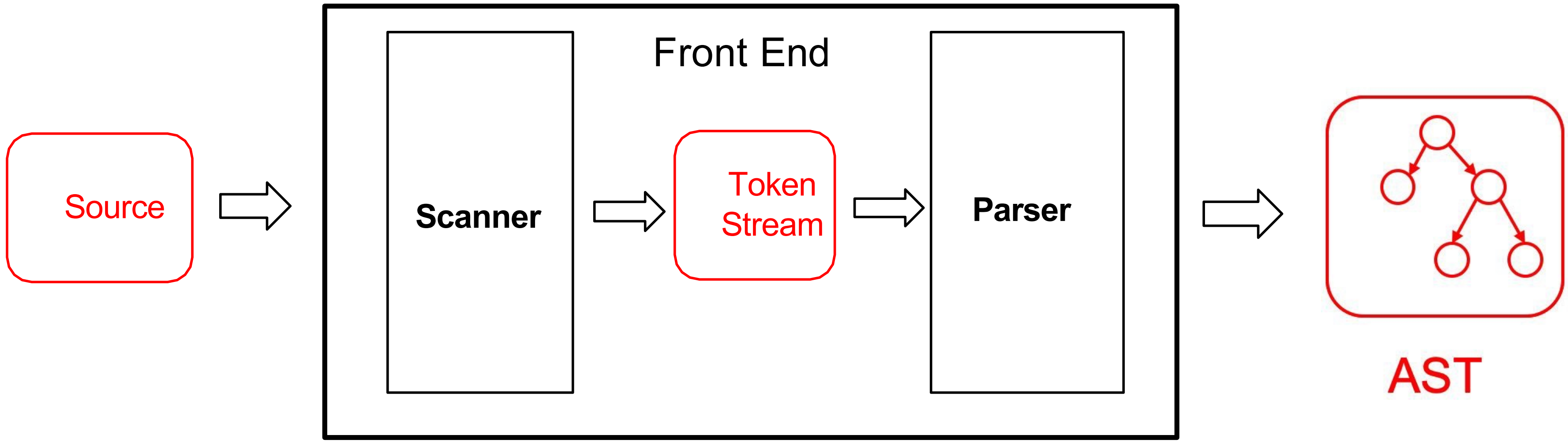
CS 314: Principles of Programming Languages

Parsing

Recall: Front End Scanner and Parser



- Scanner / lexer / tokenizer converts program source into tokens (keywords, variable names, operators, numbers, etc.) with regular expressions
- Parser converts tokens into an AST (abstract syntax tree) based on a context free grammar

Scanning ("tokenizing")

- Converts textual input into a stream of tokens
  - These are the terminals in the parser's CFG
  - Example tokens are keywords, identifiers, numbers, punctuation, etc.

- Scanner typically ignores/eliminates whitespace

Scanning ("tokenizing")

```
type token =
    Tok_Num of char
  | Tok_Sum
```

```
tokenize "1+2" =
  [Tok_Num '1'; Tok_Sum; Tok_Num '2']
```

A Scanner in OCaml

```
type token =
   Tok_Num of char
 | Tok_Sum

let tokenize (s:string) = (* returns token list *)
```

```
let re_num = Str.regexp "[0-9]" (* single digit *)
let re_add = Str.regexp "+"
let tokenize str =
 let rec tok pos s =
   if pos >= String.length s then
     []
   else
     if (Str.string_match re_num s pos) then
       let token = Str.matched_string s in
         (Tok_Num token.[0])::(tok (pos+1) s)
     else if (Str.string_match re_add s pos) then
       Tok_Sum::(tok (pos+1) s)
     else
       raise (IllegalExpression "tokenize")
 in
 tok 0 str
```

Uses **Str** library module for regexps

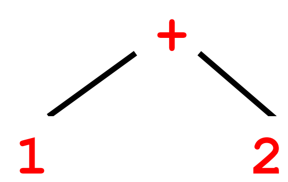
Parsing (to an AST)

```
type token =
   Tok_Num of char
 | Tok_Sum
```

```
type expr =
  Num of int
| Sum of expr * expr
```

```
let tokens = tokenize "1+2" in
(* tokens = [Tok_Num '1'; Tok_Sum; Tok_Num '2'] *)

parse tokens
  = Sum (Num 1, Num 2)
```



Implementing Parsers

- Many efficient techniques for parsing
  - LL(k), SLR(k), LR(k), LALR(k)…
  - Take CS 415 for more details
- One simple technique: recursive descent parsing
  - This is a top-down parsing algorithm
- Other algorithms are bottom-up

Top-Down Parsing (Intuition)

