

Q  $\sin(-65^\circ) = -\sin 65^\circ$

Q  $\cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$

$\cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 27^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$



$\sin(90-63^\circ) \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\sin 63^\circ}$

$+ \cos 63^\circ \times \frac{1}{\cos 63^\circ} = 1$



$\frac{\cos 0}{(+\cos 0)} + \frac{+\sin 0}{(+\sin 0)} + \frac{(+\cos 0)}{\cos 0}$

$1 + 1 + 1 = 3$

Q  $\frac{\cos 0}{\sin(90+0)} + \frac{\sin(-0)}{\sin(180+0)} - \frac{\tan(90+0)}{\cos 0}$

Q  $\frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ} = 3 + 2\sqrt{2}$

$$\sin(90+45) = +\cos 45$$

②

$$Q \sin(-65^\circ) = -\sin 65^\circ$$

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$$\cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 27^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$$



$$\sin(90-63^\circ) \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\sin 63^\circ}$$

$$+ \cos 63^\circ \times \frac{1}{\cos 63^\circ} = 1$$

$$\frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ}$$

$$\frac{\frac{1}{\sqrt{2}} + \left(+\frac{1}{2}\right)}{\frac{1}{\sqrt{2}} + \left(-\frac{1}{2}\right)} = \frac{\frac{\sqrt{2}+1}{2\sqrt{2}}}{\frac{\sqrt{2}-1}{2\sqrt{2}}}$$

$$= \frac{\sqrt{2}+1}{\sqrt{2}-1} \times \frac{\sqrt{2}+1}{\sqrt{2}+1}$$

$$= \frac{(\sqrt{2}+1)^2}{(\sqrt{2})^2 - 1^2} = \frac{2+1+2\sqrt{2}}{2-1} = 3+2\sqrt{2}$$

$$Q \frac{\sin 135^\circ - \cos 120^\circ}{\sin 135^\circ + \cos 120^\circ} = 3+2\sqrt{2}$$



Q  $\sin(-65^\circ) = -\sin 65^\circ$

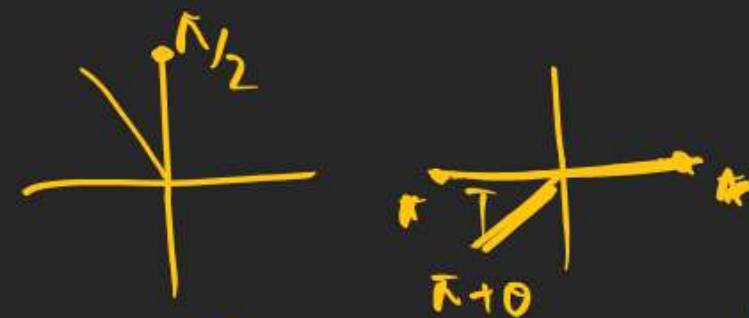
Q  $\cos 27^\circ \cdot \tan 27^\circ \cdot \tan 63^\circ \cdot \sec 63^\circ = ?$

$\cos 27^\circ \cdot \frac{\sin 27^\circ}{\cos 27^\circ} \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \cdot \sec 63^\circ$



$\sin(90-63^\circ) \cdot \frac{\sin 63^\circ}{\cos 63^\circ} \times \frac{1}{\sin 63^\circ}$

$+ \cos 63^\circ \times \frac{1}{\cos 63^\circ} = 1$



Q.  $\frac{\tan(90+\theta) \cdot \sec(180+\theta)}{\cos(180+\theta) \cdot \sec(-\theta)} = -1$

$\frac{(+\cancel{\cos}\theta) \cdot (+\cancel{\sec}\theta)}{(-\cancel{\cos}\theta) \cdot (-\cancel{\sec}\theta)}$

