

EE210: HW-9 Solution

Date: 06/03/2019

Unless stated otherwise, the BJT in the problems given below has the following characteristics

$I_S = 2.03 \times 10^{-15} \text{ A}$; $\beta_F = 100$; $\beta_R = 1$; $V_A = \infty$; $r_{bb} = 200 \Omega$; $V_T = 26 \text{ mV}$; $C_{je0} = 1 \text{ pF}$; $C_{jco} = 0.5 \text{ pF}$; $C_{jso} = 3 \text{ pF}$; $m = 0.5$; $V_{bi} = 0.85$; $\tau_F = 1 \text{ ns}$ (For simplicity, include r_{bb} only in high frequency analysis and ignore C_{js})

Q.1 Figure.1 shows a common-base amplifier schematic. Determine voltage gain, input and output resistance and upper cutoff frequency for $R_S = 0$. Determine the voltage gain and upper cutoff frequency again for the case where source has a resistance of 1K.

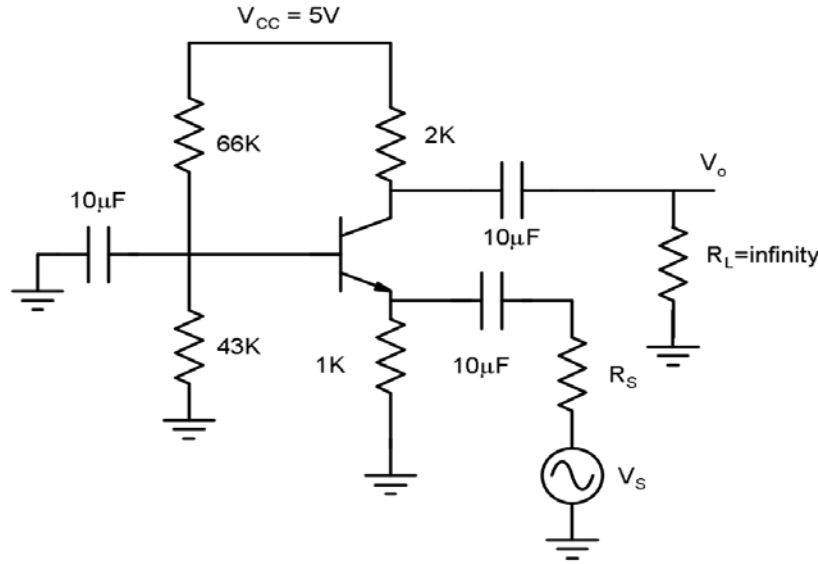


Fig. 1

Sol.

Exact dc analysis (including base current) gives,

$$I_{CQ} = 1 \text{ mA}; V_{CEQ} = 2 \text{ V}$$

Small signal analysis gives

$$g_m = 0.038 \Omega^{-1}; r_\pi = 2.6 \text{ K}\Omega$$

$$A_V = +g_m R_C = 77.0$$

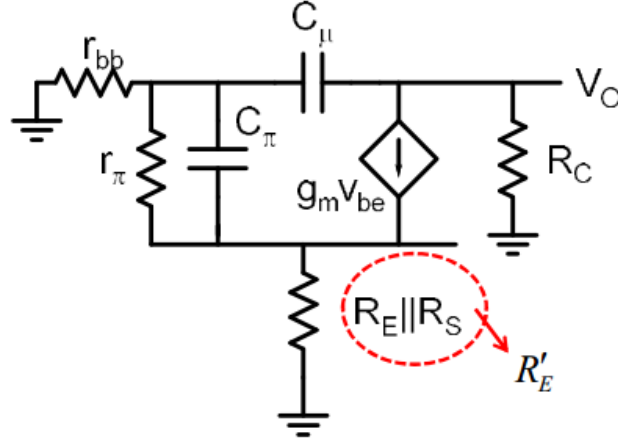
$$R_{in} = \frac{r_\pi}{\beta} \parallel R_E \cong 25 \Omega; R_0 = R_C = 2 \text{ k}\Omega$$

$$f_L \cong \frac{1}{2\pi * 10 * 10^{-6} * R_{in}} = 634 \text{ Hz}$$

$$V_{BC} = V_{BE} - V_{CE} = -1.3 \text{ V}$$

$$C_{jc} = \frac{0.5 \text{ pF}}{\left(1 - \frac{V_{BC}}{0.85}\right)^{1/2}} = 0.32 \text{ pF}; C_{je} = \frac{1 \text{ pF}}{\left(1 - \frac{V_{BE}}{0.85}\right)^{1/2}} = 2.38 \text{ pF}$$

$$C_{\pi} = g_m \tau_F + C_{je} = 41.21 \text{pF}; C_{\mu} = 0.3 \text{pF}$$



$$R_{\pi} = \frac{1 + \frac{R_E \parallel R_S}{r_{bb}}}{1 + \frac{g_m R_E \parallel R_S}{1 + \frac{r_{bb}}{r_{\pi}}}} * (r_{bb} \parallel r_{\pi})$$

