

GAUSS'S LAW

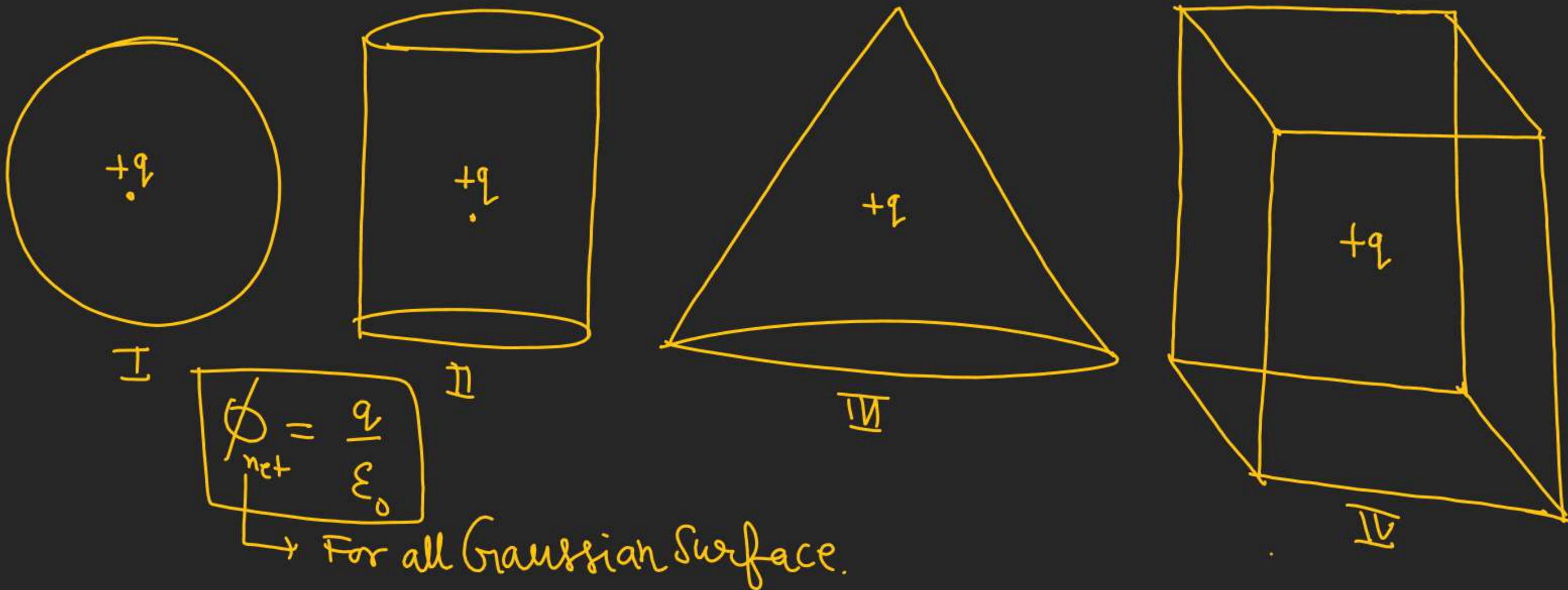
Some Important points about Gauss's Law:-

- Applicable only for the closed Surface.
- It fundamentally gives Electric flux not the electric field intensity
- It relates the total flux linked with a closed surface to the charge enclosed by the closed surface. If a closed surface doesn't enclose any Charge then

$$\oint \vec{E} \cdot d\vec{S} = 0$$

GAUSS'S LAW

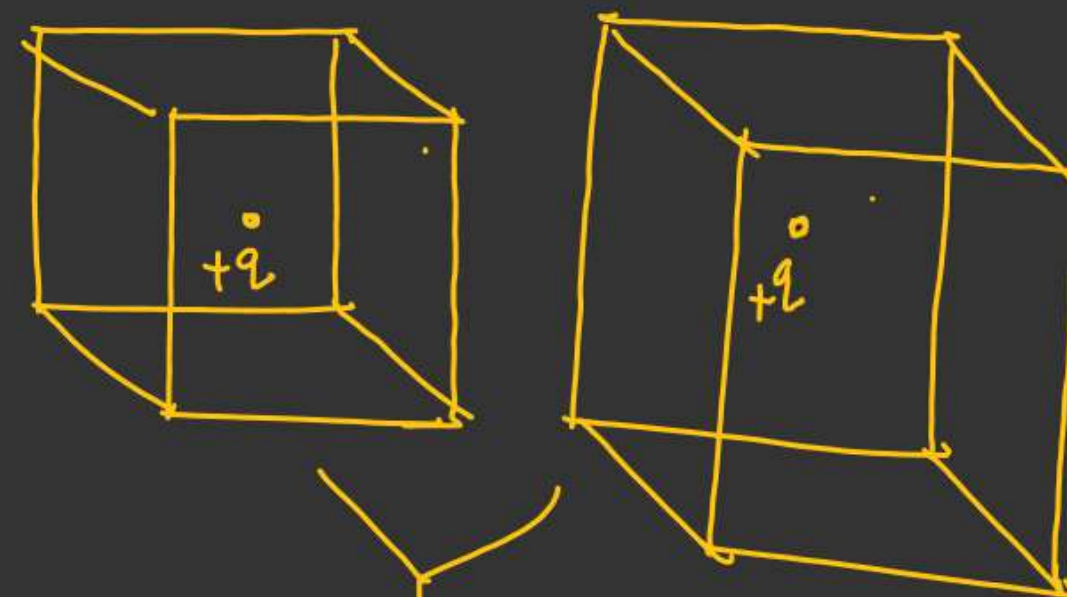
Q. Total flux linked with a closed surface is independent of the shape and size of the body and position of charge inside it.



Flux independent of the Location of Charge inside
Gaussian surface.



$$\phi_T = \frac{q}{\epsilon_0}$$



$$(\phi_T)_{\perp} = \frac{q}{\epsilon_0}$$

Total flux through whole cube

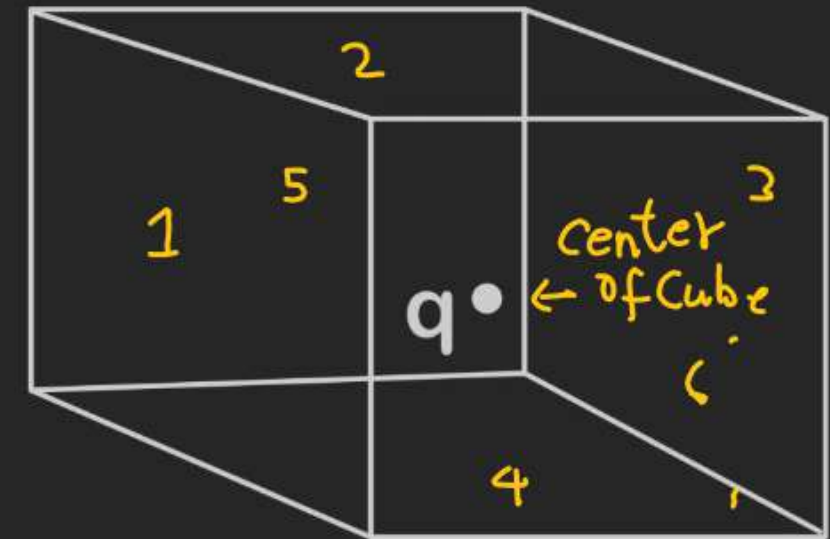
GAUSS'S LAW

Q. If a symmetrical closed body has n-identical faces with point charge at its center, flux linked with each face will be $\frac{1}{n}(\phi_T)$.

