

Fundamental limits on the rate of bacterial cell division

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Abstract This will be written next (promise).

Synthesis of the Cell Envelope

The subjects of our estimates thus far have been localized to the periphery of the cell, embedded within the hydrophobic lipid bilayer of the inner membrane. As outlined in ??, cells could in principle increase the expression of the membrane-bound ATP synthases and electron transport chains to support a larger energy budget across a wide range of cell volumes and membrane surface areas. This ability, however, is contingent on the ability of the cell to expand the surface area of the cell by synthesizing new lipids and peptidoglycan for the cell wall. In this next class of estimates, we will turn our focus to these processes and consider the copy numbers of the relevant enzymes.

Lipid Synthesis

The cell envelopes of gram negative bacteria (such as *E. coli*) are composed of inner and outer phospholipid bilayer membranes separated by a ≈ 10 nm periplasmic space (BNID: 100016, *Milo et al. (2010)*). As mentioned in our discussion of the surface area to volume constraints on energy production, *E. coli* is a rod-shaped bacterium with a 4:1 length-to-width aspect ratio. At modest growth rates, such as our stopwatch of 5000 s, the total cell surface area is $\approx 5 \mu\text{m}^2$ (BNID: 101792, *Milo et al. (2010)*). As there are two membranes, each of which composed of two lipid leaflets, the total membrane area is $\approx 20 \mu\text{m}^2$, a remarkable value compared to the $\approx 2 \mu\text{m}$ length of the cell.

While this represents the total area of the membrane, this does not mean that it is composed entirely of lipid molecules. Rather, the dense packing of the membrane with proteins means that only ≈ 40 % of the membrane area is occupied by lipids (BNID: 100078, *Milo et al. (2010)*). Using a rule-of-thumb of 0.5 nm^2 as the surface area of the typical lipid (BNID: 106993, *Milo et al. (2010)*), we arrive at an estimate of $\approx 2 \times 10^7$ lipids per cell, an estimate in close agreement with experimental measurements (BNID: 100071, 102996; *Milo et al. (2010)*).

The membranes of *E. coli* are composed of a variety of different lipids, each of which are unique in their structures and biosynthetic pathways (*Sohlenkamp and Geiger, 2016*). With such diversity

in biosynthesis, it becomes difficult to identify which step(s) may be the rate-limiting, an objective further complicated by the sparsity of *in vivo* kinetic data. Recently, a combination of stochastic kinetic modeling (Ruppe and Fox, 2018) and *in vitro* kinetic measurements (Ranganathan et al., 2012; Yu et al., 2011) have revealed remarkably slow steps in the fatty acid synthesis pathways which may serve as the rate limiting reactions. One such step is the removal of hydroxyl groups from the fatty-acid chain by ACP dehydratase that leads to the formation of carbon-carbon double bonds. This reaction, catalyzed by proteins FabZ and FabA in *E. coli* (Yu et al., 2011), have been estimated to have kinetic turnover rates of ≈ 1 dehydration per second per enzyme (Ruppe and Fox, 2018). Combined with this rate, our previous estimates for the number of lipids to be formed, and a 5000 second division yields an estimate that the cell requires ≈ 4000 ACP dehydratases. This is in reasonable agreement with the experimentally observed copy numbers of FabZ and FabA (Figure 1(A)). Furthermore, we can extend this estimate to account for the change in membrane surface area as a function of the growth rate (grey line in Figure 1(A)), which captures the observed growth rate dependent expression of these two enzymes.

Despite the slow catalytic rate of FabZ and FabA, we argue that the generation of fatty acids is not a bottleneck in cell division and is not the key process responsible for setting the bacterial growth rate. Experimental evidence has shown that the rate of fatty-acid synthesis can be drastically increased *in vitro* by increasing the concentration of FabZ (Yu et al., 2011). Stochastic simulations of the complete fatty acid synthesis pathway of *E. coli* further supports this experimental observation (Ruppe and Fox, 2018). Thus, if this step was the determining factor in cell division, increasing growth rate could be as simple as increasing the number of ACP dehydratases per cell. With a proteome size of $\approx 3 \times 10^6$ proteins, a hypothetical increase in expression from 4000 to 40,000 ACP dehydratases would result in a $\approx 1\%$ increase in the size of the proteome. As many other proteins are in much larger abundance than 4000 per cell (as we will see in the coming sections), it is unlikely that expression of ACP dehydratases couldn't be increased to facilitate faster growth.