$= -1$

$$Q \quad 4 \tan^2 45^\circ - \sec^2 60^\circ + \sin^2 30^\circ = \frac{1}{4}$$

$$Q \quad \tan^2 \frac{\pi}{6} + \tan^2 \frac{\pi}{4} + \tan^2 \frac{\pi}{3} = \frac{13}{3}$$

$$Q_6 \quad 4 \times (1)^2 - (2)^2 + \left(\frac{1}{2}\right)^2$$

$$4 - 4 + \frac{1}{4} = \frac{1}{4}$$

$$Q_7 \quad \tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ$$

$$\left(\frac{1}{\sqrt{3}}\right)^2 + (1)^2 + (\sqrt{3})^2 = \frac{1}{3} + 1 + 3 = 4 + \frac{1}{3} = \frac{13}{3}$$

$$Q \quad \tan \theta + \tan(\pi - \theta) + \tan\left(\frac{\pi}{2} + \theta\right) - \tan(2\pi - \theta)$$

$$\tan \theta + (-\tan \theta) + (-\tan \theta) + (\tan \theta) = 0$$



## Complementary Angles

When Sum of 2 Angle =  $\frac{\pi}{2}$  both are Complementary Angle  
 (0 &  $90^\circ - \theta$ )

$$30^\circ \text{ \& } 60^\circ \checkmark$$

$$-30^\circ \text{ \& } 120^\circ \checkmark$$

$$\sin(90^\circ - \theta) = \cos \theta$$

$$\cos(90^\circ - \theta) = \sin \theta$$

$$\tan(90^\circ - \theta) = \cot \theta$$

$$\cot(90^\circ - \theta) = \tan \theta$$

$$\operatorname{cosec}(90^\circ - \theta) = \sec \theta$$

$$\sec(90^\circ - \theta) = \operatorname{cosec} \theta$$

sin, cos

tan, cot

sec cosec are Complementary Trigonometric

## Supplementary Angle

When Sum of 2 angles are  $180^\circ$

$$30^\circ, 150^\circ$$

$$90^\circ, 90^\circ$$

$$60^\circ, 120^\circ$$

$$-30^\circ, 210^\circ$$

Supplementary

(2)

$$\sin(\pi - \theta) = + \sin \theta$$

$$\cos(\pi - \theta) = - \cos \theta$$

$$\tan(\pi - \theta) = - \tan \theta$$

$$\cot(\pi - \theta) = - \cot \theta$$

$$\sec(\pi - \theta) = - \sec \theta$$

$$\operatorname{cosec}(\pi - \theta) = + \operatorname{cosec} \theta$$

Q If ABCD is cyclic Quad. then S.I.

$$\cos A + \cos B + \cos C + \cos D = 0$$

$$A + C = \pi, \quad B + D = \pi$$

$$\cos A + \cos B + \cos(\pi - A) + \cos(\pi - B)$$

$$\cancel{\cos A} + \cancel{\cos B} - \cancel{\cos A} - \cancel{\cos B}$$

$$= 0$$



① 1	$\sin 1^\circ > 0$	$\cos 1^\circ > 0$	$\tan 1^\circ > 0$
	$\sin 2^\circ > 0$	$\cos 2^\circ < 0$	$\tan 2^\circ < 0$
② 2	$\sin 3^\circ > 0$	$\cos 3^\circ < 0$	$\tan 3^\circ < 0$
	$\sin 4^\circ < 0$	$\cos 4^\circ < 0$	$\tan 4^\circ > 0$
3	$\sin 5^\circ < 0$	$\cos 5^\circ > 0$	$\tan 5^\circ < 0$
4	$\sin 6^\circ < 0$	$\cos 6^\circ > 0$	$\tan 6^\circ < 0$
4	$\sin 7^\circ > 0$	$\cos 7^\circ > 0$	$\tan 7^\circ > 0$

$$1^\circ \approx 57^\circ \rightarrow 1^{\text{st}}$$

$$2^\circ \approx 114^\circ \rightarrow 2^{\text{nd}}$$

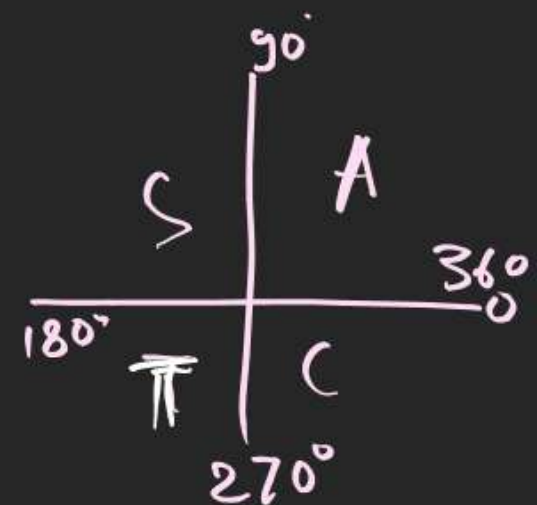
$$3^\circ \approx 171^\circ \rightarrow 2^{\text{nd}}$$

