

Examples and Exercises from Think Stats, 2nd Edition

<http://thinkstats2.com> (<http://thinkstats2.com>)

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```
In [11]:  from __future__ import print_function, division

          %matplotlib inline

          import warnings
          warnings.filterwarnings('ignore', category=FutureWarning)

          import numpy as np
          import pandas as pd


          import random

          import thinkstats2
          import thinkplot
```

Exercises

**Exercise12-1 Page No 161: The linear model I used in this chapter has the obvious drawback that it is linear, and there is no reason to expect prices to change linearly over time. We can add flexibility to the model by adding a quadratic term, as we did in Section 11.3.**

Use a quadratic model to fit the time series of daily prices, and use the model to generate predictions. You will have to write a version of `RunLinearModel` that runs that quadratic model, but after that you should be able to reuse code from the chapter to generate predictions.

```
In [59]:  # Solution goes here  
# As per line 17, statsmodels to run a linear model of price as a function of  
# I have referred the fit method in time series and linear regression  
# Here Daily data passed, then fit the time series of daily prices  
  
def RunQuadraticModel(daily):  
  
    daily['years2'] = daily.years**2  
    # smf.ols - Linear Regression, also called Ordinary Least Squares (OLS)  
    # this comes from statsmodel  
    model = smf.ols('ppg ~ years + years2', data=daily)  
    results = model.fit()  
    #returning the model and results  
    return model, results
```

```
In [60]: # Solution goes here
# I referred Line15 in Time Series about dailies and mentioned in my write up
# calling the method of RunQuadraticModel

name = 'high'
daily = dailies[name]
model, results = RunQuadraticModel(daily)

#ols Regression output will be displayed by using the summary method
results.summary()
```

Out[60]:

OLS Regression Results

| | | | |
|--------------------------|------------------|----------------------------|-----------|
| Dep. Variable: | ppg | R-squared: | 0.455 |
| Model: | OLS | Adj. R-squared: | 0.454 |
| Method: | Least Squares | F-statistic: | 517.5 |
| Date: | Tue, 10 Nov 2020 | Prob (F-statistic): | 4.57e-164 |
| Time: | 18:42:13 | Log-Likelihood: | -1497.4 |
| No. Observations: | 1241 | AIC: | 3001. |
| Df Residuals: | 1238 | BIC: | 3016. |
| Df Model: | 2 | | |
| Covariance Type: | nonrobust | | |

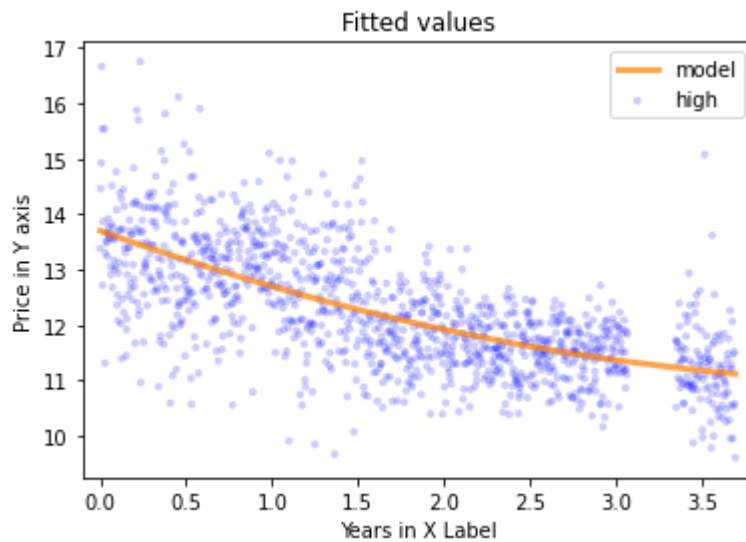
| | coef | std err | t | P> t | [0.025 | 0.975] |
|------------------|---------|---------|---------|-------|--------|--------|
| Intercept | 13.6980 | 0.067 | 205.757 | 0.000 | 13.567 | 13.829 |
| years | -1.1171 | 0.084 | -13.326 | 0.000 | -1.282 | -0.953 |
| years2 | 0.1132 | 0.022 | 5.060 | 0.000 | 0.069 | 0.157 |

| | | | |
|-----------------------|--------|--------------------------|----------|
| Omnibus: | 49.112 | Durbin-Watson: | 1.885 |
| Prob(Omnibus): | 0.000 | Jarque-Bera (JB): | 113.885 |
| Skew: | 0.199 | Prob(JB): | 1.86e-25 |
| Kurtosis: | 4.430 | Cond. No. | 27.5 |

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

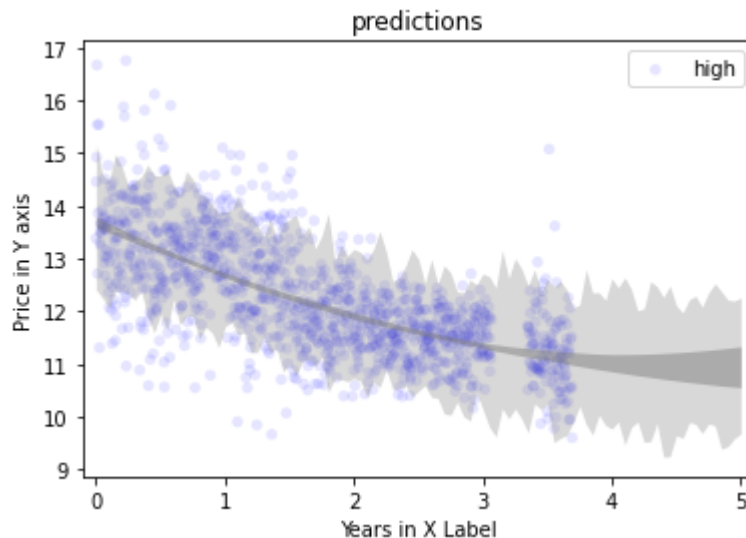
```
In [61]: # Solution goes here  
# plotting the fitted values  
# I referred Line 45  
PlotFittedValues(model, results, label=name)  
thinkplot.Config(title='Fitted values',  
                  xlabel='Years in X Label',  
                  xlim=[-0.1, 3.8],  
                  ylabel='Price in Y axis')
```



