

S3-Class2[Stack-2]

## GATE CSE 2021 Set 1 | Question: 21

asked in DS Feb 18, 2021 • retagged Nov 30, 2022 by Lakshman Bhaiya

6,351 views



Consider the following sequence of operations on an empty stack.

7

push(54); push(52); pop(); push(55); push(62); s = pop();

$S = 62$  ✓



Consider the following sequence of operations on an empty queue.

enqueue(21); enqueue(24); dequeue(); enqueue(28); enqueue(32); q = dequeue();

$q = 24$

The value of  $s+q$  is 86 ✓

21

24

gatecse-2021-set1

data-structures

stack

numerical-answers

1-mark

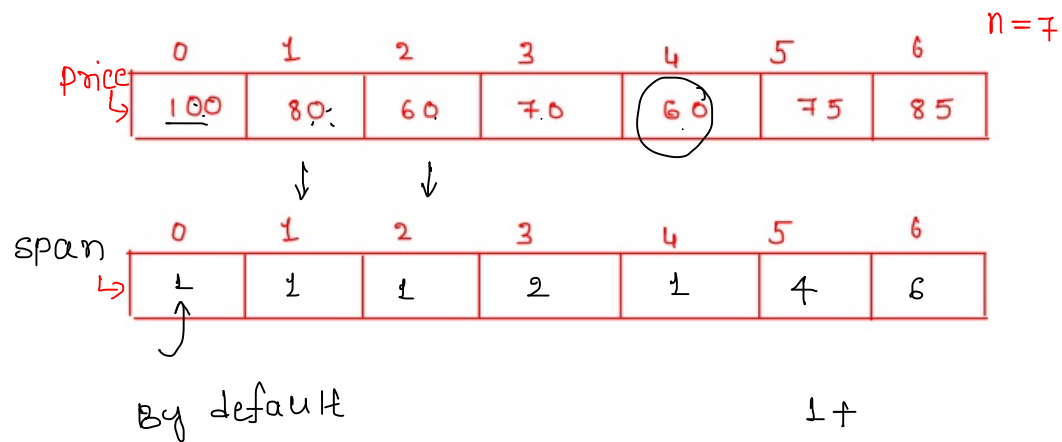
# 1) Stock Span problem

to memo:-

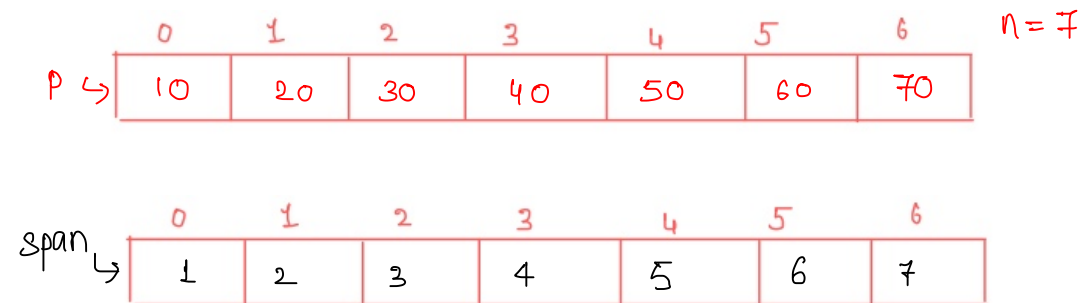
1 problem

↳ NO-duplicates (All values are dist)

4 more ques.



1 + see it's prev day's  
for how many days  
price is continuously  
smaller



BF:-

```
✓ int[] findSpan(int p[], int n)
{
```

```
    int res[] = new int[n];
```

```
    res[0] = 1;
```

```
    for(int i=1; i<n; i++)
```

```
    {        count = 1;
```

```
        → for(int j=i-1; j>0; j--)
```

```
        {
```

```
            if( p[i] > p[j] )
```

```
            {
```

```
                count++;
```

```
            }
```

```
            else
```

```
            {
```

```
                break;
```

```
            }
```