$$(\phi_T)_{\text{cube}} = \frac{q}{\epsilon_0} \leftarrow$$

$$(\phi)_{\text{each face}} = \left(\frac{q}{\epsilon_0} \right) \frac{1}{6}$$

$$(\phi)_{\text{each face}} = \frac{q}{6\epsilon_0}$$



GAUSS'S LAW

At the Corner of the Cube

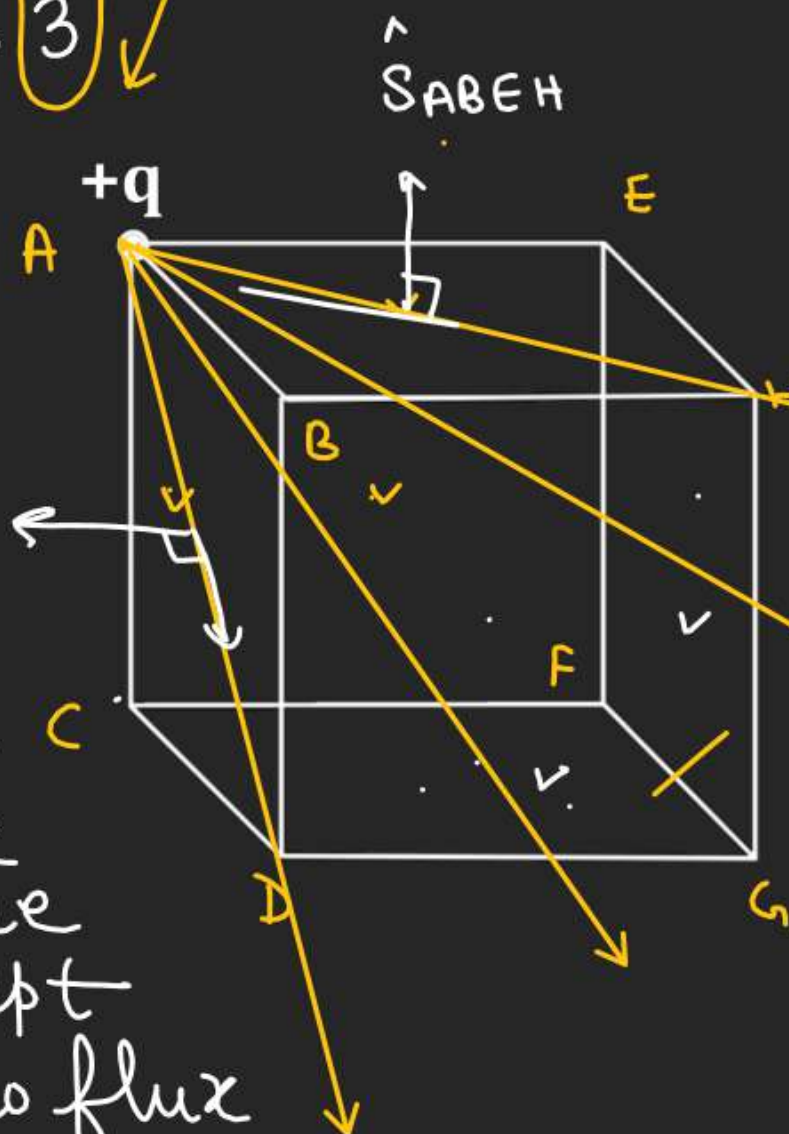
Flux through each face??

$$\phi_{\text{each face}} = \frac{q}{8\epsilon_0} \times \frac{1}{3}$$

$$\underline{\underline{\phi_{\text{each face}} = \frac{q}{24\epsilon_0}}}$$

Note

(*) Faces Contributing towards the Corner where Charge is kept have zero flux as $\hat{s} \perp \vec{E}$



Flux through the Cube

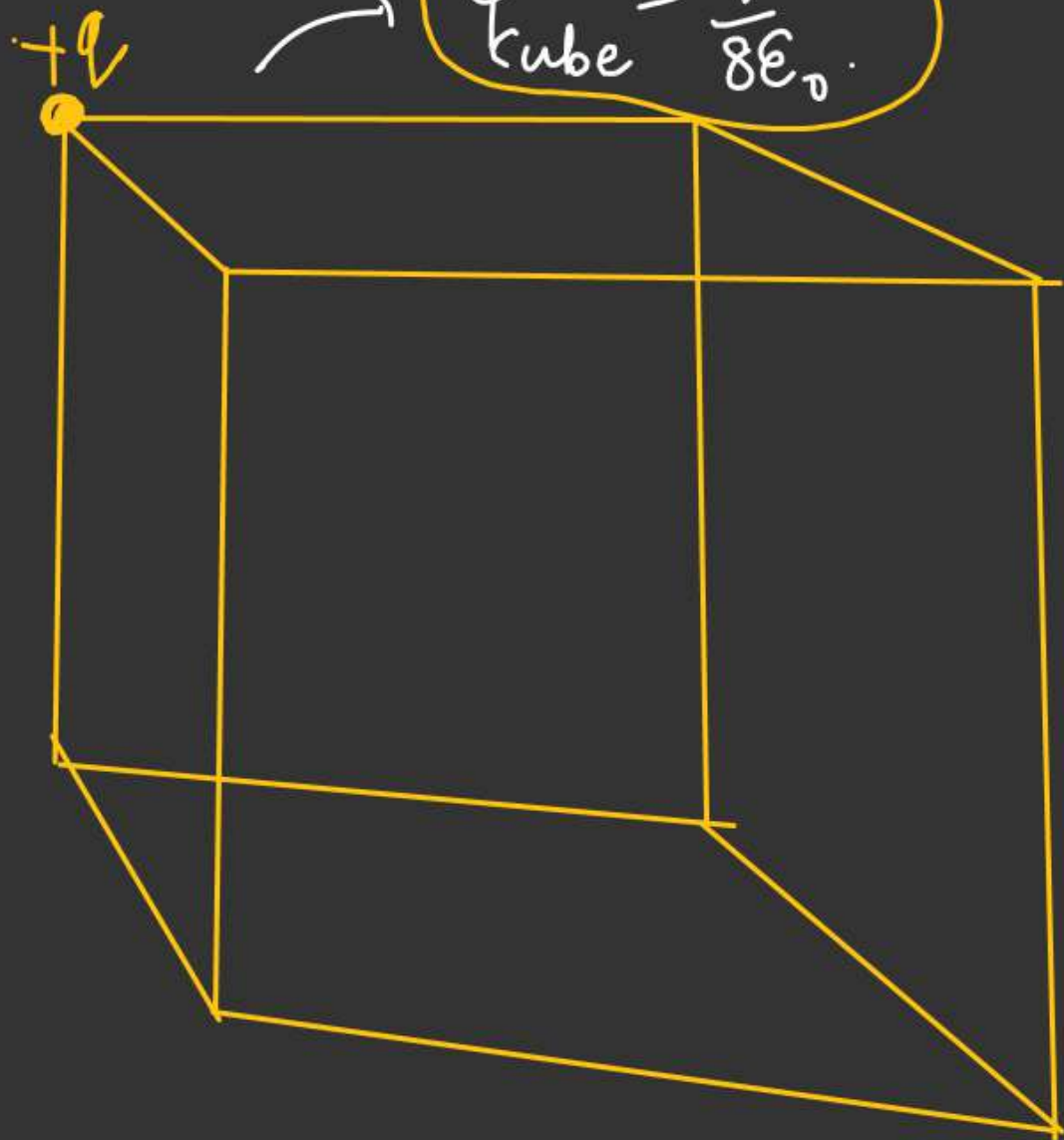
$$\phi_{\text{both the cube}} = \frac{q}{\epsilon_0}$$

