# Initial models for optimisation

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## Initial model for installation

$$\max_{\substack{O_p, N_{rp} \in \mathbb{Z}^* \\ s_{ajt} \in \{0,1\}}} \sum_{p \in P} [DIS^p(O_p \cdot v_p - \sum_{r \in R} N_{rp} \cdot C_{rp})] \tag{1}$$

subject to:

$$s_{ait} \le s_{ai(t+1)}$$
  $\forall a \in A, \forall i \in I, \forall t \in T$  (2)

$$s_{ai\sigma_{it_N}} \ge 1 \qquad \forall a \in A, \forall i \in I$$
 (3)

$$s_{ajt} \leq s_{ai\sigma_{it}} \qquad \forall a \in A, \forall (i,j) \in IP, \forall t \in T$$
 (4)

$$N_{rp} \ge \sum_{a \in A} \sum_{i \in I} (\rho_{ir} \cdot (s_{ait} - s_{ai\sigma_{it}})) \qquad \forall r \in R, \forall p \in P, \forall t \in T_p$$
 (5)

$$O_p = \sum_{a \in A} s_{ai_N \sigma_{i_N t_p}} \qquad \forall p \in P$$
 (6)

$$N_{rp} \le m_{rp}$$
  $\forall r \in R, \forall p \in P$  (7)

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# Installation Model Explanation

- (1) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (2) Makes every task that is started stay started
- (3) Forces every task to be starded and finished by the final timestep
- (4) For every precedence relation (i,j), ensures that i is finished before j is started
- (5) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished
- (6) Counts the number of turbines which finished installing by the end of a period
- (7) Sets a limit on the amount of vessels that can be charatered in a given period

## Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale)
   [t<sub>0</sub>,...,t<sub>N</sub>]
- T<sub>p</sub> ⊂ T: All time intervals (small scale) in period p
- R: All resources
- I: All tasks per asset  $[1, ..., i_N]$
- IP: All precedency pairs (i, j)
- A: All assets

## Decision variables:

- O<sub>p</sub>: Number of online turbines after period p
- N<sub>rp</sub>: Number of resources r used in period p
- $s_{ait}$ : Binary variable, 1 if task  $i \in I$  for asset a has started at or before time t

- DIS: The discount factor per period
- v<sub>p</sub>: The value of energy a single turbine produces in period p
- C<sub>rp</sub>: The cost of chartering resource r in period p
- σ<sub>it</sub>: Indicates the timestep at which task i should have been started for it to be finished by timestep t, taking into account the duration and the weather conditions
- $\rho_{ir}$ : The amount of resource r used by task i
- t<sub>p</sub>: The final time interval (from T) before period p
- m<sub>rp</sub>: The maximum amount of resources r that can be charatered in period p

# Initial model for maintenance

$$\max_{\substack{O_t, N_{rp} \in \mathbb{Z}^* \\ s_{ait}, b_{at} \in \{0,1\}}} \sum_{p \in P} [DIS^p (\sum_{t \in \mathcal{T}_p} (O_t \cdot v_t) - \sum_{r \in R} (N_{rp} \cdot C_{rp}))] \tag{8}$$

$$s_{ait} \le s_{ai(t+1)} \qquad \forall a \in A, \forall i \in M, \forall t \in T$$
 (9)

$$s_{ai\sigma_{it_N}} \ge 1$$
  $\forall a \in A, \forall i \in M^M$  (10)

$$N_{rp} \ge \sum_{a \in A} \sum_{i \in M} (\rho_{ir} \cdot (s_{ait} - s_{ai\sigma it})) \qquad \forall r \in R, \forall p \in P, \forall t \in T_p$$
 (11)

$$b_{at} > \sum_{i \in M} [s_{ai\sigma_{i(t-\lambda_a)}} - s_{ai\sigma_{it}}] \qquad \forall a \in A, \forall t \in T$$
 (12)

$$O_t = |A| - \sum_{a \in A} b_{at} \qquad \forall t \in T$$
 (13)

$$N_{rp} \le m_{rp}$$
  $\forall r \in R, \forall p \in P$  (14)