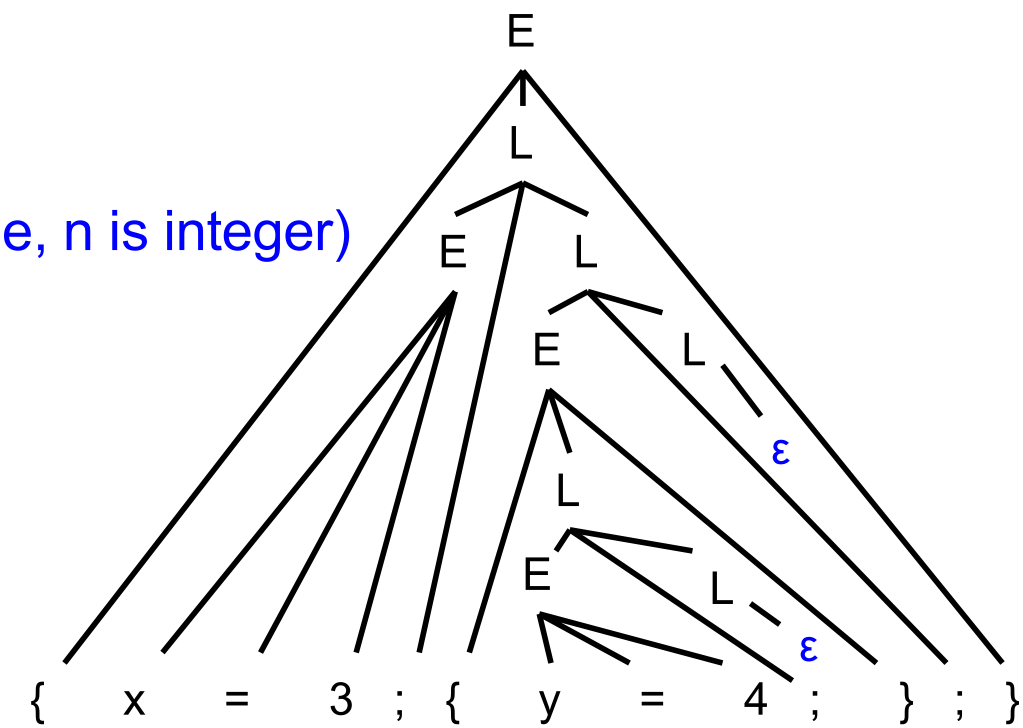
$E \rightarrow$ id = n | { L }

$L \rightarrow$ E ; L | ε

(Assume: id is variable name, n is integer)

Show parse tree for

{ x = 3 ; { y = 4 ; } ; }



Recursive Descent Parsing

- Goal
  - Can we “parse” a string – does it match our grammar?
    - We will talk about constructing an AST later

- Approach: Try to produce leftmost derivation

  Begin with start symbol S, and input tokens t

  Repeat:

  Rewrite S and consume tokens in t via a production in the grammar

  Until all tokens matched, or failure

Recursive Descent Parsing

- At each step, we keep track of two facts
  - What grammar element are we trying to match/expand?
  - What is the lookahead (next token of the input string)?
- At each step, apply one of three possible cases
  - If we're trying to match a terminal
    - If the lookahead is that token, then succeed, advance the lookahead, and continue
  - If we're trying to match a nonterminal
    - Pick which production to apply based on the lookahead
  - Otherwise fail with a parsing error

Example

$E \rightarrow$ id = n | { L }

$L \rightarrow E$; L | ε

- Here n is an integer and id is an identifier

- One input might be
  - { x = 3; { y = 4; }; }
  - This would get turned into a list of tokens

    { x = 3 ; { y = 4 ; } ; }
  - And we want to parse it
    - i.e., just determine if it's in the grammar's language; no AST for now

