

KINEMATICS

(8). Concept of distance & displacement :-

- Distance:- It is the^(actual) path length of the particle.
- Displacement:- [It is the vector joining initial position to the final position of the particle.]
Or, "Change in position vector" → [Position vector must be w.r.t origin].

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[Change in an interval]

By Δ -Law of vector addition:-

$$\vec{r}_i + \Delta r = \vec{r}_f$$

$$\Delta r = [\vec{r}_f - \vec{r}_i]$$

[Displacement vector] [Change in position vector.]

\vec{r}_{AB} = (Displacement vector)

$$= (x_2 - x_1) \hat{i} + (y_2 - y_1) \hat{j} + (z_2 - z_1) \hat{k}$$

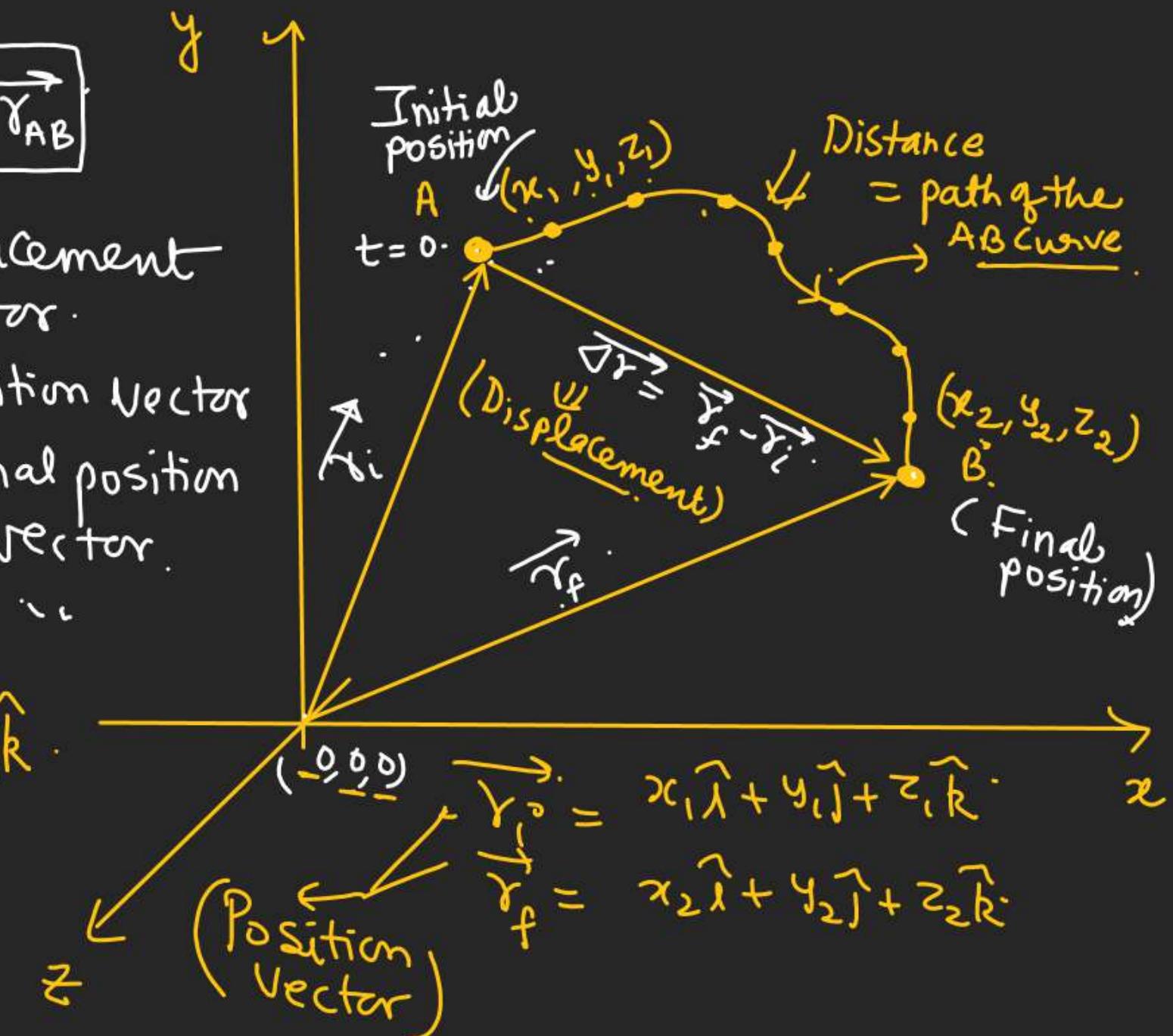
$$|\vec{r}_{BB}| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

$$\boxed{\Delta r = \vec{r}_{AB}}$$

↓
Displacement Vector.

