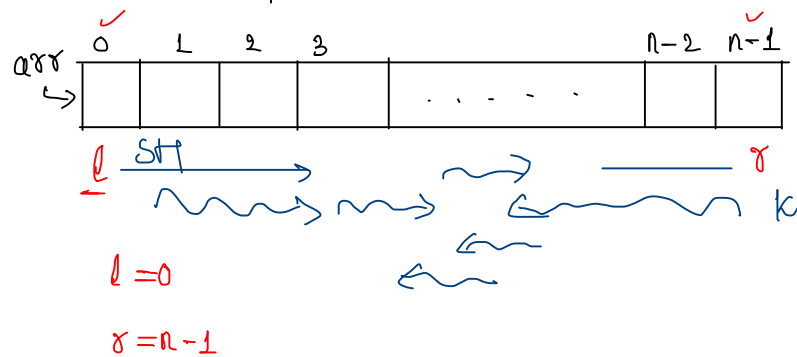


DDLJ

Two - Pointer Technique (2-variables)

Type-1

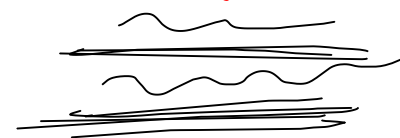
→ Both pointers, moves in the opposite direction.



Type-2

→ Both pointers, moves in the same direction.

(running race)



Two Pointer [Model-1 : Moves in Opposite Direction]

1) Find a pair whose sum is equal to k [$a+b=k$]

arr

0	1	2	3	4	5	6	7
7	4	9	6	2	8	11	17

$$7 + 9 = 16$$

$$n = 8 \checkmark$$

$$k = 16 \checkmark$$

is there any 2 ele's in array (let x, y)

$$x, y \in arr[]$$

$$x + y = k$$

Yes /
T False

Appt:-

```
boolean findSum(int arr[], int n, int k)
{
    for(int i=0; i<n; i++)
    {
        for(int j=i+1; j<n; j++)
        {
            if(arr[i]+arr[j]==k)
                return true;
        }
    }
    return false;
}
```

$\Rightarrow O(n^2)$
 $\hookrightarrow TLE [01]$

$$\checkmark S_1: O(n \log n)$$

$$\checkmark S_2: O(n^3) \times$$

S-c:-

$O(1)$ \because we used only variables, i, j

✓ Ap₂:-

0	1	2	3	4	5	6	7
7	4	9	6	21	8	11	17

$n = 8$

$k = 27$

} 27 ✓ (T)

$$\begin{matrix} \downarrow 6 & \textcircled{21} \\ a + b & = \underline{27} \\ 1 & 1 \end{matrix}$$

$$27 - a = b$$

$$27 - \textcircled{7}^a = \underline{20}$$

$$27 - \textcircled{4}^a = \underline{23}$$

$$27 - \textcircled{9}^a = \underline{18}$$

$$27 - \textcircled{6}^a = \underline{21}$$

$$27 - 21 = 6 \checkmark$$

2 ele

27

Set: { 7, 4, 9, 6 }

↑
O(L) time

$$27 - 21 = 6$$

HashSet ? \Rightarrow

✓
✓
✓
✓
?

 } every ele (key)

HashMap \Rightarrow

k	v
✓	✓
✓	✓
✓	✓
?	?

```
boolean findSum(int arr[], int n, int k)
```

```
{
```

```
    HashSet<Integer> hs = new HashSet<>();
```

```
    for(int i=0; i<n; i++) → n
```

```
    {
```

```
        temp = k - arr[i];
```

```
        if(hs.contains(temp))
```

```
        {
```

```
            return true;
```

```
        }
```

```
        else
```

```
        {
```

```
            hs.add(arr[i]);
```

```
        }
```

```
    }
```

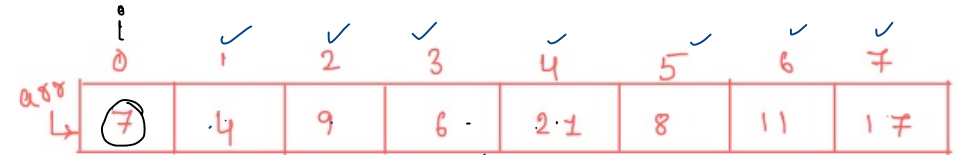
```
    return false;
```

```
}
```

T.C: $O(n)$

S.C: $O(n)$

Worst-case -



$n=8$

$K=27$

1000

$hs = \{ 7, 4, 9, 6, \dots \}$
 \leftarrow W.C, $size(hs) = size(arr) = n$

What about Space Complexity ?

→ Apart from given i/p, see what is the extra space that we are using.

