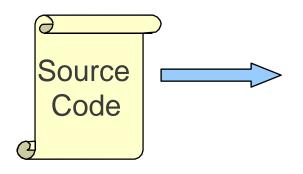
Compilers and Interpreters

Intermediate Code Generation

Where We Are



Lexical Analysis

Syntax Analysis

Semantic Analysis

IR Generation

IR Optimization

Code Generation

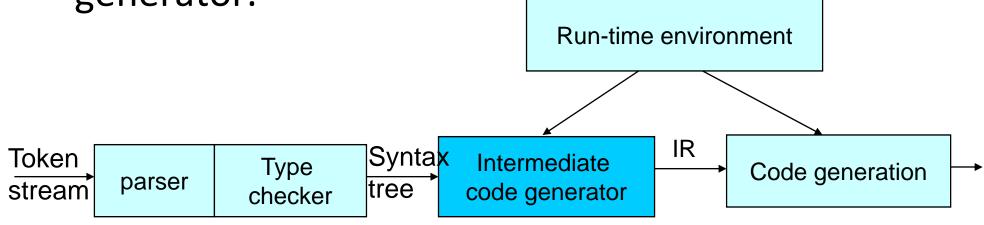
Optimization



Machine Code

Intermediate Code Generation

- Intermediate codes are machine independent codes, but they are close to machine instructions.
- The given program in a source language is converted to an <u>equivalent program</u> in an intermediate language by the intermediate code generator.



Keywords

- Intermediate Representation
 - Directed Acyclic Graph (DAG)
 - Three-address Code
 - Postifx
 - ...
- Checking and Translation
 - Type Checking
 - Translation of Expressions
 - Boolean Expressions Translation
 - Flow-of-Control Statements Translation

Intermediate language

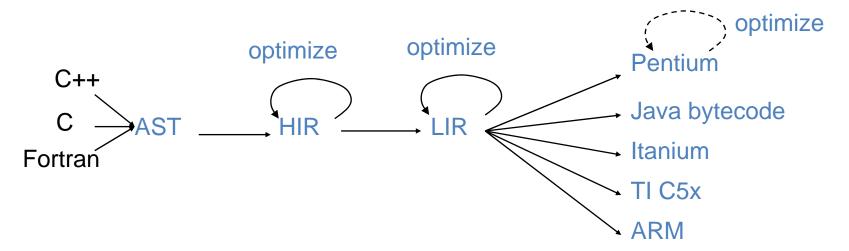
- Intermediate language can be many different languages
 - -syntax trees can be used as an intermediate language.
 - -postfix notation can be used as an intermediate language.
 - -three-address code (Quadruples) can be used as an intermediate language
 - •we will use quadruples to discuss intermediate code generation
 - •quadruples are close to machine instructions, but they are not actual machine instructions.
 - -some programming languages have well defined intermediate languages.
 - •java java virtual machine
 - •In fact, there are byte-code emulators to execute instructions in these intermediate languages.

What Makes a Good IR?

- Captures high-level language constructs
 - –Easy to translate from AST
 - -Supports high-level optimizations
- Captures low-level machine features
 - -Easy to translate to assembly
 - -Supports machine-dependent optimizations
- Narrow interface: small number of node types (instructions)
 - -Easy to optimize
 - –Easy to retarget

Multiple IRs

- Most compilers use 2 IRs:
 - -High-level IR (HIR): Language independent but closer to the language
 - -Low-level IR (LIR): Machine independent but closer to the machine
 - –A significant part of the compiler is both language and machine independent!



Intermediate Representation Categories

Structural (High-level IR)

- graphically oriented
 - e.g.: trees, DAGs
- nodes, edges tend to be large

Linear (Low-level IR)

- pseudo-code for abstract machine
- large variation in level of abstraction
- simple, compact data structures