$$\phi_{\text{each cube}} = \frac{1}{8} \times \frac{q}{\epsilon_0}$$

$$\underline{\underline{= \frac{q}{8\epsilon_0} \checkmark}}$$

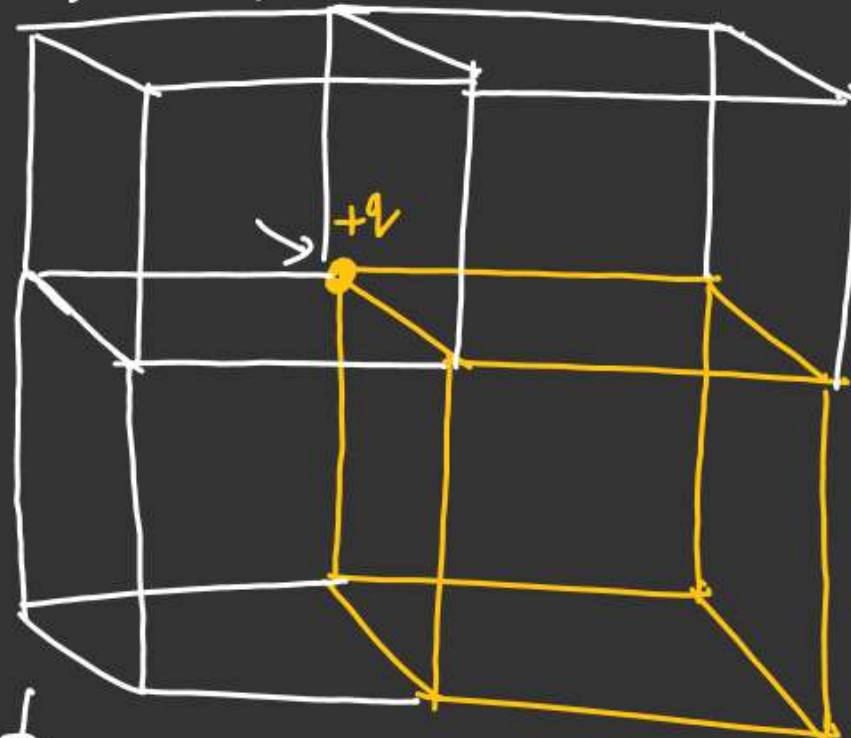
Gaussian Surface

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$$\phi_{cube} = \frac{q}{8\epsilon_0}$$

4 → back sides

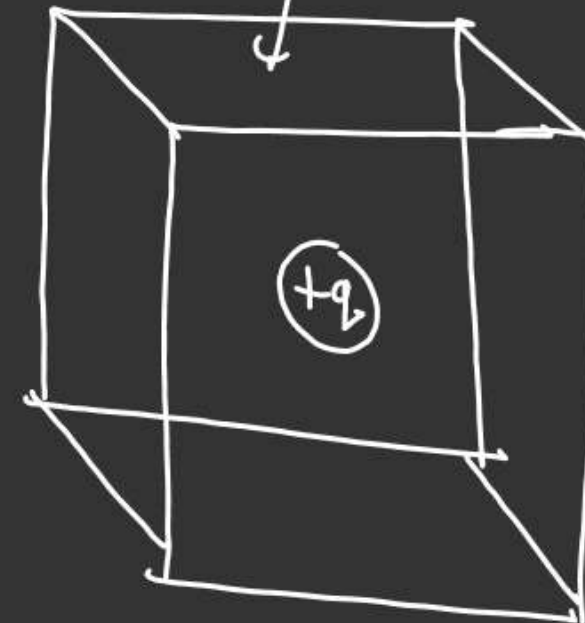


$$\phi_{\text{Eight Cubes}} = \left(\frac{q}{\epsilon_0} \right)$$

All the Eight Cubes are identically located w.r. to +q.

$$\phi_{\text{each cube}} = \left(\frac{q}{\epsilon_0} \times \frac{1}{8} \right) = \frac{q}{8\epsilon_0}$$

