

$$(3) \quad (5x+4y)dx + (4x-8y^3)dy = 0$$

$$\Pi(x,y) = 5x+4y \quad y \quad N(x,y) = 4x-8y^3$$

Wago

$$\frac{\partial \Pi}{\partial y} = 4 = \frac{\partial N}{\partial x}$$

Por definición $\exists f(x,y)$ /

$$\frac{\partial f}{\partial x} = \Pi(x,y) \quad y \quad \frac{\partial f}{\partial y} = N(x,y)$$

$$\frac{\partial f}{\partial x} = 5x+4y$$

$$\bullet \quad \int \partial f = \int (5x+4y)dx$$

$$f(x,y) = \frac{5x^2}{2} + 4yx + g(y) \quad \dots \quad (1)$$

$$\bullet \quad \frac{\partial f}{\partial y} = 4x - 8y^3$$

$$4x + \frac{\partial g}{\partial y} = 4x - 8y^3$$

$$\int \partial g = \int -8y^3 dy$$

$$g(y) = -2y^4 \quad \dots \quad (2)$$

(wsgo)

$$f(x,y) = C$$

de ① y ②

$$\frac{5x^2}{2} + 4xy - 2y^4 = C$$

(Solução implícita)

⑩ $(x^3 + y^3)dx + 3xy^2dy = 0$

$$\Pi(x,y) = x^3 + y^3 \quad \text{y} \quad N(x,y) = 3xy^2$$

Existe $f(x,y)$ tal que

$$\frac{\partial f}{\partial x} = \Pi(x,y) \quad \text{y} \quad \frac{\partial f}{\partial y} = N(x,y)$$

$$\rightarrow \frac{\partial f}{\partial x} = x^3 + y^3$$

$$\int \partial f = \int (x^3 + y^3)dx$$

$$f(x,y) = \frac{x^4}{4} + y^3x + g(y) \quad \therefore \quad ①$$

$$\rightarrow \frac{\partial f}{\partial y} = 3xy^2 \rightarrow 3y^2x + \frac{\partial g}{\partial y} = 3xy^2$$

$$\frac{\partial g}{\partial y} = 0$$

$$\int \partial g = \int 0 dy$$

$$g(y) = 0 \quad \dots \quad (2)$$

wegs

$$f(x,y) = c$$

$$y \text{ d}c = (1) y (2)$$

$$\frac{x^4}{y} + y^3x + 0 = c$$

SOL $\frac{x^4}{y} + y^3x = c$ ~~y~~

$$(2) \quad (x+y)^2 dx + (2xy+x^2-1) dy = 0, \quad y(1) = 1$$

Ecuación de la forma

$$\Pi(x,y) + N(x,y) dy = 0$$

$$\rightarrow \frac{\partial \Pi}{\partial y} = 2(x+y) = \frac{\partial N}{\partial x} \quad \text{... Ecuación exacta.}$$

Ahora por definición \exists

$$f(x,y) /:$$

$$\frac{\partial f}{\partial x} = \Pi(x,y) \quad y \quad \frac{\partial f}{\partial y} = N(x,y)$$

$$\rightarrow \frac{\partial f}{\partial x} = (x+y)^2$$

$$\int \partial f = \int (x+y)^2 dx \rightarrow f(x,y) = \frac{(x+y)^3}{3} + g(y)$$

$$\rightarrow \frac{\partial f}{\partial y} = 2xy + x^2 - 1$$

$$(x+y)^2 + \frac{\partial g}{\partial y} = 2xy + x^2 - 1$$

$$\cancel{x^2+y^2} + 2xy + \cancel{\frac{\partial g}{\partial y}} = 2xy + x^2 - 1$$

