

(5) Prod \rightarrow Sum/Dif

$$(6) 3 \sin \alpha = 5 \sin \beta$$

$$\frac{\sin \alpha}{\sin \beta} = \frac{5}{3} \quad (\text{C & D})$$

$$\frac{\sin \alpha + \sin \beta}{\sin \alpha - \sin \beta} = \frac{5+3}{5-3} = \frac{8}{2} = 4$$

$$\frac{2 \sqrt{\sin \left(\frac{\alpha+\beta}{2}\right)} \cdot \cos \left(\frac{\alpha-\beta}{2}\right)}{2 \cos \left(\frac{\alpha+\beta}{2}\right) \sin \left(\frac{\alpha-\beta}{2}\right)} = 4$$

$$\frac{\tan \left(\frac{\alpha+\beta}{2}\right)}{\tan \left(\frac{\alpha-\beta}{2}\right)} = 1$$

$$(7) \frac{2 \sin A \cos C + 2 \sin A}{2 \sin B \cos C + 2 \sin B}$$

$$\frac{2 \sin A \cdot \cos \left(\frac{\pi}{2}-C\right)}{2 \sin B \cdot \cos \left(\frac{\pi}{2}-C\right)} =$$

COMPOUND ANGLE

DPP

Compound Angle

- Q.1 If $\sin x + \sin^2 x = 1$, then the value of $\cos^2 x + \cos^4 x$ is -
 (A) 0 (B) 2 (C) 1 (D) 3
- Q.2 $2(\sin^6 \theta + \cos^6 \theta) - 3(\sin^4 \theta + \cos^4 \theta) + 1$ is equal to -
 (A) 2 (B) 0 (C) 4 (D) 6
- Q.3 $\tan A = -\frac{1}{2}$ and $\tan B = -\frac{1}{3}$, then $A + B =$
 (A) $\frac{\pi}{4}$ (B) $\frac{3\pi}{4}$ (C) $\frac{5\pi}{4}$ (D) $\frac{7\pi}{4}$
- Q.4 $\cos^2 48^\circ - \sin^2 12^\circ$ is equal to -
 (A) $\frac{\sqrt{5}-1}{4}$ (B) $\frac{\sqrt{5}+1}{8}$ (C) $\frac{\sqrt{3}-1}{4}$ (D) $\frac{\sqrt{3}+1}{2\sqrt{2}}$
- Q.5 The expression $\frac{\sin 80^\circ \cos 0^\circ - \sin 60^\circ \cos 30^\circ}{\cos 20^\circ \cos 0^\circ - \sin 30^\circ \sin 40^\circ}$ is equals.
 (A) $\tan \theta$ (B) $\tan 2\theta$ (C) $\sin 2\theta$ (D) $\cos 2\theta$
- Q.6 If $3 \sin \alpha = 5 \sin \beta$, then $\frac{\tan \frac{\alpha+\beta}{2}}{\tan \frac{\alpha-\beta}{2}} =$
 (A) 1 (B) 2 (C) 3 (D) 4
- Q.7 $\frac{\sin(A-C)+2\sin A+\sin(A+C)}{\sin(B-C)+2\sin B+\sin(B+C)}$ is equal to -
 (A) $\tan A$ (B) $\frac{\sin A}{\sin B}$ (C) $\frac{\cos A}{\cos B}$ (D) $\frac{\sin C}{\cos B}$
- Q.8 $\frac{1+\sin 2\theta+\cos 2\theta}{1+\sin 2\theta-\cos 2\theta} =$
 (A) $\frac{1}{2} \tan \theta$ (B) $\frac{1}{2} \cot \theta$ (C) $\tan \theta$ (D) $\cot \theta$
- Q.9 If $A = \tan 6^\circ \tan 42^\circ$ and $B = \cot 66^\circ \cot 78^\circ$, then -
 (A) $A = 2B$ (B) $A = 1/3B$ (C) $A = B$ (D) $3A = 2B$
- Q.10 If $x = y \cos \frac{2\pi}{3} = z \cos \frac{4\pi}{3}$ then $xy + yz + zx =$
 (A) -1 (B) 0 (C) 1 (D) 2
- Q.11 If $\tan \alpha = (1+2^{-1})$, $\beta = (1, 2^{5+1})^{-1}$, then $\alpha + \beta =$
 (A) $\pi/6$ (B) $\pi/4$ (C) $\pi/3$ (D) $\pi/2$
- Q.12 If $\tan A - \tan B + \tan C = \tan A \tan B \tan C$, then
 (A) A, B, C must be angles of a triangle
 (B) the sum of any two of A, B, C is equal to the third
 (C) A + B + C must be a integral multiple of π
 (D) None of these

AK

① Done in copy \downarrow Direct form.

$$② 2 \{ 1 - 3 \sin^2 \theta \cdot \cos^2 \theta \}$$

$$- 3 \{ 1 - 2 \sin^2 \theta \cos^2 \theta \} + 1 \\ \Rightarrow 0$$

$$(3) \tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$= -\frac{1}{2} + -\frac{1}{3} \\ \frac{1}{2} + \frac{1}{3} \\ 1 - \left(-\frac{1}{2} \right) \left(-\frac{1}{3} \right)$$

$$\tan(A+B) = \frac{-\frac{5}{6}}{\frac{5}{6}} = -1 \mid \frac{3\pi}{4}$$

$$(4) \tan^2 B - \sin^2 A = \tan(A+B) \cdot \tan(A-B)$$

$$\tan(60^\circ) \cdot \tan(36^\circ) = \frac{1}{2} \times \frac{\sqrt{5}+1}{4}$$

Q10 $\text{G}(180^\circ + 60^\circ) = -\text{G}60^\circ$
 $x = \sqrt{6 \cdot \frac{2\pi}{3}} = 2\sqrt{6} \cdot \frac{\pi}{3}$.

