

Mid Semester Exam

Name: Ananab Sen

Subject: Theory of Computation

Code: CS2204

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En.no: 510519006

Guide: 510519006.ananab @ iis students. iisr.ac.in

(1)

(b) FALSE

Regular languages are context free but the opposite is not true i.e. all context free are not regular.

For RG, $G = (V, \Sigma, R, \emptyset)$ $R \subseteq (V - \Sigma) \times (\Sigma^* \cdot (V - \Sigma) \cup \{e\})$
 $R \subseteq (V - \Sigma) \times (\Sigma^* \cdot (V - \Sigma) \cup \{e\})$

For Context free grammar

$G = (V, \Sigma, R, \emptyset)$

$R \subseteq (V - \Sigma) \times V^*$

(a) TRUE

~~if fin~~
we can consider a finite language L over an alphabet Σ as a finite set of strings. It contains the symbols of Σ .

But, we can also say that those strings are symbols for some other language alphabet Σ' and hence L can be alphabet of some other language. Hence we can conclude that any finite language L over an alphabet Σ can itself be the alphabet for some other language L' thus TRUE

(c) TRUE

We know ϕ is a regular language over Σ

Also if $a \in \Sigma$, then a

and $a \in \Sigma$.

Since regular language is closed under Kleene star we can also say the $\{a\}^* \in \{a\}^*$

hence the statement both ϕ and $\{a\}^*$ are regular languages over the alphabet $\{a, b\}$.

(2) (a) $\{ a^m b^n c^l \mid l, m, n \geq 0 \text{ and } m \leq l + n \}$.

m	l	n	equiv string
0	0	0	e
0	0	1	b
1	2	2	abbe abbbcc
0	1	1	bc
1	1	1	
1	1	1	

rules

$S_1 \rightarrow S_1 c$
 $S_1 \rightarrow a S_1 c$
 $S_1 \rightarrow S_2$
 $S_2 \rightarrow S_2 b$
 $S_2 \rightarrow a S_2 b$
 $S_1 \rightarrow e$
 $S_2 \rightarrow e$

$G = (V, \Sigma, R, S)$

where $V = \{ S_1, c, a, S_2, b \}$

$\Sigma = \{ a, b, c \}$

$R = \{ S_1 \rightarrow S_1 c, S_1 \rightarrow a S_1 c, S_1 \rightarrow S_2, S_2 \rightarrow S_2 b, S_2 \rightarrow a S_2 b, S_1 \rightarrow e, S_2 \rightarrow e \}$

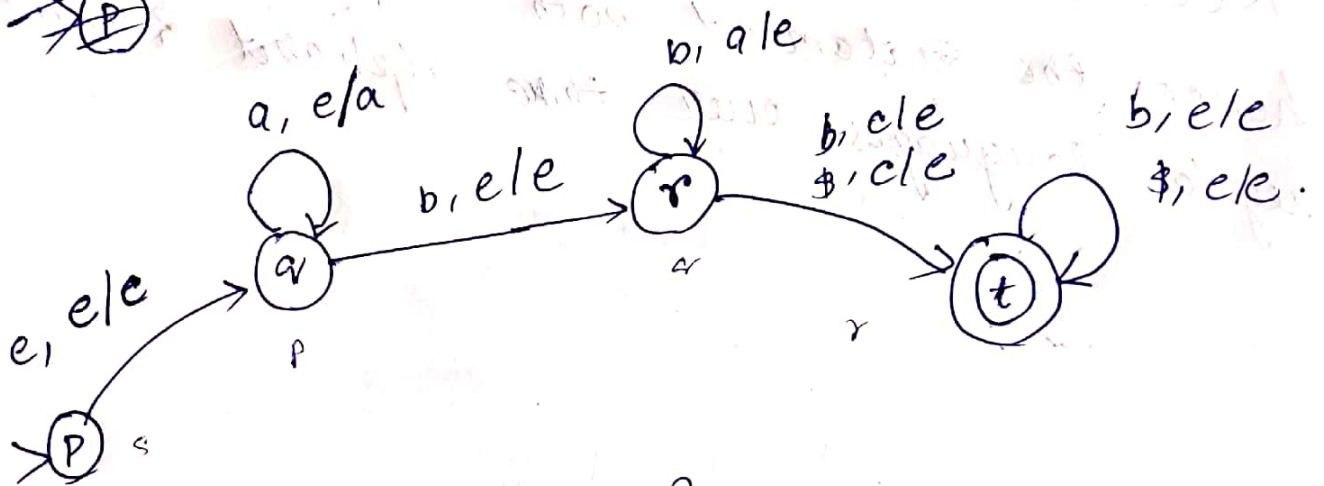
$S = S_1$

(2)

(b)