④

$$\frac{\partial g}{\partial y} = -1 - y^2$$

$$\int \partial g = - \int (1 + y^2) dy$$

$$g(y) = -y - \frac{y^3}{3} \dots \textcircled{2}$$

Weg 0 $f(x,y) = c$

↓ $\textcircled{3}$ y $\textcircled{2}$

$$\frac{(x+y)^3}{3} + \left(-y - \frac{y^3}{3}\right) = c$$

$$\frac{(x+y)^3}{3} - \frac{3y}{3} - \frac{y^3}{3} = c$$

$$\frac{(x+y)^3 - y^3 - 3y}{3} = c$$

Weg 0

$$\frac{(z+1)^3 - z^3 - 3z}{3} = c$$

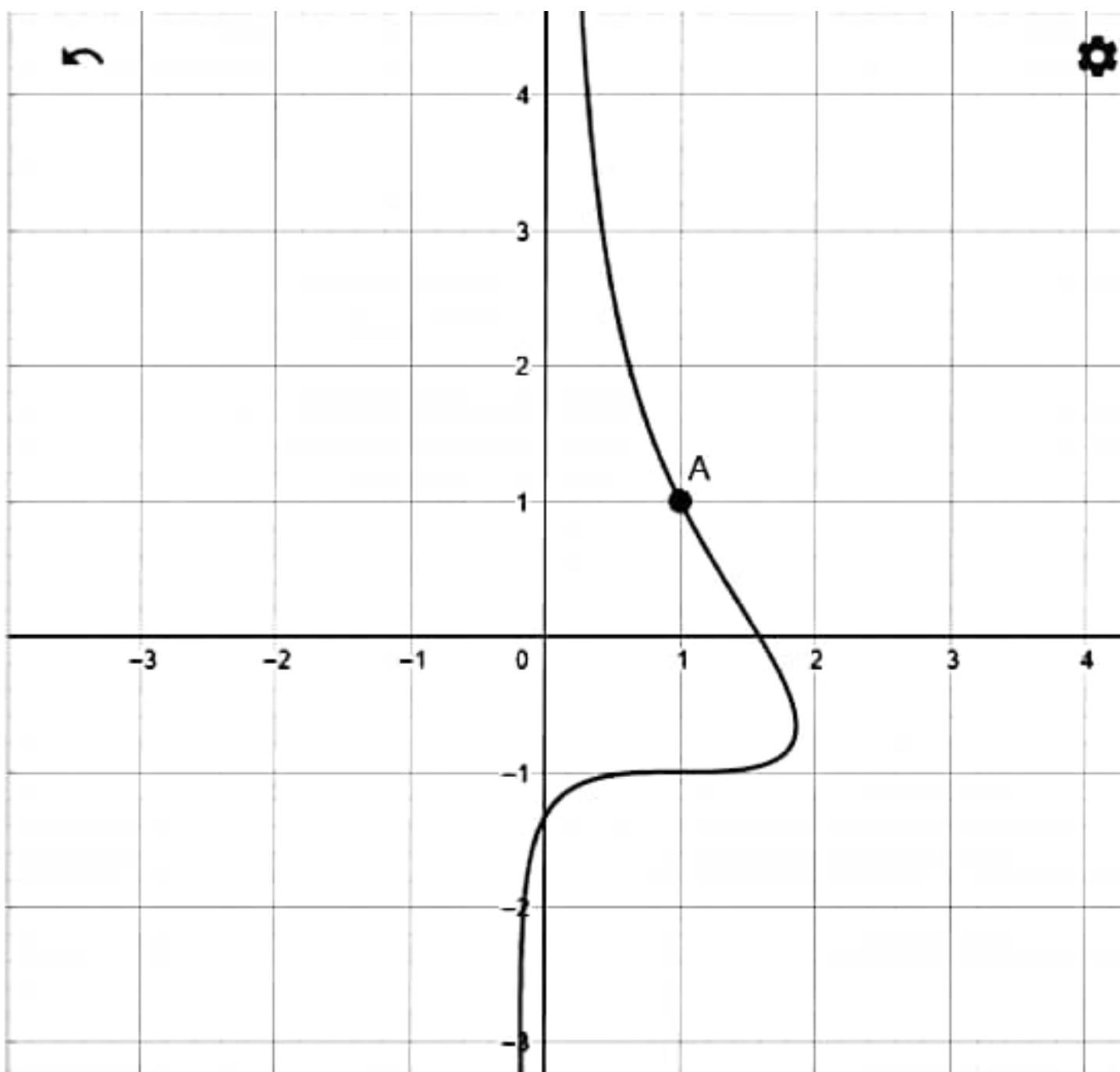
$$c = \frac{5}{3}$$

Sol $(x+y)^3 - y^3 - 3y = 4$

eq1: $(x + y)^3 - y^3 - 3y = 4$

A = (1, 1)

Input...



