

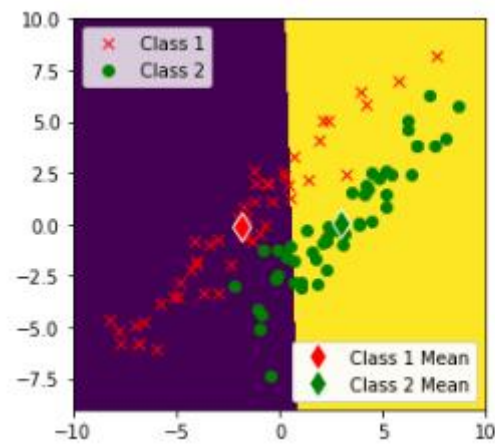
**EE-559-MATHEMATICAL PATTERN RECOGNITION**  
**HOMEWORK-1-WRITTEN REPORT**

*Rakshitha Panduranga*

*USC ID-7890-1614-34*

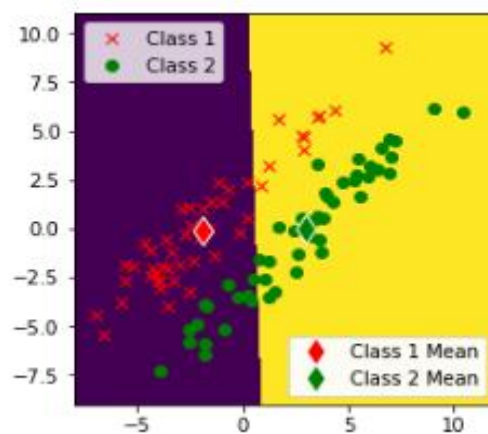
*Email-rpandura@usc.edu*

1. a)



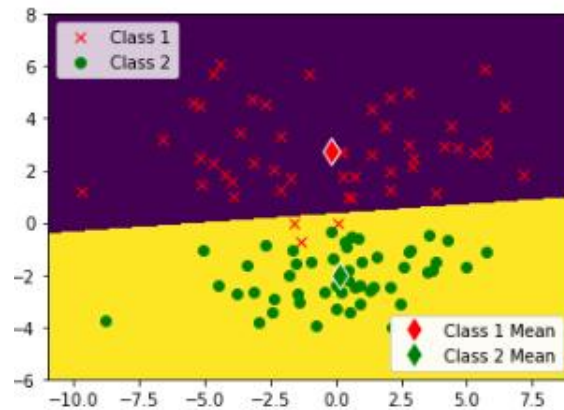
*Fig 1. Plot of Synthetic1 Training-set along with Class Means, Decision Boundaries and Decision Regions*

The error rate for Synthetic 1 Training data set is 21.0  
The success rate for Synthetic 1 Training data set is 79.0



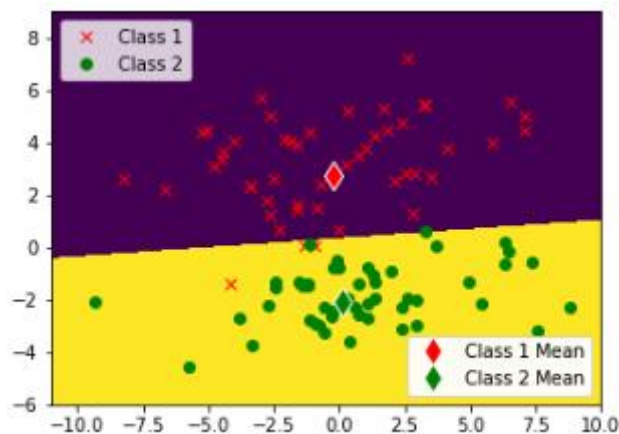
*Fig 2. Plot of Synthetic1 Testing-set along with Class Means, Decision Boundaries and Decision Regions*

The error rate for Synthetic 1 Testing data set is 24.0  
The success rate for Synthetic 1 Testing data set is 76.0



