

Agenda

- ① Query → $(n+1)$ or (n) → Box plot ✓ { by $n-1$ }
- ② Github → Submit the Assignments { Bond's correction }
- ③ Super way of new support (Monday)
- ④ Normal Distribution, Standard Normal Distribution, Z-score

5

Number Summary

50 percentile.

| 18 |

1, 2, 2, [2, 3], 3, 4, 5, 5, 6, 6, 6, [6, 7] 8, 8, 9
 ↓ ↓ ↓ ↓ ↓
 2.5 (25 percentile) 5 6.5 (75 percentile)
 = = =

Median

25 percentile

$$= \frac{25}{100} \times (n+1) = \frac{25}{100} \times 19 \approx 4.75 \Rightarrow \text{Index}$$

lower fence x

$$= \frac{75}{100} \times (19) = \underline{\underline{14.25}} \Rightarrow \text{Index} = \underline{\underline{6.5}}$$

$$= \frac{25}{100} \times (18) \boxed{4.75}$$

20 yrs,

{ No need to apply formula }

$$[2, 3, \boxed{4}, 6, 6, \boxed{6}, \boxed{8}, 9, \boxed{11}, 13, 14] \rightarrow Q3$$

↓ ↓

$25^{\text{th}} \text{ percentile}$ $6 \Rightarrow 50^{\text{th}} \text{ percentile}$

