

0-1 5-12

5-1 7-12

$$\textcircled{8} \quad Z = 1 - \frac{a}{V_m RT}$$

$$\frac{P V_m}{RT} = Z$$

$$Z = 1 - \frac{a P}{Z (RT)^2}$$

$$Z = 1 - \frac{100 \times 0.1}{Z (20)^2}$$

$$(2Z - 1)^2 = 0$$

$$Z = 1 - \frac{1}{4Z}$$

$$4Z^2 = 4Z - 1$$

$$Z^2 - Z + \frac{1}{4} = 0$$

$$Z = \frac{+1 \pm \sqrt{1-1}}{2}$$

$$= \frac{1 + \cancel{0}}{2} = \frac{2 \cdot 4}{2}$$

$$= 0.5$$

$$(9) \quad Z = \frac{PV}{nRT}$$

$$\frac{PV}{n} = RT + Pb$$

$$PV = nRT + nPb$$

$$\boxed{\begin{array}{l} nRT = 40 \\ RT = 20 \end{array}}$$

(12)

$$Z = 1 + \frac{Pb}{RT}$$

$$\frac{b}{RT} = 0.01$$

$$b = 0.20$$

PV vs P

$$\frac{PV_m}{RT} = 1 + \frac{Pb}{RT}$$

$$PV_m = RT + Pb$$

Boyle's temperature  $\rightarrow$

$$\left(P + \frac{a}{V_m^2}\right)(V_m - b) = RT$$

$$\frac{V_m}{RT} \times \left[ P = \frac{RT}{V_m - b} - \frac{a}{V_m^2} \right]$$

$$Z = \frac{PV_m}{RT} = \frac{V_m}{V_m - b} - \frac{a}{V_m RT}$$

$$Z = \frac{1}{\left(1 - b/V_m\right)} - \frac{a}{V_m RT}$$

$$Z = \left(1 - b/V_m\right)^{-1} - \frac{a}{V_m RT}$$

$$(1-x)^{-1} = 1 + x + x^2 + \dots$$

$$\left(1 - \frac{b}{V_m}\right)^{-1} = 1 + \frac{b}{V_m} + \frac{b^2}{V_m^2} + \dots$$

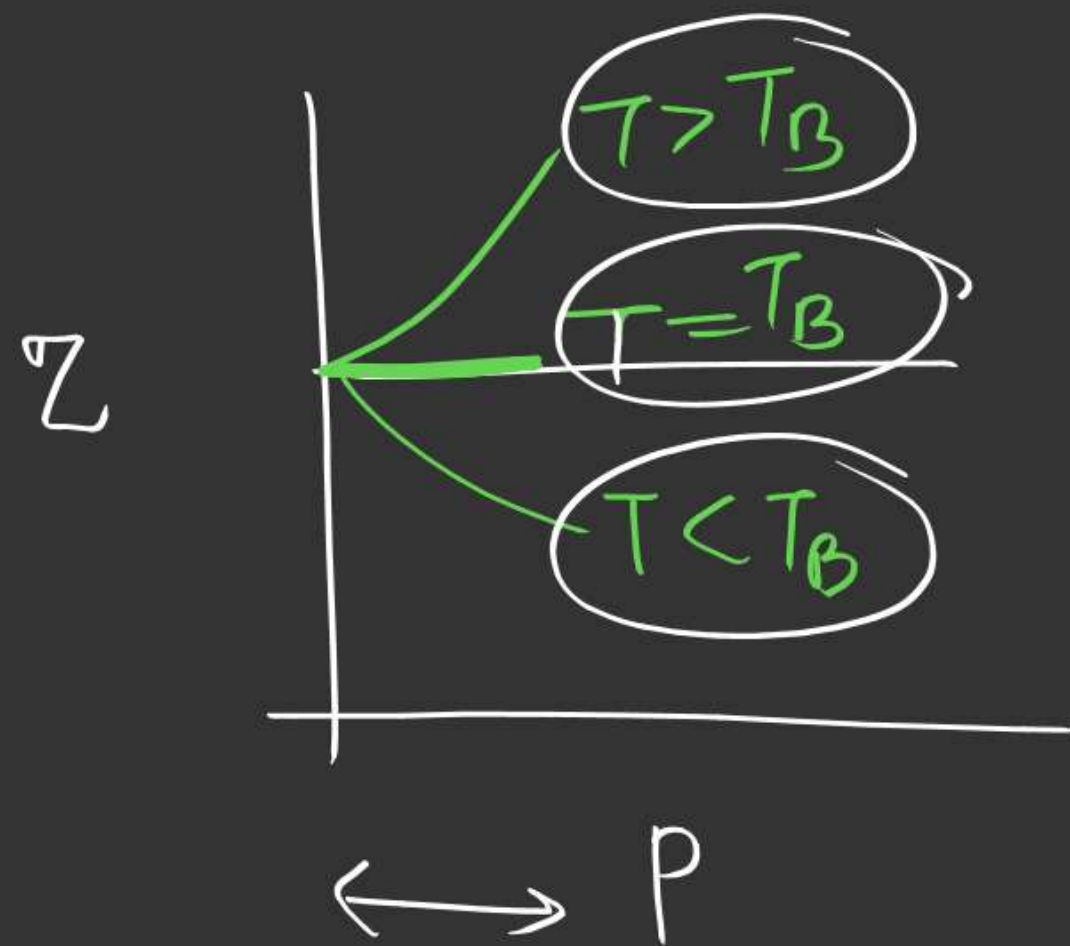
$$Z = 1 + \frac{b}{V_m} + \frac{b^2}{V_m^2} + \dots - \frac{a}{V_m RT}$$

