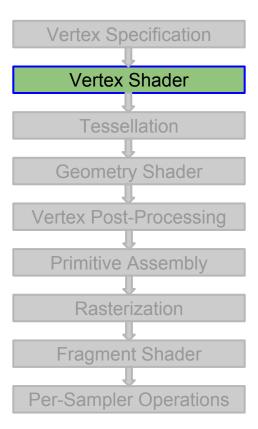
# Game Architecture Graphics II

Attack of the Matrices

#### Recap

- We've described our world using triangles.
- Triangles are made up of vertices.
- We've specified vertex data in buffers of a particular vertex format.
- We've issued a draw call to draw the geometry.
- Now what?

# Programmable Pipeline



#### Scene Representation

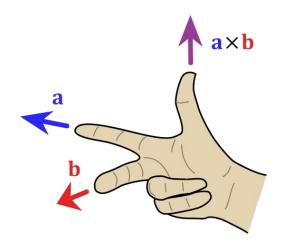
- How do we describe objects in the scene?
- How do we describe scene topology?
- How do we describe where things are?
- How do we describe how we see things?

#### Scene Representation

- How do we describe objects in the scene?
- How do we describe scene topology?
- How do we describe where things are?
- How do we describe how we see things?

- Handedness
- World space
- Model space
- View space

- Handedness
- World space
- Model space
- View space



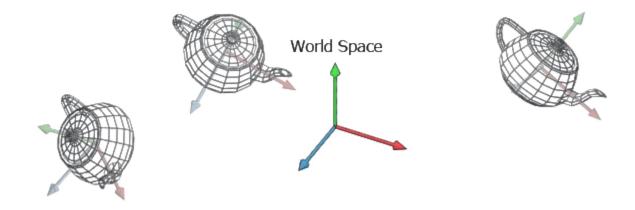
Handedness determines the direction of the cross product result.

Assuming positive x to the right, and positive y up...

- In a right-handed system, the z-axis comes out of the screen.
- In a left-handed system, the z-axis goes into the screen.

- Handedness
- World space
- Model space
- View space

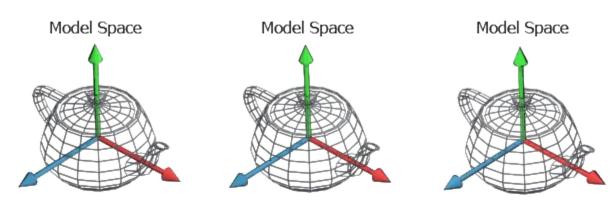
World space is the highest order coordinate system which describes absolute positions for all objects in the game.



- Handedness
- World space
- Model space
- View space

Model space is the coordinate system local to a single object in the game world.

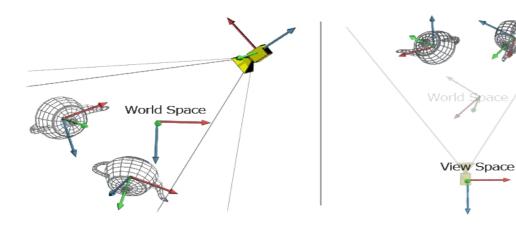
The origin is the origin point of the model, and is typically user defined. It could be the exact center, a corner, the bottom center; anywhere.



- Handedness
- World space
- Model space
- View space

View space describes the coordinate system of the camera, with the origin being the position of the camera.

Transforming into view space is an essential part of the graphics pipeline.



#### Scene Representation

- How do we describe objects in the scene?
- How do we describe scene topology?
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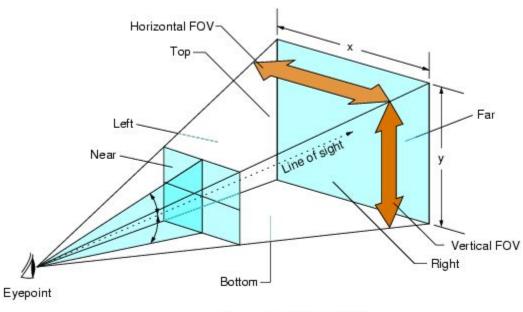
#### Virtual Camera

- A virtual camera can be created with three components:
  - A position.
  - A forward, or 'look-at' vector.
  - An up vector.
- It also needs a frustum.
  - A frustum defines the bounds that the camera can see.
  - o To define the frustum, we also need...

