 = 81$$

$$36\pi = \frac{1}{6} \pi d^3$$

$$\underline{\underline{6 = d}}$$

Ideal Gas

⑤



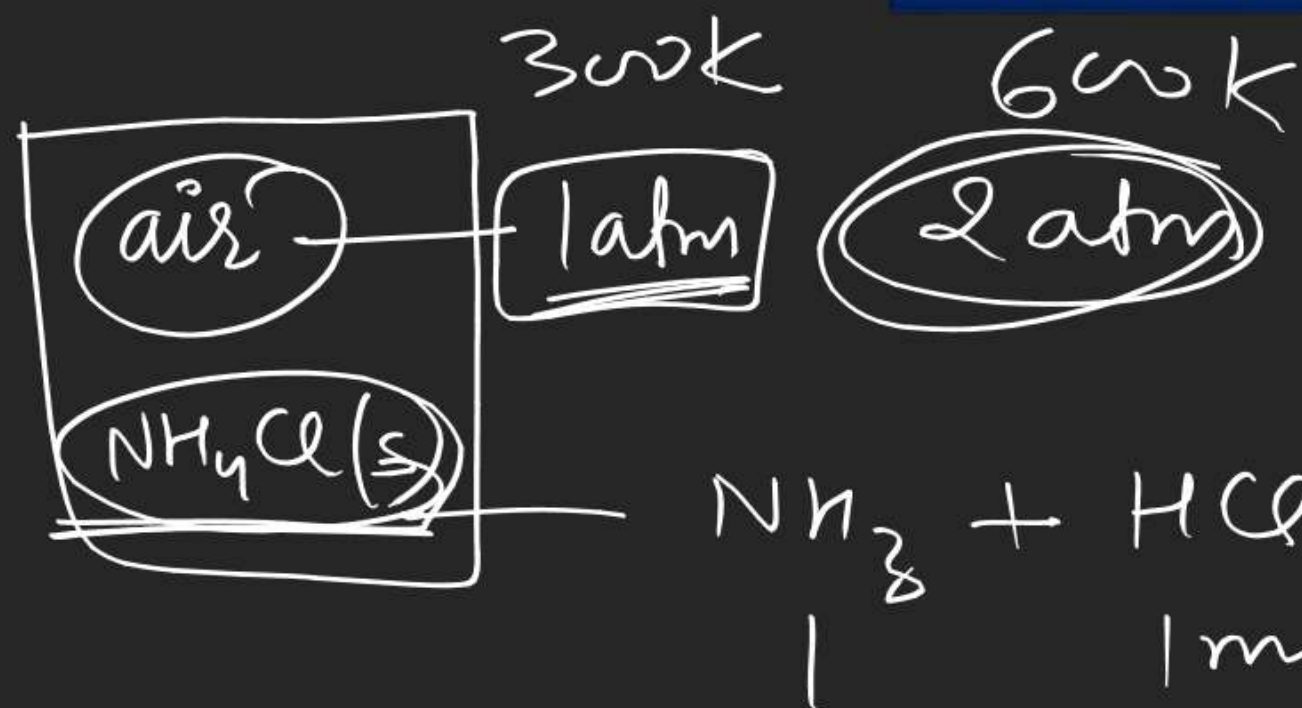
$$M_{\text{avg}} = \frac{71}{1+\alpha}$$

$$\frac{\gamma_{\text{mix}}}{\gamma_{\text{kr}}} = 1.16 = \sqrt{\frac{84}{M_{\text{mix}}}}$$

