(3 Hours) **Total Marks: 80**

N.B: 1. Question No. 1 is compulsory
2. Attempt any 3 from remaining questions
3. Assume any suitable data if necessary and justify the assumptions

Q.1 Attempt any **Four**. 20

a) Give difference between random scan display and raster scan display.

b) Define Aliasing, Describe different antialiasing techniques.

c) Compare DDA and BRESENHAM line drawing algorithm.

d) Explain point clipping algorithm.

e) Give fractal dimension for KOCH curve.

Q.2 a) Derive formula for mid-point circle algorithm. 10

b) Given a line AB where A(3,1) and B(0,0) calculate all the points of line AB using 10
DDA algorithm.

Q.3 a) With neat diagram explain Composite transformation. 10

b) Describe what is Homogeneous coordinates. 10

Q.4 a) With neat diagram explain window to viewport coordinate transformation. 10

b) With neat diagram explain Sutherland Hodgman polygon clipping algorithm. 10

Q.5 a) Define projection, with neat diagram describe planar geometric projection. 10

b) Describe properties of BEZIER curve. 10

Q.6 a) Describe various principles of traditional animation. 10

b) Write short note on Depth buffer algorithm. 10

****

11857

(3 hours)   Total Marks: 80

N.B.   1. Question **No. 1** is compulsory
       2. Attempt any **three** questions from remaining five questions
       3. Assume suitable data if **necessary** and justify the assumptions
       4. Figures to the **right** indicate full marks

Q1   A   Convert   05
         i) 123 in to binary
         ii) $(AB9)_{16}$ in to Decimal
         iii) $(351)_8$ in to decimal
         iv) 129 in to BCD
         v) 64 in to gray code

     B   Draw the single and double precision format for representing floating point number   05
Q1   using IEEE 754 standards and explain the various fields
     C   Explain SR Flip Flop   05
     D   Differentiate between Hardwired control unit and Micro programmed control unit   05

Q2   A   Draw the flow chart of Booths algorithm for signed multiplication and Perform   -   10
         5 x 2 using booths algorithm

     B   Explain the different addressing modes.   10

Q3   A   For 132.65 obtain the IEEE 754 standards of Single precision and Double precision   10
         format
     B   Explain Micro instruction format and write a microprogram for the instruction   10
         ADD R_1 , R_2

Q4   A   Consider a 4-way set associative mapped cache with block size 4 KB. The size of the   10
         main memory is 16 GB and there are 10 bits in the tag. Find-
         1. Size of cache memory
         2. Tag directory size

     B   Explain Flynn's classification   10

Q5   A   Explain different types Distributed and Centralized bus arbitration methods   10

     B   Describe the detailed Von-Neumann Model with a neat block diagram   05

     C   Describe the characteristics of Memory.   05

Q6   Write Short notes on   20

         a) Grey code, BCD, Excess-3 Code with example

         b) Encoder and Decoder

         c) Cache coherence

         d) Instruction Pipelining

14070   **1**

(3 Hours) [Total Marks : 80

N.B.
1) **Q.1 is compulsory.**
2) Solve any 3 questions out of remaining 5 questions.
3) Assumptions made should be clearly stated.
4) Draw the figures wherever required.

Q.1 Solve any four of the following questions.

a) Prove using Mathematical Induction that n^3+2n is divisible by 3 for all $n >=1$ **5**

b) Explain the following terms with suitable example: **5**
   i) Partition set
   ii) Power set.

c) State the Pigeonhole principle and show that if any five numbers from 1 to 8 are chosen, then two of them will add to 9. **5**

d) Consider the function $f(x) = 2x-3$. Find a formula for the composition functions **5**
   i) $f^2 = f \circ f$
   ii) $f^3 = f \circ f \circ f$

e) Explain the bipartite graph with suitable example. **5**

Q.2

a) What is a transitive closure? Find the transitive closure of R using Warshall's algorithm where A={1, 2, 3, 4, 5 } & R={$(x,y) \mid$ x-y $= \pm 1$} **10**

b) What is a ring? Let A= {0, 1, 2, 3, 4, 5, 6, 7}. Determine whether a set A with addition modulo 8 & multiplication modulo 8 is a commutative ring? Justify your answer. **10**

