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### Step 1: Import CSV Data

(reference apolloMain\_5 amd apolloMain\_6 as example for data manipulation) biasData = readtable('user\_choices.csv'); % Replace with the path to your data file disp('User bias data imported successfully.'); taskChoice\_Data = readtable('user\_choices.csv'); % Replace with the path to your data file disp('User task choice data imported successfully.');

```
robotChoice_Data = readtable('G:\My Drive\myResearch\Research Experimentation\Apollo\apollo\data\WarehouseRobot_Pairing_Data\test_pairing_data.csv');
disp('User robot choice data imported successfully.');
% Extract relevant data (modify based on your CSV structure)
% task_attributes = data{:, {'efficiency', 'speed', 'safety', 'durability', 'skill'}};
% Extract and organize robot states for all three alternatives
robot_states = struct();
attributes = {'energy','pace','safety','reliability','intelligence'};
for i = 1:3
   for attr = attributes
       robot_states.(['robot' num2str(i)]).(attr{1}) = ...
            robotChoice Data.(['robot' num2str(i) attr{1}]);
    end
end
% Extract choice data and other metadata
choices = robotChoice_Data.choice;
participant_ids = robotChoice_Data.participantid;
trial_numbers = robotChoice_Data.trial;
stake_types = robotChoice_Data.staketype;
time_spent = robotChoice_Data.timespent;
```

User robot choice data imported successfully.

# Step 2: R Bridge Implementation

```
disp('Initializing R bridge...');
% Configure paths
rscript_path = 'C:\Program Files\R\R-4.4.2\bin\x64\Rscript.exe';
\label{eq:r_script} $$ 'G:\My Drive\myResearch\Research Experimentation\Apollo\apollo\example\DFT_Resource\_Allocation.R'; $$ $$
csvFile = 'G:\My Drive\myResearch\Research Experimentation\Apollo\apollo\data\WarehouseRobot_Pairing_Data\HumanData_Resource_Allocation.csv';
outputDir = 'G:\My Drive\myResearch\Research Experimentation\Apollo\apollo\ResourceAllocation_Output';
% Verify installations
if ~isfile(rscript_path)
    error('Rscript.exe not found at: %s', rscript_path);
elseif ~isfile(r_script)
    error('R script not found at: %s', r_script);
elseif ~isfile(csvFile)
    error('Input CSV not found at: %s', csvFile);
elseif ~isfolder(outputDir)
    warning('Output folder does not exist, creating: %s', outputDir);
    mkdir(outputDir);
% Execute R with JSON output
    % Use proper argument formatting
    cmd = sprintf(['"%s" "%s" ', ...
```

```
'-i "%s" -o "%s"'], ...
               rscript_path, r_script, csvFile, outputDir);
[status,result] = system(cmd);
    if status == 0
        % Handle output path (whether directory or file)
        if isfolder(outputDir)
            jsonFile = fullfile(outputDir, 'DFT_output.json');
            jsonFile = outputDir;
        % Parse JSON output
        if exist(jsonFile, 'file')
            jsonText = fileread(jsonFile);
            params = jsondecode(jsonText);
            % Extract parameters with validation
            %Boundedphi1, phi2 parameters
            %phi1 = max(0, validateParam(params, 'phi1', 0.5)); % Ensure non-negative
            %phi2 = min(max(0, validateParam(params, 'phi2', 0.8)), 1); % Constrain 0-1
            %Raw phi1, phi2 parameters
            phi1 = validateParam(params, 'phi1', 0.5);
            phi2 = validateParam(params, 'phi2', 0.8);
            tau = 1 + exp(validateParam(params, 'timesteps', 0.5));
            error_sd = min(max(0.1, validateParam(params, 'error_sd', 0.1)), 1); % still clip here
            % Extract attribute weights
            beta_weights = exp([
                params.b_energy;
                params.b_pace;
                params.b_safety;
                params.b_reliability;
                params.b_intelligence
            1);
            % Get initial preferences from ASCs
            initial_P = [
               params.asc_1;
                params.asc_2;
               params.asc_3;
              % 0 % Control alternative1 has 0 initial preference
              % 0 % Control alternative2 has 0 initial preference
            ];
            disp('Estimated Parameters:');
            disp(['phi1: ', num2str(phi1)]);
disp(['phi2: ', num2str(phi2)]);
            disp(['tau: ', num2str(tau)]);
            disp(['error_sd: ', num2str(error_sd)]);
            disp('Initial Preferences (from ASCs):');
            disp(initial_P');
        else
            error('R output file not found');
    else
        error('R execution failed: %s', result);
    end
catch ME
    disp('Error during R execution:');
    disp(getReport(ME, 'extended'));
    [phi1, phi2, tau, error_sd] = getFallbackParams();
    beta\_weights = [0.3; 0.2; 0.4]; \% Default weights ; 0.1; 0.5
    initial_P = zeros(3,1); % Neutral initial preferences
end
```

Initializing R bridge...

