

Program:

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import sys
from sympy import symbols, sin
from sympy.galgebra.printer import Format, xpdf
from sympy.galgebra.ga import Ga

Format()
X = (r, th, phi) = symbols('r theta phi')
s3d = Ga('e_r e_theta e_phi', g=[1, r**2, r**2*sin(th)**2], coords=X, norm=True)
(er, eth, ephi) = s3d.mv()
grad = s3d.grad

f = s3d.mv('f', 'scalar', f=True)
A = s3d.mv('A', 'vector', f=True)
B = s3d.mv('B', 'bivector', f=True)

print 'f =', f
print 'A =', A
print 'B =', B

print 'grad*f =', grad*f
print 'grad|A =', grad|A
print '-I*(grad^A) =', (-s3d.i*(grad^A)).simplify()
print 'grad^B =', grad^B
print r'%\nabla\cdot\lp\nabla f\rp =', s3d.grad|(s3d.grad*f)
xpdf(paper='letter', prog=True)
```

Code Output:

$$\begin{aligned} f &= f \\ A &= A^r \mathbf{e}_r + A^\theta \mathbf{e}_\theta + A^\phi \mathbf{e}_\phi \\ B &= B^{r\theta} \mathbf{e}_r \wedge \mathbf{e}_\theta + B^{r\phi} \mathbf{e}_r \wedge \mathbf{e}_\phi + B^{\phi\phi} \mathbf{e}_\theta \wedge \mathbf{e}_\phi \\ \nabla f &= \partial_r f \mathbf{e}_r + \frac{1}{r} \partial_\theta f \mathbf{e}_\theta + \frac{\partial_\phi f}{r \sin(\theta)} \mathbf{e}_\phi \\ \nabla \cdot A &= \frac{1}{r} \left(r \partial_r A^r + 2A^r + \frac{A^\theta}{\tan(\theta)} + \partial_\theta A^\theta + \frac{\partial_\phi A^\phi}{\sin(\theta)} \right) \\ -I(\nabla \wedge A) &= \frac{1}{r} \left(\frac{A^\phi}{\tan(\theta)} + \partial_\theta A^\phi - \frac{\partial_\phi A^\theta}{\sin(\theta)} \right) \mathbf{e}_r + \frac{1}{r} \left(-r \partial_r A^\phi - A^\phi + \frac{\partial_\phi A^r}{\sin(\theta)} \right) \mathbf{e}_\theta + \frac{1}{r} (r \partial_r A^\theta + A^\theta - \partial_\theta A^r) \mathbf{e}_\phi \\ \nabla \wedge B &= \frac{1}{r} \left(r \partial_r B^{\phi\phi} - \frac{B^{r\phi}}{\tan(\theta)} + 2B^{\phi\phi} - \partial_\theta B^{r\phi} + \frac{\partial_\phi B^{r\theta}}{\sin(\theta)} \right) \mathbf{e}_r \wedge \mathbf{e}_\theta \wedge \mathbf{e}_\phi \\ \nabla \cdot (\nabla f) &= \frac{1}{r^2} \left(r^2 \partial_r^2 f + 2r \partial_r f + \partial_\theta^2 f + \frac{\partial_\theta f}{\tan(\theta)} + \frac{\partial_\phi^2 f}{\sin^2(\theta)} \right) \end{aligned}$$