$O(1)$ ✓	NOT $O(1)$
All variables $i, temp, \dots$	any extra array (or) any " collection HashSet/HashMap

Ap1:- ✓ Brute Force

T.C: $O(N^2)$

S.C: $O(1)$

Ap2:- Hashset

T.C: $O(N)$

S.C: $O(N)$

Ap3

"2ptr"

T.C: $> n$ $\xleftrightarrow{?}$ $< n^2$
S.C: $O(1)$ $O(\rightarrow n \cdot \log_2)$

0 0 0 0 0 1 7

AP₃ (2pts)

	0	1	2	3	4	5	6	7
arr	7	4	9	6	21	8	11	17

$$n=8$$

$$k=16$$

$$(x+y=16) \checkmark$$

	0	1	2	3	4	5	6	7
arr	4	6	7	8	9	11	17	21

l++ ✓ r--

step 1:-

sort the array (↑ order)

$$\frac{a[l] + a[r]}{2} \text{ v/s } k$$

C ₁	C ₂	C ₃
$a[l] + a[r] = k$	$a[l] + a[r] < k$	$a[l] + a[r] > k$
stop (return true)	l++	r--

$$a_5 > 16 \Rightarrow C_3$$

$$\frac{25+6}{2} > 25$$

DDLJ-2

```
boolean findSum(int arr[], int n, int k)
```

```
{
```

```
    int l=0, r=n-1;
```

```
    Arrays.sort(arr);
```

```
    // multiple times I need do
```

```
    while(l<r)
```

```
    {
```

```
        // case1
```

```
        if(arr[l]+arr[r]==k)
```

```
            return true;
```

```
        // case2
```

```
        if(arr[l]+arr[r] < k)
```

```
            l++;
```

```
        // case3
```

```
        else
```

```
            r--;
```

```
    }
    return false;
```

```
}
```

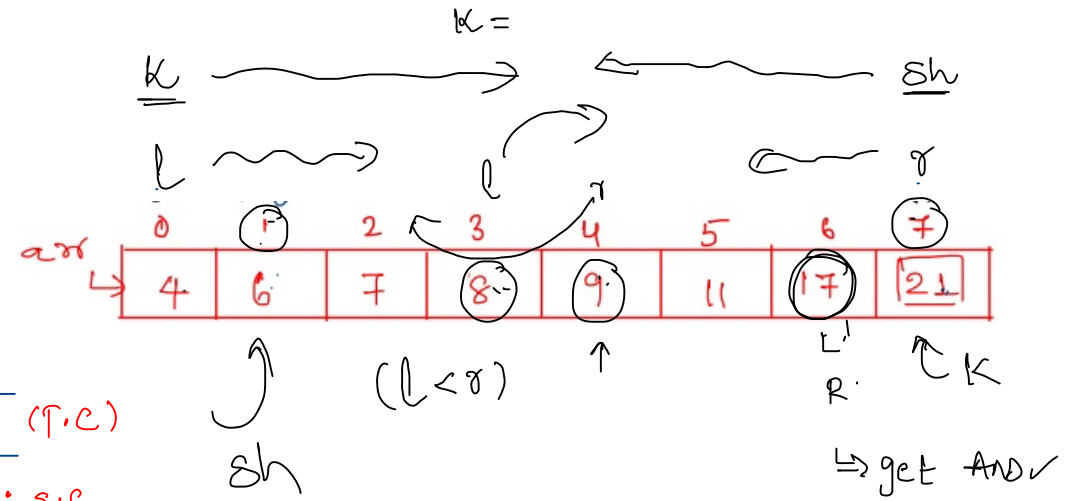
$O(n \cdot \log_2 n)$

$O(n)$

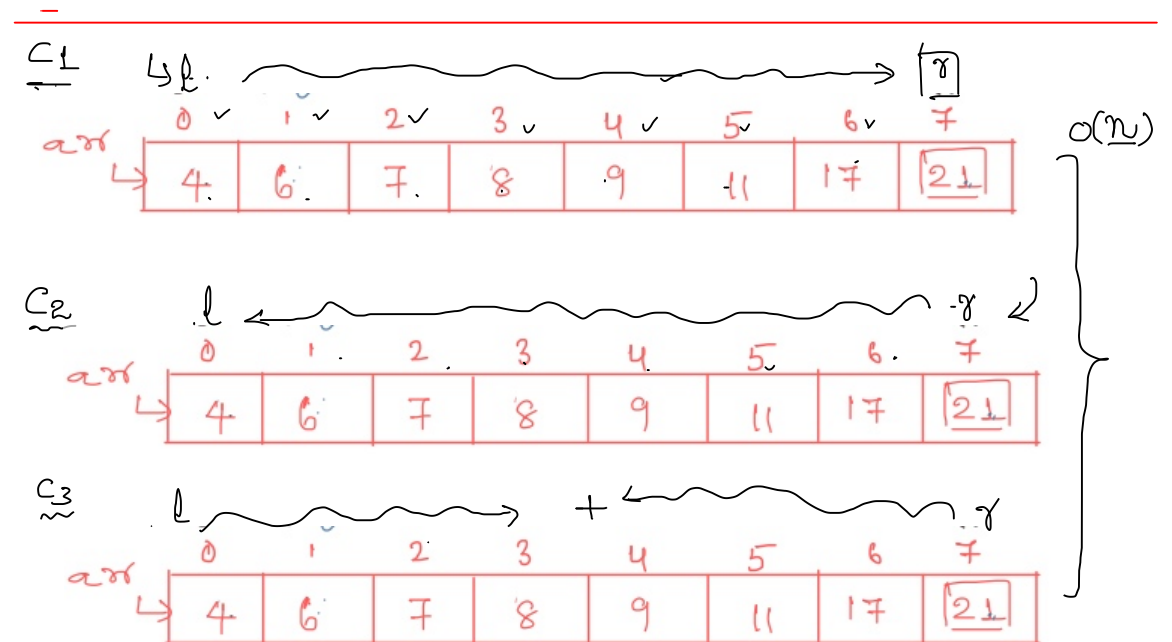
$\therefore O(n \cdot \log_2 n)$ (T.C)

