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Two-Stage Modelling – Cross-Sell Broadband  
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Limited data and methods used!

Presentation serves as an example only!

:)



# Basic Idea Behind Two-Stage Modeling

- Target customers that are likely to give high revenue
- Including more customers with higher expected revenue should compensate lower response probability
  - => Total ROI is probably better but response-rate may suffer
- Terms to look in literature
  - Two-stage models
  - Limited dependence models
  - Double hurdle models
  - Zero-inflated models
  - Bivariate Tobit models
  - Dual response models
  - Component models

# Cross-Selling Broadband Subscriptions Setup

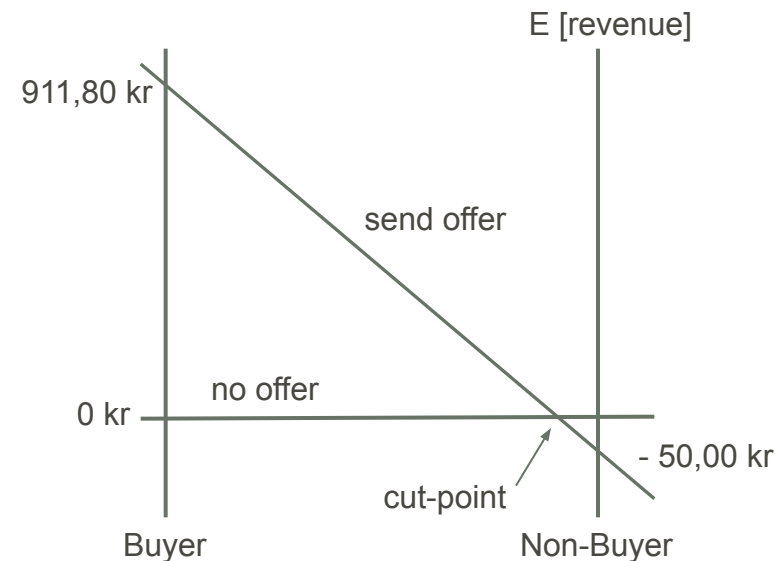
- Goal: offer broadband subscription to current customers who can get broadband but who do not have it today
- Modeling bases on responses to June 2008 BB cross-sell campaign with slight modifications
  - 319 960 customers
  - 42 variables (transformations not included)
- Two target variables available
  - Binary target: customer accepts offer, 12 155 (3,80%) buyers
  - Interval target: if customer accepts offer, what will be the chosen speed (= price)
    - 199 kr – 2 363 customers (19,44%)
    - 229 kr – 5 057 customers (41,60%)
    - 279 kr – 3 587 customers (29,51%)
    - 329 kr – 1148 customers (9,44%)
    - Mean 247,39 kr & median 229 kr
    - Missing value for non-buyers

# Profit Matrix

- Simple profit calculus
  - Campaign cost = 50 kr per customer
  - Assume 229 kr/month median revenue with 12 months binding and 35% margin and we get  $229 \text{ kr/month} * 12 \text{ months} * 0,35 - 50 \text{ kr} = 911,80 \text{ kr}$  income per customers
- Profit matrix (note unbalance):

Outcome	Decision 1 (send offer)	Decision 2 (do not send offer)
1 (Buyer)	911,80	0
0 (Non-Buyer)	- 50,00	0

=> cut-point = 0,05198



# On Selecting Customers to Target Group

Some possible selection criteria

- $P\_BINARY\_TARGET > 0.5$
- $P\_BINARY\_TARGET > \text{cut-point}$
- $P\_BINARY\_TARGET * MEAN\_REVENUE > 0$
- $P\_BINARY\_TARGET * MEDIAN\_REVENUE > 0$
- $P\_BINARY\_TARGET * MEDIAN\_REVENUE - CAMPAIGN\_COST > 0$
- $P\_BINARY\_TARGET * MEDIAN\_REVENUE * MARGIN - CAMPAIGN\_COST > 0$
- $P\_BINARY\_TARGET * P\_REVENUE * MARGIN - CAMPAIGN\_COST > 0$
  
- Expected profit if we decide to send offer:
  - $E(\text{PROFIT} \mid \text{SEND\_OFFER}) = P\_BINARY\_TARGET=1 * \text{REVENUE} + P\_BINARY\_TARGET=0 * (-\text{COST})$
- Expected profit if we decide not to send offer:
  - $E(\text{PROFIT} \mid \text{NO\_OFFER}) = P\_BINARY\_TARGET=1 * 0 + P\_BINARY\_TARGET=0 * 0 = 0$
- Profit matrix can always be transposed so that no-offer column contains zeroes