*Fig 3. Plot of Synthetic2 Training-set along with Class Means, Decision Boundaries and Decision Regions*

The error rate for Synthetic 2 Training data set is 3.0  
The success rate for Synthetic 2 Training data set is 97.0



*Fig 4. Plot of Synthetic2 Testing-set along with Class Means, Decision Boundaries and Decision Regions*

The error rate for Synthetic 2 Testing data set is 4.0  
The success rate for Synthetic 2 Testing data set is 96.0

**1. b) Yes, there is a significant change in the error rates.**

Training set difference - 17%

Testing set difference - 20%

This change in the error rates is because-

- In Synthetic dataset 1 the distance measure between data points and sample mean is more compared to the distance measure between the data points and sample mean of Synthetic data set 2.

Due to which, there is a huge dissimilarity between the data points and the mean which in turn makes the training of the Synthetic data set 1 harder than the Synthetic dataset 2.

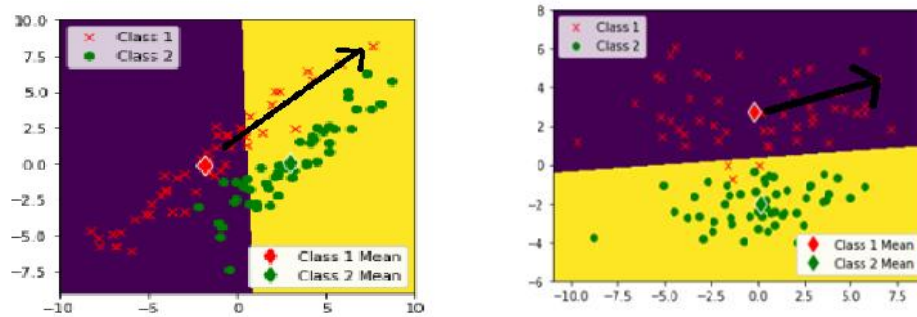


Fig 5. Plots of Synthetic1 Training-set and Synthetic2 Training set comparing their distance measures of the last data point from their respective sample means

1. c) For the Wine dataset with total  $C = 3$  Classes and picking the first two features  $\rightarrow$  x1 - Alcohol Content

x2-Malic Acid Content

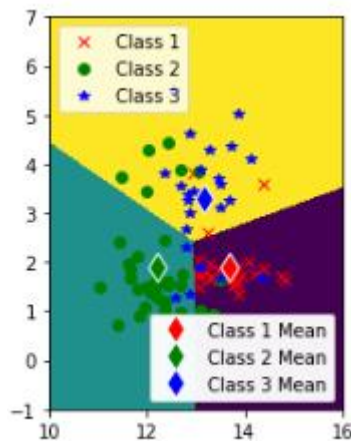
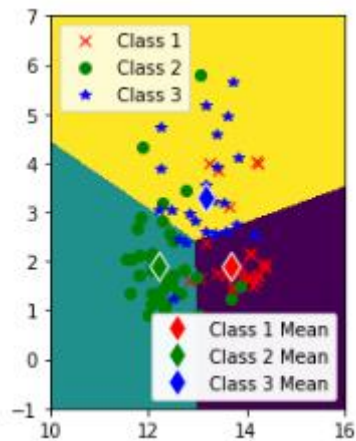


Fig 6. Plot of Wine Training-set along with Class Means, Decision Boundaries and Decision Regions for first two features

The error rate for Wine Training data set is 20.224719101123593

The success rate for Wine Training data set is 79.7752808988764



*Fig 7. Plot of Wine Testing-set along with Class Means, Decision Boundaries and Decision Regions for first two features*

**The error rate for Wine Testing data set is 22.47191011235955**

**The success rate for Wine Testing data set is 77.52808988764045**

### **1.e)**

*For the Wine dataset, taking all the combinations of features, the respective error rates and success rates are-*

