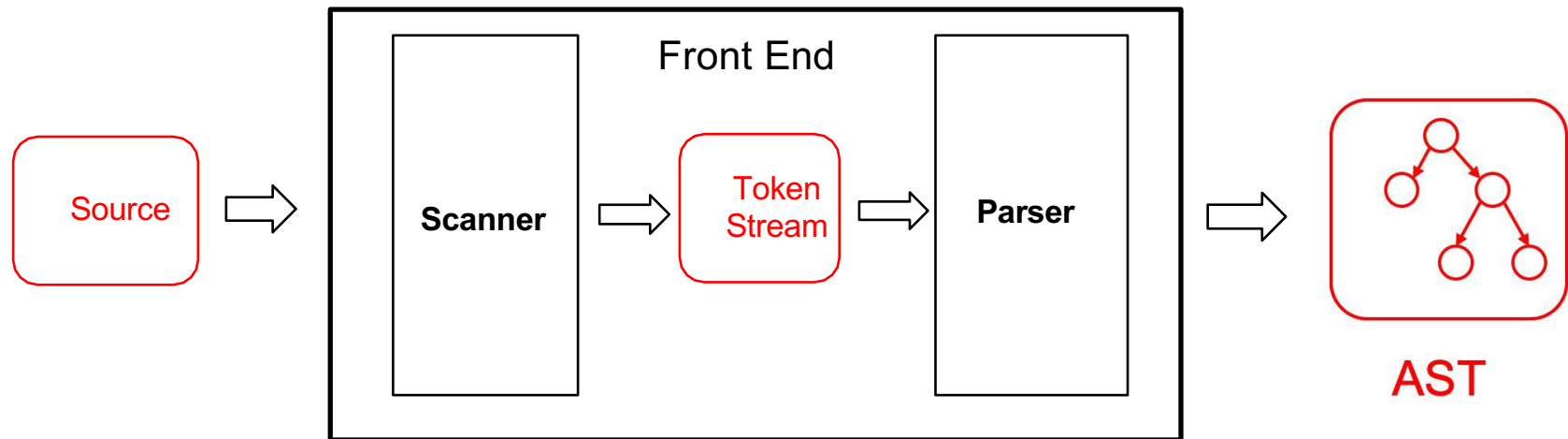


CS 314: Principles of Programming Languages

Parsing

Recall: Front End Scanner and Parser



- **Scanner / lexer / tokenizer** converts program source into **tokens** (keywords, variable names, operators, numbers, etc.) with **regular expressions**
- **Parser** converts tokens into an **AST** (abstract syntax tree) based on a **context free grammar**

Scanning (“tokenizing”)

- Converts textual input into a stream of **tokens**
 - These are the **terminals** in the parser’s CFG
 - Example tokens are keywords, identifiers, numbers, punctuation, etc.
- Scanner typically ignores/eliminates whitespace

Scanning (“tokenizing”)

```
type token =  
    Tok_Num of char  
  | Tok_Sum
```

```
tokenize "1+2" =  
  [Tok_Num '1'; Tok_Sum; Tok_Num '2']
```

A Scanner in OCaml

```
type token =  
  Tok_Num of char  
  | Tok_Sum  
  
let tokenize (s:string) = (* returns token list *)
```

```
let re_num = Str.regexp "[0-9]" (* single digit *)  
let re_add = Str.regexp "+"  
let tokenize str =  
  let rec tok pos s =  
    if pos >= String.length s then  
      []  
    else  
      if (Str.string_match re_num s pos) then  
        let token = Str.matched_string s in  
        (Tok_Num token.[0])::(tok (pos+1) s)  
      else if (Str.string_match re_add s pos) then  
        Tok_Sum::(tok (pos+1) s)  
      else  
        raise (IllegalExpression "tokenize")  
  in  
  tok 0 str
```

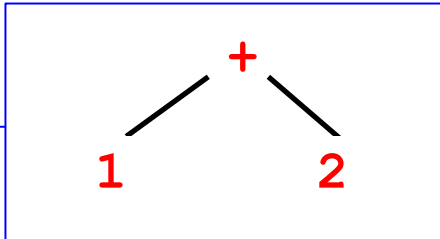
Uses **Str**
library module
for regexps

Parsing (to an AST)

```
type token =  
  Tok_Num of char  
  | Tok_Sum
```

```
type expr =  
  Num of int  
  | Sum of expr * expr
```

```
let tokens = tokenize "1+2" in  
(* tokens = [Tok_Num '1'; Tok_Sum; Tok_Num '2'] *)  
  
parse tokens  
  = Sum (Num 1, Num 2)
```



Implementing Parsers

- Many efficient techniques for parsing
 - LL(k), SLR(k), LR(k), LALR(k)...
 - Take CS 415 for more details
- One simple technique: **recursive descent parsing**
 - This is a **top-down** parsing algorithm
- Other algorithms are **bottom-up**

