

**Bsc 1 Game/Web Dev**  
**Maths 1**  
**Integral Calculus Tutorial III**

**Area between two curves**

Find the bounded area by the functions below (on the relevant interval where applicable):

1.  $f(x) = 3x + 6$  and  $g(x) = x^2 - 1 \quad \forall x \in [1, 4]$
2.  $f(x) = x^2 - x + 4$  and  $g(x) = x^3 - 2x^2 + 1 \quad \forall x \in [1, 4]$
3.  $f(x) = x^2$  and  $g(x) = x^4$
4.  $f(x) = x$  and  $g(x) = x^3$
5.  $f(x) = a \in \mathbb{R}$  and  $g(x) = x^3 \quad \forall x \in \mathbb{R}^+$

**Volumes of Rotation**

Evaluate each of the following volumes of rotation using, if possible,

- (a) Disk like slices
  - (b) Cylindrical shells
1. Area bounded by  $y = x^3$ ,  $x = 0$ ,  $y = 1$  rotated about the  $y$ -axis .
  2. Area bounded by  $y = x^3$ ,  $x = 0$ ,  $y = 1$  rotated about the  $x$ -axis .
  3. Area bounded by  $y = x^2$ ,  $x = 0$ ,  $y = 4$  rotated about the  $y$ -axis .
  4. Area bounded by  $y = x^3$  and  $y = x^2$  rotated about the  $y$ -axis .
  5. Area bounded by  $y = x^3$  and  $y = x^2$  rotated about the  $x$ -axis .