```
In [62]: # Solution goes here
#NumPy used for linspace
# I referred Line 52

years = np.linspace(0, 5, 101)

#Scatter plots
thinkplot.Scatter(daily.years, daily.ppg, alpha=0.1, label=name)
PlotPredictions(daily, years, func=RunQuadraticModel)
thinkplot.Config(title='predictions',
                  xlabel='Years in X Label',
                  xlim=[years[0]-0.1, years[-1]+0.1],
                  ylabel='Price in Y axis')
```



Exercise 12.2 Page Number 161 : Write a definition for a class named `SerialCorrelationTest` that extends `HypothesisTest` from Section 9.2. It should take a series and a lag as data, compute the serial correlation of the series with the given lag, and then compute the p-value of the observed correlation.

Use this class to test whether the serial correlation in raw price data is statistically significant. Also test the residuals of the linear model and (if you did the previous exercise), the quadratic model.

```
In [63]: # Solution goes here
# Solution

class SerialCorrelationTest(thinkstats2.HypothesisTest):
    """Tests serial correlations by permutation."""

    def TestStatistic(self, data):
        """Computes the test statistic.

        data: tuple of xs and ys
        """
        series, lag = data
        test_stat = abs(SerialCorr(series, lag))
        return test_stat

    def RunModel(self):
        """Run the model of the null hypothesis.

        returns: simulated data
        """
        series, lag = self.data
        permutation = series.reindex(np.random.permutation(series.index))
        return permutation, lag
```

```
In [64]: # Solution goes here

# Testing the prices by using pvalue method

name = 'high'
daily = dailies[name]

series = daily.ppg
test = SerialCorrelationTest((series, 1))
pvalue = test.PValue()
```

```
In [65]: # Solution goes here

# verifying the acutal value vs p value
#I reffered line 55 with P value testing

_, results = RunLinearModel(daily)
series = results.resid
test = SerialCorrelationTest((series, 1))
pvalue = test.PValue()
print(test.actual, pvalue)
```

```
0.07570473767506261 0.001
```

In [66]:  *# Solution goes here*

```
# verifying the acutal value vs p value by using n residuals  
#I reffered line 55 with P value testing
```

```
_, results = RunQuadraticModel(daily)  
series = results.resid  
test = SerialCorrelationTest((series, 1))  
pvalue = test.PValue()  
print(test.actual, pvalue)
```

