Data Analysis using R and Python



DISSERTATION SUBMITTED TO CENTRAL UNIVERSITY OF HARYANA, MAHENDERGARH, HARYANA - 123031. FOR THE AWARD OF THE DEGREE OF MASTER OF SCIENCE IN STATISTICS

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DEPARTMENT OF STATISTICS CENTRAL UNIVERSITY OF HARYANA, MAHENDERGARH, HARYANA - 123031. June 2018

DECLARATION

I hereby declare that the dissertation work entitled "Data Analysis using R and Python" submitted to the Department of Statistics, Central University of Haryana for the partial fulfillment of award of the degree of Master of Science in Statistics, is done by me under the supervision of Dr. Kapil Kumar, Assistant Professor, Department of Statistics, Central University of Haryana. The content of this dissertation has not been submitted so far in full or part for any degree or diploma in any other University or Institution.

Place: Central University of Haryana

Date:

Jogesh Dhiman M.Sc. Statistics Roll No. 8952

CERTIFICATE

This is to certify that the dissertation entitled "Data Analysis using R and Python" is being submitted to the Department of Statistics, Central University of Haryana, Mahendergarh, as dissertation work for partial fulfillment of requirements for the award of the degree of Master of Science in Statistics.

This work has been completed by Mr. Jogesh Dhiman under my supervision and has not been submitted elsewhere for any degree or diploma in any form.

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Place: Central University of Haryana

Date:

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Chapter 1

Introduction

Python and R are two very popular open source software's used for data analysis. However both software's are of equal importance and can be used as complement of each other. When it comes to choose one, R offers more depth when it comes to data analysis, data modelling while Python is easier to learn and tends to represent graphs in more polished way.

1.1 Why R?

- Open Source: R is an open source software and can be installed easily.
- Learning: R requires you to learn and understand coding. It's a low level programming which can take longer codes.
- Statistical Analysis: Designed by statisticians for doing statistical analysis. In R, statistical analysis is made strong using large number of packages. Currently, on dated 09th June 2018, the CRAN package repository features 12611 available packages. Some of the well known packages are:

For Visualization: ggplot2 (See Hadley Wickham, Winston Chang, RStudio (2016)) For Reporting: knitr (See Yihui Xie (2018))

For Geography: maps, ggmaps (See David Kahle, Hadley Wickham (2016))

1.2 Why Python?

- Open source: Python is also a open source software and can be installed easily.
- Learning: Python is easy to learn. Python is known for its simplicity in programming world.
- Speed: People are inappropriately obsessed with speed. Python is a high-level language, which means it has number of benefits to accelerate codes. Another benefit is that it is easy to learn.

• Statistical Analysis: Python is widely used in scientific computing and statistical analysis in industry and academics. A large number of analytics libraries are available, including numerical analysis, statistical analysis, data analysis, visualization. (See https://docs.python.org/3/library/)

1.3 Installing R software

R is an open source and can obtained from **Comprehensive R Archive Network (CRAN)**, which can be done as follows:

- Open an internet browser and go to www.r-project.org.
- Click the "download R" link in the middle of the page under "Getting Started."
- Select a CRAN location (a mirror site) and click the corresponding link.
- Click on the "Download R for (Mac) OS X" link at the top of the page.
- Click on the file containing the latest version of R under "Files."
- Save file, double-click it to open, and follow the installation instructions.

1.4 Installing Python Software

Python is an open Source and can be downloaded from website www.python.org , which can be done as follows:

- Go to the python website www.python.org and click on the 'Download' menu choice.
- Next click on the Python 3.7 (note that the version number may change) 'Windows Installer' to download the installer. If you know you're running a 64-bit OS, you can choose the x86-64 installer.
- Be sure to save the file that you are downloading.
- Once you have downloaded the file, open it. (You can also double-click on it to open it.)
- Now follow the installation instructions.
- Now for doing data analysis. We need to install packages.

Note: For new users of python, Anaconda (from https://www.continuum.io) is recommended due to complication in installing packages in python used in 'Data Analysis'. Anaconda provides you almost all necessary packages you need at work.

Otherwise, you would need to install every package separately and many times you will run into installation errors because of incompatible packages' versions.

Once the software is installed, now it can be executed by launching corresponding executable. The prompt, by default '>' and '>>>' in R and Python respectively, indicates that software is waiting for your commands. At this stage, new user will think, "what do I do now?" Using for the first time, let's start with their basic uses i.e. use these software's as a calculator. We can write commands in window at command prompt and use both software as powerful calculators.

1.5 Basic Operators in R

R language have usual basic operators. The common operators are:

1.5.1 Arithmetic Operators:

Following are the arithmetic operators in R.

Arithmetic Operators

Operators	Meaning	Examples
+	Addition	>7+6
		[1] 13
-	Subtraction	> 9-5
		[1] 4
*	Multiplication	> 6*2
		[1] 12
/	Division	> 9/3
		[1] 3
%%	Modulus i.e. remainder of the division	> 5%%2
	of left operand by the right	[1] 1 (i.e. remainder of 5/2)
٨	Exponent - left operand raised to	> 2^3
	the power of right	[1] 8 (i.e. 2 to the power 3)
pi	Pi (R knows about pi i.e. π)	> pi
		[1] 3.141593
sin	Sin trigonometric function	$> \sin(90*(pi/180))$
	_	[1] 1 (i.e. converts angle
		radians then take sin())
log	Logarithm	> log(25)
_		[1] 3.218876

4.12e-2

[1] 0.0412

```
cos(120*pi/180)
## [1] -0.5
log(100,base=10) #Takes the logarithm of x with base y;
## [1] 2
#if base is not specified, returns the natural logarithm
exp(25) #Returns the exponential of x
## [1] 72004899337
sqrt(25) #Returns the square root of x
## [1] 5
factorial(4) #Returns the factorial of x (x!)
## [1] 24
choose(5,3) #Returns the number of possible combinations
## [1] 10
#when drawing y elements at a time from x possibilities
```

1.5.2 Logical Operators

Following are logical operators in R:

Logical operators

Operators	Meaning
<	Less than
>	Greater than
<=	Less than equal to
>=	Greater than equal to
==	Exactly equal to
!=	Not equal to
! x	Not x
xly	x or y
x&y	x and y

```
x=c(1:5)
y=2
x<y
## [1] TRUE FALSE FALSE FALSE FALSE
x>y
## [1] FALSE FALSE TRUE TRUE TRUE
x<=y
## [1] TRUE TRUE FALSE FALSE FALSE
x>=y
## [1] FALSE TRUE TRUE TRUE TRUE
х==у
## [1] FALSE TRUE FALSE FALSE FALSE
x! = y
## [1] TRUE FALSE TRUE TRUE TRUE
! X
## [1] FALSE FALSE FALSE FALSE
y
## [1] FALSE
```

1.6 Basic Operators in Python

Python also have usual basic arithmetic operators. The common operators are:

1.6.1 Arithmetic Operators

Some arithmetic operators used in Python are given below in table.

```
In [1]: import math
In [2]: math.log10(100)#Return the base-10 logarithm
```

Arithmetic operators

Operators	Meaning	Examples
+	Addition	>>> 3+5
		8
-	Subtraction	>>> 6+4
		10
*	Multiplication	>>> 5*2
	_	10
/	division	>>> 8/4
		2.0
%	Modulus - remainder of the division	>>> 5%2
	of left operand by the right	1
		(remainder of 5/2)
**	Exponent - left operand raised	>>> 2**3
	to the power of right	8 (i.e. 2 to
		the power 3)
math.sin	Sin trigonometric function	>>> math.sin(90*(math.pi/180))
		1.0
math.log	logarithm	>>> math.log(25)
		3.2188758248682006

Out[2]: 2.0

In [3]: math.cos(25) #return the cosine of 25 radians

Out[3]: 0.9912028118634736

In [4]: math.factorial(5) #return the value of 5!

Out[4]: 120

In [5]: math.gamma(5) #return the gamma function at 5

Out[5]: 24.0

In [6]: math.degrees(90) #return angle 90 from radians to degree

Out[6]: 5156.620156177409

1.6.2 Logical Operators

The following are Logical operators used in Python:

In [1]: x=2 y=7

Logical operators

Operators	Meaning
<	Less than
>	Greater than
<=	Less than equal to
>=	Greater than equal to
==	Exactly equal to
!=	Not equal to
!x	Not x
xly	x or y
x&y	x and y

```
In [2]: if(x==y):
            print("x is equal to y")
        else:
            print("x is not equal to y")
x is not equal to y
In [3]: if (x>y):
            print("x is greater than y")
        else:
            print("x is not greater than y")
x is not greater than y
In [4]: if (x < y):
            print("x is less than y")
            print("x is not less than y")
x is less than y
In [5]: if (x>=y):
            print("x is greater than equal to y")
        else:
            print("x is not greater than equal to y")
x is not greater than equal to y
```

Since every value has a data type. Data type are classes and variables are instances of these classes.

1.7 Data types in R

R has various type of 'data type' which includes vectors, matrices, array, data frame and lists.

• Vectors: when we have to create a vector with more than one variable, then we use c() function which means combining elements into vector. For example:

```
#create a vector
X<- c(1,2,3,5,6,7)
X

## [1] 1 2 3 5 6 7

print(class(X)) # to get class of vector

## [1] "numeric"</pre>
```

• Matrices: Matrices is 2 dimensional data structure. It consists of elements of same class. It can be created using vector input to a matrix function. For example:

• List: List is a special type of vector which contain elements of different data types. For example:

```
# Create a list.
list1 <- list(c(2,5,3),21.3,sin)

# Print the list.
print(list1)

## [[1]]
## [1] 2 5 3
##

## [[2]]
## [1] 21.3
##

## [[3]]
## function (x) .Primitive("sin")</pre>
```

• Dataframe: Data frame is commonly used data type to store tabular data. It is different from matrices data type. In matrix, every element should be from same class. But in data frame you can use list of vector of different class. Every column act as a list. Every time you read data in R will be stored in a data frame. For example:

1.8 Data types in Python

Python has five standard type data.

• Number: Number variables are created by the standard Python method. For example:

```
In [1]: a=5
```

```
In [2]: print(a,type(a))
5 <class 'int'>
In [3]: b=0.265
In [4]: print(b,type(b))
0.265 <class 'float'>
```

• String: String can be defined by using single('), double(") or triple("') inverted commas. For example:

```
In [5]: greeting='greeting'
In [6]: print(greeting,type(greeting))
greeting <class 'str'>
```

• List: List are most useful data structures in Python. List can be simply defined by using comma separated values in square brackets. List can contain items of different type. But usually items have same type. Python lists are mutable and individual elements of a list can be changed. For example:

```
In [7]: square_list=[0,1,2,4,5,15,25,30]
In [8]: print(square_list,type(square_list))
[0, 1, 2, 4, 5, 15, 25, 30] <class 'list'>
In [9]: square_list[0]
Out[9]: 0
In [10]: square_list[2:6]
Out[10]: [2, 4, 5, 15]
```

 Tuple: Tuple is represented by number of values separated by commas. Tuple are immutable and can not change, they are faster in processing as compared to list. Hence, if your list is unlikely to change, you should use letups, instead of list. For example:

```
In [11]: tulle_ex=1,2,3,5,9,77,44,55,21,36,59
In [12]: print(tulle_ex,type(tulle_ex))
(1, 2, 3, 5, 9, 77, 44, 55, 21, 36, 59) <class 'tulle'>
```

• Dictionary: Dictionaries in Python are lists of key:value pair. Dictionaries can be used to sort, iterate and compare data. Dictionaries are created using braces({}) with pairs separated by commas() and key values associated with a colon(:). In dictionaries key must be unique. For example:

```
In [13]: dict={"A":1,"B":2,"C":3}
```

```
In [13]: dict={"A":1,"B":2,"C":3}
In [14]: dict.keys()
Out[14]: dict_keys(['A', 'B', 'C'])
In [15]: dict.values()
Out[15]: dict_values([1, 2, 3])
```

1.9 Data Analysis

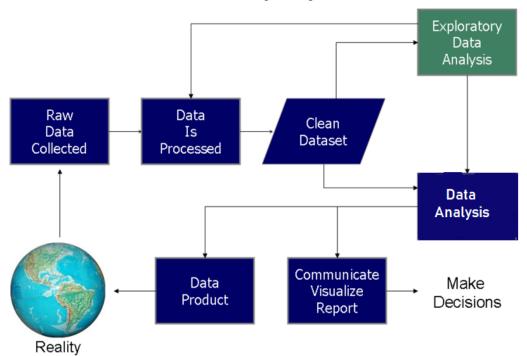
Data analysis is a process of cleaning, transforming and modelling data with goal of getting a useful information, suggesting conclusions and making decision from data. In other words main purpose of data analysis is to look at what the data is trying to tell us. Data analysis with good statistical program is not difficult. Data analysis doesn't require much knowledge of mathematics or formulas that program uses for analysis. Data analysis requires few things:

- A clean data that is ready for analysis.
- A clear idea that what questions you want the data to answer.

Process of data analysis have following steps:

- Data cleaning
- Explanatory data dnalysis
- Data analysis
- Visualize report
- Decision making

Data analysis process



Chapter 2

Graphics And Visualization

Graphics and visualization are powerful tool for describing and assisting analysis of data. The power of graphics and visualization arises from the fact that they describes the large quantities of information quickly. Graphics play an important role in good data analysis. They are useful for storing large data sets during data analysis, assist in describing and summarizing the data, and they can be tightly integrated with formal analytical statistical tools such as model-fitting techniques so that the analysis process can be refined.

