From Policy Gradient to Actor-Critic methods

TRPO and ACKTR

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Outline

- Start from algorithms close to PG: TRPO and ACKTR
- Three aspects distinguish TRPO:
  - Surrogate return objective
  - Natural policy gradient
  - Conjugate gradient approach
- Differences in ACKTR:
  - Approximate second order gradient descent (Hessian)
  - Using Kronecker Factored Approximated Curvature

Surrogate return objective

- The standard policy gradient algorithm for stochastic policies is:

$$\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}) = \mathbb{E}_t[\nabla_{\boldsymbol{\theta}} \log \pi_{\boldsymbol{\theta}}(\mathbf{a}_t|\mathbf{s}_t) \hat{A}^{\pi_{\boldsymbol{\theta}}}_{\boldsymbol{\phi}}]$$

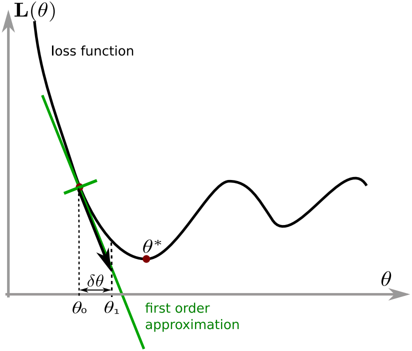
- This gradient is obtained from differentiating $Loss^{PG}(\boldsymbol{\theta}) = \mathbb{E}_t[\log \pi_{\boldsymbol{\theta}}(\mathbf{a}_t|\mathbf{s}_t) \hat{A}^{\pi_{\boldsymbol{\theta}}}_{\boldsymbol{\phi}}]$
- But we obtain the same gradient from differentiating

$$Loss^{IS}(\boldsymbol{\theta}) = \mathbb{E}_t[\frac{\pi_{\boldsymbol{\theta}}(\mathbf{a}_t|\mathbf{s}_t)}{\pi_{\boldsymbol{\theta}old}(\mathbf{a}_t|\mathbf{s}_t)} \hat{A}^{\pi_{\boldsymbol{\theta}}}_{\boldsymbol{\phi}}]$$

  where $\pi_{\boldsymbol{\theta}old}$ is the policy at the previous iteration
- Because $\nabla_{\boldsymbol{\theta}} \log f(\boldsymbol{\theta})|_{\boldsymbol{\theta}old} = \frac{\nabla_{\boldsymbol{\theta}} f(\boldsymbol{\theta})|_{\boldsymbol{\theta}old}}{f(\boldsymbol{\theta}old)} = \nabla_{\boldsymbol{\theta}}(\frac{f(\boldsymbol{\theta})}{f(\boldsymbol{\theta}old)})|_{\boldsymbol{\theta}old}$

- Another view based on importance sampling
- See John Schulmann's Deep RL bootcamp lecture #5
  https://www.youtube.com/watch?v=SQtOI9jsrJ0 (8')

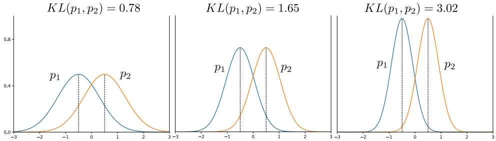
Trust region



- The gradient of a function is only accurate close to the point where it is calculated
- $\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta})$ is only accurate close to the current policy $\pi_{\boldsymbol{\theta}}$
- Thus, when updating, $\pi_{\boldsymbol{\theta}}$ must not move too far away from a "trust region" around $\pi_{\boldsymbol{\theta}old}$

Kakade, S. & Langford, J. (2002) Approximately optimal approximate reinforcement learning. In *ICML*, volume 2, pages 267–274

Natural Policy Gradient



- One way to constrain two stochastic policies to stay close is constraining their KL divergence
- The KL divergence is smaller when the variance is larger
- Under fixed KL constraint, it is easier to move the mean further away when the variance is large
- Thus the mean policy converges first, then the variance is reduced
- Ensures a large enough amount of exploration noise
- Other properties presented in the Pierrot et al. (2018) paper

Sham M. Kakade. A natural policy gradient. In *Advances in neural information processing systems*, pp. 1531–1538, 2002

Pierrot, T., Perrin, N., & Sigaud, O. (2018) First-order and second-order variants of the gradient descent: a unified framework. *arXiv preprint arXiv:1810.08102*

Trust Region Policy Optimization

- Theory: monotonous improvement towards the optimal policy (Assumptions do not hold in practice)
- To ensure small steps, TRPO uses a natural gradient update instead of standard gradient
- Minimize Kullback-Leibler divergence to previous policy
- $$\max_{\boldsymbol{\theta}} \mathbb{E}_t\left[\frac{\pi_{\boldsymbol{\theta}}(\mathbf{a}_t|\mathbf{s}_t)}{\pi_{\boldsymbol{\theta}old}(\mathbf{a}_t|\mathbf{s}_t)} A_{\boldsymbol{\phi}}^{\pi_{\boldsymbol{\theta}old}}(\mathbf{s}_t, \mathbf{a}_t)\right]$$
  $$\text{subject to } \mathbb{E}_t[KL(\pi_{\boldsymbol{\theta}old}(.|\mathbf{s})||\pi_{\boldsymbol{\theta}}(\mathbf{a}_t|\mathbf{s}_t))] \leq \delta$$
- In TRPO, optimization performed using a conjugate gradient method to avoid approximating the Fisher Information matrix