Peptidoglycan Synthesis

While variation in cell size can vary substantially across growth conditions, bacterial cells demonstrate exquisite control over their cell shape. This is primarily due to the cell wall, a stiff meshwork of polymerized disaccharides interspersed with short peptide crosslinks termed the peptidoglycan. The cell wall is also a vital structural component that counteracts turgor pressure. In *E. coli*, this enormous peptidoglycan molecule is a few nanometers thick and resides within the periplasmic space between the inner and outer membrane. The formation of the peptidoglycan is an intricate process, involving the bacterial actin homolog MreB (Shi et al., 2018) along with a variety of membrane-bound and periplasmic enzymes (Morgenstein et al., 2015). The coordinated action of these components result in a highly-robust polymerized meshwork that maintains cell shape even in the face of large-scale perturbations and can restore rod-shaped morphology even after digestion of the peptidoglycan (Harris and Theriot, 2018; Shi et al., 2018).

In glucose-supported steady-state growth, the peptidoglycan alone comprises $\approx 3\%$ of the cellular dry mass (BNID: 101936, Milo et al. (2010)), making it the most massive molecule in *E. coli*. The polymerized unit of the peptidoglycan is a N-acetylglucosamine and N-acetylmuramic acid disaccharide, of which the former is functionalized with a short pentapeptide. With a mass of ≈ 1000 Da, this unit, which we refer to as a murein monomer, is polymerized to form long strands in the periplasm which are then attached to each other via their peptide linkers. Using the aforementioned measurement that $\approx 3\%$ of the dry mass is peptidoglycan, it can be estimated that the peptidoglycan is composed of $\approx 6 \times 10^6$ murein monomers.

During growth, peptidoglycan is constantly being broken down to allow insertion of new murein monomers and cellular expansion. In order to maintain structural integrity these monomers must be crosslinked into the expanding cell wall, potentially limiting how quickly new material can be added and we consider this process as a possible rate-limiting step. In principle, each one of these murein monomers can be crosslinked to another glycan strand via the pentapeptide. In some