It is easier to remember as,

$$R_{\pi} = \left(1 + \frac{R'_E}{r_{bb}}\right) \left(r_{\pi} \parallel \frac{r_{bb}}{1 + g_m R'_E}\right)$$

$$R_{\mu} = r_{bb} + R_C + \frac{(\beta R_C - r_{bb}) * r_{bb}}{r_{\pi} + r_{bb} + (1 + \beta) R_E \parallel R_S}$$

It is easier to remember as,

$$R_{\mu} = r_{bb}(1 - x) + R_C * (1 + x\beta)$$

$$x = \frac{r_{bb}}{r_{bb} + r_{\pi} + \beta R'_E}$$

$$C_{\pi} = g_m \tau_F + C_{je} = 41.21 \text{pF}; C_{\mu} = 0.3 \text{pF}$$

For $R_S = 0$, we get

$$R_{\pi} = 185.6 \Omega; R_{\mu} = 16.6 \text{k}\Omega$$

$$R_{\pi} C_{\pi} = 7.65 \text{ns}; R_{\mu} C_{\mu} = 5.25 \text{ns};$$

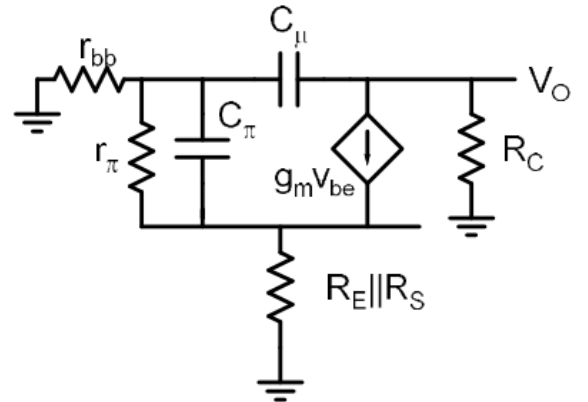
$$f_H \cong \frac{1}{2\pi * (R_{\pi} C_{\pi} + R_{\mu} C_{\mu})} = 12.34 \text{ MHz}$$

For $R_S = 1 \text{k}\Omega$, then $A_v = 1.9$

$$R_{\pi} = 34 \Omega; R_{\mu} = 2.95 \text{k}\Omega$$

$$R_{\pi} C_{\pi} = 1.4 \text{ns}; R_{\mu} C_{\mu} = 0.93 \text{ns}$$

$$f_H \cong \frac{1}{2\pi * (R_{\pi} C_{\pi} + R_{\mu} C_{\mu})} = 68 \text{ MHz}$$



Q.2 Determine gain, input resistance, output resistance, voltage swing with $HD_2 = 10\%$, upper and lower cutoff frequencies for the Cascode amplifier shown in Fig. 2.

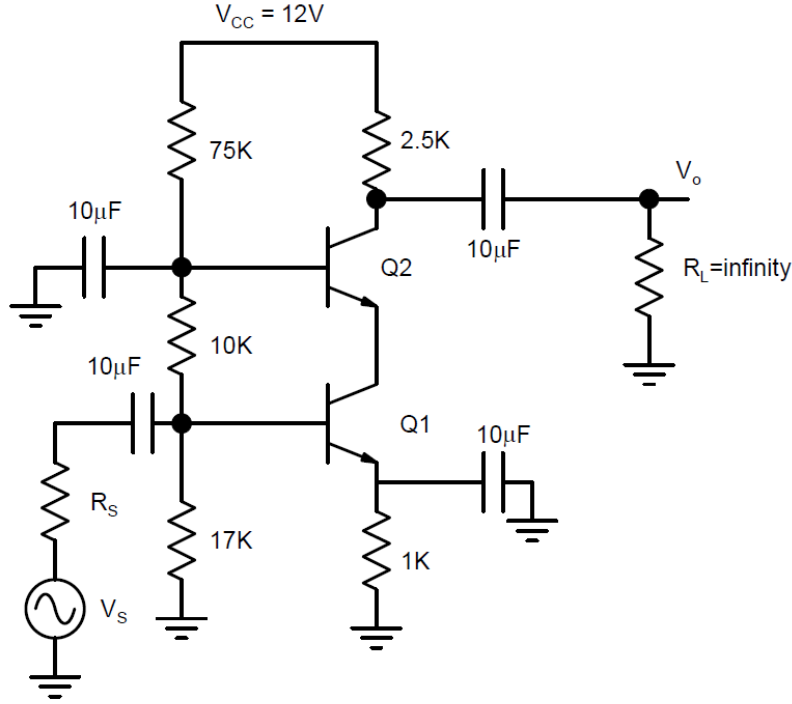


Fig. 2

Sol.