Hybrids

- combination of graph & linear code
- examples: control flow graphs

IR Category example

Source

```
float a[10][20];
a[i][j+2];
```

Low $\leftarrow \rightarrow$ High

<u>High-level IR</u>

$$t1 = a[i, j+2]$$

Middle-level IR

$$t1 = j + 2$$

$$t2 = i * 20$$

$$t3 = t1 + t2$$

$$t4 = 4 * t3$$

$$t5 = addr a$$

$$t6 = t5 + t4$$

$$t7 = *t6$$

Low-level IR

$$r1 = [fp - 4]$$

$$r2 = [r1 + 2]$$

$$r3 = [fp - 8]$$

$$r4 = r3 * 20$$

$$r5 = r4 + r2$$

$$r6 = 4 * r5$$

$$r7 = fp -216$$

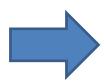
$$f1 = [r7 + r6]$$

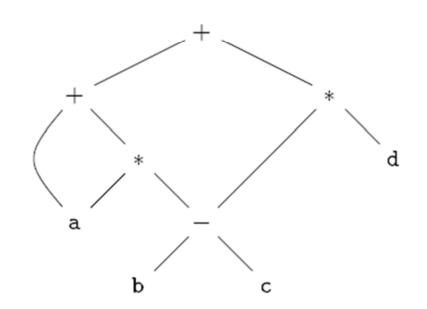
Directed Acyclic Graphs

- A DAG has leaves corresponding to atomic operands and interior codes corresponding to operators.
- A DAG not only represents expressions more succinctly, it gives the compiler important clues regarding the generation of efficient code to evaluate the expressions.

Directed Acyclic Graphs (Cont.)

$$a+a*(b-c)+(b-c)*d$$

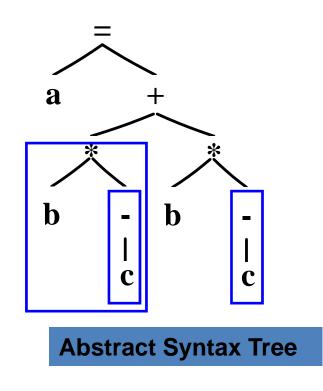


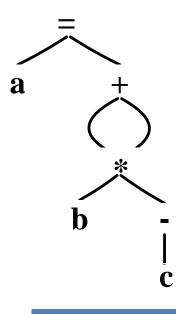


	PRODUCTION	Semantic Rules
1)	$E \to E_1 + T$	$E.node = \mathbf{new} \ Node('+', E_1.node, T.node)$
2)	$E \to E_1 - T$	$E.node = \mathbf{new} \ Node('-', E_1.node, T.node)$
3)	$E \to T$	E.node = T.node
4)	$T \to (E)$	T.node = E.node
5)	$T o \mathbf{id}$	$T.node = \mathbf{new} \ Leaf(\mathbf{id}, \mathbf{id}.entry)$
6)	$T o \mathbf{num}$	$T.node = \mathbf{new} \ Leaf(\mathbf{num}, \mathbf{num}.val)$

Directed Acyclic Graphs

- a=(b*(-c))+ (b*(-c))
- Postfix: a b c uminus * b c uminus * + =





DAG

Postfix Notation

• $a*b+c \Rightarrow ab*c+$

$E \rightarrow T + E_1$	E.code=T.code E ₁ .code +
E→T	E.code =T.code
$T \rightarrow F * T_1$	T.code=F.code T ₁ .code *
T→F	E.code =F.code
F→(E)	E.code =E.code
F→id	F.code =id

```
■ (E, E.code)\Rightarrow(T+E<sub>1</sub>, T.code||E<sub>1</sub>.code||+)

\Rightarrow (F *T<sub>1</sub>+E<sub>1</sub>, F.code||T<sub>1</sub>.code|| * ||E<sub>1</sub>.code||+)

\Rightarrow (a*T<sub>1</sub>+E<sub>1</sub>, a||T<sub>1</sub>.code|| * ||E<sub>1</sub>.code||+)

\Rightarrow (a*F+E<sub>1</sub>, a||F.code|| * ||E<sub>1</sub>.code||+)

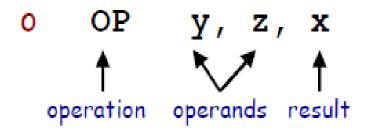
\Rightarrow (a*b+E<sub>1</sub>, a||b||*||E<sub>1</sub>.code||+)

\Rightarrow (a*b+T, a||b||*||T.code||+)

\Rightarrow (a*b+F, a||b||*||F.code||+)

\Rightarrow (a*b+c, a||b||*||c||+)
```

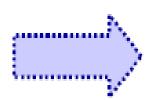
Three-Address Code (Quadruples)



- o Has three names/addresses (x, y, z), or less
- A single operator (OP)
- o We will write as: $x \leftarrow y$ OP z

Example:

$$x \leftarrow (y + z)*(-r);$$



Three-Address Code (Quadruples)

A quadruple is:

$$x := y op z$$

where x, y and z are names, constants or compiler-generated temporaries; op is any operator.

