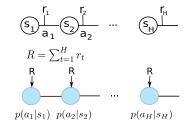
# From Policy Gradient to Actor-Critic methods Policy Gradient and Reward Weighted Regression

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#### Reminder: the most basic PG algorithm



- ► Sample a set of trajectories from  $\pi_{\theta}$
- ► Compute:

$$Loss(\boldsymbol{\theta}) = \frac{1}{m} \sum_{i=1}^{m} \sum_{t=1}^{H} \log \pi_{\boldsymbol{\theta}}(\mathbf{a}_{t}^{(i)}|\mathbf{s}_{t}^{(i)}) R(\tau^{(i)})$$
(1)

- Minimize the loss
- Iterate: sample again



#### Behavioral cloning

- Assume we have a set of expert trajectories,
- $\blacktriangleright$  Data is a list of pairs  $(\mathbf{s}_t^{(i)}, \mathbf{a}_t^{(i)}), t$  is time, H is horizon, i is the trajectory index
- If the trajectories are optimal, a good option is behavioral cloning
- Use regression to find a policy  $\pi_{\boldsymbol{\theta}}$  behaving as close as possible to data
- Use a validation set to avoid overfitting.
- ▶ If the policy  $\pi_{\theta}$  is deterministic, this amounts to minimizing the loss function:

$$Loss(\boldsymbol{\theta}) = \frac{1}{m} \sum_{i=1}^{m} \sum_{t=1}^{H} (\mathbf{a}_{t}^{(i)} - \pi_{\boldsymbol{\theta}}(\mathbf{s}_{t}^{(i)}))^{2}$$

If the policy  $\pi_{\theta}$  is stochastic, a standard approach (among many others) consists in minimizing the log likelihood loss function:

$$Loss(\boldsymbol{\theta}) = \frac{1}{m} \sum_{i=1}^{m} \sum_{t=1}^{H} \log \pi_{\boldsymbol{\theta}}(\mathbf{a}_{t}^{(i)} | \mathbf{s}_{t}^{(i)})$$

### Reward Weighted Regression

- Now, if the expert trajectories are not optimal
- Let  $R(\tau)$  be the return of trajectory  $\tau$
- Still use regression, but weight each sample depending on the return of the corresponding trajectory.
- That is, imitate "more strongly" what is good in the batch than what is bad.
- Still use a validation set to avoid overfitting.
- If the policy  $\pi_{\theta}$  is deterministic, this amounts to minimizing the loss function:

$$Loss(\boldsymbol{\theta}) = \frac{1}{m} \sum_{i=1}^{m} \sum_{t=1}^{H} (\mathbf{a}_{t}^{(i)} - \pi_{\boldsymbol{\theta}}(\mathbf{s}_{t}^{(i)}))^{2} R(\tau^{(i)})$$

If the policy  $\pi_{\theta}$  is stochastic, we minimize the function:

$$Loss(\boldsymbol{\theta}) = \frac{1}{m} \sum_{i=1}^{m} \sum_{t=1}^{H} \log \pi_{\boldsymbol{\theta}}(\mathbf{a}_{t}^{(i)}|\mathbf{s}_{t}^{(i)}) R(\boldsymbol{\tau}^{(i)})$$

▶ Then we can iterate: generate new data from the new policy, and so on

#### PG = RWR!

- ▶ Equation (2) is the same as (1)!
- But wait, the basic PG algorithm is on-policy, and RWR uses expert data in the first step! What's happening?
- My guess: An on-policy algorithm will work from behavioral samples if they are not worse than the current policy
- There also exists AWR, close to REINFORCE with V(s) baseline, thus weight  $= \hat{A}^{\pi}_{\phi_i}(\mathbf{s}^{(i)}_t, \mathbf{a}^{(i)}_t)$
- See my youtube video
- And this blogpost for a wider perspective: Data-driven Deep Reinforcement Learning https://bair.berkeley.edu/blog/2019/12/05/bear/



Peng, X. B., Kumar, A., Zhang, G., and Levine, S. Advantage-weighted regression: Simple and scalable off-policy reinforcement learning. arXiv preprint arXiv:1910.00177, 2019

## Any question?



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References



Xue Bin Peng, Aviral Kumar, Grace Zhang, and Sergey Levine.

Advantage-weighted regression: Simple and scalable off-policy reinforcement learning. arXiv preprint arXiv:1910.00177, 2019.