

PERMUTATION & COMBINATION

Q. There are 6 roads between A & B and 4 roads between B & C.

(i) In how many ways can one drive from A to C by way of B? 6×4

(ii) In how many ways can one drive from A to C and back to A, passing through B on both trips? $6 \times 4 \times 4 \times 6$.

(iii) In how many ways can one drive the circular trip described in (ii) without using the same road more than once. $6 \times 4 \times 3 \times 5$



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90-5

Q. How many natural numbers are there from 1 to 1000 which have none of their digits repeated.

10 ——— 99 $11 \times 22 \times 33 \times 44 \times 55 \times 66 \times 77 \times 88 \times 99$

$$\begin{array}{c}
 \boxed{1} + \boxed{\begin{array}{c|c} 0 & a \\ \hline a & \end{array}} + \boxed{\begin{array}{c|c|c} 0 & 1 & \\ \hline & & \end{array}} \\
 \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\
 9 + 9 \times 9 + 9 \times 9 \times 8 \\
 9 + 81 + 648 = 738
 \end{array}$$

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Q. A family is being arranged in a line for a group photograph. If the family consists of a mother, a father, a baby and five children, the number of arrangements that begin and end with a parent is.

(A) 720

(B) 1440

(C) 5040

(D) 40320


$$\begin{aligned} & 2 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 \times 1 \\ & \hline & 720 \times 2 \\ & = 1440 \end{aligned}$$

PERMUTATION & COMBINATION

Q. (i) Find the number of four letter word that can be formed from the letters of the word HISTORY. (each letter to be used at most once)

(ii) How many of them contain only consonants?

(iii) How many of them begin & end in a consonant?

(iv) How many of them begin with a vowel?

(v) How many contain the letters Y?

(vi) How many begin with T & end in a vowel?

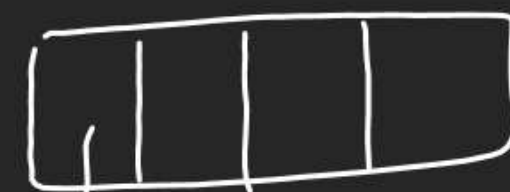
(vii) How many begin with T & also contain S?

(viii) How many contain both vowels?

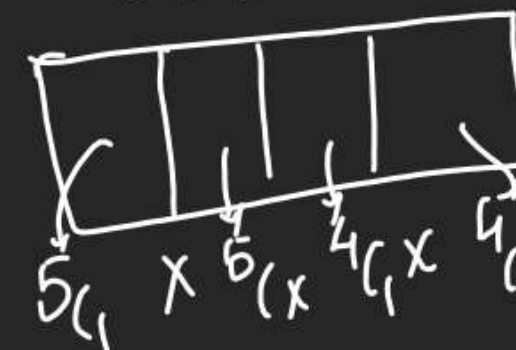
HISTORY



$$7C_1 \times 6C_1 \times 5C_1 \times 4C_1 = 7 \times 6 \times 5 \times 4$$



$$5 \times 4 \times 3 \times 2 =$$



3 (left)
2 Vowel



$$6 \times 5$$

(1,0)

OHSTRY



$$1 \times 5 \times 4 \times 2$$



$$2C_1 \times 6 \times 5 \times 4$$



$$4C_2 \times 2 \times 5 \times 4$$

(vii)



$$1 \times 3C_1 \times 1 \times 5 \times 4 = 60$$

PERMUTATION & COMBINATION

Q. If repetitions are not permitted

(i) How many 3 digit numbers can be formed from the six digits 2, 3, 5, 6, 7 & 9?

(ii) How many of these are less than 400?

(iii) How many are even?

(iv) How many are odd?

(v) How many are multiples of 5?