 But we may also the following notation for quadruples (much better notation because it looks like a machine code instruction)

apply operator op to y and z, and store the result in x.

• We use the term "three-address code" because each statement usually contains three addresses (two for operands, one for the result).

Three-Address Code

Binary Operator:

```
op result, y, z or result := y op z
```

where op is a binary arithmetic or logical operator. This binary operator is applied to y and z, and the result of the operation is stored in result.

```
Ex: add a,b,c addi a,b,c gt a,b,c
```

Unary Operator:

```
op result,,y or result := op y
```

where op is a unary arithmetic or logical operator. This unary operator is applied to y, and the result of the operation is stored in result.

```
Ex: uminus a,,c not a,,c inttoreal a,,c
```

Move Operator:

movr a,,c

Unconditional Jumps:

```
jmp ,,L or goto L
```

We will jump to the three-address code with the label \bot , and the execution continues from that statement.

```
Ex: jmp , ,L1 // jump to L1 jmp , ,7 // jump to the statement 7
```

Conditional Jumps:

```
jmp relop y,z,L or
if y relop z goto L
```

We will jump to the three-address code with the label \bot if the result of y relop z is true, and the execution continues from that statement. If the result is false, the execution continues from the statement following this conditional jump statement.

```
Ex: jmpgt y,z,L1 // jump to L1 if y>z
jmpge y,z,L1 // jump to L1 if y>=z
jmpeq y,z,L1 // jump to L1 if y==z
jmpne y,z,L1 // jump to L1 if y!=z
```

Our relational operator can also be a unary operator.

```
jmpnz y,,L1 //jump to L1 if y is not zero
jmpz y,,L1 //jump to L1 if y is zero
jmpt y,,L1 //jump to L1 if y is true
jmpf y,,L1 //jump to L1 if y is false
```

Procedure Parameters:

```
param x,, or param x
```

Procedure Calls:

```
call p,n, or call p,n
```

where x is an actual parameter, we invoke the procedure p with n parameters.

Indexed Assignments:

```
move x, y[i] or x := y[i]
move y[i], x or y[i] := x
```

Address and Pointer Assignments:

```
moveaddr x, y or x := &y movecont x, y or x := *y
```

Three-Address Code Example 1

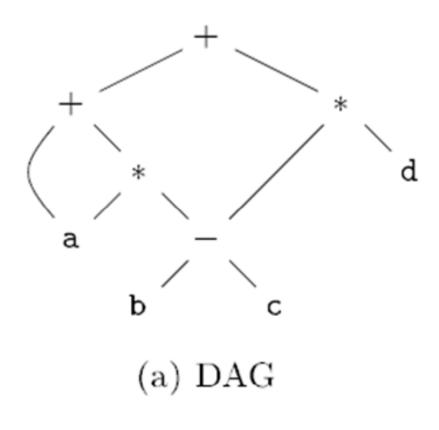
```
n \leftarrow 0
                                       label lTEST
n = 0;
                                       t2 ← n < 10
while (n < 10) {
                                       t3 ← NOT t2
    n = n + 1;
                                       cjmp t3 lEND
                                       label 1BODY
                                       n \leftarrow n+1
                                       jump lTEST
                                       label lEND
```

Three-Address Code Example 2

```
\mathbf{m} = 0;
if (c == 0) {
    m = m + n*n;
   else {
    m = m + n;
```

```
m \leftarrow 0
t1 \leftarrow c == 0
cjmp t1 lTRUE
m \leftarrow m + n
jump lEND
label lTRUE
t2 ← n * n
m \leftarrow m + t2
label lEND
```

Different IRs



$$t_1 = b - c$$
 $t_2 = a * t_1$
 $t_3 = a + t_2$
 $t_4 = t_1 * d$
 $t_5 = t_3 + t_4$

(b) Three-address code

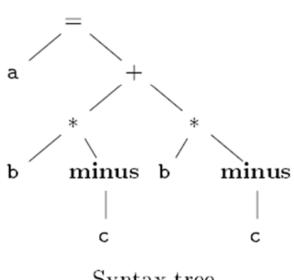
a=(b*(-c))+(b*(-c))

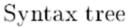
$$t_1$$
 = minus c
 t_2 = b * t_1
 t_3 = minus c
 t_4 = b * t_3
 t_5 = t_2 + t_4
a = t_5