(23)

$$(4y+2t-5)dt + (6y+4t-1)dy = 0 \quad y(-1) = 2$$

Ecación de la forma

$$P(t,y) + Q(t,y) = 0$$



$$\begin{aligned} P(t,y) &= (4y+2t-5) \\ Q(t,y) &= (6y+4t-1) \end{aligned}$$

Por def. \exists

$$f(t,y) \mid \frac{\partial f}{\partial t} = P(t,y) \quad \text{y} \quad \frac{\partial f}{\partial y} = Q(t,y)$$

Wogo

$$\rightarrow \frac{\partial f}{\partial t} = 4y+2t-5 \rightarrow \int \partial f = \int (4y+2t-5) dt$$

$$f(t,y) = 4yt+t^2-5t+g(y) \quad \text{oo. } ①$$

$$\rightarrow \frac{\partial f}{\partial y} = 6y+4t-1$$

$$yt + \frac{\partial g}{\partial y} = 6y+4t-1 \rightarrow \int \partial g = \int (6y-1) dy$$

$$g(y) = 3y^2 - y \quad \text{oo. } ②$$

Wago

$$f(t, y) = c$$

de ① y ②

$$4yt + t^2 - st + g(y^2 - y) = c$$

Reemplazando

$$4(2)(-1) + (-1)^2 - 5(-1) + 3(2) - 2 = c$$

$$c = 24$$

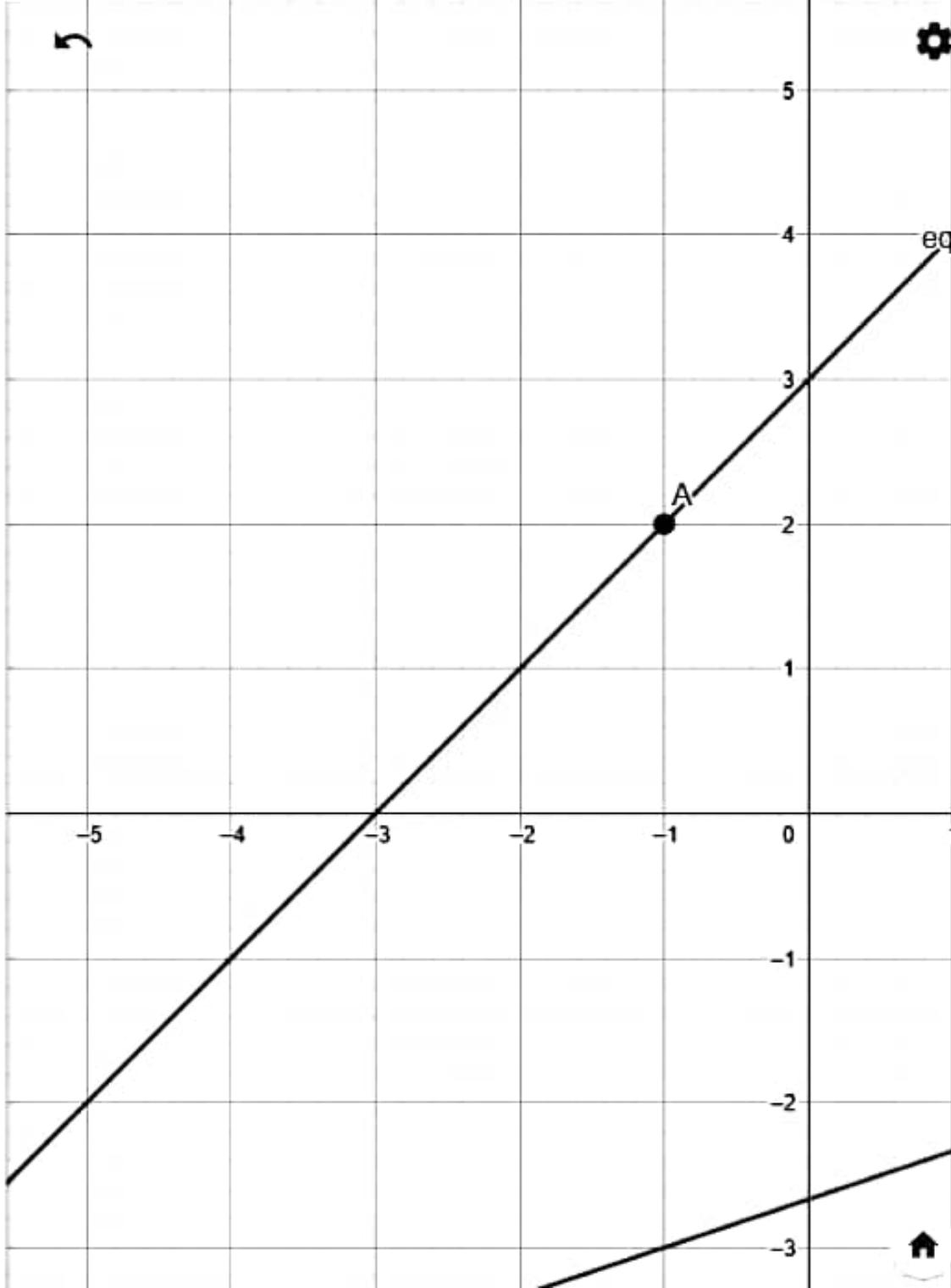
SOL

$$t^2 + 3y^2 - 4yt - st - y = 24$$

eq1: $x^2 + 3y^2 - 4x - 5x - y = 24$:

A = (-1, 2)

+ Input...



(15)

$$T_1 = 20^\circ\text{C}$$

¿Cuánto tiempo tardará la barra los 90°C si se sabe que su T aumenta en 2°C en 1 segundo?

¿Cuánto tiempo tardaría alcanzar 98°C ?

$$\frac{dT}{dt} = K(T - T_m)$$

$$\frac{dT}{T - T_m} = K dt \rightarrow \int \frac{dT}{T - T_m} = \int K dt$$

$$\ln(T - T_m) = kt + C$$

$$T - T_m = e^{kt+C}$$

$$T(t) = C \cdot e^{kt} + T_m$$

$$20 = C + 100$$

$$C = -80$$

$$t=1$$

$$22 = -80e^{k} + 100$$

$$-78 = -80e^k$$

$$\rightarrow k = \ln(78/80)$$

$$① q_0 = -80 e^{\ln\left(\frac{78}{80}\right)t} + 100$$

$$\frac{1}{8} = e^{\ln\left(\frac{78}{80}\right)t}$$

$$\ln\left(\frac{1}{8}\right) = \ln\left(\frac{78}{80}\right)t$$

$$t = 82.13$$

Alcanzara 90°C despues de 82.13 s

$$② \ln\left(\frac{1}{40}\right) = \ln\left(\frac{78}{80}\right)t$$

$$t = 145.70$$

Alcanzara 98°C despues de 145.7 seg

(29) Datos

$$E(t) = 30V$$

$$i(0) = 0$$

$$L = 0.5 \text{ Henrys}$$

$$R = 50 \Omega$$

$$L \frac{di}{dt} + Ri = E(t)$$

$$0.5 \frac{di}{dt} + 50i = 30$$

$$i' + 500i = 300$$

$p(t)$ $f(t)$

$$\rightarrow u(t) = e^{\int 500 dt}$$

$$u(t) = e^{500t}$$

$$i(t) = \frac{1}{u(t)} \int p(t)u(t) dt$$

$$i(t) = \frac{1}{e^{500t}} \int e^{500t} \cdot 300 dt$$

$$i(t) = \frac{1}{e^{500t}} \left(\frac{3e^{500t}}{5} + C \right)$$