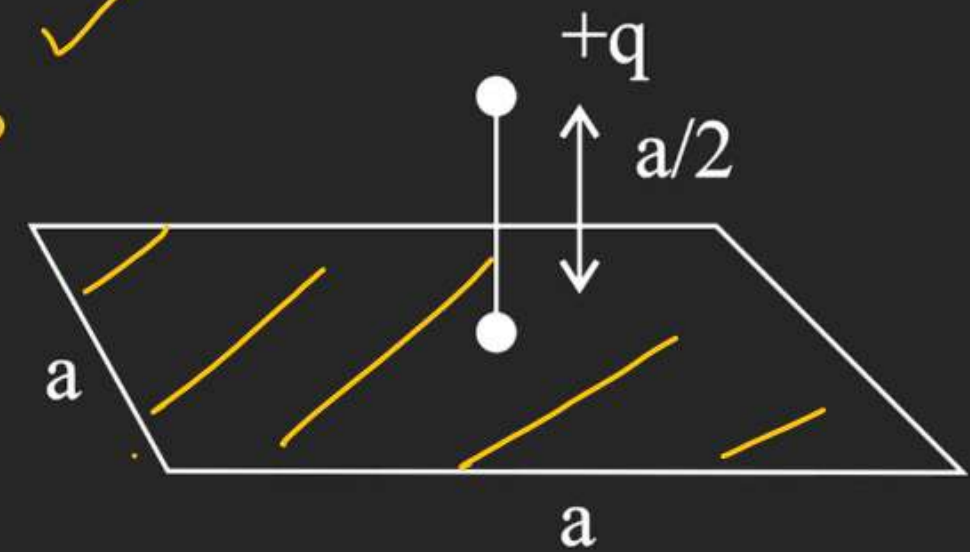
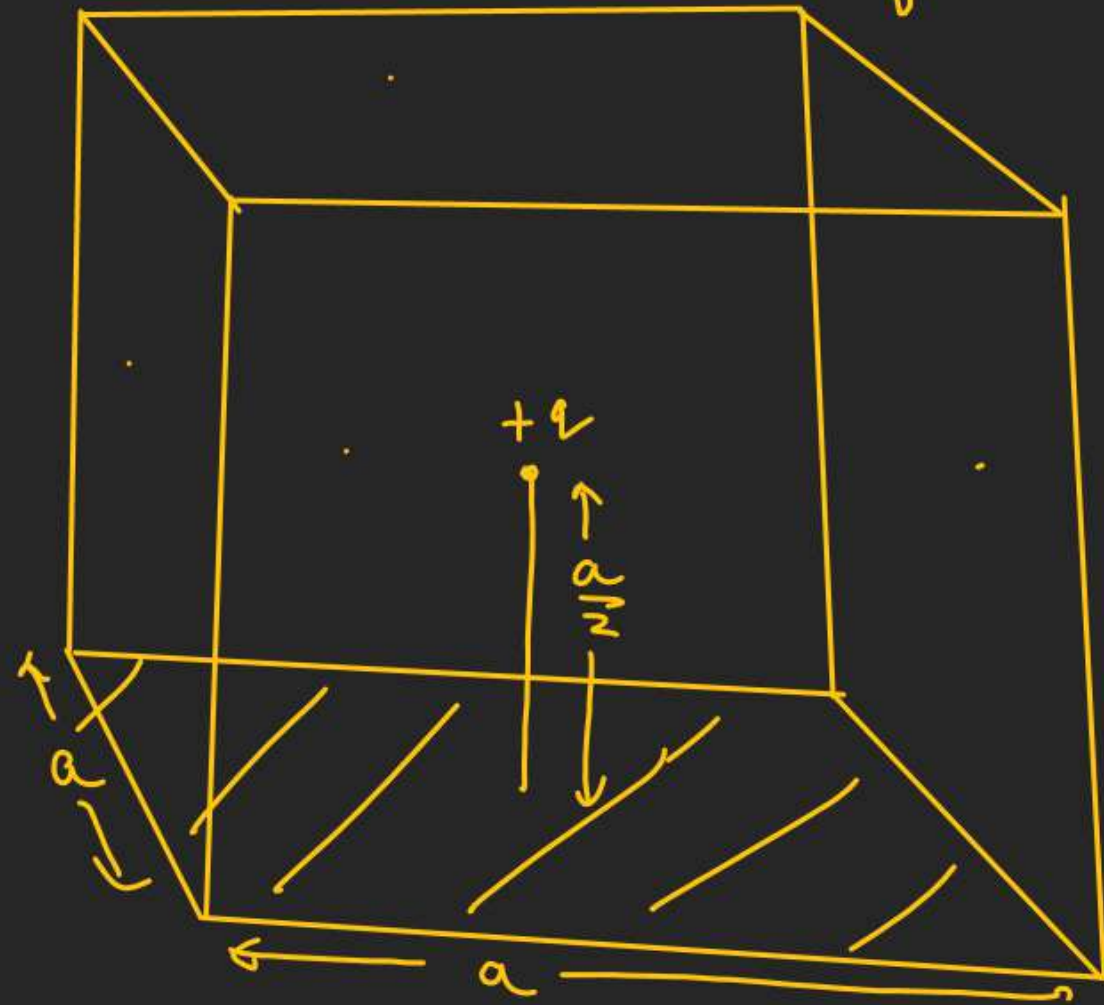
8 → Cubes



GAUSS'S LAW

$$\Phi_{\text{face}} = ?$$

$$\phi_{\text{cube}} = \frac{q}{\epsilon_0}, \quad \phi_{\text{each face}} = \frac{q}{6\epsilon_0} \checkmark$$



GAUSS'S LAW

Fig. shows an imaginary cube of side a . A uniformly charged rod of length a moves towards right at a constant speed v . At $t = 0$, the right end of the rod just touches the left face of the cube. Plot a graph between electric flux passing through the cube versus time. [ϕ v t]