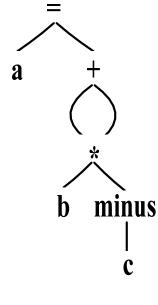
Three-address code

	op	arg_1	arg_2	resuit		
0	minus	c	l I	t_1		
1	*	b	$^{L}_{L}$ t $_{1}$	t_2		
2	minus	С	l I	t_3		
3	*	b	$^{L}_{L}$ t_3	t_4		
4	+	t_2	t_4	L t $_{5}$		
5	=	t ₅	I I	a a		
	•					

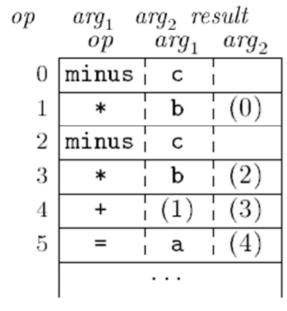
Quadruples







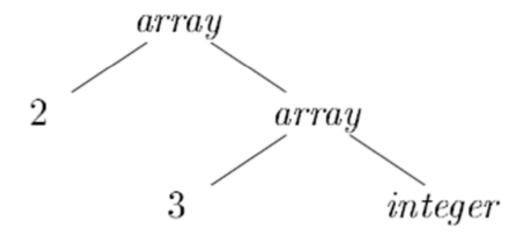
DAG



Triples

Type Expressions

 A type expression is either a basic type or is formed by applying an operator called a type constructor to a type expression. The sets of basic types and constructors depend on the language to be checked.



Type expression for int[2][3]

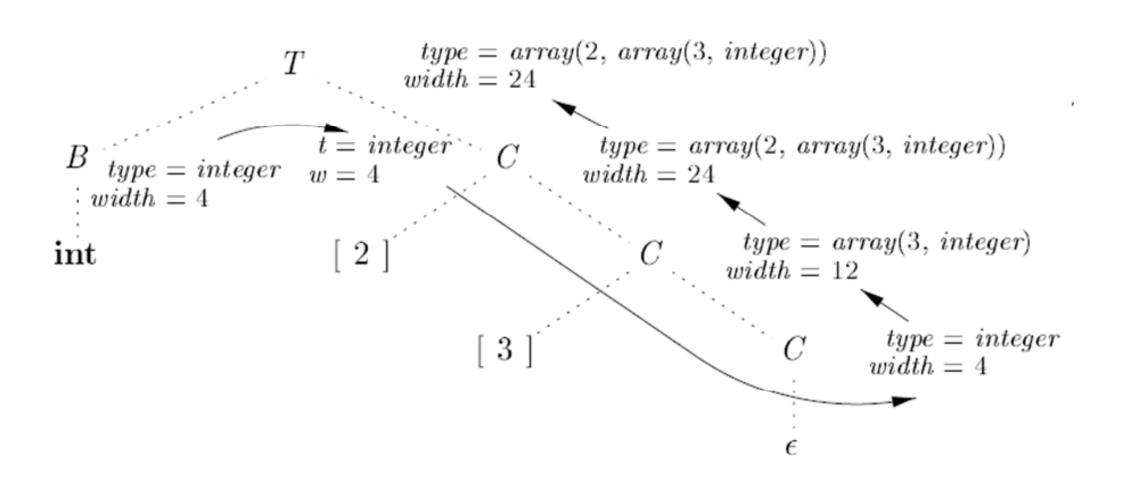
Declarations

- At compile time, we can use these amounts to assign each name a relative address. The type and relative address are saved in the symbol-table entry for the name.
- Data of varying length, such as strings, or data whose size cannot be determined until run time, such as dynamic arrays, is handled by reserving a known fixed amount of storage for a pointer to the data.

```
\begin{array}{lll} T & \rightarrow & B & \{ \ t = B.type; \ w = B.width; \ \} \\ C & \{ \ T.type = C.type; \ T.width = C.width; \ \} \\ B & \rightarrow & \mathbf{int} & \{ \ B.type = integer; \ B.width = 4; \ \} \\ B & \rightarrow & \mathbf{float} & \{ \ B.type = float; \ B.width = 8; \ \} \\ C & \rightarrow & \epsilon & \{ \ C.type = t; \ C.width = w; \ \} \\ C & \rightarrow & [ \ \mathbf{num} \ ] \ C_1 & \{ \ C.type = array(\mathbf{num}.value, \ C_1.type); \\ C.width = \mathbf{num}.value \times C_1.width; \ \} \end{array}
```

