

Prilabko.

112 Progression.

[2-29]

Q4 Find sum of 20 terms of AP

if 2<sup>st</sup> term is 2 & 7<sup>th</sup> is 20.

$$a = 2, T_7 = a + 6d = 20$$

$$6d = 20 - 2$$

$$6d = 18$$

$$d = 3$$

$$S_{20} = \frac{20}{2} [2 \times 2 + (20-1) \times 3]$$

$$610$$

Q5 Find  $a = ?$  &  $d = ?$  if sum of 1st 5 terms is equal to 15 & sum of 1st 3 terms = -3.

$$S_5 = a + (a+d) + (a+2d) + (a+3d) + (a+4d) = 15$$

$$5a + 10d = 15$$

$$a + 2d = 3 \rightarrow ①$$

$$S_3 = a + (a+d) + (a+2d) = -3$$

$$3a + 3d = -3$$

$$a + d = -1 \rightarrow ②$$

$$a + 2d = 3 \rightarrow ①$$

$$\begin{array}{r} \\ -d = -4 \Rightarrow \end{array} \boxed{d = 4}$$

$$a + 4 = -1$$

$$\boxed{a = -5}$$

$Q_{10}$  How many terms of an AP must be taken for their sum to be equal to 91, if its 3<sup>rd</sup> term is 9 & difference betw 7<sup>th</sup> & 2<sup>nd</sup> term is 20?

Let 1) Sum of  $n$  terms = 91

$$S_n = 91$$

2)  $a + 2d = 9$

(3)  $(a + 6d) - (a + d) = 20$

$$5d = 20$$

$$\boxed{d = 4}$$

$$\boxed{4 = 1}$$

$$\frac{n}{2} \left[ 2a + (n-1)d \right] = 91$$

$$n + 2n^2 - 2n = 91$$

$$2n^2 - n - 91 = 0$$

$$2n^2 - 14n + 13n - 91 = 0$$

$$2n(n-7) + 13(n-7) = 0$$

$$n = 7, \left(\frac{13}{2}\right) \times$$

$Q_8$  Sum of Sqr of 5<sup>th</sup> & 11<sup>th</sup> term of an AP is 3

& Prod of 2<sup>nd</sup> by 14<sup>th</sup> = K Find the Prod

of 1<sup>st</sup> by 15<sup>th</sup> of this Progression.

1)  $(a+4d)^2 + (a+10d)^2 = 3$

$$2a^2 + 116d^2 + 28ad = 3$$

$$a^2 + 14ad + 26d^2 = \frac{3}{2}$$

2)  $(a+d)(a+13d) = K$

$$a^2 + 14ad + 13d^2 = K \times 2$$

$$2a^2 + 28ad + 26d^2 = 2K$$

$$90d^2 = 3 - 2K$$

less      (3)  $a \times (a+14d) = a^2 + 14ad$

$$= 2K - 26 \left( \frac{3-2K}{90} \right)$$

# Khushiyani Hi Khushiyani!!

Q Sum of 1<sup>st</sup> 2<sup>nd</sup> terms of an AP

2, 5, 8, ... is equal to sum of 1<sup>st</sup>  
n terms of AP 57, 59, 61, ... then n = ?

Sum of 1<sup>st</sup> 2<sup>nd</sup> terms of AP<sub>1</sub> = Sum of 1<sup>st</sup> n terms of AP<sub>2</sub>

$$\frac{2n}{2} [2 \cdot 2 + (2n-1) \times 3] = \frac{n}{2} [2 \cdot 57 + (n-1) \times 2]$$

$$8 + 12n - 6 = 114 + 2n - 2$$

$$10n = 110$$

$$\underline{n = 11}$$

Q How many terms of series

54 + 51 + 48 + 45 + ... have sum = 513.

let sum of n terms = 513.

$$\frac{n}{2} [2 \times 54 + (n-1) \times (-3)] = 513$$

$$108n - 3n^2 + 3n = 1026$$

$$3n^2 - 111n + 1026 = 0$$

$$n^2 - 37n + 342 = 0$$

$$(n-18)(n-19) = 0$$

$$\underline{\underline{n = 18, 19}}$$

Both answers are correct

$$\begin{array}{l} 4+3+2+1 = 10 \\ \swarrow \text{4 terms} \end{array}$$

$$\begin{array}{l} 4+3+2+1+0 = 10 \\ \swarrow \text{5 terms} \end{array}$$

Q Find AP sum of 1st 4 terms = 56.