$y = \sqrt{6} \cdot \text{G}120^\circ = 2\sqrt{6} \cdot \underline{240^\circ}$

$\boxed{x = -\frac{y}{2}} = -\frac{z}{2}$

$y = -2x, z = -2x$

$xy + yz + zx$

$-2x^2 + (-2x)(-2x) + -2x^2$

$-4x^2 + 4x^2 = 0$

Q11 $\tan \alpha = (1+2^{-x})^{-1}$

$\tan \beta = (1+2^{x+1})^{-1}$

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(8) $\frac{(1+\text{G}2\theta)\sin 2\theta}{(1-\text{G}2\theta)\cos 2\theta}$

$$\frac{2(\text{G}^2\theta + 2\sin \theta \text{G}0)}{2\sin^2 \theta + 2\sin \theta \text{G}0}$$

$$\frac{2\text{G}0(\text{G}0 + \sin \theta)}{2\sin \theta (\sin \theta + \text{G}0)} = (\text{G}0)$$

(9) $\frac{A = \tan 6^\circ \tan 42^\circ}{B = \cot 66^\circ \cot 78^\circ}$

$\frac{A}{B} = \tan 6^\circ \tan 66^\circ \tan 42^\circ \tan 78^\circ$

$\frac{\tan(60-6^\circ) \tan 6^\circ \tan(60+6^\circ)}{\tan 54^\circ} \cdot \frac{\tan(60-18^\circ) \tan(60+18^\circ) \tan 18^\circ}{\tan 18^\circ}$

$\frac{\tan 54^\circ \times 6^\circ}{\tan 54^\circ} \times \frac{\tan 54^\circ \times 18^\circ}{\tan 18^\circ} = 1$

$A \approx B$

$$\tan \alpha = (1+2^{-\alpha})^{\frac{1}{2}} = \frac{2^{\frac{\alpha}{2}}}{1+2^{\frac{-\alpha}{2}}}$$

$$\tan \beta = \frac{1}{1+2^{1+\alpha}}$$

$$\begin{aligned}\tan(\alpha+\beta) &= \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \cdot \tan \beta} \\ &= \frac{\frac{2^{\frac{\alpha}{2}}}{1+2^{\frac{-\alpha}{2}}} + \frac{1}{1+2^{\frac{\alpha}{2}+1}}}{1 - \frac{2^{\frac{\alpha}{2}}}{1+2^{\frac{-\alpha}{2}}} \times \frac{1}{1+2^{\frac{\alpha}{2}+1}}}\end{aligned}$$

$$= \frac{2^{\frac{\alpha}{2}} + 2^{\frac{\alpha}{2}} \cdot 2^{\frac{\alpha}{2}} \cdot 2 + 1 + 2^{\frac{\alpha}{2}}}{1+2^{\frac{\alpha}{2}} + (2^{\frac{\alpha}{2}} + 2^{\frac{\alpha}{2}} \cdot 2^{\frac{\alpha}{2}} \cdot 2) - 1}$$

$$\begin{aligned}\tan(\alpha+\beta) &= \frac{1+2 \cdot 2^{\frac{\alpha}{2}} + 2(2^{\frac{\alpha}{2}})^2}{1+2 \cdot 2^{\frac{\alpha}{2}} + 2 \cdot (2^{\frac{\alpha}{2}})^2} - 1 \\ \alpha + \beta &\approx \frac{\pi}{4}\end{aligned}$$

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- Q.5** The expression $\frac{\sin 8\theta \cos \theta - \sin 6\theta \cos 3\theta}{\cos 2\theta \cos \theta - \sin 3\theta \sin 4\theta}$ is equals.
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A

$$A+B+C = n\pi$$

then.

$$\tan \alpha + \tan \beta + \tan (\alpha + \beta) = \tan \alpha \cdot \tan \beta \cdot \tan (\alpha + \beta)$$

$$\tan \alpha + \tan \beta + \tan (\alpha + \beta) = \tan \alpha \cdot \tan \beta \cdot \tan (\alpha + \beta)$$

from $\alpha + \beta + \gamma = ?$ $n\pi$

$$\frac{\sin(\frac{360+10}{2})}{\sin(\frac{10}{2})} \times \sin\left(\frac{10+360}{2}\right)$$