Storage Layout for Local Names

Syntax-directed translation of array types



Type Checking

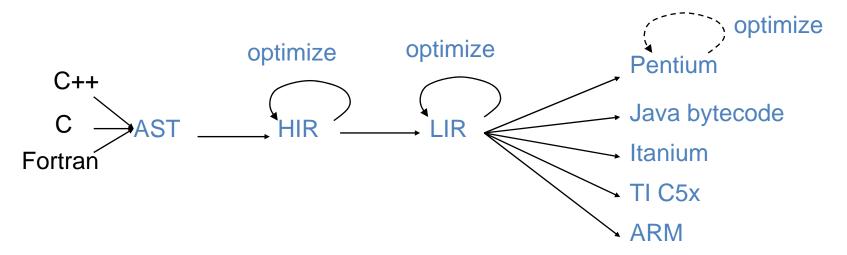
 To do type checking a compiler needs to assign a type expression to each component of the source program. The compiler must then determine that these type expressions conform to a collection of logic al rules that is called the type

Type Systems

- A type system is a collection of rules for assigning type expressions to the parts of a program.
- A type checker implements a type system.
- A sound type system eliminates run-time type checking for type errors.
- A programming language is strongly-typed, if every program its compiler accepts will execute without type errors.
 - -In practice, some of type checking operations are done at runtime (so, most of the programming languages are not stronglytyped).
 - -Ex: int x[100]; ... x[i] most of the compilers cannot guarantee that i will be between 0 and 99

Multiple IRs

- Most compilers use 2 IRs:
 - -High-level IR (HIR): Language independent but closer to the language
 - -Low-level IR (LIR): Machine independent but closer to the machine
 - –A significant part of the compiler is both language and machine independent!



Type Expressions

- The type of a language construct is denoted by a type expression.
- A type expression can be:

–A basic type

- •a primitive data type such as *integer, real, char, boolean, ...*
- type-error to signal a type error
- •void : no type

–A type name

a name can be used to denote a type expression.

A Simple Type Checking System

 The type checker is a translation scheme that synthesizes the type of each expression from the types of its sub-expressions.

```
P \rightarrow D; E

D \rightarrow D; D

D \rightarrow id: T { addtype(id.entry,T.type) }

T \rightarrow char { T.type=char }

T \rightarrow int { T.type=int }

T \rightarrow real { T.type=real }

T \rightarrow \uparrow T_1 { T.type=pointer(T_1.type) }

T \rightarrow array[intnum] of T_1 { T.type=array(0..intnum.val,T_1.type) }
```

Type Checking of Expressions

```
E \rightarrow id
                            { E.type=lookup(id.entry) }
E \rightarrow charliteral { E.type=char }
E \rightarrow intliteral { E.type=int }
E \rightarrow realliteral { E.type=real }
E \rightarrow E_1 + E_2 { if (E<sub>1</sub>.type=int and E<sub>2</sub>.type=int) then E.type=int
                     else if (E<sub>1</sub>.type=int and E<sub>2</sub>.type=real) then E.type=real
                     else if (E<sub>1</sub>.type=real and E<sub>2</sub>.type=int) then E.type=real
                     else if (E<sub>1</sub>.type=real and E<sub>2</sub>.type=real) then E.type=real
                     else E.type=type-error }
E \rightarrow E_1[E_2] { if (E_2.type=int and E_1.type=array(s,t)) then E.type=t
                     else E.type=type-error }
E \rightarrow \uparrow E_1 { if (t=pointer(E1.type)) then E.type=t
                     else E.type=type-error }
```

Type Checking of Functions

```
E → E<sub>1</sub> (E<sub>2</sub>) { if (E<sub>2</sub>.type=s and E<sub>1</sub>.type=s→t) then E.type=t else E.type=type-error }

Ex: int f(double x, char y) { ... }

f: double x char → int argument types return type
```

Structural Equivalence of Type Expressions

- How do we know that two type expressions are equal?
- As long as type expressions are built from basic types (no type names),
 we may use structural equivalence between two type expressions

Structural Equivalence Algorithm (sequiv):

```
if (s and t are same basic types) then return true else if (s=array(s_1,s_2) and t=array(t_1,t_2)) then return (sequiv(s_1,t_1) and sequiv(s_2,t_2)) else if (s = s_1 x s_2 and t = t_1 x t_2) then return (sequiv(s_1,t_1) and sequiv(s_2,t_2)) else if (s=pointer(s_1) and t=pointer(t_1)) then return (sequiv(s_1,t_1)) else if (s = s_1 \rightarrow s_2 and t = t_1 \rightarrow t_2) then return (sequiv(s_1,t_1) and sequiv(s_2,t_2)) else return false
```

