BSc 2 Software Design (Game/Web Dev) Integral Calculus Tutorial I

Integration by Parts

Evaluate each of the following integrals:

$$1. \qquad \int\limits_0^{\pi/2} 3 \, x^2 \cos(x) dx$$

$$2. \qquad \int \cosh(x) e^{2x} dx$$

3.
$$\int \sin(x) \sinh(x) dx$$

4.
$$\int_{0}^{\pi} (6x^{2} - 4x + 2) \sin(x) dx$$

Integration by Substitution

Evaluate each of the following integrals:

1.
$$\int 3x^2 \sin(x^3) dx$$

$$2. \qquad \int \frac{2x}{\sqrt{1-x^2}} dx$$

$$3. \qquad \int e^{\sin(x)} \cos(x) \, dx$$

4.
$$\int_{0}^{\pi} \cos^{2n}(x) \sin(x) dx; \quad \forall n \in \mathbb{N}$$

Miscellaneous

Evaluate each of the following

1. Prove that

$$\int e^{ax} \cos(bx) dx = \frac{e^{ax}}{a^2 + b^2} (a\cos(bx) + b\sin(bx)) + C; \quad \forall a, b, C \in \mathbb{R}, a^2 + b^2 \neq 0.$$

2. Evaluate

$$\int_{0}^{\pi/2} \left(\cos(x)\right)^{2n} dx \quad \forall n \in \mathbb{N}$$

3. Show that

$$\int_{0}^{\pi/2} \sin^{2n}(x) dx = \frac{2n-1}{2n} \times \frac{2n-3}{2n-2} \times \dots \times \frac{3}{4} \times \frac{\pi}{4} \quad \forall n \in \mathbb{N}$$

4. Show that

$$\int \frac{1}{a x^2 + b^x + c} dx = \frac{2}{\sqrt{4 a c - b^2}} \left(\tan^{-1} \left(\frac{2 a x + b}{\sqrt{4 a c - b^2}} \right) \right) + C \iff 4 a c > b^2$$