Years spanning model

$$\frac{1}{|S|} \cdot \sum_{\sigma \in S} \sum_{m \in M} \left[\sum_{y \in Y} (N_{y,m,\sigma} \cdot c_{y,m}) + e_m^H \cdot \left(\sum_{ip \in I^P} [P_{m,ip} \cdot d^P \cdot e_m^H] + min \right) \right] \\ \sum_{m \in I^P} (N_{y,m,\sigma}, P_{m,ip}, p \in \mathbb{Z}^*) \sum_{ir \in I^R} \left[F_{m,ir,\sigma}^U \cdot \frac{H_m}{2} + \left(F_{m,ir,\sigma}^T - F_{m,ir,\sigma}^U \right) \cdot \left(d_{ir}^R + d_{ir}^D \right) + R_{m,ir,\sigma} \cdot d_{ir}^R \right] \right]$$

$$(1)$$

subject to:

$$\sum_{ir \in I^R} d_{y,ir}^R \cdot (F_{m,ir,\sigma}^T + F_{m-1,ir,\sigma}^U - \underbrace{\sum_{ly \in I^R} (P_{m,ir} - \sum_{ip \in I^R} (P_{m,ip} \cdot d_y^P) - \sum_{ly \in I^R} (P_{m,ir,\sigma} \cdot d_y^R) - \underbrace{\sum_{ly \in I^R} (R_{m,ir,\sigma} \cdot d_{y,ir}^R) - \epsilon_{\sigma,m,y}} \forall \sigma \in S, \forall m \in M, \forall y \in Y \quad (2)$$

$$\rho_{\sigma,m,y} - N_{y,m}^{lnst} \le N_{y,m,\sigma} \le A_{y,m} \qquad \forall \sigma \in S, \forall m \in M, \forall y \in Y$$
 (3)

$$R_{m+1,ir,\sigma} \le F_{m,ir,\sigma}^U \le F_{m,ir,\sigma}^T \qquad \forall \sigma \in S, \forall m \in M, \forall ir \in I^R \quad (4)$$

$$\sum_{m'=0}^{m-G^{U}} P_{m',(ip-1)} - \sum_{m'=0}^{m-1} P_{m',ip} \le P_{m,ip} \le \sum_{m'=0}^{m-G^{L}} P_{m',(ip-1)} - \sum_{m'=0}^{m-1} P_{m',ip} \qquad \forall m \in M, \forall ip \in I^{P} \quad (5)$$

Years model Explanation

- (1) The objective takes an average cost of all scenarios by counting up the cost per month. Each month has a cost for vessels chartered (by type), the energy lost due to planned maintenance, and the cost of failures (broken up in missed energy from unrepaired failures, repaired failures, and planned repair tasks that fix older failures)
- (2) For each vessel type the available time (based on charters and spare time from installation) minus the planned time the vessels are used (for planned maintenance and repairs) needs to be greater than the time spend fixing new failures. This LHS will never be negative, which enforces enough vessels are chartered to at least deal with all planned tasks.
- (3) Ensures enough vessels are assigned to a given month (based on feedback from that month), and the amount of vessels chartered doesn't surpass the available vessels
- (4) For any type of reactive task, the amount of tasks performed cannot exceed the amount of unhandled failures of that type from the previous month
- (5) Ensures planned tasks are not scheduled too close together or too far apart by counting up the turbines that were last visited G^U and G^L or more months ago respectively, and subtracting all that were revisited more recently

December 15, 2020

Years model notation overview

Sets:

- S: Scenarios
- M: Months
- Y: Vessel types
- I^P: Indices for the planned tasks (first time a turbine is visited is index 1, second time is index 2, etc...)
- I^R: Types of failures and reactive tasks

Decision variables:

- $N_{y,m,\sigma}$: The amount of vessels of type y chartered in month m in scenario σ
- $lackbox{ }P_{m,ip}$: Planned tasks in iteration $ip\in I^P$ in month m
- $lackbox{ }R_{m,ir,\sigma}\colon \mbox{Reactive tasks of type }ir\in I^R \mbox{ in month }m$ and scenario σ
- $F_{m,ir,\sigma}^U$: Unhandled failures of type $ir \in I^R$ in month m and scenario σ

Parameters:

- c_{y,m}: The cost of chartering a vessel of type y in month m
- e^H_m: The energy produced by a single turbine per hour in month m
- $F_{m,ir,\sigma}^T$: The total amount of failures of type $ir \in I^R$ in month m in scenario σ
- H_m: The number of hours in month m

Parameters (cont):