Top-Down Parsing (Intuition)

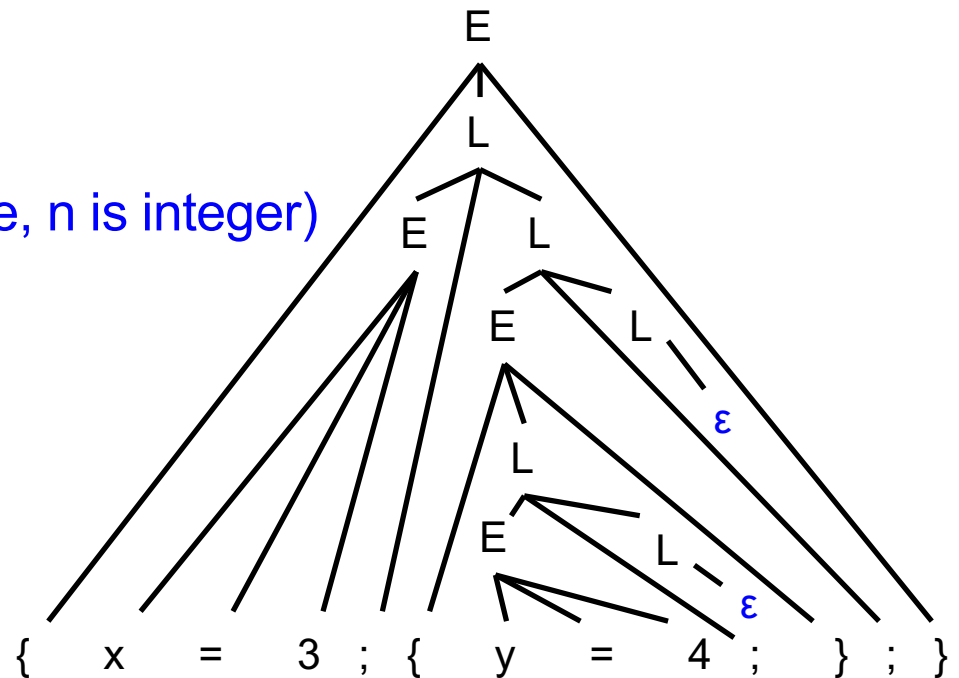
$E \rightarrow \text{id} = n \mid \{ L \}$

$L \rightarrow E ; L \mid \epsilon$

(Assume: id is variable name, n is integer)

Show parse tree for

$\{ x = 3 ; \{ y = 4 ; \} ; \}$



Recursive Descent Parsing

- Goal
 - Can we “parse” a string – does it match our grammar?
 - We will talk about constructing an AST later
- Approach: Try to produce leftmost derivation
 - Begin with start symbol S , and input tokens t
 - Repeat:
 - Rewrite S and consume tokens in t via a production in the grammar
 - Until all tokens matched, or failure

Recursive Descent Parsing

- At each step, we keep track of two facts
 - What grammar element are we trying to match/expand?
 - What is the **lookahead** (next token of the input string)?
- At each step, apply one of three possible cases
 - If we're trying to match a **terminal**
 - If the lookahead is that token, then succeed, advance the lookahead, and continue
 - If we're trying to match a **nonterminal**
 - Pick which production to apply based on the lookahead
 - Otherwise fail with a **parsing error**

Example

$E \rightarrow \text{id} = n \mid \{ L \}$

$L \rightarrow E ; L \mid \varepsilon$

- Here n is an integer and id is an identifier
- One input might be
 - $\{ x = 3; \{ y = 4; \}; \}$
 - This would get turned into a list of tokens
 $\{ x = 3 ; \{ y = 4 ; \} ; \}$
 - And we want to parse it
 - i.e., just determine if it's in the grammar's language; no AST for now