# Maintenance Model Explanation

- (8) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (9) Makes every task that is finished stay finished
- (10) Forces every mandatory maintenance task to be done at some point
- (11) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished
- (12) If no maintenance tasks have finished in the past  $\lambda_a$  timesteps this asset is broken
- (13) The number of active (online) turbines is equal to everything that isn't broken
- (14) Sets a limit on the amount of vessels that can be charatered in a given period

### Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale)
   [t<sub>0</sub>,...,t<sub>N</sub>]
- T<sub>p</sub> ⊂ T: All time intervals (small scale) in period p
- R: All resources
- A: All assets
- $M = M^M \cup M^O$ : All (mandatory and optional) maintenance tasks

### Decision variables:

- O<sub>t</sub>: Number of active turbines at timestep t
- N<sub>rp</sub>: Number of resources r used in period p
- s<sub>ait</sub>: Binary variable, 1 if maintenance task i for asset a has started at or before time t
- b<sub>at</sub>: Binary variable, 1 if asset a is broken at timestep t

- DIS: The discount factor per time period
- v<sub>t</sub>: The value of energy a single turbine produces at timestep t
- C<sub>rp</sub>: The cost of chartering resource r in period p
- λ<sub>a</sub>: The number of timesteps after the last maintenance before asset a fails
- $\sigma_{it}$ : Indicates the timestep at which task i should have been started for it to be finished by timestep t, taking into account the duration and the weather conditions
- ρ<sub>ir</sub>: The amount of resource r used per task for maintenance task i
- m<sub>rp</sub>: The maximum amount of resources r that can be charatered in period p

## Initial 2-mixed model

$$\max_{\substack{N_{rp} \in \mathbb{Z}^* \\ s_{ait}, o_{at} \in \{0,1\}}} \sum_{p \in P} [DIS^{p}(\sum_{t \in T_{p}} \sum_{a \in A} (o_{at} \cdot v_{t}) - \sum_{r \in R} (N_{rp} \cdot C_{rp}))]$$
(15)

$$s_{ait} \le s_{ai(t+1)}$$
  $\forall a \in A, \forall i \in \mathcal{I}, \forall t \in \mathcal{T}$  (16)

$$s_{ai\sigma_{it_N}} \ge 1 \qquad \forall a \in A, \forall i \in I \cup M^M \qquad (17)$$

$$s_{ajt} \le s_{ai\sigma_{it}}$$
  $\forall a \in A, \forall (i,j) \in IP, \forall t \in T$  (18)

$$N_{rp} \ge \sum_{s \in \Delta} \sum_{i \in T} (\rho_{ir} \cdot (s_{ait} - s_{ai\sigma_{it}})) \qquad \forall r \in R, \forall p \in P, \forall t \in T_p$$
 (19)

$$o_{at} \le s_{ai_N \sigma_{i_N t}}$$
  $\forall a \in A, \forall t \in T$  (20)

$$o_{at} \le \sum_{i \in M \cup \{i_M\}} [s_{ai\sigma_{it}} - s_{ai\sigma_{i(t-\lambda_a)}}] \qquad \forall a \in A, \forall t \in T$$
 (21)

$$N_{rp} \le m_{rp}$$
  $\forall r \in R, \forall p \in P$  (22)

# 2-Mixed Model Explanation

- (15) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (16) Makes every task that is started stay started
- (17) Forces every installation and mandatory maintenance task to be starded and finished by the final timestep
- (18) For every precedence relation (i,j), ensures that i is finished before j is started
- (19) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished
- (20) An asset can only be online if it finished installation
- (21) An asset can only be online if it had work done on it recently enough
- (22) Sets a limit on the amount of vessels that can be charatered in a given period

### Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale) [t<sub>0</sub>, . . . , t<sub>N</sub>]
- $\bullet$   $T_p \subset T$ : All time intervals (small scale) in period p
- R: All resources
- I: All installation tasks per asset [1, ..., i<sub>N</sub>]
- $M = M^M \cup M^O$ : all mandatory and optional maintenance tasks
- IP: All precedency pairs (i, j)
- A: All assets

### Decision variables:

- o<sub>at</sub>: Binary variable, 1 if asset a is online at timestep
- N<sub>rp</sub>: Number of resources r used in period p
- s<sub>ait</sub>: Binary variable, 1 if task i ∈ I for asset a has started at or before time t