$$4^\circ = 228^\circ = 3^{\text{rd}}$$

$$5^\circ = 285^\circ = 4^{\text{th}}$$

$$6^\circ = 342^\circ = 4^{\text{th}}$$

$$7^\circ = 399^\circ = 1^{\text{st}}$$



$$Q \quad \sin 85^\circ = \cos 5^\circ \quad [T/F]$$

$\underbrace{\quad\quad\quad}_{90^\circ = \text{Sum}}$

$$Q \quad \tan 27^\circ = \cot 63^\circ \quad [T/F]$$

Comp.  $\underbrace{\quad\quad\quad}_{\text{Sum} = 90}$

5 - 85°  
1 17 Pairs

$$\tan 27^\circ = \tan(90 - 63^\circ) = \cot 63^\circ$$

$$Q \quad \frac{\cot 54^\circ}{\tan 36^\circ} + \frac{\tan 20^\circ}{\cot 70^\circ} = ?$$

$20^\circ + 70^\circ = 90^\circ$

$$54 + 36 = 90$$

$$\frac{\cancel{\cot 54^\circ}}{\cancel{\tan 36^\circ}} + \frac{\cancel{\tan 20^\circ}}{\cancel{\cot 70^\circ}} = 1 + 1 = 2$$

$$\begin{aligned} * \cot 54^\circ &= \cot(90 - 36^\circ) = \tan 36^\circ \\ \tan 20^\circ &= \tan(90 - 70^\circ) = \cot 70^\circ \end{aligned}$$

$$Q \quad \sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \sin^2 75^\circ + \sin^2 80^\circ + \sin^2 85^\circ + \sin^2 90^\circ$$

$\sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ \quad \cos^2 15^\circ + \cos^2 10^\circ + \cos^2 5^\circ + 1^2$

$$\frac{1 + 1 + 1 + \dots + 1 + \sin^2 45^\circ + 1}{\leftarrow 8 \text{ Pairs} \rightarrow} = \frac{8 + 1 + \frac{1}{2}}{2} = 9 + \frac{1}{2} = \frac{19}{2}$$

$$\begin{aligned} \sin 85^\circ &= \cos 5^\circ \\ \sin 80^\circ &= \cos 10^\circ \end{aligned}$$



$$\underline{\tan^2 5^\circ + \tan^2 10^\circ + \tan^2 15^\circ + \tan^2 20^\circ + \tan^2 25^\circ + \tan^2 30^\circ + \tan^2 35^\circ + \tan^2 40^\circ + \frac{1}{2} \tan^2 45^\circ + \tan^2 55^\circ + \tan^2 60^\circ + \tan^2 65^\circ + \tan^2 70^\circ + \tan^2 75^\circ + \tan^2 80^\circ + \tan^2 85^\circ + 1}$$

$$1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + \frac{1}{2} + 1 = 9.5$$