### Step 3: MDFT Formulation to Calculate Preference Dynamics

(MDFT calculations based on estimated parameters)

```
%current_trial = 1; % Analyze first trial (can be looped later)
num_trials = size(robotChoice_Data, 1); % Assuming each row is a trial
```

```
for current_trial = 1:num_trials
   % Extract data for the current trial
   trial_data = robotChoice_Data(current_trial, :);
\% Create M matrix from current trial's attributes
M = [
   robotChoice_Data.robot1energy(current_trial), ...
   robotChoice_Data.robot1pace(current_trial), ...
   robotChoice_Data.robot1safety(current_trial), ...
   robotChoice_Data.robot1reliability(current_trial), ...
   robotChoice_Data.robot1intelligence(current_trial);
   robotChoice_Data.robot2energy(current_trial), ...
   robotChoice_Data.robot2pace(current_trial), ...
   robotChoice_Data.robot2safety(current_trial), ...
   robotChoice_Data.robot2reliability(current_trial), ...
   robotChoice_Data.robot2intelligence(current_trial);
   robotChoice_Data.robot3energy(current_trial), ...
   robotChoice_Data.robot3pace(current_trial), ...
   robotChoice_Data.robot3safety(current_trial), ...
   robotChoice_Data.robot3reliability(current_trial), ...
   robotChoice_Data.robot3intelligence(current_trial);
  % 0.1*ones(1,5) % Control alternative1
  % 0.9*ones(1,5) % Control alternative2
];
% Normalize beta weights
beta = beta_weights ./ sum(abs(beta_weights));
% Calculate DFT dynamics with initial preferences
[E_P, V_P, probs, P_tau] = calculateDFTdynamics(...
   phi1, phi2, tau, error_sd, beta, M, initial_P);
% Display results
disp('=== Current Trial Analysis ===');
disp(['Trial: ', num2str(current_trial)]);
disp(['Participant: ', num2str(participant_ids(current_trial))]);
disp(['Actual Choice: Robot ', num2str(choices(current_trial))]);
disp('M matrix (alternatives × attributes):');
disp(array2table(M, ...
    'RowNames', {'Robot1', 'Robot2', 'Robot3'}, ...
    'VariableNames', attributes)); %, 'Control Alt1', 'Control Alt2'
% Create comparison table
result_table = table(probs, 'VariableNames', {'Probability'}, ...
                    'RowNames', {'Robot1', 'Robot2', 'Robot3'});
disp('Choice Probability Distribution:'); %,'Control1','Control2'
disp(result_table);
% Display DFT results with prediction
disp('DFT Results:');
disp(['E_P: ', num2str(E_P', '%.2f ')]);
disp(['Choice probabilities: ', num2str(probs', '%.3f ')]);
[~, predicted_choice] = max(probs); % Get index of highest probability
disp(['Predicted choice: Robot ', num2str(predicted_choice)]);
disp(['Actual choice: Robot ', num2str(choices(current_trial))]);
disp(' ');
% Display match/mismatch
if predicted_choice == choices(current_trial)
   disp(' \checkmark Prediction stayed the same');
else
   disp('X Prediction changed');
end
% Plot preference evolution
figure;
time_steps = 0:size(P_tau, 2)-1;
h = plot(time_steps, P_tau', 'LineWidth', 2);
legend(h, {'Robot 1', 'Robot 2', 'Robot 3'}, 'Location', 'best');
xlabel('Time Step (\tau)');
ylabel('Preference Strength');
title(sprintf('Preference Evolution (Trial %d)', current_trial));
```

```
grid on;
end
%{
%% Step 4: Solve Equilibrium Function
\% Ensure DFT outputs match expected dimensions
assert(length(E_P) == 5, 'DFT must return 5 alternatives');
assert(isequal(size(V_P), [5 5]), 'DFT covariance must be 5x5');
\ensuremath{\mathrm{W}} Use DFT outputs for equilibrium calculation
Ep_mins = E_P;
                    % 4×1 expected preferences from DFT
                     % 4×4 preference covariance from DFT
Varp_mins = V_P;
\% using robot attribute to map to product the robot can build type A vs
\ensuremath{\mathrm{W}} type B. this is made using each robot attribute.
\% 5 robot produce 2 things. each trial outputs x_mins as 10x1
x\_mins = robot\_production\_capacity(M); \ \ 10\times 1 \ robot \ state \ vector \ could \ recursive \ for \ each \ neighboring \ robot
% Call equilibrium solver
solutions = solve_equilibrium(Ep_mins, Varp_mins, x_mins);
% Extract solutions (works with both old and new versions)
if isfield(solutions, 'x')
    % Old version field names
    P_final = solutions.x;
    E_P_eq = solutions.lambda;
    V_P_eq = solutions.mu_vec;
else
    % New version field names
    P_final = solutions.P_final;
    E_P_eq = solutions.E_P_eq;
    V_P_eq = solutions.V_P_eq;
end
% Display results
disp('=== Equilibrium Results ===');
disp(['Final Preferences (P_final): ', num2str(P_final')]);
disp(['Expected Preferences (E_P_eq): ', num2str(E_P_eq')]);
disp(['Preference Variance (V_P_eq diagonal): ', num2str(V_P_eq')]);
%% Step 5: Output Results
disp('Saving results to CSV...');
output_table = table(E_P, V_P, P_final, ...
                       'VariableNames', {'ExpectedPreference', 'VariancePreference', 'FinalPreferences'});
writetable(output_table, 'results.csv');
disp('Results saved successfully!');
%}
=== Current Trial Analysis ===
Trial: 1
Participant: 1001
Actual Choice: Robot 2
M matrix (alternatives × attributes):
                                                           intelligence
               energy pace safety
                                            reliability
    Robot1
                0.65
                         0.55 0.7
                                                0.6
                                                                 0.58
                         0.45
                                                                 0.62
    Robot 2
               0.75
                                  0.8
                                               0.65
    Robot3
                0.5
                         0.6
                                  0.65
                                               0.55
                                                                  0.5
```

