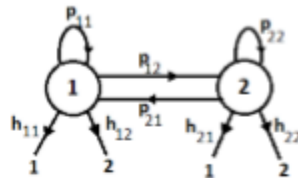


Assignment-3 (HMM, SVM and ANN)

HMM



Model 1		Model 2	
$p_{11} = 0.8$	$p_{21} = 0.3$	$p_{11} = 0.2$	$p_{21} = 0.7$
$h_{11} = 0.9$	$h_{21} = 0.2$	$h_{11} = 0.1$	$h_{21} = 0.8$

Identify the model from which the following data has been generated.

DATA 1: [1 1 1 1 1 | 2 1 1 1 2 | 2 1 1 1 2 | ...
 ... 2 2 1 1 1 | 1 1 1 2 2 | 1 1 2 2 2 | 2 1 1 1 1 | ...
 ... 1 1 1 1 1 | 1 2 1 1 1 | 2 1 1 2 2 | 2 1 1 1 1 | ...
 ... 1 1 1 2 1 | 1 2 1 2 2 | 2 2 2 2 2 | 2 2 1 2 2 | ...
 ... 2 1 1 2 1 | 1 1 1 1 2 | 1 2 1 2 1 | 1 2 2 2 2 | ...
 ... 2 2 2 1 1]

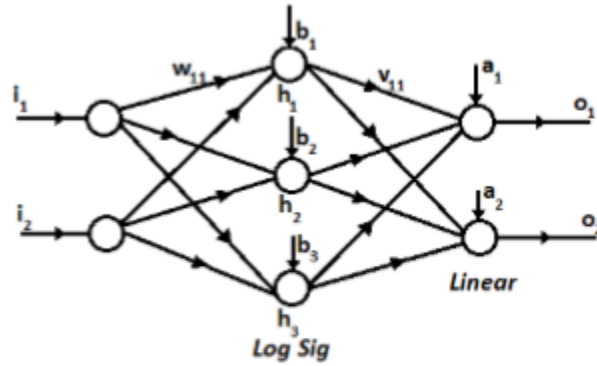
DATA 2: [1 1 1 1 1 | 1 1 1 2 1 | 1 2 2 1 1 | ...
 ... 2 1 2 1 2 | 2 2 1 1 1 | 2 2 1 1 1 | 1 2 2 1 2 | ...
 ... 1 2 1 1 1 | 1 2 1 1 1 | 1 2 2 1 2 | 1 2 1 1 1 | ...
 ... 2 2 1 2 1 | 1 1 1 1 1 | 2 1 1 1 2 | 2 1 1 1 2 | ...
 ... 1 2 1 1 1 | 1 2 1 1 1 | 1 1 1 1 1 | 2 1 1 1 2 | ...
 ... 1 1 2 1 1]

with and without state sequence.

STATE 1: [1 1 1 1 2 | 2 1 1 1 1 | 2 1 1 1 2 | ...
 ... 2 2 1 1 1 | 1 1 2 2 1 | 1 1 1 1 2 | 2 1 1 1 1 | ...
 ... 1 1 1 1 1 | 1 1 1 1 1 | 1 1 1 1 1 | 2 1 1 2 2 | ...
 ... 2 1 1 1 1 | 1 1 1 1 1 | 1 2 2 2 2 | 2 2 2 2 2 | ...
 ... 2 2 2 2 2 | 2 2 2 2 1 | 1 1 1 1 2 | 1 2 2 2 2 | ...
 ... 2 2 2 1 1]

STATE 2: [1 2 2 2 2 | 2 1 2 2 2 | 2 2 1 2 1 | ...
 ... 2 2 1 2 2 | 1 1 2 2 2 | 1 2 2 2 2 | 2 2 1 2 1 | ...
 ... 2 1 2 2 2 | 2 1 2 2 1 | 2 1 1 2 1 | 2 1 1 2 2 | ...
 ... 2 2 2 1 2 | 1 2 2 2 2 | 1 2 2 2 2 | 1 2 2 2 1 | ...
 ... 2 1 2 2 2 | 2 1 1 2 2 | 2 1 2 2 2 | 2 2 2 2 2 | ...
 ... 2 2 1 2 1]

PART-1 ANN



TRAINING:

$$DATA_1 = \begin{bmatrix} 1.08 & 0.75 & 0.85 & 0.94 & 0.40 \\ 0.08 & -0.19 & -0.11 & 0.01 & -0.09 \end{bmatrix}$$

$$DATA_2 = \begin{bmatrix} 0.01 & -0.01 & 0.09 & -0.05 & -0.45 \\ 0.85 & 1.05 & 0.93 & 1.41 & 1.45 \end{bmatrix}$$

