

## Program:

```
import sys
from sympy import symbols, sin, cos
from sympy.galgebra.printer import Format, xpdf, Get_Program, Print_Function
from sympy.galgebra.ga import Ga

Format()
coords = symbols('t x y z', real=True)
(st4d, g0, g1, g2, g3) = Ga.build('gamma*t|x|y|z', g=[1, -1, -1, -1], coords=coords)
I = st4d.i

(m, e) = symbols('m e')

psi = st4d.mv('psi', 'spinor', f=True)
A = st4d.mv('A', 'vector', f=True)
sig_z = g3*g0

print '\\text{4-Vector Potential}\\;\\;}\\ \\bm{A} =' , A
print '\\text{8-component real spinor}\\;\\;}\\ \\bm{\\psi} =' , psi

dirac_eq = (st4d.grad*psi)*I*sig_z - e*A*psi - m*psi*g0
dirac_eq = dirac_eq.simplify()

dirac_eq.Fmt(3, r '%\\text{Dirac Equation}\\;\\;}\\ \\nabla \\bm{\\psi} '+\\
r ' I \\sigma_{z} - e\\bm{A}\\bm{\\psi} - m\\bm{\\psi}\\gamma_{t} = 0')
xpdf(paper='landscape', prog=True)
```

## Code Output:

4-Vector Potential  $\mathbf{A} = A^t \gamma_t + A^x \gamma_x + A^y \gamma_y + A^z \gamma_z$

8-component real spinor  $\psi = \psi + \psi^{tx} \gamma_t \wedge \gamma_x + \psi^{ty} \gamma_t \wedge \gamma_y + \psi^{tz} \gamma_t \wedge \gamma_z + \psi^{xy} \gamma_x \wedge \gamma_y + \psi^{xz} \gamma_x \wedge \gamma_z + \psi^{yz} \gamma_y \wedge \gamma_z + \psi^{txyz} \gamma_t \wedge \gamma_x \wedge \gamma_y \wedge \gamma_z$

Dirac Equation  $\nabla \psi I \sigma_z - e \mathbf{A} \psi - m \psi \gamma_t = 0 =$

$$\begin{aligned} & (-e A^t \psi - e A^x \psi^{tx} - e A^y \psi^{ty} - e A^z \psi^{tz} - m \psi - \partial_y \psi^{tx} - \partial_z \psi^{txyz} + \partial_x \psi^{ty} + \partial_t \psi^{xy}) \gamma_t \\ & + (-e A^t \psi^{tx} - e A^x \psi - e A^y \psi^{xy} - e A^z \psi^{xz} + m \psi^{tx} + \partial_y \psi - \partial_t \psi^{ty} - \partial_x \psi^{xy} + \partial_z \psi^{yz}) \gamma_x \\ & + (e A^x \psi^{xy} - e A^y \psi - e A^z \psi^{yz} + (-e A^t + m) \psi^{ty} - \partial_x \psi + \partial_t \psi^{tx} - \partial_y \psi^{xy} - \partial_z \psi^{xz}) \gamma_y \\ & + (e A^x \psi^{xz} + e A^y \psi^{yz} - e A^z \psi + (-e A^t + m) \psi^{tz} + \partial_t \psi^{txyz} - \partial_z \psi^{xy} + \partial_y \psi^{xz} - \partial_x \psi^{yz}) \gamma_z \\ & + (e A^x \psi^{ty} - e A^y \psi^{tx} - e A^z \psi^{txyz} + (-e A^t - m) \psi^{xy} - \partial_t \psi + \partial_x \psi^{tx} + \partial_y \psi^{ty} + \partial_z \psi^{tz}) \gamma_t \wedge \gamma_x \wedge \gamma_y \\ & + (-e A^t \psi^{xz} + e A^x \psi^{tz} + e A^y \psi^{txyz} - e A^z \psi^{tx} - m \psi^{xz} + \partial_x \psi^{txyz} + \partial_z \psi^{ty} - \partial_y \psi^{tz} - \partial_t \psi^{yz}) \gamma_t \wedge \gamma_x \wedge \gamma_z \\ & + (-e A^t \psi^{yz} - e A^x \psi^{txyz} + e A^y \psi^{tz} - e A^z \psi^{ty} - m \psi^{yz} - \partial_z \psi^{tx} + \partial_y \psi^{txyz} + \partial_x \psi^{tz} + \partial_t \psi^{xz}) \gamma_t \wedge \gamma_y \wedge \gamma_z \\ & + (-e A^t \psi^{txyz} - e A^x \psi^{yz} + e A^y \psi^{xz} - e A^z \psi^{xy} + m \psi^{txyz} + \partial_z \psi - \partial_t \psi^{tz} - \partial_x \psi^{xz} - \partial_y \psi^{yz}) \gamma_x \wedge \gamma_y \wedge \gamma_z \end{aligned}$$