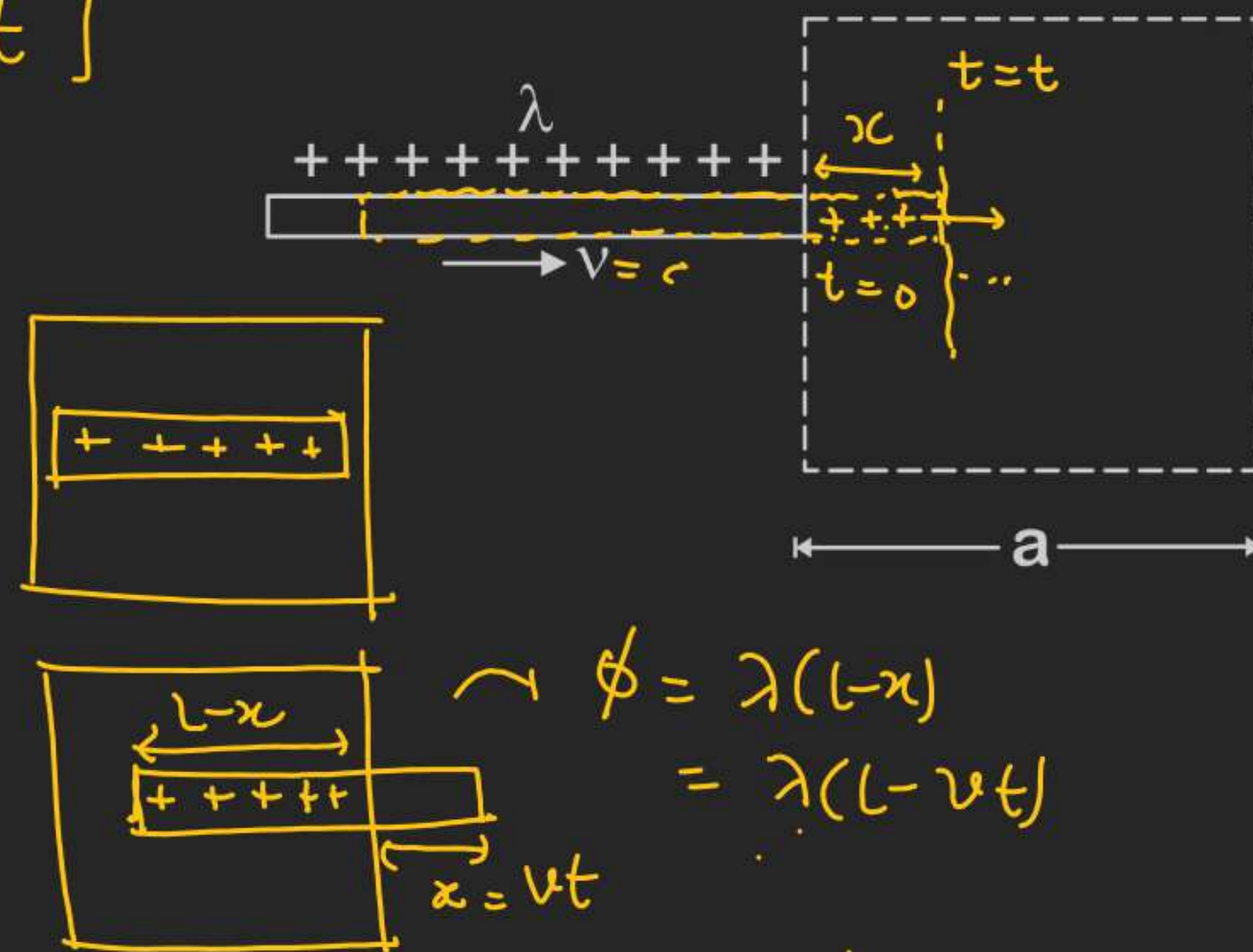
$$x = vt$$

$$(q_{\text{enc}})_{t=t} = \lambda \cdot x = \lambda v t$$

$$\phi_{\text{cube}} = \frac{(q_{\text{enc}})_{t=t}}{\epsilon_0} = \left(\frac{\lambda v}{\epsilon_0} \times t \right)$$

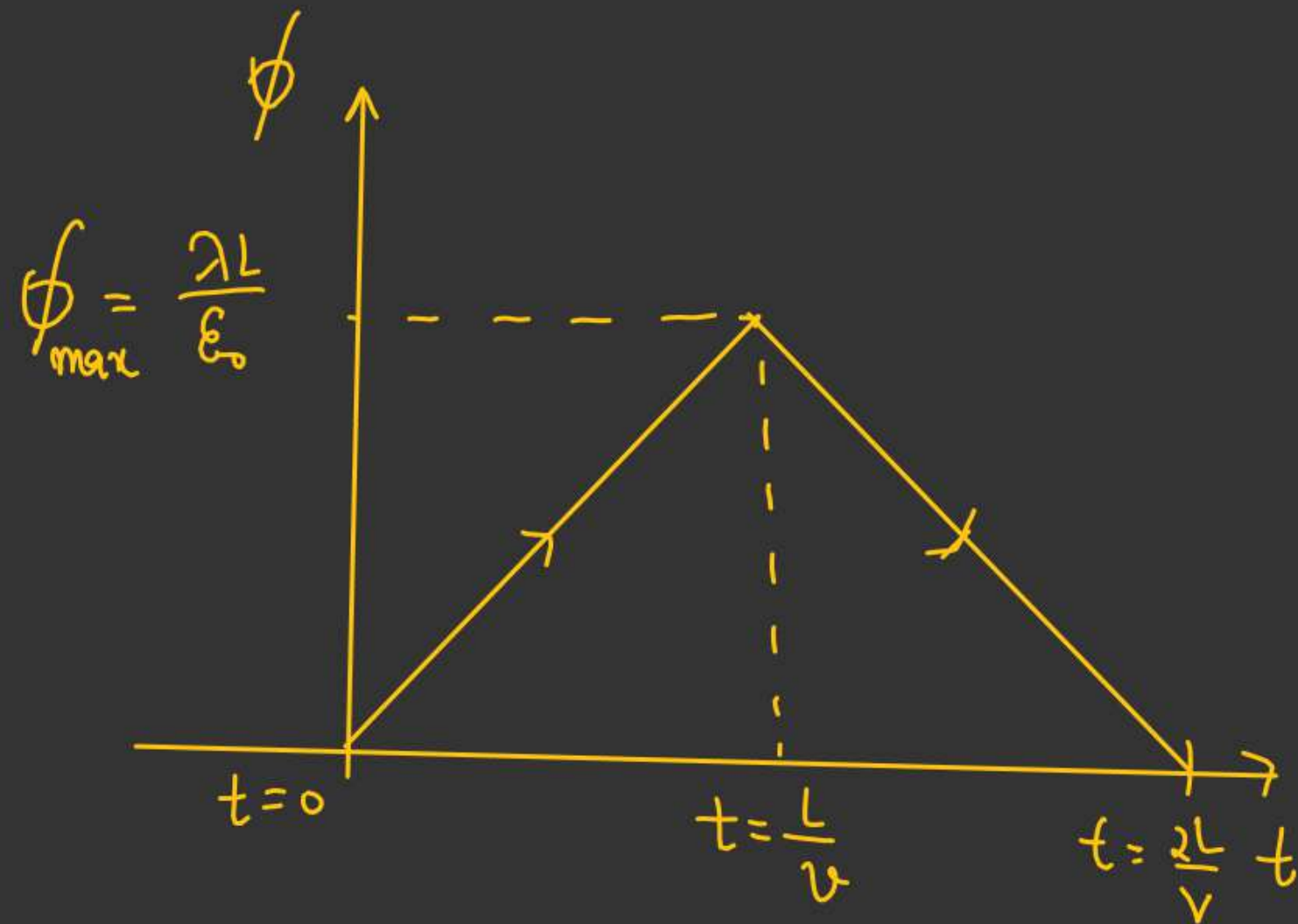
$$\phi_{\text{cube}} = \left(\frac{\lambda v}{\epsilon_0} \right) t$$

$$y = mx$$



$$\phi = \lambda(L-x)$$

$$= \lambda(L-vt)$$



GAUSS'S LAW

H.W.