#### Virtual Screen

- The screen is defined by dimensions, and therefore aspect ratio.
  - o 1280x720 16:9
  - o 1920x1080 16:9
  - 1920x1200 16:10
  - 1024x768 4:3
- The screen dimensions define the near plane of the frustum.
  - The near plane is defined to be a certain distance from the camera position.
  - The far plane as well.
  - The field-of-view angles defines the rest of the frustum planes.
  - Note that vertical or horizontal field-of-view can be calculated using one another and the aspect ratio.

# **Example Frustum**



Aspect Ratio = 
$$\frac{y}{x} = \frac{\tan(\text{vertical FOV/2})}{\tan(\text{horizontal FOV/2})}$$

#### **Transformations**

- Our goal is to get something from the world to the screen. How?
- We need a series of transformations (matrices)
  - Model Transform from model into world space.
  - View Transform from world space into view space.
  - Projection Transform from view space into clip space.
  - Viewport Transform from NDC to screen space.
    - This is done in the hardware.

- The view matrix transforms the world into camera space.
- This essentially means applying the inverse of the camera's transform.
  - Translation
  - Orientation
- Translation is easy:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -x & -y & -z & 1 \end{bmatrix}$$

- Orientation is a little trickier.
- Recall that rows (or columns) of a transformation matrix are orthogonal vectors representing an orientation.
- Find them for the camera!
  - Given direction (z) (eye at) and up vector...
  - Cross direction and up to get right (x).
  - Cross right (x) and direction (z) to get an accurate up (y).
  - Then stick 'em in a matrix:

$$\begin{bmatrix} x_x & x_y & x_z & 0 \\ y_x & y_y & y_z & 0 \\ z_x & z_y & z_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- But wait!
  - That describes a transformation from the camera space to world space.
  - We want world space to camera space.
- Solution: invert the matrix.
  - It's orthogonal, so the inverse is just the transpose.
- Finally, combine with translation.
  - The translation is pre-multiplied with the orientation.

- So, given:
  - Camera position (eye)
  - Right vector (x)
  - Up vector (y)
  - Forward vector (z)

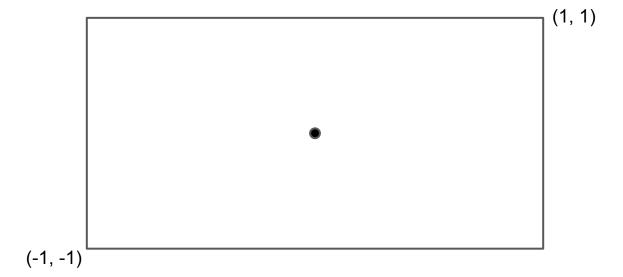
$$\begin{bmatrix} x_x & y_x & z_x & 0 \\ x_y & y_y & z_y & 0 \\ x_z & y_z & z_z & 0 \\ -dot(eye, x) & -dot(eye, y) & -dot(eye, z) & 1 \end{bmatrix}$$

## Calculating the Projection Matrix

- The projection matrix takes a point in the frustum and prepares it for a transformation to a point on a plane.
  - Basically flattening the 3D scene onto a 2D plane.
- The destination is typically a rectangle.
  - Output screen
  - Texture
  - GUI minimap