Parsing Example Input

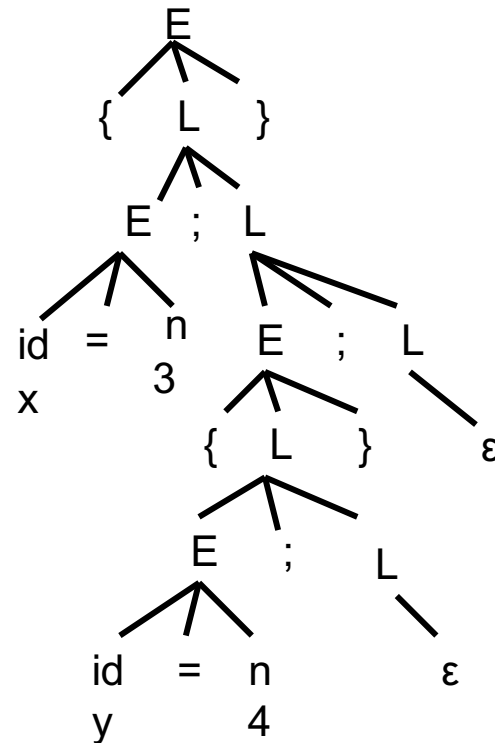
$E \rightarrow id = n \mid \{ L \}$

$L \rightarrow E ; L \mid \epsilon$

$\{ x = 3 ; \{ y = 4 ; \} ; \}$



lookahead



Parsing Example: Previewing the Code

$E \rightarrow id = n \mid \{ L \}$
 $L \rightarrow E ; L \mid \epsilon$

```
let rec parse_E (toks:token list) =  
  match lookahead toks with  
  | Some Tok_Id -> (* E → id = n *)  
    let toks = match_tok toks Tok_Id in  
    let toks = match_tok toks Tok_Eq in  
    match_tok toks Tok_Num  
  | Some Tok_Lbrace -> (* E → { L } *)  
    let toks = match_tok toks Tok_Lbrace in  
    let toks = parse_L toks in  
    match_tok toks Tok_Rbrace  
  | _ -> raise (ParseError "parse_E")
```

```
type token = Tok_Num (* of string *)  
           | Tok_Id (* of string *)  
           | Tok_Eq | Tok_Semi  
           | Tok_Lbrace  
           | Tok_Rbrace  
  
and parse_L (toks:token list) =  
  match lookahead toks with  
  | Some Tok_Id  
  | Some Tok_Lbrace -> (* L → E ; L *)  
    let toks = parse_E toks in  
    let toks = match_tok toks Tok_Semi  
    in parse_L toks  
  | _ ->  
    (* L → ε *) toks
```

Parsing Example: Previewing the Code

$E \rightarrow id = n \mid \{ L \}$
 $L \rightarrow E ; L \mid \epsilon$

```
type token = Tok_Num (* of int *)  
           | Tok_Id  (* of string *)  
           | Tok_Eq  | Tok_Semi  
           | Tok_Lbrace  
           | Tok_Rbrace
```

```
let rec parse_E toks =  
... and parse_L toks = ...
```

```
let tok_list = tokenize "{ x = 3 ; { y = 4 ; } ; }" in  
  (* tok_list = [ Tok_Lbrace; Tok_Id; Tok_Eq; Tok_Num; Tok_Semi; ...] *)  
  parse_E tok_list;;  
  (* returns [] -- successfully parses input *)  
  
let tok_list = tokenize "{ x = ; }" in  
  (* tok_list = [ Tok_Lbrace; Tok_Id; Tok_Eq; Tok_Semi; Tok_Rbrace ] *)  
  parse_E tok_list;;  
  (* raises exception ParseError "bad match" *)
```

Recursive Descent Parsing: Key Step

- Key step: Choosing the right production
- Two approaches
 - Backtracking
 - Choose some production
 - If fails, try different production
 - Parse fails if all choices fail
 - Predictive parsing (what we will do)
 - Analyze grammar to find FIRST sets for productions
 - Compare with lookahead to decide which production to select
 - Parse fails if lookahead does not match FIRST

Selecting a Production

- Motivating example
 - If grammar $S \rightarrow xyz \mid abc$ and lookahead is x
 - Select $S \rightarrow xyz$ since 1st terminal in RHS matches x
 - If grammar $S \rightarrow A \mid B$ $A \rightarrow x \mid y$ $B \rightarrow z$
 - If lookahead is x , select $S \rightarrow A$, since A can derive string beginning with x
- In general
 - Choose a production that can derive a sentential form beginning with the lookahead
 - Need to know what terminal may be **first** in any sentential form derived from a nonterminal / production

First Sets

- Definition
 - **First**(y), for any terminal or nonterminal y , is the set of initial terminals of all strings that y may expand to
 - We'll use this to decide which production to apply
- Example: Given grammar
$$S \rightarrow A \mid B$$
$$A \rightarrow x \mid y$$
$$B \rightarrow z$$
 - $\text{First}(A) = \{ x, y \}$ since $\text{First}(x) = \{ x \}$, $\text{First}(y) = \{ y \}$
 - $\text{First}(B) = \{ z \}$ since $\text{First}(z) = \{ z \}$
- So: If we are parsing S and see x or y , we choose $S \rightarrow A$;
if we see z we choose $S \rightarrow B$

Calculating First(γ)

- For a terminal a
 - $\text{First}(a) = \{ a \}$
- For a nonterminal N
 - If $N \rightarrow \epsilon$, then add ϵ to $\text{First}(N)$
 - If $N \rightarrow \alpha_1 \alpha_2 \dots \alpha_n$, then (note the α_i are all the symbols on the right side of one single production):
 - Add $\text{First}(\alpha_1 \alpha_2 \dots \alpha_n)$ to $\text{First}(N)$, where $\text{First}(\alpha_1 \alpha_2 \dots \alpha_n)$ is defined as
 - $\text{First}(\alpha_1)$ if $\epsilon \notin \text{First}(\alpha_1)$
 - Otherwise $(\text{First}(\alpha_1) - \epsilon) \cup \text{First}(\alpha_2 \dots \alpha_n)$
 - If $\epsilon \in \text{First}(\alpha_i)$ for all i , $1 \leq i \leq n$, then add ϵ to $\text{First}(N)$