2.1 Graphics and Visualization using R

R offers a variety of powerful tools for graphics and visualization. Each graphical function have a large number of options for producing graphs making it flexible. It is possible to display data and outcomes in wide variety of different ways. Base R plotting commands are used to display a variety of graphs and is divided into two basic groups:

• High-level plotting function: High-level plotting function create a new graph on the device, possibly with axis, labels, etc. Function such as hist(), plot(), boxplot() produces a entire plot or initialize a plot. High level potting function starts a new plot, erasing the current plot if following. Some of standard plot functions are:

```
S.No Function
                     Name of the plot
1
      plot()
                     Scatter plot
2
      hist()
                    Histogram
3
      boxplot()
                    Box plot or Box-and-whiskers plot
      stripchart()
                    Strip-chart
5
      barplot()
                    Bar-diagram
6
                     Stem and leaf display
      stem()
```

The number of arguments can be passed to high-level plotting function, as follows:

```
S.No. Arguments Explanation
1 main=" " Title of the plot
2 xlab=" " Label for x axis
```

```
ylab=" "
                       Label for y axis
3
4
      xlim=
                       Specify x limit
5
                       Specify y limit
      ylim=
      type="p/l/o" Style of plotting symbol
psh=" " Shape of the points
6
      pch=" "
                       Shape of the points
7
      ltv=" "
8
                       Style of the line
```

• Low-Level plotting function: Sometimes high-level plotting functions do not produce the graphs which we desire or we want to add more information to the graph then we use low-level plotting functions those add more information to an existing plot, such as lines, labels, extra points. Some low-level ploting functions are:

```
S.No. Function
                    Explanation
1
     lines()
                    Lines
2
      abline()
                    lines given by intercept and slope
3
     points()
                    points
4
                    Text in the plot
     text()
5
      legend()
                    List of symbols
```

R has many powerful packages for graphical representation and visualization. Two most widely used packages are:

- lattice: lattice was created by Deepayan Sarkar, see Sarkar(2017) lattice is a powerful and high-level plotting data visualization system. The lattice is based on Gridgraphics engine and requires grid add on package. lattice provides its own interface for modification of set of graphical and non-graphical settings.
- ggplot2: ggplot2 was created by Hadley Wickham in 2005, see Wickham(2016). Since 2005 ggplot2 has been grown in use to become most powerful R package. In comparison to R base, ggplot2 allows user to add or remove components at high-level of abstraction. This abstraction comes at a cost, that ggplot2 is being slower than lattice graphics.

Dataset:

We are using Motor Trend Car Road tests datasets in R dataset package.

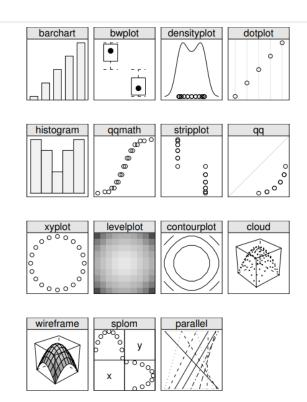
Description: The data was extracted from the 1974 Motor Trend US magazine, and comprises fuel consumption and 10 aspects of automobile design and performance for 32 automobiles (1973-74 models).

2.1.1 Application of lattice

The lattice package created by Deepayan Sarkar is an attempt to improve R base graphics. Lattice package provides better default and ability to simply display multivariate analysis. (See Sarkar D.(2017)) The plotting functions available in lattice:

```
Lattice Function Description R base analogue bwplot() Boxplots boxplot()
```

Barcharts	<pre>barplot()</pre>
Histograms	hist()
density plots	none
Quantile-quantile	qqnorm()
plot (Data set vs	
$theoretical\ distribution)$	
Dotplots	<pre>dotchart()</pre>
Scatterplots	plot()
Stripplots	stripchart()
Quantile-quantile	qqplot()
plots(Data set vs	
data set)	
3-D scatterplot	none
3-D surfaces	persp()
Level plots	<pre>image()</pre>
Contour plots	contour()
Scatterplot matrices	pairs()
Parallel coordinate	none
plots	
	Histograms density plots Quantile-quantile plot (Data set vs theoretical distribution) Dotplots Scatterplots Stripplots Quantile-quantile plots(Data set vs data set) 3-D scatterplot 3-D surfaces Level plots Contour plots Scatterplot matrices Parallel coordinate

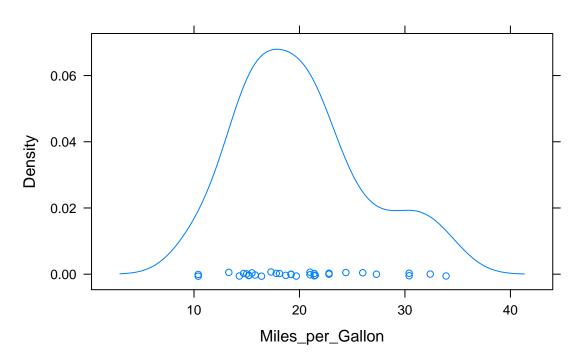


The lattice package supports the trellis graph that shows the relationship variables. The basic format of lattice is:

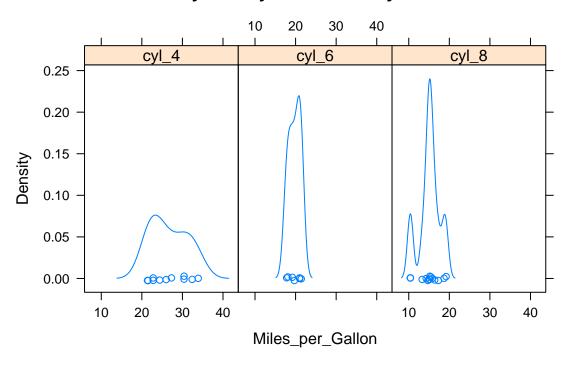
graph_type(formula, data=)

Here we show some applications of lattice function with example of dataset of mtcars:

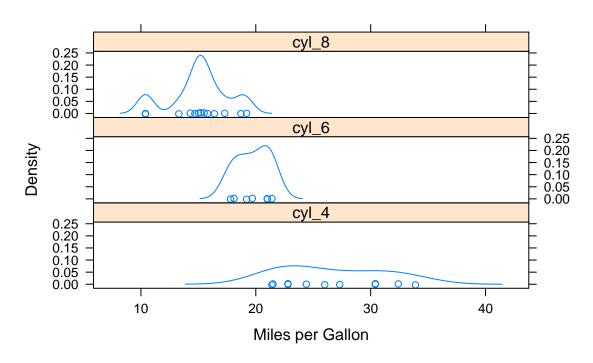
Density_Plot



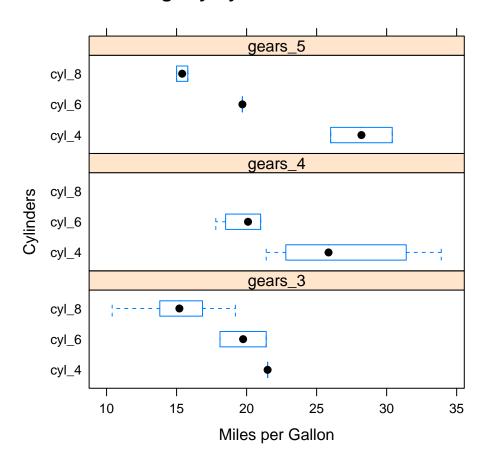
Density Plot by Number of Cylinders



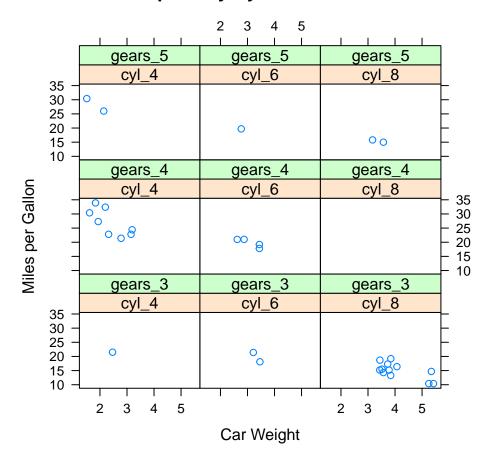
Density Plot by Number of Cylinders



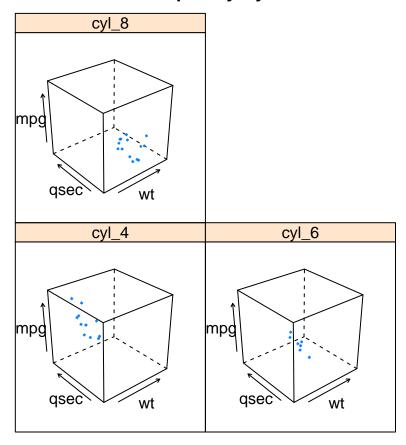
Mileage by Cylinders and Gears



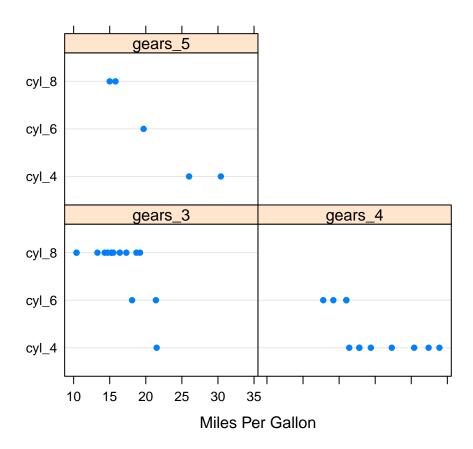
Scatterplots by Cylinders and Gears



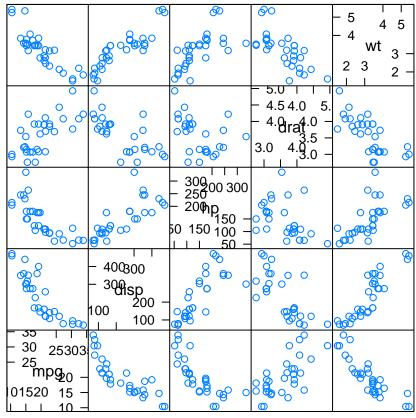
3D Scatterplot by Cylinders



Dotplot Plot by Number of Gears and Cylinders



Scatter Plot of mtcars Data



Scatter Plot Matrix

2.1.2 Applications of ggplot2

Here we show some applications of ggplot2 package

Advantages of ggplot2

- Plot at high-level of abstraction.
- Very flexible
- Consistent grammar of graphics

Grammar of graphics

- data
- aesthetic mapping
- geometric objects
- scales

- coordinate system
- position adjustments
- statistical transformation

Basic format of ggplot2: $ggplot(data = , aes(x =, y =, ...)) + geom_xxx()$

- ggplot(): start object and specify the data.
- geom_xxx(): There are many types of geometric objects some are as follow:
 - geom_bar: bars with bases on the x-axis
 - geom_boxplot: boxes-and-whiskers
 - geom_histogram: histogram
 - geom_smooth: smoothed conditional means (e.g. loess smooth)
 - geom_line: lines
 - geom_ribbon: bands spanning y-values across a range of x-values
 - geom_point: points (scatterplot)
 - geom_errorbar: T-shaped error bars
- aes(): specify the aesthetic elements.

Installing and attaching package ggplot2

Like other package ggplot2 can be installed using function install.package(" ") and can be attached using attach() or library function. installing package

```
> install.packages("ggplot2")
```

```
#attaching library ggplot
library("ggplot2")

## Warning: package 'ggplot2' was built under R version 3.4.4

##

## Attaching package: 'ggplot2'

## The following object is masked from 'mtcars':

##

##

##

##

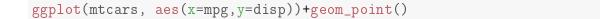
##

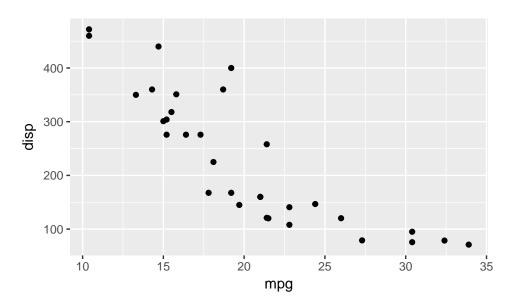
##

##

##
```

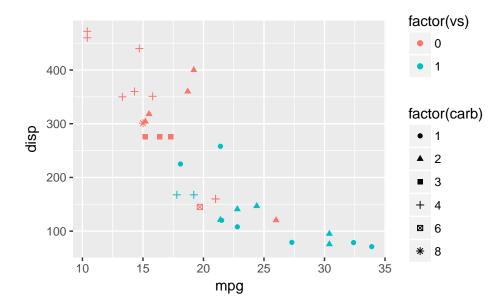
How to make scatter plot





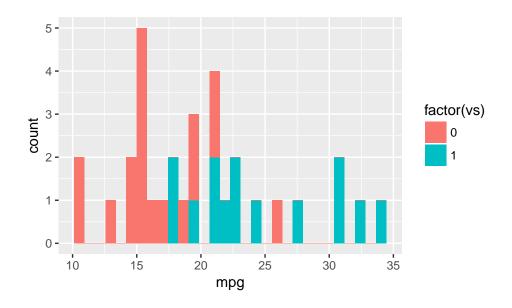
Distinguish groups:To distinguish first change integers into factors. To distinguish we can use two methods either distinguish by color or by shape. We will use both in same graph using two different groups as follow:

```
ggplot(mtcars, aes(x=mpg,y=disp, shape=factor(carb), colour=factor(vs)))+
  geom_point()
```

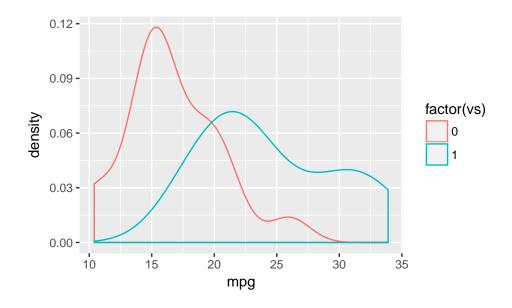


• How to make Histogram, density and boxplot: If we want to plot the distribution of mpg in mtcars and want to show trends by different groups. We can also show density graph by simply adding a geom_density() function as follow:

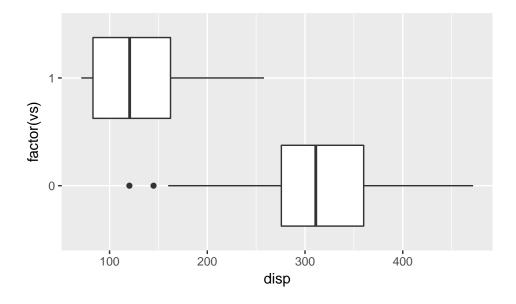
```
ggplot(mtcars, aes(x=mpg, fill=factor(vs)))+geom_histogram()
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



ggplot(mtcars, aes(x=mpg, colour=factor(vs)))+geom_density()



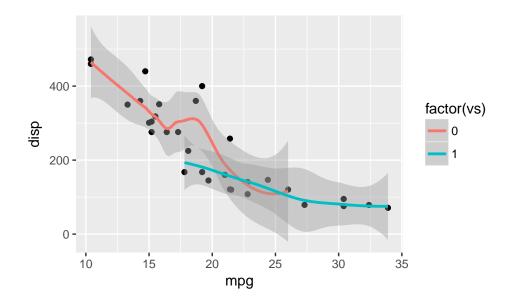
ggplot(mtcars, aes(x=factor(vs),y=disp))+geom_boxplot()+coord_flip()



#coord_flip() function to flip the coordinates

• How to make Trend line: Trend line can aid the eye in seeing patterns in the presence of over plotting. Using geom_smooth() to add Trend line to your graph:

```
ggplot(mtcars, aes(x=mpg,y=disp))+geom_point()+
  geom_smooth(aes(colour=factor(vs))) #aes() will show the trend line
## 'geom_smooth()' using method = 'loess'
```



#by groups trend line is not necessarily describing the regression #results of your data. It may be very DIFFERENT from the regression #line of your model.

- Faceting: Faceting generates small multiples each showing a different subset of the data.
 - facet_null(): a single plot, the default.
 - facet_wrap(): "wraps" a 1 dimensional ribbon of panels into 2 dimension, facet_wrap(GI)
 - facet_grid(): produces a 2D grid of panels defined by variables which form the rows and columns. facet_grid(row col)

Faceting is an alternative approach to use aesthetics (like color, shape or size) to differentiate groups. It is good when groups overlap a lot, but it make small differences that are harder to observe.

```
library(dplyr)

##

## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':

##

## filter, lag

## The following objects are masked from 'package:base':

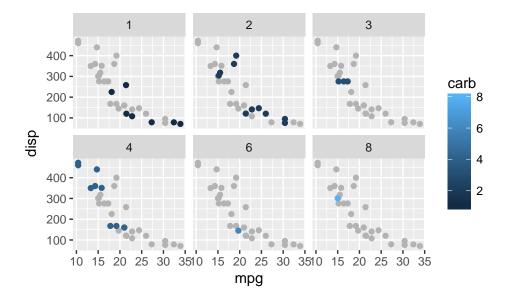
##

## intersect, setdiff, setequal, union

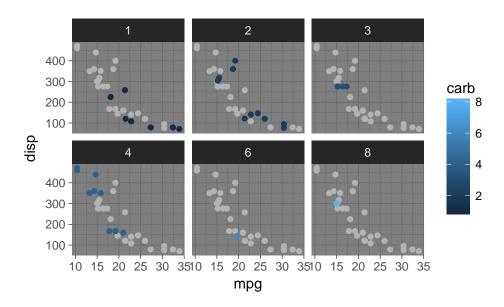
mtcars_new<-select(mtcars,-carb)

ggplot(mtcars, aes(x=mpg,y=disp))+geom_point(data=mtcars_new, colour="grey70")+

geom_point(aes(colour = carb))+facet_wrap(~carb)</pre>
```

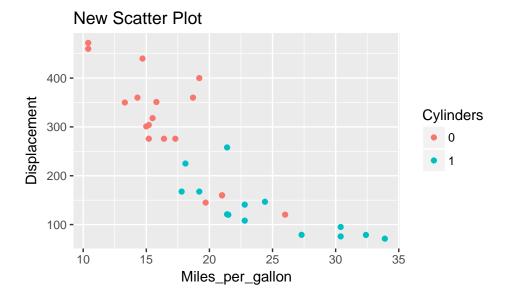


• Theme: The theme system in ggplot2 enables a user to control non-data elements of a ggplot object. It makes the ggplot2 a flexible and powerful graphing tool for data visualization.



- Setting axis limits and labeling scales: We commonly need to adjust axis so ggplot2
 provides several convenient functions to label axis and adjust axis and other aesthetics:
 - lims, xlim, ylim: set axis limits

- expand_limits: extend limits of scales for various aethetics
- xlab, ylab, ggtitle, labs: give labels (titles) to x-axis, y-axis, or graph; labs can set labels for all aesthetics and title



2.2 Graphics and Visualization using Python

Python has many visualization tools for building an interactive visualization. It is possible to make beautiful plots for display in python. There are number of other visualization tools in wide use. Few of them are:

- matplotlib
- seaborn
- ggplot
- mayavi
- chaos

But here we'll be focused on two of above that is matplotlib and seaborn.

2.2.1 Applications of matplotlib

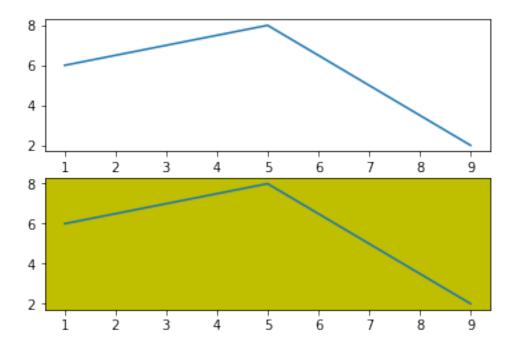
matplotlib is a plotting package designed for creating quality plot. matplotlib was created by John Hunter in 2002 to enable a MATLAB like plotting in python. matplotlib has a number of add-on toolkits, such as mplot3d for 3D plots and basemap for mapping. There are several ways to interact with matplotlib and the most common is through pylab mode in ipython. matplotlib is probably the single most used Python package for 2D-graphics. It provides both a very quick way to visualize data from Python and publication-quality figures in many formats. pyplot provides a convenient interface to the matplotlib object-oriented plotting library. It is modeled closely after Matlab(TM). Firstly we will import (See https://matplotlib.org/) all the library needed by using following commands

```
In [1]: import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        %matplotlib inline
```

• Simple plotting a line for two array using plot() function and subplot() function.

```
In [2]: # plot a line, implicitly creating a subplot(111)
    plt.plot([1,2,3],[6,7,8])
    # now create a subplot which represents the top plot of a grid
    # with 2 rows and 1 column. Since this subplot will overlap the
    # first, the plot (and its axes) previously created, will be removed
    plt.subplot(211)
    plt.plot([1,5,9],[6,8,2])
    plt.subplot(212, facecolor='y')
    # creates 2nd subplot with yellow background
    plt.plot([1,5,9],[6,8,2])
```

```
Out[2]: [<matplotlib.lines.Line2D at 0x202a31f93c8>]
```



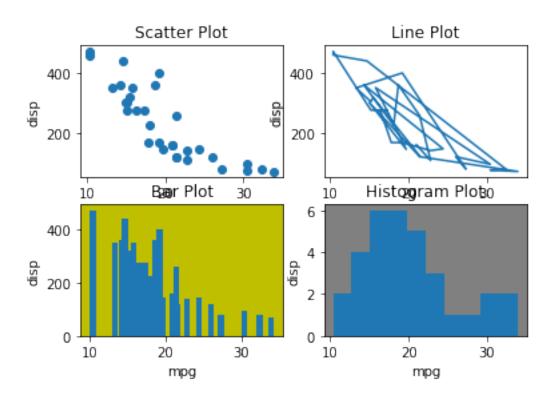
```
Unnamed: 0
                                     disp
                                                                 qsec
                         mpg
                              cyl
                                             hp
                                                 drat
                                                           wt
                                                                       ٧s
                                                                            am
                                                                                gear
            Mazda RX4
                                    160.0
0
                        21.0
                                           110
                                                 3.90
                                                        2.620
                                                                16.46
                                                                         0
                                                                             1
                                                                                    4
1
       Mazda RX4 Wag
                        21.0
                                    160.0
                                            110
                                                 3.90
                                                        2.875
                                                                17.02
                                                                         0
                                                                             1
                                                                                    4
2
           Datsun 710
                        22.8
                                    108.0
                                             93
                                                 3.85
                                                        2.320
                                                                18.61
                                                                         1
                                                                             1
                                                                                    4
3
      Hornet 4 Drive 21.4
                                 6
                                    258.0
                                           110
                                                 3.08
                                                        3.215
                                                               19.44
                                                                         1
                                                                             0
                                                                                    3
                                                                17.02
                                                                                    3
   Hornet Sportabout
                        18.7
                                    360.0
                                            175
                                                 3.15
                                                        3.440
```

```
carb
0 4
1 4
2 1
3 1
4 2
```

- Scatter plot, line plot, barplot and histogram in matplotlib:
- scatter() function for plotting scatter plot
- plot() function for plotting line plot
- bar() function for plotting bar plot
- hist() function for histogram plot
- plt.xlabel() function is used to labeling x-axis.

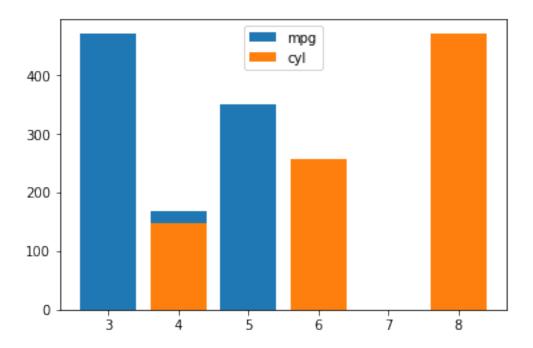
- plt.ylabel() function is used to labeling y-axis.
- plt.title() function is used to give title to graph.