\vec{r}_i = Position Vector

\vec{r}_f = final position vector.



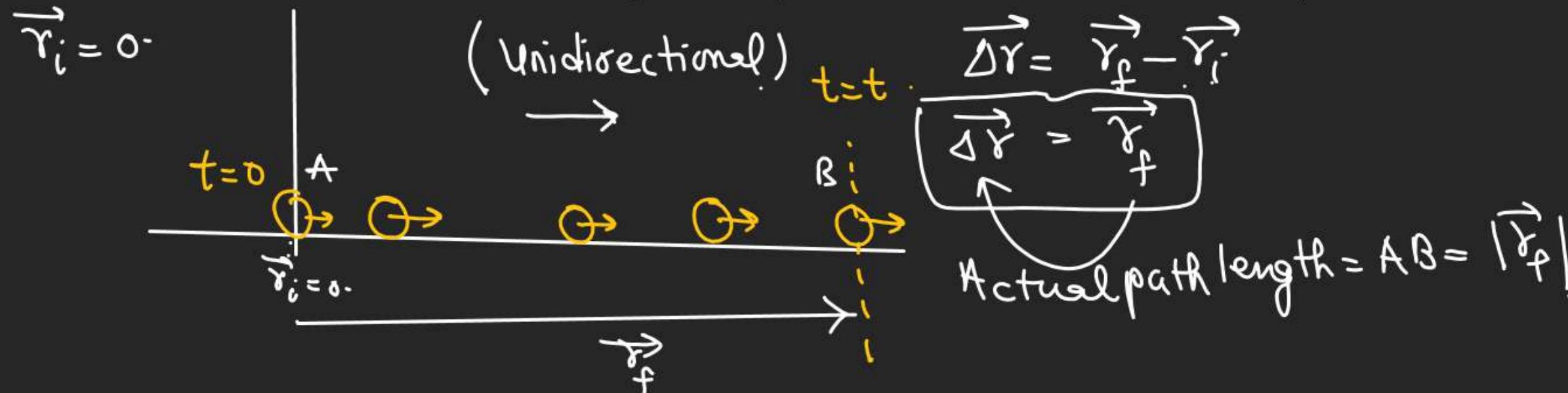
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(*) \Rightarrow Distance $>$ |Displacement|.

\Rightarrow Distance is always 've' it is a Scalar quantity
but displacement can be (+ve) or (-ve) and it is a vector quantity.

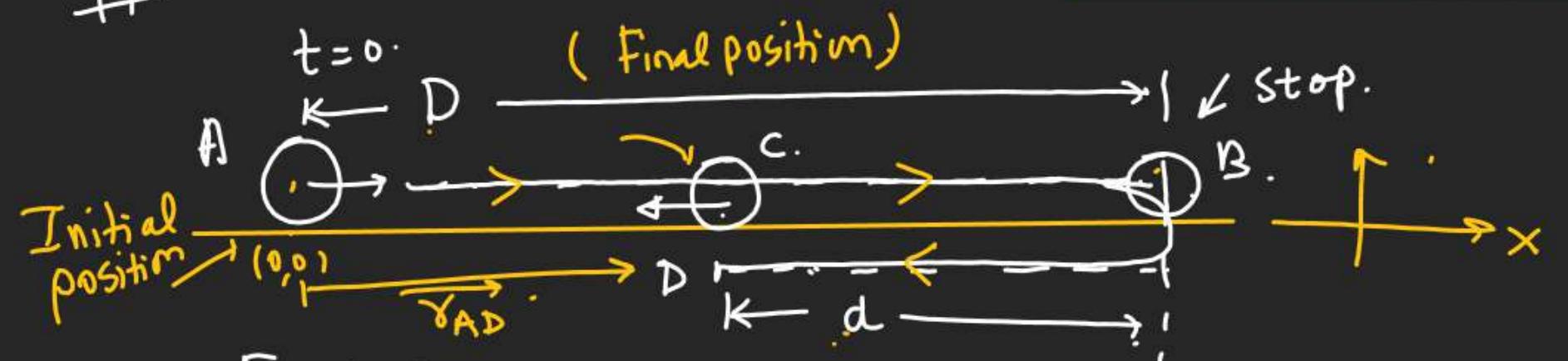
\Rightarrow [Distance = Displacement]

\Rightarrow When motion of the particle is a straight line and unidirectional



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\Rightarrow Find Distance and displacement for the motion A C B D

$$\text{Displacement} \Rightarrow \vec{r}_{AD} = (D-d)\hat{i}$$

$$|\vec{r}_{AD}| = \underline{(D-d) \text{ m}}$$

Distance = Actual path length
of A C B D = $(D+d)$ m.