First() Examples

$$E \rightarrow \text{id} = n \mid \{ L \}$$
$$L \rightarrow E ; L \mid \varepsilon$$
$$\text{First}(\text{id}) = \{ \text{id} \}$$
$$\text{First}("=") = \{ "=" \}$$
$$\text{First}(n) = \{ n \}$$
$$\text{First}("\{") = \{ "\{" \}$$
$$\text{First}("\}") = \{ "\}" \}$$
$$\text{First}(";") = \{ ";" \}$$
$$\text{First}(E) = \{ \text{id}, "\{", \varepsilon \}$$
$$\text{First}(L) = \{ \text{id}, "\{", \varepsilon \}$$
$$E \rightarrow \text{id} = n \mid \{ L \} \mid \varepsilon$$
$$L \rightarrow E ; L$$
$$\text{First}(\text{id}) = \{ \text{id} \}$$
$$\text{First}("=") = \{ "=" \}$$
$$\text{First}(n) = \{ n \}$$
$$\text{First}("\{") = \{ "\{" \}$$
$$\text{First}("\}") = \{ "\}" \}$$
$$\text{First}(";") = \{ ";" \}$$
$$\text{First}(E) = \{ \text{id}, "\{", \varepsilon \}$$
$$\text{First}(L) = \{ \text{id}, "\{", "\cdot;" \}$$

Quiz #1

Given the following grammar:

S	\rightarrow	$aAB \mid B$
A	\rightarrow	CBC
B	\rightarrow	b
C	\rightarrow	$cC \mid \epsilon$

What is $\text{First}(S)$?

- A. $\{b, c\}$
- B. $\{b\}$
- C. $\{a, b\}$
- D. $\{c\}$

Quiz #1

Given the following grammar:

S	\rightarrow	$aAB \mid B$
A	\rightarrow	CBC
B	\rightarrow	b
C	\rightarrow	$cC \mid \epsilon$

What is $\text{First}(S)$?

- A. $\{b, c\}$
- B. $\{b\}$
- C. $\{a, b\}$**
- D. $\{c\}$

Quiz #2

Given the following grammar:

S	->	aAB
A	->	CBC
B	->	b
C	->	cC ϵ

What is **First(B)**?

- A. {a}
- B. {b, c}
- C. {b}**
- D. {c}

Quiz #2

Given the following grammar:

S	\rightarrow	aAB
A	\rightarrow	CBC
B	\rightarrow	b
C	\rightarrow	$cC \mid \epsilon$

What is $\text{First}(B)$?

- A. $\{a\}$
- B. $\{b, c\}$
- C. $\{b\}$**
- D. $\{c\}$

Quiz #3

Given the following grammar:

S	\rightarrow	aAB
A	\rightarrow	CBC
B	\rightarrow	b
C	\rightarrow	$cC \mid \epsilon$

What is $\text{First}(A)$?

- A. $\{a\}$
- B. $\{b, c\}$
- C. $\{b\}$
- D. $\{c\}$

Quiz #3

Given the following grammar:

S	\rightarrow	aAB
A	\rightarrow	CBC
B	\rightarrow	b
C	\rightarrow	$cC \mid \epsilon$

What is $\text{First}(A)$?

- A. $\{a\}$
- B. $\{b, c\}$**
- C. $\{b\}$
- D. $\{c\}$

Note:

$\text{First}(B) = \{b\}$

$\text{First}(C) = \{c, \epsilon\}$

Recursive Descent Parser Implementation

- For all terminals, use function `match_tok a`
 - If lookahead is `a` it consumes the lookahead by advancing the lookahead to the next token, and returns
 - Fails with a parse error if lookahead is not `a`
- For each nonterminal `N`, create a function `parse_N`
 - Called when we're trying to parse a part of the input which corresponds to (or can be derived from) `N`
 - `parse_S` for the start symbol `S` begins the parse

match_tok, lookahead in OCaml

```
exception ParseError of string

let match_tok tok_list a =
  match tok_list with
  | (h::t) when a = h -> t
  | _ -> raise (ParseError "bad match")

(* used by parse_X *)
let lookahead tok_list =
  match tok_list with
  | [] -> None
  | (h::t) -> Some h
```