$$M_{\text{mix}} = M_{\text{avg}} = \underline{\underline{62.4}}$$

Ideal Gas

⑥



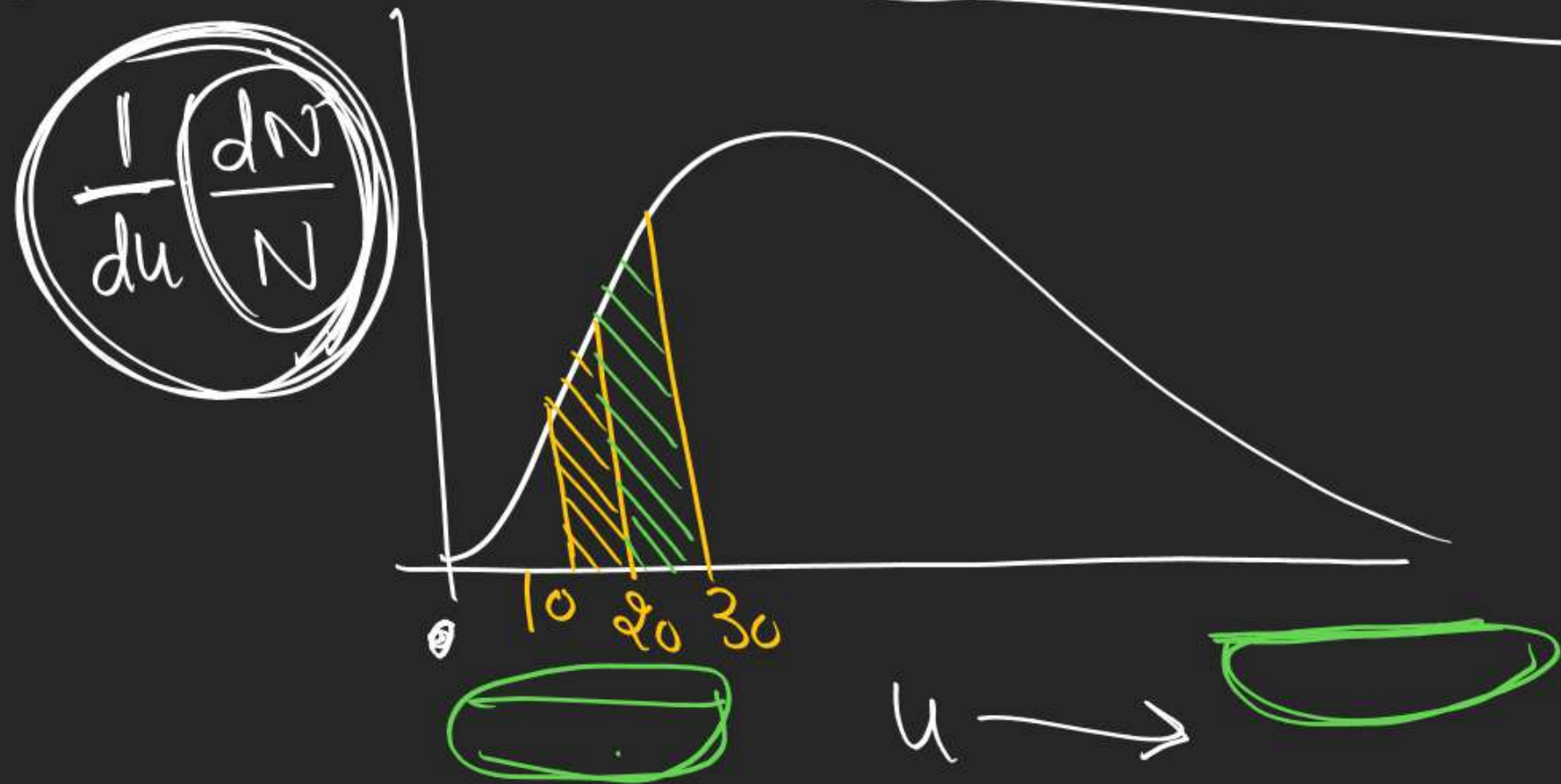
$$P = \frac{2 \times 0.0821 \times 300 \times 2}{24.63}$$