(4) $\begin{array}{|c|c|c|} \hline & & \text{odd} \\ \hline & & 3/5/7 \\ \hline \downarrow & & \downarrow \\ & & 9 \\ \hline \end{array}$
 $5 \times 4 \times 4 = 5 \times 4 \times 4 = 80$

(5) $\begin{array}{|c|c|c|} \hline & & 5 \\ \hline \downarrow & & \downarrow \\ & & 1 \\ \hline \end{array}$
 $5 \times 4 \times 1 = 20$

1) $\begin{array}{|c|c|c|} \hline & & \\ \hline \downarrow & & \\ & & \\ \hline \end{array}$
 $6 \times 5 \times 4$

2) $\begin{array}{|c|c|c|} \hline 2/3 & & \\ \hline \downarrow & & \\ & & \\ \hline \end{array}$
 $2 \times 5 \times 4$

3) $\begin{array}{|c|c|c|} \hline & & 2/6 \\ \hline & & \downarrow \\ & & \\ \hline \end{array}$
 $5 \times 4 \times 2$

PERMUTATION & COMBINATION

Q. Every telephone number consists of 7 digits. How many telephone numbers are there which do not include any other digits but 2, 3, 5 & 7?

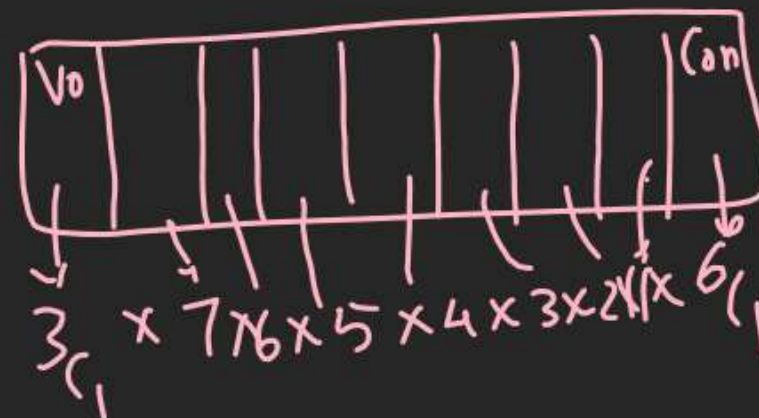
2, 3, 5, 7. ਇਹੋ ਟੈਲੀ ਨੰਬਰਾਂ



$4 \times 4 \times 4 \times 4 \times 4 \times 4 \times 4$

$$= 4^7$$

→ Automatically
Understood
Rep. allowed.

$$V = 0 \text{ A}$$
$$C \equiv L \cup R \sqcup HM$$


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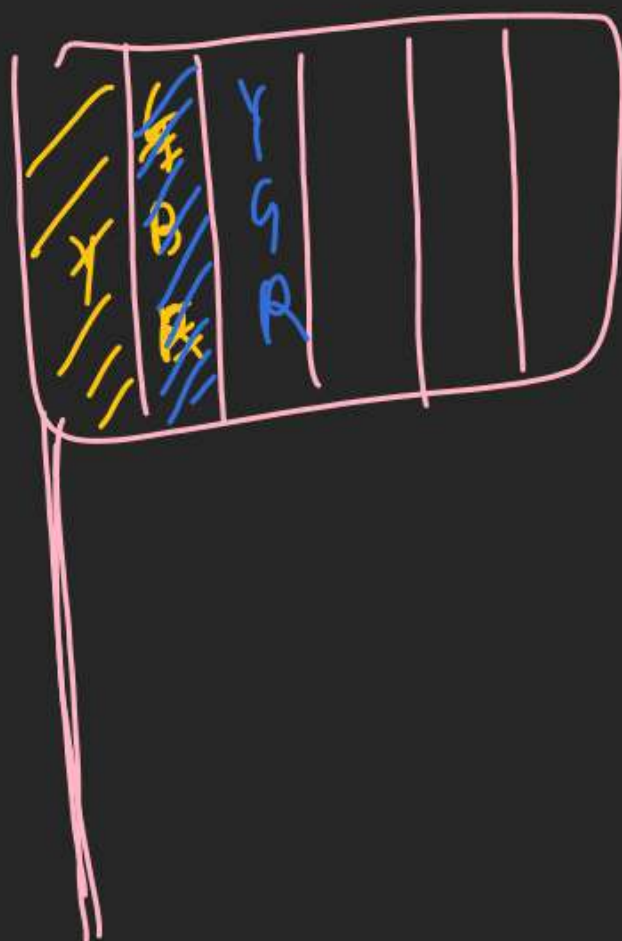
Q. A new flag is to be designed with six vertical strips using some or all of the Ach colours yellow, green, blue and red. Then, the number of ways this can be done such that no two adjacent strips have the same colour is