Parsing Nonterminals

- The body of `parse_N` for a nonterminal `N` does the following
 - Let $N \rightarrow \beta_1 \mid \dots \mid \beta_k$ be the productions of `N`
 - Here β_i is the entire right side of a production- a sequence of terminals and nonterminals
 - Pick the production $N \rightarrow \beta_i$ such that the lookahead is in $\text{First}(\beta_i)$
 - It must be that $\text{First}(\beta_i) \cap \text{First}(\beta_j) = \emptyset$ for $i \neq j$
 - If there is no such production, but $N \rightarrow \epsilon$ then return
 - Otherwise fail with a parse error
 - Suppose $\beta_i = \alpha_1 \alpha_2 \dots \alpha_n$. Then call `parse_α1()`; ... ; `parse_αn()` to match the expected right-hand side, and return

Example Parser

- Given grammar $S \rightarrow xyz \mid abc$
 - $\text{First}(xyz) = \{ x \}$, $\text{First}(abc) = \{ a \}$
- Parser

```
let parse_S toks =  
  if lookahead toks = Some "x" then (* S → xyz *)  
    let toks = match_tok toks "x" in  
    let toks = match_tok toks "y" in  
    match_tok toks "z"  
  else if lookahead toks = Some "a" then (* S → abc *)  
    let toks = match_tok toks "a" in  
    let toks = match_tok toks "b" in  
    match_tok toks "c"  
  else raise (ParseError "parse_S")
```

Note: We are not producing an AST here; we are only determining if the string is in the language. We'll produce an AST later.

Another Example Parser

- Given grammar $S \rightarrow A \mid B$ $A \rightarrow x \mid y$ $B \rightarrow z$

- $\text{First}(A) = \{ x, y \}, \text{First}(B) = \{ z \}$

- Parser:

Syntax for
*mutually
recursive
functions in
OCaml* –
`parse_S` and
`parse_A` and
`parse_B` can
each call the
other

```
let rec parse_S toks =  
  if lookahead toks = Some "x" ||  
    lookahead toks = Some "y" then  
    parse_A toks (* S → A *)  
  else if lookahead toks = Some "z" then  
    parse_B toks (* S → B *)  
  else raise (ParseError "parse_S")  
and parse_A toks =  
  if lookahead toks = Some "x" then  
    match_tok toks "x" (* A → x *)  
  else if lookahead toks = Some "y" then  
    match_tok toks "y" (* A → y *)  
  else raise (ParseError "parse_A")  
and parse_B toks =  
  ...
```

Execution Trace = Parse Tree

- If you draw the execution trace of the parser
 - You get the parse tree

- Examples

- Grammar

$S \rightarrow xyz$

$S \rightarrow abc$

- String “xyz”

parse_S toks

match_tok toks “x”

match_tok toks “y”

match_tok toks “z”

S
/**|**\n
x y z

- Grammar

$S \rightarrow A | B$

$A \rightarrow x | y$

$B \rightarrow z$

- String “x”

parse_S toks

parse_A toks

match_tok toks “x”

S
|
A
|
x

Predictive Parsing

- This is a **predictive** parser
 - Because the lookahead determines exactly which production to use
- This parsing strategy may fail on some grammars
 - Production First sets overlap
 - Possible infinite recursion
- Does not mean grammar is not usable
 - Just means this parsing method not powerful enough
 - May be able to change grammar

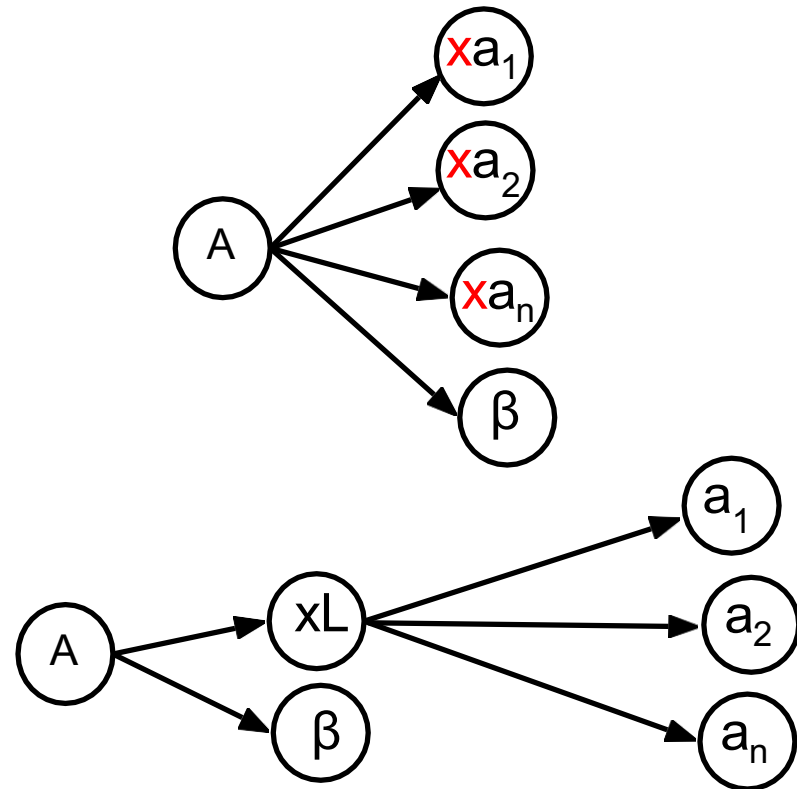
Conflicting First Sets

- Consider parsing the grammar $E \rightarrow ab \mid ac$
 - $\text{First}(ab) = a$
 - $\text{First}(ac) = a$

