Case Study 6 (Unit 12): Evaluate Neural Nets using Keras

Team: Hieu Nguyen, Nithya Devadoss, Ramesh Simhambhatla, Ramya Mandava

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Abstract

In Artificial Intelligence, Artificial Neural Networks (ANN) are computing systems vaguely inspired by the biological neural networks that constitute animal brains. The neural network itself is not an algorithm, but rather a framework for many different machine learning algorithms to work together and process complex data inputs. Such systems "learn" to perform tasks by considering examples, generally without being programmed with any task-specific rules. In this case study, we will leverage Keras API, a python package, capable of fast experimentation for deep learning training and testing. We will experiment with a subset of Higgs Boson experimental data acquired from UCI Machine Learning repository. We will use ROC AUC (Area under ROC Curve, which provides an aggregate measure of performance across all possible classification thresholds) as our model performance metric to measure and compare our models. We will experiment with varying number of neurons, hidden layers, activation functions, kernel initializers, optimizers and various other hyper parameters such as epochs, batch sizes, learning rates etc. We will compare the performance results between each of these model in order to extract best model and conloude our findings.

Introduction

The Higgs boson is an elementary particle in the Standard Model of particle physics, produced by the quantum excitation of the Higgs field, one of the fields in particle physics theory [1].

The data set is acquired from UCI Machine Learning repository: https://archive.ics.uci.edu/ml/datasets/HIGGS (https://archive.ics.uci.edu/ml/datasets/HIGGS)

Data Set Information:

The data has been produced using Monte Carlo simulations. The first 21 features (columns 2-22) are kinematic properties measured by the particle detectors in the accelerator. The last seven features are functions of the first 21 features; these are high-level features derived by physicists to help discriminate between the two classes. There is an interest in using deep learning methods to obviate the need for physicists to manually develop such features. Benchmark results using Bayesian Decision Trees from a standard physics package and 5-layer neural networks are presented in the original paper. The last 500,000 examples are used as a test set.

Attribute Information:

The first column is the class label (1 for signal, 0 for background), followed by the 28 features (21 low-level features then 7 high-level features): lepton pT, lepton eta, lepton phi, missing energy magnitude, missing energy phi, jet 1 pt, jet 1 eta, jet 1 phi, jet 1 b-tag, jet 2 pt, jet 2 eta, jet 2 phi, jet 2 b-tag, jet 3 pt, jet 3 eta, jet 3 phi, jet 3 b-tag, jet 4 pt, jet 4 eta, jet 4 phi, jet 4 b-tag, m_jj, m_jjj, m_lv, m_jlv, m_bb, m_wbb, m_wwbb. For more detailed information about each feature see the original paper.

```
In [41]: import pandas as pd
import numpy as np
from keras.models import Sequential
from keras.layers.core import Dense, Dropout, Activation
from keras.optimizers import SGD
from keras.optimizers import Adam
from keras.optimizers import Adagrad
from keras.optimizers import RMSprop
from keras.optimizers import Adamax
from sklearn.metrics import roc_auc_score
```

We will use the data set of 1100000 observations to train and use 60000 observations to test the model

```
In [42]: N=1100000. #Change this line adjust the number of rows.
         data=pd.read csv("HIGGS.csv", nrows=N, header=None)
         test data=pd.read csv("HIGGS.csv", nrows=60000, header=None, skiprows=1100000)
In [43]: def size it (df):
             total=0
             for i in range(len(data.memory_usage())):
                 total=total+data.memory usage()[i]
             size=total/(2**20)
             print("%.2f Megabytes" % size)
In [44]: size it(data)
         data.shape
         251.77 Megabytes
Out[44]: (1100000, 29)
In [45]: | size_it(test_data)
         test_data.shape
         251.77 Megabytes
Out[45]: (60000, 29)
In [46]: data.columns=['label','lepton pT', 'lepton eta', 'lepton phi', 'missing energy magnitude', 'missing e
         nergy phi', 'jet 1 pt',
                       'jet 1 eta', 'jet 1 phi', 'jet 1 b-tag', 'jet 2 pt', 'jet 2 eta', 'jet 2 phi', 'jet 2 b-
         tag', 'jet 3 pt',
                       'jet 3 eta', 'jet 3 phi', 'jet 3 b-tag', 'jet 4 pt', 'jet 4 eta', 'jet 4 phi', 'jet 4 b-
         tag', 'm_jj',
                       'm_jjj', 'm_lv','m_jlv', 'm_bb', 'm_wbb', 'm_wwbb']
```