$$= 4\text{ atm}$$



$$dN = 4\pi N \left(\frac{M}{2\pi RT} \right)^{3/2} e^{-Mu^2/2RT} u^2 du$$

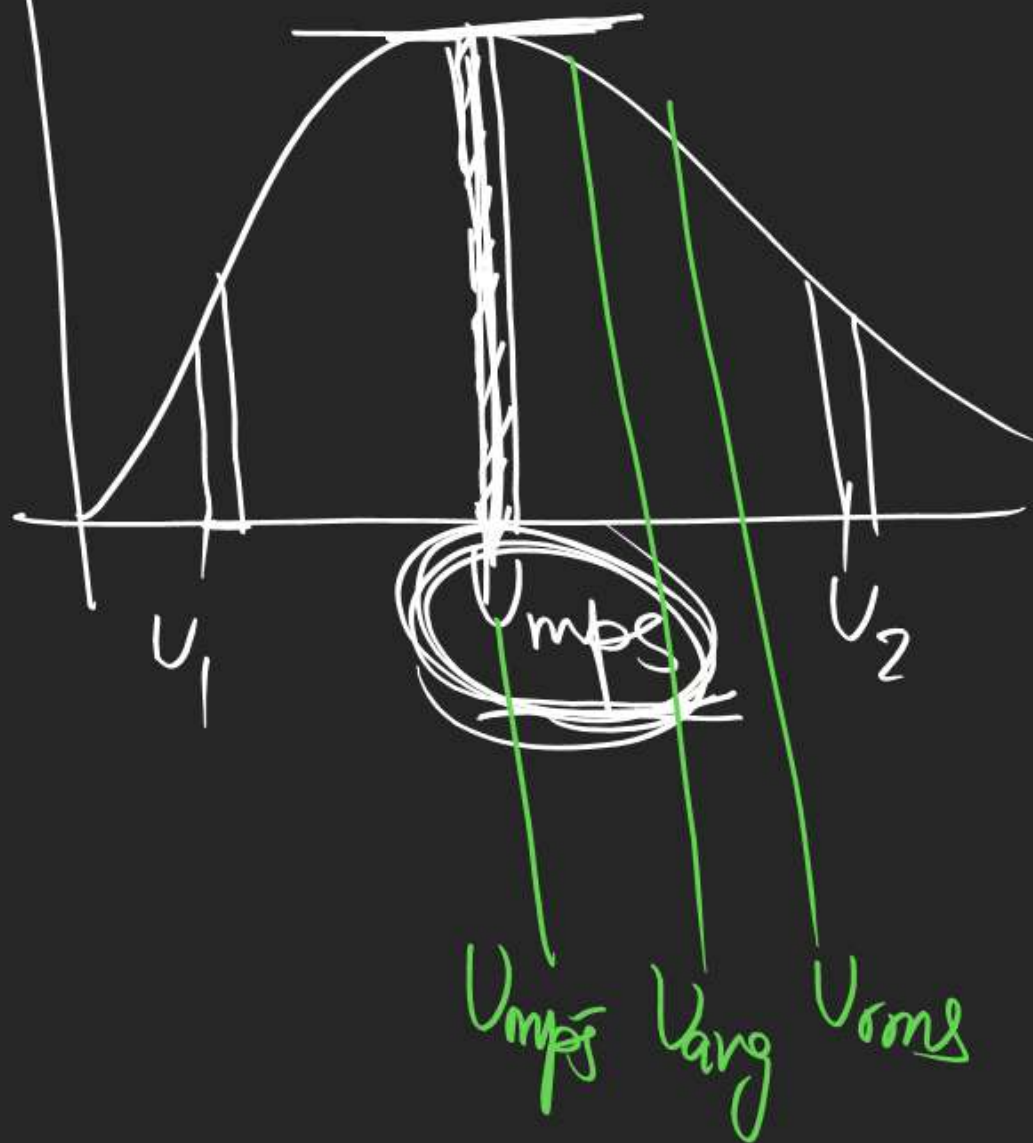
$$\frac{1}{du} \left(\frac{dN}{N} \right) = 4\pi \left(\frac{M}{2\pi RT} \right)^{3/2} e^{-Mu^2/2RT} u^2$$



$$\begin{aligned} \textcircled{1} \text{ Area} &= \int y \, dx \\ &= \int \frac{1}{du} \cdot \frac{dN}{N} \cdot du \\ &= \int \frac{dN}{N} \\ &= \text{fraction of particles} \end{aligned}$$