- DIS: The discount factor per time period
- v<sub>t</sub>: The value of energy a single turbine produces at timestep t
- C<sub>rp</sub>: The cost of chartering resource r in period p
- λ<sub>a</sub>: The number of timesteps after the last maintenance before asset a fails
- \( \sigma\_{it} :\) Indicates the timestep at which task \( i \) should have been started for it to be finished by timestep \( t \), taking into account the duration and the weather conditions
- $\bullet$   $\rho_{ir}$ : The amount of resource r used for task  $i \in \mathcal{I}$
- m<sub>rp</sub>: The maximum amount of resources r that can be charatered in period p

## Initial model for decommission

$$\max_{\substack{N_{rp} \in \mathbb{Z}^* \\ s_{ait} \in \{0,1\}}} \sum_{p \in P} [DIS^p (\sum_{t \in T_p} \sum_{a \in A} ((1 - s_{ai_0t}) \cdot v_t) - \sum_{r \in R} (N_{rp} \cdot C_{rp}))]$$
(23)

$$s_{ait} \le s_{ai(t+1)}$$
  $\forall a \in A, \forall i \in D, \forall t \in T$  (24)

$$s_{ai\sigma_{it_N}} \ge 1$$
  $\forall a \in A, \forall i \in D$  (25)

$$s_{ajt} \le s_{ai\sigma_{it}}$$
  $\forall a \in A, \forall (i,j) \in IP, \forall t \in T$  (26)

$$N_{rp} \ge \sum_{a \in A} \sum_{i \in I} (\rho_{ir} \cdot (s_{ait} - s_{ai\sigma_{it}})) \qquad \forall r \in R, \forall p \in P, \forall t \in T_p$$
 (27)

$$N_{rp} \le m_{rp}$$
  $\forall r \in R, \forall p \in P$  (28)

# Installation Model Explanation

- (23) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (24) Makes every task that is started stay started
- (25) Forces every task to be starded and finished by the final timestep
- (26) For every precedence relation (i,j), ensures that i is finished before j is started
- (27) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished
- (28) Sets a limit on the amount of vessels that can be charatered in a given period

### Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale)
   [t<sub>0</sub>,...,t<sub>N</sub>]
- T<sub>p</sub> ⊂ T: All time intervals (small scale) in period p
- R: All resources
- D: All tasks per asset  $[i_0, \ldots, i_N]$
- IP: All precedency pairs (i, j)
- A: All assets

### Decision variables:

- N<sub>rp</sub>: Number of resources r used in period p
- $s_{ait}$ : Binary variable, 1 if task  $i \in I$  for asset a has started at or before time t

- DIS: The discount factor per period
- v<sub>t</sub>: The value of energy a single turbine produces in timestep t
- C<sub>rp</sub>: The cost of chartering resource r in period p
- σ<sub>it</sub>: Indicates the timestep at which task i should have been started for it to be finished by timestep t, taking into account the duration and the weather conditions
- ρ<sub>ir</sub>: The amount of resource r used by task i
- $t_p$ : The final time interval (from T) before period p
- m<sub>rp</sub>: The maximum amount of resources r that can be charatered in period p

## Initial 3-mixed model

$$\max_{\substack{N_{rp} \in \mathbb{Z}^* \\ s_{ait}, o_{at} \in \{0,1\}}} \sum_{p \in P} [DIS^p (\sum_{t \in \mathcal{T}_p} \sum_{a \in A} (o_{at} \cdot v_t) - \sum_{r \in R} (N_{rp} \cdot C_{rp}))]$$

$$(29)$$

$$s_{ait} \le s_{ai(t+1)}$$
  $\forall a \in A, \forall i \in \mathcal{I}, \forall t \in \mathcal{T}$  (30)

$$s_{ai\sigma_{it_N}} \ge 1$$
  $\forall a \in A, \forall i \in \mathcal{I} - M^O$  (31)

$$s_{ai_0^D t} - 1 \le s_{ai\sigma_{it}} - s_{ait} \qquad \forall a \in A, \forall i \in \mathcal{I} - D, \forall t \in \mathcal{T}$$
 (32)

$$s_{ajt} \le s_{ai\sigma_{jt}}$$
  $\forall a \in A, \forall (i,j) \in IP, \forall t \in T$  (33)