In [48]: data.tail()

Out[48]:

	label	lepton pT	lepton eta	lepton phi	missing energy magnitude	missing energy phi	jet 1 pt	jet 1 eta	jet 1 phi	jet 1 b- tag	 jet 4 eta
1099995	0.0	1.147101	-0.290297	-0.502390	0.787117	-0.115922	1.501992	-0.961539	-0.940719	2.173076	 0.785724
1099996	1.0	1.078290	0.090525	-1.113295	0.828900	0.153260	1.389315	-0.565447	0.124895	0.000000	 0.542540
1099997	1.0	0.915960	0.174286	-0.096232	1.543762	0.596144	0.664335	-0.476326	-1.245072	1.086538	 -0.108728
1099998	1.0	0.585263	-0.882470	-1.682583	0.990881	0.796417	1.032413	-0.100039	-0.312609	0.000000	 -0.585103
1099999	0.0	1.175833	0.074941	1.691634	0.293551	-0.324434	0.932928	2.726078	0.404855	0.000000	 1.120519

5 rows × 29 columns

In [49]: test_data.tail()

Out[49]:

	label	lepton pT	lepton eta	lepton phi	missing energy magnitude	missing energy phi	jet 1 pt	jet 1 eta	jet 1 phi	jet 1 b- tag	 jet 4 eta	j
59995	0.0	0.370959	1.178448	-0.839749	0.772050	1.058658	0.807243	0.743637	-0.260498	2.173076	 0.321009	0.
59996	0.0	0.971595	-1.077263	1.713273	0.314970	0.231261	0.641067	-0.844692	0.510741	0.000000	 -0.909071	1.1
59997	1.0	1.003622	-0.219197	1.164516	0.555159	0.221953	1.710307	0.027701	1.581794	0.000000	 -0.401049	-0
59998	0.0	1.891765	0.042800	-0.227179	0.876925	0.322577	0.782142	2.035887	-1.363153	0.000000	 1.459478	1.0
59999	1.0	0.989347	-1.482435	-0.797579	0.924406	0.210223	0.481304	-1.085317	1.071214	2.173076	 0.146949	1.1

5 rows × 29 columns

In [50]: data.iloc[:,0:10].describe()

Out[50]:

	label	lepton pT	lepton eta	lepton phi	missing energy magnitude	missing energy phi	jet 1 pt	jet 1 e
count	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+0
mean	5.295173e-01	9.913837e-01	9.533126e-04	-7.382432e-04	9.981465e-01	-7.666476e-04	9.906847e-01	-7.511484e-0
std	4.991282e-01	5.649399e-01	1.008487e+00	1.005848e+00	5.991570e-01	1.006687e+00	4.751833e-01	1.010139e+0
min	0.000000e+00	2.746966e-01	-2.434976e+00	-1.742508e+00	6.259872e-04	-1.743944e+00	1.386017e-01	-2.969725e+(
25%	0.000000e+00	5.907533e-01	-7.363746e-01	-8.719308e-01	5.762637e-01	-8.717909e-01	6.788095e-01	-6.882352e-0
50%	1.000000e+00	8.535544e-01	9.198132e-04	9.714414e-04	8.915848e-01	-1.158754e-03	8.942697e-01	-1.015666e-0
75%	1.000000e+00	1.236592e+00	7.391881e-01	8.693294e-01	1.293202e+00	8.711392e-01	1.170740e+00	6.871941e-01
max	1.000000e+00	8.711782e+00	2.434868e+00	1.743236e+00	9.900929e+00	1.743257e+00	8.382610e+00	2.969674e+0

In [51]: data.iloc[:,10:20].describe()

