

# Inducing Universal Access to Privately Managed Social Interest Goods via Location Decisions

Javier Elizalde (U. Navarra)

Amaya Erro (UPNA)

Diego Ruiz-Hernández (CUNEF)

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# Research fields

- Economics, Industrial Organization
  - Competition
  - Regulation
- Location
- Effects of the location choice on
  - Competition
  - Prices
  - Level of provision
  - Welfare

# Outline

- 1) Introduction
- 2) Analytical approach
- 3) Problem formulation
- 4) Analytical insights

# Introduction

- Universal service obligations (e.g. public utilities, Laffont and Tirole (2000))
  - Universal access / full coverage
  - Uniform prices (no price discrimination)
- Nature of decision
  - Economic (network effects)
  - Political
    - Redistribution: consumers with low income, remote location or limited geographical mobility
    - Regional planning: limit congestion, maintain rural habitat

# Introduction

- On-site services
  - Health care, education, community services
  - Mill pricing
  - Transport costs → paid by the consumer
- Home-delivered services
  - Electricity, gas, water, postal services
  - Most often natural monopolies
  - Delivered pricing
  - Transport costs → paid by the provider
- Uniform prices
  - Price discrimination, often unpopular (e.g. British Gas, 1998)
  - Uniform mill prices (on-site services)
  - Uniform delivered prices (home-delivered services)

# Related literature

- **Operations research → universal acces through location** (covering problems, no price analysis)
  - Education centres: Bruno and Anderson (1982); Diamond and Wright (1987); Church and Murray (1993); Malczewski and Kackson (2000); Ewing et al. (2004); Pal (2010)
  - Health and emergency services: Marianov and ReVelle (1995); Daskin and Dean (2005); Günes and Nickel (2015)
- **Economics**
  - **Universal service obligations:** Laffont and Tirole (2000) (telecommunications); Armstrong (2008) (postal services)
  - **Privatization of monopoly utilities:** Wright (1987) (British Gas)
  - **Monopoly regulation** (regulated price, subsidies): Hotelling (1938) (railway); Stigler and Friedland (1962) (electricity); Lyon (1994) (telecommunications)

# Analytical approach

- Theoretical model of spatial monopoly
- Interest of public sector: provision, adequate prices
- Monopoly: simplify the analysis of regulation
- Spatial approach: provision and price discrimination regarding location of consumers
- Firm
  - Private: maximise profits
  - Public: maximise social welfare
- Universal service obligations
  - Full provision
  - Uniform prices: mill prices, delivered prices
- Two decisions: location and prices

# Analytical approach

Our work builds on the contributions of:

- Hotelling (1929): customer location on a straight line; two firms located along the line; no price discrimination;
- Hwang and Mai (1990): population concentrated in two urban areas with an uninhabited connecting motorway; monopolist's location either along the line or in one of the urban areas; price discrimination between cities → barbell model

# Analytical approach

## Assumptions

- One plant to be open (located at  $x$ ,  $0 \leq x \leq 1$ )
- Two markets: 1 ( $x_1 = 0$ ), 2 ( $x_2 = 1$ )
- Mass of consumers (consumer density):  $M_1, M_2$
- Reservation price:  $\nu$
- Linear transportation costs, no costs of production
- Prices:  $p_1, p_2$
- Full provision if  $\nu > \max\{p_1 + tx, p_2 + t(1 - x)\}$
- Market 1 is more populated:  $M_1 > M_2$

# Analytical approach

- Decisions
  - 1<sup>st</sup> → level of provision:  $q = \{M_1, M_1 + M_2\}$
  - 2<sup>nd</sup> → location:  $x$
  - 3<sup>rd</sup> → prices:  $p_1, p_2$
- Solved by backward induction
- Nature of the firm:
  - Private (max profits)
  - Public (max social welfare)
- Cases
  - Unregulated monopoly
  - USO through uniform mill prices:  $p_1 = p_2$
  - USO through uniform delivered prices:  
$$p_1 + tx = p_2 + t(1 - x)$$

# Private monopoly

## 1) Unregulated monopoly

- 1<sup>st</sup> → level of provision:  $q = \{M_1, M_1 + M_2\}$  (max  $\pi$ )
- 2<sup>nd</sup> → location:  $x$  (max  $\pi$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $\pi$ )

## 2) USO through uniform mill prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $\pi$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $\pi$ ), s.t.  $p_1 = p_2$

## 3) USO through uniform delivered prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $\pi$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $\pi$ ), s.t.  $p_1 + tx = p_2 + t(1 - x)$

# Private monopoly

## 1) Unregulated monopoly

- 1<sup>st</sup> → level of provision:  $q = \{M_1, M_1 + M_2\}$  (max  $\pi$ )
- 2<sup>nd</sup> → location:  $x$  (max  $\pi$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $\pi$ )

### • Partial provision

- $\pi = p_1 M_1$
- $CS = (v - p_1 - tx)M_1$ 
  - $x = 0, p_1 = v$

### • Full provision

- $\pi = p_1 M_1 + p_2 M_2$
- $CS = (v - p_1 - tx)M_1 + [v - p_2 - t(1 - x)]M_2$ 
  - $p_1 = v - tx, p_2 = v - t(1 - x)$
  - $\pi = (v - tx)M_1 + [v - t(1 - x)]M_2 \rightarrow x = 0$

# Private monopoly

## 1) Unregulated monopoly

$$\begin{cases} x = 0 \\ q = M_1 + M_2 \\ p_1 = v \\ p_2 = v - t \\ \pi = vM_1 + (v - t)M_2 \\ CS = 0 \\ SS = vM_1 + (v - t)M_2 \end{cases} \quad \text{when } v \geq t,$$

$$\begin{cases} x = 0 \\ q = M_1 \\ p_1 = v \\ \pi = vM_1 \\ CS = 0 \\ SS = vM_1 \end{cases} \quad \text{when } v < t$$