- ullet $\epsilon_{\sigma,m,y}$: Feedback parameter that enforces leighway in the amount of vessel time available to month m
- $\rho_{\sigma,m,y}$: Feedback parameter that enforces a minimum amount of a certain vessel assigned to month m
- L_y: The amount of hours a vessel of type y is available if chartered for a month
- L^{Inst}_{y,m}: Leftover hours vessels of type y are available in month m based on the installation schedule
- N_{y,m}: Amount of vessels of type y used by the installation schedule in month m that can also partially help out with maintenance operations
- $lack d^P$: The duration that a preventive task will take a turbine offline
- $lack egin{aligned} lack d_y^P \colon & \text{The duration of a preventive task for vessel type} \\ y & y \end{aligned}$
- d^R_{ir}: The duration that reactive task ir will take a turbine offline
- d_{ir}^D: The delay before a failure of type ir is detected and can be worked on
- $lack d_{y,ir}^R$: The duration of a reactive task ir for vessel type y
- G^U & G^L: The Upper and Lower bounds months between two planned maintenance tasks

Months spanning model

$$\min_{\substack{s_i \in \mathbb{R} \geq 0 \\ a_{v,i}^F, a_{v,i}^I, a_{v,i,i'}^I \in \{0,1\}}} \sum_{i \in I} c_i \cdot (s_i + \max_{y \in Y} (s_{y,i} + d_{y,i}))$$
(6)

subject to:

$$\sum_{i \in I} a_{v,i}^F \le 1 \qquad \forall v \in V \tag{7}$$

$$a_{v,i}^{F} + \sum_{i' \in I - \{i\}} a_{v,i',i} = a_{v,i}^{L} + \sum_{i' \in I - \{i\}} a_{v,i,i'} \qquad \forall v \in V, \forall i \in I$$
 (8)

$$\sum_{v \in V_{y}} (a_{v,i}^{F} + \sum_{i' \in I - \{i\}} a_{v,i',i}) \ge \rho_{y,i} \qquad \forall y \in Y, \forall i \in I^{Maint}$$
 (9)

$$s_{i'} + s_{y,i'} - s_i - s_{i,y} \ge (M + d_{y,i}) \cdot a_{v,i,i'} - M \qquad \qquad \forall y \in Y, \forall v \in V_y, \\ \forall i, i' \in I | i \ne i' \qquad (10)$$

$$r_i \le s_i \le T - \max_{y \in Y} (s_{y,i} + d_{y,i}) \qquad \forall i \in I^{Maint}$$
 (11)

$$a_{v,i}^F + \sum_{i' \in I - \{i\}} a_{v,i',i} = a_{v,i}^{Inst} \qquad \forall v \in V, \forall i \in I^{Inst}$$
 (12)

$$s_i = s_i^{lnst} \qquad \forall I \in I^{lnst}$$
 (13)

Months model Explanation

- (6) Objective is to minimise costs of tasks being uncompleted (the +max bit is optional as it's about constants)
- (7) Ensures every vessel has at most one first task
- (8) Ensures that a vessel follows a path without brances
- (9) Ensures every task has enough resourses assigned to it
- (10) Ensures the starting times of consecutive tasks are separated by at least the duration of the first task
- (11) Ensures all tasks are started after their release time, and finished on time
- (12) Forces every installation task to be assigned as in the installation schedule
- (13) Forces every installation task to be started as in the installation schedule

Months model notation overview

Sets:

- Y: Vessel types
- V: Individual vessels
- $V_y \subseteq V$: Vessels of type $y \in Y$
- I^{Inst}: Installation tasks completed this month by vessels that are also available for maintenance tasks
- I^{Maint}: Maintenance tasks to be scheduled this month
- I = I^{Inst} ∪ I^{Maint}: Tasks to be completed in this month

Decision variables:

- s_i : Start time of task i
- \$\mathbb{A}_{v,i}^F\$ & \$\mathbb{A}_{v,i}^L\$: Binary variables, 1 for the first and last task \$i\$ of vessel \$v\$ respectively
- a_{v,i,i'}: Binary variable which is 1 if vessel v performs task i' after task i'

Parameters:

- c_i: The cost per hour of a task not being completed
- s_{y,i}: The start time offset between task i starting and vessel type y being used for it
- d_{y,i}: The duration of task i for vessel type y
- $\rho_{y,i}$: The amount of vessels of type y required for task i
- M: A large number
- r_i: The release time of task i; it cannot be started before this time
- *T*: The end time of the month
- s_i^{Inst} : Start time of task $i \in I^{Inst}$, as in the installation schedule
- $a_{v,i}^{Inst}$: Binary assignment variable of task $i \in I^{Inst}$, as in the installation schedule