The error rate of f1 = 1	f2 = 2	of Wine Training data set is	20.224719101123593
The error rate of f1 = 1	f2 = 2	of Wine Testing data set is	22.47191011235955
The error rate of f1 = 1	f2 = 3	of Wine Training data set is	31.46067415730337
The error rate of f1 = 1	f2 = 3	of Wine Testing data set is	28.08988764044944
The error rate of f1 = 1	f2 = 4	of Wine Training data set is	44.9438202247191
The error rate of f1 = 1	f2 = 4	of Wine Testing data set is	40.44943820224719
The error rate of f1 = 1	f2 = 5	of Wine Training data set is	56.17977528089888
The error rate of f1 = 1	f2 = 5	of Wine Testing data set is	44.9438202247191
The error rate of f1 = 1	f2 = 6	of Wine Training data set is	14.606741573033707
The error rate of f1 = 1	f2 = 6	of Wine Testing data set is	15.730337078651685
The error rate of f1 = 1	f2 = 7	of Wine Training data set is	8.98876404494382
The error rate of f1 = 1	f2 = 7	of Wine Testing data set is	11.235955056179774

The error rate of f1 = 1 f2 = 8 of Wine Training data set is 33.70786516853933

The error rate of f1 = 1 f2 = 8 of Wine Testing data set is 28.08988764044944

The error rate of f1 = 1 f2 = 9 of Wine Training data set is 16.853932584269664

The error rate of f1 = 1 f2 = 9 of Wine Testing data set is 24.719101123595504

The error rate of f1 = 1 f2 = 10 of Wine Training data set is 25.842696629213485

The error rate of f1 = 1 f2 = 10 of Wine Testing data set is 22.47191011235955

The error rate of f1 = 1 f2 = 11 of Wine Training data set is 25.842696629213485

The error rate of f1 = 1 f2 = 11 of Wine Testing data set is 26.96629213483146

**The error rate of f1 = 1 f2 = 12 of Wine Training data set is 7.865168539325842**

**The error rate of f1 = 1 f2 = 12 of Wine Testing data set is 12.359550561797752**

The error rate of f1 = 1 f2 = 13 of Wine Training data set is 24.719101123595504

The error rate of f1 = 1 f2 = 13 of Wine Testing data set is 30.337078651685395

The error rate of f1 = 2 f2 = 3 of Wine Training data set is 39.325842696629216

The error rate of f1 = 2 f2 = 3 of Wine Testing data set is 38.20224719101123

The error rate of f1 = 2 f2 = 4 of Wine Training data set is 39.325842696629216

The error rate of f1 = 2 f2 = 4 of Wine Testing data set is 42.69662921348314

The error rate of f1 = 2 f2 = 5 of Wine Training data set is 57.30337078651685

The error rate of f1 = 2 f2 = 5 of Wine Testing data set is 43.82022471910113

The error rate of f1 = 2 f2 = 6 of Wine Training data set is 29.213483146067414

The error rate of f1 = 2 f2 = 6 of Wine Testing data set is 29.213483146067414

The error rate of f1 = 2 f2 = 7 of Wine Training data set is 20.224719101123593

The error rate of f1 = 2 f2 = 7 of Wine Testing data set is 23.595505617977526

The error rate of f1 = 2 f2 = 8 of Wine Training data set is 32.58426966292135

The error rate of f1 = 2 f2 = 8 of Wine Testing data set is 39.32584269  
6629216

The error rate of f1 = 2 f2 = 9 of Wine Training data set is 40.4494382  
0224719

The error rate of f1 = 2 f2 = 9 of Wine Testing data set is 37.07865168  
539326

The error rate of f1 = 2 f2 = 10 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 2 f2 = 10 of Wine Testing data set is 22.4719101  
1235955

The error rate of f1 = 2 f2 = 11 of Wine Training data set is 38.202247  
19101123

