

$$b) L_2 = \{ 0^i 1^j \mid i > j \}$$

Let  $L_2$  be ~~se~~ regular

$\therefore L_2$  satisfies pumping property

Let  $k$  be pumping constant

$$s = 0^{k+1} 1^k \quad |s| = 2k+1 > k$$

$$s = uvw, \quad u = \text{empty}$$

$$v = 0^m \quad m \geq 1, \quad m \leq k$$

$$w = 0^{k+1-m} 1^k$$

$$uv^i w = 0^{im} 0^{k+1-m} 1^k$$

$$= 0^{k+1+(i-1)m} 1^k$$

for  $i = 0$ , it becomes  $0^{k+1-m} 1^k$

$m \geq 1, \therefore k+1-m \leq k$

$$uv^0 w \notin L_2$$

pumping property is not satisfied

$\therefore L_2$  is not regular



d)

$$L_4 = \{ (10)^p 1^q \mid p \geq q \}$$

Let  $L_4$  be regular

$\therefore L_4$  satisfies pumping property

Let  $k$  be pumping constant

$$S = (10)^k 1^k \quad |S| = 3k > k$$

$$S = uvw, \quad u = \text{empty}$$

$$v = 10$$

$$w = (10)^{k-1} 1^k$$

$$uv^i w = (10)^i (10)^{k-1} 1^k$$

$$= (10)^{k+i-1} 1^k$$

$$\text{At } i=0,$$

$$uv^0 w = (10)^{k-1} 1^k$$

$$k-1 < k, \therefore uv^0 w \notin L_4$$

$\therefore$  Pumping property not satisfied

$\therefore L_4$  is not regular