```
In [4]: fig=plt.figure()
        fig.add_subplot(2,2,1) #axis of first graph
        #scatter plot can be drawn using scatter() function
        plt.scatter(data.mpg, data.disp)
        plt.ylabel('disp')
        plt.title('Scatter Plot')
        fig.add_subplot(2,2,2) #axis of second graph
        #line plot can be drawn using plot() function
        plt.plot(data.mpg, data.disp)
        plt.ylabel('disp')
        plt.title('Line Plot')
        fig.add_subplot(2,2,3,facecolor='y') #axis of third graph
        #bar plot can be drawn using bar() function
        plt.bar(data.mpg, data.disp)
        plt.xlabel('mpg')
        plt.ylabel('disp')
        plt.title('Bar Plot')
        fig.add_subplot(2,2,4,facecolor='gray') #axis of second graph
        #bar plot can be drawn using hist() function
        plt.hist(data.mpg)
        plt.xlabel('mpg')
        plt.ylabel('disp')
        plt.title('Histogram Plot')
```



• Plotting bar plot to distinguish displacement by different groups.

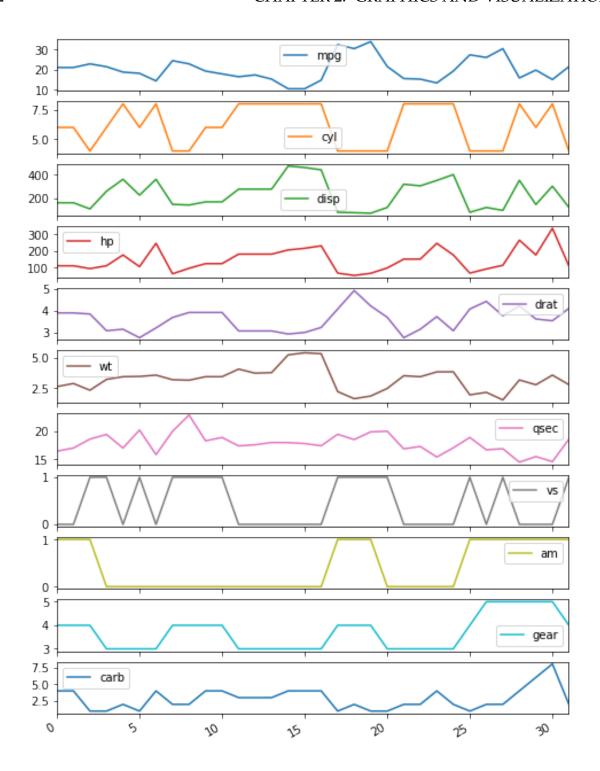
Out[5]: <matplotlib.legend.Legend at 0x202a38ccb00>



• To plot different pline plot in single command for all the variables

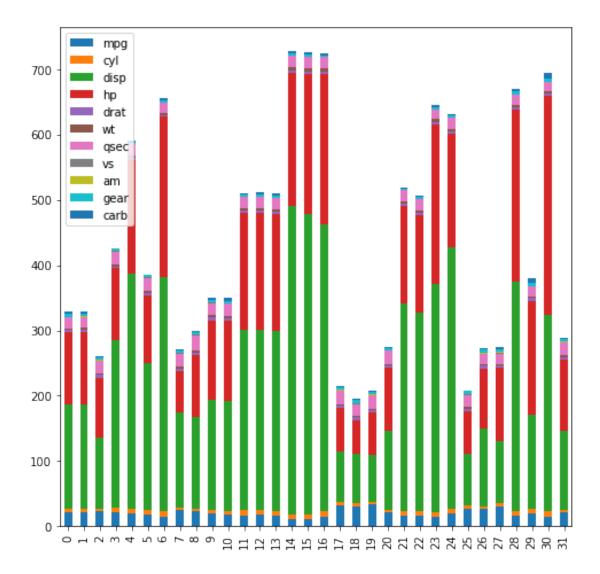
In [6]: data.plot(subplots=True, figsize=(8,12)); plt.legend(loc='best')

Out[6]: <matplotlib.legend.Legend at 0x202a3973278>



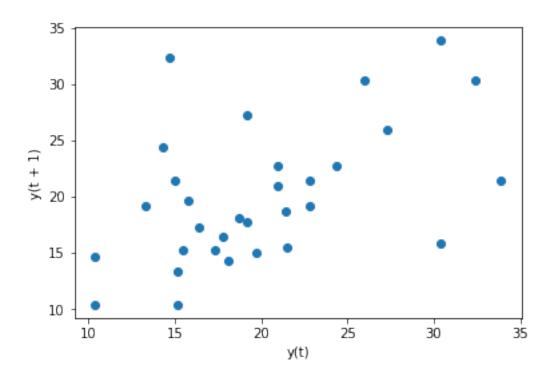
In [7]: data.plot(kind='bar',stacked=True, figsize=(8,8))

Out[7]: <matplotlib.axes._subplots.AxesSubplot at 0x202a4d61828>



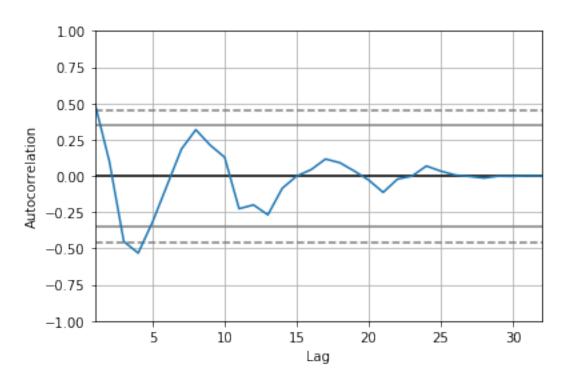
Auto-correlation plots which are a commonly-used for checking randomness in a
data set. This randomness is ascertained by computing auto correlation for data
values at varying time lags. If random, such autocorrelation should be near zero for
any and all time-lag separations. If non-random, then one or more of the autocorrelation will be significantly non-zero. It can be computed using following functions:

Out[8]: <matplotlib.axes._subplots.AxesSubplot at 0x202a5314a58>

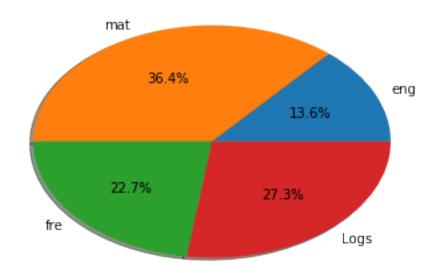


In [9]: autocorrelation_plot(data.mpg)

Out[9]: <matplotlib.axes._subplots.AxesSubplot at 0x202a4df8ef0>



• Pie chart: Pie chart can be easily drawn using pie() function.

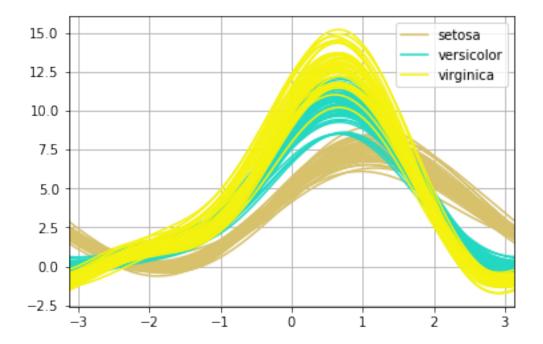


Now using iris dataset to show some more attractive plots in matplotlib

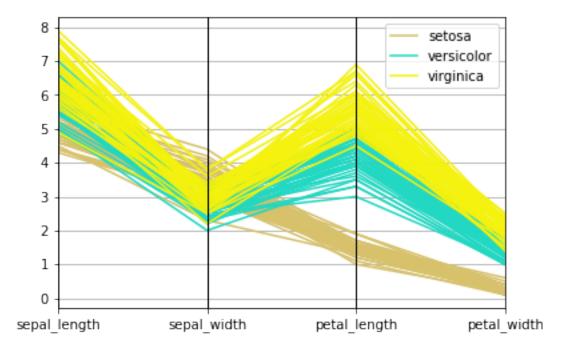
```
In [11]: iris=pd.read_csv("E:/jimmy/J project/Book1.csv",header=0)
In [12]: iris.head()
Out[12]:
            sepal_length
                        sepal_width petal_length petal_width
                                                                    Name
        0
                     5.1
                                  3.5
                                                1.4
                                                             0.2 setosa
                                  3.0
        1
                     4.9
                                                1.4
                                                             0.2 setosa
         2
                                  3.2
                     4.7
                                                1.3
                                                             0.2 setosa
        3
                     4.6
                                  3.1
                                                1.5
                                                             0.2 setosa
         4
                     5.0
                                  3.6
                                                1.4
                                                             0.2 setosa
```

• Andrews plot: Andrews plot or Andrews curve is a way to visualize structure in high-dimensional data.

Out[13]: <matplotlib.axes._subplots.AxesSubplot at 0x202a550b6d8>

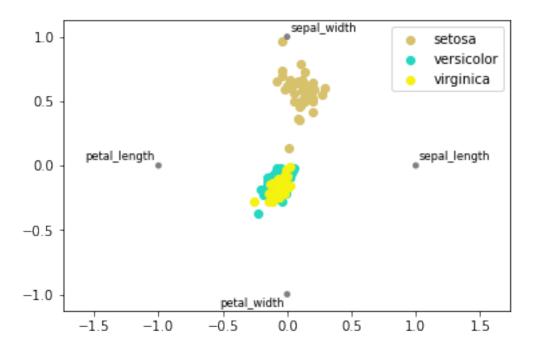


• Parallel coordinate plot: A parallel coordinate plot maps each row in the data table as a line, or profile. Each attribute of a row is represented by a point on the line. This makes parallel coordinate plots similar in appearance to line charts, but the way data is translated into a plot is substantially different.



• RadViz is based on a simple spring tension minimization algorithm. Basically you set up a bunch of points in a plane. In our case, they are equally spaced on a unit circle. Each point represents a single attribute. You then pretend that each sample in the data set is attached to each of these points by a spring, the stiffness of which is proportional to the numerical value of that attribute (they are normalized to unit interval). The point in the plane, where our sample settles to (where the forces acting on our sample are at an equilibrium) is where a dot representing our sample will be drawn. Depending on which class that sample belongs it will be colored differently.

Out[16]: <matplotlib.axes._subplots.AxesSubplot at 0x202a53c2080>



2.2.2 Applications of seaborn

Seaborn is a library for making attractive and informative statistical graphics in python. It is built on top of matplotlib and is integrated with pyData(See https://seaborn.pydata.org/). Some of the features that seaborn offers are:

- Several built-in themes for styling matplotlib graphics
- Tools for choosing color palettes to make beautiful plots that reveal patterns in your data
- Functions for visualizing uni-variate and bi-variate distributions for comparing them between subsets of data
- Tools that fit and visualize linear regression models for different kinds of independent and dependent variables
- Functions that visualize matrices of data and use clustering algorithms to discover structure in those matrices
- A function to plot statistical time series data with flexible estimation and representation of uncertainty around the estimate
- High-level abstractions for structuring grids of plots that let you easily build complex visualizations

Chapter 3

Data Cleaning

Most statistical theory focuses on data modelling, prediction and inference, while it is assumed that our data is inaccurate for analysis. Here, inaccurate data is data that is incorrect, incomplete, out-of-date, or wrongly formatted. In practice, it is very rare that raw data one works with is in correct format or without error. Often our data can be quite messy, if we will do direct analysis it might corrupt our analysis. So we need to process our data before doing any further analysis. A data analyst spend its most of the time in doing data cleaning i.e preparing the data for statistical analysis. Data cleaning is process of correcting the errors and transforming raw data into consistent data that can be analysed. R and python provides good environment for data cleaning.

3.1 Why data cleaning is important?

Activity of transforming raw data into consistent data without errors duplicates and inconsistencies i.e.

- Cleaning and transforming data into high quality data.
- To get reliable and unbiased data.
- To get valid, accurate and complete data.

No quality data, No quality decision: Quality decision must be based on good quality data(data with errors may lead to misleading statistics). The ultimate goal of data cleaning is to make inconsistent data get ready for analysis.

3.2 Problem if we don't clean our data

- Inaccurate or biased conclusions: If we don't clean our data then conclusion made on that data may be inaccurate or biased.
- Violation of statistical assumption: Statistical assumption may violate in raw data. Leading to robust conclusions.

3.3 Data cleaning process

3.3.1 ETL process

ETL i.e. extract transform and load

- Extract: Extract data from original data source
- Transform: Manipulate the data into useful format and clean the data.
- Load: Load the data into data warehouse intended for analysis

3.3.2 Extraction of data using R

R offers wide range of packages to import data in any format such as .txt, .csv, .XLXS/ .XLS(Excel)

• Import data from excel We have to use 'readxl' package to access excel files. In excel file first row should contain variable/column names. library(readxl)

```
dataset = read_excel("C : /Users/example2.xls")
```

Import data from csv In csv file first row should contain variable/column names.
 Where each element is comma separated and header is true. We use command as follow:

```
mydata = read.table("c : /mydata.csv", header = TRUE, sep = ",", row.names = "id")
```

3.3.3 Extraction data using Python

To import data in python we use pandas package. Pandas is a powerful data analysis package. It has several function to read data(if you are using Anaconda, Pandas must be pre installed). Data can be in any of the popular formats - CSV, TXT, XLS/XLSX (Excel), sas7bdat (SAS), Rdata (R) etc. To import data in python we use pandas. using pandas:

Firstly you need to need to load pandas by running command as follow:

import pandas as pd

- To import CSV file import pandas as pd mydata = pd.read_csv("C: /Users/Documents/file1.csv")
- To import excel file import pandas as pd mydata = pd.read_excel("C:/User/file1.xls")

```
• To import text file import pandas as pd 

mydata = pd.read_table("C: /Users/example2.txt")

mydata = pd.read_csv("C: /example2.txt", sep = "\t") (if tab separated file)
```

3.3.4 Transformation

- Rebuild Missing Data: Recreating missing information as and when possible, such as Post codes, states, country, phone area codes, gender, web address from email addresses etc.
- Standardize and Normalize Data: The entries in fields or the categories of the given data set must be homogeneous i.e. all the entries must have the same format for Name, Address, Email, Contact Number, abbreviated/full name of provinces, titles. Moreover, this step ensures that similar information e.g. sir, Mr., Mr are altogether changed over to Mr. Or, on the other hand road, st., strt. are altogether changed over to St.). Convert telephone numbers to their standard format, or as required.
- De-Duplicate data: Identify potential duplicates. Seek high accuracy matches with a tolerance for misspelling, missing values or different address orders. For mission critical data, these results should be manually reviewed and then update the database accordingly.
- Verification to enrich data: Validate the data against internal and external data sources to append value adding info. I.e., business contacts can be validated against yellow pages to verify their current phone number and addresses. Same goes for various other fields including credit ratings, geo-coords, key contacts, employee size, profit, revenue, time zones etc., can be fetched for each company.

3.3.5 Transformation using R

• **Merging Data**: merging two datasets require atleast one variable in common. In R we use merge() function to merge two datasets.

```
mydata1<-data.frame(
   id = c (1:6),
   name = c("Rick","Dan","Michelle","Ryan","Gary","Ryan"),
   salary = c(623.3,515.2,611.0,729.0,843.25,552.1))
mydata2<-data.frame(
   id = c (1:6),
   name = c("Rick","Dan","Michelle","Ryan","Gary","Ryan"),
   age = c(32,31,26,29,36,29))
mydata3<-merge(mydata1,mydata2)
mydata3</pre>
## id name salary age
```

```
## 1 1 Rick 623.30 32

## 2 2 Dan 515.20 31

## 3 3 Michelle 611.00 26

## 4 4 Ryan 729.00 29

## 5 5 Gary 843.25 36

## 6 6 Ryan 552.10 29
```

By default the data frames are merged on the columns with names they both have, but separate specifications of the columns can be given by by.x and by.y. The rows in the two data frames that match on the specified columns are extracted, and joined together.

• **Removing Duplicates**: In R removing duplicates can be done by using unique() function, but another related and interesting function to achieve the same end is duplicated(). dplyr::distinct(): Keep only unique element and is more efficient than unique(). distinct() is best-suited for interactive use.

```
x<-c(0,1,1,1,2,3,6,5,5)
unique(x)

## [1] 0 1 2 3 6 5

df = data.frame(
    A=c("foo", "foo", "foo", "bar"),
    B=c(0,1,1,1,1),
    C=c("A","A","A","B","A"))
print(df)

## A B C
## 1 foo 0 A
## 2 foo 1 A</pre>
```

```
## 3 foo 1 A
## 4 foo 1 B
## 5 bar 1 A
#The dplyr package can be loaded as follow:
# Load
library(dplyr)
#Remove duplicate rows based on all columns:
distinct(df)
##
       ABC
## 1 foo 0 A
## 2 foo 1 A
## 3 foo 1 B
## 4 bar 1 A
#Remove duplicate rows based on certain columns (variables):
distinct(df,A)
##
       Α
## 1 foo
## 2 bar
```

The function distinct() in dplyr package can be used to keep only unique/distinct rows from a data frame. If there are duplicate rows, only the first row is preserved. It's an efficient version of the R base function unique().

- **Missing Observations**: In R, missing values are represented by the symbol NA (not available). Impossible values (e.g., dividing by zero) are represented by the symbol NaN (not a number).
 - Detecting missing values: Missing values can be detected using is.na() function.

