Years spanning model

$$\frac{1}{|S|} \cdot \sum_{\sigma \in S} \left(\sum_{m \in M} \left[\sum_{y \in Y} (N_{y,m,\sigma} \cdot c_{y,m}) + \sum_{i \in I^{P}} (P_{m,i} \cdot d^{P} \cdot e_{m}^{H}) + \sum_{i \in I^{R}} \sum_{m'=0}^{m} \left[\sum_{m'=0}^{m} (f_{m',i,\sigma} - R_{m',i,\sigma}) \right] \cdot e_{m}^{H} \cdot H_{m} \right]$$

$$(1)$$

subject to:

$$L_{y} \cdot N_{y,m,\sigma} + L_{y,m}^{Inst} \ge \sum_{i \in I^{P}} (P_{m,i} \cdot d_{y}^{P}) + \sum_{i \in I^{R}} (R_{m,i,\sigma} \cdot d_{y,i}^{R}) \quad \forall \sigma \in S, \forall m \in M, \forall y \in Y$$
 (2)

$$\sum_{m'=0}^{m-1} f_{m',i,\sigma} \ge \sum_{m'=0}^{m} R_{m',i,\sigma} \qquad \forall \sigma \in S, \forall m \in M, \forall i \in I^R$$
 (3)

$$P_{m,i} \le \sum_{m'=0}^{m-G^{NMN}} P_{m',(i-1)} - \sum_{m'=0}^{m-1} P_{m',i} \qquad \forall m \in M, \forall i \in I^P$$
 (4)

$$P_{m,i} \ge \sum_{m'=0}^{m-G^{MAX}} P_{m',(i-1)} - \sum_{m'=0}^{m-1} P_{m',i} \qquad \forall m \in M, \forall i \in I^P$$
 (5)

$$N_{y,m,\sigma} \le A_{y,m} - N_{y,m}^{Inst}$$
 $\forall \sigma \in S, \forall m \in M, \forall y \in Y$ (6)

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Years model Explanation

- (1) The objective takes an average cost of all scenarios by counting up the cost per month. Each month has a cost for vessels chartered (by type), the energy lost due to planned maintenance, and the energy lost due to unrepaired failures
- (2) For each vessel type the available time (based on charters and spare time from installation) needs to surpass the estimated total time all tasks take
- (3) For any type of reactive task, the amount of tasks performed cannot exceed the amount of failures of that type (with a 1 month delay before a failure can be solved)
- (4) Ensures planned tasks are not scheduled too close together by counting up the turbines that were last visited G^{MIN} or more months ago and subtracting all that were revisited later
- (5) Ensures planned tasks are not scheduled too far apart, in similar manner as the previous constraint
- (6) Limits the maximum amount of vessels chartered based on normal availability and vessels used for installation

Years model notation overview

Sets:

- S: Scenarios
- M: Months
- Y: Vessel types
- I^P: Indices for the planned tasks (first time a turbine is visited is index 1, second time is index 2, etc...)
- I^R: Types of failures reactive tasks

Decision variables

- $N_{y,m,\sigma}$: The amount of vessels of type y chartered in month m in scenario σ
- P_{m,i}: Planned ith tasks in month m
- $R_{m,i,\sigma}$: Reactive tasks of type i in month m and scenario σ

Parameters:

- c_{y,m}: The cost of chartering a vessel of type y in month m
- d^P: The duration of a preventive task
- ullet e_m^H : The energy produced by a single turbine per hour in month m
- $f_{m,i,\sigma}$: The amount of failures of type i in month m in scenario σ
- H_m: The number of hours in month m
- L_y: The amount of hours a vessel of type y is available if chartered for a month
- L^{Inst}: Leftover hours vessels of type y are available in month m based on the installation schedule
- $lackbreak d_y^P$: The duration of a preventive task for vessel type
- $lack lack d_{y,i}^R$: The duration of a reactive task i for vessel type y
- G^{MIN} & G^{MAX}: The minimum and maximum amounts of months between two planned maintenance tasks
- A_{y,m}: The number of maximum available vessels of type y in month m
- $N_{y,m}^{lnst}$: Amount of vessels of type y used by the installation schedule in month m

Months spanning model

$$\min_{\substack{s_i \in \mathbb{R}_{\geq 0} \\ a_{v,i,j} \in \{0,1\}}} \sum_{i \in I} c_i \cdot (s_i + \max_{y \in Y} (s_{y,i} + d_{y,i}))$$
(7)

subject to:

$$\sum_{i \in I} a_{v,i,j} \le 1 \qquad \forall v \in V, \forall j \in J \qquad (8)$$

$$\sum_{j \in J} a_{v,i,j} \le 1 \qquad \forall v \in V, \forall i \in I^{Maint} \qquad (9)$$

$$\sum_{i \in I} a_{v,i,j} \le \sum_{i \in I} a_{v,i,(j-1)} \qquad \forall v \in V, \forall j \in J - \{0\}$$
 (10)

$$\rho_{y,i} \le \sum_{v \in V_y} \sum_{j \in J} a_{v,i,j} \qquad \forall y \in Y, \forall i \in I^{Maint}$$
 (11)

$$\frac{M \cdot (a_{v,i,j} + a_{v,i',(j-1)}) +}{d_{y,i'} \cdot a_{v,i',(j-1)} - 2M} \le s_i + s_{y,i} - s_{i'} - s_{i',y} \qquad \forall y \in Y, \forall v \in V_y, \\
\forall i, i' \in I | i \neq i', \forall j \in J - \{0\}$$
(12)

$$s_i + \max_{y \in Y} (s_{y,i} + d_{y,i}) \le T$$
 $\forall i \in I^{Maint}$ (13)

$$\sum_{j \in J} a_{v,i,j} = a_{v,i}^{lnst} \qquad \forall v \in V, \forall I \in I^{lnst}$$
 (14)

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Months model Explanation

- (7) Objective is to minimise costs of tasks being uncompleted (the +max bit is optional as it's about constants)
- (8) Ensures every vessel only does one task at a time
- (9) Ensure every vessel visits each task at most once
- (10) Ensures that if a vessel has an xth task it also has an x 1th task
- (11) Ensures every task has enough resourses assigned to it
- (12) Ensures the starting times of consecutive tasks are separated by at least the duration of the first task (the M factors ensure that if the tasks are not consecutive the starting times don't matter)
- (13) Ensures all tasks are finished on time
- (14) Forces every installation task to be assigned as in the installation schedule
- (15) Forces every installation task to be started as in the installation schedule

Months model notation overview

Sets:

- Y: Vessel types
- V: Individual vessels
- $V_y \subseteq V$: Vessels of type $y \in Y$
- I^{Inst}: Installation tasks completed this month by vessels that are also available for maintenance tasks
- I^{Maint}: Maintenance tasks to be scheduled this month
- I = I^{Inst} ∪ I^{Maint}: Tasks to be completed in this month
- J: Maximum amount of tasks assigned to a single vessel

Decision variables:

- s_i : Start time of task i
- a_{v,i,j}: Binary variable which is 1 if vessel v performs task i as its jth task

Parameters:

- c_i: The cost per hour of a task not being completed
- s_{y,i}: The start time offset between task i starting and vessel type y being used for it
- d_{y,i}: The duration of task i for vessel type y
- ρ_{y,i}: The amount of vessels of type y required for task i
- M: A large number
- T: The end time of the month
- s_i^{Inst} : Start time of task $i \in I^{Inst}$, as in the installation schedule
- a^{Inst}_{V,i}: Binary assignment variable of task
 i ∈ I^{Inst}, as in the installation schedule