$$m_{rp} \ge N_{rp} \ge \sum \sum (\rho_{ir} \cdot (s_{ait} - s_{ai\sigma_{it}}))$$
  $\forall r \in R, \forall p \in P, \forall t \in T_p$  (34)

$$o_{at} \le s_{ai_N^I \sigma_{i_N^I t}} - s_{ai_0^D t} \qquad \forall a \in A, \forall t \in T$$
 (35)

$$o_{at} \le \sum_{i \in M \cup \{i'_{ai}\}} (s_{ai\sigma_{it}} - s_{ai\sigma_{i(t-\lambda_a)}}) \qquad \forall a \in A, \forall t \in T$$
 (36)

$$o_{at} \le 1 + s_{ai\sigma_{it}} - s_{ait}$$
  $\forall a \in A, \forall i \in M, \forall t \in T$  (37)

# 3-Mixed Model Explanation

- (29) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (30) Makes every task that is started stay started
- (31) Forces every installation and mandatory maintenance task to be started and finished by the final timestep
- (32) Ensures every non-decommission task is inactive during decomission
- (33) For every precedence relation (i, j), ensures that i is finished before j is started
- (34) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished. It also sets a limit on the amount of vessels that can be charatered in a given period
- (35) An asset can only be online if installation is complete and decomission has not started yet
- (36) An asset can only be online if it had maintenance done recently (or only completed installation recently)
- (37) Ensures an asset if offline is maintenance work is going on at this moment

### Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale) [t<sub>0</sub>, . . . , t<sub>N</sub>]
- $T_p \subset T$ : All time intervals (small scale) in period p
- R: All resources
- I: All installation tasks per asset  $[i_0^I, \ldots, i_N^I]$
- $M = M^M \cup M^O$ : all mandatory and optional maintenance tasks
- D: All decomission tasks per asset  $[i_0^D, \ldots, i_N^D]$
- $I = I \cup M \cup D$ : All tasks
- IP: All precedency pairs (i, j). Includes relations stating that the final installation task is finished before maintenance and decomission are started.
- A: All assets

#### Decision variables:

- o<sub>at</sub>: Binary variable, 1 if asset a is online at timestep
- N<sub>rp</sub>: Number of resources r used in period p
- $s_{ait}$ : Binary variable, 1 if task  $i \in \mathcal{I}$  for asset a has started at or before time t

- DIS: The discount factor per time period
- v<sub>t</sub>: The value of energy a single turbine produces at timestep t
- $C_{rp}$ : The cost of chartering resource r in period p
- λ<sub>a</sub>: The number of timesteps after the last maintenance before asset a fails
- σ<sub>it</sub>: Indicates the timestep at which task i should have been started for it to be finished by timestep t, generated duration and the weather conditions
- $lackbox{ } 
  ho_{ir}$ : The amount of resource r used for task  $i\in\mathcal{I}$
- m<sub>rp</sub>: The maximum amount of resources r that can be charatered in period p

## Initial Corrective model

$$\max_{\substack{N_{rp} \in \mathbb{Z}^* \\ s_{ait}, o_{at} \in \{0,1\}}} \sum_{p \in P} [DIS^{p}(\sum_{t \in T_{p}} \sum_{a \in A} (o_{at} \cdot v_{t}) - \sum_{r \in R} (N_{rp} \cdot C_{rp}))]$$
(38)

$$s_{ait} \le s_{ai(t+1)}$$
  $\forall a \in A, \forall i \in \mathcal{I}, \forall t \in T$  (39)

$$s_{ai\sigma_{it_N}} \ge 1$$
  $\forall a \in A, \forall i \in \mathcal{I} - M^C$  (40)

$$s_{ai_0^D t} - 1 \le s_{ai\sigma_{it}} - s_{ait} \qquad \forall a \in A, \forall i \in \mathcal{I} - D, \forall t \in \mathcal{T}$$
 (41)

$$s_{ajt} \le s_{ai\sigma_{it}}$$
  $\forall a \in A, \forall (i,j) \in IP, \forall t \in T$  (42)

$$m_{rp} \ge N_{rp} \ge \sum_{s \in A} \sum_{i \in T} (\rho_{ir} \cdot (s_{ait} - s_{ai\sigma_{it}})) \qquad \forall r \in R, \forall p \in P, \forall t \in T_p$$
 (43)