VALIDATION:

$$DATA_1 = \begin{bmatrix} 1.25 & 1.19 & 0.99 & 0.69 & 1.32 \\ -0.21 & 0.07 & 0.04 & -0.02 & 0.02 \end{bmatrix}$$

$$DATA_2 = \begin{bmatrix} 0.07 & -0.33 & -0.06 & -0.33 & -0.24 \\ 1.20 & 0.88 & 1.08 & 1.10 & 1.01 \end{bmatrix}$$

1. Initialize the weights:

$w_{11} = 0.85$	$w_{12} = 0.90$	$w_{13} = 0.12$	$w_{21} = 0.91$	$w_{22} = 0.63$	$w_{23} = 0.09$
$v_{11} = 0.28$	$v_{12} = 0.55$	$v_{21} = 0.96$	$v_{22} = 0.96$	$v_{31} = 0.16$	$v_{32} = 0.97$
$b_1 = 0.96$	$b_2 = 0.49$	$b_3 = 0.80$	$a_1 = 0.14$	$a_2 = 0.42$	

2. For the Input $DATA_1$, $DATA_2$, Obtain the hidden layer output and output layer output and error vectors $e_1 = t_1 - o_1$, $e_2 = t_2 - o_2$.

Data Index	h_1	h_2	h_3	o_1	o_2	t_1	t_2	e_1	e_2
1						1	0		
2						1	0		
3						1	0		
4						1	0		
5						1	0		
6						0	1		
7						0	1		
8						0	1		
9						0	1		
10						0	1		

$SSE =$

3. Update the weights using the following:

$$w_{11}(t+1) = w_{11}(t) + \eta h_1(1 - h_1) i_1 [e_1 v_{11} + e_2 v_{12}]$$

$$w_{12}(t+1) = w_{12}(t) + \eta h_2(1 - h_2) i_1 [e_1 v_{21} + e_2 v_{22}]$$

$$w_{13}(t+1) = w_{13}(t) + \eta h_3(1 - h_3) i_1 [e_1 v_{31} + e_2 v_{32}]$$

$$w_{21}(t+1) = w_{21}(t) + \eta h_1(1 - h_1) i_2 [e_2 v_{11} + e_2 v_{12}]$$

$$w_{22}(t+1) = w_{22}(t) + \eta h_2(1 - h_2) i_2 [e_2 v_{21} + e_2 v_{22}]$$

$$w_{23}(t+1) = w_{23}(t) + \eta h_3(1 - h_3) i_2 [e_2 v_{31} + e_2 v_{32}]$$

$$v_{11}(t+1) = v_{11}(t) + \eta h_1 e_1 \quad v_{12}(t+1) = v_{12}(t) + \eta h_1 e_2$$

$$v_{21}(t+1) = v_{21}(t) + \eta h_2 e_1 \quad v_{22}(t+1) = v_{22}(t) + \eta h_2 e_2$$

$$v_{31}(t+1) = v_{31}(t) + \eta h_3 e_1 \quad v_{32}(t+1) = v_{32}(t) + \eta h_3 e_2$$

$$a_1(t+1) = a_1(t) + \eta e_1 \quad a_2(t+1) = a_2(t) + \eta e_2$$

$$b_1(t+1) = b_1(t) + \eta h_1(1 - h_1) [e_1 v_{11} + e_2 v_{12}]$$

$$b_2(t+1) = b_2(t) + \eta h_2(1 - h_2) [e_1 v_{21} + e_2 v_{22}]$$

$$b_3(t+1) = b_3(t) + \eta h_3(1 - h_3) [e_1 v_{31} + e_2 v_{32}]$$

4. Repeat steps 2 and 3 to obtain the following for 5 epochs.

EPOCH 2:

Data Index	h_1	h_2	h_3	o_1	o_2	t_1	t_2	e_1	e_2
1						1	0		
2						1	0		
3						1	0		
4						1	0		
5						1	0		
6						0	1		
7						0	1		
8						0	1		
9						0	1		
10						0	1		

$SSE =$

EPOCH 3:

Data Index	h_1	h_2	h_3	o_1	o_2	t_1	t_2	e_1	e_2
1						1	0		
2						1	0		
3						1	0		
4						1	0		
5						1	0		
6						0	1		
7						0	1		
8						0	1		
9						0	1		
10						0	1		

$SSE =$

EPOCH 4:

Data Index	h_1	h_2	h_3	o_1	o_2	t_1	t_2	e_1	e_2
1						1	0		
2						1	0		
3						1	0		
4						1	0		
5						1	0		
6						0	1		
7						0	1		
8						0	1		
9						0	1		
10						0	1		

$SSE =$

EPOCH 5:

Data Index	h_1	h_2	h_3	o_1	o_2	t_1	t_2	e_1	e_2
1						1	0		
2						1	0		
3						1	0		
4						1	0		
5						1	0		
6						0	1		
7						0	1		
8						0	1		
9						0	1		
10						0	1		

$SSE =$

- Plot SSE versus number of epochs.
- Use the latest weights to obtain the output of the following vectors

<i>Vector</i>	o_1	o_2	Class Index
1.25 -0.21			
1.19 0.07			
0.99 0.04			
0.69 -0.02			
1.32 0.02			
0.07 1.20			
-0.33 0.88			
-0.06 1.08			
-0.33 1.10			
-0.24 1.01			

SVM

Given the data $DATA_1 = [X_1 \ X_2 \ \dots \ X_{10}]$ and $DATA_2 = [X_{11} \ X_{12} \ \dots \ X_{20}]$

$$DATA_1 = \begin{bmatrix} 1.08 & 0.75 & 0.85 & 0.94 & 0.40 & 1.25 & 1.19 & 0.99 & 0.69 & 1.32 \\ 0.08 & -0.19 & -0.11 & 0.01 & -0.09 & -0.21 & 0.07 & 0.04 & -0.02 & 0.02 \end{bmatrix}$$

$$DATA_2 = \begin{bmatrix} 0.01 & -0.01 & 0.09 & -0.05 & -0.45 & 0.07 & -0.33 & -0.06 & -0.33 & -0.24 \\ 0.85 & 1.05 & 0.93 & 1.41 & 1.45 & 1.20 & 0.88 & 1.08 & 1.10 & 1.01 \end{bmatrix}$$

1. Assign $t_i = 1 \ \forall i = 1, \dots, 10$, $t_i = -1 \ \forall i = 11, \dots, 20$

2. Construct the linear equation

$$\begin{bmatrix} K(X_1, X_1)t_1^2 & K(X_1, X_2)t_1t_2 & \dots & K(X_1, X_{20})t_1t_{20} \\ K(X_2, X_1)t_2t_1 & K(X_2, X_2)t_2^2 & \dots & K(X_2, X_{20})t_2t_{20} \\ \vdots & \vdots & \ddots & \vdots \\ K(X_{20}, X_1)t_{20}t_1 & K(X_{20}, X_2)t_{20}t_2 & \dots & K(X_{20}, X_{20})t_{20}^2 \\ t_1 & t_2 & \dots & t_{20} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_{20} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ \vdots \\ 1 \\ 0 \end{bmatrix}$$

where $K(X_i, X_j) = X_i^T \cdot X_j$ with $\sigma^2 = 1$

3. Solve for a_1, \dots, a_{20} .

4. Choose the values $0 \leq a_i \leq C$. C is the box variable. Choose it as 10.
Let $n(M_1) = N_1$. Let the set be M_1 .

5. Choose the values $0 \leq a_i \leq C$. Let $n(M_2) = N_2$. Let the set be M_2 .

6. Compute \mathbf{W} matrix as follows

$$\mathbf{W} = \sum_{n=1, n \in M_2}^{20} a_n t_n \underline{x}_n$$

$\mathbf{W} =$

7. Obtain \mathbf{b} using the following:

$$\mathbf{b} = \frac{1}{N_1} \sum_{m \in M_1} [t_m - \sum_{n \in M_2} a_n t_n K(X_n, X_m)]$$

$\underline{\mathbf{b}} =$

8. Plot the data.

Plot the line $\mathbf{W}^T \cdot \underline{X} + \mathbf{b}$

Inference: See that the obtained line partitions $DATA_1$ and $DATA_2$

Use the kernel function $K(X_i, X_j) = \exp\left(-\frac{(X_i - X_j)^T (X_i - X_j)}{2\sigma^2}\right)$, with $\sigma^2 = 1$.

Obtain the expression for the linear separation line/plane/hyperplane

that partitions the classes.

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Obtain the index obtained for the following test data using the trained SVM.

Data	0.0083		0.08		0.06		1.13		1.21
	0.85		0.93		1.2		0.07		0.20
Index									

(OR) Demonstrate soft-margin SVM classifier using Image.mat (dataset).