Parser cannot choose between RHS based on lookahead!
- Parser fails whenever $A \rightarrow \alpha_1 \mid \alpha_2$ and
 - $\text{First}(\alpha_1) \cap \text{First}(\alpha_2) \neq \varepsilon$ or \emptyset
- Solution
 - Rewrite grammar using left factoring

Left Factoring Algorithm

- Given grammar
 - $A \rightarrow x\alpha_1 \mid x\alpha_2 \mid \dots \mid x\alpha_n \mid \beta$
- Rewrite grammar as
 - $A \rightarrow xL \mid \beta$
 - $L \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid \alpha_n$
- Repeat as necessary



Left Factoring Algorithm

- Given grammar
 - $A \rightarrow x\alpha_1 \mid x\alpha_2 \mid \dots \mid x\alpha_n \mid \beta$
- Rewrite grammar as
 - $A \rightarrow xL \mid \beta$
 - $L \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid \alpha_n$
- Examples
 - $S \rightarrow ab \mid ac \quad \Rightarrow S \rightarrow aL \quad L \rightarrow b \mid c$
 - $S \rightarrow abcA \mid abB \mid a \quad \Rightarrow S \rightarrow aL \quad L \rightarrow bcA \mid bB \mid \epsilon$
 - $L \rightarrow bcA \mid bB \mid \epsilon \quad \Rightarrow L \rightarrow bL' \mid \epsilon \quad L' \rightarrow cA \mid B$

Alternative Approach

- Change structure of parser
 - First match **common prefix** of productions
 - Then use lookahead to chose between productions
- Example
 - Consider parsing the grammar $E \rightarrow a+b \mid a*b \mid a$

```
let parse_E toks =  
  let toks = match_tok "a" in (* common prefix *)  
  if lookahead toks = Some "+" then (* E → a+b *)  
    let toks = match_tok toks "+" in  
    match_tok toks "b")  
  else if lookahead toks = Some "*" then (* E → a*b *)  
    let toks = match_tok toks "*" in  
    match_tok toks "b")  
  else toks (* E → a *)
```

Left Recursion

- Consider grammar $S \rightarrow Sa \mid \epsilon$
 - Try writing parser

```
let rec parse_S toks =  
  if lookahead toks = Some "a" then  
    let toks = parse_S toks in  
    match_tok toks "a" (* S → Sa *)  
  else toks
```

- Body of `parse_S toks` has an infinite loop!
 - Infinite loop occurs in grammar with **left recursion**

Right Recursion

- Consider grammar $S \rightarrow aS \mid \epsilon$ Again, $\text{First}(aS) = a$
 - Try writing parser

```
let rec parse_S toks =  
  if lookahead toks = Some "a" then  
    let toks = match_tok toks "a" in  
    parse_S toks (* S → aS *)  
  else toks
```

- Will `parse_S` toks infinite loop?
 - Invoking `match_tok` will advance lookahead, eventually stop
- Top-down parsers handles grammar w/ right recursion

Algorithm To Eliminate Left Recursion

- Given grammar
 - $A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_n \mid \beta$
 - β must exist or no derivation will yield a string
- Rewrite grammar as (repeat as needed)
 - $A \rightarrow \beta L$
 - $L \rightarrow \alpha_1 L \mid \alpha_2 L \mid \dots \mid \alpha_n L \mid \epsilon$
- Replaces left recursion with right recursion
- Examples
 - $S \rightarrow Sa \mid \epsilon$ $\Rightarrow S \rightarrow L \quad L \rightarrow aL \mid \epsilon$
 - $S \rightarrow Sa \mid Sb \mid c$ $\Rightarrow S \rightarrow cL \quad L \rightarrow aL \mid bL \mid \epsilon$

Quiz #4

- What does the following code parse?

```
let parse_S toks =  
  if lookahead toks = Some "a" then  
    let toks = match_tok toks "a" in  
    let toks = match_tok toks "x" in  
    let toks = match_tok toks "y" in  
    match_tok toks "q"  
  else  
    raise (ParseError "parse_S")
```

- A. $S \rightarrow axyq$
- B. $S \rightarrow a \mid q$
- C. $S \rightarrow aaxy \mid qq$
- D. $S \rightarrow axy \mid q$

Quiz #4

- What does the following code parse?

```
let parse_S toks =  
  if lookahead toks = Some "a" then  
    let toks = match_tok toks "a" in  
    let toks = match_tok toks "x" in  
    let toks = match_tok toks "y" in  
    match_tok toks "q"  
  else  
    raise (ParseError "parse_S")
```