```
is.na(df1) # is.na is used to detect which is NA with TRUE or FALSE

## A B C
## [1,] FALSE FALSE FALSE
## [2,] FALSE FALSE TRUE
## [3,] FALSE FALSE TRUE
## [4,] FALSE FALSE TRUE

## [5,] FALSE FALSE TRUE

which(is.na(df1))

## [1] 13 15
```

- Ways to exclude missing values: Math functions generally have a way to exclude missing values in their calculations. mean(), median(), colSums(), var(), sd(), min() and max() all take the na.rm argument. When this is TRUE, missing values are omitted. The default is FALSE, meaning that each of these functions returns NA if any input number is NA.

More functions used to exclude missing values. If you have large number of observations in your dataset, then try deleting (or not to include missing values while model building, for example by setting na.action=na.omit) those observations (rows) that contain missing values.

- * na.omit: Drop out any rows with missing values anywhere in them and forgets them forever.
- * na.exclude: Drop out rows with missing values, but keeps track of where they were (so that when you make predictions, for example, you end up with a vector whose length is that of the original response.)
- * na.pass: returns the object unchanged
- * na.fail: returns the object only if it contains no missing values

```
x <- c(1,2,NA,3)
mean(x) # returns NA

## [1] NA

mean(x, na.rm=TRUE) #return 2

## [1] 2

na.omit(df1) # Drop out rows with missing values

## A B C
## 1 1 a one
## 2 2 c two
## 4 4 f three</pre>
```

A couple of other packages supply more efficient results:

 Hmisc library can be used to replace missing values with mean, median and mode

```
df2 = data.frame(A=c(1,2,3,4,5,NA),
                B=c(0.5,0.8,1.2,NA,0.1,1.5),
                C=c(15, 26, NA, 12, NA, NA))
df2
##
     Α
         B C
## 1 1 0.5 15
## 2 2 0.8 26
## 3 3 1.2 NA
## 4 4 NA 12
## 5 5 0.1 NA
## 6 NA 1.5 NA
library(Hmisc)
## Loading required package: survival
## Loading required package: Formula
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##
     src, summarize
## The following objects are masked from 'package:base':
##
##
     format.pval, units
impute(df2$A, mean) # replace with mean
##
      2 3 4 5 6
## 1 2 3 4 5 3*
impute(df2$B, median) # replace with median
               3 4
##
         2
                         5
## 0.5 0.8 1.2 0.8* 0.1 1.5
impute(df2$C,0) # replace specific number
##
    1
        2
            3
                4
                    5
                        6
## 15 26 0* 12 0* 0*
```

3.3.6 Transformation using Python

- Merging data: Merge or Join operation will combine data sets by linking rows using one or more keys. few merge function arguments
 - left: DataFrame to be merged on the left side.
 - right: DataFrame to be merged on the right side.
 - on: Column names to join on. Must be found on both DataFrame objects.
 - left on: Columns in left DataFrame to use as a join keys.
 - right on: Columns in right DataFrame to use as a join keys.

```
In [10]: from pandas import Series, DataFrame
         import pandas as pd
In [11]: df_1=DataFrame({'key': ['b','b','a','c','a','a','b'],
                       'd':['0','1','2','3','4','5','6']})
         print(df_1)
  d key
0
  0
       b
1
  1
      b
2
  2
      а
3
  3
      С
4
  4
       а
  5
       a
6
  6
      b
In [12]: df_2=DataFrame({'key': ['a', 'b', 'd'],
                       'd2':['0','1','2']})
         print(df_2)
 d2 key
  0
0
       a
  1
      b
2
  2
       d
In [13]: pd.merge(df_1,df_2)
Out[13]:
            d key d2
                b
              b 1
         1
           1
         2 6 b 1
         3
           2
              a 0
         4
           4
                a 0
         5
           5
                a 0
```

```
In [14]: df_3=DataFrame({'lkey':['b','b','a','c','a','a','b'],
                            'data1':range(7)})
          print(df_3)
   data1 lkey
0
        0
             b
        1
1
             b
2
        2
3
        3
             С
4
        4
             a
        5
5
             а
6
        6
             b
In [15]: df_4=DataFrame({'rkey':['a','b','d'],
                            'data2': range(3)})
          print(df_3)
   data1 lkey
0
        0
1
        1
             b
2
        2
             а
3
        3
             С
4
        4
             a
5
        5
             а
6
        6
In [16]: pd.merge(df_3,df_4,left_on='lkey',right_on='rkey',how='outer')
             data1 lkey
Out[16]:
                           data2 rkey
                0.0
                             1.0
          1
                1.0
                       b
                             1.0
                                     b
          2
                6.0
                       b
                             1.0
                                     b
          3
                2.0
                             0.0
                        a
                                     а
          4
                4.0
                             0.0
                                     а
          5
                5.0
                             0.0
                        a
                                     а
          6
                3.0
                        С
                             {\tt NaN}
                                   {\tt NaN}
          7
                             2.0
                NaN
                     {\tt NaN}
                                     d
```

• **Removing Duplicates**: Duplicate rows may be found in DataFrame for number of reasons. In python removing duplicates can be done using drop_duplicates(). DataFrame.drop_duplicates() return DataFrame with duplicate rows removed, optionally only considering certain columns

```
In [8]: import pandas as pd
        df = pd.DataFrame({"A":["foo", "foo", "foo", "bar"],
                           "B": [0,1,1,1], "C": ["A", "A", "B", "A"]})
        print(df)
       В С
     Α
  foo
       0 A
1 foo 1 A
2 foo 1 B
3 bar
      1 A
In [9]: df.drop_duplicates(subset=['A', 'C'], keep=False)
Out[9]:
             A B C
        2 foo 1 B
        3 bar 1 A
where keep: {'first', 'last', False}, default 'first'
```

- first : Drop duplicates except for the first occurrence.
- last: Drop duplicates except for the last occurrence.
- False : Drop all duplicates.
- Missing Observations: By "missing" we simply mean NA ("not available") or "not present for whatever reason". Many data sets simply arrive with missing data, either because it exists and was not collected or it never existed. In pandas, one of the most common ways that missing data is introduced into a data set is by re-indexing

```
In [28]: import pandas as pd
         import numpy as np
        df = pd.DataFrame(np.random.randn(5, 3),
                          index=['a', 'c', 'e', 'f', 'h'],
                          columns=['one', 'two', 'three'])
         df['four'] = 'bar'
         df['five'] = df['one'] > 0
        print(df)
                         three four
                                      five
        one
                 two
a -0.336057 0.512864 -0.854062 bar False
c -0.424267 -0.101321 0.948349 bar False
 0.957720 -0.602851 0.859344 bar
                                      True
f 0.734610 -0.769397 0.355850 bar
                                      True
h -1.733099 -0.451442 -0.785071 bar False
```

```
In [29]: df2 = df.reindex(['a', 'b', 'c', 'd', 'e', 'f', 'g', 'h'])
         print(df2)
         one
                    two
                            three four
                                           five
a -0.336057
              0.512864 -0.854062
                                    bar
                                          False
b
        NaN
                               {\tt NaN}
                                    {\tt NaN}
                                            NaN
                   NaN
  -0.424267 -0.101321
                         0.948349
                                    bar
                                          False
        NaN
                               NaN NaN
                                            NaN
d
                   NaN
   0.957720 -0.602851
                         0.859344 bar
                                           True
   0.734610 -0.769397
f
                         0.355850 bar
                                           True
        NaN
                   NaN
                               {\tt NaN}
                                    {\tt NaN}
                                            NaN
h -1.733099 -0.451442 -0.785071
                                          False
                                    bar
```

pandas objects are equipped with various data manipulation methods for dealing with missing data.

- Filling missing values: fillna
 - * The fillna function can "fill in" NA values with non-NA data in a couple of ways, which we illustrate:
 - * Replace NA with a scalar value
 - * Fill gaps forward or backward

```
In [30]: df2.fillna(0)
Out[30]:
                                   three four
                                                 five
                 one
                           two
                                           bar
         a -0.336057
                     0.512864 -0.854062
                                                False
           0.000000 0.000000
                                0.000000
                                             0
                                                    0
         c -0.424267 -0.101321
                               0.948349
                                           bar
                                                False
         d 0.000000 0.000000
                               0.000000
                                             0
           0.957720 -0.602851
                                0.859344
                                           bar
                                                 True
         f
          0.734610 -0.769397
                                                 True
                                0.355850
                                           bar
         g 0.000000 0.000000
                                0.000000
                                             0
         h -1.733099 -0.451442 -0.785071
                                               False
                                          bar
In [31]: df.fillna(method='pad')
Out[31]:
                                                 five
                           two
                                   three four
                 one
         a -0.336057 0.512864 -0.854062
                                                False
                                           bar
         c -0.424267 -0.101321
                                0.948349
                                               False
                                           bar
         e 0.957720 -0.602851
                                0.859344
                                           bar
                                                 True
         f 0.734610 -0.769397
                                0.355850
                                           bar
                                                 True
         h -1.733099 -0.451442 -0.785071
                                          bar False
```

To remind you, these are the available filling methods:

- pad / ffill:Fill values forward.
- bfill / backfill:Fill values backward.

You may wish to simply exclude labels from a data set which refer to missing data. To do this, use the dropna method:

```
In [36]: df2.dropna(axis=0)
Out[36]:
                                   three four
                                                 five
                 one
                           two
         a -0.336057 0.512864 -0.854062
                                          bar
                                                False
         c -0.424267 -0.101321
                               0.948349
                                               False
                                          bar
          0.957720 -0.602851
                                0.859344
                                                 True
                                          bar
         f 0.734610 -0.769397 0.355850
                                          bar
                                                 True
         h -1.733099 -0.451442 -0.785071
                                          bar False
```

You can also fillna using a dict or Series that is align-able. The labels of the dict or index of the Series must match the columns of the frame you wish to fill. The use case of this is to fill a DataFrame with the mean of that column.

```
In [38]: df2.fillna(df2.mean())
Out[38]:
                 one
                            two
                                    three four
                                                  five
         a -0.336057
                      0.512864 -0.854062
                                           bar
                                                 False
                                                   0.4
         b -0.160219 -0.282429
                                 0.104882
                                            NaN
         c -0.424267 -0.101321
                                0.948349
                                                 False
                                            bar
         d -0.160219 -0.282429
                                                   0.4
                                0.104882
                                            {\tt NaN}
         e 0.957720 -0.602851
                                                  True
                                0.859344
                                           bar
         f 0.734610 -0.769397
                                0.355850
                                                  True
                                            bar
         g -0.160219 -0.282429
                                0.104882
                                            {\tt NaN}
                                                   0.4
         h -1.733099 -0.451442 -0.785071
                                           bar False
```

Chapter 4

Explanatory Data Analysis

Explanatory Data Analysis (EDA) is an approach to data analysis. EDA is a critical step in analyzing data. Its where the experimenter takes the bird's eye of the data and tries to make some sense of it. Exploratory Data Analysis takes place after gathering and cleaning data, and is often implemented before any formal statistical technique is applied. Among the main purposes of this type of analysis are of course getting to know our data, its tendencies and its quality, and also to check or even start formulating our hypothesis. Here are some reasons why we use EDA:

- Detection of mistakes.
- Gain maximum insight into the dataset and its underlying structure.
- Determining relationships among the explanatory variables.
- Check assumptions associated with any model fitting or hypothesis test.
- Detection of outliers

Most EDA techniques are graphical in nature with a few quantitative techniques. The reason for the heavy reliance on graphics is that by its nature the main role of EDA is to open-mindedly explore. The particular graphical techniques employed in EDA are often quite simple consisting of various techniques of:

- Plotting the raw data (such as data traces, histograms, bihistograms, probability plots, lag plots, block plots, and Youden plots.
- Plotting simple statistics such as mean plots, standard deviation plots, box plots, and main effects plots of the raw data.

Types of Exploratory Data Analysis:

EDA falls into four main areas:

- Univariate EDA- Looking at one variable of interest, like age, height, income level etc.
- Multivariate EDA- Analysis of multiple variables at the same time.

4.1 Univarate Explanatory Data Analysis

In univariate EDA our interest is analyzing each variable, like age, gender, income etc. The usual goal of univariate EDA is to better appreciate the "sample distribution". Outlier detection is also a part of this analysis. Below are some techniques used in univariate EDA:

- Summary statistics: Summary statistics summarize and provide information about your sample data. It includes where the average lies and whether your data is skewed. Summary statistics fall into three main categories:
 - Measures of location and central tendency(e.g. mean, median, mode etc.).
 - Measure of dispersion(e.g. Standard deviation)
 - Measures of shape(e.g. skewness and kurtosis)

A common collection of statistics used as summary statistics are the five-number summary i.e. the minimum, 25th percentile, median, 75th percentile, maximum of the data

- Histogram: The purpose of a histogram is to graphically summarize the distribution of a univariate data set. The histogram graphically shows the following:
 - Center (i.e., the location) of the data.
 - Spread (i.e., the scale) of the data.
 - Skewness of the data.
 - Presence of outliers.
 - Presence of multiple modes in the data.
- Stem and leaf plots: A simple substitute to histogram is stem and leaf plot. Nevertheless, a histogram is generally considered better for estimating the shape of a sample distribution than the stem and leaf plot.
- Boxplots: Boxplot is visualization of five-number summary with more information. Boxplot graphically shows the following:
 - Displays variable's location and spread.
 - Provide indication of data symmetry and skewness.
 - Shows outliers
- Density plot: A Density Plot visualizes the distribution of data over a continuous interval or time period.

4.2 Multivariate Explanatory Data Analysis

Multivariate EDA techniques generally show the relationship between two or more variables in the form of either cross-tabulation or statistics. Below are some techniques used in univariate EDA:

- Correlation matrix: Correlation matrix measures degree of relationship between the variables under consideration. The degree of relationship is expressed by coefficient which range from correlation ($-1 \le r \le +1$). It deals with the association between two or more variables.
- Scatter plot: Scatter plot is a diagrammatic representation of bivariate data. It is used to plot data points on a horizontal and a vertical axis in the attempt to show how much one variable is affected by another. Scatter plots are important in statistics because they can show the extent of correlation. Besides showing the extent of correlation, a scatter plot shows the sense of the correlation:
 - If the vertical (or y-axis) variable increases as the horizontal (or x-axis) variable increases, the correlation is positive.
 - If the y-axis variable decreases as the x-axis variable increases or vice-versa, the correlation is negative.
 - If it is impossible to establish either of the above criteria, then the correlation is zero.
- Multiple Boxplot: Unlike regular box plots in which the range of values of one variable is represented, the multiple box plot represents ranges of values of multiple variables. Multiple Boxplot can be used to visualize multiple variables together. It can be used for comparing two or more variables.
- Multiple histogram: A panel of histograms enables you to compare the data distributions of different groups. You can create the histograms in a column (stacked vertically) or in a row.

4.3 Explanatory Data Analysis using R

We will use a popular dataset in R library "dataset" and the dataset used is cars.

Description: The data give the speed of cars and the distances taken to stop. Note that the data were recorded in the 1920s.

Data is imported using read.csv() function of pandas module.

