Definition: Point

A **point** is a primitive notion in geometry that represents a location in space with no dimension (no length, width, or height). In Euclidean geometry, points are the fundamental building blocks from which all other geometric objects are constructed.

### Formal Treatment

In different mathematical contexts, points are formalized differently:

- 1. Euclidean Geometry: Points are undefined primitives satisfying Euclid's axioms
- 2. Coordinate Geometry: A point in *n*-dimensional space is represented as an ordered n-tuple  $(x_1, x_2, ..., x_n)$
- 3. Set-Theoretic: In Euclidean Space, a point is simply an element of  $\mathbb{R}^n$

#### Notation

Points are typically denoted by capital letters: A, B, C, P, Q, etc.

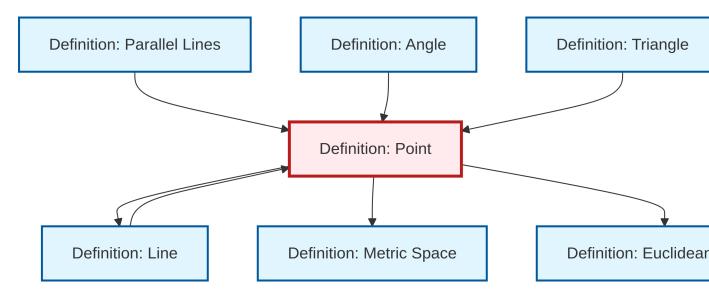
# **Properties**

- Points have position but no size
- Two distinct points determine a unique Line
- Three non-collinear points determine a unique plane

## Examples

- The origin (0,0) in the Cartesian plane
- Any element of a Metric Space
- Vertices of geometric figures like triangles and polygons

# Dependency Graph



Local dependency graph