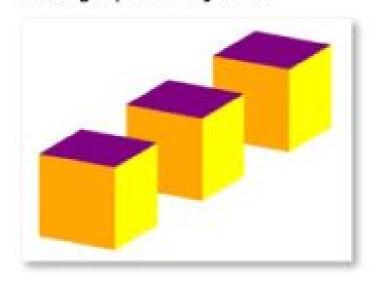
#### **Normalized Device Coordinates**

- Abbreviated NDC
- Describe the screen as a square from (-1, -1) to (1, 1)
  - Origin at (0, 0)

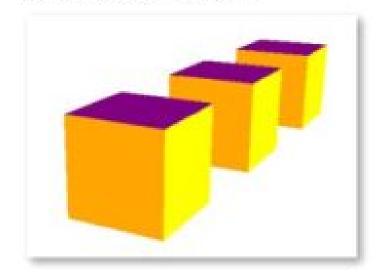


# Orthographic vs. Perspective

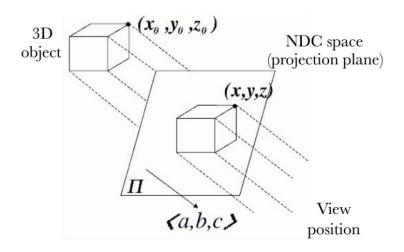
#### Orthographic Projection

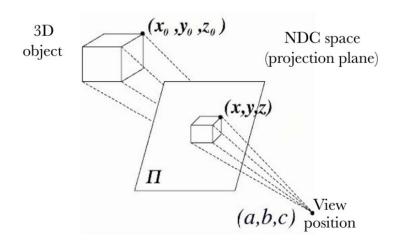


#### Perspective Projection



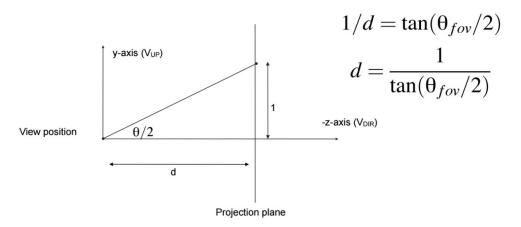
## Orthographic vs. Perspective





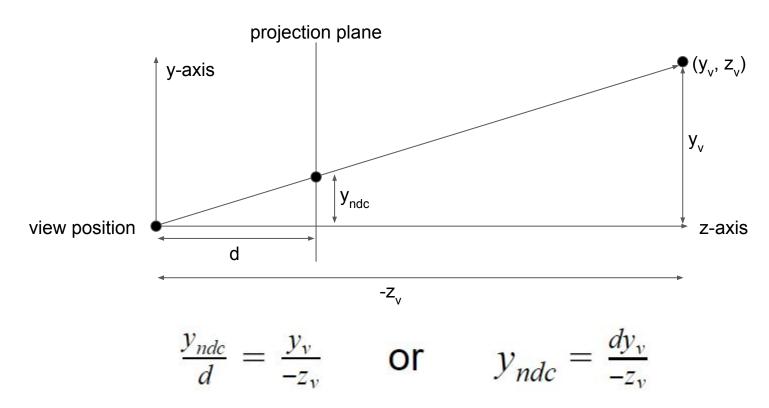
#### Field of View

Related to the location of the projection plane



We'll need this distance next.

# Perspective Projection



# Perspective Projection

- The target probably isn't a square.
- We need to adjust by the aspect ratio:

$$a = \frac{w_s}{h_s}$$

If we assume that y height is 1, we only need to adjust x:

$$x_{ndc} = \frac{dx_v}{-az_v}$$

#### Perspective Projection

- The further away an object is, the smaller it should appear.
  - Solution is to divide *x* and *y* by the *z* coordinate.
  - Hardware is going to perform division by the w component.
  - So we need to move the z coordinate into the w position.
- Which gives us the homogenous perspective matrix:

$$\begin{bmatrix} \frac{d}{a} & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & -d & -1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

# Perspective Projection in Action

$$\begin{bmatrix} \frac{d}{a} & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & -d & -1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} x_v & y_v & z_v & w_v \end{bmatrix} \begin{bmatrix} \frac{dx_v}{a} & dy_v & -dz_v & -z_v \end{bmatrix}$$

#### Projecting the Z Coordinate

- We want to use the z coordinate for depth and sorting.
- It needs to be mapped onto a (-1, 1) range depending on the near and far planes.

$$z_c = \frac{z_v(n+f) + 2nf}{n-f} \left(\frac{1}{-z_v}\right)$$

For DirectX, the range is (0, 1). Ugh.