50^{th} percentile

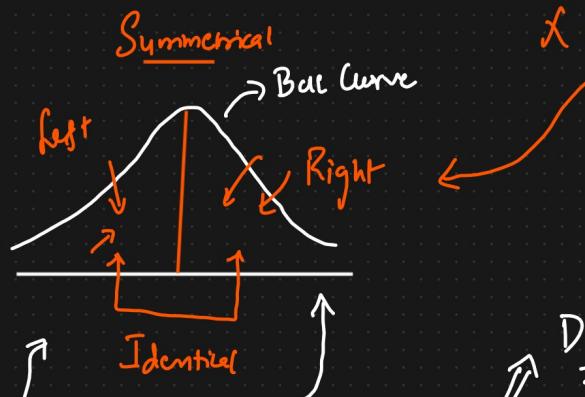
$96^{\text{th}} \text{ percentile}$

99

98.5°

$$\left\{ \frac{99}{100} \times (n_{q1}) \right\}$$

(K) Gaussian or Normal Distribution

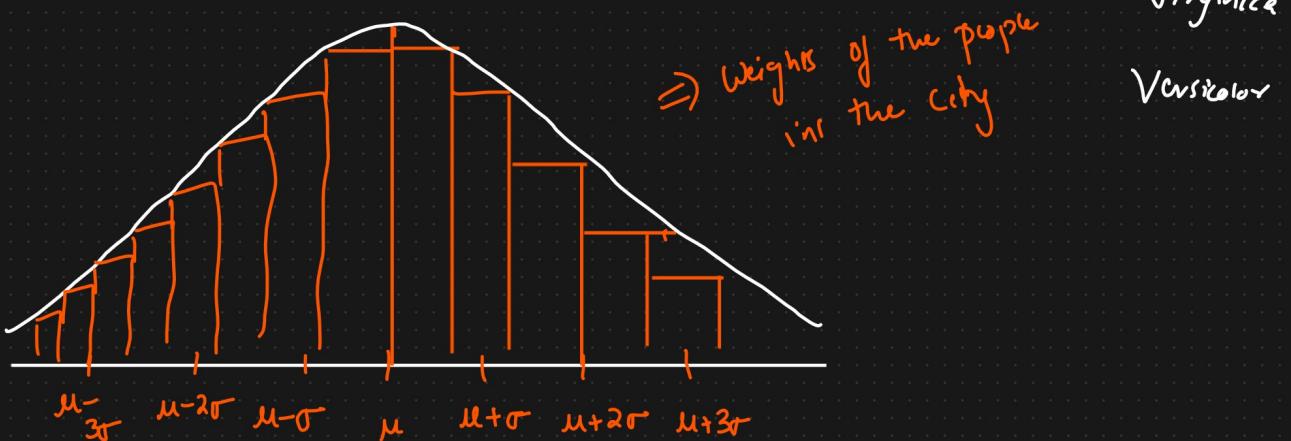


$$x = \{ \quad \}$$

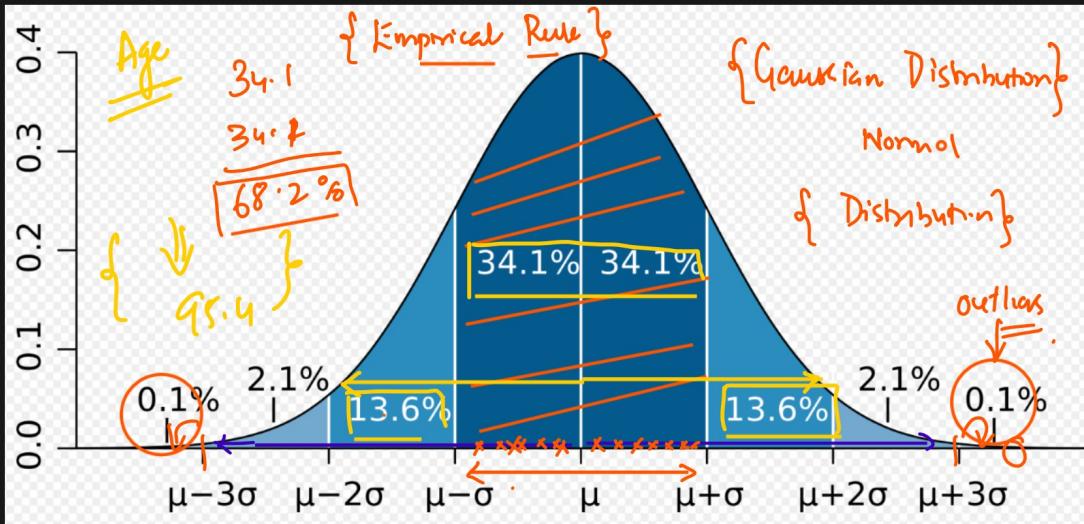
{ IRIS Flower Dataset }

Ex: { Weights of the people in a city? } { Domain Expertise }

Heights of the people in a city?



Virginica
Versicolor



$$X = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\} \rightarrow \text{Gaussian Distribution}$$

1
 168.2
 13.6
 13.6
 $\frac{1}{95.4}$
 2.1
 2.1
 $\frac{1}{99.7}$

68.2% $\frac{100}{68.2} = 168.2\%$

$$\left[68.2 - 95.4 - 99.7 \right] \Rightarrow \text{Empirical Formula}$$

$$\left[68.2, 95.4, 99.7 \right]$$

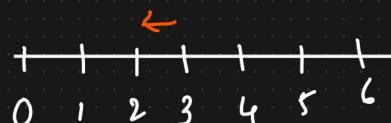
① $\{1, 2, 3, 4, 5\} \Rightarrow \text{Normal Distribution}$

$$\begin{array}{|c|} \hline -1 \\ \hline \end{array} \quad \begin{array}{|c|} \hline 1, 2, 3, 4, 5 \\ \hline \end{array}$$

+1

$$\bar{x} = \frac{1+2+3+4+5}{5} = \underline{\underline{3}}$$

$$\sigma = \sqrt{\frac{1+4+9+16+25}{5}} = \underline{\underline{1.58}}$$



Standard Normal Distribution

$$X = \{1, 2, 3, 4, 5\}$$

$X \approx$ Gaussian Distribution (μ, σ)

$\Downarrow \Downarrow$

$$Y \approx SND \left(\mu=0, \sigma=1 \right) \quad Y = \{ \quad \}$$

$$Z\text{-Score} = \frac{x_i - \mu}{\sigma}$$

$$\Rightarrow \sqrt{n}$$



$$\boxed{\frac{x_i - \mu}{\sigma}}$$

$$\frac{3-3}{1} = \boxed{0}$$

$$\mu = 0 \quad \sigma = 1$$

$$\boxed{n=1}$$

$$\downarrow \quad \{ \boxed{1}, 2, 3, 4, 5 \}$$

$$\mu = 3 \quad \sigma = 1$$

$$\frac{1-3}{1} = \boxed{-2}$$

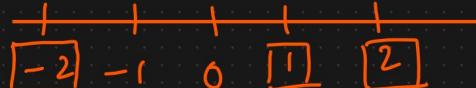
$$\{ \boxed{1}, 2, \boxed{3}, 4, \boxed{5} \}$$

$$\frac{2-3}{1} = \boxed{-1}$$

Z score

$$\{ -2, -1, 0, 1, 2 \}$$

$$\frac{4-3}{1} = 1$$



\bar{x} 10 min break

$$\boxed{n=1}$$

$$X = \{ \boxed{2}, 3, 4, 5, 8 \}$$

$$\Rightarrow Y$$

$$\boxed{\mu=0, \sigma=1}$$

$$\boxed{\mu} = ? \quad \sigma = ? \quad 2.05$$

$$\Downarrow 4.4 =$$

$$Y = \{ -1.17, -0.68, \quad \}$$

Population

$$N = Z\text{-score} = \frac{x_i - \mu}{\sigma}$$

$$\frac{3-4.4}{2.05}$$

$$\frac{2 - 4.4}{2.05} =$$

$$[\mu=0, \sigma=1]$$



Scale down

↓ Same scal.