- A. $S \rightarrow axyq$
- B. $S \rightarrow a \mid q$
- C. $S \rightarrow aaxy \mid qq$
- D. $S \rightarrow axy \mid q$

Quiz #5

- What does the following code parse?

```
let rec parse_S toks =  
  if lookahead toks = Some "a" then  
    let toks = match_tok toks "a" in  
    parse_S toks  
  else if lookahead toks = Some "q" then  
    let toks = match_tok toks "q" in  
    match_tok toks "p")  
  else  
    raise (ParseError "parse_S")
```

- A. $S \rightarrow aS \mid qp$
- B. $S \rightarrow a \mid S \mid qp$
- C. $S \rightarrow aqSp$
- D. $S \rightarrow a \mid q$

Quiz #5

- What does the following code parse?

```
let rec parse_S toks =  
  if lookahead toks = Some "a" then  
    let toks = match_tok toks "a" in  
    parse_S toks  
  else if lookahead toks = Some "q" then  
    let toks = match_tok toks "q" in  
    match_tok toks "p")  
  else  
    raise (ParseError "parse_S")
```

- A. $S \rightarrow aS \mid qp$
- B. $S \rightarrow a \mid S \mid qp$
- C. $S \rightarrow aqSp$
- D. $S \rightarrow a \mid q$

Quiz #6

Can recursive descent parse this grammar?

$S \rightarrow aBa$
$B \rightarrow bC$
$C \rightarrow \varepsilon \mid Cc$

- A. Yes
- B. No

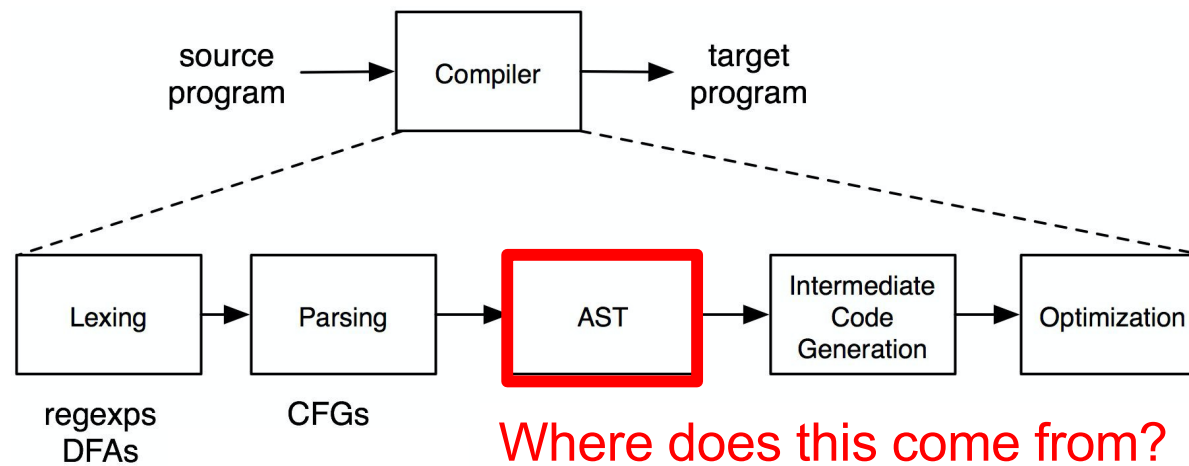
Quiz #6

Can recursive descent parse this grammar?

$S \rightarrow aBa$
$B \rightarrow bC$
$C \rightarrow \varepsilon \mid Cc$

- A. Yes
- B. No**
(due to left recursion)