$$Z = 1 + \left(b - \frac{a}{RT}\right) \frac{1}{V_m} + \frac{b^2}{V_m^2} + \dots$$

$$\boxed{P \rightarrow \text{low}} \quad b - \frac{a}{RT} = 0$$

$$\boxed{T_B = \frac{a}{Rb}}$$

$\boxed{T_B + \text{low } p} \rightarrow \text{Real gas} - \text{ideal gas}$



$$Z = 1 + \left( b - \frac{a}{RT} \right) \frac{1}{V_m} \quad \text{---}$$



Other eq<sup>n</sup> for real gases

① Berthlot eq<sup>n</sup>

$$\left(p + \frac{an^2}{TV^2}\right)(V - nb) = nRT$$

② Dieterici eq<sup>n</sup>

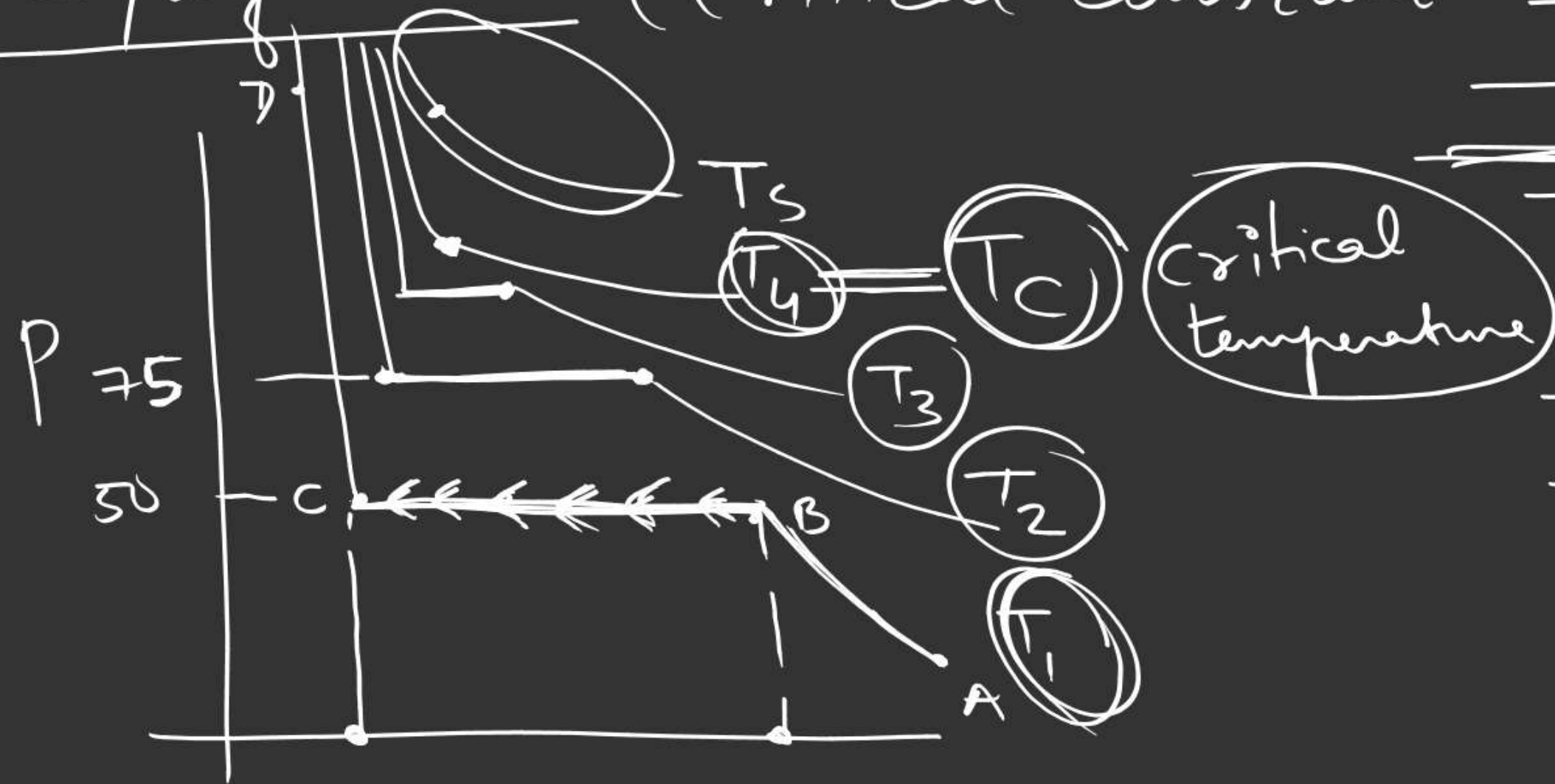
$$p e^{\frac{a}{V_m RT}} (V_m - b) = RT$$