The intensity of an electric field depends only on the coordinates x and y as follows,

$$\vec{E} = \frac{a(x\hat{i} + y\hat{j})}{x^2 + y^2}$$

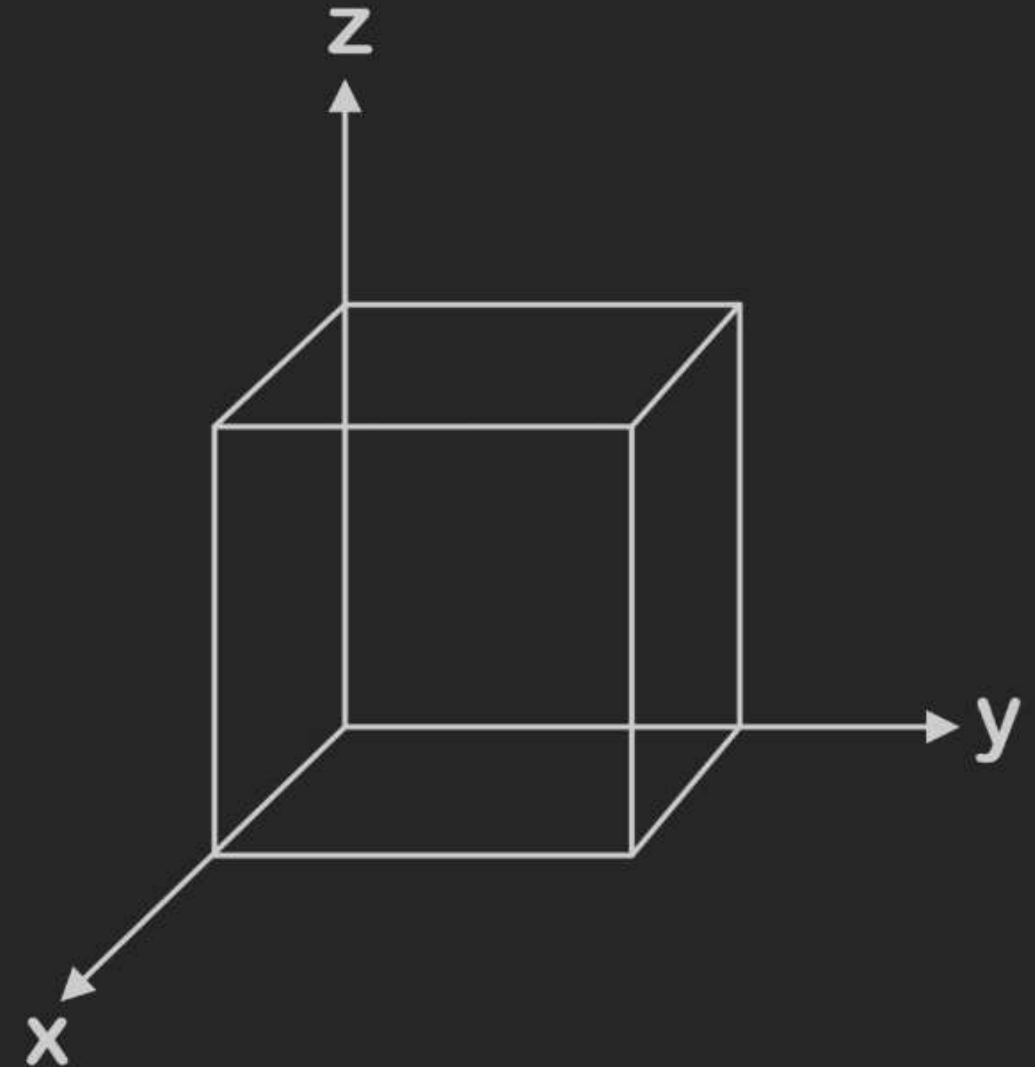
where, a is a constant and \hat{i} and \hat{j} are the unit vectors of the x and y axes.

Find the charge within a sphere of radius R with the centre at the origin.

GAUSS'S LAW

H.W.

Electric field in a region is given by $\vec{E} = -4x\hat{i} + 6y\hat{j}$. Find charge enclosed in the cube of side 1 m as shown in the diagram.



GAUSS'S LAW

Find flux through the cube if line charge is along body diagonal.

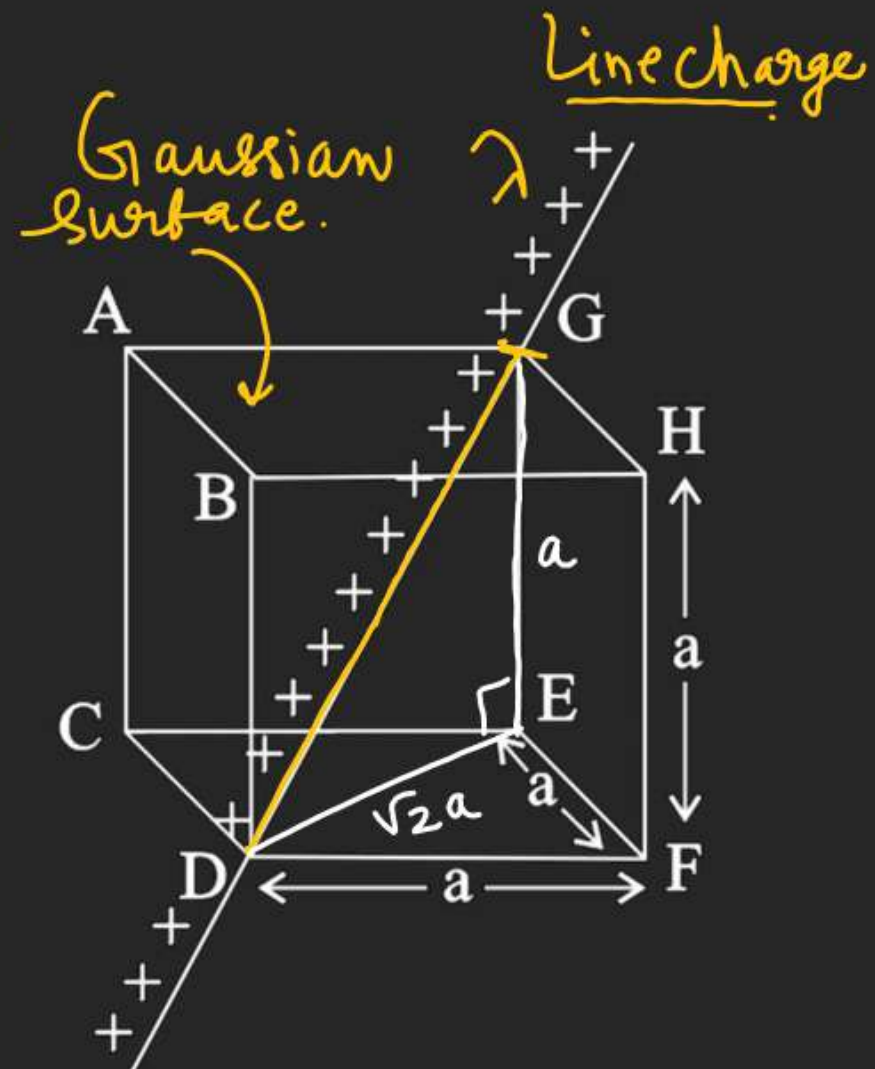
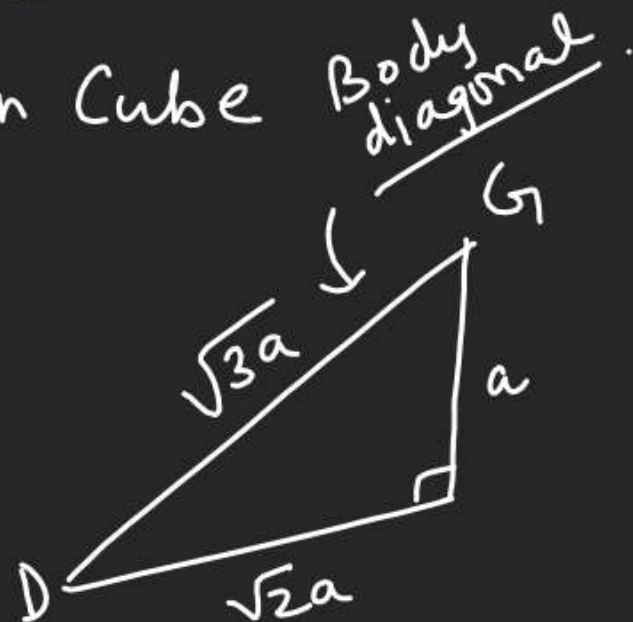
$$\Phi_{\text{cube}} = ?$$

