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1. Suppose we define the following type for binary trees, where each leaf has a label of type 'a' and each internal node has a label of type 'b':

```
type ('a, 'b) bintree =
  | Bleaf of 'a
  | Bnode of 'b * ('a, 'b) bintree * ('a, 'b) bintree
```

left *right?*

1a (8 minutes). What is the type of the following function 'mystery'? Briefly explain how you inferred its type.

```
let rec mystery w x = function
  | Bleaf(_) -> None
  | Bnode(y, a, b) ->
    match w x y with
    | 0 -> Some y
    | n -> mystery w x (if n < 0 then a else b)
```

(some node or leaf)

Mystery is type `int option`. This is because of `w x y`, we know `w` allows for a ~~com~~ ^{comparison} ~~computation~~ between `x` and `y`, meaning they must be the same type. Then, because of the condition `n < 0`, we know `n` is `int` because of the integer comparator `<`. Thus, we know `mystery` is

1b (8 minutes). What does 'mystery' do? Give a sample call to illustrate. ^{type}

~~mystery finds the node with value~~ ^{int option}
~~label x that matches label of~~

~~there is a~~ ~~there is a node with label y that equals x~~ ~~for instance~~ ~~after w is applied to x.~~ ~~mystery~~ ~~will look~~

For instance, `mystery - x` some tree finds a node in some tree with label that has diff of 0 from `x`.

1c (12 minutes). Write a function 'flatten' that takes as an argument a binary tree and returns a list of labels on the tree, in left-to-right order so that all the labels of the left subtree of a node appear before the node's label, and all the labels of the right subtree appear after the node's label.

The function should take a bintree argument and return a binvisit list, where bintree is defined in (a) and binvisit is defined by:

```
type ('a, 'b) binvisit = | Vleaf of 'a | Vnode of 'b
```

For example, the expression:

```
flatten (Bnode ("a",
               Bnode ("b", Bleaf 1, Bnode ("c", Bleaf 2, Bleaf 3)),
               Bnode ("d",
                     Bnode ("e", Bleaf 4, Bleaf 5),
                     Bnode ("f", Bnode ("g", Bleaf 6, Bleaf 7), Bleaf 8))))
```

should return:

```
[Vleaf 1; Vnode "b"; Vleaf 2; Vnode "c"; Vleaf 3; Vnode "a"; Vleaf 4;
 Vnode "e"; Vleaf 5; Vnode "d"; Vleaf 6; Vnode "g"; Vleaf 7;
 Vnode "f"; Vleaf 8]
```

When writing 'flatten' do not use the OCaml standard library; just use builtin types and operators such as '::' and '@'.

let rec flatten ~~bintree~~ function =

| Bleaf (~~val~~) → ~~[Vleaf val]~~ [Vleaf val]

| Bnode (~~label~~, ~~left~~, ~~right~~) → ~~(a @ [Vleaf a] @ b)~~

((left @ [Vnode label]) @ right);;

let rec flatten function =

| Bleaf (label) → [Vleaf val]

| Bnode (label, left, right) → ((flatten left) @
[Vnode label]) @ (flatten right);;

1d (10 minutes). Write a grammar 'flatten_grammar' in the style of Homework 2 that describes the values returned by the 'flatten' function on bintrees where all leaf values are the integers 1 through 8, and all node values are the strings "a" through "g".

let flatten_grammar =
 (~~BNode~~) (VNode, (BNode,
 function function
 INode → VNode →
 [1-8];
 On back
 page

1e (10 minutes). Assume you have the aforementioned grammar 'flatten_grammar' and a solution to Homework 2, how would you go about writing a function 'unflatten' that is the inverse of 'flatten'? That is, (unflatten (flatten X)) should equal X. You need not implement 'unflatten', just describe how you would implement it if you had more time.

Go
~~Iterate through~~ ~~thoughts~~ ~~list~~
~~of rules to find~~ of values
 To unflatten, we would be building a tree ~~that~~ so we iterate through ~~flatten grammar~~ the list and dfs through flatten grammar to find a matching derivation. If there full
 none, return none, otherwise build the tree using the same methodology as parse ~~through~~ tree through using a list of applied rules from flatten_grammar.

2 (10 minutes). If a Java program does an exit-monitor operation E followed by a normal-load operation L, a Java implementation can do L before E. However, the reverse is not true: if a Java program does a normal load L before an exit monitor E, the implementation cannot do E before L. Explain why this is, giving an example of reordering that is OK and why it is OK, and reordering that is not OK and why it is not OK.