```
data<-read.csv("E:/jimmy/J project/cars.csv", header = T,sep = ',')
head(data)

## speed dist
## 1 4 2</pre>
```

We can see some basic characteristics of the dataset using dim(), str(), names(), head(), tail(), summary() functions.

```
dim(data)
## [1] 50
str(data)
## 'data.frame': 50 obs. of 2 variables:
## $ speed: int 4 4 7 7 8 9 10 10 10 11 ...
## $ dist : int 2 10 4 22 16 10 18 26 34 17 ...
names(data)
## [1] "speed" "dist"
head(data)
##
     speed dist
        4
             2
## 1
## 2
        4
            10
## 3
            4
## 4
       7
            22
## 5
        8
            16
## 6
            10
tail(data)
##
      speed dist
        23
## 45
             54
## 46
        24
             70
## 47
        24
             92
## 48
        24
            93
## 49
        24
           120
## 50
        25
             85
summary(data)
##
       speed
                       dist
## Min. : 4.0
                  Min. : 2.00
## 1st Qu.:12.0 1st Qu.: 26.00
## Median :15.0
                 Median : 36.00
## Mean :15.4
                Mean : 42.98
   3rd Qu.:19.0
                3rd Qu.: 56.00
## Max. :25.0 Max. :120.00
```

In R we are using dplyr package for doing EDA. Some of the key "verbs" provided by the dplyr package are

- select: return a subset of the columns of a data frame, using a flexible notation
- filter: extract a subset of rows from a data frame based on logical conditions
- arrange: reorder rows of a data frame
- rename: rename variables in a data frame
- mutate: add new variables/columns or transform existing variables
- summaries / summarize: generate summary statistics of different variables in the data frame, possibly within strata

Installing the dplyr package

The dplyr package can be installed from CRAN. To install from CRAN, just run > install.packages("dplyr")

```
\#After\ installing\ the\ package\ it\ is\ important\ to\ load\ it\ into\ your\ R\ session\ library(dplyr)
```

The arrange() function is used to reorder rows of a data frame according to one of the variables/columns.

```
head(arrange(data, speed))
     speed dist
##
## 1
         4
               2
## 2
         4
             10
## 3
         7
              4
         7
             22
## 4
## 5
         8
              16
             10
## 6
```

The select() function can be used to select columns of a data frame that you want to focus on. Often you'll have a large data frame containing "all" of the data, but any given analysis might only use a subset of variables or observations.

```
head(select(data, speed))

## speed
## 1     4
## 2     4
## 3     7
## 4     7
## 5     8
## 6     9
```

```
tail(select(data, speed))

## speed
## 45   23
## 46   24
## 47   24
## 48   24
## 49   24
## 50   25
```

Renaming a variable in a data frame in R is surprisingly hard to do! The rename() function is designed to make this process easier.

```
d=head(rename(data, velocity=speed))
##
    velocity dist
           4
## 1
## 2
           4
               10
           7
               4
## 3
## 4
           7 22
           8
## 5
               16
## 6
                10
```

Univariate Explanatory data analysis

• five-number summary: five-number summary can be computed using fivenum() function. It's often a bit nice to use the summary() function.

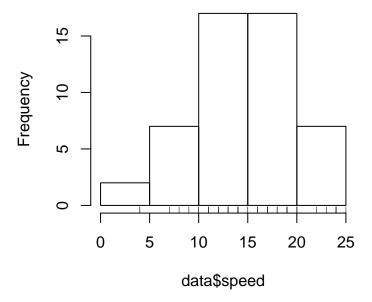
```
fivenum(data$speed)
## [1] 4 12 15 19 25

summary(data$speed)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 4.0 12.0 15.0 15.4 19.0 25.0
```

• Histogram: Histogram can be drawn using hist() function. We can get a little more detail by using the rug() function to show us the actual data points.

```
hist(data$speed, main="Histogram of Speed")
rug(data$speed)
```

Histogram of Speed



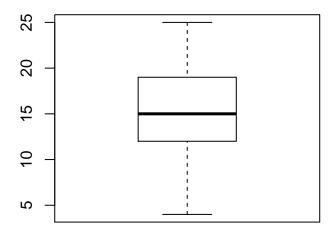
• Stem-leaf plot: Stem-leaf plot can be drawn using stem() function.

```
stem(data$speed)
##
##
     The decimal point is at the |
##
##
      4 | 00
##
      6 | 00
      8 | 00
##
     10 | 00000
##
     12 |
          00000000
##
##
     14 |
          0000000
##
     16
          00000
##
     18
          0000000
     20 |
          00000
##
##
     22 | 00
     24 | 00000
##
```

• Box plot: Box-plot can be drawn using boxplot() function.

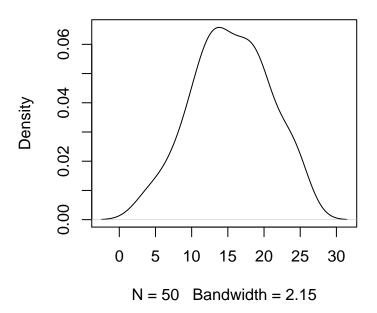
```
boxplot(data$speed, main="Boxplot of Speed")
```

Boxplot of Speed



• Density plot: Density plot can be drawn using plot(density()) where density() function return the density data and plot() function returns the result.

Density plot of Speed



Multivariate Explanatory data analysis

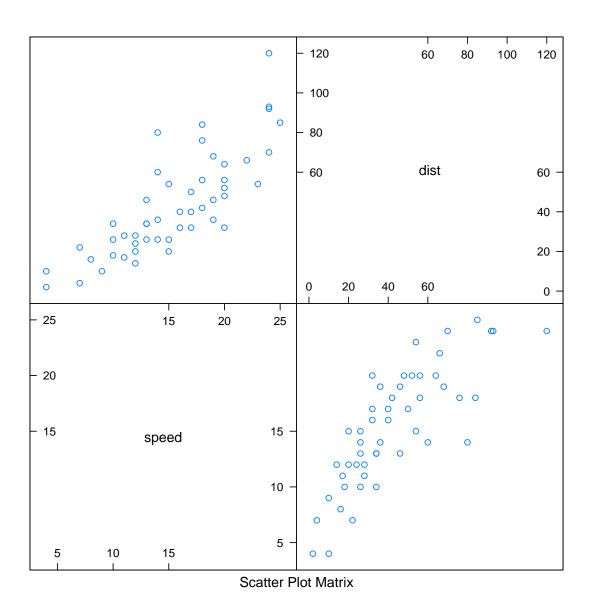
• Correlation matrix:The function cor() can be used to compute a correlation matrix. The function rcorr() [in Hmisc package] can be used to compute the significance levels for pearson and spearman correlations.

```
cor(data)

## speed dist
## speed 1.0000000 0.8068949
## dist 0.8068949 1.0000000
```

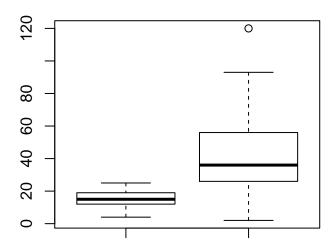
• Scatter plot: The function splom()[in the package lattice], can be used to display a scatter plot. The function chart.Correlation()[in the package PerformanceAnalytics], can be used to display a chart of a scatter plot and correlation between variables.

```
library(lattice)
splom(data)
```



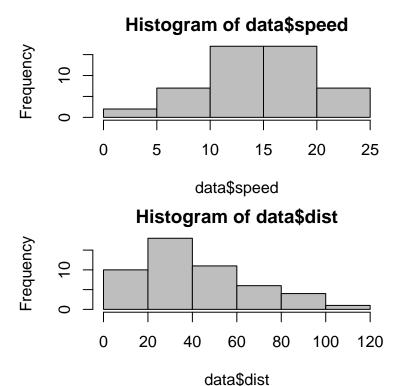
• Multiple boxplot: Multiple boxplot can be simply drawn by adding up variable in boxplot() function.

Boxplot of Speed and distance



• Multiple Histogram: Mulptiple histogram can be simply drawn using hist() function for different variables of interest after par() function which divides the graph window in different rows and columns.

```
par(mfrow = c(2, 1), mar = c(4, 4, 2, 1))
hist(data$speed, col = "gray")
hist(data$dist, col = "gray")
```



4.4 Explanatory Data Analysis using Python

We will use a popular dataset in R library "dataset" and the dataset used is cars.

Description: The data give the speed of cars and the distances taken to stop. Note that the data were recorded in the 1920s.

Data is imported using read_csv() function of pandas module.

Out[1]:		speed	dist
	1	4	2
	2	4	10
	3	7	4
	4	7	22
	5	8	16
	6	9	10
	7	10	18
	8	10	26
	9	10	34
	10	11	17
	11	11	28

```
12
        12
               14
13
        12
               20
14
        12
               24
15
        12
               28
16
        13
               26
17
        13
               34
18
        13
               34
19
               46
        13
20
        14
               26
21
               36
        14
22
        14
               60
23
        14
               80
24
        15
               20
25
        15
               26
26
        15
               54
27
        16
               32
28
               40
        16
29
               32
        17
30
        17
               40
31
        17
               50
32
               42
        18
33
               56
        18
34
               76
        18
35
        18
               84
36
        19
               36
37
        19
               46
38
        19
               68
39
        20
               32
40
        20
               48
41
        20
               52
42
        20
               56
43
        20
               64
44
        22
               66
45
        23
               54
46
        24
               70
47
        24
               92
48
        24
               93
49
        24
              120
50
        25
               85
```

• We can see some basic characteristics of the dataset using DataFrame.info(), DataFrame.tail(), DataFrame.head(), DataFrame.loc[], DataFrame.describe() functions.

```
In [2]: data.info()
```

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 50 entries, 1 to 50
Data columns (total 2 columns):
         50 non-null int64
speed
dist
         50 non-null int64
dtypes: int64(2)
memory usage: 1.2 KB
In [3]: data.tail()
Out[3]:
            speed
                   dist
               24
        46
                     70
        47
               24
                     92
               24
        48
                     93
        49
               24
                    120
        50
               25
                     85
In [4]: data.head()
Out[4]:
           speed
                  dist
        1
               4
                      2
        2
               4
                    10
        3
               7
                     4
               7
        4
                     22
        5
               8
                     16
In [5]: data.loc[3:6]
Out[5]:
           speed dist
        3
               7
                     4
        4
               7
                     22
        5
               8
                    16
        6
               9
                     10
In [6]: data.describe()
Out[6]:
                   speed
                                 dist
        count
               50.000000
                            50.000000
        mean
               15.400000
                            42.980000
        std
                5.287644
                            25.769377
        min
               4.000000
                          2.000000
        25%
               12.000000
                            26.000000
        50%
               15.000000
                            36.000000
        75%
               19.000000
                            56.000000
```

25.000000 120.000000

max

• Univariate Explanatory data Analysis

• five-number summary:five number summary can be computed using Data.Frame.variable.describe() function.

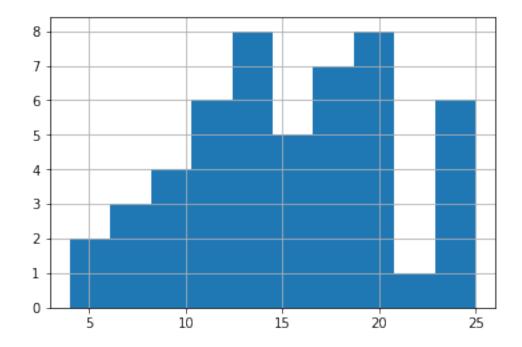
In [7]: data.speed.describe()

```
Out[7]: count
                 50.000000
        mean
                 15.400000
        std
                  5.287644
        min
                  4.000000
        25%
                 12.000000
        50%
                 15.000000
        75%
                 19.000000
                 25.000000
        max
```

Name: speed, dtype: float64

• Histogram: Histogram can be drawn using hist() function from matplotlib module.