Out[51]:

	jet 2 pt	jet 2 eta	jet 2 phi	jet 2 b-tag	jet 3 pt	jet 3 eta	jet 3 phi	jet 3 b-ta
count	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+06	1.100000e+(
mean	9.930826e-01	1.694100e-03	2.226422e-04	1.000497e+00	9.924060e-01	2.097878e-03	6.820779e-05	9.992596e-C
std	5.000212e-01	1.008805e+00	1.006862e+00	1.049272e+00	4.867730e-01	1.008249e+00	1.005805e+00	1.193635e+(
min	1.889811e-01	-2.913090e+00	-1.742372e+00	0.000000e+00	2.636076e-01	-2.729663e+00	-1.742069e+00	0.000000e+(
25%	6.573421e-01	-6.925291e-01	-8.707339e-01	0.000000e+00	6.512039e-01	-6.970776e-01	-8.711343e-01	0.000000e+(
50%	8.906413e-01	1.031646e-03	3.514990e-04	0.000000e+00	8.977762e-01	2.903640e-03	-7.519117e-04	0.000000e+(
75%	1.202001e+00	6.965352e-01	8.715371e-01	2.214872e+00	1.222500e+00	7.019747e-01	8.708400e-01	2.548224e+(
max	1.164708e+01	2.913210e+00	1.743175e+00	2.214872e+00	8.864838e+00	2.730009e+00	1.742884e+00	2.548224e+(

In [52]: types={}
 for i in data.columns:
 types[i]=data[i].dtype

```
In [53]: types
Out[53]: {'jet 1 b-tag': dtype('float64'),
          'jet 1 eta': dtype('float64'),
          'jet 1 phi': dtype('float64'),
          'jet 1 pt': dtype('float64'),
          'jet 2 b-tag': dtype('float64'),
          'jet 2 eta': dtype('float64'),
          'jet 2 phi': dtype('float64'),
          'jet 2 pt': dtype('float64'),
          'iet 3 b-tag': dtype('float64'),
          'jet 3 eta': dtype('float64'),
          'jet 3 phi': dtype('float64'),
          'jet 3 pt': dtype('float64'),
          'jet 4 b-tag': dtype('float64'),
          'jet 4 eta': dtype('float64'),
          'jet 4 phi': dtype('float64'),
          'jet 4 pt': dtype('float64'),
          'label': dtype('float64'),
          'lepton eta': dtype('float64'),
          'lepton pT': dtype('float64'),
          'lepton phi': dtype('float64'),
          'm bb': dtype('float64'),
          'm jj': dtype('float64'),
          'm_jjj': dtype('float64'),
          'm jlv': dtype('float64'),
          'm lv': dtype('float64'),
          'm wbb': dtype('float64'),
          'm wwbb': dtype('float64'),
          'missing energy magnitude': dtype('float64'),
          'missing energy phi': dtype('float64')}
```

We further examined the data types of all the features to optimize the memory consumption in roder to improve computational process. We found all the features are of type float, and so we did not change them any futher.

Splitting the data into features and output as well test data.

```
In [54]: y = np.array(data.iloc[:,0])
x = np.array(data.iloc[:,1:])

In [55]: x_test = np.array(test_data.iloc[:,1:])
y_test = np.array(test_data.iloc[:,0])
```

1. Pick 3 or more different architectures (add/subtract layers+neurons) and run the model + score.

1.1 Architecture1: 1 hidden layer with 100 nodes - Base Model

We will begin with our starter model with 1 hidden layer that has 100 neurons and signmoid activation functions

```
In [56]: test results = {}
      arch name = "sigmoid-llayer-100nodes"
      model = Sequential()
      #hidden layer 1: 100 nodes
      model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
      model.add(Activation('sigmoid'))
      model.add(Dropout(0.10))
      #output layer: 1 node
      model.add(Dense(1, kernel initializer='uniform'))
      model.add(Activation('sigmoid'))
      #optimizer
      sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
      #compile
      model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
      model.fit(x, y, epochs=5, batch size=1000)
      score = roc auc score(y test,model.predict(x test))
      print("")
      print("ROC AUC Score for " + arch_name + " is: " + str(score))
      test results[arch name] = score
      Epoch 1/5
      Epoch 2/5
      Epoch 3/5
      Epoch 4/5
```