$$o_{at} \le s_{ai'_N \sigma_{i'_{t,t}}} - s_{ai'_0 t} \qquad \forall a \in A, \forall t \in T$$
 (44)

$$o_{at} \le \sum_{i \in M \cup \{i_M^l\}} (s_{ai\sigma_{it}} - s_{ai\sigma_{i(t-\lambda_{ai})}}) \qquad \forall a \in A, \forall t \in T \qquad (45)$$

$$s_{ait} - s_{ai(t-1)} \le 1 - \sum_{j \in M \cup \{i_N^I\}} \frac{\left(s_{aj\sigma_{jt}} - s_{aj\sigma_{j(t-\lambda_{aj})}}\right)}{L} \qquad \forall a \in A, \forall i \in M^C, \forall t \in T$$
 (46)

$$o_{at} \le 1 + s_{ai\sigma_{it}} - s_{ait}$$
  $\forall a \in A, \forall i \in M, \forall t \in T$  (47)

# Corrective Model Explanation

- (38) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (39) Makes every task that is started stay started
- (40) Forces every installation and preventive maintenance task to be started and finished by the final timestep
- (41) Ensures every non-decommission task is inactive during decomission
- (42) For every precedence relation (i, j), ensures that i is finished before j is started
- (43) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished. It also sets a limit on the amount of vessels that can be charactered in a given period
- (44) An asset can only be online if installation is complete, and decomission has not started yet
- (45) An asset is offline if it has not gotten maintained recently enough
- (46) A corrective maintenance task can only be started if the asset is in a failure state (division by L means any number of tasks can have been recent enough for their time to matter)
- (47) Ensures an asset if offline is maintenance work is going on at this moment

### Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale) [t<sub>0</sub>, . . . , t<sub>N</sub>]
- T<sub>p</sub> ⊂ T: All time intervals (small scale) in period p
- R: All resources
- I: All installation tasks per asset  $[i_0^I, \ldots, i_N^I]$
- $M = M^P \cup M^C$ : all preventive and corrective maintenance tasks
- D: All decomission tasks per asset  $[i_0^D, \ldots, i_N^D]$
- $I = I \cup M \cup D$ : All tasks
- IP: All precedency pairs (i, j). Includes relations stating that the final installation task is finished before maintenance and decomission are started.
- A: All assets

#### Decision variables:

- $lack o_{at}$ : Binary variable, 1 if asset a is online at timestep t
- N<sub>rp</sub>: Number of resources r used in period p
- $s_{ait}$ : Binary variable, 1 if task  $i \in \mathcal{I}$  for asset a has started at or before time t

#### Deterministic parameters:

- DIS: The discount factor per time period
- C<sub>rp</sub>: The cost of chartering resource r in period p
- lacksquare  $ho_{ir}$ : The amount of resource r used for task  $i\in\mathcal{I}$
- m<sub>rp</sub>: The maximum amount of resources r that can be charatered in period p
- L: A large number (at least |M| + 1)

#### Stochastic parameters:

- v<sub>t</sub>: The value of energy a single turbine produces at timestep t
- λ<sub>ai</sub>: The number of timesteps after the last maintenance before asset a fails
- \( \sigma\_{it}:\) Indicates the timestep at which task \( i \) should have been started for it to be finished by timestep \( t \), generated based on duration and the weather conditions (stochastic based on those)

## Initial Stochastic model

$$\max_{\substack{N_{rp} \in \mathbb{Z}^* \\ s_{ait}, o_{at\sigma} \in \{0,1\}}} \sum_{\sigma \in S} \sum_{p \in P} [DIS^p (\sum_{t \in T_p} \sum_{a \in A} (o_{at\sigma} \cdot v_{t\sigma}) - \sum_{r \in R} (N_{rp} \cdot C_{rp}))]$$
(48)

$$s_{ait} \le s_{ai(t+1)}$$
  $\forall a \in A, \forall i \in M, \forall t \in T$  (49)

$$s_{ai\omega_{it_N}} \ge 1$$
  $\forall a \in A, \forall i \in M^P$  (50)

$$m_{rp} \ge N_{rp} \ge \sum_{a \in A} \sum_{i \in T} (\rho_{ir} \cdot (s_{ait} - s_{ai\omega_{it}})) \qquad \forall r \in R, \forall p \in P, \forall t \in T_p \quad (51)$$