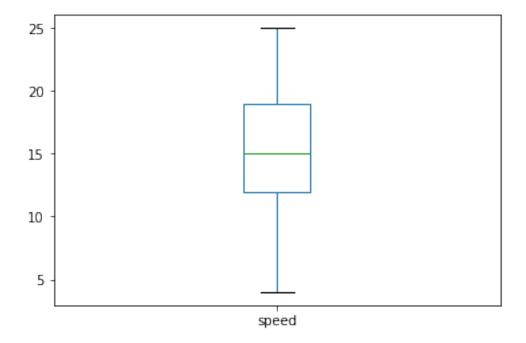
Out[8]: <matplotlib.axes._subplots.AxesSubplot at 0x27dd9d87cf8>



• Box-plot: Box-plot can be drawn using DataFrame.plot.box() function from matplotlib module.

```
In [9]: data['speed'].plot.box()
```

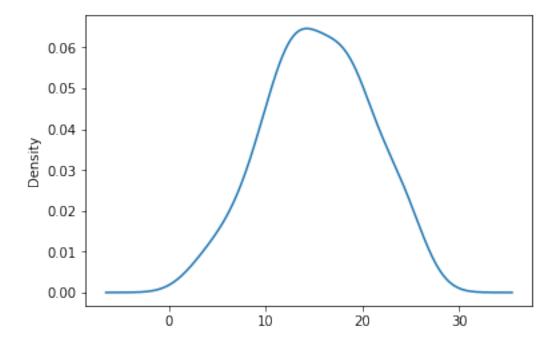
Out[9]: <matplotlib.axes._subplots.AxesSubplot at 0x27dd9dc2710>



• Density-plot: Density-plot can be drawn using DataFrame.plot.kde() function from matplotlib module.

```
In [10]: data['speed'].plot.kde()
```

Out[10]: <matplotlib.axes._subplots.AxesSubplot at 0x27dd94a0160>



Note: There are some of the tools in seaborn module for examining univariate and bivariate distributions. That can be used as follows:

Multivariate Explanatory Data Analysis*

• Correlation matrix: DataFrame.corr(method='pearson') compute pairwise correlation of columns. where argument method:{"pearson,'kendall,'spearman'}

• Scatter-plot: scatter_matrix() function in pandas.plotting module can be used to plot Scatter-plot matrix.

```
In [12]: from pandas.tools.plotting import scatter_matrix as scattermatrix

In [13]: scattermatrix(data, diagonal='kde') #diagonal='kde'
argument shows density plot in diagonal by default it will show histogram.
```

^{*}import seaborn as sns #for calling seaborn module

^{*} sns.distplot() #will give density plot

^{*} sns.distplot(x, kde=False, rug=True) #will give histogram plot

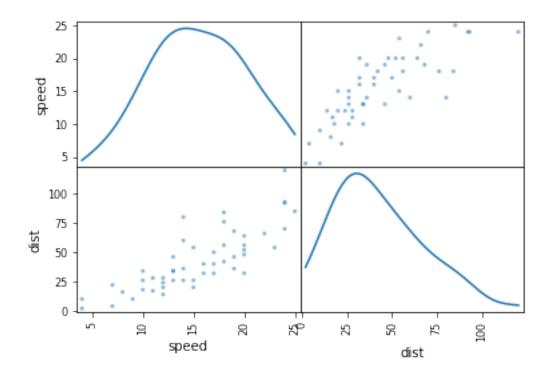
^{*} sns.distplot(x, hist=False, rug=True) #will give density plot

Out[13]: array([[<matplotlib.axes._subplots.AxesSubplot object at
0x0000027DDBD52438>,

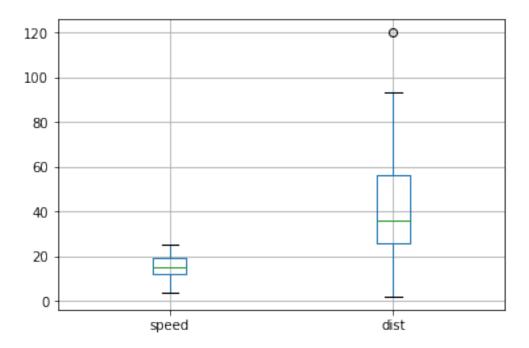
<matplotlib.axes._subplots.AxesSubplot object at
0x0000027DDBDB0048>],

[<matplotlib.axes._subplots.AxesSubplot object at 0x0000027DDBDE7588>,

<matplotlib.axes._subplots.AxesSubplot object at
0x0000027DDBE20550>]], dtype=object)

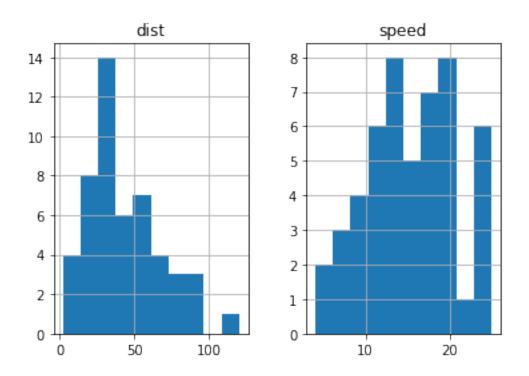


• Multiple Box-plot: Multiple Box-plot can be drawn using DataFrame.boxplot(column=[]) as follow:



• Multiple Histogram: Multiple Histogram can be drawn similarly like multiple boxplot using DataFrame.hist(column=[]) as follow:

```
In [15]: data.hist(column=['speed','dist'])
```



Note: For more visualization tools on pandas refer to https://pandas.pydata.org/pandas-docs/stable/visualization.html

Chapter 5

Regression Analysis

Regression analysis is used to know the nature of relationship between two or more variables i.e. probable form of mathematical relation between X and Y (where X represent various explanatory variables and Y represents response variable). Regression is also used to predict or estimate the value of one variable(response or dependent variable) corresponding to given value of another variable (explanatory or independent variable). **Linear model**: A model is said to be linear when it is linear in parameter. **Non-linear model**: A model is said to be non-linear when it is non-linear in parameter.

5.1 Linear Regression Analysis

In scatter diagram, quite often it is seen that there is a tendency for the point of two variable to cluster around some curve called the curve of regression. If curve is straight line it is called line of regression. And it tells, there is linear regression among the variables. If curve is a line, then it tells there is non linear regression among the variables. The Linear regression model is given by:

$$Y = X\beta + \varepsilon \tag{5.1}$$

where:

- Y denotes the dependent(or response) variable.
- X denotes the k independent(or explanatory) variable $x_1, x_2, ..., x_k$.
- β denotes the regression coefficient associated with $x_1, x_2, ..., x_k$ variables.

We write equation (1) as $y = x_1\beta_1 + x_2\beta_2 + ... + x_k\beta_k + \varepsilon$ for k explanatory variables. This is called as multiple linear regression model.

Example: Income and education of a person are related it is expected that for an average higher level of education provides higher income. So, the simple linear regression model can be

expressed as:

$$Income = \beta_0 + \beta_1 education + \varepsilon_i \tag{5.2}$$

 β_0 reflects income when education is zero as it is expected that even an illiterate person can also have some income and β_1 reflects average change in income with respect to per unit change in education. Further, this model neglects that most people have higher income when they are older then they are younger.

So, better model is multiple linear regression model and can be expressed as:

$$Income = \beta_0 + \beta_1 education + \beta_2 age + \varepsilon_i$$
 (5.3)

5.1.1 Assumptions in Linear regression model

The linear regression has five key assumptions:

- There should be a linear relationship between dependent and independent variables.
- The error term should be normally distributed.
- The error term must have constant variance. The presence of constant variance among error term is known as homoskedasticity. And the absence of constant variance among the error term is known as heteroskedasticity.
- The independent variables should not be correlated. Absence of this phenomenon is called multicollinearity.
- There should be no correlation between the residual or error term. Absence of this phenomenon is known as Autocorrelation

Note: Normal probability plot and plot of residual versus corresponding fitted values is helpful in detecting several common type of model assumption.

5.2 Logistic Regression Analysis

When we have binary variable or categorical variable (dependent variable) we use logistic regression. Logistic model is used for prediction of probability of occurrence of an event by fitting data to a logistic curve. In this regression, the response variable has only two possible outcome coded as 0 or 1. It makes use of several predictor variables that may be either categorical or numerical.

Example: The probability that a person has a heart attack within a specified time period can be predicted from knowledge of person's age, sex, cholesterol level, weight, etc.

Logistic model belongs to a class of model known as **Generalized Linear Model**(GLM). The logistic regression model uses the odd ratio, which is given by:

$$Oddratio = \frac{probability of an event of interest}{1 - probability of an event of interest}$$
(5.4)

The logistic regression is based on log odd ratio, ln(odd ratio). Equation given below defines logistic regression model for k independent variables.

$$ln(Oddratio) = \beta_0 + x_1\beta_1 + x_2\beta_2 + \dots + x_k\beta_k + \varepsilon_i$$
 (5.5)

where:

- k= no. of independent variable in model
- ε_i =random error in observation i

5.3 Regression Analysis using R

Description of dataset: For analysis we are using a dataset in which record times in 1984 for Scottish Hill races are recorded having 35 observation and whose component variables are following:

- dist: distance in miles(on the map).
- climb: total height gained during the route, in feet.
- time: record time in minutes.

5.3.1 Multiple Linear Regression

Loading dataset in R

```
Hills_data<-read.csv("E:/jimmy/j2/Hills.csv",header=TRUE)
head(Hills_data)
##
               X dist climb
                             time
     Greenmantle 2.5 650 16.083
       Carnethy 6.0 2500 48.350
## 2
## 3 Craig Dunain 6.0 900 33.650
         Ben Rha 7.5 800 45.600
## 4
      Ben Lomond 8.0 3070 62.267
## 5
        Goatfell 8.0 2866 73.217
names(Hills_data)
## [1] "X" "dist" "climb" "time"
```

Fitting Multiple Linear Regression:

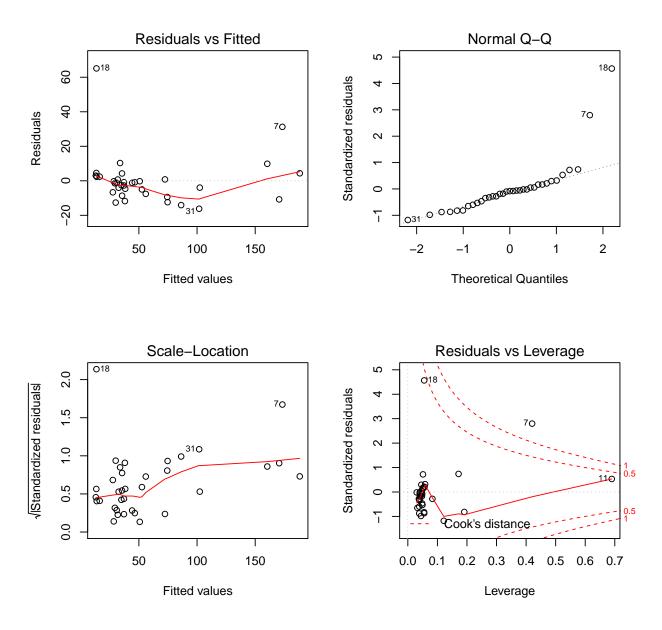
```
#model for multiple linear regression model
model1=lm(time~dist+climb,data=Hills_data)
summary(model1)
##
## Call:
## lm(formula = time ~ dist + climb, data = Hills_data)
##
## Residuals:
    Min 1Q Median 3Q Max
## -16.215 -7.129 -1.186 2.371 65.121
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.992039 4.302734 -2.090 0.0447 *
## dist 6.217956 0.601148 10.343 9.86e-12 ***
## climb
            ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.68 on 32 degrees of freedom
## Multiple R-squared: 0.9191, Adjusted R-squared: 0.914
## F-statistic: 181.7 on 2 and 32 DF, p-value: < 2.2e-16
```

To check assumption of model we can use following steps:

For a quick check of model assumption we can use plot() function which give 2*2 plot containing following:

- Residual versus fitted values.
- Normal quantile-quantile plot.
- Standardized residual versus Fitted values.
- Residual versus Leverage.

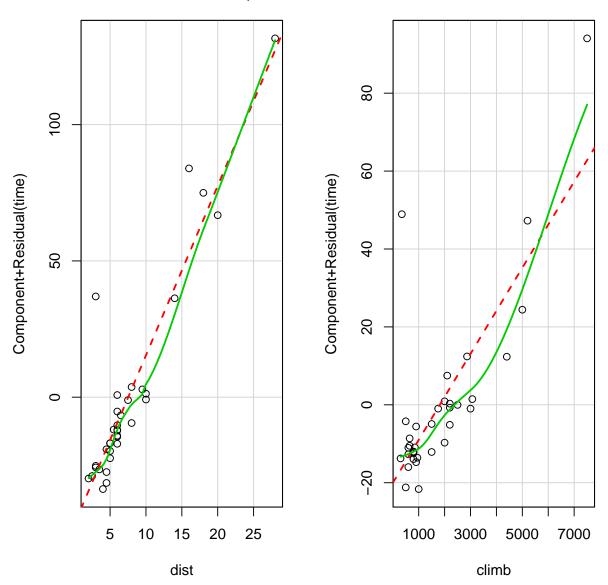
```
par(mfrow=c(2,2)) #used to partion are window into 2 rows and 2 columns
plot(model1)
```



• Component residual plot can be drawn using cr.Plots() function in library(car)

```
## Warning: package 'car' was built under R version 3.4.4
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
## recode
crPlots(model1)
```