Schulman, J., Levine, S., Moritz, P., Jordan, M. I., & Abbeel, P. (2015) Trust Region Policy Optimization. *CoRR, abs/1502.05477*

Advantage estimation

- To get $\hat{A}_{\boldsymbol{\phi}}^{\pi_{\boldsymbol{\theta}}}$, an empirical estimate of $V^{\pi_{\boldsymbol{\theta}}}(s)$ is needed
- TRPO uses a MC estimate approach through regression, but constrains it (as for the policy):

$$\min_{\boldsymbol{\phi}} \sum_{n=0}^{N} ||V_{\boldsymbol{\phi}}^{\pi_{\boldsymbol{\theta}}}(s_n) - V^{\pi_{\boldsymbol{\theta}}}(s_n)||^2$$

$$\text{subject to } \frac{1}{N} \sum_{n=0}^{N} \frac{||V_{\boldsymbol{\phi}}^{\pi_{\boldsymbol{\theta}}}(s_n) - V_{\boldsymbol{\phi}_{old}}^{\pi_{\boldsymbol{\theta}}}(s_n)||^2}{2\sigma^2} \leq \epsilon$$

- Equivalent to a mean KL divergence constraint between $V_{\boldsymbol{\phi}}^{\pi_{\boldsymbol{\theta}}}$ and $V_{\boldsymbol{\phi}_{old}}^{\pi_{\boldsymbol{\theta}}}$

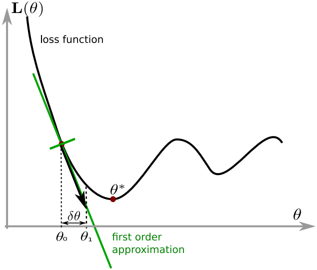
Properties

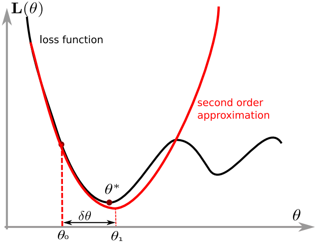
- Moves slowly away from current policy
- Key: use of line search to deal with the gradient step size
- More stable than DDPG, performs well in practice, but less sample efficient
- Conjugate gradient approach not provided in standard tensor gradient librairies, thus not much used
- Greater impact of PPO
- Related work: NAC, REPS

Jan Peters and Stefan Schaal. Natural actor-critic. *Neurocomputing*, 71 (7-9):1180–1190, 2008

Jan Peters, Katharina Mülling, and Yasemin Altun. Relative entropy policy search. In *AAAI*, pp. 1607–1612. Atlanta, 2010

First order versus second order derivative





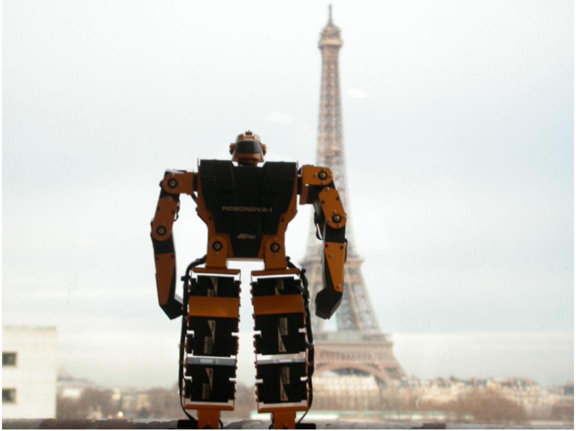
- In first order methods, need to define a step size
- Second order methods provide a more accurate approximation
- They also provide a true minimum, when the Hessian matrix is symmetric positive-definite matrix (SPD)
- In both cases, the derivative is very local
- The trust region constraint applies too

ACKTR

- K-FAC: Kronecker Factored Approximated Curvature: efficient estimate of the gradient
- Using block diagonal estimations of the Hessian matrix, to do better than first order
- ACKTR: TRPO with K-FAC natural gradient calculation
- But closer to actor-critic updates (see PPO)
- The per-update cost of ACKTR is only 10% to 25% higher than SGD
- Improves sample efficiency
- Not much excitement: less robust gradient approximation?
- Next lesson: PPO

Yuhuai Wu, Elman Mansimov, Shun Liao, Roger Grosse, and Jimmy Ba (2017) Scalable trust-region method for deep reinforcement learning using Kronecker-factored approximation. *arXiv preprint arXiv:1708.05144*

Any question?



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