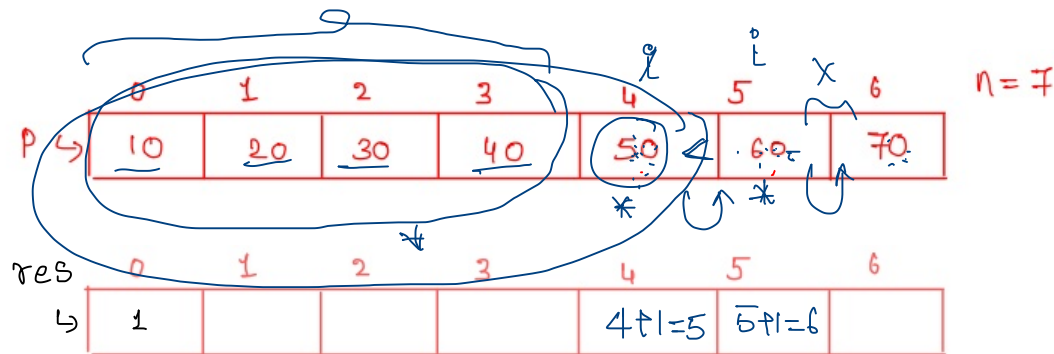
```
        }
```

```
        res[i] = count;
```

```
    }
```

```
    return res;
```

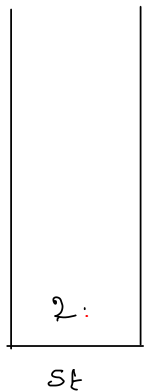
```
}
```



when  
 $i=4$   
 $p[4]=50$   
 $j=1$  ✓  $j=2$  ✓  $j=3$  ✓  
 $j=0$  ✓

when  
 $i=5$   
 $p[5]=60$   
 $j=1$  ✓  $j=2$  ✓  $j=3$  ✓  $j=4$  ✓

top (big) → delete()  
small → don't pop()



	0	1	2	3	4	5	6
p	100	80	60	70	60	75	85
res	1	?	X				

$$\frac{p[\text{st.peek()}]}{v/s} \quad \frac{p[i]}{p[i]}$$

>  
<

left  $\frac{a[i]}{> a[i]}$   
 $< a[i]$

$p[\text{st.peek()}] > p[i]$   
deleting  
X

```
int[] findSpan(int p[], int n)
{
    int res[] = new int[n];
    res[0] = 1;
    for (int i = 1; i < n; i++)
    {
        while (p[st.peek()] < p[i])
            st.pop();
    }
}
```

wrong - one  
↳ correct one

\*once you are done with arr[i], push the index into stack

useful :  $\frac{\text{see all left } a[i]}{\text{side ele's}}$   
useless :  $\Rightarrow$  these are smaller, then I need it  
so I will pop()

```
int[] findSpan(int p[], int n)
```

```
{
```

```
    int res[] = new int[n];
```

```
    res[0] = 1;
```

```
    for(int i = 1; i < n; i++)
```

```
    {
```

```
        while(p[st.peek()] < p[i]) xxx
```

```
            st.pop();
```

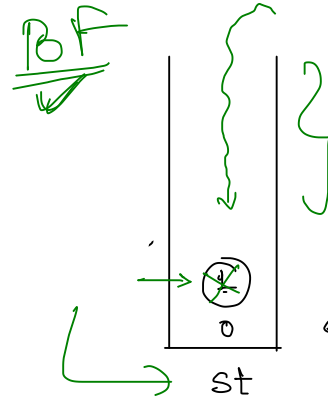
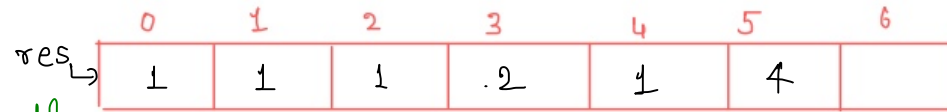
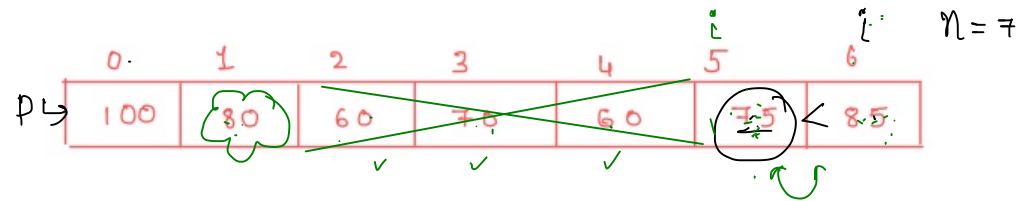
```
        res[i] = i - st.peek();
```

```
        st.push(i);
```

```
    }
```

```
}
```

Done.