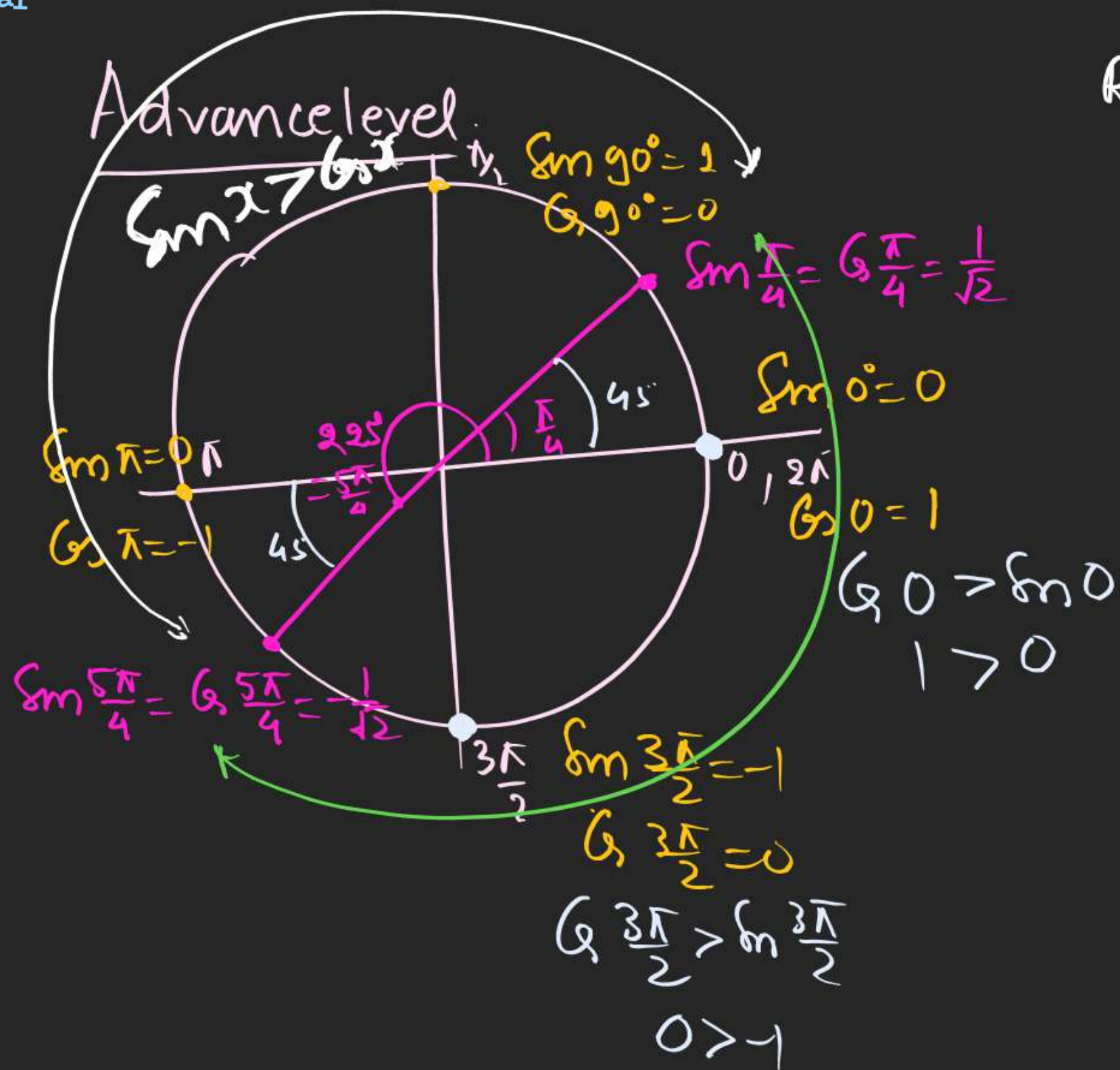
Q  $\sum_{r=1}^{89} \log_{10} (\tan r^\circ)$

$$\log_{10} \tan 1^\circ + \log_{10} \tan 2^\circ + \log_{10} \tan 3^\circ + \dots$$

$$\dots \log_{10} \tan 87^\circ + \log_{10} \tan 88^\circ + \log_{10} \tan 89^\circ$$

$$\begin{aligned} \tan 1^\circ \times \cot 1^\circ \\ \tan 0^\circ \times \cot 0^\circ \\ = 1 \end{aligned}$$

$$\begin{aligned} &= \log \left\{ \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 45^\circ \dots \tan 87^\circ \cdot \tan 88^\circ \cdot \tan 89^\circ \right\} \\ &= \log \left\{ \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 87^\circ \cdot \tan 88^\circ \cdot \tan 89^\circ \right\} \\ &\quad \text{44 Pairs} \\ &= \log \{1\} = 0 \end{aligned}$$