Sum of last 4 terms = 112, if  $a=11$

Find No of terms in AP.

$$1) \rightarrow a + (a+d) + (a+2d) + (a+3d) = 56.$$

$$4a + 6d = 56$$

$$2a + 3d = 28 \rightarrow ①$$

$$3d = 28 - 22 = 6 \Rightarrow d=2$$

$$2) l + (l-d) + (l-2d) + (l-3d) = 112$$

$$4l - 6d = 112$$

$$2l - 3d = 56 \rightarrow ②$$

$$2l = 56 + 3 \times 2 = 62$$

$$l = 31$$

$$n = \frac{l-a}{d} + 1 = \frac{31-11}{2} + 1 = 11$$

Q Find Sum of series.

$$1^2 - 2^2 + 3^2 - 4^2 + 5^2 - 6^2 + 7^2 - \dots - 2002^2 + 2003^2 = ?$$

$$1 + (3^2 - 2^2) + (5^2 - 4^2) + (7^2 - 6^2) - \dots - (2003^2 - 2002^2)$$

$$1 + (3-2)(3+2) + (5-4)(5+4) + (7-6)(7+6) - \dots - \frac{(2003-2002)}{(2003+2002)}$$

$$1 + 5 + 9 + 13 + 17 - \dots - 4005$$

$$n = \frac{4005-1}{4} + 1 = 1001 + 1 = 1002$$

$$\therefore S_n = \frac{1002}{2} [1 + 4005]$$

$$= \underbrace{1002 \times 2003}$$

Q) Let  $S_n = \sum_{k=1}^{4n} (-1)^{\frac{(k)(k+1)}{2}} \cdot k^2$  then  $S_n$  (ans be 1056 1088 1120 1332).

$$S_n = (-1)^{\frac{1 \times 2}{2}} \cdot 1^2 + (-1)^{\frac{2 \times 3}{2}} \cdot 2^2 + (-1)^{\frac{3 \times 4}{2}} \cdot 3^2 + (-1)^{\frac{4 \times 5}{2}} \cdot 4^2 + (-1)^{\frac{5 \times 6}{2}} \cdot 5^2 + (-1)^{\frac{6 \times 7}{2}} \cdot 6^2 + \dots + (-1)^{\frac{(4n)(4n+1)}{2}} \cdot (4n)^2$$

$\leftarrow 4n \text{ terms}$

$$S_n = \underbrace{(-1)^1 \cdot 1^2}_{-1 \times 1^2} + \underbrace{(-1)^3 \cdot 2^2}_{-1 \times 2^2} + \underbrace{(-1)^6 \cdot 3^2}_{-1 \times 3^2} + \underbrace{(-1)^{10} \cdot 4^2}_{-1 \times 4^2} + \underbrace{(-1)^{15} \cdot 5^2}_{-1 \times 5^2} + \underbrace{(-1)^{21} \cdot 6^2}_{-1 \times 6^2} + \dots$$

$$S_n = -1^2 - 2^2 + 3^2 + 4^2 - 5^2 - 6^2 + 7^2 + 8^2 - 9^2 - 10^2 + 11^2 + 12^2 - 13^2 - 14^2 + 15^2 + 16^2 - \dots$$

$$= (\underbrace{3^2 - 1^2}_{2n \text{ terms}}) + (\underbrace{4^2 - 2^2}_{2n \text{ terms}}) + (\underbrace{7^2 - 5^2}_{2n \text{ terms}}) + (\underbrace{8^2 - 6^2}_{2n \text{ terms}}) + (\underbrace{11^2 - 9^2}_{2n \text{ terms}}) + (\underbrace{12^2 - 10^2}_{2n \text{ terms}}) + (\underbrace{15^2 - 13^2}_{2n \text{ terms}}) + (\underbrace{16^2 - 14^2}_{2n \text{ terms}}) + \dots$$