$$i(t) = \frac{3}{5} + \frac{C}{e^{500t}}$$

Reemplazando en los valores iniciales

$$0 = \frac{3}{5} + \frac{c}{e^0}$$

$$c = \frac{3}{5}$$

$$\therefore i(t) = \frac{3}{5} + \frac{3}{5 e^{500t}}$$

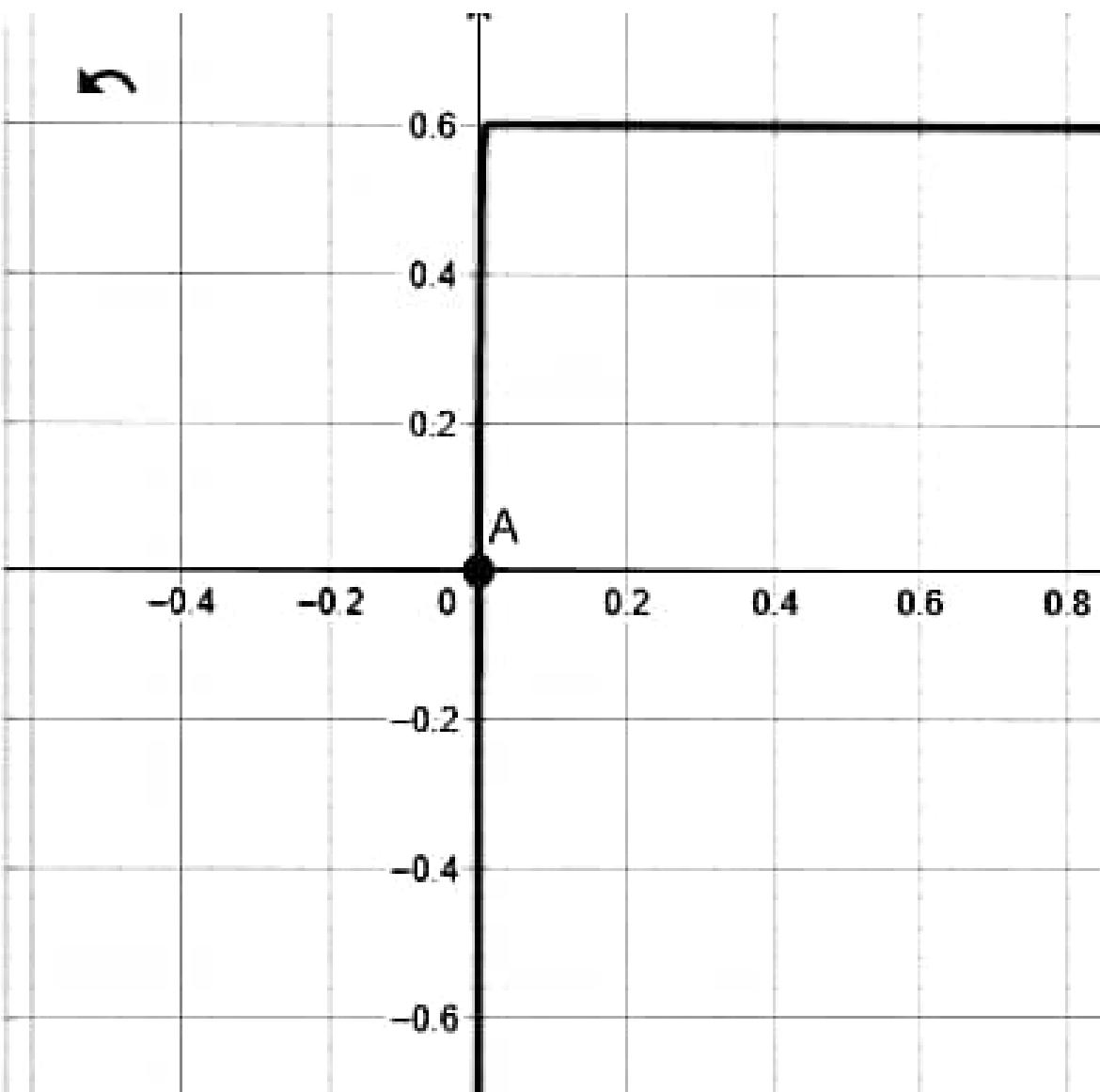
$f(x) = \frac{3}{5} - \frac{3}{5} e^{500x}$

:

$A = (0, 0)$

:

Input...



32) Se aplica una fuerza electromotriz de 100 voltios a un circuito en serie RC en el que la resistencia es de 200 ohms y la capacitancia es de 10^{-4} farads determinar la carga $q(t)$ del capacitor si $q(0)=0$ Encuentre la corriente $i(t)$

$$E(t) = 100 \text{ voltios}$$

$$R = 200 \Omega$$

$$C = 10^{-4} \text{ Farads}$$

$$200 \frac{dq}{dt} + \frac{1}{10^{-4}} q = 100$$

$$\frac{dq}{dt} + 50q = 0.5$$

$\overbrace{p(t)}$ $\overbrace{f(t)}$

$$u(t) = e^{\int p(t) dt}$$

$$u(t) = e^{50t}$$

$$u(t)q = \int u(t)f(t)dt$$

$$e^{50t}q = \int e^{50t}0.5 dt$$

$$e^{50t}q = 0.5 \frac{e^{50t}}{50} + C$$

$$q(t) = \frac{1}{100} + \frac{C}{e^{50t}}$$

~~q(0)~~

Evaluando en la condición inicial

$$0 = \frac{1}{100} + \frac{C}{1} \rightarrow C = -\frac{1}{100} = -0.01$$

$$q(t) = 0.01 - \frac{0.01}{e^{50t}}$$

$$200i + \frac{1}{10^4} q = 100$$

$$200i + \left(0.01 - \frac{0.01}{e^{50t}}\right) \frac{1}{10^4} = 100$$

~~$$200i + 100 - \frac{100}{e^{50t}} = 100$$~~

~~$$i = \frac{1}{e^{50t}}$$~~