Recall: The Compilation Process

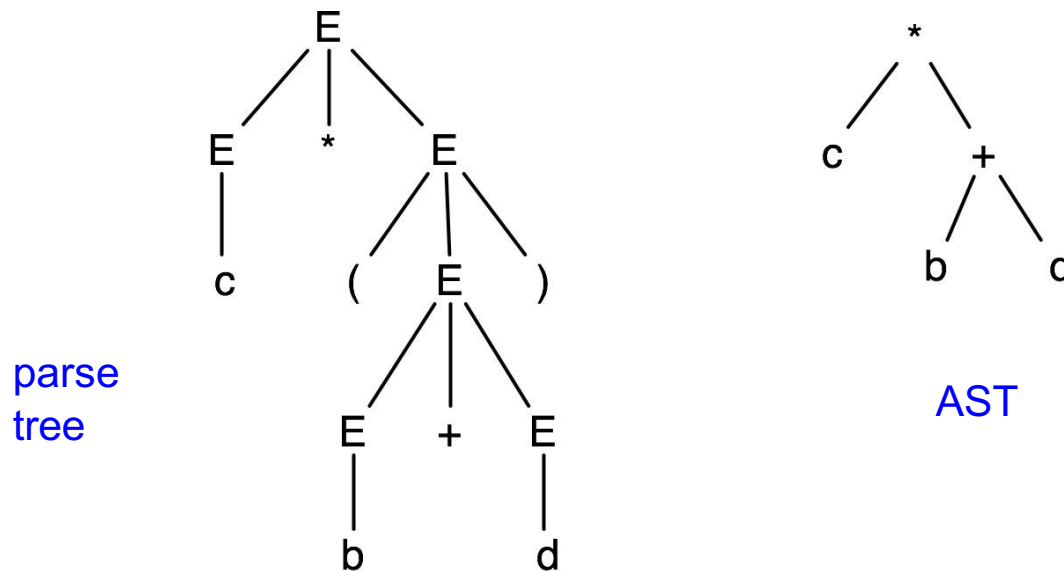


Parse Trees to ASTs

- Parse trees are a representation of a parse, with all of the syntactic elements present
 - Parentheses
 - Extra nonterminals for precedence
- This extra stuff is needed for parsing
- Lots of that stuff is not needed to actually implement a compiler or interpreter
 - So in the abstract syntax tree we get rid of it

Abstract Syntax Trees (ASTs)

- An abstract syntax tree is a more compact, abstract representation of a parse tree, with only the essential parts



Example: Simple Assignment

$E \rightarrow id = n \mid \{ L \}$
 $L \rightarrow E ; L \mid \epsilon$

```
type token = Tok_Num (* of string *)  
            | Tok_Id  (* of string *)  
            | Tok_Eq  | Tok_Semi  
            | Tok_Lbrace  
            | Tok_Rbrace
```

- Here, *id* stands for a general identifier (variable), like **a**, **bob**, **chandra**, **toy**, etc.
 - The scanner will match this via a regular expression, and can track of what the actual string was; we'll ignore here
- Similar situation for *n*, which represents an integer

Matching Strings; no AST

$E \rightarrow id = n \mid \{ L \}$
 $L \rightarrow E ; L \mid \epsilon$

```
let rec parse_E (toks:token list) =  
  match lookahead toks with  
  | Some Tok_Id -> (* E → id = n *)  
    let toks = match_tok toks Tok_Id in  
    let toks = match_tok toks Tok_Eq in  
    match_tok toks Tok_Num  
  | Some Tok_Lbrace -> (* E → { L } *)  
    let toks = match_tok toks Tok_Lbrace in  
    let toks = parse_L toks in  
    match_tok toks Tok_Rbrace  
  | _ -> raise (ParseError "parse_E")
```

```
type token = Tok_Num (* of string *)  
            | Tok_Id (* of string *)  
            | Tok_Eq | Tok_Semi  
            | Tok_Lbrace  
            | Tok_Rbrace  
  
and parse_L (toks:token list) =  
  match lookahead toks with  
  | Some Tok_Id  
  | Some Tok_Lbrace -> (* L → E ; L *)  
    let toks = parse_E toks in  
    let toks = match_tok toks Tok_Semi  
    in parse_L toks  
  | _ ->  
    (* L → ε *) toks
```

Defining the AST

$E \rightarrow id = n \mid \{ L \}$
 $L \rightarrow E ; L \mid \epsilon$

```
type token = Tok_Num of string
            | Tok_Id  of string
            | Tok_Eq  | Tok_Semi
            | Tok_Lbrace
            | Tok_Rbrace
```

```
type stmt =
  | Assign of string * int
  | Block  of stmt list
```

- The AST is just a sequence of assignment statements

Parsing, producing AST

$$E \rightarrow id = n \mid \{ L \}$$
$$L \rightarrow E ; L \mid \varepsilon$$

```
let rec parse_E toks: (token list * stmt) =
  match lookahead toks with
  | Some (Tok_Id v) ->
    let toks = match_tok toks (Tok_Id v) in
    let toks = match_tok toks Tok_Eq in
    let Some (Tok_Num n) = lookahead toks in
    let toks = match_tok toks (Tok_Num n) in
    toks, Assign (v, int_of_string n)
  | Some Tok_Lbrace ->
    let toks = match_tok toks Tok_Lbrace in
    let toks, stms = parse_L toks in
    let toks = match_tok toks Tok_Rbrace in
    toks, Block stms
  | _ -> raise (ParseError "parse_E")
```

```
type token = Tok_Num of string
            | Tok_Id of string
            | Tok_Eq | Tok_Semi
            | Tok_Lbrace
            | Tok_Rbrace
```

```
type stmt =
  Assign of string * int
  | Block of stmt list
```

```
and parse_L toks: (token list * stmt list) =
  match lookahead toks with
  | Some (Tok_Id _)
  | Some Tok_Lbrace ->
    let toks, stm = parse_E toks in
    let toks = match_tok toks Tok_Semi in
    let toks, stms = parse_L toks in
    toks, stm :: stms
  | _ -> toks, []
```