The error rate of f1 = 2 f2 = 11 of Wine Testing data set is 44.9438202  
247191

The error rate of f1 = 2 f2 = 12 of Wine Training data set is 42.696629  
21348314

The error rate of f1 = 2 f2 = 12 of Wine Testing data set is 37.0786516  
8539326

The error rate of f1 = 2 f2 = 13 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 2 f2 = 13 of Wine Testing data set is 30.3370786  
51685395

The error rate of f1 = 3 f2 = 4 of Wine Training data set is 47.1910112  
3595505

The error rate of f1 = 3 f2 = 4 of Wine Testing data set is 50.56179775  
280899

The error rate of f1 = 3 f2 = 5 of Wine Training data set is 57.3033707  
8651685

The error rate of f1 = 3 f2 = 5 of Wine Testing data set is 46.06741573  
033708

The error rate of f1 = 3 f2 = 6 of Wine Training data set is 32.5842696  
6292135

The error rate of f1 = 3 f2 = 6 of Wine Testing data set is 28.08988764  
044944

The error rate of f1 = 3 f2 = 7 of Wine Training data set is 14.6067415  
73033707

The error rate of f1 = 3 f2 = 7 of Wine Testing data set is 22.47191011  
235955

The error rate of f1 = 3 f2 = 8 of Wine Training data set is 51.6853932  
5842697

The error rate of f1 = 3 f2 = 8 of Wine Testing data set is 32.58426966  
292135

The error rate of f1 = 3 f2 = 9 of Wine Training data set is 38.2022471  
9101123

The error rate of f1 = 3 f2 = 9 of Wine Testing data set is 40.44943820  
224719

The error rate of f1 = 3 f2 = 10 of Wine Training data set is 30.337078  
651685395

The error rate of f1 = 3 f2 = 10 of Wine Testing data set is 23.5955056  
17977526

The error rate of f1 = 3 f2 = 11 of Wine Training data set is 30.337078  
651685395

The error rate of f1 = 3 f2 = 11 of Wine Testing data set is 26.9662921  
3483146

The error rate of f1 = 3 f2 = 12 of Wine Training data set is 29.213483  
146067414

The error rate of f1 = 3 f2 = 12 of Wine Testing data set is 28.0898876  
4044944

The error rate of f1 = 3 f2 = 13 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 3 f2 = 13 of Wine Testing data set is 30.3370786  
51685395

The error rate of f1 = 4 f2 = 5 of Wine Training data set is 42.6966292  
1348314

The error rate of f1 = 4 f2 = 5 of Wine Testing data set is 38.20224719  
101123

The error rate of f1 = 4 f2 = 6 of Wine Training data set is 47.1910112  
3595505

The error rate of f1 = 4 f2 = 6 of Wine Testing data set is 47.19101123  
595505

The error rate of f1 = 4 f2 = 7 of Wine Training data set is 42.6966292  
1348314

The error rate of f1 = 4 f2 = 7 of Wine Testing data set is 41.57303370  
786517

The error rate of f1 = 4 f2 = 8 of Wine Training data set is 47.1910112  
3595505

The error rate of f1 = 4 f2 = 8 of Wine Testing data set is 50.56179775  
280899

The error rate of f1 = 4 f2 = 9 of Wine Training data set is 44.9438202  
247191

The error rate of f1 = 4 f2 = 9 of Wine Testing data set is 48.31460674  
157304

The error rate of f1 = 4 f2 = 10 of Wine Training data set is 21.348314  
60674157

The error rate of f1 = 4 f2 = 10 of Wine Testing data set is 29.2134831  
46067414

The error rate of f1 = 4 f2 = 11 of Wine Training data set is 47.191011  
23595505

The error rate of f1 = 4 f2 = 11 of Wine Testing data set is 50.5617977  
5280899

The error rate of f1 = 4 f2 = 12 of Wine Training data set is 43.820224  
71910113