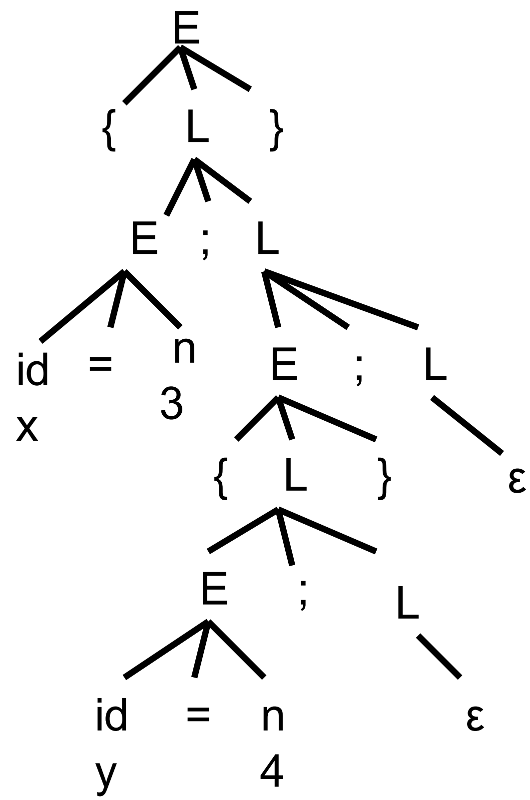
Parsing Example Input

$E \rightarrow id = n \mid \{ L \}$

$L \rightarrow E \; ; \; L \mid \varepsilon$

{ x = 3 ; { y = 4 ; } ; }

lookahead



Parsing Example: Previewing the Code

E → *id* = *n* | { L }
L → E ; L | ε

```
type token = Tok_Num (* of string *)
           | Tok_Id (* of string *)
           | Tok_Eq | Tok_Semi
           | Tok_Lbrace
           | Tok_Rbrace
```

```
let rec parse_E (toks:token list) =
  match lookahead toks with
   | Some Tok_Id -> (* E → id = n *)
    let toks = match_tok toks Tok_Id in
    let toks = match_tok toks Tok_Eq in
    match_tok toks Tok_Num
   | Some Tok_Lbrace -> (* E → { L } *)
    let toks = match_tok toks Tok_Lbrace in
    let toks = parse_L toks in
    match_tok toks Tok_Rbrace
   | _ -> raise (ParseError "parse_E")
```

```
and parse_L (toks:token list) =
  match lookahead toks with
   | Some Tok_Id
   | Some Tok_Lbrace -> (* L → E ; L *)
    let toks = parse_E toks in
    let toks = match_tok toks Tok_Semi
    in parse_L toks
   | _ ->
    (* L → ε *) toks
```

Parsing Example: Previewing the Code

$E \rightarrow id = n \mid \{ L \}$
$L \rightarrow E ; L \mid \varepsilon$

```
type token = Tok_Num (* of int *)
           | Tok_Id (* of string *)
           | Tok_Eq | Tok_Semi
           | Tok_Lbrace
           | Tok_Rbrace
```

```
let rec parse_E toks =
… and parse_L toks = …
```

```
  let tok_list = tokenize "{ x = 3 ; { y = 4 ; } ; }" in
    (* tok_list = [ Tok_Lbrace; Tok_Id; Tok_Eq; Tok_Num; Tok_Semi; …] *)
  parse_E tok_list;;
    (* returns [] -- successfully parses input *)

  let tok_list = tokenize "{ x = ; }" in
    (* tok_list = [ Tok_Lbrace; Tok_Id; Tok_Eq; Tok_Semi; Tok_Rbrace ] *)
  parse_E tok_list;;
    (* raises exception ParseError "bad match" *)
```

Recursive Descent Parsing: Key Step

- Key step: Choosing the right production
- Two approaches
  - Backtracking
    - Choose some production
    - If fails, try different production
    - Parse fails if all choices fail
  - Predictive parsing (what we will do)
    - Analyze grammar to find FIRST sets for productions
    - Compare with lookahead to decide which production to select
    - Parse fails if lookahead does not match FIRST

Selecting a Production

- Motivating example
  - If grammar $S \rightarrow xyz \mid abc$ and lookahead is x
    - Select $S \rightarrow xyz$ since 1st terminal in RHS matches x
  - If grammar $S \rightarrow A \mid B \quad A \rightarrow x \mid y \quad B \rightarrow z$
    - If lookahead is x, select $S \rightarrow A$, since A can derive string beginning with x
- In general
  - Choose a production that can derive a sentential form beginning with the lookahead
  - Need to know what terminal may be first in any sentential form derived from a nonterminal / production

First Sets

- Definition
  - First(γ), for any terminal or nonterminal γ, is the set of initial terminals of all strings that γ may expand to
  - We'll use this to decide which production to apply
- Example: Given grammar

  $S \rightarrow A \mid B$

  $A \rightarrow x \mid y$

  $B \rightarrow z$

  - First(A) = { x, y } since First(x) = { x }, First(y) = { y }
  - First(B) = { z } since First(z) = { z }
- So: If we are parsing S and see x or y, we choose $S \rightarrow A$; if we see z we choose $S \rightarrow B$

Calculating First(γ)

- For a terminal a
  - $\text{First}(a) = \{ a \}$
- For a nonterminal N
  - If $N \rightarrow \varepsilon$, then add ε to First(N)
  - If $N \rightarrow \alpha_1\ \alpha_2\ \ldots\ \alpha_n$, then (note the α_i are all the symbols on the right side of one single production):
    - Add First($\alpha_1\alpha_2\ \ldots\ \alpha_n$) to First($N$), where First($\alpha_1\ \alpha_2\ \ldots\ \alpha_n$) is defined as
      - First(α_1) if $\varepsilon \notin \text{First}(\alpha_1)$
      - Otherwise $(\text{First}(\alpha_1) - \varepsilon) \cup \text{First}(\alpha_2\ \ldots\ \alpha_n)$
    - If $\varepsilon \in \text{First}(\alpha_i)$ for all i, $1 \le i \le n$, then add ε to First(N)