ROC AUC Score for sigmoid-llayer-100nodes is: 0.7320651934415888

Epoch 5/5

1.2 Architecture 2: 2 hidden layers with 100 nodes each

```
In [57]: arch name = "sigmoid-2layers-100nodes"
      model = Sequential()
      #hidden layer 1: 100 nodes
      model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
      model.add(Activation('sigmoid'))
      model.add(Dropout(0.10))
      #hidden layer 2: 100 nodes
      model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
      model.add(Activation('sigmoid'))
      model.add(Dropout(0.10))
      #output layer: 1 node
      model.add(Dense(1, kernel_initializer='uniform'))
      model.add(Activation('sigmoid'))
      #optimizer
      sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
      #compile
      model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
      model.fit(x, y, epochs=5, batch size=1000)
      score = roc auc score(y test,model.predict(x test))
      print("")
      print("ROC AUC Score for " + arch name + " is: " + str(score))
      test results[arch name] = score
      Epoch 1/5
      Epoch 2/5
      Epoch 3/5
      Epoch 4/5
      Epoch 5/5
      ROC AUC Score for sigmoid-2layers-100nodes is: 0.6863232135063109
```

1.3 Architecture 3: 3 hidden layers with 100 nodes each

```
In [58]: arch name = "sigmoid-3layers-100nodes"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results[arch name] = score
```

2. With those same 3 architectures, run the SAME architecture but with 2 different (from sigmoid) activation functions. Google the Keras documentation for a look at different available activations.

Architecture 2 using ReLU

2.1.1 Architecture1: 1 hidden layer with 100 nodes using ReLU

```
In [59]: | arch_name = "relu-1layer-100nodes"
      model = Sequential()
      #hidden layer 1: 100 nodes
      model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
      model.add(Activation('relu'))
      model.add(Dropout(0.10))
      #output layer: 1 node
      model.add(Dense(1, kernel initializer='uniform'))
      model.add(Activation('sigmoid'))
      #optimizer
      sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
      #compile
      model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
     model.fit(x, y, epochs=5, batch_size=1000)
      score = roc auc score(y test,model.predict(x test))
      print("")
      print("ROC AUC Score for " + arch name + " is: " + str(score))
      test results[arch name] = score
      Epoch 1/5
      Epoch 2/5
      Epoch 3/5
      Epoch 4/5
      Epoch 5/5
      ROC AUC Score for relu-llayer-100nodes is: 0.7868069467401482
```

2.1.2 Architecture 2: 2 hidden layers with 100 nodes each using ReLU

```
In [60]: | arch_name = "relu-2layers-100nodes"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results[arch name] = score
         Epoch 1/5
```

2.1.3 Architecture 3: 3 hidden layers with 100 nodes each using ReLU

```
In [61]: arch name = "relu-3layers-100nodes-batch1000"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results[arch name] = score
```

Architecture 3 using Tanh

2.2.1 Architecture1: 1 hidden layer with 100 nodes using Tanh

```
In [62]: arch_name = "tanh-1layer-100nodes"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('tanh'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch_size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results[arch name] = score
```

2.2.2 Architecture 2: 2 hidden layers with 100 nodes each using tanh

```
In [63]: | arch_name = "tanh-2layers-50nodes"
      model = Sequential()
      #hidden layer 1: 100 nodes
      model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
      model.add(Activation('tanh'))
      model.add(Dropout(0.10))
      #hidden layer 2: 100 nodes
      model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
      model.add(Activation('tanh'))
      model.add(Dropout(0.10))
      #output layer: 1 node
      model.add(Dense(1, kernel initializer='uniform'))
      model.add(Activation('sigmoid'))
      #optimizer
      sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
      #compile
      model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
      model.fit(x, y, epochs=5, batch size=1000)
      score = roc auc score(y test,model.predict(x test))
      print("")
      print("ROC AUC Score for " + arch_name + " is: " + str(score))
      test results[arch name] = score
      Epoch 1/5
      Epoch 2/5
      Epoch 3/5
      Epoch 4/5
      Epoch 5/5
      ROC AUC Score for tanh-2layers-50nodes is: 0.7703052432297541
```

2.2.3 Architecture 3: 3 hidden layers with 100 nodes each using tanh

```
In [64]: arch name = "tanh-3layers-100nodes"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('tanh'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('tanh'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('tanh'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results[arch name] = score
```

