

RISRIhet(loglindispersion).Rmd

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$$Y_{ij} = (\beta_0 + \mu_{0j}) + (\beta_1 + \mu_{1j})\mathbf{time}_{ij} + \beta_2 \mathbf{SNP}_j + \epsilon_{ij}$$

$$\epsilon_{ij} \sim N(0, \sigma_{\epsilon ij}^2)$$

$$\sigma_{\epsilon ij} = \exp(\alpha + \gamma + \tau \mathbf{SNP})$$

$$\begin{bmatrix} \mu_{0j} \\ \mu_{1j} \\ \gamma_j \end{bmatrix} \sim N(0, \Omega_{\mu\gamma})$$

$$\Omega_{\mu\gamma} = \begin{bmatrix} \sigma_{\mu 0}^2 & & \\ \sigma_{\mu 01} & \sigma_{\mu 1}^2 & \\ \sigma_{\mu 0\gamma} & \sigma_{\mu 1\gamma} & \sigma_{\gamma}^2 \end{bmatrix}$$

NOTE: I removed the \wedge^2 in $\sigma_{\epsilon ij}$ since the function `stats::rnorm` takes the standard deviation not variance in the data generating process. Similarly, `nlme::lme` returns the SD and not the variance in `modmer` objects.