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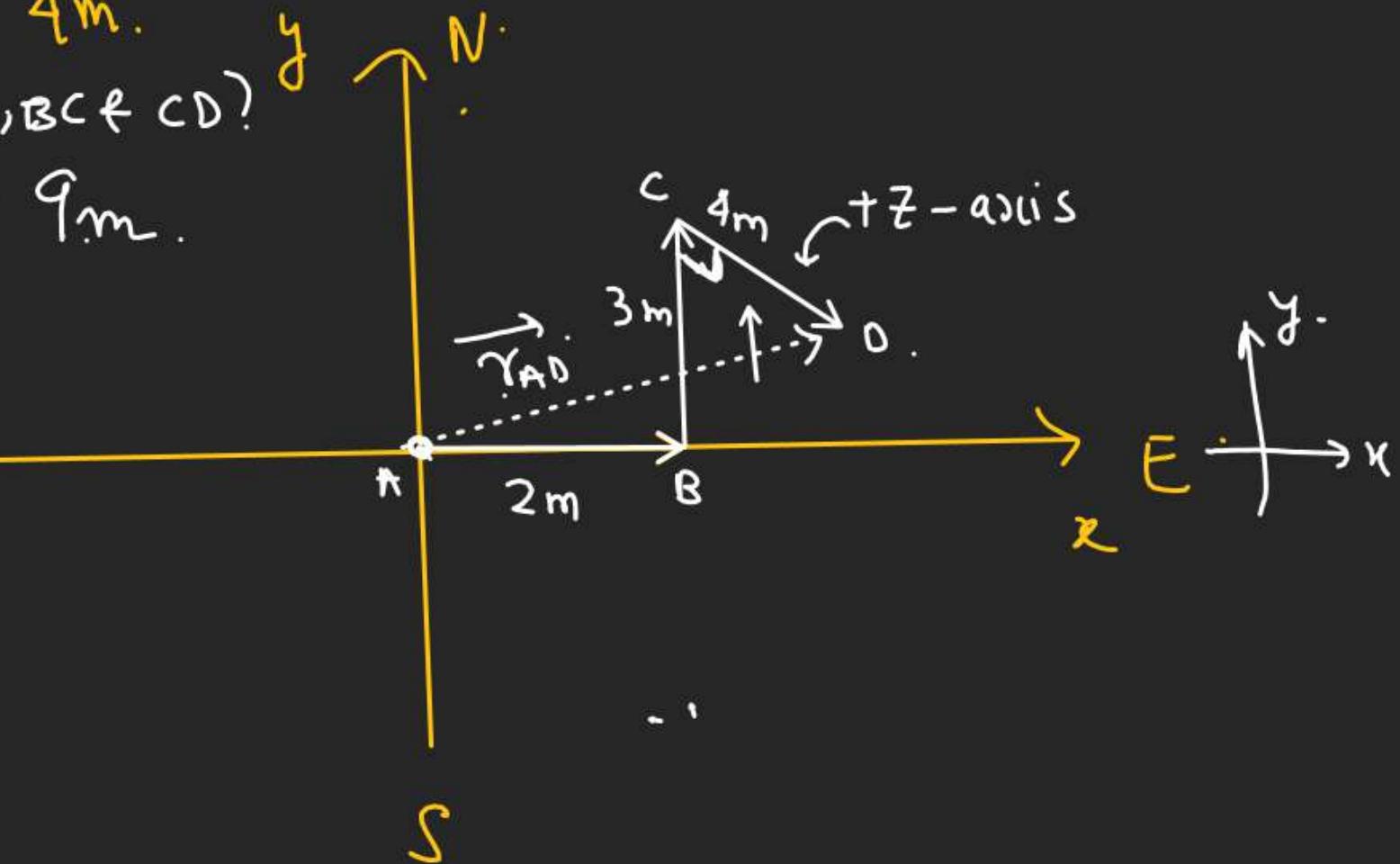
A bird starts flying in east direction and cover a distance of 2m after that it turns towards north and cover a distance of 3m. and finally move perpendicularly outward and cover a distance of 4m.