(A) 12×81

(B) 16×192

(C) 20×125

(D) 24×216



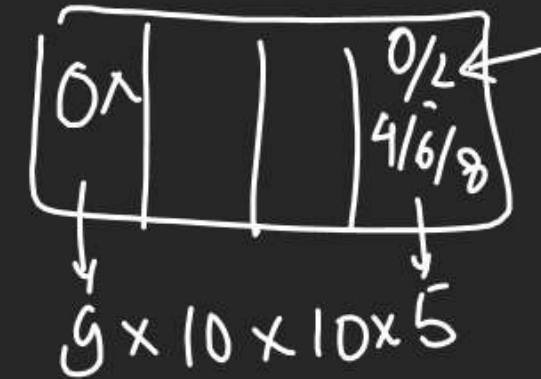
Y G B R

$${}^4_1 \times {}^3_1 \times {}^3_1 \times {}^3_1 \times {}^3_1 \times {}^3_1$$

$$(4 \times 3) \times (3 \times 3 \times 3 \times 3) = 24 \times 81$$

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Q. How many four digit numbers are there which are divisible by 2.



PERMUTATION & COMBINATION

Q. In a telephone system four different letter P, R, S, T and the four digits 3, 5, 7, 8 are used. Find the maximum number of "telephone numbers" the system can have if each consists of a letter followed by a four-digit number in which the digit may be repeated.

A

P/R				
S/T				

letter

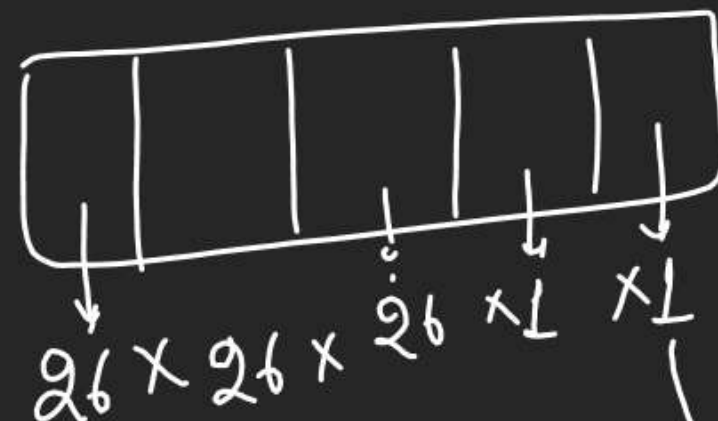
$$4 \times 4 \times 4 \times 4 \times 4 = 4^5 = 256$$

PERMUTATION & COMBINATION

Q. Find the number of 5 lettered palindromes which can be formed using the letters from the English alphabets.

malayalam.

ULTA SIDHA $\overline{\text{उल्टा सिधा}}$



$$= (26)^3$$

To 1st Place Pr

Aya vahi last Par
Aayega.

\Rightarrow 1 hi Tarika

N A Y A N

~~M A L Y A L A M~~ $\overline{\text{म ल य ल म}}$

J A H A J

A A A A A

S A S

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Q. Number of ways in which 7 different colours in a rainbow can be arranged if green is always in the middle.

V.I.B.G.Y.O.R.

