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☆ Key Points

training set.

You can only construct

probabilities for vectors whose

exact combination of features

have already been "seen" in the

Directly estimating a Binomial or

Bernoulli distribution with MLE is

only useful if there are many

training inputs with feature

vectors identical to a test input.













Course Shortcuts

> Student Lounge

> Q&A

> Estimating Distributions from Data

 Classification with the Naive **Bayes Algorithm**

- Module Introduction: Classification with the Naive Bayes Algorithm
- Limitations of High Dimensional Space in MLE

MLE Curse of Dimensionality

- Formalize the Curse of Dimensionality
- <u>Capturing All Possibilities</u> in d Dimensions
- Naive Bayes Assumption
- Data Sets Where the Naive **Bayes Assumption Holds**
- Naive Bayes Classifier
- <u>Derivation of Naive Bayes</u> Classifier
- Naive Bayes Cheat Sheet
- <u>Determine Probability</u> With Categorical Naive <u>Bayes</u>
- <u>Categorical Naive Bayes</u> Classifiers
- Naive Bayes in Action
- Module Wrap-up: Classification with the Naive Bayes Algorithm
- > Building a Baby Name **Classifying System**
- Course Resources

Estimating Probability Distributions >

MLE Curse of Dimensionality

In the previous module, you saw that MLE can be used to estimate the parameters of a distribution from a data set. For the binomial distribution you can directly estimate the labels given an input. However, there is a major problem with this approach on highly dimensional data sets: the more dimensions in your data set, the less likely it becomes that any two feature vectors will match exactly. You can only construct probabilities for vectors whose exact combination of features have already been "seen" in the training set.

Spam Email Example

Let's suppose you are trying to build an email classifier. For the initial implementation of this email classifier, you'll use a very simple set of three features:

- 1. Does the email contain the word "bacon"?
- 2. Does the email come from a recognized IP address?
- 3. Does the email contain any misspelled words?

Suppose the (very-limited) training data set looks like this, where each id is an email, 0 represents "no", 1 represents "yes", and the

label tells us if the email is spam or not.					
	ID	Contains word "bacon"	Recognized IP	Misspelled words	Label
	1	О	0	1	spam
	2	0	0	1	spam
	3	1	0	0	spam
	4	0	0	1	spam
	5	1	0	1	spam
	6	1	1	1	spam
	7	0	0	1	spam
	8	0	0	1	spam
	9	1	0	1	spam
	10	0	0	1	spam
	11	0	1	0	not spam
	12	0	1	1	not spam
	13	1	1	1	not spam
	14	0	1	1	not spam

What would be the most likely label for an email whose feature vector is (0,0,0) based on a Bernoulli distribution fit with MLE on the given data?

Spam

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✓ Undefined

Not spam

Correct! There is no exact match for this feature vector in our data.

0





not spam