5.3.2 Logistic Regression

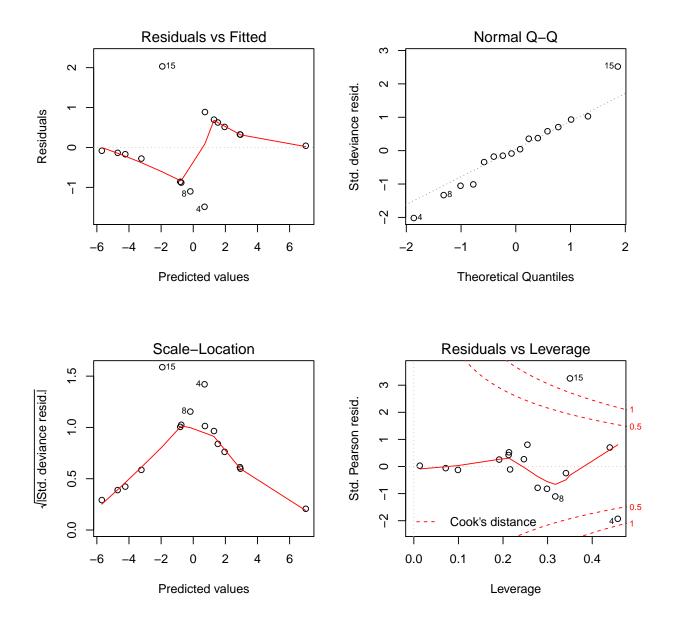
Description of data: For analysis we are using dataset of Contraceptive use data, showing the distribution of 1607 currently married and fecund women interviewed in Fiji Fertility Survey, according to age, education, desire for more children and current use of contraception. Loading dataset in R

```
c_data=read.csv("E:/jimmy/j2/contraceptive_use.xlsx", header=TRUE)
print(c_data)
## age education wantsMore notUsing using
```

```
## 1
        <25
                    low
                                          53
                                                  6
                               yes
## 2
                                                  4
        <25
                    low
                                          10
                                no
## 3
        <25
                   high
                               yes
                                         212
                                                 52
## 4
        <25
                                                 10
                   high
                                          50
                                no
## 5
     25-29
                    low
                               yes
                                          60
                                                 14
## 6 25-29
                    low
                                          19
                                                 10
                                no
## 7
     25-29
                                                 54
                   high
                               yes
                                         155
## 8 25-29
                   high
                                          65
                                                 27
                                no
## 9 30-39
                    low
                                         112
                                                 33
                               yes
## 10 30-39
                    low
                                          77
                                                 80
                                no
## 11 30-39
                   high
                               yes
                                         118
                                                 46
## 12 30-39
                   high
                                          68
                                                 78
                                no
## 13 40-49
                                          35
                    low
                               yes
                                                  6
## 14 40-49
                    low
                                          46
                                                 48
                                no
## 15 40-49
                                                  8
                   high
                                           8
                               yes
## 16 40-49
                                                 31
                   high
                                no
                                          12
```

• contrasts() function shows how variable is dummyfied by R. str() function shows the structure of data.

```
contrasts(c_data$education)
##
        low
## high
          0
## low
          1
contrasts(c_data$wantsMore)
##
       yes
## no
## yes
str(c_data)
## 'data.frame': 16 obs. of 5 variables:
              : Factor w/ 4 levels "<25","25-29",..: 1 1 1 1 2 2 2 2 3 3 ...
   $ education: Factor w/ 2 levels "high", "low": 2 2 1 1 2 2 1 1 2 2 ...
##
## $ wantsMore: Factor w/ 2 levels "no", "yes": 2 1 2 1 2 1 2 1 2 1 ...
    $ notUsing : int 53 10 212 50 60 19 155 65 112 77 ...
    $ using
               : int
                      6 4 52 10 14 10 54 27 33 80 ...
mymodel<-glm(wantsMore~notUsing+using+education,data=c_data,family = binomial</pre>
             (link='logit'))
par(mfrow=c(2,2))
plot(mymodel)
```



5.4 Regression Analysis using Python

Description of dataset: For analysis we are using a dataset in which record times in 1984 for Scottish Hill races are recorded having 35 observation and whose component variables are following:

- dist: distance in miles(on the map).
- climb: total height gained during the route, in feet.
- time: record time in minutes.

Statsmodels is a python module that provide functions for estimation of many different statistical model, as well as conducting statistical test and statistical data exploration. We are using statsmodels for conducting multiple linear regression and checking assumptions of model by analyzing the residuals (See http://www.statsmodels.org/dev/regression.html) Loading all important modules used in regression analysis:

Loading Dataset for Multiple regression analysis:

```
Unnamed: 0
                        dist
                              climb
                                         time
0
         Greenmantle
                         2.5
                                 650
                                       16.083
1
             Carnethy
                         6.0
                               2500
                                       48.350
2
        Craig Dunain
                         6.0
                                 900
                                       33.650
3
              Ben Rha
                         7.5
                                800
                                       45.600
4
           Ben Lomond
                         8.0
                               3070
                                       62.267
5
             Goatfell
                         8.0
                               2866
                                       73.217
6
        Bens of Jura
                        16.0
                               7500
                                      204.617
7
         Cairnpapple
                         6.0
                                800
                                       36.367
8
               Scolty
                         5.0
                                 800
                                       29.750
9
             Traprain
                         6.0
                                 650
                                       39.750
10
         Lairig Ghru
                        28.0
                                2100
                                      192.667
11
               Dollar
                         5.0
                               2000
                                       43.050
12
                         9.5
                               2200
                                       65.000
              Lomonds
13
         Cairn Table
                         6.0
                                500
                                       44.133
14
           Eildon Two
                         4.5
                               1500
                                       26.933
15
                        10.0
                               3000
                                       72.250
            Cairngorm
16
          Seven Hills
                        14.0
                               2200
                                       98.417
17
           Knock Hill
                         3.0
                                350
                                       78.650
18
                         4.5
                               1000
                                       17.417
           Black Hill
19
           Creag Beag
                         5.5
                                 600
                                       32.567
20
        Kildcon Hill
                         3.0
                                 300
                                       15.950
21
                         3.5
    Meall Ant-Suidhe
                               1500
                                       27.900
22
      Half Ben Nevis
                         6.0
                               2200
                                       47.633
23
                         2.0
                                 900
             Cow Hill
                                       17.933
24
       N Berwick Law
                         3.0
                                 600
                                       18.683
                         4.0
                                2000
25
                                       26.217
           Creag Dubh
26
            Burnswark
                         6.0
                                800
                                       34.433
```

```
27
           Largo Law
                       5.0
                              950
                                    28.567
             Criffel
28
                       6.5
                             1750
                                    50.500
29
              Acmony
                       5.0
                              500
                                    20.950
30
           Ben Nevis 10.0
                             4400
                                    85.583
         Knockfarrel
31
                       6.0
                             600
                                    32.383
32
       Two Breweries 18.0
                             5200 170.250
33
           Cockleroi
                       4.5
                             850
                                    28.100
34
        Moffat Chase 20.0
                             5000 159.833
In [3]: print(Hills_data.shape, Hills_data.dtypes)
(35, 4) Unnamed: 0
                       object
dist
              float64
climb
                int64
time
              float64
dtype: object
  Fitting a Multiple regression model
In [4]: model=sm.ols(formula='time~dist+climb',data=Hills_data).fit()
In [5]: print(dir(model)) #qives number of objects in model.
['HCO_se', 'HC1_se', 'HC2_se', 'HC3_se', '_HCCM', '__class__', '__
delatt__', '__dict__', '__dir__', '__doc__', '__eq__', '_ _forma
__','__ge__', '__getattribute__', '__gt__', '__hash__
', '__init__','__init_subclass__', '__le__', '__lt__', '__
module__','__ne__','__new__', '__reduce__', '__reduce_ex__
', '__repr__', '__setattr__', '__sizeof__', '__str__', '__
subclasshook__', '__weakref__','_cache', '_data_attr', '_get_robust
cov_results', '_is_nested', '_wexog_singular_values', 'aic', 'bic', 'bse
', 'centered_tss', 'compare_f_test', 'compare_lm_test', 'compare_lr_test
', 'condition_number', 'conf_int', 'conf_int_el','cov_HCO', 'cov_HC1','
cov_HC2', 'cov_HC3', 'cov_kwds', 'cov_params', 'cov_type', 'df_model', 'df
_resid', 'eigenvals', 'el_test', 'ess', 'f_pvalue', 'f_test', 'fittedvalues
', 'fvalue', 'get_influence', 'get_prediction', 'get_robustcov_results','
initialize', 'k_constant', 'llf', 'load', 'model', 'mse_model', 'mse_resid',
'mse_total', 'nobs', 'normalized_cov_params', 'outlier_test', 'params',
'predict', 'pvalues', 'remove_data', 'resid', 'resid_pearson', 'rsquared',
'rsquared_adj', 'save', 'scale', 'ssr', 'summary', 'summary2', 't_test', '
tvalues', 'uncentered_tss','use_t', 'wald_test', 'wald_test_terms', 'wresid']
```

summary() function displays details of the result.

In [6]: print(model.summary())

$\alpha + \alpha$			
111 6	Roamoda	an Rai	711 I ± 7
ULD	Regressi	on nea	sure

Dep. Variabl	e:		time	R-sq	uared:		0.919
Model:			OLS	Adj.	R-squared:		0.914
Method:		Least Squ	ares	F-st	atistic:		181.7
Date:	S [.]	un, 25 Mar	2018	Prob	(F-statistic)	:	3.40e-18
Time:		17:0	04:52	Log-	Likelihood:		-142.11
No. Observat	ions:		35	AIC:			290.2
Df Residuals	:		32	BIC:			294.9
Df Model:			2				
Covariance T	уре:	nonro	bust				
========	========	========	=====	=====	=========	======	=======
	coef	std err		t	P> t	[0.025	0.975]
Intercept	-8.9920	4.303	-2	2.090	0.045	-17.756	-0.228
dist	6.2180	0.601	10	0.343	0.000	4.993	7.442
climb	0.0110	0.002	Ę	5.387	0.000	0.007	0.015
Omnibus:	=======	 47	 7.910	===== Durb	========= in-Watson:	======	2.249
Prob(Omnibus):	(0.000	Jarq	ue-Bera (JB):		233.976
Skew:		3	3.026	-	(JB):		1.56e-51
Kurtosis:		14	1.127	Cond	. No.		4.20e+03
========	=======	=======			==========	======	=======

Warnings:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 4.2e+03. This might indicate that there are strong multicollinearity or other numerical problems.

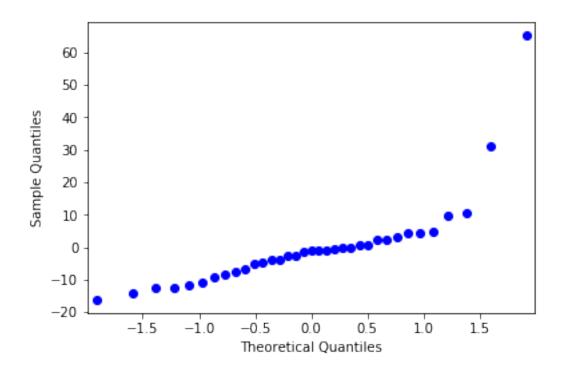
The coefficient of determination is equal to R-squared value i.e. 0.846. Warning message is indicating that there might be strong multicollinearity present.

To check assumption of model we can use following steps

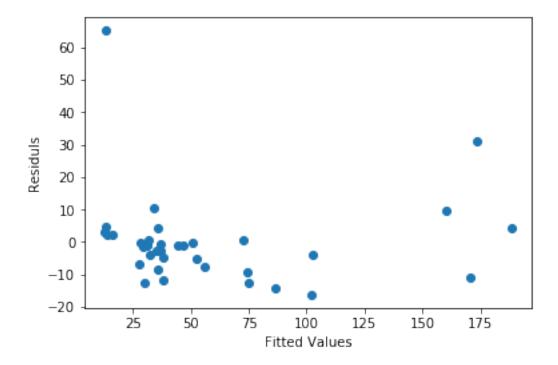
• Normal Probability plot to show assumption of normality of residuals.

```
In [7]: import statsmodels.api as sma
    sma.qqplot(model.resid)
```

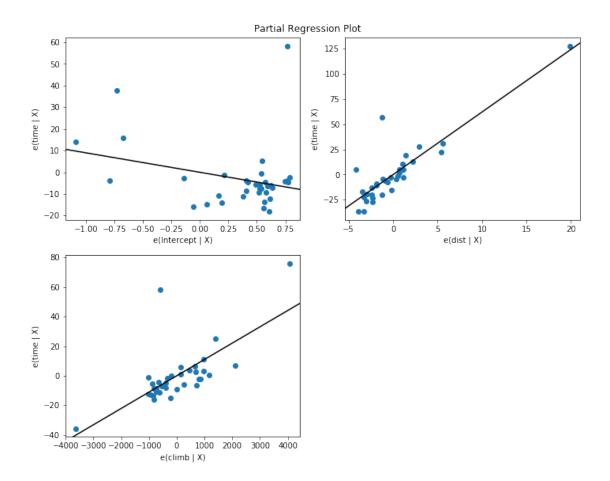
Out[7]:



• residual vs fitted value plot to show holding assumptions

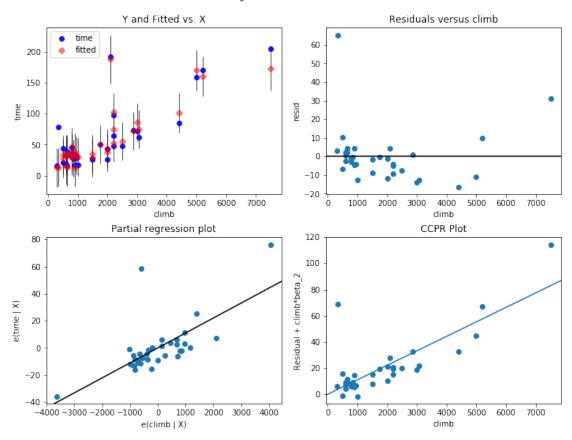


• For quick check of all the regressors, you can use plot_partregress_grid() function.



- The function plot_regress_exog() gives a 2*2 plot containing following:
 - *Dependent variable and fitted values confidence interval versus independent variable chosen.
 - * Residual versus independent variable chosen.
 - * Partial regression plot.
 - * Component-component plus residual plot. This function can be used quickly to check assumptions w.r.t a single regressor.

Regression Plots for climb



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