Compare all tests

```
In [65]: testSeries = pd.Series(test_results)
         testSeries.sort values(ascending=False, inplace=True)
         testSeries
Out[65]: relu-3layers-100nodes-batch1000
                                             0.812324
         relu-2layers-100nodes
                                             0.808900
         relu-1layer-100nodes
                                             0.786807
         tanh-2layers-50nodes
                                             0.770305
         tanh-3layers-100nodes
                                             0.768831
         tanh-1layer-100nodes
                                             0.759942
         sigmoid-1layer-100nodes
                                             0.732065
         sigmoid-2layers-100nodes
                                             0.686323
         sigmoid-3layers-100nodes
                                             0.506056
         dtype: float64
```

3. Take your best model from parts 1&2 and vary the batch size by at least 2 orders of magnitude

Our best model from previous tests was using ReLU activation functions with 3 layers and 100 neurons each. We will now experiment changing the batch sizes of 100, 10000, and 100000 - and compare results

```
In [66]: test_results_batch = {}
         test results batch["relu-3layers-100nodes-batch1000"] = testSeries[0]
         arch name = "relu-3layers-100nodes-batch10K"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=10000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results batch[arch name] = score
```

ROC AUC Score for relu-3layers-100nodes-batch10K is: 0.7454849185402521

```
In [67]: arch name = "relu-3layers-100nodes-batch100K"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=100000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results batch[arch name] = score
```

ROC AUC Score for relu-3layers-100nodes-batch100K is: 0.5542685851098367

```
In [68]: arch name = "relu-3layers-100nodes-batch100"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=100)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results batch[arch name] = score
```

```
Epoch 1/5
    Epoch 2/5
    Epoch 3/5
    Epoch 4/5
    Epoch 5/5
    ROC AUC Score for relu-3layers-100nodes-batch100 is: 0.8095547108313648
In [69]: testSeries = pd.Series(test results batch)
    testSeries.sort values(ascending=False, inplace=True)
    testSeries
Out[69]: relu-3layers-100nodes-batch1000
                     0.812324
    relu-3layers-100nodes-batch100
                     0.809555
    relu-3layers-100nodes-batch10K
                     0.745485
    relu-3layers-100nodes-batch100K
                     0.554269
    dtype: float64
```

4. Take your best model (score) from parts 1&2 and use 3 different kernel initializers. Use a reasonable batch size.

In this section, we will use our best model (ReLU activation function, with 3 hidden layers of 100 neurons each w/batch size of 1000 inputs), and experiment with kernel initilizers such as 'random_uniform', 'glorot_uniform' and 'he_uniform'

```
In [70]: test_results_kernals = {}
         test results kernals["relu-3layers-100nodes-batch1000-uniform"] = testSeries[0]
         arch name = "relu-3layers-100nodes-batch1000-randomuniform"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results kernals[arch name] = score
```

ROC AUC Score for relu-3layers-100nodes-batch1000-randomuniform is: 0.813445948173916

```
In [71]: arch name = "relu-3layers-100nodes-batch1000-glorotuniform"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='glorot uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='glorot uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='glorot uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results kernals[arch name] = score
```

ROC AUC Score for relu-3layers-100nodes-batch1000-glorotuniform is: 0.8124337469460416

```
In [72]: arch name = "relu-3layers-100nodes-batch1000-heuniform"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='he uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='he uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='he uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch_name + " is: " + str(score))
         test results kernals[arch name] = score
```

```
Epoch 1/5
    Epoch 2/5
    Epoch 3/5
    Epoch 4/5
    Epoch 5/5
    ROC AUC Score for relu-3layers-100nodes-batch1000-heuniform is: 0.8014568339834331
In [73]: testSeries = pd.Series(test results kernals)
    testSeries.sort values(ascending=False, inplace=True)
    testSeries
Out[73]: relu-3layers-100nodes-batch1000-randomuniform
                              0.813446
    relu-3layers-100nodes-batch1000-glorotuniform
                              0.812434
    relu-3layers-100nodes-batch1000-uniform
                              0.812324
    relu-3layers-100nodes-batch1000-heuniform
                              0.801457
    dtype: float64
```