```
0.05607308161289916 0.043
```

Observation

p values as 0.001 & p values as 0.043 which shows that statistically highly significant.

Worked example: There are several ways to extend the EWMA model to generate predictions. One of the simplest is something like this:

1. Compute the EWMA of the time series and use the last point as an intercept, `inter` .
2. Compute the EWMA of differences between successive elements in the time series and use the last point as a slope, `slope` .
3. To predict values at future times, compute $\text{inter} + \text{slope} * \text{dt}$, where `dt` is the difference between the time of the prediction and the time of the last observation.

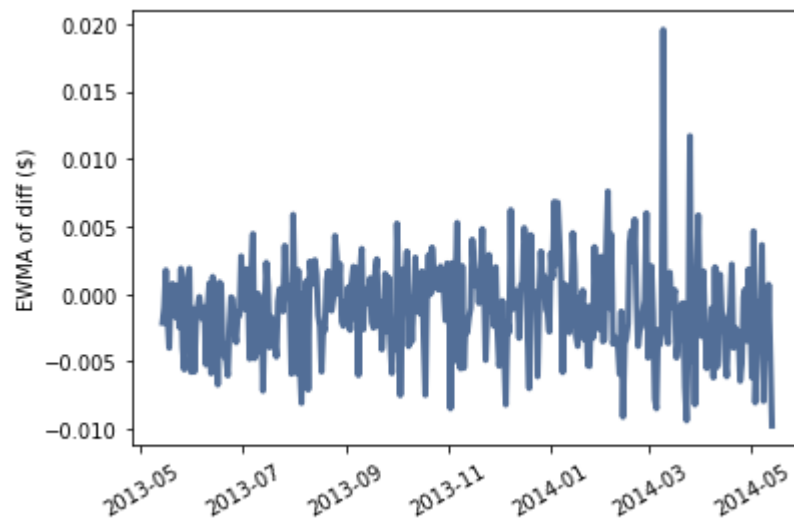
```
In [51]: name = 'high'
daily = dailies[name]

filled = FillMissing(daily)
diffs = filled.ppg.diff()

thinkplot.plot(diffs)
plt.xticks(rotation=30)
thinkplot.Config(ylabel='Daily change in price per gram ($)')
```



```
In [52]: filled['slope'] = diffs.ewm(span=365).mean()
thinkplot.plot(filled.slope[-365:])
plt.xticks(rotation=30)
thinkplot.Config(ylabel='EWMA of diff ($)')
```




```
In [53]: # extract the last inter and the mean of the last 30 slopes
start = filled.index[-1]
inter = filled.ewma[-1]
slope = filled.slope[-30:].mean()

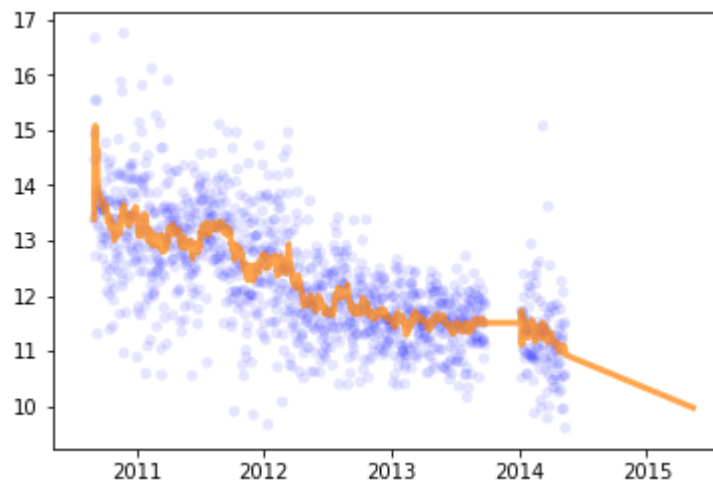
start, inter, slope
```

```
Out[53]: (Timestamp('2014-05-13 00:00:00', freq='D'),
10.92951876545549,
-0.00262422491642447)
```

```
In [54]: # reindex the DataFrame, adding a year to the end
dates = pd.date_range(filled.index.min(),
                      filled.index.max() + np.timedelta64(365, 'D'))
predicted = filled.reindex(dates)
```

```
In [55]: # generate predicted values and add them to the end
predicted['date'] = predicted.index
one_day = np.timedelta64(1, 'D')
predicted['days'] = (predicted.date - start) / one_day
predict = inter + slope * predicted.days
predicted.ewma.fillna(predict, inplace=True)
```

```
In [56]: # plot the actual values and predictions
thinkplot.Scatter(daily.ppg, alpha=0.1, label=name)
thinkplot.Plot(predicted.ewma, color='#ff7f00')
```



As an exercise, run this analysis again for the other quality categories.

```
In [ ]: #
```