The error rate of f1 = 4 f2 = 12 of Wine Testing data set is 44.9438202  
247191

The error rate of f1 = 4 f2 = 13 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 4 f2 = 13 of Wine Testing data set is 30.3370786  
51685395

The error rate of f1 = 5 f2 = 6 of Wine Training data set is 56.1797752  
8089888

The error rate of f1 = 5 f2 = 6 of Wine Testing data set is 44.94382022  
47191

The error rate of f1 = 5 f2 = 7 of Wine Training data set is 56.1797752  
8089888

The error rate of f1 = 5 f2 = 7 of Wine Testing data set is 41.57303370  
786517

The error rate of f1 = 5 f2 = 8 of Wine Training data set is 57.3033707  
8651685

The error rate of f1 = 5 f2 = 8 of Wine Testing data set is 46.06741573  
033708

The error rate of f1 = 5 f2 = 9 of Wine Training data set is 56.1797752  
8089888

The error rate of f1 = 5 f2 = 9 of Wine Testing data set is 44.94382022  
47191

The error rate of f1 = 5 f2 = 10 of Wine Training data set is 49.438202  
24719101

The error rate of f1 = 5 f2 = 10 of Wine Testing data set is 43.8202247  
1910113

The error rate of f1 = 5 f2 = 11 of Wine Training data set is 57.303370  
78651685

The error rate of f1 = 5 f2 = 11 of Wine Testing data set is 46.0674157  
3033708

The error rate of f1 = 5 f2 = 12 of Wine Training data set is 56.179775  
28089888

The error rate of f1 = 5 f2 = 12 of Wine Testing data set is 43.8202247  
1910113

The error rate of f1 = 5 f2 = 13 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 5 f2 = 13 of Wine Testing data set is 30.3370786  
51685395

The error rate of f1 = 6 f2 = 7 of Wine Training data set is 22.4719101  
1235955

The error rate of f1 = 6 f2 = 7 of Wine Testing data set is 24.71910112  
3595504

The error rate of f1 = 6 f2 = 8 of Wine Training data set is 34.8314606  
74157306

The error rate of f1 = 6 f2 = 8 of Wine Testing data set is 35.95505617  
977528

The error rate of f1 = 6 f2 = 9 of Wine Training data set is 40.4494382  
0224719

The error rate of f1 = 6 f2 = 9 of Wine Testing data set is 32.58426966  
292135

The error rate of f1 = 6 f2 = 10 of Wine Training data set is 28.089887  
64044944

The error rate of f1 = 6 f2 = 10 of Wine Testing data set is 22.4719101  
1235955

The error rate of f1 = 6 f2 = 11 of Wine Training data set is 32.584269  
66292135

The error rate of f1 = 6 f2 = 11 of Wine Testing data set is 28.0898876  
4044944

The error rate of f1 = 6 f2 = 12 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 6 f2 = 12 of Wine Testing data set is 25.8426966  
29213485

The error rate of f1 = 6 f2 = 13 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 6 f2 = 13 of Wine Testing data set is 30.3370786  
51685395

The error rate of f1 = 7 f2 = 8 of Wine Training data set is 16.8539325  
84269664

The error rate of f1 = 7 f2 = 8 of Wine Testing data set is 24.71910112  
3595504

The error rate of f1 = 7 f2 = 9 of Wine Training data set is 16.8539325  
84269664

The error rate of f1 = 7 f2 = 9 of Wine Testing data set is 26.96629213  
483146

The error rate of f1 = 7 f2 = 10 of Wine Training data set is 21.348314  
60674157

The error rate of f1 = 7 f2 = 10 of Wine Testing data set is 15.7303370  
78651685

The error rate of f1 = 7 f2 = 11 of Wine Training data set is 15.730337  
078651685

The error rate of f1 = 7 f2 = 11 of Wine Testing data set is 24.7191011  
23595504

The error rate of f1 = 7 f2 = 12 of Wine Training data set is 13.483146  
06741573

The error rate of f1 = 7 f2 = 12 of Wine Testing data set is 17.9775280  
8988764