$\sin 180^\circ$ x - - -

~~~ = 0

Q14  $y = \sin(e^x) = \sqrt{2^x + \frac{1}{2^x}}$

Q17  $\sin\left(\frac{\pi}{14}\right) \cdot \sin\left(\frac{3\pi}{14}\right) \cdot \sin\left(\frac{5\pi}{14}\right)$

(g)  $\left(\frac{\pi}{2} - \frac{\pi}{14}\right) \cdot \sin\left(\frac{\pi}{2} - \frac{3\pi}{14}\right) \cdot \sin\left(\frac{\pi}{2} - \frac{5\pi}{14}\right)$

(g)  $\left(\frac{6\pi}{14}\right) \cdot \sin\left(\frac{4\pi}{14}\right) \cdot \sin\left(\frac{2\pi}{14}\right)$

-  $\left(\sin\left(\frac{8\pi}{14}\right) \cdot \sin\left(\frac{4\pi}{14}\right) \cdot \sin\left(\frac{2\pi}{14}\right)\right) =$

## COMPOUND ANGLE

A

- Q.13 The value of  $\sin 10^\circ + \sin 20^\circ + \sin 30^\circ + \dots + \sin 360^\circ$  is equal to -  
 (A) 0 (B) 1 (C)  $\sqrt{3}$  (D) 2
- Q.14 The number of real solutions of the equation  $\sin(e^x) = 2^x + 2^{-x}$  is -  
 (A) 1 (B) 0 (C) 2 (D) Infinite
- Q.15 If  $f(x) = \frac{\sin 3x}{\sin x}$ ,  $x = 11\pi$ , then the range of values of  $f(x)$  for real values of  $x$  is -  
 (A)  $[-1, 3]$  (B)  $(-\infty, -1]$  (C)  $(3, +\infty)$  (D)  $[-1, 3]$
- Q.16 If  $\cos x + \cos y + \cos \alpha = 0$  and  $\sin x + \sin y + \sin \alpha = 0$ , then  $\cot\left(\frac{x+y}{2}\right) =$   
 (A)  $\sin \alpha$  (B)  $\cos \alpha$  (C)  $\cot \alpha$  (D)  $2\sin \alpha$
- Q.17 The value of  $\sin \frac{\pi}{14} \sin \frac{3\pi}{14} \sin \frac{5\pi}{14}$  is :-  
 (A)  $\frac{1}{16}$  (B)  $\frac{1}{8}$  (C)  $\frac{1}{2}$  (D) 1
- Q.18 Maximum and minimum value of  $2\sin^2 \theta - 3\sin \theta + 2$  is -  
 (A)  $\frac{1}{4}, -\frac{7}{4}$  (B)  $\frac{1}{4}, \frac{21}{4}$  (C)  $\frac{21}{4}, -\frac{3}{4}$  (D)  $7, \frac{7}{8}$
- Q.19 For  $\theta \in (0, \pi/2)$ , the maximum value of  $\sin\left(\theta + \frac{\pi}{6}\right) + \cos\left(\theta + \frac{\pi}{6}\right)$  is attained at  $\theta =$   
 (A)  $\frac{\pi}{12}$  (B)  $\frac{\pi}{6}$  (C)  $\frac{\pi}{3}$  (D)  $\frac{\pi}{4}$
- Q.20 Minimum value of the expression  $\cos^2 \theta - (6\sin \theta \cos \theta) + 3\sin^2 \theta + 2$ , is -  
 (A)  $4 + \sqrt{10}$  (B)  $4 - \sqrt{10}$  (C) 0 (D) 4

(g)  $0.6720.640 = \frac{\sin(2 \cdot LA)}{2^n (\sin(SA))}$

(g)  $\left(\frac{14\pi - 6\pi}{14}\right) = (1 - \frac{6\pi}{14}) = \frac{6\pi}{14}$

-  $\frac{\sin(2 \cdot \frac{8\pi}{14})}{2^3 \sin(\frac{2\pi}{14})} = -\frac{\sin\left(\frac{14\pi + 2\pi}{14}\right)}{8 \cdot \sin\left(\frac{2\pi}{14}\right)} = -\frac{\sin(\pi + 2\pi/14)}{8 \sin(2\pi/14)}$

Q.16

$$6x + 6y = -6\cos\alpha \Rightarrow 2\left(\sin\left(\frac{x+y}{2}\right) \cdot \sin\left(\frac{x-y}{2}\right)\right) = -6\sin\alpha$$

$$2\sin\left(\frac{x+y}{2}\right) \cdot \sin\left(\frac{x-y}{2}\right) = -6\sin\alpha$$

$$\left(\sin\left(\frac{x+y}{2}\right)\right) = \left(-3\sin\alpha\right)$$

Sum of Any +ve No / f(x) with its Reciprocal  
is always gr.than

$$2^x + \frac{1}{2^x} \geq 2 \text{ or equal to}$$

Q15  $y = \frac{\sin 3x}{\sin x} = \frac{3\sin x - 4\sin^3 x}{\sin x}$

$y = \frac{\sin x (3 - 4\sin^2 x)}{\sin x} \Rightarrow y = 3 - 4\sin^2 x$

$0 \leq \sin^2 x \leq 1$

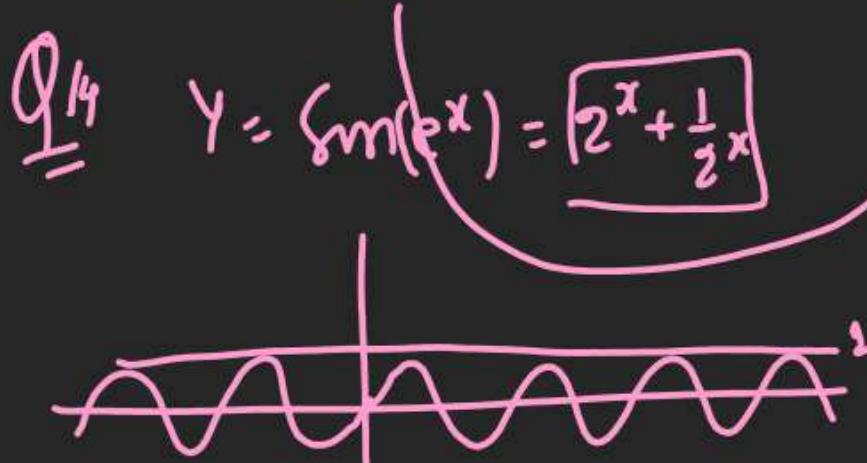
$0 > -4\sin^2 x > -4 \Rightarrow 3 > 3 - 4\sin^2 x > -1$

$\frac{8\sin(2\pi/14)}{8\sin(2\pi/14)} = \frac{1}{8}$

$$\frac{\sin\left(\frac{360+10}{2}\right)}{\sin\left(\frac{10}{2}\right)} \times \sin\left(\frac{10+360}{2}\right)$$

$\sin 180^\circ$  x - - -

