

S3-Class3 [Stack-3]

Stack Permutation :-

✓ push(1), push(2), push(3),
~~pop()~~ ✓ ✓ ✓ ✓ ✓

total 6! = 5 valid
 ↳ stack per-

General permutations

i/p: - 1 2 3 ✓

✓ 1 2 3

push(1), pop(), push(2), pop(), push(3), pop()

⇒ 1 2 3 ✓

✓ 1 3 2

push(1), pop(), push(2), push(3), pop(), pop()

⇒ 1, 3, 2 ✓

✓ 2 1 3

push(1), push(2), pop(), pop(), push(3), pop()

H/W

⇒ 2 3 1

3 1 2

push(1), push(2), push(3), pop(), X invalid

→ $\begin{matrix} 3 \\ 2 \\ 1 \end{matrix}$ St

→ 3 2 1

valid

push(3), pop(), push(1), pop(), push(2), pop()

GATE CSE 1994 | Question: 1.14

Stack

push(a)

~~pop(y)~~ ← X

asked in DS Oct 4, 2014 • recategorized Apr 25, 2021 by Lakshman Bhaiya

28,060 views



Which of the following permutations can be obtained in the output (in the same order) using a stack assuming that the input is the sequence 1, 2, 3, 4, 5 in that order?

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A. 3, 4, 5, 1, 2

✓ B. 3, 4, 5, 2, 1

C. 1, 5, 2, 3, 4

D. 5, 4, 3, 1, 2

2 H/W

A) 3, 4, 5, 1, 2

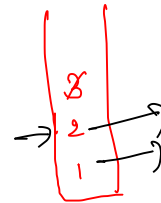
P(1)
→ P(2)
P(3)
→ P(4) : 3

P(4)

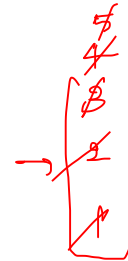
P(5) 4

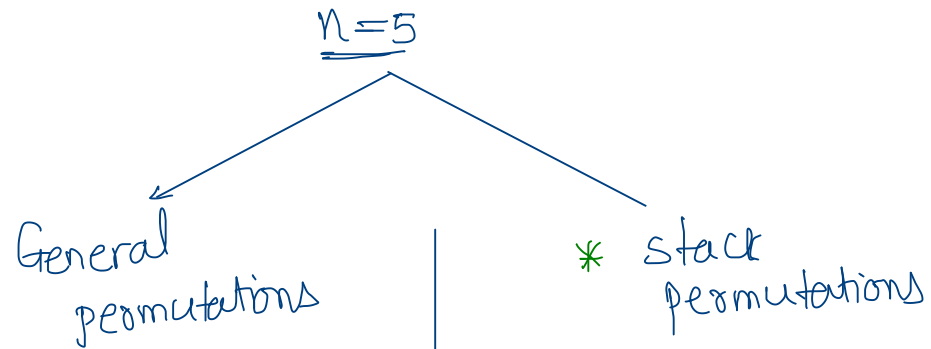
P(5)

P(5)



B) 3 4 5 2 1



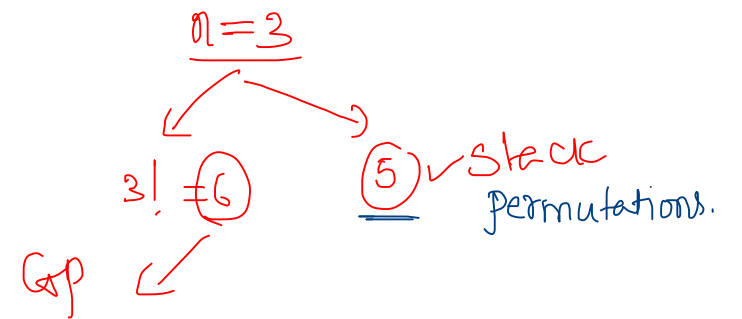


$$5! = 120$$

\Rightarrow catalan number

$$\frac{2n C_n}{n+1}$$

$\swarrow n=3$



$$n C_r = \frac{n!}{(n-r)! \times r!}$$

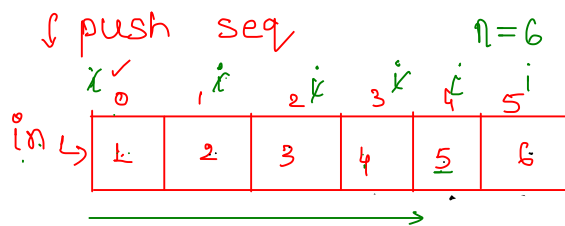
$$\frac{6 C_3}{4} = \frac{1}{4} \times 6 C_3 = \frac{1}{4} \times \frac{6!}{3! \times 3!}$$

$$= \frac{6 \times 5 \times 4 \times 3!}{4 \times 3! \times 6}$$

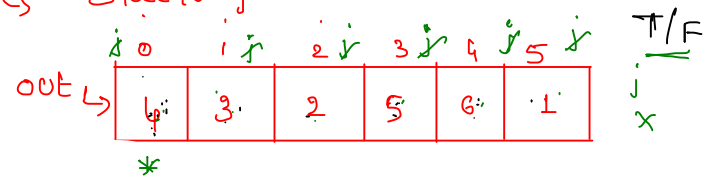
$$= 5 \checkmark$$

Q5

i/p

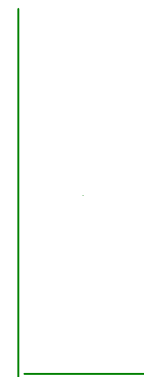


↳ stack permutation.



$$6! = 720 \checkmark$$

How long pop()



st ✓

→ valid ✓

code !

$O(1)$: min ele ✓

getmin()

```
boolean isValid(int push[], int pop[], int n)
{
    Stack<Integer> st=new Stack<>();
    int j=0;
    for(int i=0;i<n;i++)
    {
        st.push(in[i]);
        while(!st.isEmpty() && j<n && st.peek()== out[j])
        {
            st.pop();
            j++;
        }

    }
    return st.isEmpty;
}
```

3) Get minimum Element of stack in $O(1)$ time :-

push(5)

push(20)

push(15)

push(3)

push(14)

pop()

GetMin()

push(2)

GetMin()

3) Get minimum Element of stack in $O(1)$ time :-

push(5)

push(20)

push(15)

push(3)

push(2)

pop()

GetMin()

push(2)

GetMin()

C₁

push(5), push(7), push(8), getMin()

push(5), push(3), getMin(), pop(), getMin()

C.

push(5), push(3), getMin(), pop(), getMin()

push(3), push(5), push(2), push(7) , push(8), pop(), getMin(), pop(), push(1), getMin(), pop(), getMin()

*

```
void push(int x)
{
    if(st.size()==0)
    {
        st.push(x);
        minElement=x;
    }
    else
    {
        if(x>=minElement)
        {
            st.push(x);
        }
        else
        {
            st.push(2*x-minElement);
            minElement=x;
        }
    }
}
```

```
int pop()
{
    if(st.size()==0)
    {
        return -1; // UnderFlow
    }
    else
    {
        if(st.peek>=minElement)
        {
            st.pop();
        }
        else
        {
            minElement=2*minElement-st.peek();
            st.pop();
        }
    }
}
```

```
int getMin()
{
    if(st.size()==0)
        return -1;
    else
    {
        if(st.peek()>=minElement)
            return st.peek();
        else
            return minElement;
    }
}
```