Why Standard Normal Distribution



Weights

$$\boxed{(Years)} \Leftrightarrow \boxed{(kg)} \Leftrightarrow \boxed{(Km/miles)}$$

Age

Weight

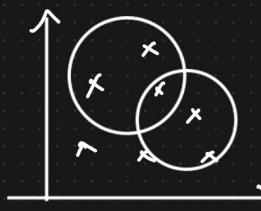
Distance

Same Scale

Age

$$\chi \left\{ \begin{array}{l} 24 \leftrightarrow 100 \\ 26 \leftrightarrow 120 \\ 28 \leftrightarrow 140 \\ 30 \leftrightarrow 160 \end{array} \right\} \bar{x}$$

Standardization



Age

σ

x

x

weight

$$y \left\{ \begin{array}{l} \text{m:0, } \sigma:1 \\ \mathcal{Z}^1 (\mu=0, \sigma=1) \end{array} \right.$$

Feature Scaling =

Z -Score :

$$\boxed{\text{Z-test}}$$

$X \sim \text{Normal Distribution } (\mu, \sigma)$



$y \sim \text{SND } (\mu=0, \sigma=1)$.



{ Standardization }.

$$\boxed{Z\text{-score} = \frac{x_i - \mu}{\sigma}}$$

① Gaussian or Normal Distribution

② Empirical Formula

③ Standard Normal Distribution

↓
Z-score

Quickly
logistic
actions
Manage

95 percentile
99 percentile

of days
to deliver a
panel

Percentiles

Practical

5 days
Average days ∈

$$\frac{95}{100} \times (n+1)$$

95 percentile

↑

95

↑

11

1, 2, 2, 2, 3, 4, 5, 5, 6, 8, 9, 110

15

20

↓

14.25

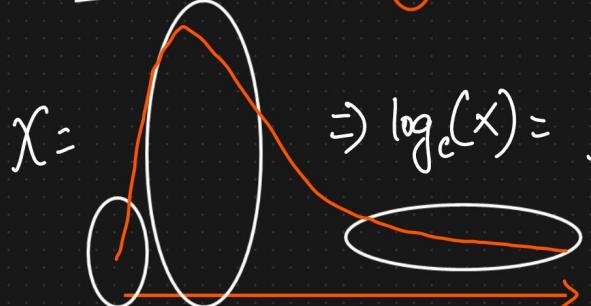
↓

\$ many

Log [Normal Distribution]

A

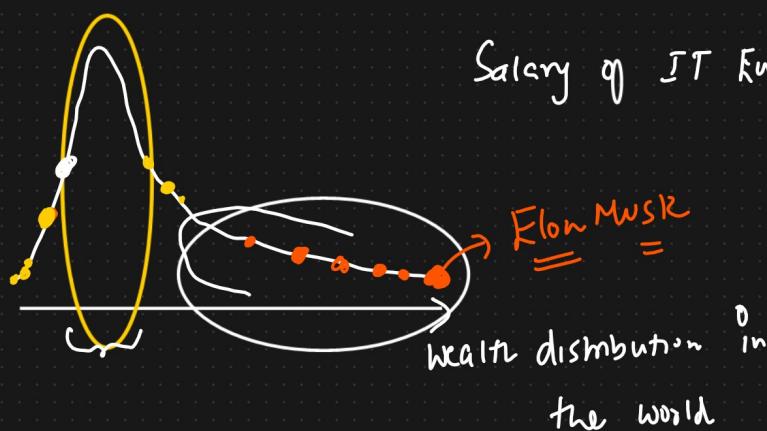
B



length of comments

people writing
in my channel

Salary of IT Employees

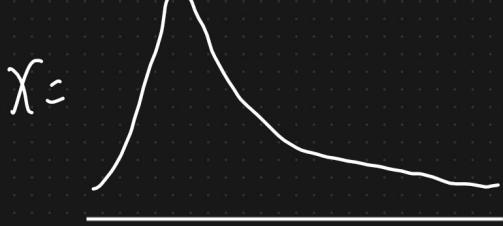


Elon Musk

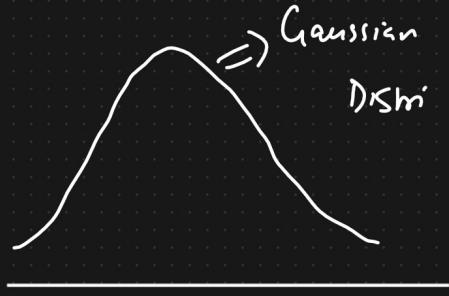
wealth distribution in

the world

Log Normal Distribution



$$X = \Rightarrow \log_e(x) = y$$



$$X = \{ \quad \} \leftarrow e^y \leftarrow$$

Assignment.

Mean, Median, Mode