Q.3

a) A survey in 1986 asked households whether they had a VCR, a CD player or cable TV. 40 had a VCR. 60 had a CD player; and 50 had cable TV. 25 owned VCR and CD player. 30 owned a CD player and had cable TV. 35 owned a VCR and had cable TV. 10 households had all three. How many households had at least one of the three? How many of them had only CD player? **8**

b) Find the complete solution of a recurrence relation **6**
   $a_n +2a_{n-1} = n+ 3$ for $n \geq 1$ and with $a_0 =3$

c) Obtain CNF & DNF for the following expression: **6**

   $p \longleftrightarrow (\sim p \vee \sim q)$

D048D42621D9225814A5E7ADF6650405

Q.4

a) What is a group? Let A={3, 6 ,9, 12}　　　　　　　　　　　　　　　　**10**
　　i) Prepare the composition table w.r.t. the operation of multiplication modulo 15.
　　ii) Whether it is an abelian group? Justify your answer.
　　iii) Find the inverses of all the elements.
　　iv) Whether it is a cyclic group?

b) What are the isomorphic graphs? Determine whether following graphs are isomorphic.　　**10**
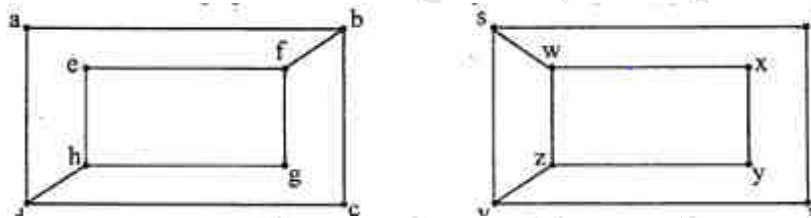
Q.5

a) Let X={1, 2, 3, 6, 24, 36} & R ={(x,y) ∈ R | x divides y}　　　　　　　　**10**
　　i) Write the pairs in a relation set R.
　　ii) Construct the Hasse diagram.
　　iii) What are the Maximal and Minimal elements?
　　iv) Mention Chains and Ant chains from above set.
　　v) Is this poset a lattice?

b) Define the term bijective function.　　　　　　　　　　　　　　　　**5**

Let $f : R \rightarrow (7/5) \rightarrow R - \left(\dfrac{2}{5}\right)$ be defined by $f(x) = \dfrac{2x - 3}{5x - 7}$.

Whether a function is bijective? Justify your answer.

c) Define minimum hamming distance. Consider $e : B^3 \rightarrow B^6$. Find the code words generated by the parity check matrix H given below.　　　　　　　　　　**5**

$$H = \begin{matrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

Q.6

a) Define with example Euler path, Euler circuit, Hamiltonian path, and Hamiltonian circuit. Determine if the following diagram has Euler circuit and Hamiltonian circuit. Mention the path/circuit.　　　　　　　　　　　　　　　　　　　　　　　**6**
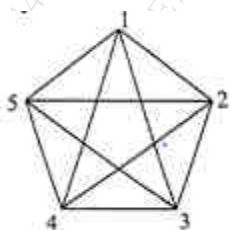
b) Let p denote the statement 'The food is good',
   q denote the statement 'The service is good' &
   r denote the statement 'The rating is 3 star.'
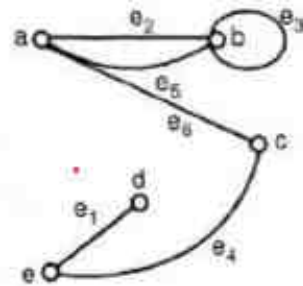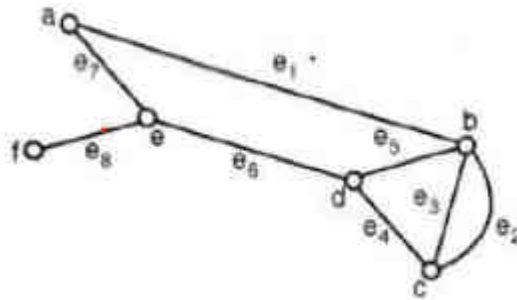   Write the following statements in a symbolic form-   **8**
 i)   Either food is good or service is good or both.
 ii)   The food is good but service is not good.
 iii)   If both food & service are good then the rating is 3 star.
 iv)   It is not true that a 3 star rating always means good food & good service.