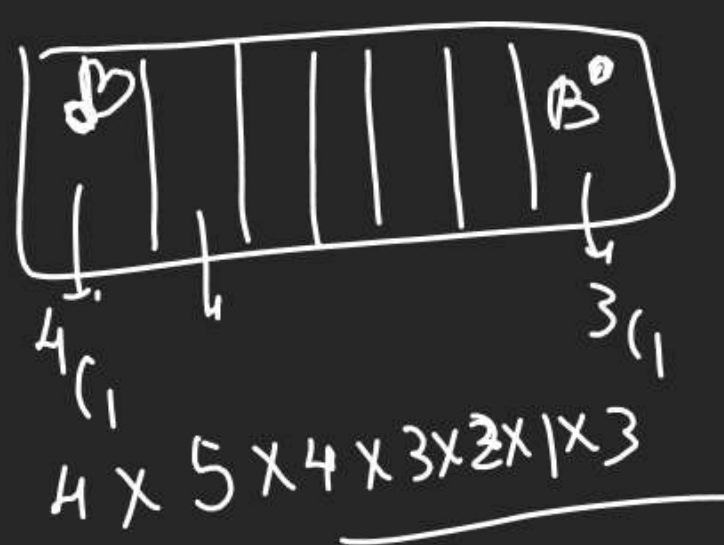


$6 \times 5 \times 4 \times 1 \times 3 \times 2 \times 1$

$= 720$

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Q. Find the number of ways in which 4 boys and 3 girls can be seated in a line if the terminal seats are occupied by the boys.



2B
3G

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Q. Numbers of words which can be formed using all the letters of the word

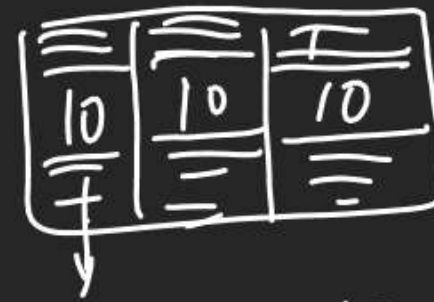
"AKSHI", if each word begins with vowel or terminates in vowel.

LATER

Venn diagram

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Q. A letter lock consists of three rings each marked with 10 different letters. Find the number of ways in which it is possible to make an unsuccessful attempts to open the lock.

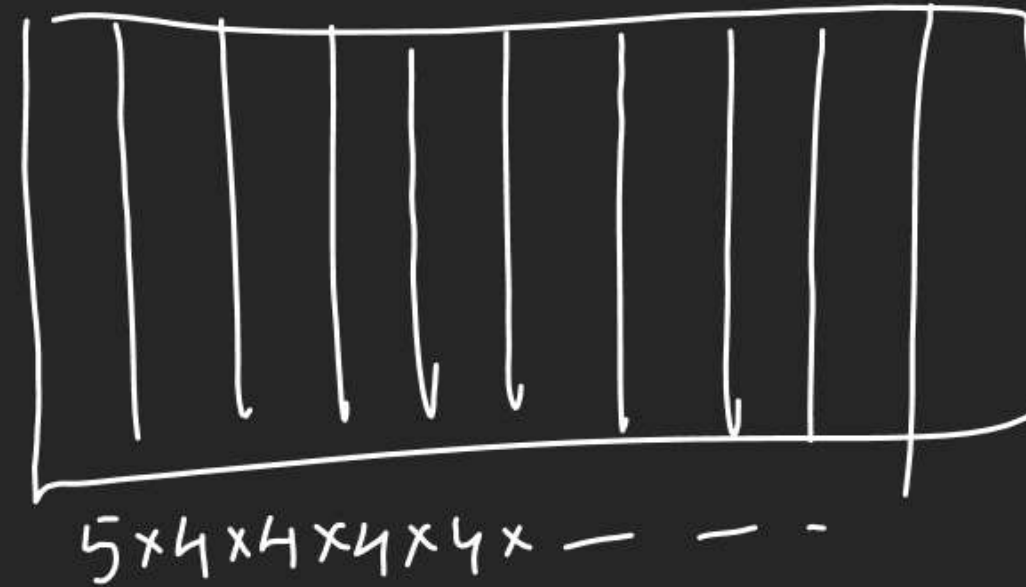


$$10 \times 10 \times 10 - \underset{\substack{\text{correct} \\ \text{option}}}{1} = 999$$

Unsuccessful Attempts

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Q. How many 10 digit numbers can be made with odd digits so that no two consecutive digits are same.