← pushing array indices

Doubt:-

60 < 70

↳ required for us, BUT pop()

are we not going to lose the info

Note:- In Brute force approach, unnecessary comparisons are happening

In stack approach, the comparisons are happening w.r.t to stack element and array element,

if the element is let's say smaller than  $p[i]$ , then if you put that element in stack, which again leads to BRUTEFORCE, So that is the reason if element is smaller than  $p[i]$   
delete it from stack  $\Rightarrow$  put only the elements which are greater than  $p[i]$

so that comparison happens only with greater elements

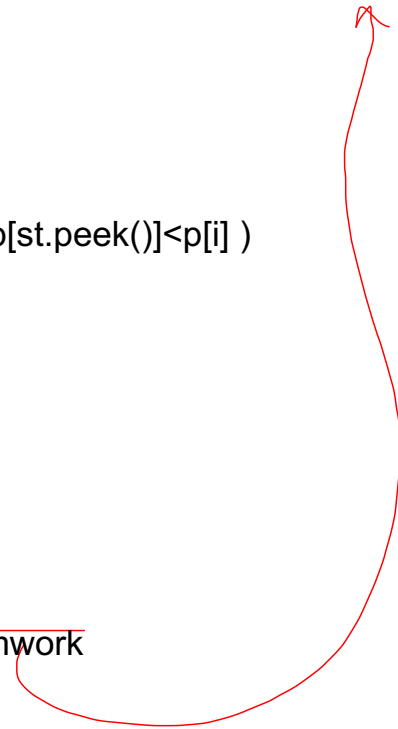
```

int[] findSpan(int p[], int n)
{
    int res[]=new int[n];
    res[0]=1;
    st.push(0)
    for(int i=1;i<n;i++)
    {
        while( !st.isEmpty()&& p[st.peek()]<p[i] )
        {
            st.pop();
        }
        if(!st.isEmpty())
        {
            res[i]=i-st.peek();
        }
        else
        {
            res[i]= ?? // hoemwork
        }
        st.push(i);
    }
}

```

$n = 7$

	0	1	2	3	4	5	6
p →	10	20	30	40	50	60	70





12:58pm

\_\_\_\_\_

✓ int[] findSpan(int p[], int n)

```

{
    int res[] = new int[n];
    res[0] = 1;
    for(int i=1; i<n; i++)
    {
        count = 1;
        → for(int j=i-1; j>0; j--)
        {
            if( p[i] > p[j] )
            {
                count++;
            }
            else
            {
                break;
            }
        }
        res[i] = count;
    }
    return res;
}

```

Dep  
↳ on-rolling

$i=0$  x

$i=1 \rightarrow j=1$

$i=2 \rightarrow j=2$

$i=3 \rightarrow j=3$

⋮

$i=n \rightarrow j=n$

$$1+2+\dots+n = \frac{n(n+1)}{2} \Rightarrow O(n^2)$$

↳ TLE





→ NOT in-terms of value, {in terms of closeness}

## 2) Nearest / Immediate Smaller Element to its Left [NSE Left]

i/p

→

$a[i]$

$n=8$

	0	1	2	3	4	5	6	7
a	7	2	4	6	9	3	8	11

BF  
↳ 2 loops ✓  
 $O(n^2)$

o/p

res

	0	1	2	3	4	5	6	7
res	-1	-1	2	4	6	2	3	8

a

	0	1	2	3	4	5	6	7
a	7	2	1	4	9	8	21	5

res

	0	1	2	3	4	5	6	7
res	-1	-1	-1	1	4	4	8	4

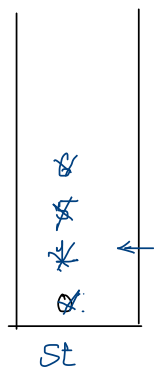
✓

arr

0	1	2	3	4	5	6	7
7	2	4	6	9	3	<del>4</del>	<del>1</del>

res

0	1	2	3	4	5	6	7
-1	-1	2	4	6	2	3	-1



$a[i]$   
 \* Among all  $i$ 's left side ele's  
 smaller ele I need,  
 so should I push/pop