# Private monopoly

## 2) USO through uniform mill prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $\pi$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $\pi$ ), s.t.  $p_1 = p_2$

$$\begin{cases} x = \frac{1}{2} \\ q = M_1 + M_2 \\ p_1 = v - \frac{t}{2} \\ p_2 = v - \frac{t}{2} & \text{when } v \geq \frac{t}{2}. \\ \pi = \left(v - \frac{t}{2}\right)(M_1 + M_2) \\ CS = 0 \\ SS = \left(v - \frac{t}{2}\right)(M_1 + M_2) \end{cases}$$

For any value  $v < \frac{t}{2}$ , universal provision is not feasible.

# Private monopoly

## 3) USO through uniform delivered prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $\pi$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $\pi$ ), s.t.  $p_1 + tx = p_2 + t(1 - x)$

$$\begin{cases} x = 0 \\ q = M_1 + M_2 \\ p = v \\ \pi = vM_1 + (v - t)M_2 & \text{when } v \geq t \frac{M_2}{M_1 + M_2} \\ CS = 0 \\ SS = vM_1 + (v - t)M_2 \end{cases}$$

For any value  $v < t \frac{M_2}{M_1 + M_2}$ , universal provision is not profitable for the firm at any location.

# Public monopoly

## 1) Unregulated monopoly

- 1<sup>st</sup> → level of provision:  $q = \{M_1, M_1 + M_2\}$  (max  $SS$ )
- 2<sup>nd</sup> → location:  $x$  (max  $SS$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $CS$ )

## 2) USO through uniform mill prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $SS$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $CS$ ), s.t.  $p_1 = p_2$

## 3) USO through uniform delivered prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $SS$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $CS$ ), s.t.  $p_1 + tx = p_2 + t(1 - x)$

# Public monopoly

## 1) Unregulated monopoly

- 1<sup>st</sup> → level of provision:  $q = \{M_1, M_1 + M_2\}$  (max SS)
- 2<sup>nd</sup> → location:  $x$  (max SS)
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max CS)
- Partial provision
  - $CS = (v - p_1 - tx)M_1, SS = (v - tx)M_1$ 
    - $x = 0, p_1 = 0$
- Full provision
  - $CS = (v - p_1 - tx)M_1 + [v - p_2 - t(1 - x)]M_2$
  - $SS = (v - tx)M_1 + [v - t(1 - x)]M_2$ 
    - $p_1 = 0, p_2 = 0, x = 0$

# Public monopoly

## 1) Unregulated monopoly

$$\begin{cases} x = 0 \\ q = M_1 + M_2 \\ p_1 = 0 \\ p_2 = 0 \\ \pi = 0 \\ CS = vM_1 + (v - t)M_2 \\ SS = vM_1 + (v - t)M_2 \end{cases} \quad \text{when } v \geq t,$$

$$\begin{cases} x = 0 \\ q = M_1 \\ p_1 = 0 \\ \pi = 0 \\ CS = vM_1 \\ SS = vM_1 \end{cases} \quad \text{when } v < t$$

# Public monopoly

## 2) USO through uniform mill prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $SS$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $CS$ ), s.t.  $p_1 = p_2$

$$\begin{cases} x = 0 \\ q = M_1 + M_2 \\ p_1 = 0 \\ p_2 = 0 \\ \pi = 0 \\ CS = vM_1 + (v - t)M_2 \\ SS = vM_1 + (v - t)M_2 \end{cases} \quad \text{when } v \geq t,$$

$$\begin{cases} x = 1 - \frac{v}{t} \\ q = M_1 + M_2 \\ p_1 = 0 \\ p_2 = 0 \\ \pi = 0 \\ CS = (2v - t)M_1 \\ SS = (2v - t)M_1 \end{cases} \quad \text{when } \frac{t}{2} \leq v < t.$$

For any value  $v < \frac{t}{2}$ , universal provision is not feasible.

# Public monopoly

## 3) USO through uniform delivered prices

- 1<sup>st</sup> → level of provision:  $q = M_1 + M_2$
- 2<sup>nd</sup> → location:  $x$  (max  $SS$ )
- 3<sup>rd</sup> → prices:  $p_1, p_2$  (max  $CS$ ), s.t.  $p_1 + tx = p_2 + t(1 - x)$

$$\begin{cases} x = 0 \\ q = M_1 + M_2 \\ p = t \\ \pi = tM_1 \\ CS = (\nu - t)(M_1 + M_2) \\ SS = \nu M_1 + (\nu - t)M_2 \end{cases} \quad \text{when } \nu \geq t,$$

$$\begin{cases} x = 1 - \frac{\nu}{t} \\ q = M_1 + M_2 \\ p = t \\ \pi = (2\nu - t)M_1 \\ CS = 0 \\ SS = (2\nu - t)M_1 \end{cases} \quad \text{when } \frac{t}{2} \leq \nu < t.$$

For any value  $\nu < \frac{t}{2}$ , universal provision is not feasible.

# Conclusions

- Without USO, partial provision if  $v < t$
- Unregulated private monopoly, consumers from the remote market pay a lower mill price → spatial price discrimination (subsidized for their journey)
- Private monopoly subject to USO on uniform delivered prices, consumers from the remote market pay a negative mill price (cross-subsidization) when  $t \frac{M_2}{M_1+M_2} \leq v < \frac{t}{2}$
- Imposing USO increases the number of users but not the efficiency ( $SS$  and  $CS$  do not increase) → USO is not economically efficient (political decision)