~~~ : 0



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$$(-\frac{9}{16})$$

$$y = 2\sin^2 \theta - 3\sin \theta + 2$$

$$= 2\left(\sin^2 \theta - \frac{3}{2}\sin \theta + \frac{3}{4}\right)^{3/2}$$

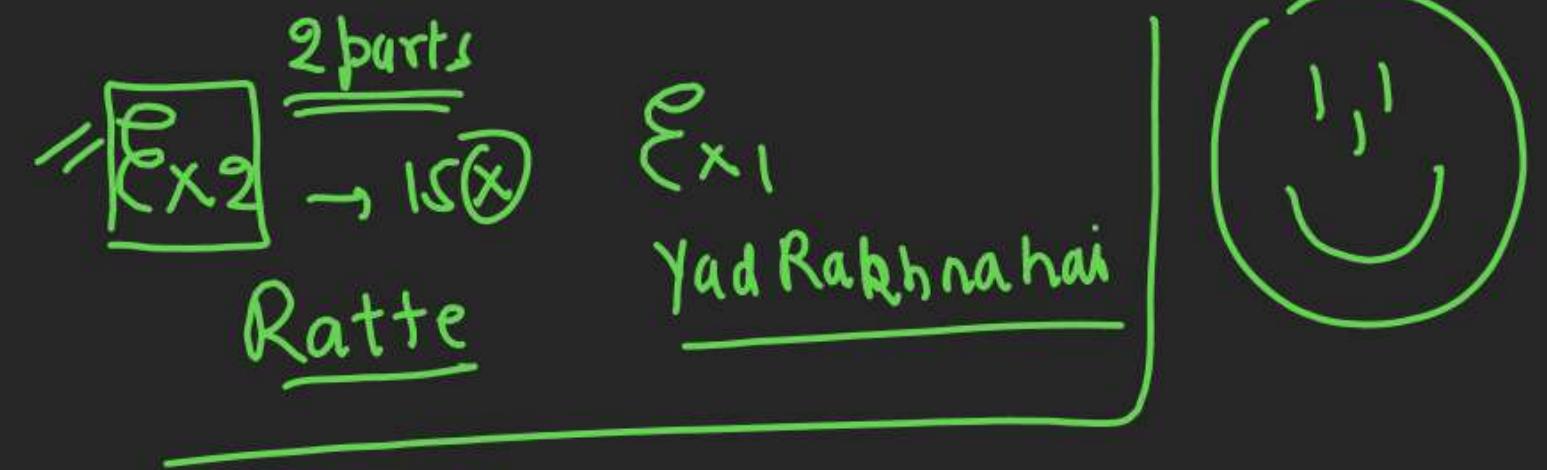
$$= 2\left((\sin \theta - \frac{3}{4})^2 - \left(\frac{3}{4}\right)^2 + 1\right)$$

$$= 2\left((\sin \theta - \frac{3}{4})^2 + \frac{1}{16}\right)$$

$$\downarrow \quad \downarrow$$

$$2\left(0 + \frac{1}{16}\right) = 2\left(1 - \frac{3}{4}\right)^2 + \frac{1}{16}$$

 $\frac{1}{8}$



Quadratic Eqn.