Choice Probability Distribution:

Probability

```
Robot1
               0.88477
   Robot2
              0.078084
   Robot3
              0.037147
DFT Results:
E_P: 1.84 -0.58 -1.33
Choice probabilities: 0.885 0.078 0.037
Predicted choice: Robot 1
Actual choice: Robot 2
X Prediction changed
=== Current Trial Analysis ===
Trial: 2
Participant: 1001
```

Actual Choice: Robot 1

M matrix (alternatives × attributes):

	energy	pace	safety	reliability	intelligence
				<del></del>	
Robot1	0.55	0.45	0.6	0.5	0.48
Robot2	0.7	0.35	0.75	0.6	0.57
Robot3	0.45	0.55	0.6	0.5	0.45

Choice Probability Distribution:

Probability

Robot1 0.040823 Robot2 0.43942 Robot3 0.51976

DFT Results:

E\_P: -1.62 0.76 0.93

Choice probabilities: 0.041 0.439 0.520

Predicted choice: Robot 3 Actual choice: Robot 1

X Prediction changed

=== Current Trial Analysis ===

Trial: 3

Participant: 1001 Actual Choice: Robot 3

M matrix (alternatives  $\times$  attributes):

	energy	pace	safety	reliability	intelligence
		—		<del></del>	
Robot1	0.6	0.5	0.65	0.55	0.53
Robot2	0.65	0.4	0.7	0.55	0.6
Robot3	0.55	0.65	0.7	0.6	0.55

Choice Probability Distribution:

Probability

Robot1 0.026676 Robot2 0.46883 Robot3 0.50449

DFT Results:

E\_P: -1.91 0.96 1.03

Choice probabilities: 0.027 0.469 0.504

Predicted choice: Robot 3 Actual choice: Robot 3

✓ Prediction stayed the same
=== Current Trial Analysis ===

Trial: 4

Participant: 1002 Actual Choice: Robot 2

M matrix (alternatives  $\times$  attributes):

	energy	pace	safety	reliability	intelligence
				<del></del>	
Robot1	0.7	0.6	0.75	0.65	0.63
Robot2	0.8	0.5	0.85	0.7	0.67
Robot3	0.6	0.7	0.75	0.65	0.6

Choice Probability Distribution:

Probability

Robot1 0.030265 Robot2 0.45697 Robot3 0.51276

DFT Results:

E\_P: -1.83 0.89 1.00

Choice probabilities: 0.030 0.457 0.513

Predicted choice: Robot 3 Actual choice: Robot 2

X Prediction changed
=== Current Trial Analysis ===

Trial: 5

Participant: 1002

Actual Choice: Robot 1

M matrix (alternatives  $\times$  attributes):

	energy	pace	safety	reliability	intelligence
				<del></del>	
Robot1	0.5	0.4	0.55	0.45	0.43
Robot2	0.6	0.3	0.65	0.5	0.52
Robot3	0.4	0.5	0.55	0.45	0.4