### ③ Virial eq<sup>n</sup>

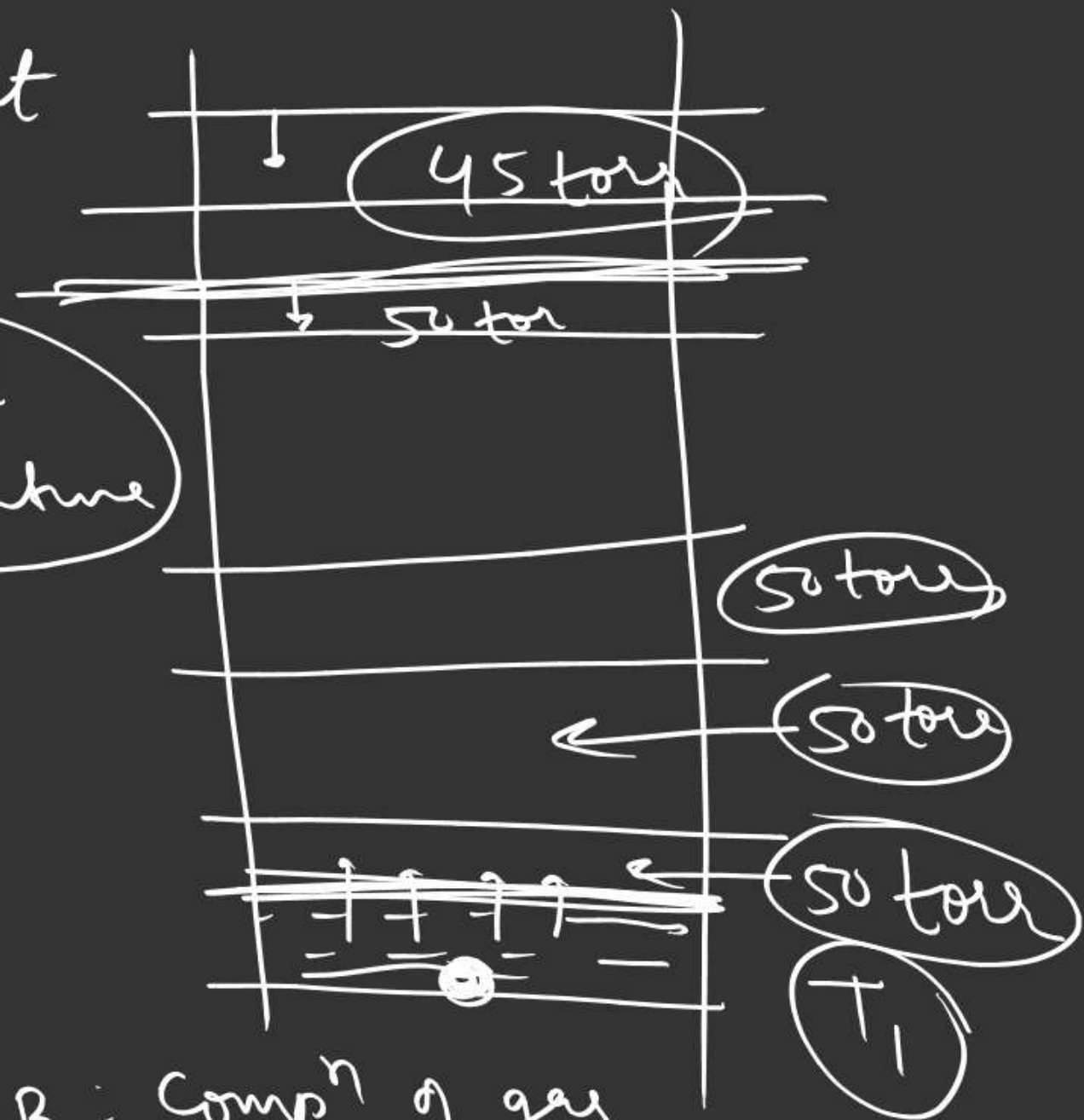
$$Z = 1 + \frac{B}{V_m} + \frac{C}{V_m^2} \dots \dots \dots$$

$B, C \dots$  are temperature dependent virial const  
which are determined experimentally

# Liquification (Critical Constant)



as  $T \uparrow$  vap pr  $\uparrow$



- AB : Comp<sup>n</sup> of gas
- BC : Condensation (liquification)
- CD : Comp<sup>n</sup> of liq

0-17

1, 2

3, 4,

J-Adv

2, 3, 4, 5, 6

10, 12, 13, 14, 15

Atomic str