c) Find out the incidence matrix of following graphs.   **6**

_____

(3 Hours)   **Total Marks: 80**

N.B: **(1) Question No. 1 is compulsory.**
      (2) Attempt any three questions out of the remaining five questions.
      (3) Figures to the right indicate full marks.
      (4) Make suitable assumptions wherever necessary.

|			
Q.1	(a)	Compare linear and non-linear data structures.	[05]
	(b)	Explain the advantage of circular queue over linear queue. Write a function in C language to insert an element in circular queue.	[05]
	(c)	Define binary search tree. Discuss the case of deletion of a node in binary search tree if node has both the children.	[05]
	(d)	Write a C function to search a node in doubly linked-list.	[05]
Q.2	(a)	Construct AVL tree for the following sequence: 67,34,90,22,45,11,2,78,37,122	[10]
	(b)	Write algorithm for postfix evaluation. Demonstrate the same step by step for the expression: 9 6 7 * 2 / -	[10]
Q.3	(a)	Write a program to perform following operations on a circular linked list: i) insert a node from the end of the list, ii) delete first node, iii) count the number of nodes with even values, iv) display the list.	[10]
	(b)	Write a C program to simulate linear queue as linked list.	[10]
Q.4	(a)	Construct Huffman tree and find the Huffman codes for each symbol given below with frequency of occurrence:	[10]

Symbol	p	g	e	r	i
Frequency	20	17	33	25	40

	(b)	Explain the various ways to represent graph in the memory with example.	[05]
	(c)	Construct binary search tree from given traversal sequences:	[05]

In-order traversal	D	E	B	A	C	F	G	I	H	J
Pre-order traversal	F	E	D	C	B	A	G	H	I	J

Q.5	(a)	Apply linear probing to hash the following values in a hash table of size 11 and find the number of collisions: 67,44,90,12,83,52,23,87,79.	[10]
	(b)	Define topological sorting. Perform topological sorting for the following graph:	[10]
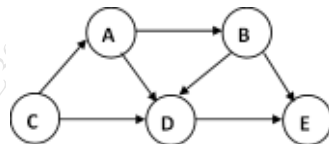
Q.6	(a)	Construct a B tree of order 3 by inserting the following given elements as: 77,97,75,64,53,14,26,49,82,59. Show the B tree at each step of insertion.	[10]
	(b)	Write a function in C for DFS traversal of graph. Explain DFS graph traversal with suitable example.	[10]

_____

00F72FA1FD894CEB50E309551CD4C8E3

(Time: 3 hours)   Max. Marks: 80

N.B. **(1) Question No. 1 is compulsory.**

(2) Answer any three questions from Q.2 to Q.6.

(3) Use of Statistical Tables permitted.

(4) Figures to the right indicate full marks.