[12-15 Lec]

↳ {4 Lec Adv. Level.}

① $y = x^2 + \boxed{x} + 1$

$$= \left(x + \frac{1}{2} \right)^2 - \left(\frac{1}{2} \right)^2 + 1$$

$$y = \left(x + \frac{1}{2} \right)^2 + \frac{3}{4} \Rightarrow y - \frac{3}{4} = \left(x + \frac{1}{2} \right)^2$$

$$y = \left(x + \frac{1}{2} \right)^2 - \frac{1}{4}$$

$y = x^2$

$y = -x^2$

$x = -\frac{1}{2}$

$y = \frac{3}{4}$

$$(2) \quad y = x^2 - \boxed{x} + \frac{1}{2}$$

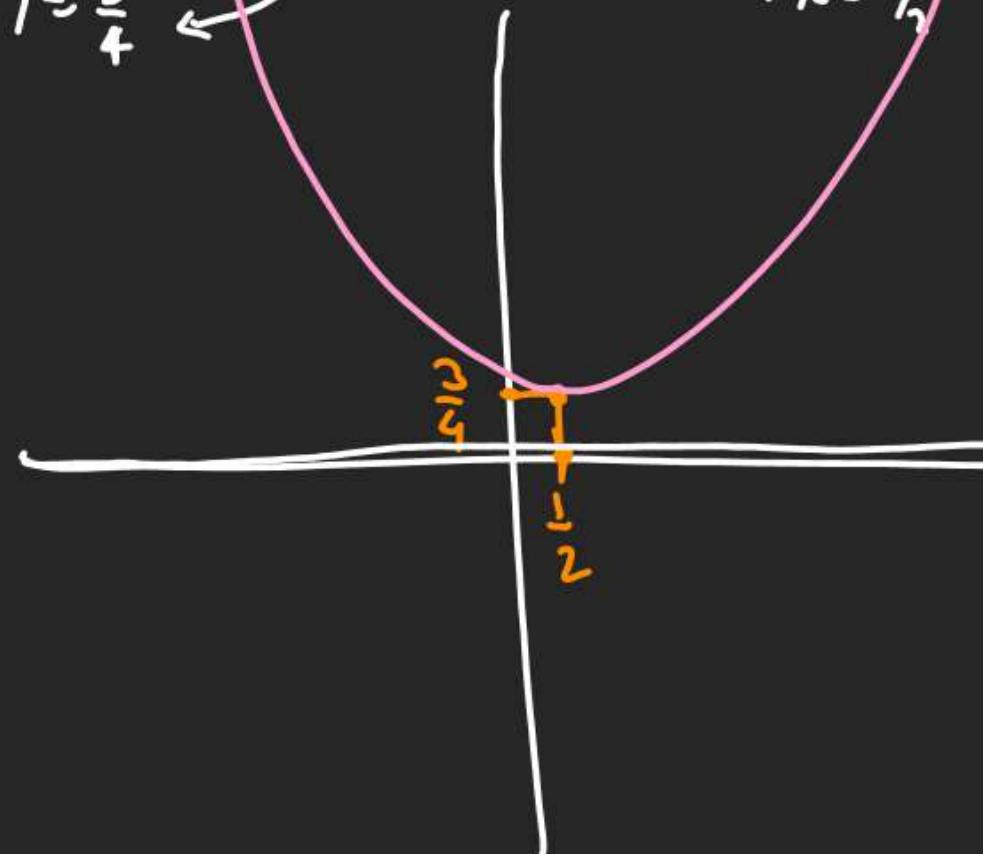
$D = (-1)^2 - 4 \times 1 \times 1$

$\boxed{D = -3} = -\text{ve}$

Total Graph above x Axis

$$y = (x - \frac{1}{2})^2 + \frac{3}{4}$$

$$y - \frac{3}{4} = (x - \frac{1}{2})^2 \rightarrow y = x^2$$



$$(3) \quad y = 2x^2 - 4x + 7$$

's graph.

$$= 2[x^2 - \boxed{2x} + \frac{7}{2}]$$

$$= 2[(x-1)^2 - (1)^2 + \frac{7}{2}]$$

$$= 2[(x-1)^2 + \frac{5}{2}]$$

$$y = 2(x-1)^2 + 5 \Rightarrow (y-5) = 2(x-1)^2 \Rightarrow y = 2x^2$$

$$\boxed{y=5} \quad \boxed{x=1}$$



$$D = (-4)^2 - 4 \times 2 \times 7$$

$$= 16 - 56 = -40 = -\text{ve}$$

. . . Graph Above x Axis

$$(4) \quad y = 2x^2 + 4x + 1$$

$$= 2 \left[x^2 + 2x + \frac{1}{2} \right] \quad \text{1) } D = 4^2 - 4 \times 2 \times 1$$

$$= 2 \left[(x+1)^2 - 1^2 + \frac{1}{2} \right] \quad D = 8 + \text{ve}$$

$$= 2 \left[(x+1)^2 - \frac{1}{2} \right] \quad \begin{array}{l} \text{X Axis is known} \\ 2) \text{ Places where graph is} \end{array}$$