$$o_{at\sigma} \le \sum_{i \in M} (s_{ai\omega_{it}} - s_{ai\omega_{i(t-\lambda_{ai\sigma})}}) \qquad \forall a \in A, \forall t \in T, \forall \sigma \in S$$
 (52)

$$s_{ait} - s_{ai(t-1)} \le 1 - \sum_{j \in M} \frac{(s_{aj\omega_{jt}} - s_{aj\omega_{j(t-\lambda_{aj\sigma})}})}{L} \qquad \forall a \in A, \forall i \in M^C, \forall t \in T, \forall \sigma \in S$$
 (53)

$$o_{at\sigma} \le 1 + s_{ai\omega_{it}} - s_{ait}$$
  $\forall a \in A, \forall i \in M, \forall t \in T, \forall \sigma \in S$  (54)

# Stochastic Model Explanation

- (48) Objective function, sums up profits from energy made, subtracts money used on resources (vessels), and multiplies it all with a discount factor
- (49) Makes every task that is started stay started
- (50) Forces every installation and preventive maintenance task to be started and finished by the final timestep
- (51) Counts up the resources needed in a time period by adding the resources needed by all tasks started, and subtracting the resources needed by all tasks finished. It also sets a limit on the amount of vessels that can be charatered in a given period
- (52) An asset is offline if it has not gotten maintained recently enough
- (53) A corrective maintenance task can only be started if the asset is in a failure state (division by L means any number of tasks can have been recent enough for their time to matter)
- (54) Ensures an asset if offline is maintenance work is going on at this moment

#### Sets:

- P: All time periods (large scale)
- T: All time intervals (small scale) [t<sub>0</sub>, ..., t<sub>N</sub>]
- $T_p \subset T$ : All time intervals (small scale) in period p
- R: All resources
- $M = M^P \cup M^C$ : all preventive and corrective maintenance tasks
- A: All assets
- S: All scenarios

#### Decision variables:

- $o_{at\sigma}$ : Binary variable, 1 if asset  $a \in A$  is online at timestep  $t \in T$  in scenario  $\sigma \in S$
- $N_{rp}$ : Number of resources  $r \in R$  used in period  $p \in P$
- s<sub>ait</sub>: Binary variable, 1 if task i ∈ M for asset a ∈ A has started at or before time t ∈ T

#### Deterministic parameters:

- DIS: The discount factor per time period
- C<sub>rp</sub>: The cost of chartering resource r ∈ R in period p ∈ P
- $m_{rp}$ : The maximum amount of resources  $r \in R$  that can be charatered in period  $p \in P$
- L: A large number (at least |M| + 1)

#### Stochastic parameters:

- $v_{t\sigma}$ : The value of energy a single turbine produces at timestep  $t \in T$  in scenario  $\sigma \in S$
- $\lambda_{ai\sigma}$ : The number of timesteps after the completion of  $i \in M$  until asset  $a \in A$  fails in scenario  $\sigma \in S$
- $\omega_{it}$ : Indicates the timestep at which task  $i \in M$  should have been started for it to be finished by timestep  $t \in T$ , generated based on duration and the weather conditions (stochastic based on those)

## Initial Multilevel model

$$\min_{N_{vm\sigma},P_m,R_{m\sigma}\in\mathbb{Z}^*} \frac{1}{|S|} \cdot \sum_{\sigma\in S} \sum_{m\in M} \left[ \sum_{v\in V} (N_{vm\sigma} \cdot C_{vm}) + P_m \cdot d_P \cdot e_m^h + \sum_{m'=0}^m (f_{m'\sigma} - R_{m'\sigma}) \cdot e_m^m \right]$$
(55)

$$I_{v} \cdot N_{vm\sigma} \ge P_{m} \cdot d_{v}^{P} + R_{m\sigma} \cdot d_{v}^{R} \qquad \forall \sigma \in S, \forall m \in M, \forall v \in V$$
 (56)

$$\sum_{m'=0}^{m-1} f_{m'\sigma} \ge \sum_{m'=0}^{m} R_{m'\sigma} \qquad \forall \sigma \in S, \forall m \in M$$
 (57)

$$\sum_{m\in M} P_m \ge A \tag{58}$$

# Multilevel Model Explanation

(55) hi