② Total Area = $\int_0^{\infty} \frac{dN}{N} = 1$

③



u_{mps} = most probable speed

$$Y = C e^{-Mu^2/2RT} \cdot \underline{u^2}$$

$$\frac{dy}{du} = 0$$

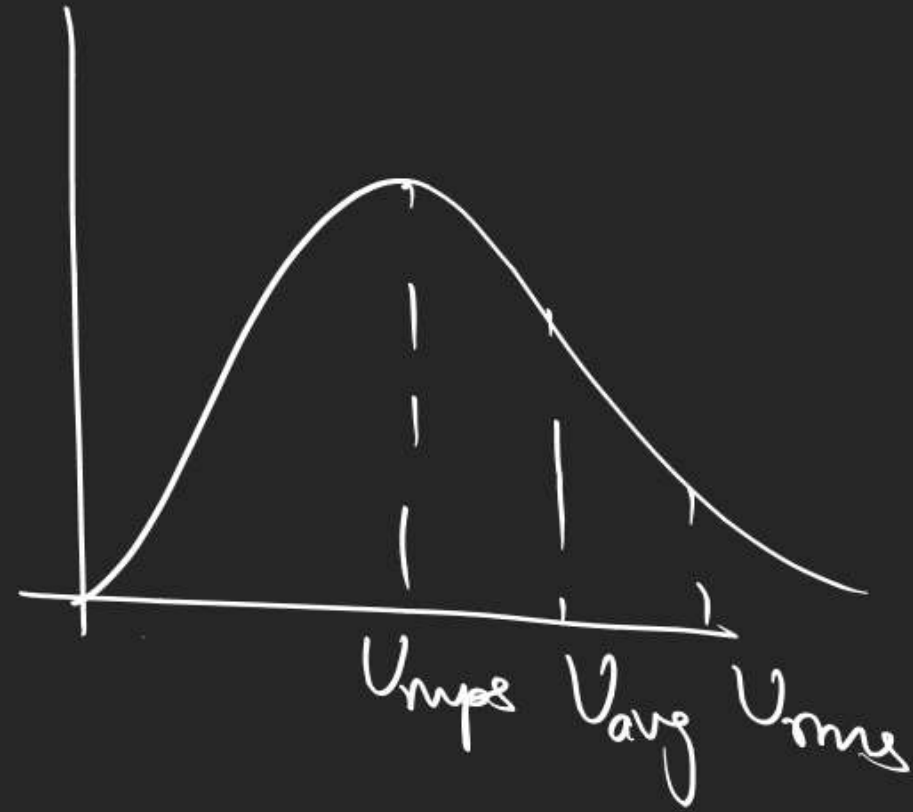
$$u_{mps} = \sqrt{\frac{2RT}{M}}$$

(4)