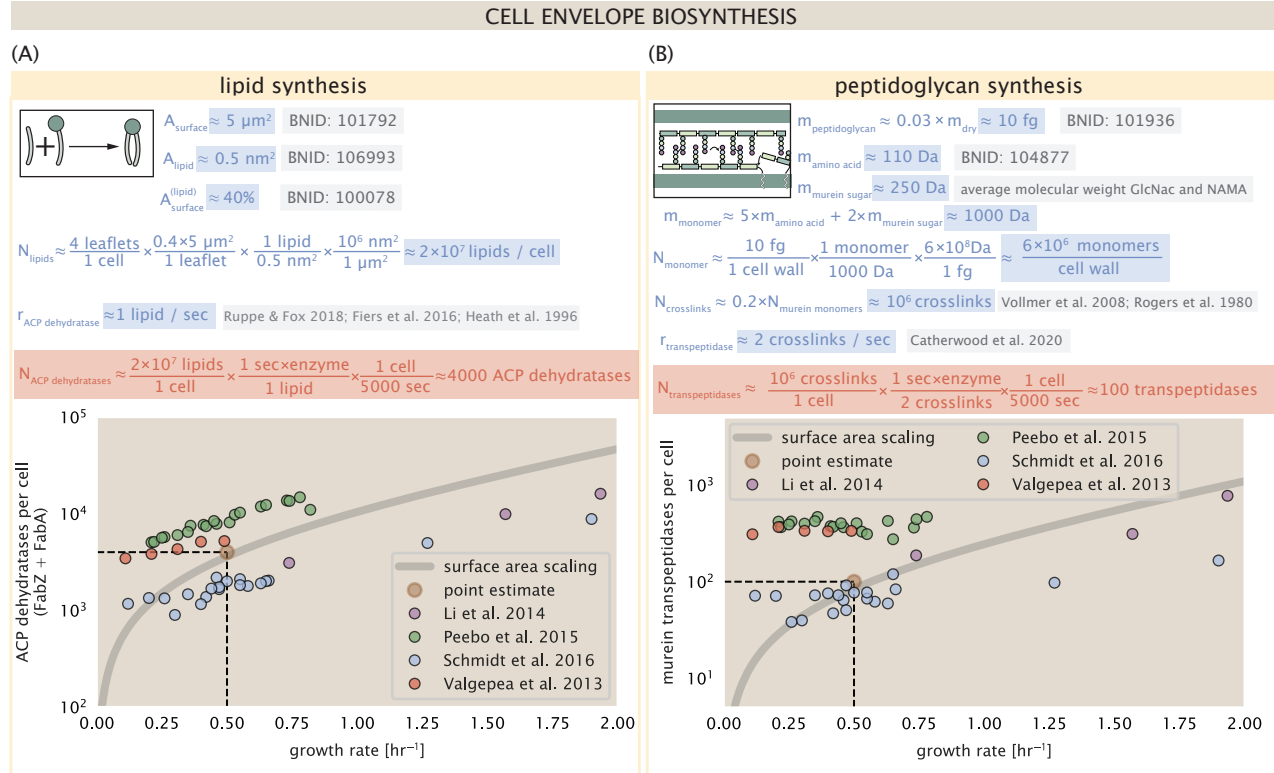


Figure 1. Estimation of the key components involved in cell envelope biosynthesis. (A) Top panel shows an estimation for the number of ACP dehydratases necessary to form functional phospholipids, which is assumed to be a rate-limiting step on lipid synthesis. The rate of ACP dehydratases was inferred from experimental measurements via a stochastic kinetic model described in *Ruppe and Fox (2018)*. Bottom panel shows the experimentally observed complex copy numbers using the stoichiometries [FabA]₂ and [FabZ]₂. (B) An estimate for the number of peptidoglycan transpeptidases needed to complete maturation of the peptidoglycan. The mass of the murein monomer was estimated by approximating each amino acid in the pentapeptide chain as having a mass of 110 Da and each sugar in the disaccharide having a mass of ≈ 250 Da. The *in vivo* rate of transpeptidation in *E. coli* was taken from recent analysis by *Catherwood et al. (2020)*. The bottom panel shows experimental measurements of the transpeptidase complexes in *E. coli* following the stoichiometries [MrcA]₂, [MrcB]₂, [MrdA]₁, and [MrdB]₁. Grey curves in each plot show the estimated number of complexes needed to satisfy the synthesis requirements scaled by the surface area as a function of growth rate. We direct the reader to the supplemental information for a more detailed discussion of this estimate.

species, such as in gram-positive bacterium *Staphylococcus aureus*, the extent of crosslinking can be large with > 90% of pentapeptides forming a connection between glycan strands. In *E. coli*, however, a much smaller proportion ($\approx 20\%$) of the peptides are crosslinked, resulting in a weaker and more porous cell wall *Vollmer et al. (2008); Rogers et al. (1980)*. The formation of these crosslinks primarily occur during the polymerization of the murein monomers and is facilitated by a family of enzymes called transpeptidases. In *E. coli*, there are four primary transpeptidases that are involved in lateral and longitudinal extension of the peptidoglycan. These transpeptidases have only recently been quantitatively characterized *in vivo* via liquid chromatography mass spectrometry *(Catherwood et al., 2020)*, which revealed a kinetic turnover rate of $\approx 1 - 2$ crosslinking reactions formed per second per enzyme.

Pulling these measurements together permits us to make an estimate that on the order of ≈ 100 transpeptidases are needed for complete maturation of the peptidoglycan, given a division time of ≈ 5000 seconds, a value that is closely aligned with the experimental observations *(Figure 1(B))*. Expanding this estimate to account for the changing volume of the peptidoglycan as a function of growth rates (grey line in *Figure 1(B)*) also qualitatively captures the observed dependence in the data, though systematic disagreements between the different data sets makes the comparison more difficult.

Much as in the case of fatty acid synthesis, we find it unlikely that the formation of peptidoglycan is a rate limiting step in bacterial cell division. The estimate we have presented considered only the transpeptidase enzymes that are involved lateral and longitudinal elongation of the peptidoglycan (proteins MrdA, MrdB, MrcA, and MrcB). This neglects the presence of other transpeptidases that are present in the periplasm and also involved in remodeling and maturation of the peptidoglycan. It is therefore possible that if this was setting the speed limit for cell division, the simple expression of more transpeptidases may be sufficient to maintain the structural integrity of the cell wall.

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