

Machine LearningLogistic Regression [classification problem]Example :- IIT / JEE

| study (hour) | playing (hour) | O/p (Pass/Fail) |
|--------------|----------------|-----------------|
| 1 | 8 | fail |
| 2 | 7 | fail |
| 3 | 7 | fail |
| 6 | 3 | Pass |

* No. of study hour increases, chance of Pass will be increase

* There will be some person, who study less but they can also clear Exam, that person consider as outliers.

Ex :- DATASET (UPSC)

| study (hours) | O/p (Pass/Fail) |
|---------------|-----------------|
|---------------|-----------------|

2

FAIL

3

FAIL

4

FAIL

5

FAIL

6

PASS

7

PASS

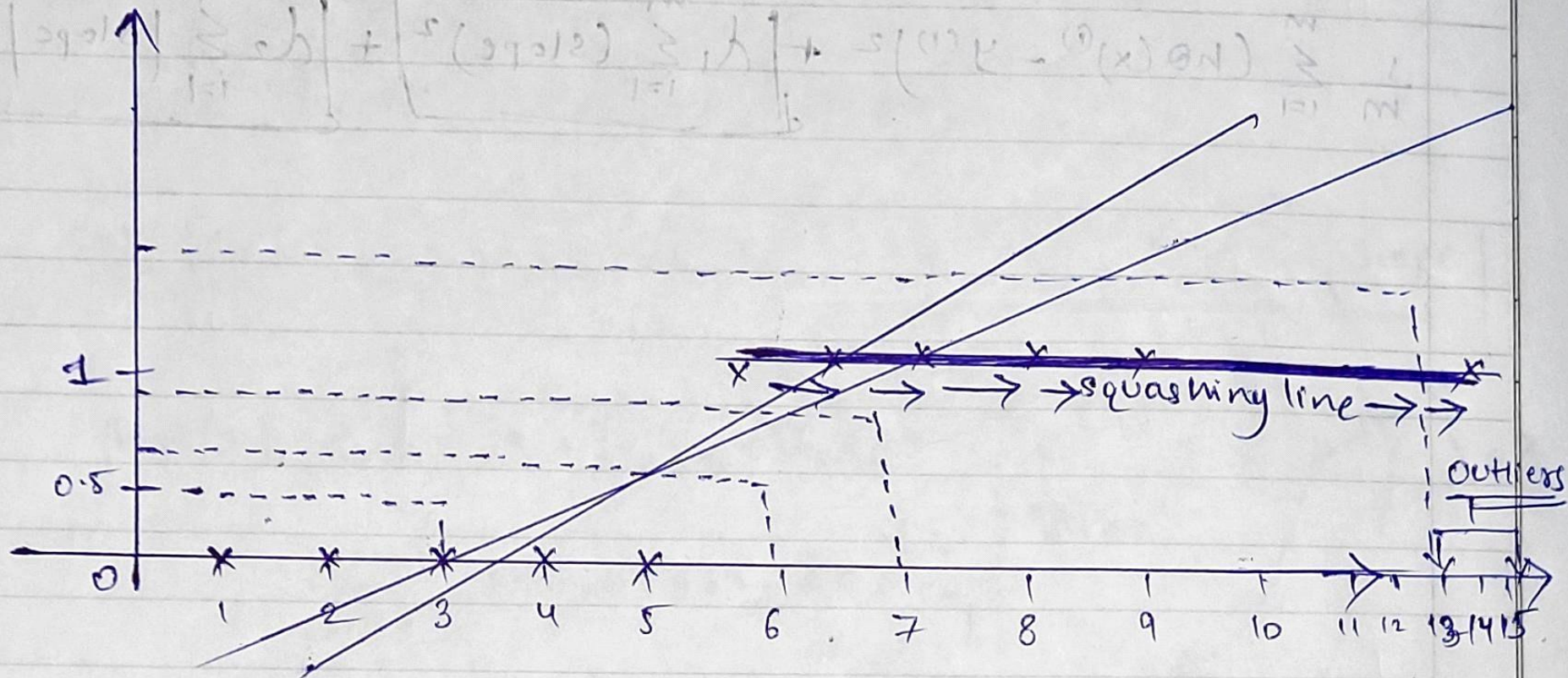
8

PASS

9

PASS

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conditions $\div y \leq 5$ and $y > 0.5$ (if more than one because of outliers than we use squashing line)

\Downarrow \Downarrow
 0 1

why use logistic instead of linear
 \rightarrow outliers causes changes Best fit line and we have only two condition

0 to 1, if go above 1 then we use sigmoid function which squash line.

Function sigmoid Activation

\Downarrow Logistic Regression.