Solⁿ

Charge enclosed within cube

$$\lambda \sqrt{3}a$$

$$\Phi_{\text{cube}} = \frac{\lambda \sqrt{3}a}{\epsilon_0}$$



GAUSS'S LAW

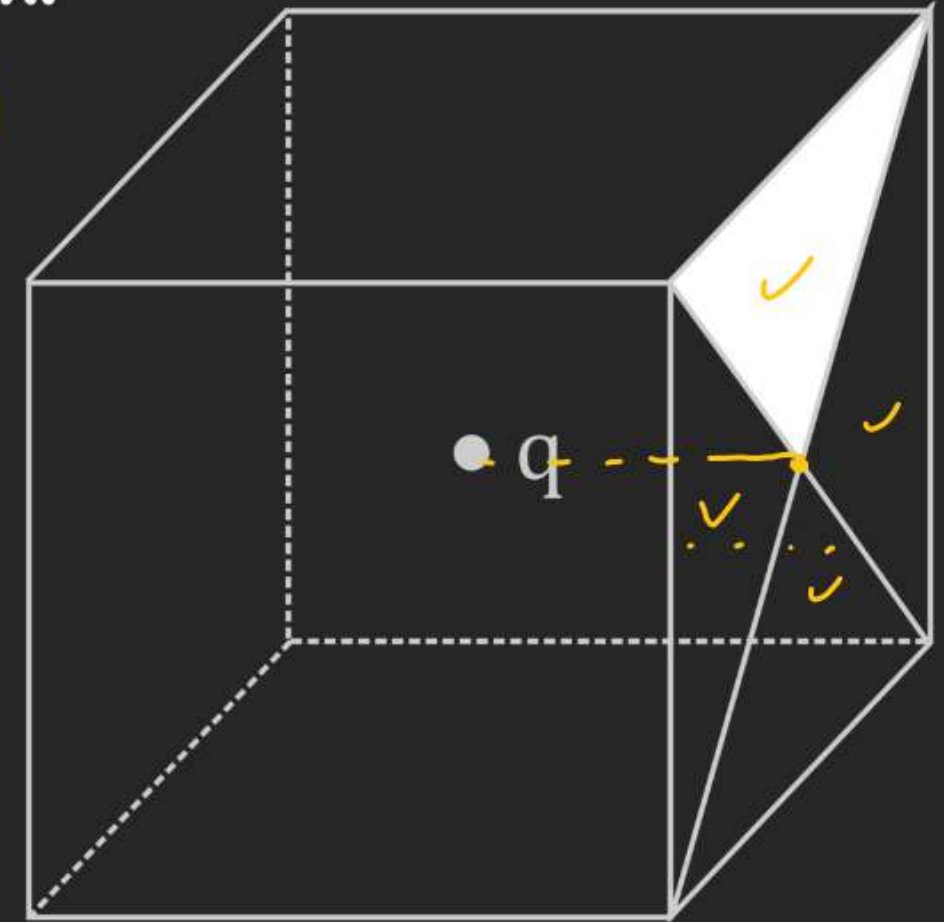
A point charge q is placed at the centre of the cubical box.

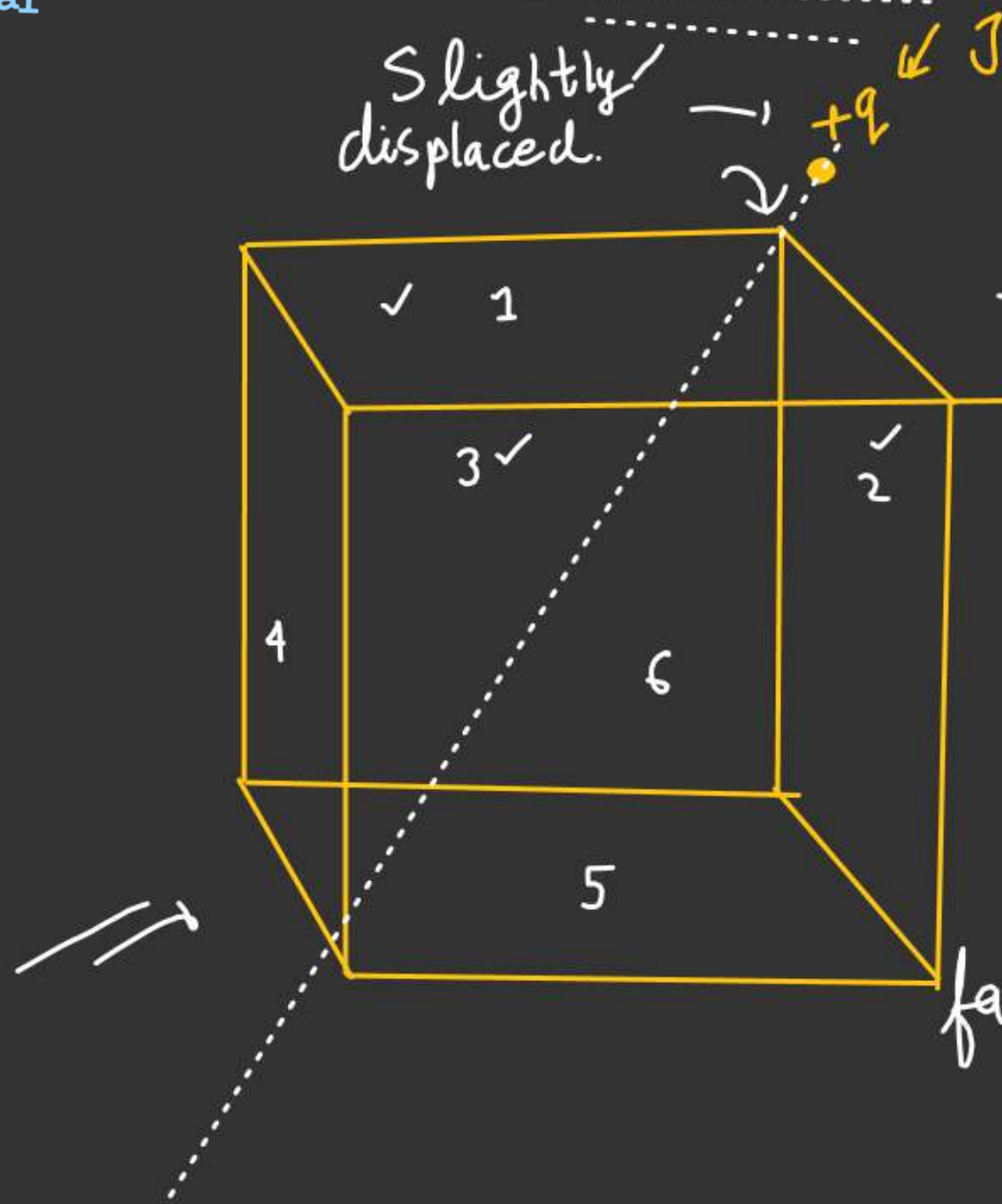
Find, (a) total flux associated with the box ✓ → $(\frac{q}{\epsilon_0})$