$O(1)$: S.C

$O(1)$



$$x + y = k$$



2) Find a triplet whose sum is equal to k [$a+b+c=k$]

	0	1	2	3	4	5	6	7
arr	7	4	9	6	21	8	11	17

	0	1	2	3	4	5	6	7
arr	4	6	7	8	9	11	17	21

	0	1	2	3	4	5	6	7
arr	4	6	7	8	9	11	17	21

	0	1	2	3	4	5	6	7
arr	4	6	7	8	9	11	17	21

BF: $O(n^3)$

\underline{n} 2ptr
 $(a+b=k) \rightarrow O(n \cdot \log_2 n)$

2ptr: - ?

↳ 1. Sort ✓

2.

$n=8$

$$\cancel{*} + (\cdot) + (\cdot) = k$$

	0	1	2	3	4	5	6	7
arr	4	6	7	8	9	11	17	21

$i = 5 \quad (n-3)$

P.C:- sort + $i=0 \rightarrow 2ptr(i+1 \text{ to } n-1)$
 $i=1 \rightarrow$ "
 $i=2 \rightarrow$ "
 \vdots
 $i=n-3 \rightarrow$ "

$$a + b + c = k$$

P.C:-

sort + $i = 0 \rightarrow \text{2ptr}(i+1 \text{ to } n-1)$
 $O(n \log_2 n)$
 $i = 1 \rightarrow \text{,,}$
 $i = 2 \rightarrow \text{,,}$
 \vdots
 $i = n-3 \rightarrow \text{,,}$

$$\approx n-3 \approx n(n) \Rightarrow n^2$$

$$n \log_2 n + n-3(n)$$

(1)

$$= n \log_2 n + n^2 - 3n \Rightarrow \underline{O(n^2)}$$

P.C

~~A)~~ $O(n)$ ✓✓

~~B)~~ $O(n^2 \log n)$

C) $O(n^2)$

$$a + b = k \text{ (2ptr)}$$

$$\Rightarrow \underbrace{n \log n}_{\text{sorting}} + \underbrace{n}_{\text{2ptr}}$$

$$O(n \log n)$$

(2)

$$\underline{O(n^2 \log_2 n)}$$

less \rightarrow better

arr

0	1	2	3	4	5	6	7
7	4	9	6	21	8	11	17

0	1	2	3	4	5	6	7

3) H/W Seperate 0's and 1's

$\underbrace{1 \ 1 \ \dots \ 1}_{\text{end}}$

(2pt) ✓

018

	0	1	2	3	4	5	6	7	8	9	10	11	12
→	1	1	0	0	0	1	1	0	0	1	0	0	0

$$\eta = 13$$
[illegible]

AP₂:- LKG

↳ sort Array

$O(n \log n)$

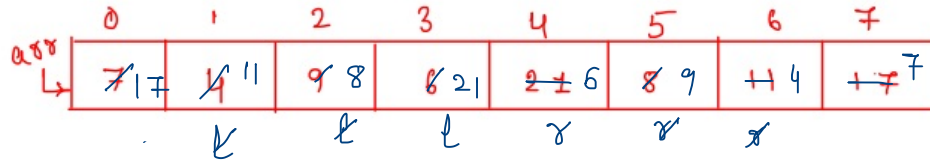
}

018
↳

0	1	2	3	4	5	6	7	8	9	10	11	12
1	1	0	0	0	1	1	0	0	1	0	0	0

4. Reverse the array [in-place]

↳ S.C : $O(1)$



while(l < r)

{

temp = a[l]