$\{a^m b^n \mid m, n \geq 0 \text{ and } m \neq n\}$

~~(P)~~



$K = \{p, q, r, t\}$

$\Sigma = \{a, b\}$

$\Gamma = \{a, e\}$

$s = p$

$F = t$

(2)

(c)

$$G = (V, \Sigma, R, S)$$

$$V = \{S, A, B, a, b\}$$

$$\Sigma = \{a, b\}$$

$$S = S$$

$$R = \{$$

$$S \rightarrow Aa,$$

$$A \rightarrow aA,$$

$$A \rightarrow e,$$

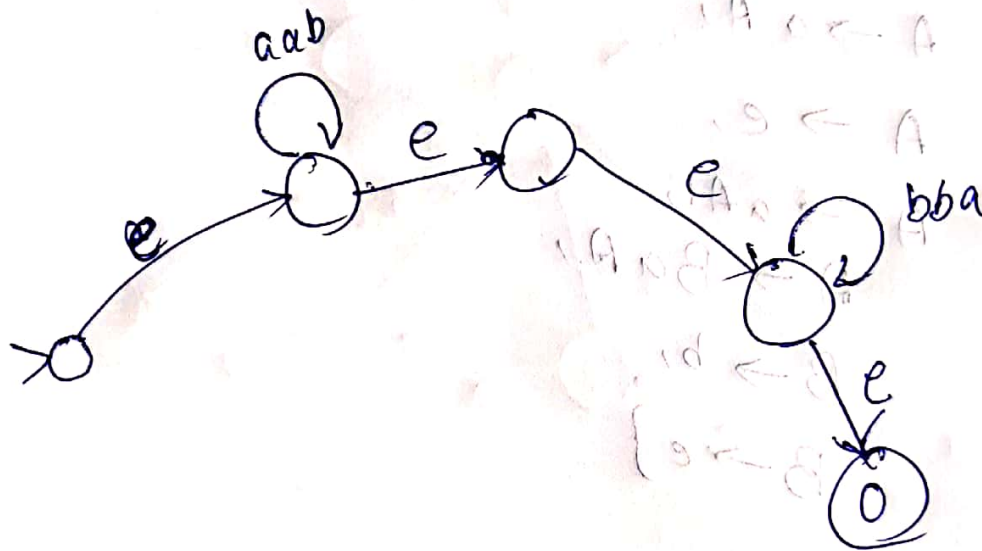
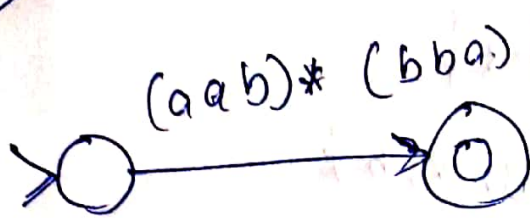
$$A \rightarrow aAB,$$

$$A \rightarrow BaA,$$

$$B \rightarrow b,$$

$$B \rightarrow e\}$$

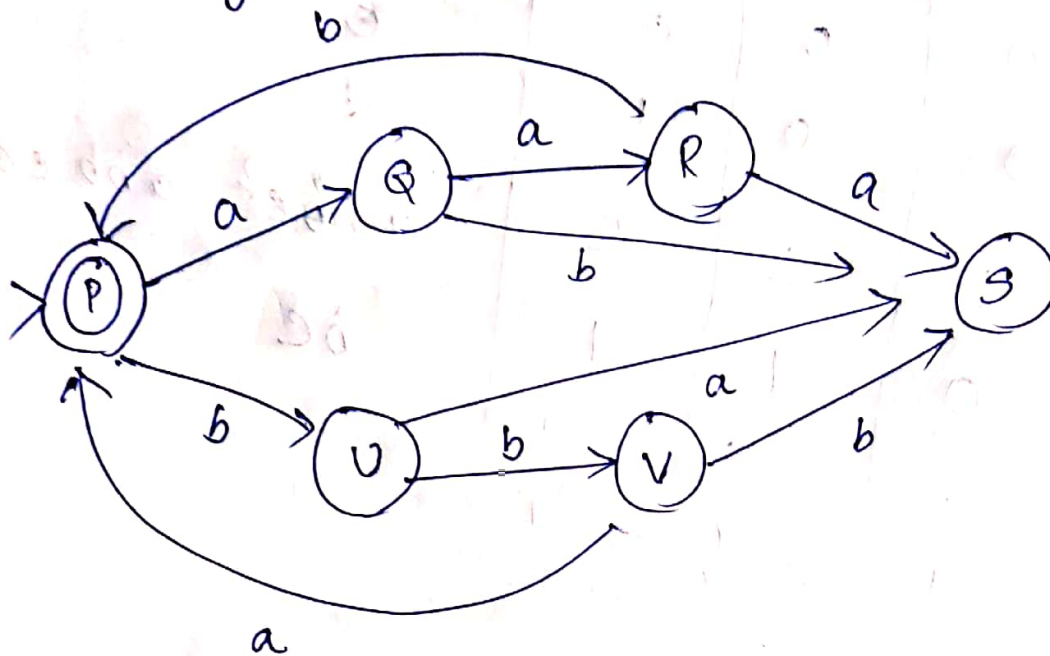
4 a)