[Find] 1) distance = (Path length of AB, BC & CD)
 2) displacement = $2 + 3 + 4 = 9\text{m}$.

Displacement: $\Rightarrow \downarrow$

$$\begin{aligned}\vec{r}_{AD} &= \vec{r}_{AB} + \vec{r}_{BC} + \vec{r}_{CD} \\ &= (2\hat{i} + 3\hat{j} + 4\hat{k})\end{aligned}$$

$$|\vec{r}_{AD}| = \sqrt{(2)^2 + (3)^2 + (4)^2} = \sqrt{29}\text{m}$$



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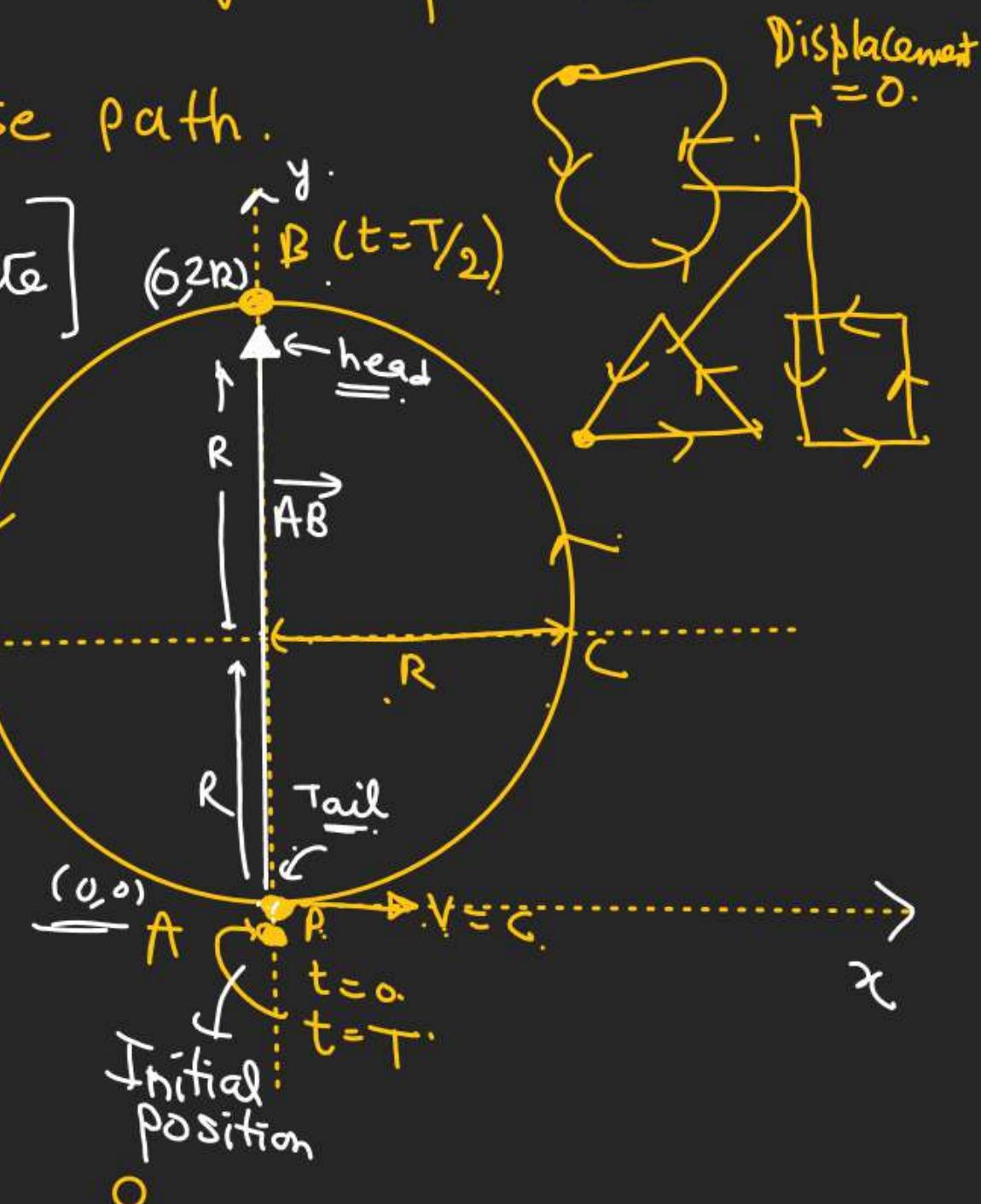
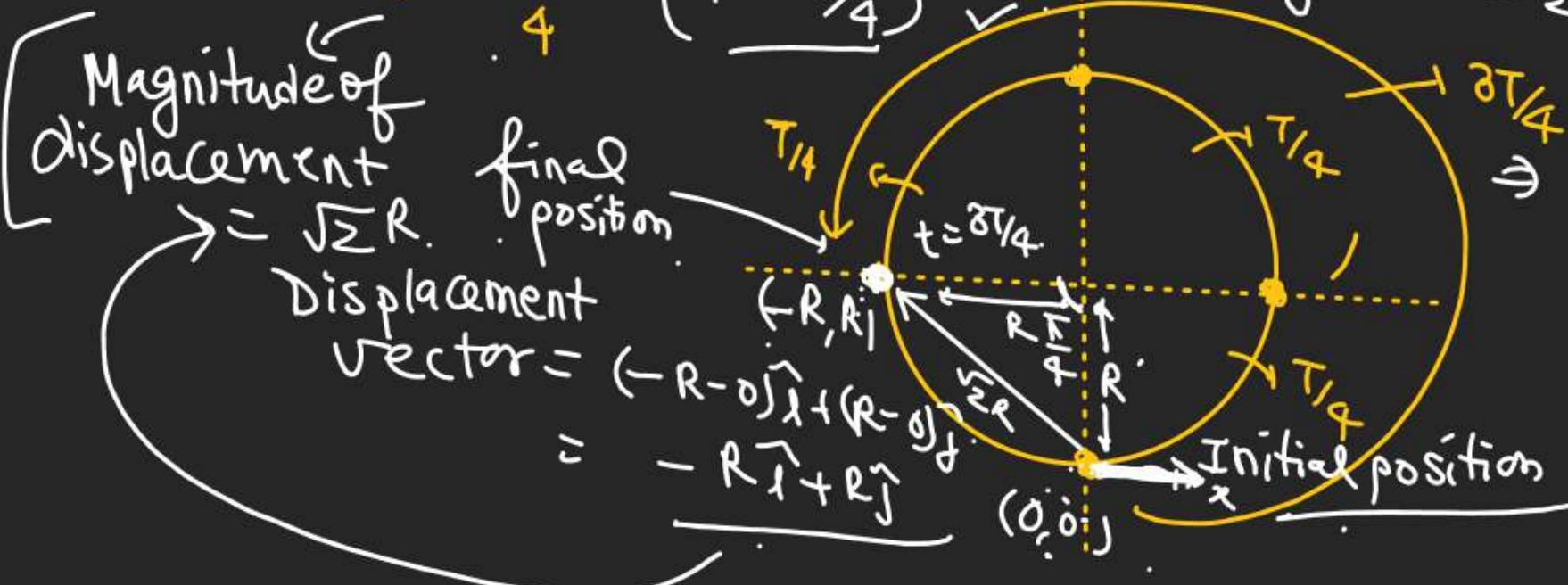
\Rightarrow Displacement is always zero if initial and final position vector is same.