$$y = 2(x+1)^2 - 1$$

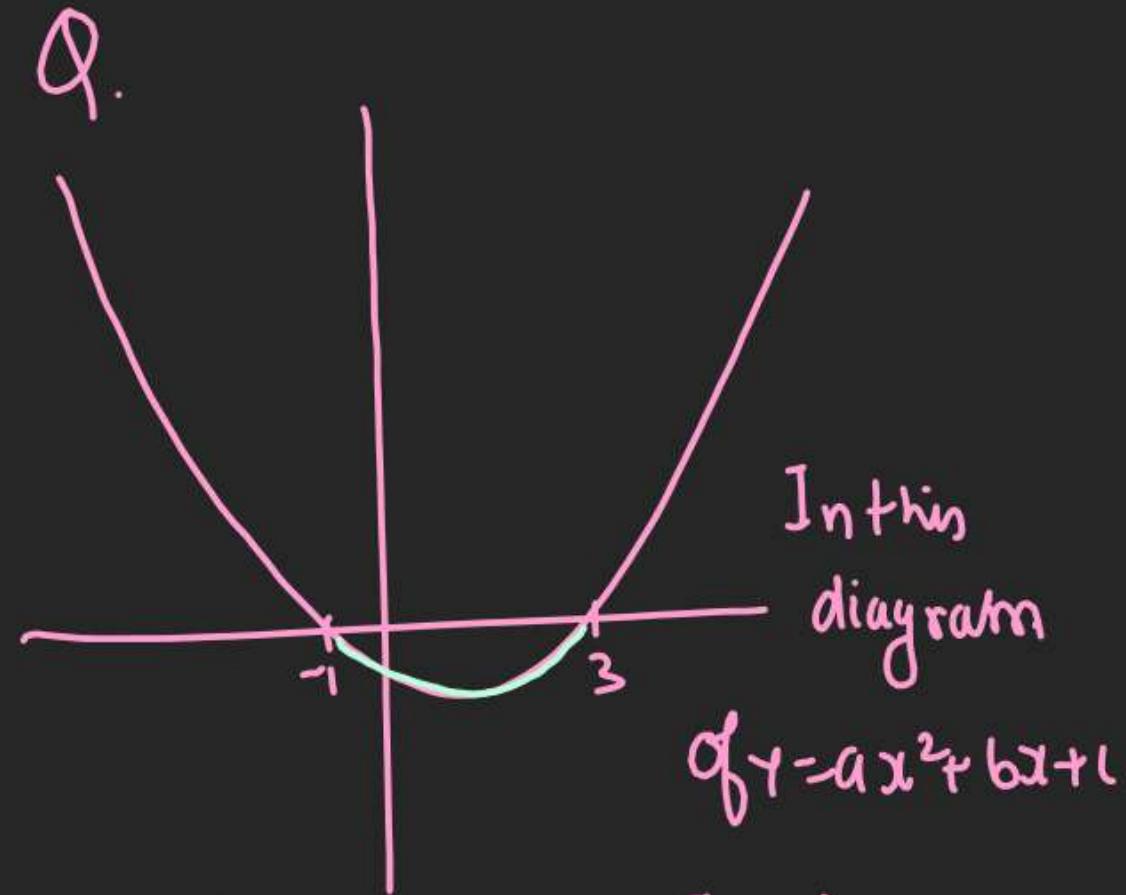
$$y = -1 \quad \begin{array}{l} \text{Graph is known} \\ x \text{ axis is known} \\ w.r.t. \text{ Roots} \end{array}$$

$$(y+1) = 2(x+1)^2 \rightarrow y = 2x^2$$

$$x = \frac{-4 \pm \sqrt{4^2 - 4 \times 2 \times 1}}{2 \times 2}$$



$$x = \frac{-4 \pm 2\sqrt{2}}{2 \times 2} = \begin{cases} \frac{-2 + \sqrt{2}}{2} \\ \frac{-2 - \sqrt{2}}{2} \end{cases}$$



A) $y < 0$ in $x \in (a, b)$
find a & b .

$y < 0$ means places where graph below x-axis
 $\therefore y < 0$ in $x \in (-1, 3)$