$$= (3-1)(3+1) + (4-2)(4+2) + (7-5)(7+5) + (8-6)(8+6) + (11-9)(11+9) + (12-10)(12+10) + (15-13)(15+13) + (16-14)(16+14) + \dots$$

$$= 2 \left\{ 4+6 + 12+14 + 20+22+28+\dots \right\} = 2 \left\{ (4+12+20+28+\dots) + (6+14+22+30+\dots) \right\}$$

$$= 2 \left\{ \frac{n}{2} (2 \times 4 + (n-1) \cdot 8) \right\} + \left\{ \frac{n}{2} (2 \times 6 + (n-1) \cdot 8) \right\} = 2n ((4n) + (4n+2)) = 4n (4n+1) - \begin{cases} n=1 & 28 \times 29 \\ n=2 & 32 \times 33 = 1056 \\ n=3 & 36 \times 37 = 1332 \end{cases}$$

Q If No of terms in AP are even & Sum of odd terms

is 24 & Sum of even terms = 30 & last term exceeds

the first term by  $\frac{21}{2}$  find n.

$$1) T_1 + T_3 + \dots = 24 \rightarrow x$$

$$T_2 + T_4 + \dots = 30 \rightarrow y$$

$$nd = y - x$$

$$nd = 6$$

$$(2) (a + (2n-1)d) - (a) = \frac{21}{2}$$

$$2nd - d = \frac{21}{2}$$

$$2d - d = \frac{21}{2} \Rightarrow d = \frac{3}{2}$$

$$n \times \frac{3}{2} = 6 \Rightarrow n = \frac{12}{3} = 4$$

① Whenever ap has

Sum of even & sum of  
odd terms = take No of  
terms =  $2n$

$$(2) T_1 + T_3 + T_5 + \dots = X \Rightarrow \frac{n}{2} [2a + (n-1)d] = X$$

$$T_2 + T_4 + T_6 + \dots = Y \Rightarrow \frac{n}{2} [2(a+d) + (n-1)d] = Y$$

$$\frac{n}{2} \left\{ (2a + nd - d) - (2a + 2d + nd - d) \right\} = X - Y$$

$$\frac{n}{2} \times (-2d) = X - Y$$

$$nd = Y - X$$

Imp Note

## Properties of AP.

1) Sum of Equidistant term Remain Same in AP

$$a_1, a_2, a_3, a_4, a_5, a_6 \rightarrow AP$$

$$a_1 + a_6 = a_2 + a_5 = a_3 + a_4 = K$$

$$(2) \quad a_1, a_2, a_3, \dots, a_n \rightarrow AP,$$

$$b_1, b_2, b_3, \dots, b_n \rightarrow AP$$

$$a_1 + b_1, a_2 + b_2, a_3 + b_3, \dots, a_n + b_n = AP$$

$$(3) \quad a_1, a_2, a_3, \dots, a_n \rightarrow AP$$

$$a_1 + K, a_2 + K, a_3 + K, \dots, a_n + K = AP$$

$$\frac{a_1}{K}, \frac{a_2}{K}, \frac{a_3}{K}, \dots, \frac{a_n}{K} \rightarrow AP$$

$$K \cdot a_1, K \cdot a_2, \dots, K \cdot a_n \rightarrow AP$$

(4) Superposition of term.

$$3 \text{ term} \rightarrow \underline{a-d, a, a+d}$$

$$4 \text{ term} \rightarrow a-3d, a-d, a+d, a+3d$$

$$5 \text{ term} \rightarrow a-2d, a-d, a, a+d, a+2d$$

$$(5) \quad 3, 5, 7, 9, \dots, d=2 \uparrow AP$$

$$9, 7, 5, 3, \dots, d=-2 \downarrow AP$$

$$3, 3, 3, 3, \dots, d=0 \quad AP$$

$a-2d, a-d, a+d, a+2d$   $\xrightarrow{AP}$

When  
Sum is given