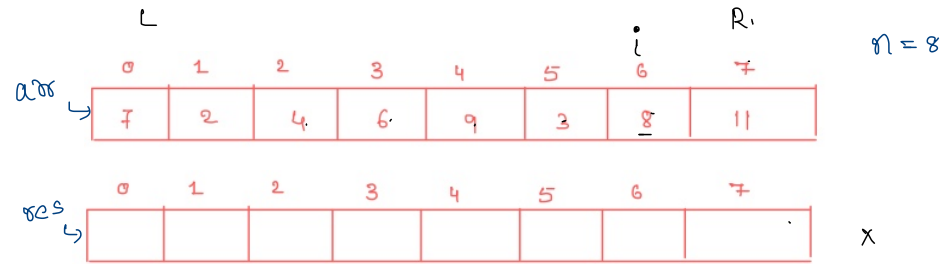
\* you will get  
in stack

$arr[st.peek()] > arr[i] \Rightarrow$  NOT required  
 so I will pop()

```

int[] NSELeft(int arr[], int n)
{
    int res[] = new int[n];
    res[0] = -1;
    st.push(0);
    for(int i = 1; i < n; i++)
    {
        while( !st.isEmpty() && arr[st.peek()] > arr[i] )
        {
            st.pop();
        }
        if( !st.isEmpty() )
        {
            res[i] = arr[st.peek()];
        }
        else
        {
            res[i] = -1;
        }
        st.push(i);
    }
}
  
```

### 3) Nearest / Immediate Smaller Element to its Right [NSE Right]

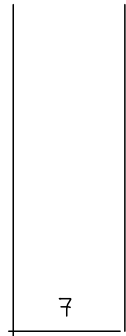


BF  
 $\hookrightarrow 2 \text{ loops} : O(n^2)$

int[] NSERight(int arr[], int n)

```

{
    int res[] = new int[n];
    res[n-1] = -1;
    st.push(n-1);
    for(int i = n-2; i >= 0; i--)
    {
        while( !st.isEmpty() && arr[st.peek()] > arr[i] )
        {
            st.pop();
        }
        if(!st.isEmpty())
        {
            res[i] = arr[st.peek()];
        }
        else
        {
            res[i] = -1;
        }
        st.push(i);
    }
}
    
```



arr[i]  $\xrightarrow{\quad}$   
 $\uparrow$   
 smaller [Right side ele]  $\Rightarrow$   
 {in stack}

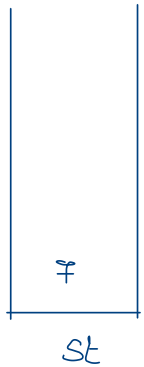
arr[st.peek()] > arr[i]  $\Rightarrow$  pop() ✓

#### 4) Nearest / Immediate Greater Element to its Right [NSE Right]

$n = 8$

	0	1	2	3	4	5	6	7
arr	7	2	4	6	9	3	8	11

	0	1	2	3	4	5	6	7
res	9	4	6	9	11	8	11	-1



$a[i]$  right

↙

$arr[st.peek()] > arr[i]$   $\Rightarrow$  required ✓

$arr[st.peek()] < arr[i]$   $\Rightarrow pop()$

not required

```
int[] NSERight(int arr[], int n)
{
```

```
    int res[] = new int[n];
    res[n-1] = -1;
    st.push(n-1);
    for(int i = n-2; i >= 0; i--)
```

```
    {
        while( !st.isEmpty() && arr[st.peek()] < arr[i] )
        {
            st.pop();
        }
        if(!st.isEmpty())
        {
            res[i] = arr[st.peek()];
        }
        else
        {
            res[i] = -1;
        }
        st.push(i);
    }
}
```



## 5) Nearest / Immediate Greater Element to its Left [NSE Left]

arr

0	1	2	3	4	5	6	7
7	2	4	6	9	3	8	11

res

0	1	2	3	4	5	6	7
-1	7	7	7	-1	9	9	-1



$a[i]$   
 $\uparrow$   
 {left ele need}

$arr[st.peek()] > arr[i] \Rightarrow \text{required}$   
 $arr[st.peek()] < arr[i] \Rightarrow \text{pop()}$

```
int[] NSELeft(int arr[], int n)
{
    int res[] = new int[n];
    res[0] = -1;
    st.push(0);
    for(int i=1; i<n; i++)
    {
        while( !st.isEmpty() && arr[st.peek()] < arr[i] )
        {
            st.pop();
        }
        if(!st.isEmpty())
        {
            res[i] = arr[st.peek()];
        }
        else
        {
            res[i] = -1;
        }
        st.push(i);
    }
}
```

① Stock - span problem

2,3  $\hookrightarrow$  NSE [left + right]

4,5  $\hookrightarrow$  NGE [left + right]

$\Rightarrow$  5 problems

---

OJ  $\hookrightarrow$  may be slight variation ✓

3) Nearest / Immediate Greater Element to its Left [NGE Left]

4) Nearest / Immediate Greater Element to its Right [NGE Right]