$$a = -1, b = 3$$

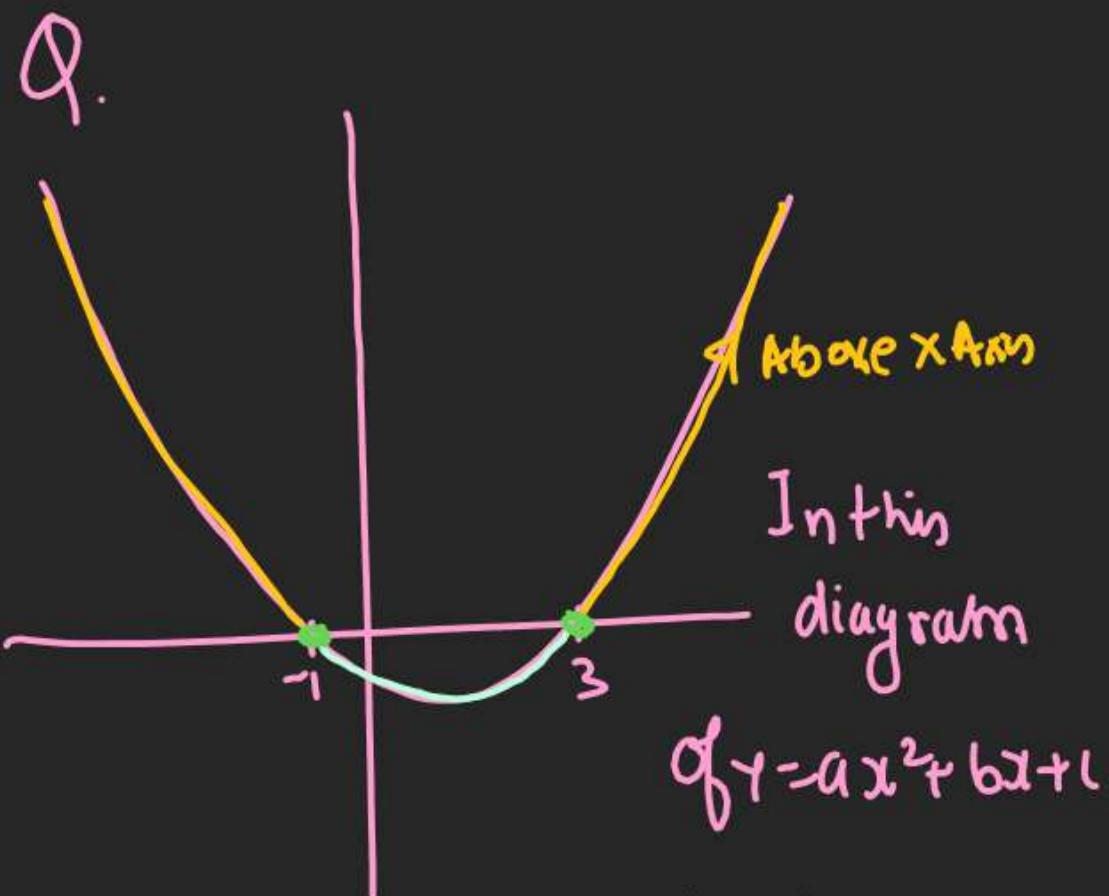
(B) $y > 0 \text{ in } x \in \dots$ $y > 0$ means graph above x Axis