(b) flux emerging through each face of the box

(c) flux through shaded area of surface. $\hookrightarrow (\frac{q}{6\epsilon_0})$

$$\begin{aligned}\Rightarrow \phi &= \frac{\text{Flux through each face}}{4} \\ &= \frac{q}{24\epsilon_0} \checkmark\end{aligned}$$





Just outside the cube but location is along body diagonal.

→ Find flux through the cube. → 0

→ Find flux through the faces which contribute to the corner.

$$\phi_4 = \phi_5 = \phi_6 = \phi = \frac{q}{24\epsilon_0}$$

$$\phi_1 = \phi_2 = \phi_3 = \phi' = ??$$

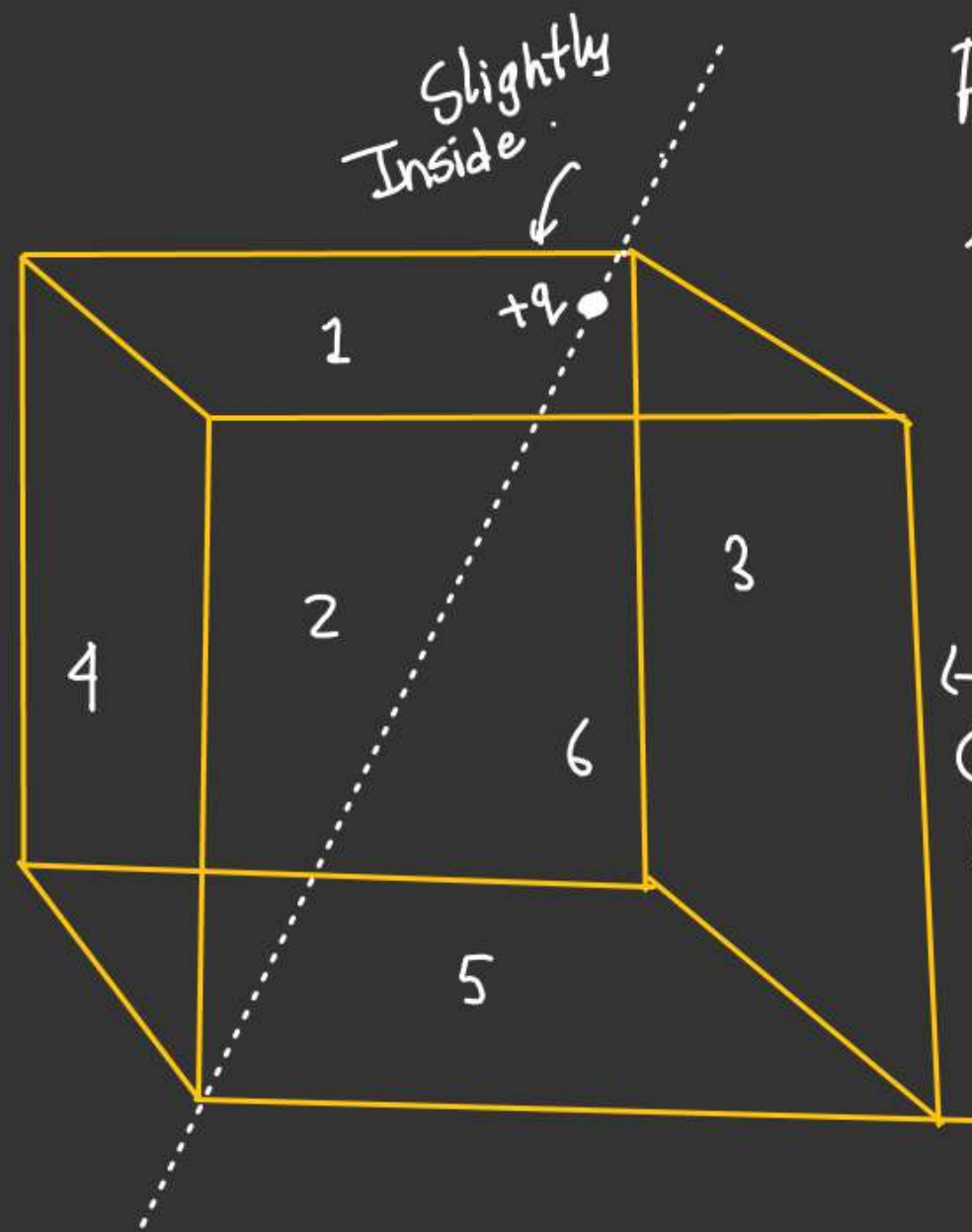
$$3(\phi + \phi') = 0$$

faces which contribute the corner

$$\phi_{\text{cube}} = 0$$

$$-\phi + \phi' = 0$$

$$\phi' = -\phi = \frac{-q}{24\epsilon_0}$$



Find flux through ^{each} faces which contributing towards the corner of the cube.

$$\phi_T = \frac{q}{\epsilon_0}$$

$$\phi_1 = \phi_2 = \phi_3 = \phi'$$

$$\phi_4 = \phi_5 = \phi_6 = \phi = \frac{q}{24\epsilon_0}$$

← Gaussian Surface

$$\phi' + \phi = \phi_T$$

$$3 \left[\phi' + \frac{q}{24\epsilon_0} \right] = \frac{q}{\epsilon_0}$$

$$\phi' + \frac{q}{24\epsilon_0} = \frac{q}{3\epsilon_0}$$

$$\underline{\phi'} = \frac{q}{3\epsilon_0} - \frac{q}{24\epsilon_0} = \frac{8q - q}{24\epsilon_0} = \frac{7q}{24\epsilon_0}$$