Choice Probability Distribution:

Probability

Robot1 0.023216 Robot2 0.45813 Robot3 0.51866

DFT Results:

E\_P: -2.00 0.98 1.10

Choice probabilities: 0.023 0.458 0.519

Predicted choice: Robot 3 Actual choice: Robot 1

X Prediction changed

=== Current Trial Analysis ===

Trial: 6

Participant: 1002 Actual Choice: Robot 3

M matrix (alternatives × attributes):

			, -		
	energy	pace	safety	reliability	intelligence
Robot1	0.75	0.65	0.8	0.7	0.68
Robot2	0.85	0.55	0.9	0.75	0.73
Robot3	0.65	0.75	0.8	0.7	0.65

Choice Probability Distribution:

Probability

Robot1 0.027882 Robot2 0.45788 Robot3 0.51424

DFT Results:

E\_P: -1.88 0.92 1.03

Choice probabilities: 0.028 0.458 0.514

Predicted choice: Robot 3 Actual choice: Robot 3

✓ Prediction stayed the same
=== Current Trial Analysis ===

Trial: 7

Participant: 1003 Actual Choice: Robot 2

M matrix (alternatives × attributes):

	energy	pace	safety	reliability	intelligence
		—		<del></del>	
Robot1	0.58	0.48	0.63	0.53	0.51
Robot2	0.68	0.38	0.73	0.58	0.61
Robot3	0.48	0.58	0.63	0.53	0.48

Choice Probability Distribution:

Probability

Robot1 0.02297 Robot2 0.45758 Robot3 0.51945

DFT Results:

E\_P: -2.01 0.98 1.11

Choice probabilities: 0.023 0.458 0.519

Predicted choice: Robot 3 Actual choice: Robot 2  ${\sf X}$  Prediction changed

=== Current Trial Analysis ===

Trial: 8

Participant: 1003 Actual Choice: Robot 1

M matrix (alternatives × attributes):

	energy	pace	safety	reliability	intelligence
		—			-
Robot1	0.62	0.52	0.67	0.57	0.55
Robot2	0.72	0.42	0.77	0.62	0.65
Robot3	0.52	0.62	0.67	0.57	0.52

Choice Probability Distribution:

Probability

Robot1 0.02297 Robot2 0.45758 Robot3 0.51945

DFT Results:

E\_P: -2.01 0.98 1.11

Choice probabilities: 0.023 0.458 0.519

Predicted choice: Robot 3 Actual choice: Robot 1

X Prediction changed

=== Current Trial Analysis ===

Trial: 9

Participant: 1003 Actual Choice: Robot 3

M matrix (alternatives  $\times$  attributes):

energy pace safety reliability intelli	gence
Robot1 0.67 0.57 0.72 0.62 0.	6
Robot2 0.77 0.47 0.82 0.67 0.	7
Robot3 0.57 0.67 0.72 0.62 0.5	7

Choice Probability Distribution:

Probability

Robot1 0.02297 Robot2 0.45758 Robot3 0.51945

DFT Results:

E\_P: -2.01 0.98 1.11

Choice probabilities: 0.023 0.458 0.519

Predicted choice: Robot 3 Actual choice: Robot 3

 $\checkmark$  Prediction stayed the same === Current Trial Analysis ===

Trial: 10

Participant: 1004 Actual Choice: Robot 2

M matrix (alternatives × attributes):

	energy	pace	safety	reliability	intelligence
Robot1	0.53	0.43	0.58	0.48	0.46
Robot2	0.63	0.33	0.68	0.53	0.56
Robot3	0.43	0.53	0.58	0.48	0.43

Choice Probability Distribution:

Probability

Robot1 0.02297 Robot2 0.45758 Robot3 0.51945

DFT Results:

E\_P: -2.01 0.98 1.11

Choice probabilities: 0.023 0.458 0.519

Predicted choice: Robot 3

```
Actual choice: Robot 2

X Prediction changed
```

## **Helper Functions**

```
function param = validateParam(params, name, default)
    if isfield(params, name) && isnumeric(params.(name))
        param = params.(name);
    else
        warning('Using default for %s', name);
        param = default;
    end
end

function [phi1, phi2, tau, error_sd] = getFallbackParams()
    phi1 = 0.5;
    phi2 = 0.8;
    tau = 10;
    error_sd = 0.1;
    warning('Using default parameters');
end
```

```
Estimated Parameters:
phi1: 32.7954
phi2: 0.1601
tau: 22027.4658
error_sd: 1
Initial Preferences (from ASCs):
-24.2300 -11.8930 0
```

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