Dc analysis gives

$$I_{CQ} = 1mA; V_{CEQ1} = 1.1V; V_{CEQ2} = 7.3V$$

Small signal analysis gives

$$g_m = 0.038\Omega^{-1}; r_\pi = 2.6k\Omega$$

$$A_V = -g_m R_C = 98.7$$

$$R_{in} = r_\pi \parallel 10k \parallel 17k \cong 1.8k\Omega; R_0 = R_C = 2k\Omega$$

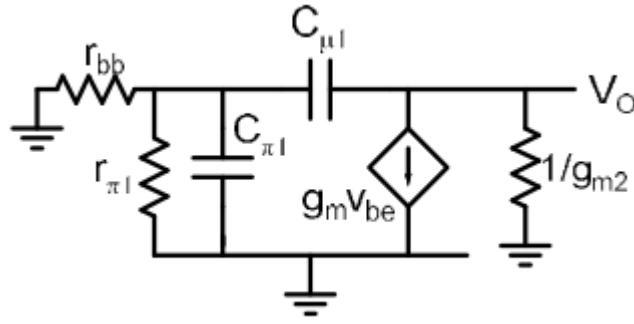
$$f_L \cong \frac{1}{2\pi * 10 * 10^{-6} * \left(\frac{r_\pi}{\beta} \parallel R_E\right)} \cong \frac{1}{2\pi * 10 * 10^{-6} * \left(\frac{r_\pi}{\beta}\right)} = 634Hz$$

$$v_{om} = I_{CQ} R_C * \frac{HD_2}{25} = 1V$$

There are four capacitances, each transistor contributing two,

$$C_{\pi1} = C_{\pi2} = g_m \tau_F + C_{je} = 41.21pF; C_{\mu1} = 0.41pF; C_{\mu2} = 0.17pF$$

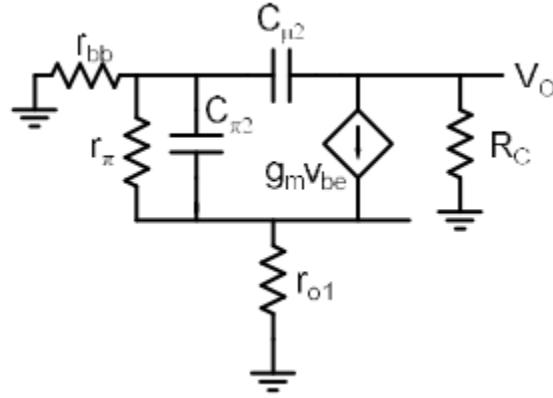
Equivalent circuit for estimating effective resistances seen by capacitances associated with Q1:



$$R_{\pi1} = \left(1 + \frac{0}{r_{bb}}\right) \left(r_{\pi} \parallel \frac{r_{bb}}{1 + 0}\right) = 185.3\Omega$$

$$x_1 = \frac{r_{bb}}{r_{bb} + r_{\pi1} + 0} = 0.073; R_{\mu1} = r_{bb}(1 - x_1) + \frac{1}{g_{m2}} * (1 + x_1\beta) = 0.39K\Omega$$

For CB stage



$$R_{\pi2} = \left(1 + \frac{r_{o1}}{r_{bb}}\right) \left(r_{\pi} \parallel \frac{r_{bb}}{1 + g_{m2}r_{o1}}\right) \cong \frac{1}{g_{m2}} = 25.3\Omega$$

$$x_2 = \frac{r_{bb}}{r_{bb} + r_{\pi1} + \beta r_{o1}} \cong \frac{r_{bb}}{\beta r_{o1}}$$

$$R_{\mu2} = r_{bb}(1 - x_2) + R_C * (1 + x_2\beta) \cong r_{bb} + R_C = 2.7k\Omega$$

$$f_H \cong \frac{1}{2\pi * (R_{\pi1}C_{\pi1} + R_{\pi2}C_{\pi2} + R_{\mu1}C_{\mu1} + R_{\mu2}C_{\mu2})} = 16.87MHz$$

*Note that f_H in Cascode amplifier is dominated by CE stage.

For CE stage only, the upper cutoff frequency comes out to be,

$$f_{H1} \cong \frac{1}{2\pi * (R_{\pi1}C_{\pi1} + R_{\mu1}C_{\mu1})} \cong 20MHz$$

While for CB stage only, the upper cutoff frequency comes out to be,

$$f_{H2} \cong \frac{1}{2\pi * (R_{\pi2}C_{\pi2} + R_{\mu2}C_{\mu2})} \cong 106MHz$$