possible when particle is moving in a close path.

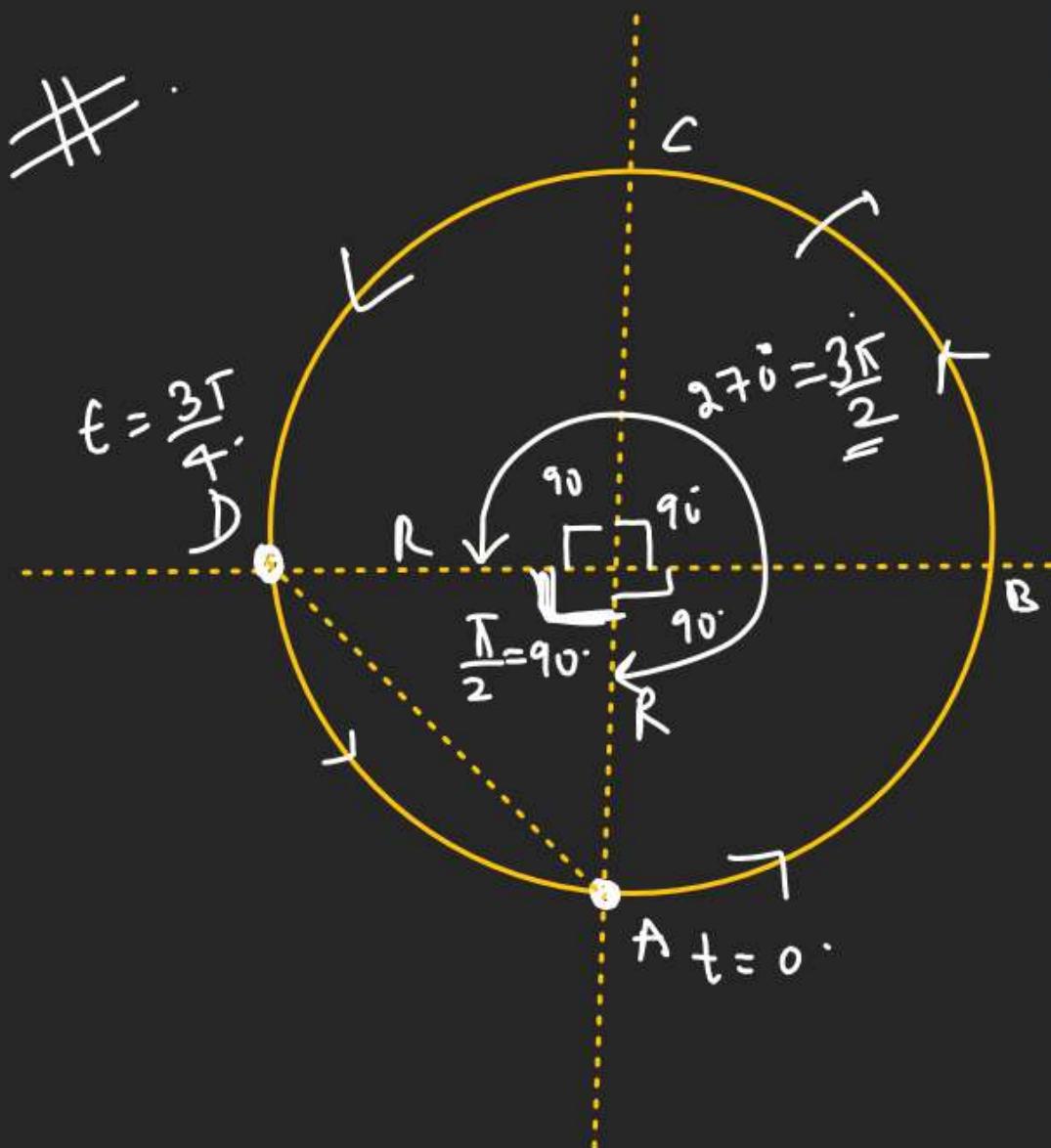
Find Distance and displacement [$T \rightarrow$ To Cover one complete rotation]

- a) for $t = 0$ to $t = T$ → $\begin{cases} \text{Distance} = 2\pi R \\ \text{Displacement} = 0 \end{cases}$ $T = \left[\frac{2\pi R}{V} \right]$
- b) for $t = 0$, to $t = \frac{T}{2}$ $\begin{cases} \text{Distance} = \text{path length} \\ \text{Displacement} = ACB = (\pi R) \end{cases}$
- c) for $t = 0$, to $t = \frac{3T}{4}$ $\begin{cases} \text{Displacement} = (2R)\hat{j} \\ \text{magnitude} = \sqrt{(2R)^2} = 2R \end{cases}$

$$t = \frac{3T}{4} = (T - \frac{T}{4})$$



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$$L = R\theta$$

$$\left[\frac{L_{ABCD}}{\text{radian}} \right] = \left[R \times \frac{3\pi}{2} \right]$$

↳ major arc

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~~Q8.~~ Distance and displacement at an angular displacement θ' in Uniform Circular motion ($v=c$)