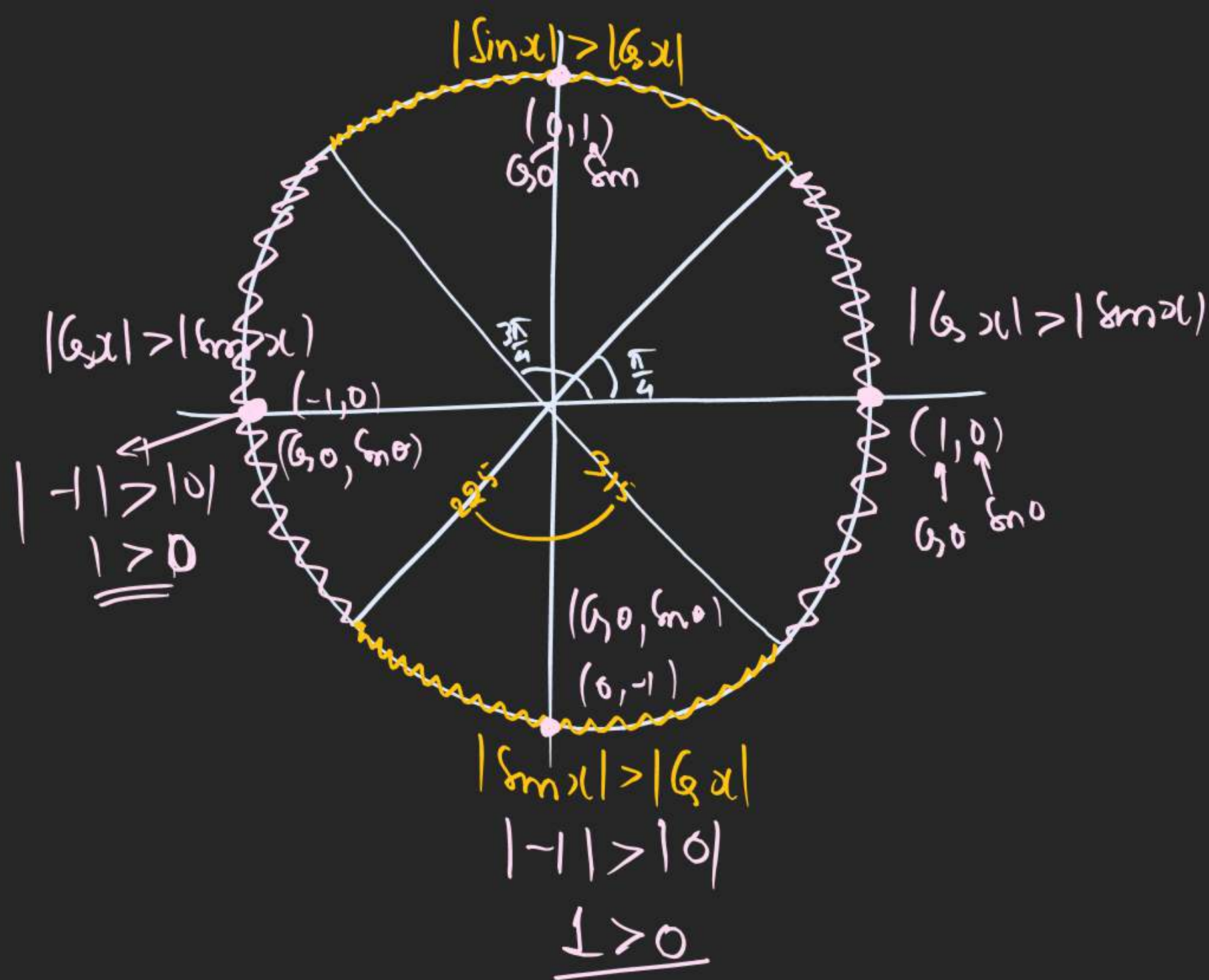
$R_k$

1)  $\theta \in (45^\circ - 225^\circ)$

$\theta \in \left(\frac{\pi}{4}, \frac{5\pi}{4}\right) \rightarrow \sin \theta > \cos \theta$

2)  $\theta \in \left(\frac{5\pi}{4}, \frac{\pi}{4}\right) \rightarrow \cos \theta > \sin \theta$