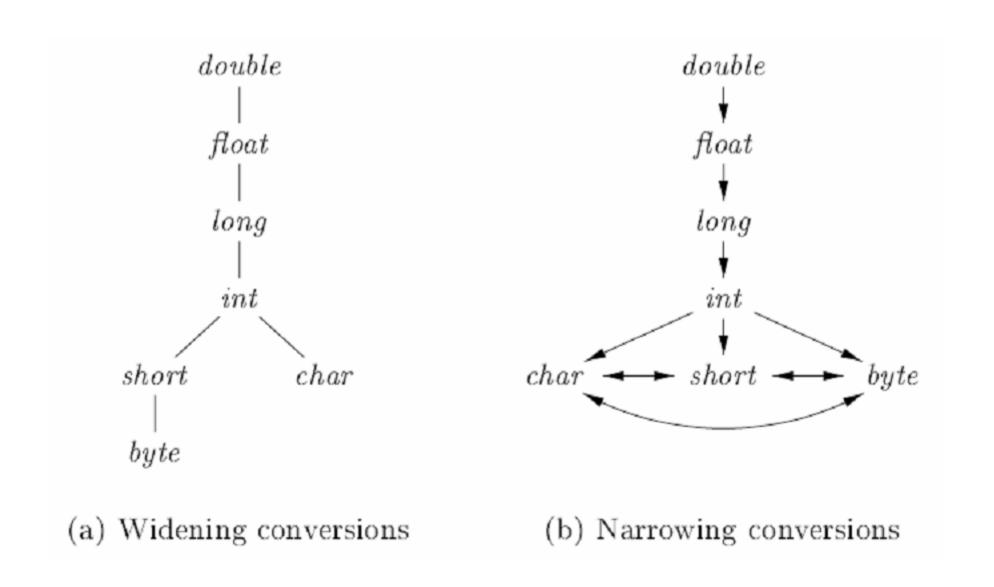
Type Coercions

X + **Y** what is the type of this expression (int or double)?

 What kind of codes we have to produce, if the type of x is double and the type of y is int?

Conversion from one type to another is said to be implicit if it is done automatically by the compiler. Implicit type conversions, also called coercions. Conversion is said to be explicit if the programmer must write something to cause the conversion. Explicit conversions are also called casts.

Type Coercions (cont.)



Overloading

Expressions might have a multitude of types.

- An overloaded symbol is one that has different meanings depending on its context.
 - -The type of E is determined by looking at the possible types of E_1 and E_2 .
- Type error will occur when E.types becomes empty for some expression.

SDD of Expressions

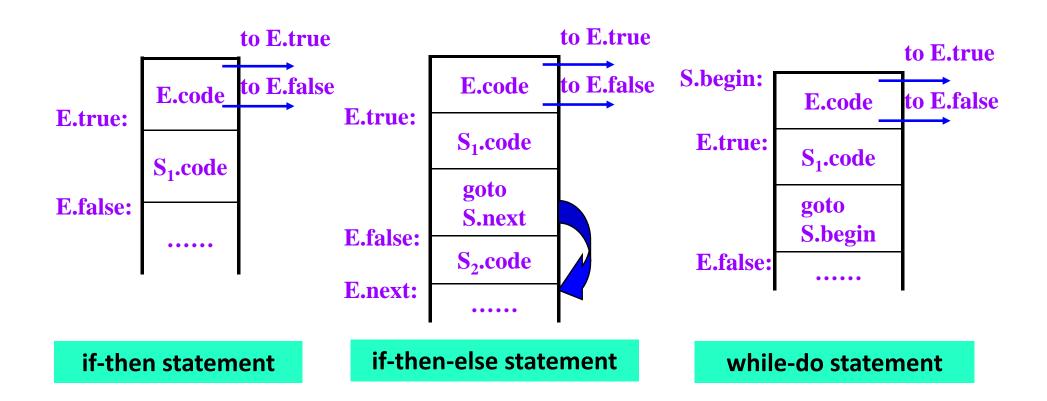
```
S \rightarrow id := E
                   S.code = E.code | | gen('mov' id.place ',,' E.place)
E \rightarrow E_1 + E_2 E.place = newtemp();
                   E.code = E_1.code || E_2.code || gen('add' E.place ',' E_1.place ',' E_2.place)
E \rightarrow E_1 * E_2
                  E.place = newtemp();
                   E.code = E_1.code || E_2.code || gen('mult' E.place ',' E_1.place ',' E_2.place)
                   E.place = newtemp();
E \rightarrow - E_1
                   E.code = E_1.code || gen('uminus' E.place ',,' E_1.place)
                  E.place = E_1.place;
E \rightarrow (E_1)
                   E.code = E_1.code
                   E.place = id.place;
\mathsf{E} 	o \mathsf{id}
                   E.code = null
```