5. Take your best results from #3 and try 3 different optimizers.

Our best model userd SGD optimizer in the previous experiment. In this section, we will use our best model to experiment with 3 different optimizers such as adagrad, adam, rmsprop to compare the model peformances

```
In [80]: test_results_optimizers = {}
    test_results_optimizers["relu-3layers-100nodes-batch1000-randomuniform-sgd"] = testSeries[0]
    test_results_optimizers
Out[80]: {'relu-3layers-100nodes-batch1000-randomuniform-sgd': 0.813445948173916}
```

```
In [81]: arch name = "relu-3layers-100nodes-batch1000-randomuniform-adagrad"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input_dim=x.shape[1], kernel_initializer='random_uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel_initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         \# sqd = SGD(lr=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         adagrad = Adagrad(lr=0.01, epsilon=None, decay=1e-6)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=adagrad)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results optimizers[arch name] = score
```

ROC AUC Score for relu-3layers-100nodes-batch1000-randomuniform-adagrad is: 0.7925072607508825

```
In [82]: arch name = "relu-3layers-100nodes-batch1000-randomuniform-adam"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input_dim=x.shape[1], kernel_initializer='random_uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel_initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         \# sqd = SGD(1r=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         adam = Adam(1r=0.1, beta 1=0., epsilon=None, decay=1e-6)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=adam)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results optimizers[arch name] = score
```

ROC AUC Score for relu-3layers-100nodes-batch1000-randomuniform-adam is: 0.5

```
In [83]: arch name = "relu-3layers-100nodes-batch1000-randomuniform-rmsprop"
         model = Sequential()
         #hidden layer 1: 100 nodes
         model.add(Dense(100, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 100 nodes
         model.add(Dense(100, input_dim=x.shape[1], kernel_initializer='random_uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 100 nodes
         model.add(Dense(100, input_dim=x.shape[1], kernel_initializer='random_uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         \# sqd = SGD(1r=0.1, decay=1e-6, momentum=0.9, nesterov=True)
         # adamax = Adamax(1r=0.1, beta 1=0.9, epsilon=None, decay=1e-6)
         #adadelta = Adadelta(lr=0.1, rho=0.95, epsilon=None, decay=1e-6)
         rmsprop = RMSprop(lr=0.001, rho=0.9, epsilon=None, decay=0.0)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=rmsprop)
         model.fit(x, y, epochs=5, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         test results optimizers[arch name] = score
```

```
Epoch 1/5
     Epoch 2/5
     Epoch 3/5
     Epoch 4/5
     Epoch 5/5
     ROC AUC Score for relu-3layers-100nodes-batch1000-randomuniform-rmsprop is: 0.8082289253285946
In [84]: testSeries = pd.Series(test results optimizers)
     testSeries.sort values(ascending=False, inplace=True)
     testSeries
Out[84]: relu-3layers-100nodes-batch1000-randomuniform-sqd
                                    0.813446
     relu-3layers-100nodes-batch1000-randomuniform-rmsprop
                                    0.808229
     relu-3layers-100nodes-batch1000-randomuniform-adagrad
                                    0.792507
     relu-3layers-100nodes-batch1000-randomuniform-adam
                                    0.500000
     dtype: float64
```

6. Take all that you've learned so far and give your best shot at producing a score.

After experimenting with various parameters, we have achieved best peformance with ReLU activation function for 3 hidden layers with 100 neurons each, with a batch size of 1000, SGD optimizer and random_uniform kernel initializer. We will now experiment changing some of these key parameters and find out if there will be further improvement in the model performance.

```
In [85]: arch name = "relu-3layers-100nodes-batch1000-randomuniform-sqd-THE BEST"
         model = Sequential()
         #hidden layer 1: 200 nodes
         model.add(Dense(200, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 2: 200 nodes
         model.add(Dense(200, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 3: 200 nodes
         model.add(Dense(200, input_dim=x.shape[1], kernel_initializer='random_uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #hidden layer 4: 200 nodes
         model.add(Dense(200, input dim=x.shape[1], kernel initializer='random uniform'))
         model.add(Activation('relu'))
         model.add(Dropout(0.10))
         #output layer: 1 node
         model.add(Dense(1, kernel initializer='uniform'))
         model.add(Activation('sigmoid'))
         #optimizer
         sqd = SGD(1r=0.15, decay=1e-8, momentum=0.95, nesterov=True)
         #compile
         model.compile(loss='binary crossentropy', metrics=['accuracy'], optimizer=sqd)
         model.fit(x, y, epochs=20, batch size=1000)
         score = roc auc score(y test,model.predict(x test))
         print("")
         print("ROC AUC Score for " + arch name + " is: " + str(score))
         # test results optimizers[arch name] = score
```

```
Epoch 1/20
Epoch 2/20
Epoch 3/20
Epoch 4/20
Epoch 5/20
Epoch 6/20
Epoch 7/20
Epoch 8/20
Epoch 9/20
Epoch 10/20
Epoch 11/20
Epoch 12/20
Epoch 13/20
Epoch 14/20
Epoch 15/20
Epoch 16/20
Epoch 17/20
Epoch 18/20
Epoch 19/20
Epoch 20/20
```