Sigmoid Activation:



$$h\theta(x) = \theta_0 + \theta_1 x \Rightarrow \text{o/p} = [0 \text{ to } 1]$$

(1) $z = h\theta(x) = \theta_0 + \theta_1 x$

Let $\rightarrow z = \theta_0 + \theta_1 x$

(2) Sigmoid function \Rightarrow

$$\frac{1}{1 + e^{-z}}$$

$\Rightarrow 0 \text{ to } 1$

Steps for logistic Regression:

(1) Create a Best fit line.

(2) Squashing \rightarrow Sigmoid Function.

Linear Regression cost fn

$$J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=1}^n (h\theta(x^{(i)}) - y^{(i)})^2$$

$$h\theta(x) = \theta_0 + \theta_1 x$$

* Gradient Descent
* 1 Global Minimal

MSE



convex function

Logistic Regression Cost fn:

$$J(\theta_0, \theta_1) = \frac{1}{n} \sum_{i=1}^n (h\theta(x) - y^{(i)})^2$$

$$h\theta(x) = \text{sig}(\theta_0 + \theta_1 x)$$

$$z = \theta_0 + \theta_1 x$$

Best fit line

$$h\theta(x) = \frac{1}{1 + e^{-(\theta_0 + \theta_1 x)}}$$

$$h\theta(x) = \frac{1}{1 + e^{-z}}$$

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Page No. Expt. No.

$$h(z) = \text{sig}(z)$$

$$h(z) = \frac{1}{1 + e^{-z}}$$

$$z = \theta_0 + \theta_1 x$$

$$h(z) = \frac{1}{1 + e^{-(\theta_0 + \theta_1 x)}} \Rightarrow 0 \text{ to } 1$$



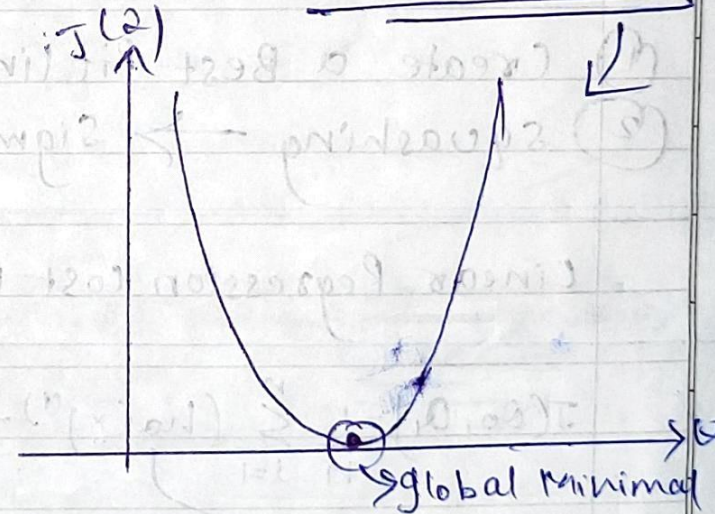
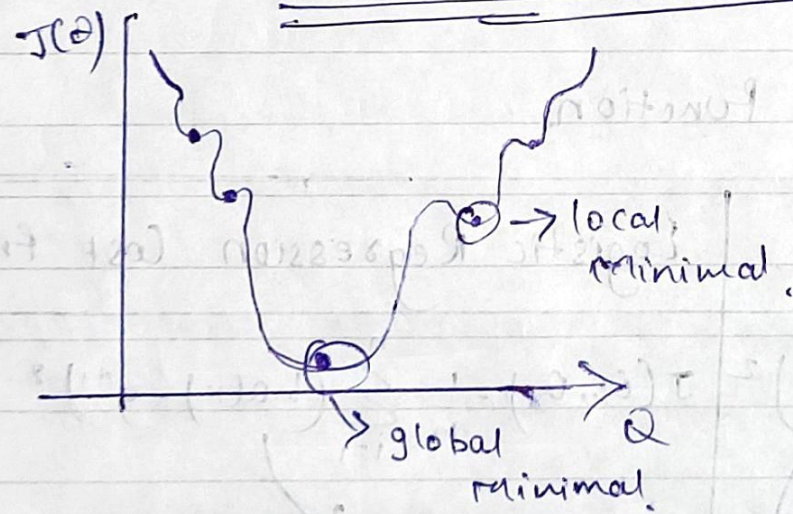
$$\leq 0.5 \Rightarrow 0 \Rightarrow \text{fail}$$

$$> 0.5 \Rightarrow 1 \Rightarrow \text{Pass}$$

Threshold = 0.5

non-convex function

convex function



* Log Loss function:

$$\text{cost}(h\theta(x)^{(i)}, y^{(i)}) = \begin{cases} -\log(h\theta(x)) & \text{if } y=1 \\ -\log(1-h\theta(x)) & \text{if } y=0 \end{cases}$$

convex function



$$\text{cost}(h\theta(x)^{(i)}, y^{(i)}) = -y \log(h\theta(x)) - (1-y) \log(1-h\theta(x))$$

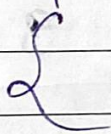


Never local minimal

Minimize cost function $J(\theta_0, \theta_1)$ by changing θ_0, θ_1

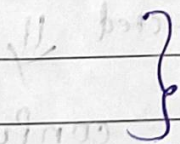
Convergence Algorithm.