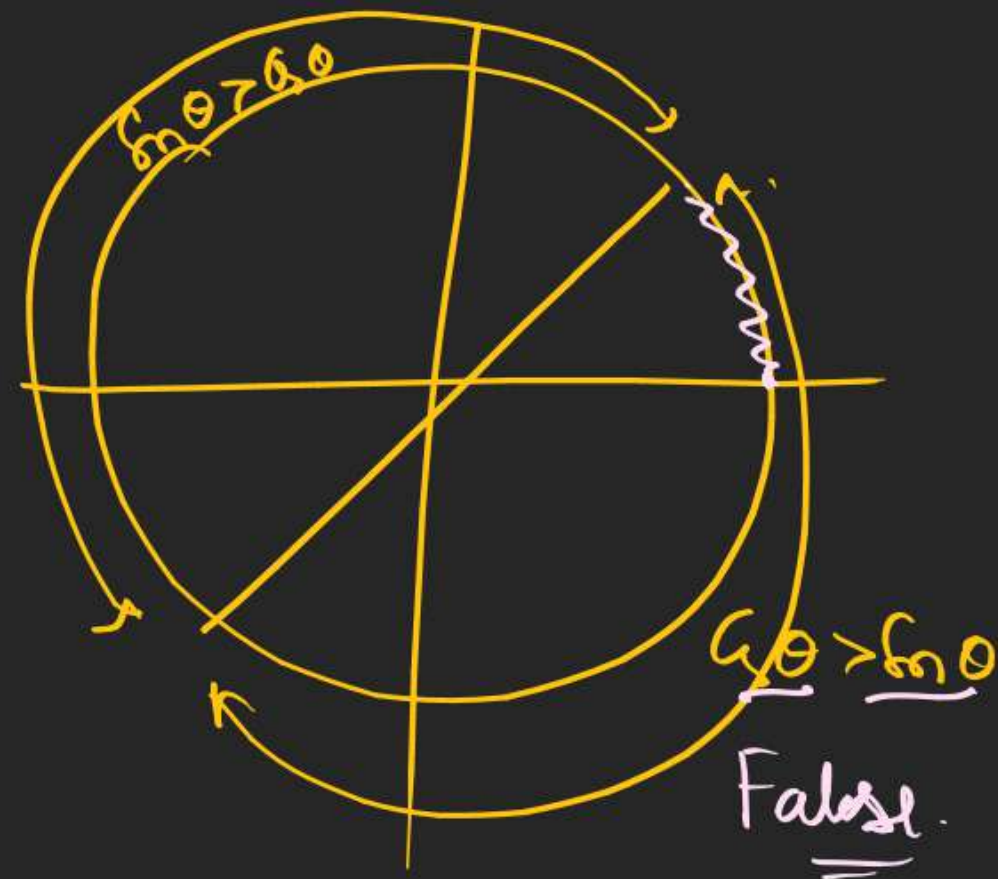
$$G\theta = x \text{ coord}$$

Q angle  $180^\circ < \theta < 360^\circ$  for what value  $\sin \theta = \cos \theta$ ?