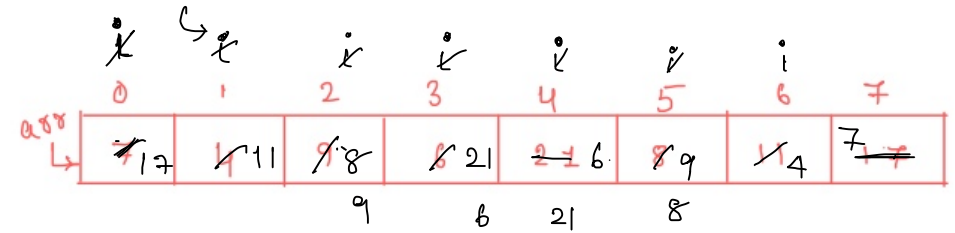
a[l] = a[r]

a[r] = temp

}

Hint: 2ptr + swap

n=8



for(i=0; i < n/2; i++)

{

temp = a[i]

a[i] = a[n-i-1]

a[n-i-1] = temp

}

i=0 temp=7
 $\hookrightarrow n-i-1 = 8-0-1 = 7$

✓
* Two Pointer [Model-2 : Same Direction]

Use in
↳ Idea : Linked list

★

5) Merge Two Sorted Arrays

i/p : 2 sorted arrays

o/p :- Final sorted array

i/p

$n_1 = 5$ ✓
sorted

arr1	0	1	2	3	4
↳	1	3	5	7	9

$n_2 = 5$ ✓
sorted

arr2	0	1	2	3	4
↳	2	4	6	8	10

club ↘ final array is sorted

arr3

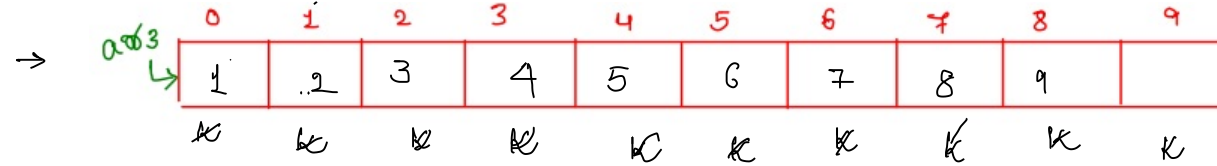
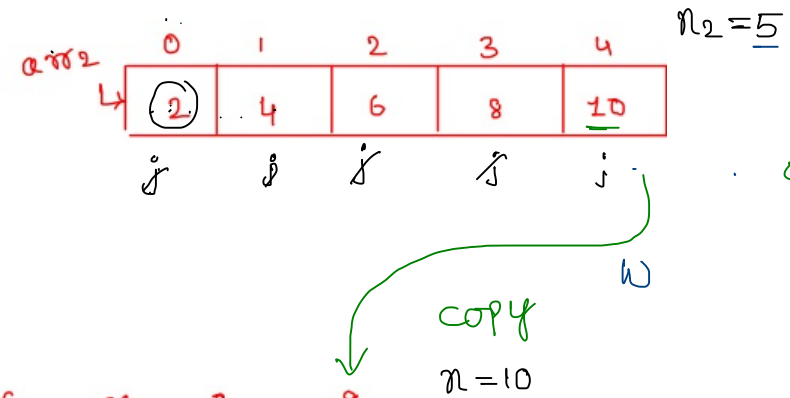
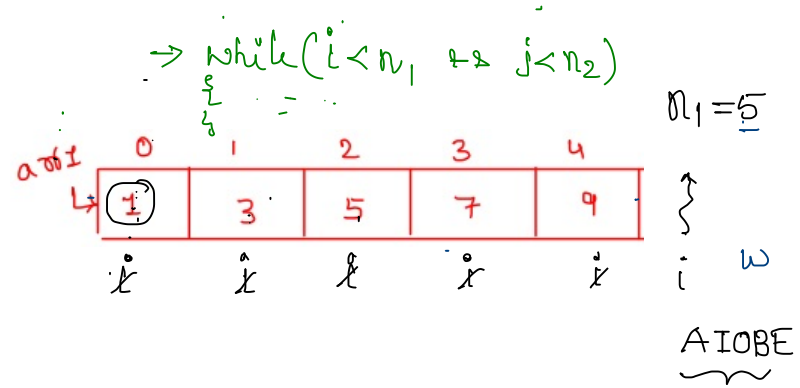
↳	0	1	2	3	4	5	6	7	8	9
	1	2	3	4	5	6	7	8	9	10

```
int[] sortArrays(int arr1[],int n1,int arr2[], int n2)
```

```
{
```

```
    int res[]=new int[n1+n2];
```

```
}
```

remaining ele's copy by taking extra loop

$i = 0, j = 0, k = 0$

$a_1[i]$ v/s $a_2[j]$

↓

$a[k] = \text{small}(a_1[i], a_2[j])$

$k++$

