PHM Users' Guide

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  author={Zhang, Rongrong and Hu, Ming and Zhu, Yu,
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}
```

1 Introduction

Piecewise helical model (PHM) is a parsimonious, easy to interpret, and robust model for inferring three-dimensional (3D) chromosomal structure from Hi-C data. PHM takes the Hi-C contact matrix and local genomic features (restriction enzyme cutting frequencies, GC content and sequence uniqueness) as input and produces, via MCMC computation, the posterior distribution of three-dimensional (3D) chromosomal structure.

In Piecewise Helical Model, we assume that chromatin within a topologically associating domain exhibits a consensus spatial organization among the cell population. Additionally, it is known from geometry that any 3D curve can be uniquely determined by its local curvature and torsion. As a special case, a constant curvature and constant torsion lead to a helical curve. Analogous to the fact that any continuous function can be approximated by a constant at each point, the curvature and torsion of an arbitrary 3D curve can be approximated by piecewise constant functions. Therefore, any continuous 3D curve can be approximated by several well-connected helixes, which we refer to as a piecewise helical curve. Based on this, we further assume that chromatin folds like a piecewise helical curve in three dimension space.

2 How to Run PHM

The full command is:
./phm -i heatmap_filename -v covariates_filename -NP no_of_helixpieces

-NG no_of_iteration -NT tune_interval -SEED seed

heatmap_filename: string of characters, file name of the input Hi-C contact matrix.

covariates_filename: string of characters, file name of the input local genomic features.

no_of_helixpieces: integers, number of helixes within the piecewise helical curve. Default value is 2.

no_of_iteration: integers, number of Gibbs sampler iterations. Default value is 5,000.

tune_interval: integers, length of tune interval in HMC. Default value is 50. seed: integers, seed for gsl random number generator. Default value is 1. output_directory: string of characters, output directory

Example:

./phm -i heatmap.txt -v cov.txt -NP 2 -NG 5000 -NT 50 -SEED 1

3 Input Files

3.1 Format of input Hi-C contact matrix

Assume the genomic region of interest contains N loci. The input file of Hi-C contact matrix is a $N \times N$ symmetric matrix separated by the tab delimiter. All off-diagonal numbers should be non-negative integers. All diagonal numbers should be zero. The number in the (i,j) th cell is the total number of Hi-C reads spanning the i th locus and the j th locus.

Example:

```
0
      197
                          140
                                147
                                       102
                                             122
             175
                   154
197
       0
             210
                   138
                          124
                                 98
                                       84
                                              102
                                                    . . .
175
      210
              0
                   348
                          143
                                110
                                       115
                                              130
154
      138
             348
                    0
                          176
                                       202
                                              167
                                171
140
      124
             143
                   176
                          0
                                448
                                       248
                                              153
147
                          448
                                       303
       98
             110
                   171
                                 0
                                              180
102
       84
             115
                   202
                          248
                                303
                                        0
                                              243
                                                    . . .
122
      102
             130
                   167
                          153
                                180
                                       243
                                              0
```

3.2 Format of input local genomic features

The input file of local genomic features is a $N \times 6$ matrix separated by the table delimiter. For the i th row $(i-1, \dots, N)$:

Column 1: chromosome name for the i th locus.

Column 2: start position for the i th locus.

Column 3: end position for the i th locus.

Column 4: number of restriction enzyme cut fragment ends in the i th locus

(positive integer).

Column 5: mean GC content in the i th locus (positive real number).

Column 6: mean mappability score in the i th locus (positive real number).

Example:

```
22
     1.6e + 07
                 1.7e + 07
                            389
                                   0.4511
                                             0.8831
22
     1.7e + 07
                 1.8e + 07
                            272
                                   0.4534
                                             0.8951
22
     1.8e + 07
                 1.9e + 07
                                   0.5365
                            218
                                             0.9065
22
     1.9e + 07
                 2.0e + 07
                            230
                                   0.4726
                                             0.8704
22
     2.0e + 07
                 2.1e + 07
                            235
                                   0.4366
                                             0.9304
22
     2.1e + 07
                 2.2e + 07
                            400
                                   0.4562
                                             0.9118
22
     2.2e + 07
                 2.3e + 07
                            246
                                   0.4928
                                             0.8788
22
     2.3e + 07
                 2.4e + 07
                            336
                                   0.4595
                                             0.9067
```

4 Output Files

time.txt: start, end and duration of the PHM running time.

mode_loglike.txt: the posterior model of the log likelihood.

record_loglike.txt: the log likelihood in each iteration of the Gibbs sampler (a vector with size no_of_iteration). It can be used to check the convergence of MCMC chain.

mode_p.txt: the posterior mode of the 3D coordinates $(N \times 3 \text{ matrix})$.

record_p.txt: the posterior samplers of the 3D coordinates (no_of_iteration \times 3N matrix). In each row, the 3D coordinates are in the order of: $x_1, y_1, z_1, x_2, y_2, z_2, \dots, x_N, y_N, z_N$.

mode_kappa_tau.txt: the posterior mode of kappas and taus of helixes in the piecewise helical curve (κ, τ) .

Column 1: number of helix.

Column 2: posterior mode of the curvature of the helix(κ).

Column 3: posterior mode of the torsion of the helix(τ).

 $mode_tnb.txt$: the posterior mode of t, n, b vectors in Frenet framework at the change points.

mode_nui.txt: the posterior mode of the nuisance parameters (5×3 matrix).

Row 1: posterior mode of the scaling parameter (β_0) .

Row 2: posterior mode of the association between # of Hi-C reads and spatial distance (β_1).

Row 3: posterior mode of the restriction enzyme effect (β_{enz}) .

Row 4: posterior mode of the GC content effect (β_{qcc}) .

Row 5: posterior mode of the mappability effect (β_{map}) .

Row 6: posterior mode of the overdispersion parameter (φ) .

 $\texttt{record_nui.txt}$: the posterior samplers of the nuisance parameters (no_of_iteration×6 matrix).

Column 1: posterior samples of the scaling parameter (β_0) .

Column 2: posterior samples of the association between # of Hi-C reads and spatial distance (β_1) .

Column 3: posterior samples of the restriction enzyme effect (β_{enz}) .

Column 4: posterior samples of the GC content effect (β_{gcc}) .

Column 5: posterior samples of the mappability effect (β_{map}) .

Column 6: posterior samples of the overdispersion parameter (φ) .

5 Contact

Comments, suggestions, questions are welcomed, and should be directed to Rongrong Zhang.

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