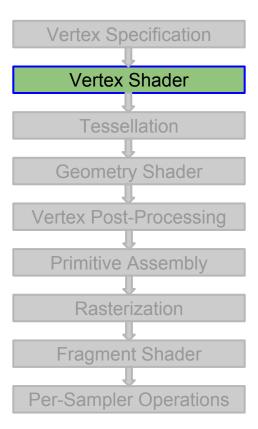
# Calculating the Projection Matrix

$$\begin{bmatrix} \frac{d}{a} & 0 & 0 & 0 \\ 0 & d & 0 & 0 \\ 0 & 0 & \frac{n+f}{n-f} & -1 \\ 0 & 0 & \frac{2nf}{n-f} & 0 \end{bmatrix}$$

#### Order of Multiplication?

- This depends on your matrix layout and multiplication code.
- For A \* B:
  - Row major layout and A rows \* B columns or
  - Column major layout and A columns \* B rows
    - Pre-multiplication = local
    - Post-multiplication = world
  - Row major layout and A columns \* B rows or
  - Column major layout and A rows \* B columns
    - Pre-multiplication = world
    - Post-multiplication = local

## Programmable Pipeline



#### Programmable Shaders

- Miniature programs which operate on vertex and fragment data.
  - Vertex shader outputs vertex position in homogenous clip space, and per-vertex values.
    - gl\_Position
  - Fragment shader outputs fragment color(s).
    - gl\_FragColor
    - And possibly depth information.
- There are many built-in functions for common operations.
  - See the OpenGL or HLSL reference pages for a list.

#### Shading Languages

- Most shading languages are C-like.
  - GLSL OpenGL Shading Language
  - HLSL High Level Shading Language (DirectX)
  - o Cg
- They are compiled to bytecode similar to assembly.
- GPU execution units execute the bytecode.

#### **GLSL**

- Program variable qualifiers.
  - in A per-element input value, like position.
  - o **out** A per-element output, like fragment color.
  - o **uniform** A per-object constant, like model-view-projection matrix or texture.

#### Basic types.

- C++ like void, float, int, bool
- Vectors vec2, vec3, vec4, ivec2, etc.
- Matrices mat2, mat3, mat4
- Textures sampler2D
- Arrays e.g. float[5]

#### Vector Types

- Shading language vector types offer different access patterns.
  - { x, y, z, w }, typically used for positions or normals.
  - { r, g, b, a }, typically used for colors.
  - { s, t, p, q }, typically used for texture coordinates.

#### Swizzling

- By definition, rearranging components of a vector.
- $\circ$  Given vector = vec4(1.0, 2.0, 3.0, 4.0)
  - vector.xxxx = { 1.0, 1.0, 1.0, 1.0 }
  - vector.wzyx = { 4.0, 3.0, 2.0, 1.0 }
  - vector.yyzz = { 3.0, 3.0, 4.0, 4.0 }
  - And so on...

#### **GLSL**

#### Control flow

- Mostly the same as C/C++.
- Notable addition is discard, which rejects a current fragment from drawing.

#### Built-in functions

- o Trig sin, cos, tan, asin, acos, atan
- Math pow, exp, log, exp2, log2, sqrt, inversesqrt
- And many more dot, cross, normalize, clamp, mix, step, reflect, etc.

#### Texture lookup

- texture2D(sampler2D, vec2)
- There are others, but this is most often used.