$$y > 0 \text{ in } x \in (-\infty, -1) \cup (3, \infty)$$

(C) $y = 0$ at $x \in ?$ Graph cuts x Axis in at

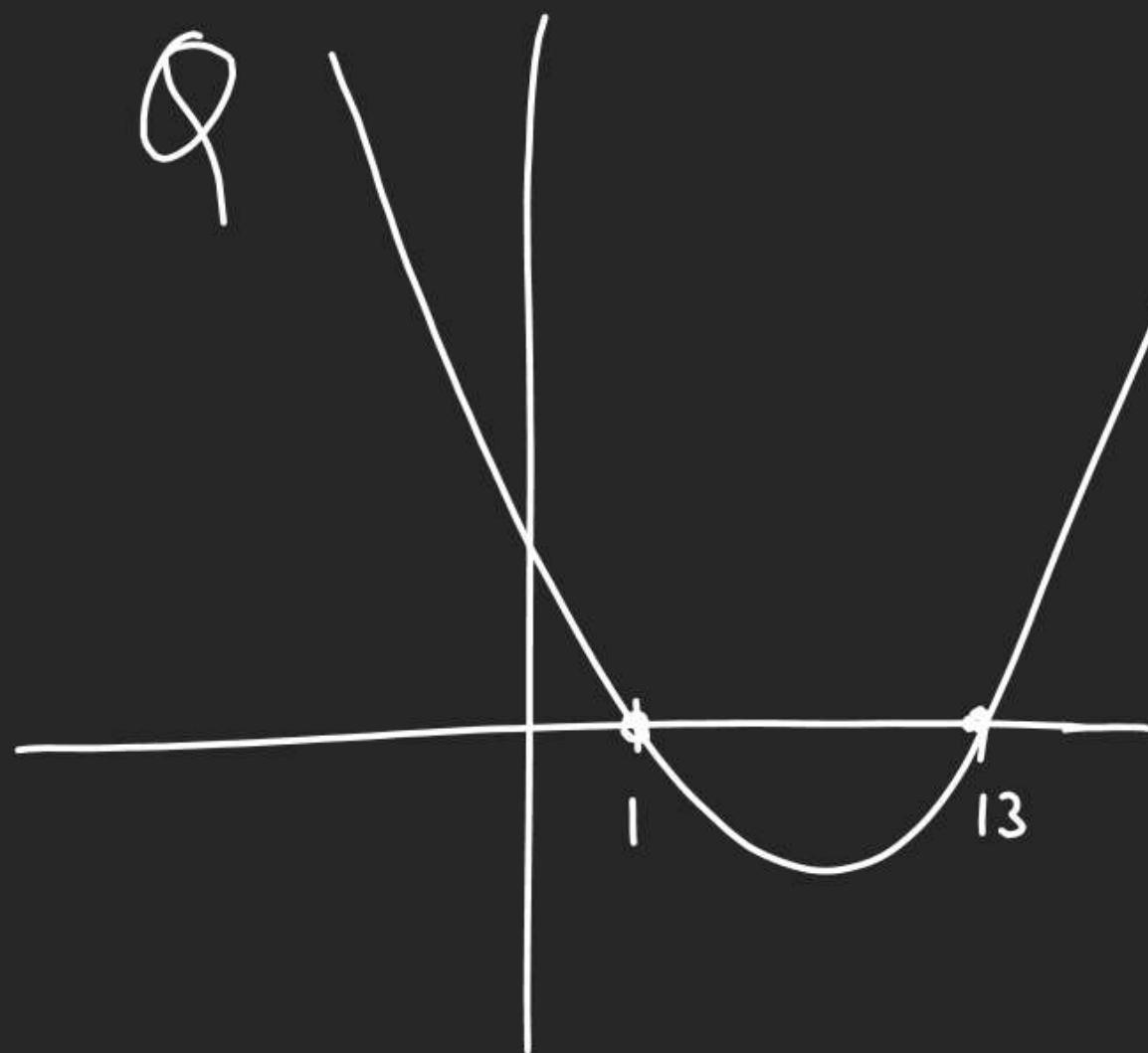
$x = -1, 3$

$x \in \{-1, 3\}$

A) $y < 0 \text{ in } x \in (a, b)$ find $a \& b$

$y < 0$ means places where
graph below x Axis
 $\therefore y < 0 \text{ in } x \in (-1, 3)$

$a = -1, b = 3$

(1) $y > 0$?

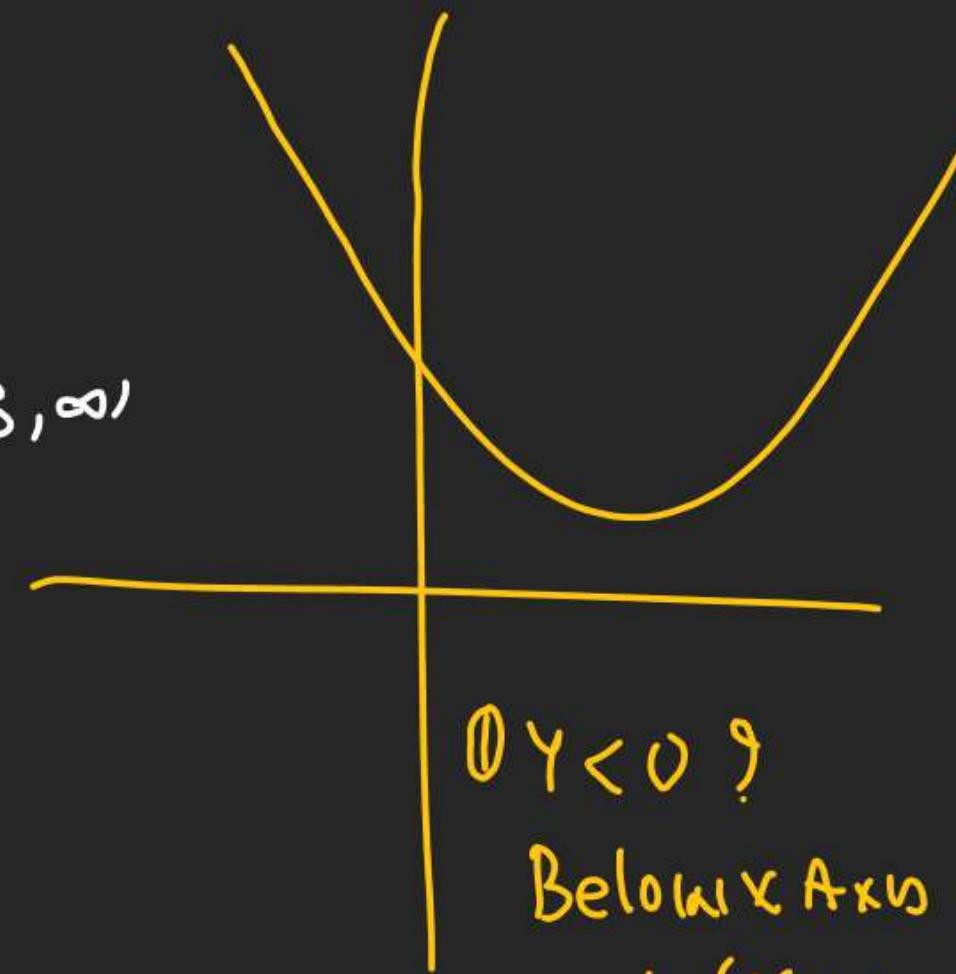
$$x \in (-\infty, 1) \cup (13, \infty)$$

(2) $y < 0$??

$$x \in (1, 13)$$

(3) $y = 0$?

$$x \in \{1, 13\}$$

(1) $y < 0$?

Below X Axis

 $x = \phi$ (Kahin)Below X Axis
Nhin hai)(2) $y > 0$? $x \in (-\infty, \infty)$ at all hrs(3) $y = 0$?X Axis Par no (utso) $x = \phi$

$$1) y = 3x^2 - 4x + 5 \text{ graph}$$

$$2) y = 2x^2 - 4x + 1 \text{ graph}$$