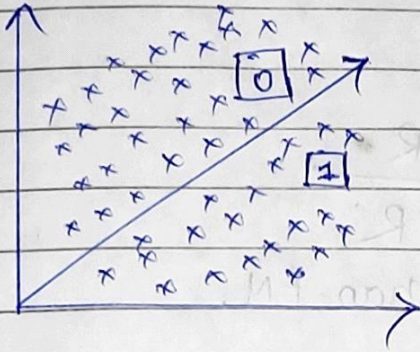
Repeat convergence



$$j=0 \text{ and } 1$$

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$



Performance Matrix:

(1) Confusion Matrix

(2) Accuracy

(3) Precision

(4) Recall

(5) F-Beta Score.

DATASET:

| Feature 1 | Feature 2 | O/P Actual | \hat{y} Predicted |
|-----------|-----------|------------|---------------------|
| - | - | 0 | 1 |
| - | - | 1 | 1 |
| - | - | 0 | 0 |
| - | - | 1 | 1 |
| - | - | 1 | 1 |
| - | - | 0 | 1 |
| - | - | - | - |

| | | | |
|---|----|----|----------|
| | 1 | 0 | y Actual |
| 1 | TP | FP | |
| 0 | FN | TN | |

Predicted

| | | | |
|---|---|---|--------|
| | 1 | 0 | Actual |
| 1 | 3 | 2 | |
| 0 | 1 | 1 | |

Predicted

Confusion Matrix

TP → True Positive

TN → True Negative

FN → False Negative

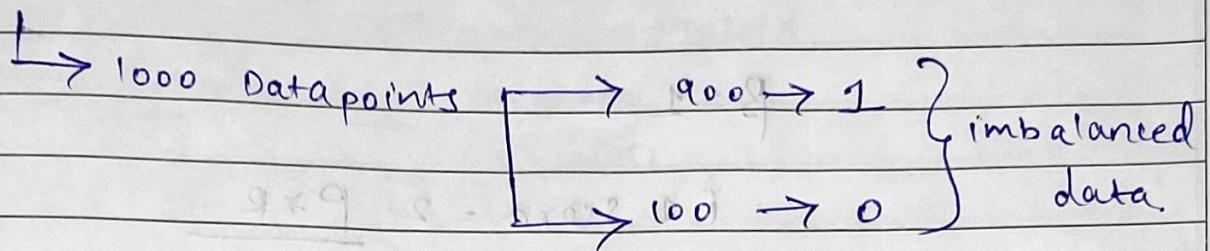
FP → False Positive

$$\text{Accuracy} = \frac{TP + TN}{TP + FP + FN + TN}$$

$$= \frac{3 + 1}{3 + 2 + 1 + 1} = \frac{4}{7} \approx 57\%$$

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* DATASET \rightarrow BINARY CLASSIFICATION



Dumb Model $\rightarrow 1 \Rightarrow 90\%$ Accuracy \rightarrow x-sufficient

* Precision \div

| |
|---------|
| TP |
| TP + FP |

 \Rightarrow out of all the actual values how many are correctly predicted.

| | | |
|---|----|----|
| 1 | TP | FP |
| 0 | FN | TN |

 Actual Predicted

Model \rightarrow Diabetes or not Diabetes.

* Recall \div

| |
|---------|
| TP |
| TP + FN |

 \Rightarrow out of all predicted values how many are correctly predicted

* Tomorrow the stock market is going to crash

| | | |
|---|----|----|
| | 1 | 0 |
| 1 | TP | FP |
| 0 | FN | TN |



\rightarrow consumers \rightarrow FN \downarrow

\rightarrow companies \rightarrow FP \downarrow

F-Beta Score \div $\frac{1 + \beta^2}{\beta^2 * Precision + Recall}$ Precision * Recall

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① If FP and FN are both important

$$\beta = 1$$

$$F1 \text{ Score} = 2 \frac{P * R}{P + R}$$

② If FP is more important than FN.

$$\beta = 0.5$$

$$F_{0.5} \text{ Score} = \frac{(1 + 0.25) P * R}{(0.25) * P + R}$$

③ If $FN \gg FP$

$$F_2 \text{ Score} = \frac{(1 + 4) P * R}{(4 * P + R)}$$

| | Actual 0 | Actual 1 |
|-------------|----------|----------|
| Predicted 0 | TP | FN |
| Predicted 1 | FP | TN |

$TP + FP + FN + TN = N$
 $TP + FN = P$
 $FP + TN = R$
 $TP + FP + FN + TN = P + R$