Translation Scheme to Produce Three-Address Code -- Assignment Statements

```
S \rightarrow id := E { p= lookup(id.name);
                    if (p is not nil) then emit('mov' p',,' E.place)
                    else error("undefined-variable") }
E \rightarrow E_1 + E_2 { E.place = newtemp();
                    emit('add' E.place ',' E<sub>1</sub>.place ',' E<sub>2</sub>.place) }
E \rightarrow E_1 * E_2  { E.place = newtemp();
                    emit('mult' E.place ',' E<sub>1</sub>.place ',' E<sub>2</sub>.place) }
E \rightarrow -E_1 { E.place = newtemp();
                    emit('uminus' E.place ',,' E<sub>1</sub>.place) }
E \rightarrow (E_1) { E.place = E_1.place; }
E \rightarrow id { p= lookup(id.name);
                    if (p is not nil) then E.place = id.place
                    else error("undefined-variable") }
```

Flow-of-Control Statement

■ S \rightarrow if E then S₁ | if E then S₁ else S₂ | while E do S₁



PRODUCTION	SEMANTIC RULES
$B \rightarrow B_1 \mid \mid B_2$	$B_1.true = B.true$ $B_1.false = newlabel()$ $B_2.true = B.true$ $B_2.false = B.false$ $B.code = B_1.code \mid\mid label(B_1.false) \mid\mid B_2.code$
$B \rightarrow B_1 \&\& B_2$	$B_1.true = newlabel()$ $B_1.false = B.false$ $B_2.true = B.true$ $B_2.false = B.false$ $B.code = B_1.code \mid\mid label(B_1.true) \mid\mid B_2.code$
$B \rightarrow ! B_1$	$B_1.true = B.false$ $B_1.false = B.true$ $B.code = B_1.code$
$B \rightarrow E_1 \operatorname{\mathbf{rel}} E_2$	$B.code = E_1.code \mid\mid E_2.code$ $\mid\mid gen('if' E_1.addr rel.op E_2.addr 'goto' B.true)$ $\mid\mid gen('goto' B.false)$
$B \rightarrow \mathbf{true}$	B.code = gen('goto' B.true)
$B \rightarrow \mathbf{false}$	B.code = gen('goto' B.false)

Figure 6.37: Generating three-address code for booleans

```
if x < 100 goto L<sub>2</sub>
goto L<sub>3</sub>
L<sub>3</sub>: if x > 200 goto L<sub>4</sub>
goto L<sub>1</sub>
L<sub>4</sub>: if x != y goto L<sub>2</sub>
goto L<sub>1</sub>
L<sub>2</sub>: x = 0
L<sub>1</sub>:
```

Figure 6.38: Control-flow translation of a simple if-statement

```
1) B \rightarrow B_1 \mid M \mid B_2 \quad \{ backpatch(B_1.falselist, M.instr); \}
                                 B.truelist = merge(B_1.truelist, B_2.truelist);
                                B.falselist = B_2.falselist; }
     B \to B_1 \&\& M B_2 \quad \{ backpatch(B_1.truelist, M.instr); \}
                                B.truelist = B_2.truelist:
                                B.falselist = merge(B_1.falselist, B_2.falselist); }
B \rightarrow ! B_1
                              \{B.truelist = B_1.falselist;
                                B.falselist = B_1.truelist; }
4) B \rightarrow (B_1)
                    \{B.truelist = B_1.truelist;
                                B.falselist = B_1.falselist;
5) B \to E_1 rel E_2 { B.truelist = makelist(nextinstr);}
                                B.falselist = makelist(nextinstr + 1);
                                qen('if' E_1.addr rel.op E_2.addr 'goto \_');
                                qen('goto _'); }
6)
     B \to \mathbf{true}
                              \{B.truelist = makelist(nextinstr);
                                gen('goto _'); }
     B \to \mathbf{false}
                              \{B.falselist = makelist(nextinstr);
                                qen('goto _'); }
8)
   M \to \epsilon
                              \{M.instr = nextinstr.\}
```

