

### Problem 1 (2 points)

What are the two main types of attributes typically found in data?

### Problem 2 (14 points)

Consider the following data matrix

$$D = \begin{array}{ccccc} & X_1 & X_2 & X_3 & \\ x_1 & 0.3 & 23 & 5.6 & \\ x_2 & 0.4 & 1 & 5.2 & \\ x_3 & 1.8 & 4 & 5.2 & \\ x_4 & 6.0 & 50 & 5.1 & \\ x_5 & -0.5 & 34 & 5.7 & \\ x_6 & 0.4 & 19 & 5.4 & \\ x_7 & 1.1 & 11 & 5.5 & \end{array}$$

1. (2 points) What is the estimated mean of  $X_3$ ?
2. (2 points) What is the estimated covariance between  $X_1$  and  $X_3$ ?
3. (2 points) What is the estimated multi-dimensional mean of  $D$ ?
4. (2 points) What is the estimated variance of  $X_2$ ?
5. (2 points) What is the covariance matrix of  $D$ ?
6. (2 points) What is the estimated correlation between  $X_1$  and  $X_3$ ?
7. (2 points) What is the total variance  $D$ ?

### Problem 3 (6 points)

Given  $a, b \in \mathbb{R}^4$  (that is a fancy way of saying that  $a$  and  $b$  are 4-dimensional vectors with real values) where

$$\begin{array}{lcl} a & = & [2.0 \quad 5.0 \quad -2.6 \quad 6.0] \\ b & = & [15.0 \quad 2.5 \quad 4.0 \quad 4.0] \end{array}$$

1. (2 points) What is  $\|a - b\|_2$ ?
2. (2 points) What is  $\|a - b\|_1$ ?
3. (2 points) What is the cosine of the angle between  $a$  and  $b$ ?

## Problem 4 (3 points)

The following questions reference the Heart Disease data set from the UCI Machine Learning Repository:

`https://archive.ics.uci.edu/ml/datasets/Heart+Disease`

1. (1 point) One attribute is named “cigs”. What information is stored in the “cigs” attribute?
2. (1 point) How many rows (i.e., observations, entities, instances) are there in the data set?
3. (1 point) How many attributes are there in the data set?

## Tips and Acknowledgements

**Acknowledgements:** Homework problems adapted from assignments of Veronika Strnadova-Neeley.