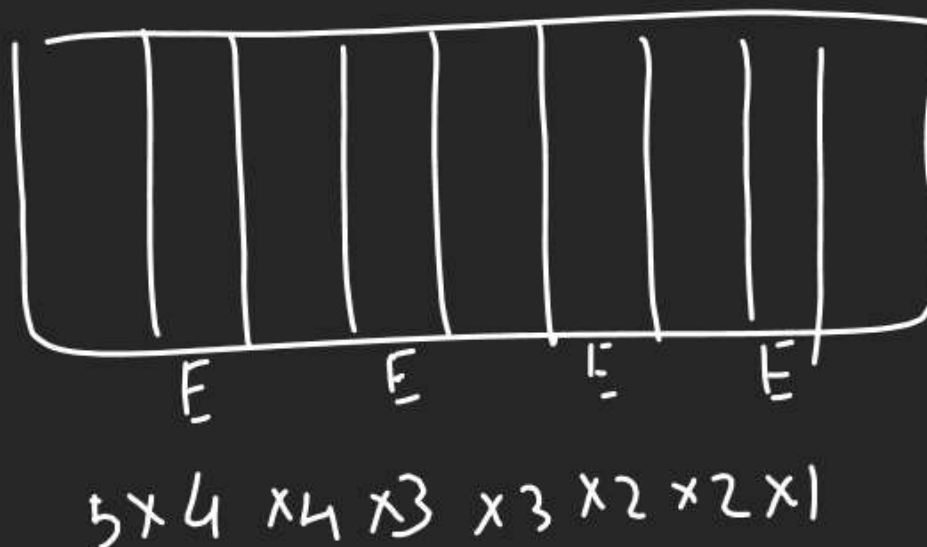


$$= 4^9 \times 5$$

1, 3, 5, 7, 9
Repeat for

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Q. It is required to seat 5 men and 4 women in a row so that the women occupy the even places. How many such arrangements are possible?



PERMUTATION & COMBINATION

Q. Find the number of three digits or four digit even numbers that can be formed from the number $\underline{2}, 3, 5, 6, 7$ (without repetition).

$$\begin{array}{|c|c|c|c|} \hline & & & 2/6 \\ \hline \end{array} + \begin{array}{|c|c|c|c|} \hline & & & 2/6 \\ \hline \end{array}$$
$$4 \times 3 \times 2 + 4 \times 3 \times 2 \times 2$$

$$24 + 48 = 72$$

Q I H M W can clear & clouded

days occur in a week

assuming that entire day
is either clear or clouded?

2^7

$$2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \\ = 2^7 = 128$$

Q For Visitors A, B, C, D arrive

at a town which has 5 hotels

In H M W can they dispense themselves
among 5 hotels, if 4 hotels are used to
accommodate them.

H₁ H₂ H₃ H₃ H₅

A B C D

$$5 \times 4 \times 3 \times 2 = 120$$

Q₃ HM 4 digit even

Nos can be made using
0, 1, 2, 3, 4, 5, 6.

RNA

$$\begin{array}{|c|c|c|c|} \hline & & & 0 \\ \hline \end{array} + \begin{array}{|c|c|c|c|} \hline 0x & 0x & & 2/4/6 \\ 4x & & & \\ \hline \end{array}$$

$$6 \times 5 \times 4 \times 1 + 5 \times 5 \times 4 \times 3$$

$$120 + 300 = 420$$

RA

$$\begin{array}{|c|c|c|c|} \hline 0x & & & 0 \\ \hline \end{array} + \begin{array}{|c|c|c|c|} \hline 0x & & & 2/4/6 \\ & & & \\ \hline \end{array}$$

$$6 \times 7 \times 7 \times 1 + 6 \times 7 \times 7 \times 3$$

$$= 6 \times 7 \times 7 \times 4$$

Q Using 0, 1, 2, 3, 4, 5, 6

How many 5 digits can be made

1) Greater than 24000

$$\begin{array}{|c|c|c|c|c|} \hline 2 & 4/5/6 & & & \\ \hline \end{array} + \begin{array}{|c|c|c|c|c|} \hline 3/4 & & & & \\ \hline \end{array}$$

$$\downarrow \quad \downarrow$$

$$1 \times 3 \times 7 \times 7 \times 7 + 4 \times 7 \times 7 \times 7 \times 7 - \textcircled{1} \text{ Jare}$$