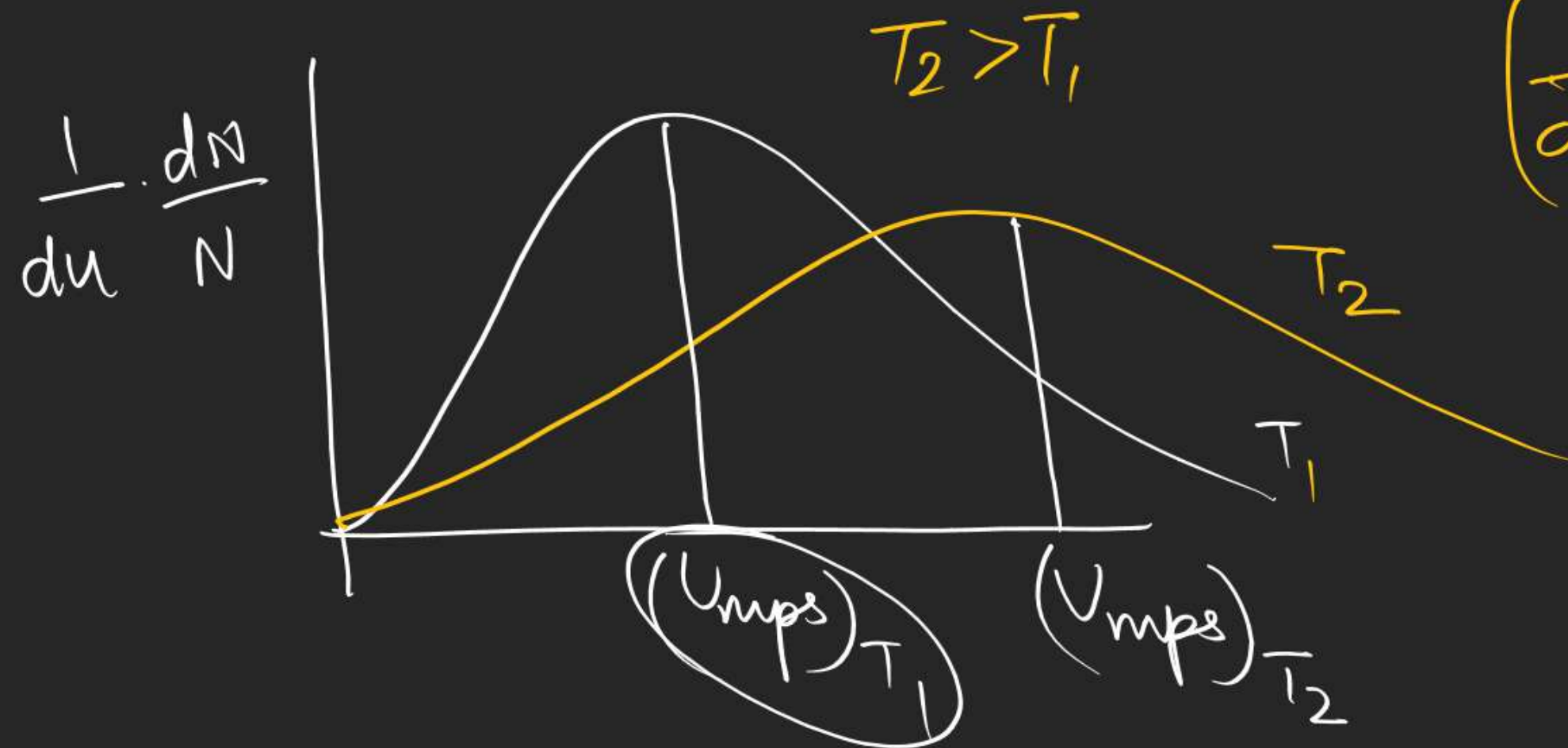
$$U_{rms} : U_{avg} : U_{rms}$$

$$\sqrt{2} : \sqrt{\frac{8}{\pi}} : \sqrt{3}$$

$$1 : \sqrt{\frac{4}{\pi}} : \sqrt{\frac{3}{2}}$$



⑤ Variation with Temperature

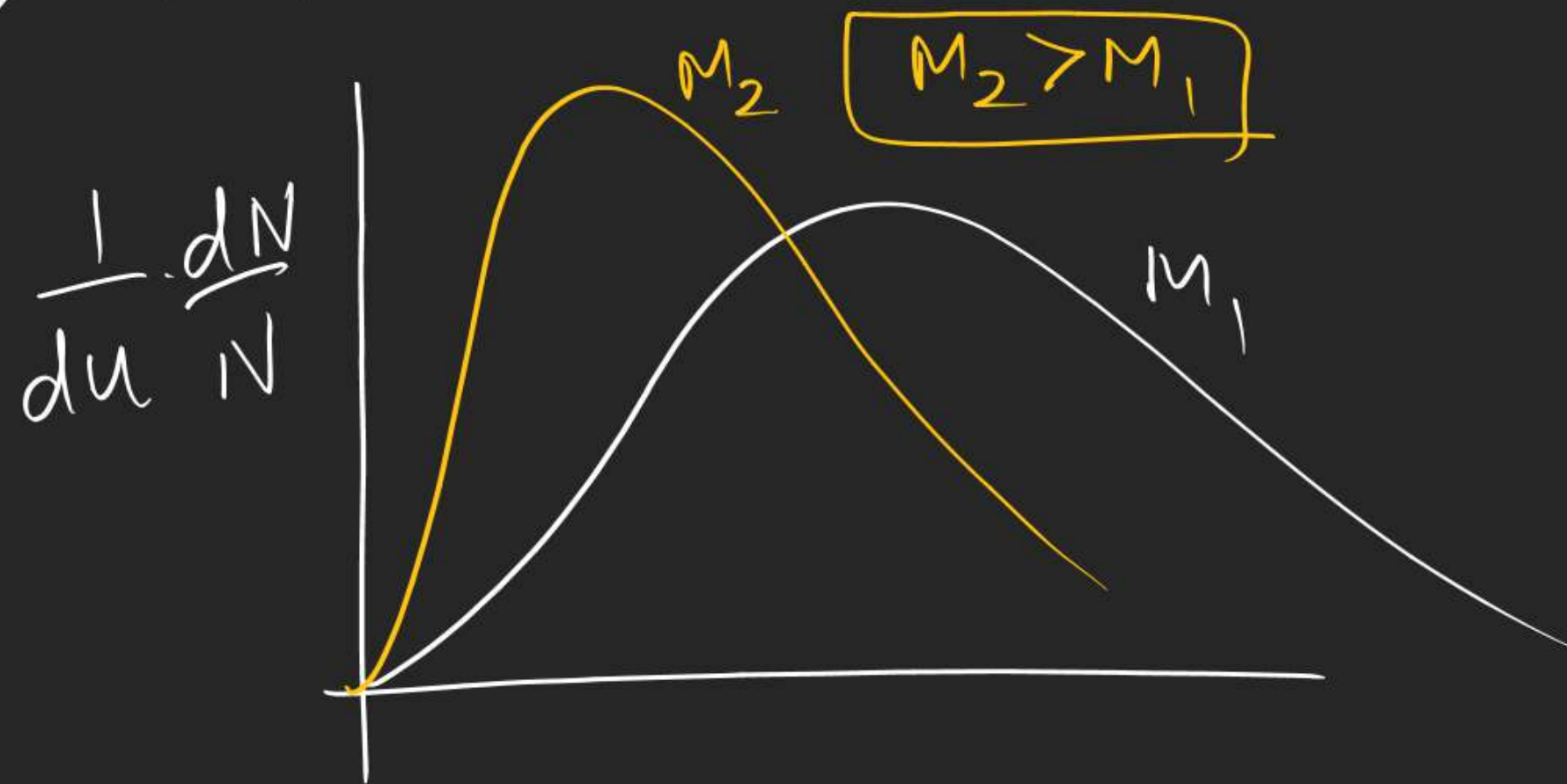


$$\left(\frac{1}{du} \frac{dN}{N} \right) = \underbrace{4\pi \left(\frac{M}{2\pi RT} \right) u^2}_{1^{st}} \underbrace{e^{-Mu^2/2RT}}_{2^{nd}}$$

$$u_{mps} = \sqrt{\frac{2RT}{M}}$$

as $T \uparrow$ $u_{mps} \uparrow$ but fractional of particles moving with u_{mps} decreases

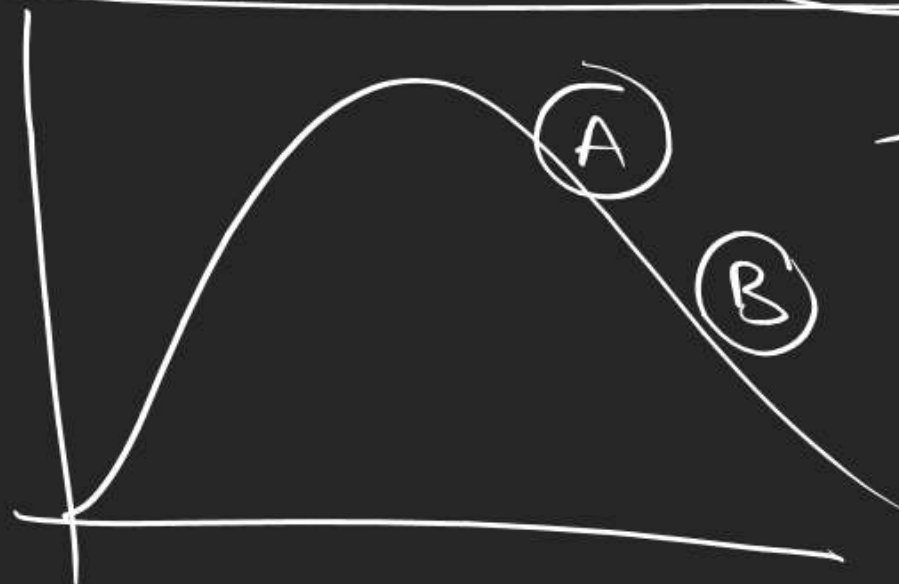
⑥ Variation with Molar mass



As $M \uparrow$ $u_{rms} \downarrow$ but fraction of particles moving with $u_{rms} \uparrow$

Q.

$M_A = 20$	$T_A = 300 \text{ K}$
$M_B = 40$	$T_B = 600 \text{ K}$



Same for
both

$$\frac{dN}{N} = \frac{4\pi}{\pi^{3/2}} \left(\frac{M}{2RT} \right)^{3/2} e^{-Mu^2/2RT} u^2 du$$

if range $du \ll 1$

Q. find no. of particles having speed betⁿ 1000 to 1001

Solⁿ Since range is very small $u = 1000$
 $du = 1001 - 1000$
 $= 1$

Q. find $\frac{dN}{N}$ having speed betⁿ U_{mps} to $U_{mps} + f U_{mps}$
where ($f \ll 1$)

Solⁿ

$$U = U_{mps} = \sqrt{\frac{2RT}{M}}$$

$$dU = f \times U_{mps} = f \sqrt{\frac{2RT}{M}}$$

$$\frac{dN}{N} = \frac{4\pi}{\pi^{3/2}} \left(\frac{M}{2RT} \right)^{3/2} e^{-\frac{M}{2RT} \times \frac{2RT}{M}} \times \left(\frac{2RT}{M} \right) \cdot f \left(\frac{2RT}{M} \right)^{1/2}$$