$$\vec{r}_{PQ} = (R\cos\theta - R)\hat{i} + (R\sin\theta)\hat{j}$$

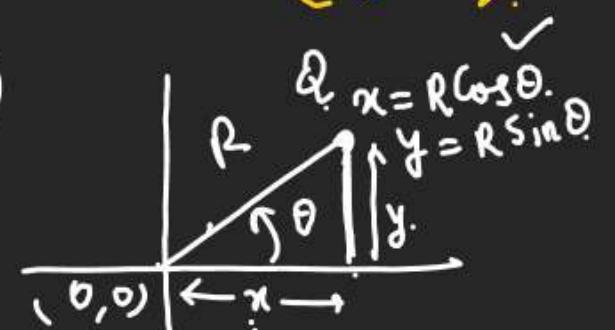
Displacement
Vector

$$|\vec{r}_{PQ}| = \sqrt{R^2(\cos\theta - 1)^2 + R^2\sin^2\theta}$$

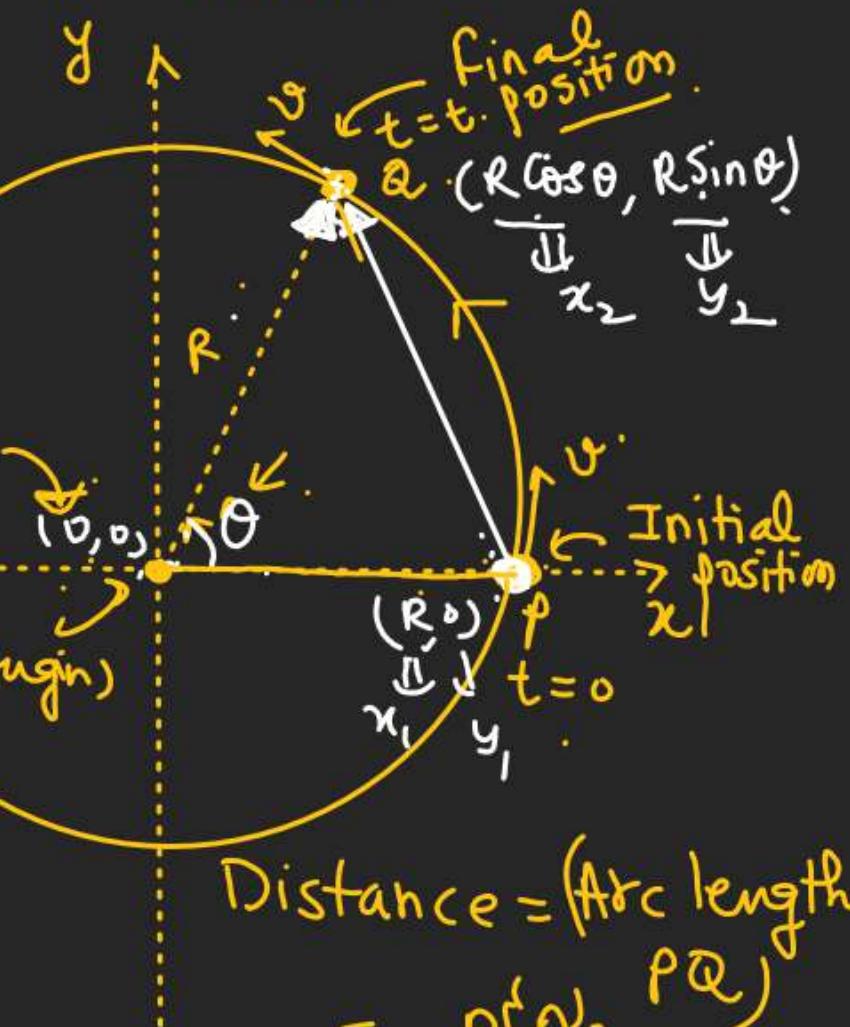
$$= R \sqrt{\cos^2\theta + 1 - 2\cos\theta + \sin^2\theta}$$

$$= R \sqrt{2 - 2\cos\theta}$$

$$|\vec{r}_{PQ}| = R \sqrt{2(1 - \cos\theta)} = R \sqrt{2 \left[1 - \left(1 - 2\sin^2\frac{\theta}{2} \right) \right]} = R \sqrt{4\sin^2\frac{\theta}{2}} = \left[2R\sin\frac{\theta}{2} \right]$$



$$\begin{aligned} \cos 2\theta &= (2\cos^2\theta - 1) \\ \cos\theta &= (1 - 2\sin^2\frac{\theta}{2}) \end{aligned}$$

