

42 $e^- p \alpha$

$$\lambda = \frac{h}{\sqrt{2(m \cdot KE)}}$$

$$m_{proton} = 1840 m_e$$

$$m_\alpha = 4 m_{proton}$$

45
47
48

$$\lambda = \sqrt{\frac{150}{13.6 \times 8}}$$

40

—

-13.6

Li^{2+}
 13.6×9

$$KE = 13.6 \times 8 \text{ eV}$$

$$37) \phi = 40 \text{ eV}$$

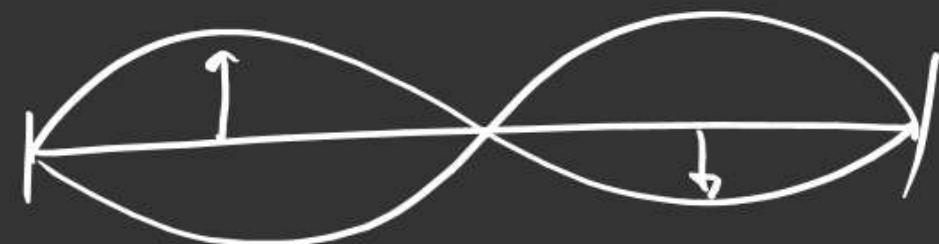
22 volt

$$KE_{\max} = \underline{22 \text{ eV}}$$

$$KE_{\max} - 22 = h\nu - 40$$

$$\underline{62 = h\nu}$$

Standing wave



$$2\pi r = n \lambda$$

$$2\pi \left(0.529 \frac{\eta^2}{z} A^0 \right) = n \lambda$$

$$\lambda = 2\pi \left(0.529 \frac{n}{z} \right) A^0$$



$$2\pi r = n \lambda$$

$$2\pi r = n \frac{h}{mv}$$

$$mv r = n \frac{h}{2\pi}$$

Heisenberg uncertainty principle.

→ It is impossible to determine the exact position and momentum of a microscopic particle (like e^-) simultaneously.

for minimum error

$$\Delta x \cdot \Delta p = \frac{h}{4\pi}$$

$$\Delta x \cdot \Delta p = \frac{h}{4\pi}$$

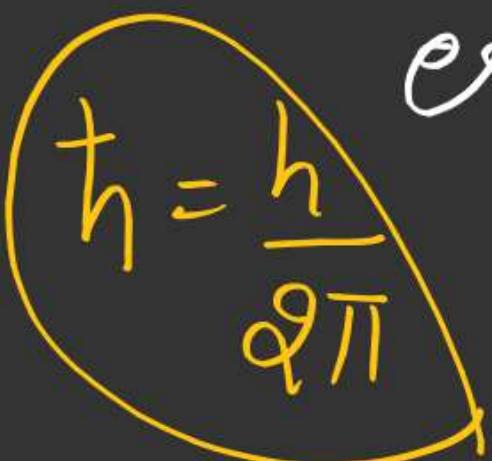
$$\Delta x \cdot \Delta v = \frac{h}{4\pi m}$$

↑
error in speed

error or uncertainty
in position

error in
momentum

$$\Delta x \cdot \Delta p = \frac{h}{4\pi}$$



Q. Calculate minimum error in velocity, if error in position is $\pm 1 \text{ A}^{\circ}$ for an e⁻.

$$\Delta x \cdot \Delta v = \frac{h}{4\pi m}$$

$$(10^{-10}) \cdot \Delta v = \frac{6.62 \times 10^{-34}}{4 \times \pi \times 9.1 \times 10^{-31}}$$

$$\Delta v = \frac{6.62}{4\pi \times 9.1} \times 10^7$$

Q. Calculate Δv if $\Delta x = 1 \text{ cm}$ for a particle having mass = 100 gm.

~~$10^{-2} \times 10^{-4}$~~

$$10^{-2} \times \Delta v = \frac{6.62 \times 10^{-34}}{4\pi \times 0.1}$$

$$\Delta v = \frac{6.62}{4\pi} \times 10^{31}$$

$$dx \cdot dp = \frac{h}{4\pi} \quad \left(\begin{array}{l} P = mv \\ dp = m dv \end{array} \right)$$

$$dx \cdot dv = \frac{h}{4\pi m} \quad \left(\frac{1}{2}mv^2 = \epsilon \right)$$

$$\underline{dx} \left(\frac{h}{\lambda^2} d\lambda \right) = \frac{h}{4\pi}$$

$$P = \frac{h}{\lambda}$$

$$dp = -\frac{h}{\lambda^2} d\lambda$$

$$\lambda = \frac{h}{mv} = \frac{h}{P}$$

error in
de broglie wavelength

Schrodinger eqⁿ:

- He considered the dual nature of particles.
- The wave associated with an e^- is considered to be a standing wave.

$$\left[\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + \frac{\partial^2 \psi}{\partial z^2} + \frac{8\pi^2 m(E - V)}{\hbar^2} \right] \psi = 0$$

$\psi = \text{Psi}$ = amplitude of
wave
or wave function

E = Total Energy
 V = Potential energy

$$\frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z} = \nabla = \text{nabla operator}$$

$$\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} = \nabla^2 = \text{Laplacian operator}$$

$$\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + \frac{\partial^2 \psi}{\partial z^2} = \nabla^2 \psi$$

$$\nabla^2 \psi + \frac{8\pi^2 m (\epsilon - v)}{\hbar^2} \psi = 0$$

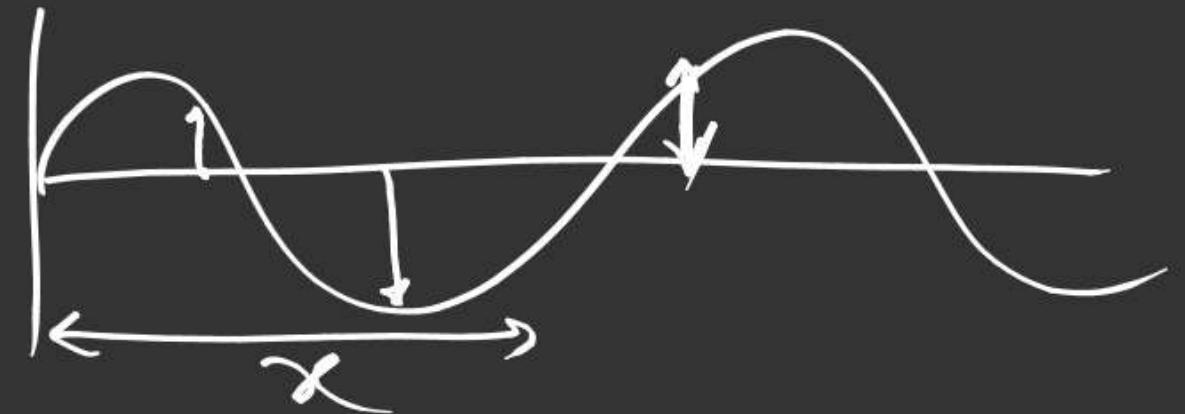
$$(\epsilon - v) \psi = - \frac{\hbar^2}{8\pi^2 m} \nabla^2 \psi$$

$$\epsilon \psi = - \frac{\hbar^2}{8\pi^2 m} \nabla^2 \psi + v \psi$$

$$\epsilon \psi = \left(- \frac{\hbar^2}{8\pi^2 m} \nabla^2 + v \right) \psi$$

$$\epsilon \psi = H \psi$$

Hamilton
operator



$$\frac{\partial^2 y}{\partial t^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial x^2}$$

$y = A \sin(\omega t - kx)$

displacement

O-I

45 - 54

S-I

41 - 53