$$\theta = 225^\circ$$

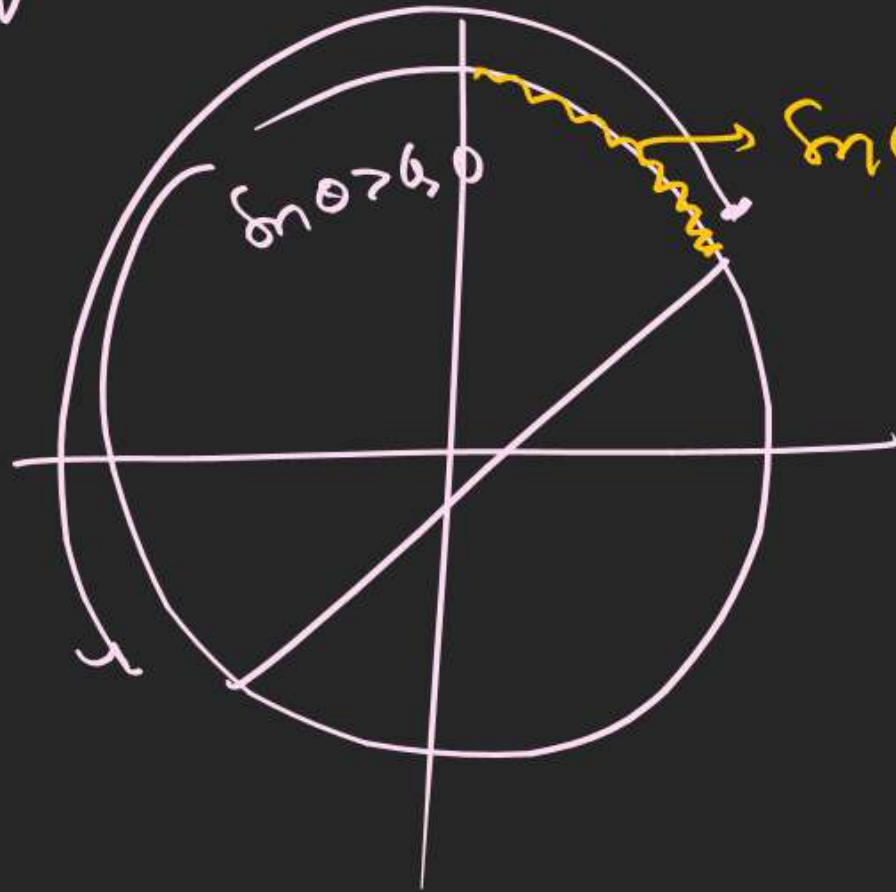


Q If  $\theta \in (0, 45^\circ)$  then  $\cos \theta < \sin \theta$  [T/F]?



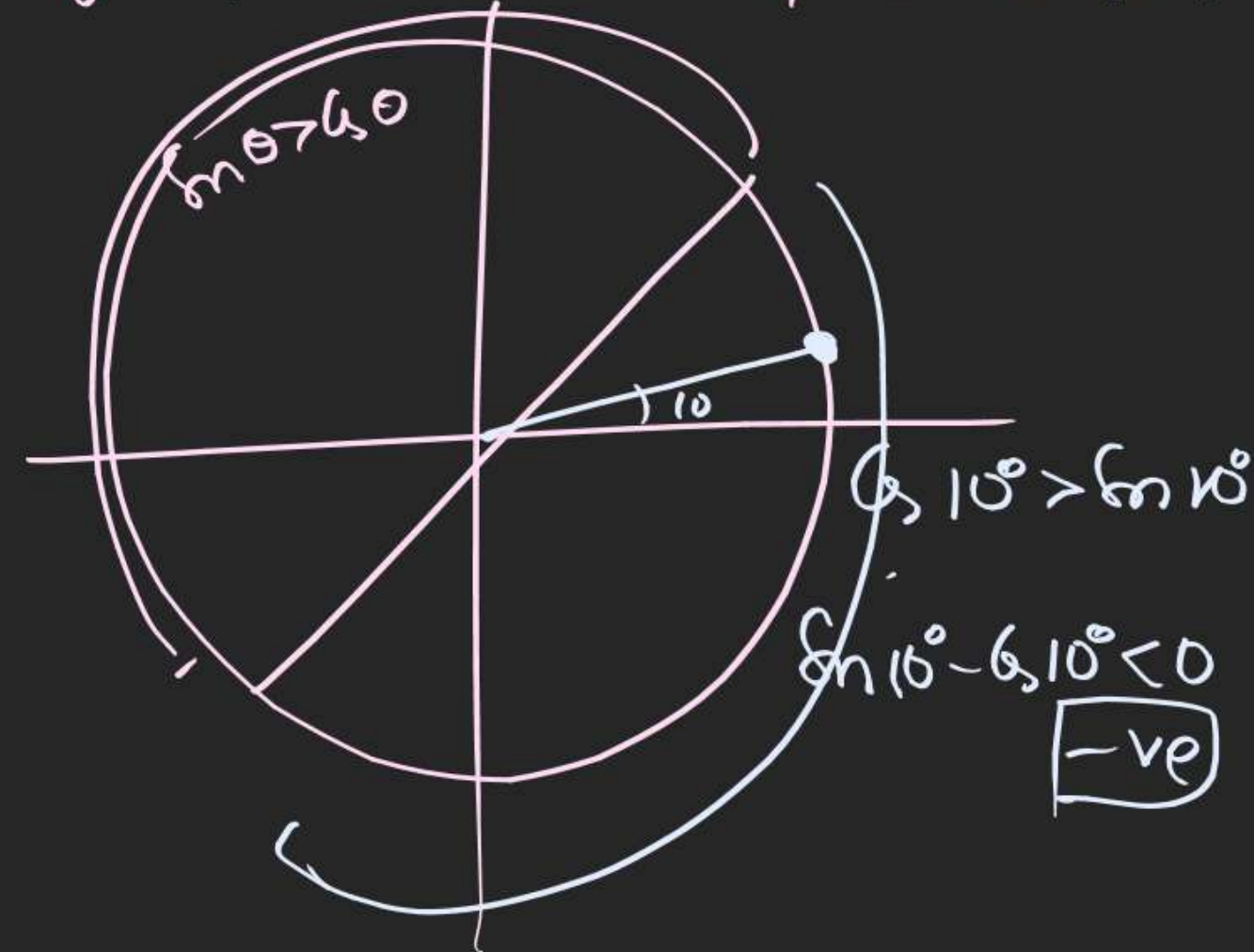


Q If  $\theta \in (45^\circ, 90^\circ)$  then  $\sin \theta < \cos \theta$  [T/F]