The error rate of f1 = 7 f2 = 13 of Wine Training data set is 24.719101  
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The error rate of f1 = 7 f2 = 13 of Wine Testing data set is 30.3370786  
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The error rate of f1 = 8 f2 = 9 of Wine Training data set is 42.6966292  
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The error rate of f1 = 8 f2 = 9 of Wine Testing data set is 47.19101123  
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The error rate of f1 = 8 f2 = 10 of Wine Training data set is 30.337078  
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The error rate of f1 = 8 f2 = 10 of Wine Testing data set is 23.5955056  
17977526

The error rate of f1 = 8 f2 = 11 of Wine Training data set is 33.707865  
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The error rate of f1 = 8 f2 = 11 of Wine Testing data set is 34.8314606  
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The error rate of f1 = 8 f2 = 12 of Wine Training data set is 40.449438  
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The error rate of f1 = 8 f2 = 12 of Wine Testing data set is 32.5842696  
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The error rate of f1 = 9 f2 = 10 of Wine Training data set is 30.337078  
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The error rate of f1 = 9 f2 = 11 of Wine Training data set is 37.078651  
68539326

The error rate of f1 = 9 f2 = 11 of Wine Testing data set is 39.3258426  
96629216

The error rate of f1 = 9 f2 = 12 of Wine Training data set is 34.831460  
674157306

The error rate of f1 = 9 f2 = 12 of Wine Testing data set is 31.4606741  
5730337

The error rate of f1 = 9 f2 = 13 of Wine Training data set is 24.719101  
123595504

The error rate of f1 = 9 f2 = 13 of Wine Testing data set is 30.3370786  
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The error rate of f1 = 10 f2 = 11 of Wine Training data set is 30.33707  
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The error rate of f1 = 10 f2 = 11 of Wine Testing data set is 23.595505  
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The error rate of f1 = 10 f2 = 12 of Wine Testing data set is 22.471910  
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The error rate of f1 = 10 f2 = 13 of Wine Training data set is 24.71910  
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The error rate of f1 = 11 f2 = 12 of Wine Testing data set is 32.58426966292135

The error rate of f1 = 11 f2 = 13 of Wine Training data set is 24.719101123595504

The error rate of f1 = 11 f2 = 13 of Wine Testing data set is 30.337078651685395

The error rate of f1 = 12 f2 = 13 of Wine Training data set is 24.719101123595504

The error rate of f1 = 12 f2 = 13 of Wine Testing data set is 30.337078651685395

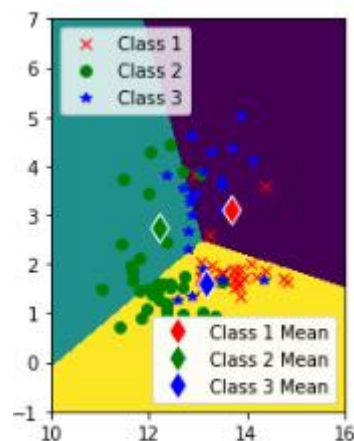
**Yes, there is a significant difference in the error rates. Because-**

- Each pair of features differentiates the data into three classes uniquely.

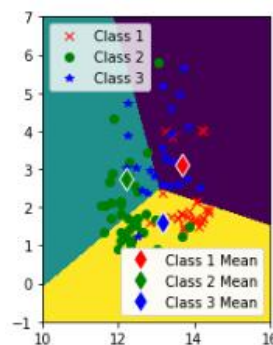
**But, the data can be easily and best differentiated with Feature 1 and Feature 12.**

### 1.d)

As seen in 1.e), the error rates are minimum for Feature 1 and Feature 12.



*Fig 6. Plot of Wine Training-set along with Class Means, Decision Boundaries and Decision Regions for best two features*



*Fig 6. Plot of Wine Testing-set along with Class Means, Decision Boundaries and Decision Regions for best two features*