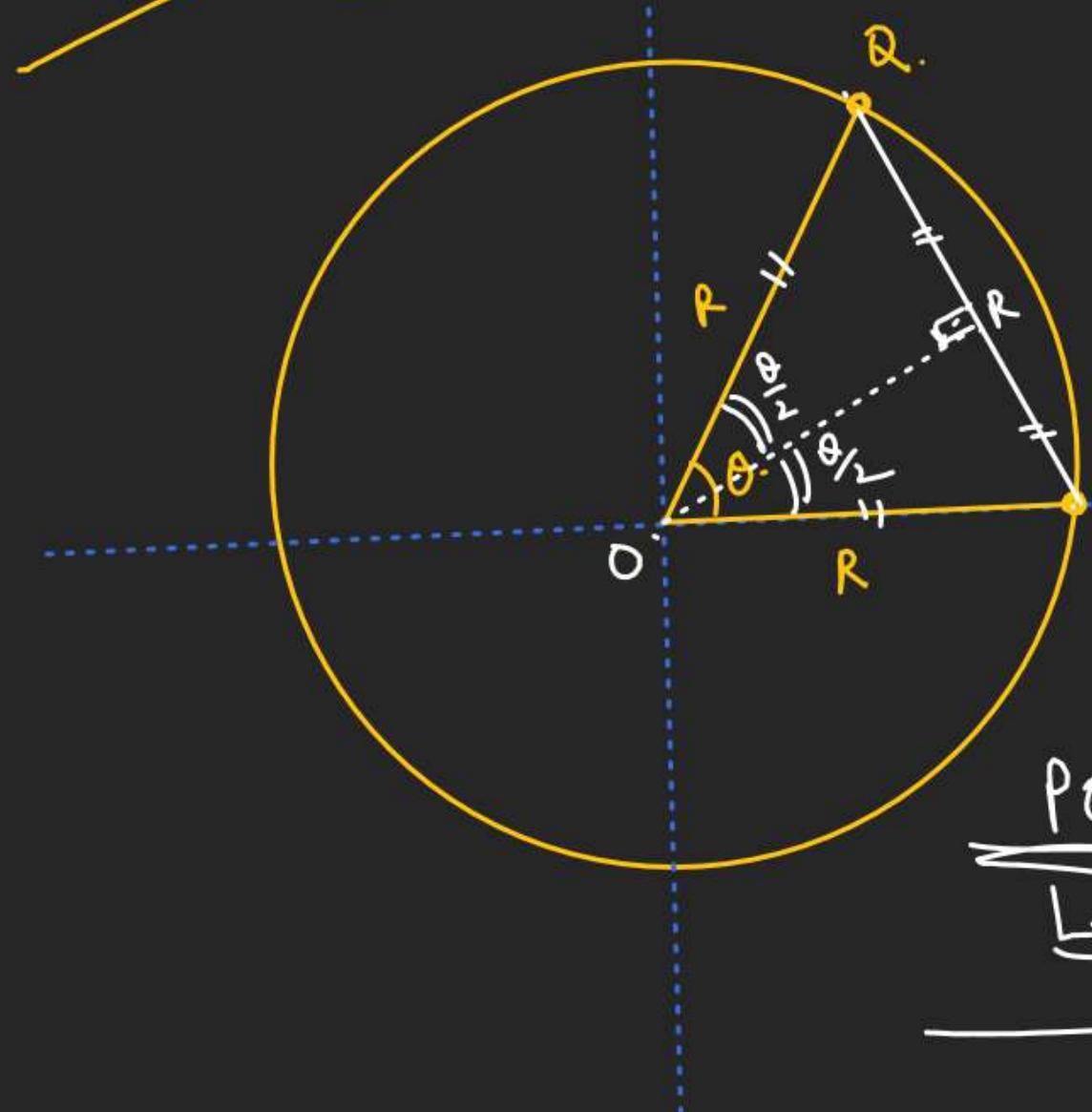


$$\begin{aligned} \text{Distance} &= (\text{arc length } PQ) \\ &= \underline{R[\theta]}_{\text{radian}} \\ &= \underline{R \times \frac{\pi}{180} \times \theta}_{\text{if } \theta \text{ in degree}} \end{aligned}$$

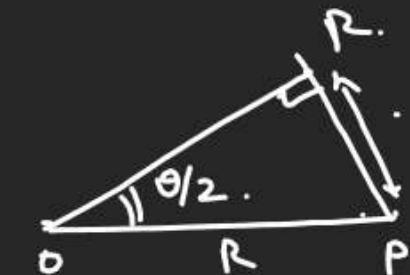
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Another method

For displacement:



In $\triangle OPR$



$$\sin \frac{\theta}{2} = \frac{PR}{R}$$

$$\underline{PR} = [R \sin \frac{\theta}{2}]$$

$$\underline{PQ} = 2 \underline{PR} = [2R \sin \frac{\theta}{2}]$$

Magnitude of displacement

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~~#. Rω ✓~~

Q. A particle moves in a semicircular path of radius R from O to A (Fig.) Then it moves parallel to z – axis covering a distance R upto B. Finally it moves along BC parallel to y – axis through a distance $2R$. Find the ratio of D/s.