Figure 6.43: Translation scheme for boolean expressions

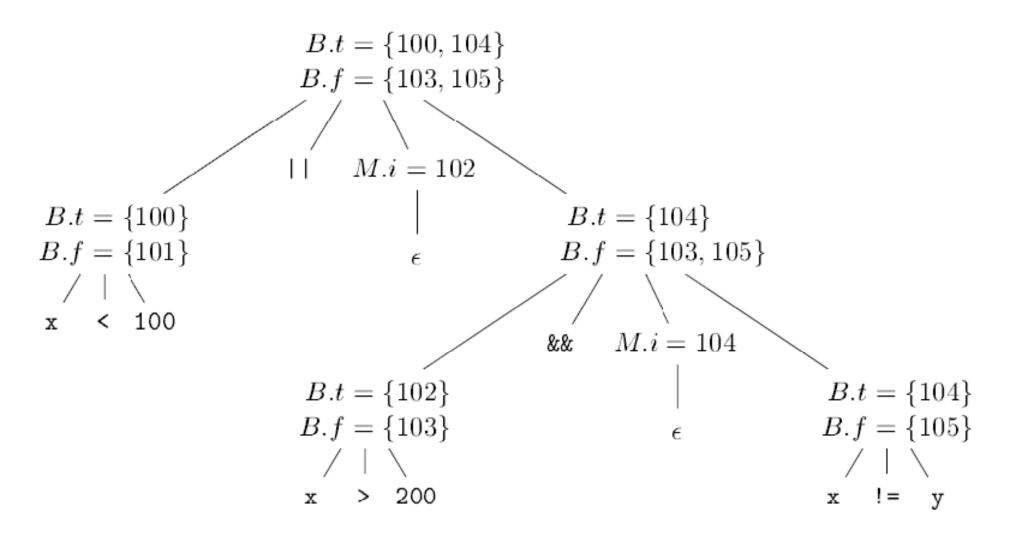


Figure 6.44: Annotated parse tree for $x < 100 \mid \mid x > 200 \&\& x ! = y$

100: if x < 100 goto _
101: goto _
102: if x > 200 goto 104
103: goto _
104: if x != y goto _
105: goto _

(a) After backpatching 104 into instruction 102.

100: if x < 100 goto _
101: goto 102
102: if x > 200 goto 104
103: goto _
104: if x != y goto _
105: goto _

(b) After backpatching 102 into instruction 101.

Figure 6.45: Steps in the backpatch process

```
1) S \to \mathbf{if}(B) M S_1 \{ backpatch(B.truelist, M.instr); \}
                         S.nextlist = merge(B.falselist, S_1.nextlist); 
2) S \rightarrow \mathbf{if}(B) M_1 S_1 N \mathbf{else} M_2 S_2
                       { backpatch(B.truelist, M_1.instr);
                         backpatch(B.falselist, M_2.instr);
                         temp = merge(S_1.nextlist, N.nextlist);
                         S.nextlist = merge(temp, S_2.nextlist); 
3) S \rightarrow while M_1 (B) M_2 S_1
                       { backpatch(S_1.nextlist, M_1.instr);
                         backpatch(B.truelist, M_2.instr);
                         S.nextlist = B.falselist;
                         gen('goto' M_1.instr); \}
4) S \rightarrow \{L\} \{S.nextlist = L.nextlist;\}
5) S \to A; { S.nextlist = null; }
6) M \to \epsilon { M.instr = nextinstr; }
7) N \to \epsilon
                      \{ N.nextlist = makelist(nextinstr); \}
                         qen('goto _'); }
8) L \to L_1 M S { backpatch(L_1.nextlist, M.instr);
                         L.nextlist = S.nextlist;
9) L \to S
                      \{L.nextlist = S.nextlist;\}
```

Figure 6.46: Translation of statements

Reference

- Compilers Principles, Techniques & Tools (Second Edition) Alfred Aho., Monica S. Lam, Ravi Sethi, Jeffrey D. Ullman, Addison-Wesley, 2007
 - Chapter 6.1, 6.2, 6.3, 6.4, 6.5, 6.6, 6.7.1, 6.7.2, 6.7.3
- Coursera Course Compiler, http://www. Coursera.org
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