then
we can construct the DFA

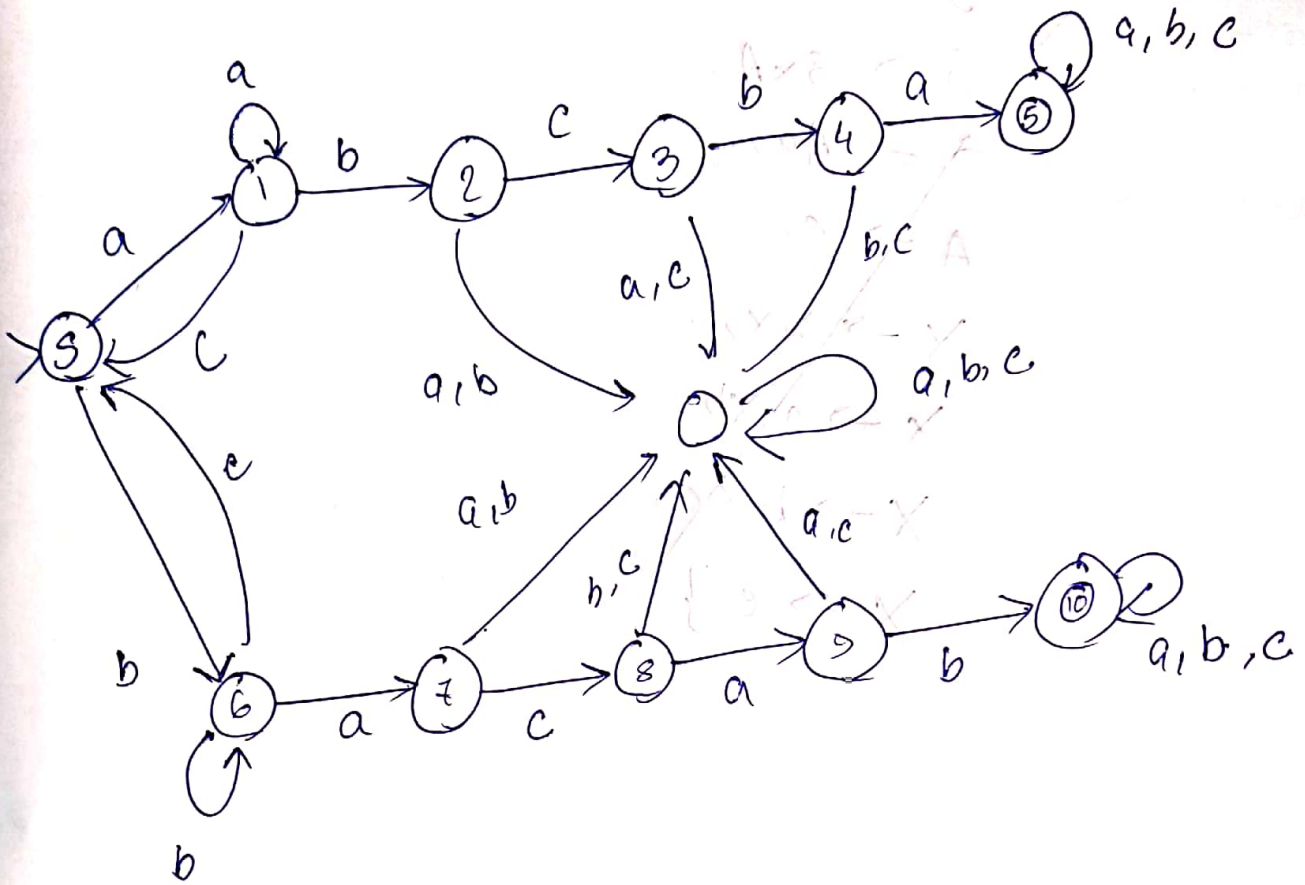
Q.4 contd

The language $L \subseteq \{a, b\}^*$ represented by the regular expression



The DFA of the language $L \subseteq \{a, b\}^*$

(4)
(6)



$$M = (K, \Sigma, \delta, s, F)$$

$$s = 0$$

$$F = \{5, 10\}$$

$$K = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$$

$$\Sigma = \{a, b, c\}$$

$\delta \rightarrow$ as drawn above