ROC AUC Score for relu-3layers-100nodes-batch1000-randomuniform-sqd-THE BEST is: 0.84338237923623

10 points - Q1: What was the effect of adding more layers/neurons.

During this exercise, we have gamed with our best model by adjusting layers and neurons. We have tested the model with 100 and 200 neurons in each of the layers, and also tested with 3, 4 and 5 hidden layers. We found that adding additional neurons to the layers increased the ROC AUC Score by about 2% (from ~0.8127 to ~0.8267), and additional 1% increase by adding 4th layer (from ~0.8267 to ~0.83) - with number of epochs at 10. However, the score slighly decreased by adding 5th layer. We reran our final model with 20 epochs and achieved the score of 0.8433. We conclude 4 layers with 200 neurons each yielded best results with all other parameters unchanged.

10 points - Q2: Which parameters gave you the best result and why (in your opinion) did they work.

We have achieved the best results with following key parameters:

Activation function for Hidden Layers: ReLU. The ReLu function is defined as A(x) = max(0,x). It gives an output x if x is positive and 0 otherwise. ReLu is less computationally expensive than tanh and sigmoid because it involves simpler mathematical operations. That is a good point to consider when we are designing deep neural nets [2].

Kernel Initializer: random_uniform. Initializer that generates tensors with a uniform distribution.

Optimizer: SGD (with learning rate=0.15; decay=1e-8, momentum=0.95) (we have increased learning rate from 0.1 to 0.15, decreased decay from 1e-6 to 1e-8 and increased momentum from 0.9 to 0.95 compared to the base model)

Number of Epochs: We started the base model with 5 epochs, and gradually increased to 10 and 20. We have observed that the score significantly increased as we increase the epochs.

Batch size: We tested the batch sizes of 100, 1000, 10000 and 100000. We have observed the best scores with the batch size at 1000.

In our opinion, Rectified Linear Units (ReLU) activation function is appropriate for the dataset as it non-linear and is computationally less expensive from other functions considering binary classification of the problem; Random_Uniform aids at removing bias while uniformly distributing initial weights; and Stochastic Gradient Descent (SGD) does batch processing that performs redundant computations for large datasets, as it recomputes gradients for similar examples before each parameter update. SGD does away with this redundancy by performing one update at a time.

20 points - Q3: For #6, how did you decide that your model was 'done'

We have started our base model with 'sigmoid' activation function with 'uniform' Kernel Initializer, 'SGD' Optimizer with 1 hidden layer, with 5 epochs and a batch size of 1000. We have used ROC AUC score as our metric to measure the performance of the model. When we gamed changing these parameters, we have observed the ROC AUC score ranging from 0.5 to 0.7 with our base model. We continued to tune the parametrs as decribed in the previous sections, we have certainly improved the model performance significantly with our BEST model (activation funtion: ReLU, Optimizer: SGG, Kernal Initializer: random_uniform, epochs:20, batch size:1000) with ROC AUC score of 0.8428. The improvement of the scores can still be possible with further tuning of number of epochs, batch size and other parameters we did not test. We conclude the exercise given the time and resource constraints, and achieved satisfactory results, and we call it done.

References

- [1] Higgs Boson Experiment (Wikipedia) https://en.wikipedia.org/wiki/Higgs boson (https://en.wiki/Higgs boson (http
- [2] https://medium.com/the-theory-of-everything/understanding-activation-functions-in-neural-networks-9491262884e0 (https://medium.com/the-theory-of-everything/understanding-activation-functions-in-neural-networks-9491262884e0)
- [3] Prof Slater's sample code and presentations

Thank you