# Selection Criteria Used This Time

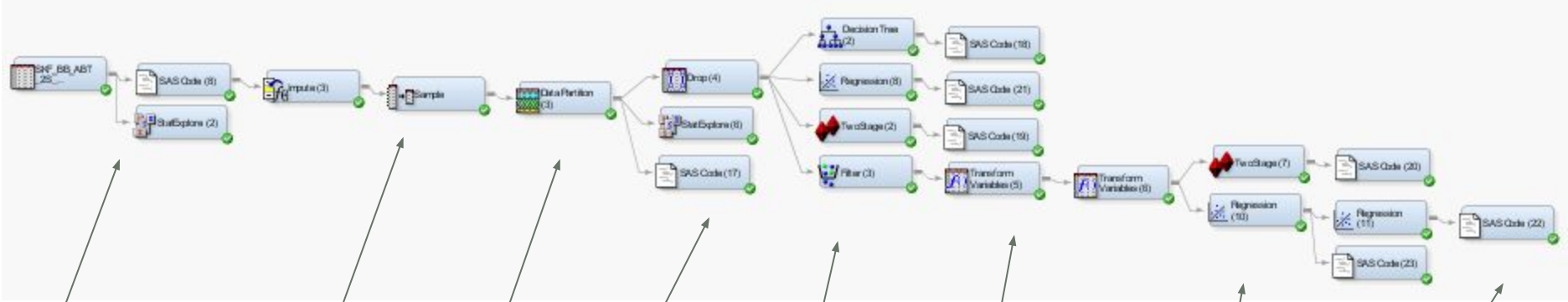
- Expected profit if we decide to send offer:
  - $E(\text{PROFIT} \mid \text{SEND\_OFFER}) = P_{\text{BINARY\_TARGET}=1} * \text{REVENUE} + P_{\text{BINARY\_TARGET}=0} * (-\text{COST})$
- Single stage models:
  - if  $P_{\text{target\_binary1}} * (229 * 12 * 0.35 - 50) - (1 - P_{\text{target\_binary1}}) * 50 > 0$ ;
- Two-Stage models:
  - if  $P_{\text{target\_binary1}} * (P_{\text{target\_interval\_price}} * 12 * 0.35 - 50) - (1 - P_{\text{target\_binary1}}) * 50 > 0$ ;

# Some Evaluation Criteria For Model Selection

- Model Complexity => pick one you understand or one that performs best
- Statistical measures => misclassification rate, average squared error, ...
- Selection-% (= target group size)
- Response-% (= traditional performance measure)
- Expected Average Return On Investment
- Expected Total Return On Investment
- Actual Average Return On Investment in validation data
- Actual Total Return On Investment in validation data
  
- Something else, for example percentage of ROI captured out of total maximum
  
- Often no single good measure, in practice combination of little bit everything chosen



# Enterprise Miner 5.3 Example Flow



Create variable  
for stratification  
and fix data

10% sample

Split to train & validation

Find out optimal  
performance

Model:  
• Tree  
• Regression  
• Two-Stage

Enhance data:  
• remove outliers  
• normalize  
• standardize

Evaluate results  
• Selection-%  
• Response-%  
• AVG ROI  
• SUM ROI

Model:  
• Two-Stage  
• Regression + Regression

## Potential improvements

- Biased sampling (50% / 50% - positive / negative ?)
- Improved modeling methods (bagging / boosting ?)
- Variable selection (variable clustering ?)
- Variable transformations (principal components, binning ?)
- Model log of interval target
- More data ...

# Combined Results

Model	Data	Target Group Size	Selection-%	Expected ROI	Avg Expected Roi	Actual ROI	Avg Actual ROI	Response-%
Tree	Train	2 676	16,73	79 719,60	29,79	217 917,60	81,43	8,3
Tree	Validation	2 798	17,49	83 380,53	29,80	232 303,20	83,02	8,4
Regression	Train	3 279	20,50	79 900,93	24,37	251 276,20	76,63	7,9
Regression	Validation	3 281	20,51	85 385,06	26,02	270 191,00	82,35	8,4
Two-Stage	Train	3 461	21,63	120 530,30	34,83	275 798,60	79,69	8,3
Two-Stage	Validation	3 367	21,05	122 537,00	36,39	214 641,60	63,75	6,6
Regression ®	Train	3 210	20,07	90 063,52	28,06	268 973,00	83,79	8,6
Regression ®	Validation	3 532	22,08	111 668,40	31,62	286 346,00	81,07	8,2
Two-Stage ®	Train	2 080	13,00	79 758,67	38,35	181 127,20	87,08	8,8
Two-Stage ®	Validation	2 248	14,05	99 708,89	44,35	170 023,00	75,63	7,8
Reg + Reg ®	Train	3 730	23,32	113 970,40	30,56	299 267,00	80,23	8,2
Reg + Reg ®	Validation	4 055	25,35	135 788,30	33,49	315 548,00	77,82	7,9

- Highest actual ROI, highest expected ROI and largest selection-%: Reg + Reg on refined data
- Highest response-%, highest average actual ROI and lowest selection-%: Decision Tree

- Reg + Reg on refined data captures 52,5% of maximum potential ROI
- Decision Tree captures only 38,7% of maximum potential ROI

=> Reg+Reg targets 45% more customers, loses 5,6% response-% (0,5 %-units) and gives 35,8% higher ROI (and Reg+Reg actually gives 26,9% more respondents)

# Predicting History...

- Interval target with few distinct values is perhaps not that suitable for two-stage modeling
  - Sales goal might not be compatible with higher ROI and lower response-%
    - However bigger target group with little lower response-% gives more respondents...
  - Availability: some customers can't get top broadband speed => buyer profiles overlap
  - Certain offers may be bundled with certain speed
  - Some customers may want to buy multiple broadband subscriptions
- => it could be more useful to predict best offer and not use two-stage modeling here



# Summary

- Choosing final model not easy
- Response rate probably goes down but total ROI is likely to be higher => marketing manager may be unhappy...
- Two-Stage Modeling is a good idea
- Takes bit more time
- Overall result is often better



# More Material

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- Increasing Profitability of MMS Activation Campaigns – Traditional Modelling Methods vs. Two-Stage Modelling, presentation at SAS Forum International 2004 - Copenhagen 15.-17.6.2004 by Riku Mäkeläinen & Sakari Forslund TeliaSonera Finland / Consumer Marketing
- SAS training course 'Advanced Predictive Modeling Using SAS Enterprise Miner 5.1'
- Two-Stage node documentation





THANK YOU!

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