#### Example

```
#version 400
layout (location = 0) in vec3 in position;
uniform vec3 u color;
out vec3 out color;
void main(void)
    // Do something with color and position.
    out color = vec4(1.0, 0.0, 0.0, 1.0);
    // Assign gl Position as position in homogenous clip space.
```

## Example: Linking Shaders

Vertex shader declarations:

Fragment shader declarations:

```
layout(location = 0) in vec3 in_position; in vec3 color;
layout(location = 1) in vec3 in_color; in vec2 texcoord0;
layout(location = 2) in vec2 in_texcoord;
out vec3 color;
out vec2 texcoord0;
```

# Mythbusters!



<i>t</i> = 0	<i>t</i> = 1	t =

t = 0

Input Data

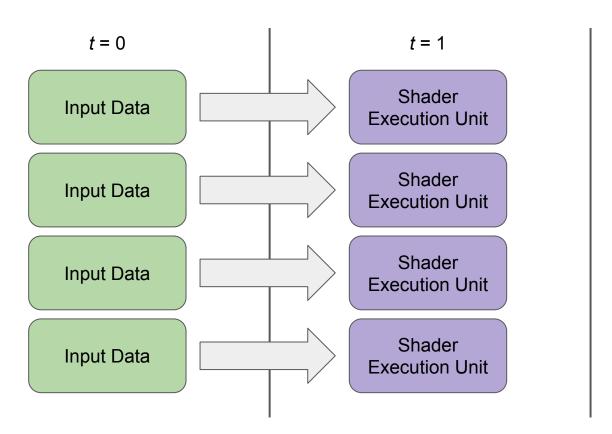
Input Data

Input Data

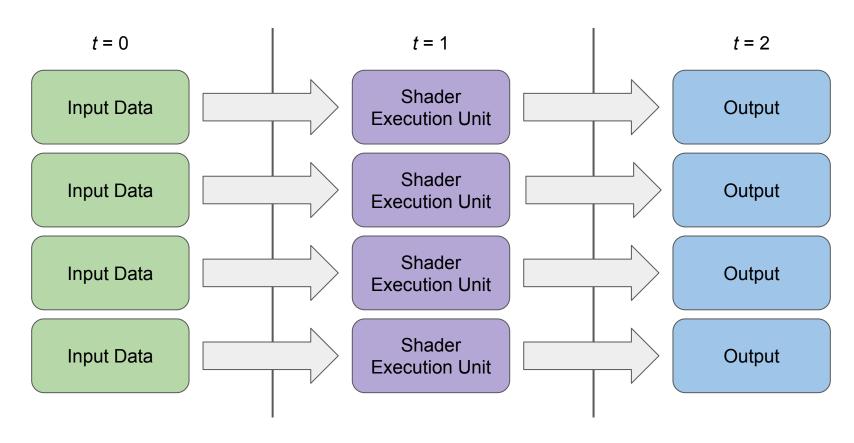
Input Data

t = 1

t = 2



t = 2



#### Vertex Shaders

- Modern vertex shaders:
  - Animate vertex positions.
  - Transform vertex positions into homogenous clip space.
  - Pass through (and possibly manipulate) per-vertex attributes.
- And that's really about it...
  - Fragment shaders get more interesting.
- They can be leveraged for optimization.
  - It's possible to use built-in hardware interpolation to your advantage.
    - Perform heavy calculations per vertex, rather than per-fragment.
  - This is really a last-resort optimization.

#### OpenGL Shaders

- OpenGL manages shaders with shader objects.
  - glCreateShader
  - glShaderSource
- Shader programs are pairings of vertex and fragment shaders.
  - glCreateProgram
  - glAttachShader
  - glLinkProgram
  - o glUseProgram
- Fun fact: shaders are usually not compiled until you actually use them.

#### End of Lecture

- Homework 3 is now actually assigned.
- It's due next Thursday, 2/16.
- On Monday, we'll finish up our trip through the graphics pipeline.