61A Lecture 28

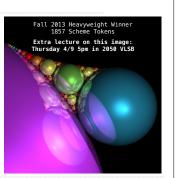
Friday, November 7

Announcements

- *Homework 7 due Wednesday 4/8 @ 11:59pm
- "Homework party Tuesday 4/7 5pm-6:30pm in 2050 VLSB
- •Quiz 2 due Thursday 4/9 @ 11:59pm
- ·Homework 8 due Wednesday 4/15 @ 11:59pm
- Project 1, 2, & 3 composition revisions due Monday 4/13 @ 11:59pm
- Project 4 due Thursday 4/23 @ 11:59pm (Big!)

Scheme Recursive Art Contest: Start Early!





Dynamic Scope

Dynamic Scope

The way in which names are looked up in Scheme and Python is called lexical scope (or static scope) [You can see what names are in scope by inspecting the definition]

Lexical scope: The parent of a frame is the environment in which a procedure was *defined* **Dynamic scope:** The parent of a frame is the environment in which a procedure was *called*

Special form to create dynamically scoped procedures (mu special form only exists in Project 4 Scheme)

(define f (tambda (x) (+ x y)))

(define g (lambda (x y) (f (+ x x))))
(g 3 7)

Dynamic scope: The parent for f's frame is g's frame 13

Global frame μ $(\lambda (x) \dots)$ $(\lambda (xy) \dots)$ f1: g [parent=global] $\times 3$ $\times 7$ f2: f [parent=global] $\times 6$ f1

Functional Programming

All functions are pure functions.

No re-assignment and no mutable data types.

Name-value bindings are permanent.

 $\label{programming:equation} \mbox{Advantages of functional programming:} \\$

- The value of an expression is independent of the order in which sub-expressions are evaluated.
- * Sub-expressions can safely be evaluated in parallel or on demand (lazily).
- Referential transparency: The value of an expression does not change when we substitute
 one of its subexpression with the value of that subexpression.

But... no for/while statements! Can we make basic iteration efficient? Yes!

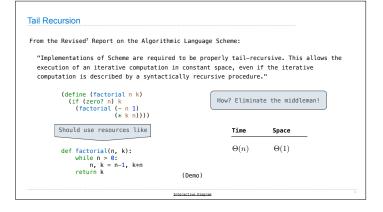
Recursion and Iteration in Python

In Python, recursive calls always create new active frames

 $\label{eq:factorial} \mbox{factorial(n, k) computes: n! * k}$

Tail Recursion

	Time	Space
<pre>def factorial(n, k): if n == 0: return k else: return factorial(n-1, k*n)</pre>	$\Theta(n)$	$\Theta(n)$
<pre>def factorial(n, k): while n > 0: n, k = n-1, k*n return k</pre>	$\Theta(n)$	Θ(1)





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Tail Calls

A procedure call that has not yet returned is active. Some procedure calls are tail calls. A Scheme interpreter should support an unbounded number of active tail calls using only a constant amount of space.

A tail call is a call expression in a tail context:

• The last body sub-expression in a lambda expression
• Sub-expressions 2 & 3 in a tail context if expression
• All non-predicate sub-expressions in a tail context cond
• The last sub-expression in a tail context and or or
• The last sub-expression in a tail context begin

(define (factorial n k)

(if (= n 0) k

(factorial (- n 1)

(* k n))))
```

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(define (length s)

(if (null? s) 0  Not a tail context

(+ 1(length (cdr s))))

A call expression is not a tail call if more computation is still required in the calling procedure

Linear recursive procedures can often be re-written to use tail calls

(define (length-tail s)

(define (length-ter s n)

(if (null? s) n  Recursive call is a tail call

(length-iter (cdr s) (+ 1 n))))

(length-iter s 0))
```

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Eval with Tail Call Optimization

The return value of the tail call is the return value of the current procedure call Therefore, tail calls shouldn't increase the environment size

(Demo)
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Tail Recursion Examples
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Which Procedures are Tail Recursive?
Which of the following procedures run in constant space? \;\Theta(1)\;
                                                     ;; Return whether s contains v.
;; Compute the length of s.
(define (length s)
                                                     (define (contains s v)
 (+ 1 (if (null? s)
                                                       (if (null? s)
                                                           false
(if (= v (car s))
           (length (cdr s))) ) )
                                                               (contains (cdr s) v))))
;; Return the nth Fibonacci number.
(define (fib n)
  (define (fib-iter current k)
                                                     ;; Return whether s has any repeated elements.
    (if (= k n)
current
                                                     (define (has-repeat s)
(if (null? s)
 (fib-iter (+ current (fib (- k 1))) (+ k 1)) (if (= 1 n) 0 ((fib-iter 1 2)))
                                                           false
(if (contains? (cdr s) (car s))
                                                                (has-repeat (cdr s)))
```

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Map and Reduce
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Example: Reduce

(define (reduce procedure s start)

(if (null? s) start

(reduce procedure

(cdr s)

(procedure start (car s)))))

Recursive call is a tail call

Space depends on what procedure requires

(reduce * '(3 4 5) 2)

(reduce (lambda (x y) (cons y x)) '(3 4 5) '(2))

(5 4 3 2)
```