OK ordering

```
Shape a = new Shape();
Shape b = new Shape();
int l = a 6;
```

~~0, 1, 2, 3, 4, 5, 6, 7~~

$a.y = l$
 $l = b.x$ \rightarrow these can be switched

this ordering is okay because with optimizations there is no difference in results between the two orders

3 (4 minutes). Which role of types is more important in OCaml: type annotation or type inference? Briefly explain.

Type inference is more important in OCaml since ~~it~~ what seems to be function invocations are treated as ~~gen~~ a generic type and the code that you provide via aspects like pattern-matching means you can typically avoid specifying types in code. Since it can be inferred from your code via rules

NOT OK ordering

```
Shape a = new Shape();
Shape b = new Shape();
int l = 6;
```

$l = b.x$ \rightarrow cannot be switched
 $a.y = l$

This ordering is not okay because the load changes L, meaning a violation, store is invalid when $LE \rightarrow EL$

4 (14 minutes). Write a simple, unambiguous grammar for OCaml that specifies only the following OCaml constructs.

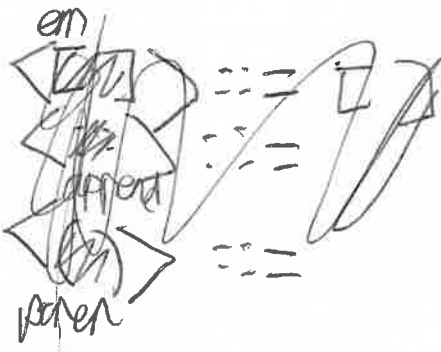
Expressions (or patterns) that contain:

- * identifiers
- * literal integer constants
- * the empty list
- * the '::' constructor
- * parenthesized subexpressions (or subpatterns)

Also, expressions that contain:

- * function definitions using the 'function' keyword and with '|' immediately after 'function'
- * function calls

Your grammar should behave the way OCaml does; for example, (a b c::d::e) should be equivalent to (((a b) c)::(d::e)).



expression = type

~~expression~~ ::= ~~expression~~ | ~~expression~~ - [] -

~~expression~~ ::= ~~expression~~ | ~~expression~~ [type] " :: " [type]

~~digit~~ = ~~0~~ | 1 | 2 | 3 |
4 | 5 | 6 | 7 |
8 | 9

type = int | float | string |
bool ...

parens = "(₁ expr)"

5a (4 minutes). Briefly explain any extra work you had to do to make the grammar unambiguous.

I ~~had to go~~ would have to
handle associativity via extra
rules

5b (10 minutes). Diagram your grammar, with boxes around nonterminals and nothing around terminals. Keep your diagram as simple as possible.

6. OCaml lacks support for shared memory parallel programming. Suppose we fix this, by adding the following concurrency primitives to the subset of OCaml studied in class:

```
type 'a thread (* The type of threads that eventually return
                  values of type 'a. *)
```

```
val create : ('a -> 'b) -> 'a -> 'b thread
(* (create func arg) creates a new thread that executes
   (func arg) concurrently with the rest of the program.
   The thread terminates when 'func' returns a value. *)
```

```
val wait : 'a thread -> 'a
(* 'wait t' suspends execution of the calling thread until the
   thread 't' terminates; it then returns the value that t's
   function returned. *)
```

6a (3 minutes). Give an example trivial use of these concurrency primitives, by multiplying 3×5 in one new thread, and 7×9 in another, and then adding the results.

*wait(create (fun x -> 3 * x) 5) +
wait(create (fun x -> 7 * x) 9);;*

6b (7 minutes). What would need to go into an OCaml Memory Model (OMM) that is like the Java Memory Model (JMM) except tailored for this variant of OCaml? Briefly explain the differences between the JMM and your OMM. Or if it's not feasible to design an OMM this way, explain why not.

*There would be no garbage collection
since every variable would be used
~~in addition~~*

let flatten - grammar =

(BNode,

BNode → [~~Bleaf~~ Vleaf Bleaf]; [VNode BNode]
[Vleaf Bleaf];
[Vnode BNode; Vnode BNode; Vnode]
[Vleaf Bleaf; Vnode BNode; Bnode]
[Vnode BNode; Vnode BNode; Bnode]
[Vnode "a"]... [Vnode "b"]

~~Vnode~~ → [~~Vnode~~ 1]; [~~Vnode~~ 2]; [~~Vnode~~ 3];
... [~~Vnode~~ 8]
leaf leaf leaf