24000 AA

(2) less than 54000

$$\begin{array}{|c|c|c|c|c|} \hline 5 & 0 & & & \\ \hline \end{array} + \begin{array}{|c|c|c|c|c|} \hline 2/3/4 & & & & \\ \hline \end{array}$$

$$\downarrow \quad \downarrow$$

$$1 \times 4 \times 7 \times 7 \times 7 + 4 \times 7 \times 7 \times 7 \times 7 = 32 \times 7^3$$

(3) No. Greater than 24000 less than 54000

$$\begin{array}{|c|c|c|c|c|} \hline 2 & 4/5/6 & & & \\ \hline \end{array} + \begin{array}{|c|c|c|c|c|} \hline 3/4 & & & & \\ \hline \end{array}$$

$$1 \times 3 \times 7 \times 7 \times 7 + 2 \times 7 \times 7 \times 7 \times 7$$

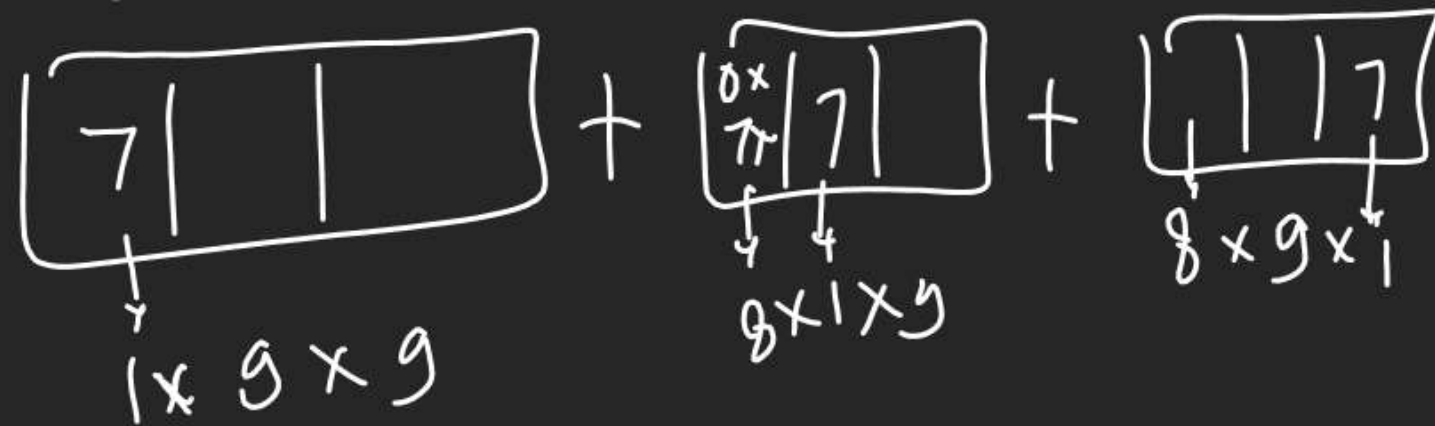
$$\begin{array}{|c|c|c|c|c|} \hline 5 & 0/1/2/3 & & & \\ \hline \end{array}$$

$$+ 1 \times 4 \times 7 \times 7 \times 7 - 1$$

$$\begin{array}{|c|c|c|c|c|} \hline 1 & 3 & 3 & 3 & 3 \\ \hline \end{array}$$

$$\begin{array}{|c|c|c|c|c|} \hline 4 & 3 & 2 & 5 & 6 \\ \hline \end{array}$$

Q Find No. of forming
3 digit No. containing
only one 7.



$$81 + 72 + 72 = 225 \underline{A}$$