False  
or.  
 $\sin \theta > \cos \theta$

Q Sign of  $\sin 10^\circ - \cos 10^\circ$  + - 0 Not



Q For a Pentagon angles are

$$\theta_1 < \theta_2 < \theta_3 < \theta_4 < \theta_5$$

find value of

$$\frac{\sin(\theta_1 + \theta_2)}{\sin(\theta_3 + \theta_4 + \theta_5)} + \frac{\sin(\theta_1 + \theta_2 + \theta_3)}{\sin(\theta_4 + \theta_5)}$$

$$\text{Sum of all Interior Angle} = (n-2)\pi$$

$$= (5-2)\pi$$

$$\boxed{\theta_1 + \theta_2 + \theta_3 + \theta_4 + \theta_5 = 3\pi}$$

$$\theta_3 + \theta_4 + \theta_5 = 3\pi - (\theta_1 + \theta_2)$$

$$\theta_1 + \theta_2 + \theta_3 = 3\pi - (\theta_4 + \theta_5)$$

$$\frac{\sin(\theta_1 + \theta_2)}{\sin(3\pi - (\theta_1 + \theta_2))} + \frac{\sin(3\pi - (\theta_4 + \theta_5))}{\sin(\theta_4 + \theta_5)}$$

$$\frac{\sin(\theta_1 + \theta_2)}{\sin(\theta_1 + \theta_2)} + \frac{\sin(\theta_4 + \theta_5)}{\sin(\theta_4 + \theta_5)} = 1 + 1 = 2$$

$$\star \sin(3\pi - \theta) = +\sin \theta$$





## Adhe Se Kam / Aadhe Se Jyada

$$Q \left(1 + \cos \frac{\pi}{6}\right) \left(1 + \cos \frac{\pi}{3}\right) \left(1 + \cos \frac{2\pi}{3}\right) \left(1 + \cos \frac{5\pi}{6}\right)$$

$$\left(1 + \cos \frac{\pi}{6}\right) \left(1 + \cos \frac{2\pi}{6}\right) \left(1 + \cos \frac{4\pi}{6}\right) \left(1 + \cos \frac{5\pi}{6}\right)$$

$$,, \quad , \quad \left(1 + \cos \left(\pi - \frac{2\pi}{6}\right)\right) \left(1 + \cos \left(\pi - \frac{\pi}{6}\right)\right)$$

$$\left(1 + \cos \frac{\pi}{6}\right) \left(1 + \cos \frac{2\pi}{6}\right) \left(1 - \cos \frac{2\pi}{6}\right) \left(1 - \cos \frac{\pi}{6}\right)$$

$$\left(1^2 - \cos^2 \left(\frac{\pi}{6}\right)\right) \left(1^2 - \cos^2 \left(\frac{2\pi}{6}\right)\right)$$

$$\sin^2 \left(\frac{\pi}{6}\right) \cdot \sin^2 \left(\frac{2\pi}{6}\right)$$

$$\sin^2 30^\circ \times \sin^2 60^\circ = \left(\frac{1}{2}\right)^2 \times \left(\frac{\sqrt{3}}{2}\right)^2 = \frac{1}{4} \times \frac{3}{4} = \frac{3}{16}$$

Q 5 ज्ञात श्रृंखला में है

(1) last 2, 3 Dekho

(2) 3 नंबर Angle में  $Nr > \text{half of } Dr$  है जि  $(\pi - \theta)$  Ki tarah treat Karo

(4)  $\frac{4\pi}{6} \rightarrow Nr = 4$   
 $Dr = 6$  half  $= 3$   
 $Nr > Dr$  K half  
 $4 > 3$

$$5) \frac{4\pi}{6} = \frac{6\pi - 2\pi}{6} = \pi - \frac{2\pi}{6}$$

$$\frac{5\pi}{6} = \frac{6\pi - \pi}{6} = \pi - \frac{\pi}{6}$$