61A Lecture 17 Wednesday, March 4

Announcements

- *Delayed: Hog contest winners will be announced Friday 3/6 in lecture
- •Quiz 2 due Thursday 3/5 @ 11:59pm (challenging!)
- Project 3 due Thursday 3/12 @ 11:59pm (get started now!)
- Delayed: Homework 6 due Monday 3/16 @ 11:59pm
- •Midterm 2 is on Thursday 3/19 7pm-9pm
- *Emphasis: mutable data, object-oriented programming, recursion, and recursive data

Generic Functions of Multiple Arguments

More Generic Functions

A function might want to operate on multiple data types

Last Tectur

- •Polymorphic functions using shared messages
- ·Interfaces: collections of messages that have specific behavior conditions
- *Two interchangeable implementations of complex numbers

This lecture:

- ·An arithmetic system over related types
- -Operator overloading
- •Type dispatching
- •Type coercion

What's different? Today's generic functions apply to multiple arguments that don't share a common interface.

```
Class Rational:

"""A rational number represented as a numerator and denominator."""

def __init (self, numer, denom):
    g = gcd(numer, denom):
    self.numer = numer // g
    self.numer = numer // g
    self.numer = numer // g

def __repr_(self):
    return 'Rational({0}, {1})'.format(self.numer, self.denom)

def add(self, other):
    nx, dx = self.numer, self.denom
    ny, dy = other.numer, other.denom
    return Rational(nx * dy + ny * dx, dx * dy)

def mul(self, other):
    numer = self.numer * other.numer
    denom = self.numer * other.numer
    denom = self.denom * other.denom
    return Rational(numer, denom)

(Demo)
```

```
Complex Numbers

class Complex:
    def add(self, other):
        return ComplexRI(self.real + other.real,
            self.imag + other.imag)

def mul(self, other):
    return ComplexMA(self.magnitude * other.magnitude,
    self.angle + other.angle)

class ComplexRI(complex):
    """A rectangular representation."""
    def _init_(self, real, imag):
        self.real = real
        self.imag = imag

@property
    def magnitude(self):
    return (self.real ** 2 + self.imag ** 2) ** 0.5

@property
    def angle(self):
    return atan2(self.imag, self.real)

(Demo)
```

Cross-Type Arithmetic Examples

Currently, we can add rationals to rationals, but not rationals to complex numbers

```
>>> Rational(3, 14).add(Rational(2, 7))
               Rational(1, 2)
               >>> ComplexRI(0, 1).mul(ComplexMA(1, 0.5 * pi))
                                                                                i \cdot i
              ComplexMA(1, 1 * pi)
              >>> Rational(3, 14) + Rational(2, 7)
              Rational(1, 2)
Operators
                >>> ComplexRI(0, 1) * ComplexMA(1, 0.5 * pi)
                                                                                 i \cdot i
             ComplexMA(1, 1 * pi)
               >>> Rational(1, 2) + ComplexRI(0.5, 2)
                                                                             \frac{1}{2} + (0.5 + 2 \cdot i)
               ComplexRI(1, 2)
               >>> ComplexMA(2, 0.5 * pi) * Rational(3, 2)
                                                                                2 \cdot i \cdot \frac{3}{2}
              ComplexMA(3, 0.5 * pi)
```

Special Method Names

```
Type Dispatching
```

```
The Independence of Data Types

Data abstraction and class definitions keep types separate

Some operations need access to the implementation of two different abstractions

How do we add a complex number and a rational number together?

Rational numbers as numerators & denominators

def add_complex_and_rational(c, r):

"""Return c + r for complex c and rational r."""

return ComplexRI(c.real + r.numer/r.denom, c.imag)
```

Type Dispatching Analysis

Type Dispatching Analysis

Minimal violation of abstraction barriers: we define cross-type functions as necessary

Extensible: Any new numeric type can "install" itself into the existing system by adding new entries to the cross-type function dictionaries ${\sf val}$

 $Number.adders[(tag0, tag1)] = add_tag0_and_tag1$

Question: How many cross-type implementations are required for m types and n operations?

m n $m \cdot n$ $m^2 \cdot n$ $m^2 \cdot n^2$

 $m \cdot (m-1) \cdot n$

Type Dispatching Analysis

Minimal violation of abstraction barriers: we define cross-type functions as necessary.

Extensible: Any new numeric type can "install" itself into the existing system by adding new entries to the cross-type function dictionaries ${\sf var}$

Arg 1	Arg 2	Add	Multiply
Complex	Complex		
Rational	Rational		
Complex	Rational		
Rational	Complex		

Type Coercion

```
Coercion

Idea: Some types can be converted into other types

Takes advantage of structure in the type system

def rational_to_complex(r):
    """Return complex equal to rational."""
    return ComplexRI(r.numer/r.denom, 0)

Question: Can any numeric type be coerced into any other?

Question: Can any two numeric types be coerced into a common type?

Question: Is coercion exact?
```