Q1 (a)   Find Laplace transform of $\frac{\cos\sqrt{t}}{\sqrt{t}}$ given that $L\{\sin\sqrt{t}\} = \frac{\sqrt{\pi}}{2s^{3/2}} e^{-(1/4s)}$ [5]

(b)   Calculate Spearman's rank correlation coefficient for the following data: [5]

X	32	55	49	60	43	37	43	49	10	20
Y	40	30	70	20	30	50	72	60	45	25

(c)   Find inverse Laplace transform of $\frac{2s-1}{s^2+8s+29}$ [5]

(d)   If $f(z)= qx^2y+2x^2+ry^3-2y^2-i(px^3 -4xy-3xy^2)$ is analytic, find the values of p, q, and r   [5]

Q2 (a)   Find Laplace transform of $e^{3t} f(t)$ where $f(t)=\begin{cases} t-1, & 1 < t < 2 \\ 3-t, & 2 < t < 3 \\ 0, & otherwise \end{cases}$ [6]

(b)   Two unbiased dice are thrown. If X represents sum of the numbers on the two dice.   [6]
Write probability distribution of the random variable X and find mean, standard
deviation , and P(|X-7|≥3)

(c)   Obtain Fourier series for f(x) = x sinx in the interval $0 \le x \le 2\pi$.   [8]

Q3 (a)   Using Milne-Thompson's method construct an analytic function   f(z)= u+ iv in   [6]
terms of z where $u+v = e^x(\cos y+\sin y) + \frac{x-y}{x^2+y^2}$

(b)   Using convolution theorem find the inverse Laplace transform of $\frac{(s+3)^2}{(s^2+6s+5)^2}$ [6]

(c)   Fit a parabola $y= a+bx+cx^2$ to the following data and estimate y when x=10   [8]

x	1	2	3	4	5	6	7	8	9
y	2	6	7	8	10	11	11	10	9

Q4 (a)   Find Laplace transform of $e^{-(1/2)t} t f(3t)$ if $L\{f(t)\} = \frac{1}{s\sqrt{s+1}}$ [6]

11988   **Page 1 of 2**

(b) Find half range sine series for $f(x) = x - x^2$, $0 < x < 1$. [6]

Hence deduce that $\dfrac{1}{1^3} - \dfrac{1}{3^3} + \dfrac{1}{5^3} - \dfrac{1}{7^3} \ldots = \dfrac{\pi^3}{32}$

(c) Given regression lines $6y = 5x + 90$, $15x = 8y + 130$, $\sigma_x{}^2 = 16$. [8]
Find i) $\bar{x}$ and $\bar{y}$, ii) r, iii) $\sigma_y{}^2$ and iv) angle between the regression lines

Q5 (a) Can the function $u = r + \dfrac{a^2}{r}\cos\theta$ be considered as real or imaginary part of an analytic function? If yes, find the corresponding analytic function. [6]

(b) An unbiased coin is tossed three times. If X denotes the absolute difference between the number of heads and the number of tails, find moment generating function of X and hence obtain the first moment about origin and the second moment about mean. [6]

(c) Evaluate $\displaystyle\int_0^\infty e^{-2t} \cosh t \int_0^t u^2 \sinh u \cosh u\, du\ dt$ [8]

Q6 (a) Find inverse Laplace transform of $\dfrac{1}{(s-2)^4(s+3)}$ using method of partial fractions. [6]

(b) If a continuous random variable X has the following probability density function [6]
$$f(x) = \begin{cases} k\,e^{-\frac{x}{4}}, & \text{for } x > 0 \\ 0, & \text{elsewhere} \end{cases} \qquad \text{find } k, \text{ mean and variance.}$$

(c) Find half range cosine series for $f(x) = x$, $0 < x < 2$. [8]

Hence deduce that i) $\dfrac{1}{1^4} + \dfrac{1}{3^4} + \dfrac{1}{5^4} + \dfrac{1}{7^4} + \ldots = \dfrac{\pi^4}{96}$

ii) $\dfrac{1}{1^4} + \dfrac{1}{2^4} + \dfrac{1}{3^4} + \dfrac{1}{4^4} + \ldots = \dfrac{\pi^4}{90}$

****