$$\left(\frac{dN}{N} \right) = \frac{4}{\sqrt{\pi}} e^{-1} \times f$$

Q. find $\frac{dN}{N}$ for O_2 at 300 K from U_{mps} to $U_{mps} + f U_{mps}$

$\frac{dN}{N}$ for N_2 at 400 K from U_{mps} to $U_{mps} + f U_{mps}$

$$\Rightarrow \text{Total KE} = \frac{1}{2} m u_1^2 + \frac{1}{2} m u_2^2 + \dots$$

$$= \frac{1}{2} m N \left(\frac{u_1^2 + u_2^2 + \dots + u_N^2}{N} \right)$$

$$= \frac{1}{2} m N_A \left(\frac{N}{N_A} \right) u_{\text{rms}}^2$$

Total KE
of n moles

$$= n \times \frac{1}{2} M u_{\text{rms}}^2 = n \times \frac{1}{2} M \frac{3RT}{M} = n \times \frac{3}{2} RT$$

$$\boxed{\text{KE}_{1\text{mol}} = \frac{3}{2} RT}$$

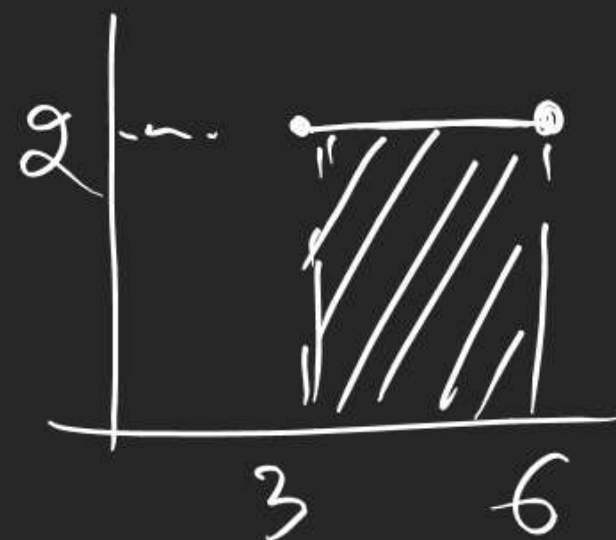
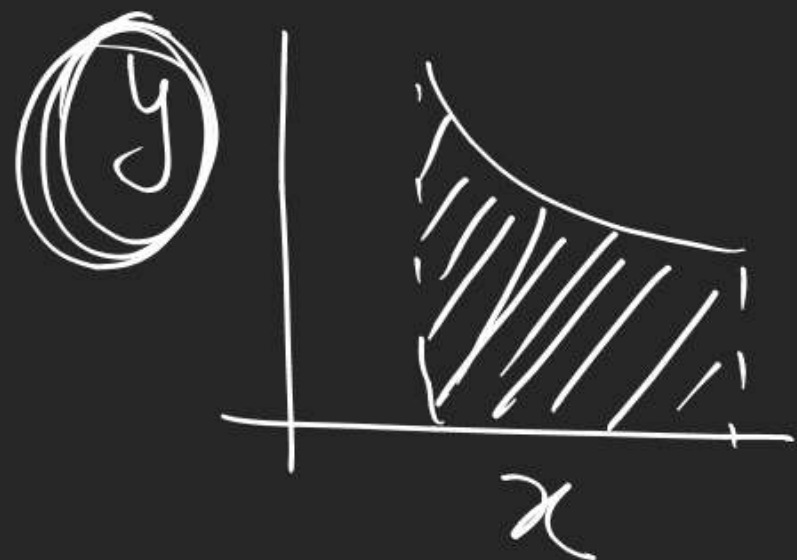
$$\boxed{\text{KE}_{1\text{molecule}} = \frac{3}{2} \frac{RT}{N_A} = \frac{3}{2} kT}$$

k = Boltzmann
Const

$$k = \frac{R}{N_A}$$

$$\boxed{\text{KE of } n \text{ moles} = n \times \frac{3}{2} RT}$$

0-1 39-58



$$Area = \int_{x_1}^{x_2} y \, dx$$

$$\begin{aligned} Area &= \int y \, dx \\ &= 2 \int dx \\ &= 2(6-3) \\ &= 6 \end{aligned}$$