

Results with all scalar variables declared as real

$$X = t\gamma_t + x\gamma_x + y\gamma_y + z\gamma_z + w\gamma_w$$

$$K = k^t\gamma_t + k^x\gamma_x + k^y\gamma_y + k^z\gamma_z + k^w\gamma_w$$

$$K \cdot X = k^t t - k^w w - k^x x - k^y y - k^z z$$

$$I^2 = 1$$

$$I_{xyzw} = I\gamma_x\gamma_y\gamma_z\gamma_w = \gamma_t$$

$$(I\gamma_x\gamma_y\gamma_z\gamma_w)^2 = 1$$

$$e^{-E\gamma_w t} = \cos(Et) - \sin(Et)\gamma_w$$

$$-E\gamma_w e^{-E\gamma_w t}\gamma_t = -Et\sin(Et) - Et\cos(Et)\gamma_w$$

$$\nabla e^{-E\gamma_w t} = -E\sin(Et)\gamma_t - E\cos(Et)\gamma_t \wedge \gamma_w$$

$$\nabla e^{-E\gamma_w t} + E\gamma_w e^{-E\gamma_w t}\gamma_t = Et\sin(Et) - E\sin(Et)\gamma_t + Et\cos(Et)\gamma_w - E\cos(Et)\gamma_t \wedge \gamma_w$$

$$e^{I_{xyzw}K \cdot X} = \cos(-k^t t + k^w w + k^x x + k^y y + k^z z) - \sin(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_t$$

$$\begin{aligned} \nabla e^{I_{xyzw}K \cdot X} = & k^t \cos(-k^t t + k^w w + k^x x + k^y y + k^z z) \\ & + k^t \sin(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_t + k^x \sin(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_x + k^y \sin(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_y + k^z \sin(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_z + k^w \sin(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_w \\ & - k^x \cos(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_t \wedge \gamma_x - k^y \cos(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_t \wedge \gamma_y - k^z \cos(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_t \wedge \gamma_z - k^w \cos(-k^t t + k^w w + k^x x + k^y y + k^z z)\gamma_t \wedge \gamma_w \end{aligned}$$