First( ) Examples

$E \rightarrow id = n \mid \{ L \}$

$L \rightarrow E ; L \mid \varepsilon$

First(id) = { id }

First("=") = { "=" }

First(n) = { n }

First("{")= { "{" }

First("}")= { "}" }

First(";")= { ";" }

First(E) = { id, "{" }

First(L) = { id, "{", ε }

$E \rightarrow id = n \mid \{ L \} \mid \varepsilon$

$L \rightarrow E ; L$

First(id) = { id }

First("=") = { "=" }

First(n) = { n }

First("{")= { "{" }

First("}")= { "}" }

First(";")= { ";" }

First(E) = { id, "{", ε }

First(L) = { id, "{", ";" }

Quiz #1

Given the following grammar:

```
S -> aAB |B
A -> CBC
B -> b
C -> cC | ε
```

What is First(S)?

A. {b,c}
B. {b}
C. {a,b}
D. {c}

Quiz #1

Given the following grammar:

```
S  ->  aAB  |B
A  ->  CBC
B  ->  b
C  ->  cC  |  ε
```

What is First(S)?

A. {b,c}

B. {b}

C. {a,b}

D. {c}

Quiz #2

Given the following grammar:

```
S -> aAB
A -> CBC
B -> b
C -> cC | ε
```

What is First(B)?

A. {a}
B. {b,c}
C. {b}
D. {c}

Quiz #2

Given the following grammar:

```
S -> aAB
A -> CBC
B -> b
C -> cC | ε
```

What is First(B)?

A. {a}
B. {b,c}
C. {b}
D. {c}

Quiz #3

Given the following grammar:

```
S -> aAB
A -> CBC
B -> b
C -> cC | ε
```

What is First(A)?

```
A.  {a}
B.  {b,c}
C.  {b}
D.  {c}
```

Quiz #3

Given the following grammar:

```
S  ->  aAB
A  ->  CBC
B  ->  b
C  ->  cC  |  ε
```

What is First(A)?

A. {a}

B. {b,c}

C. {b}

D. {c}

Note:

First(B) = **{b}**

First(C) = **{c,ε}**

Recursive Descent Parser Implementation

- For all terminals, use function match_tok a
  - If lookahead is a it consumes the lookahead by advancing the lookahead to the next token, and returns
  - Fails with a parse error if lookahead is not a

- For each nonterminal N, create a function parse_N
  - Called when we're trying to parse a part of the input which corresponds to (or can be derived from) N
  - parse_S for the start symbol S begins the parse

match_tok, lookahead in OCaml

```
exception ParseError of string

let match_tok tok_list a =
  match tok_list with
    (* checks current token; advances on match *)
    | (h::t) when a = h -> t
    | _ -> raise (ParseError "bad match")

(* used by parse_X *)
let lookahead tok_list =
  match tok_list with
  | [] -> None
  | (h::t) -> Some h
```

Parsing Nonterminals

- The body of parse_N for a nonterminal N does the following
  - Let $N \to \beta_1 \mid \ldots \mid \beta_k$ be the productions of N
    - Here β_i is the entire right side of a production- a sequence of terminals and nonterminals
  - Pick the production $N \to \beta_i$ such that the lookahead is in First(β_i)
    - It must be that $\mathrm{First}(\beta_i) \cap \mathrm{First}(\beta_j) = \varnothing$ for $i \neq j$
    - If there is no such production, but $N \to \varepsilon$ then return
    - Otherwise fail with a parse error
  - Suppose $\beta_i = \alpha_1 \alpha_2 \ldots \alpha_n$. Then call parse_$\alpha_1$(); ... ; parse_$\alpha_n$() to match the expected right-hand side, and return

Example Parser

- Given grammar S → xyz | abc
  - First(xyz) = { x }, First(abc) = { a }
- Parser

```
let parse_S toks =
  if lookahead toks = Some "x" then (* S → xyz *)
    let toks = match_tok toks "x" in
    let toks = match_tok toks "y" in
    match_tok toks "z"
  else if lookahead toks = Some "a" then (* S → abc *)
    let toks = match_tok toks "a" in
    let toks = match_tok toks "b" in
    match_tok toks "c"
  else raise (ParseError "parse_S")
```

Note: We are not producing an AST here; we are only determining if the string is in the language. We'll produce an AST later.

Another Example Parser

- Given grammar S → A | B A → x | y B → z
  - First(A) = { x, y }, First(B) = { z }
- Parser:

Syntax for *mutually recursive* functions in OCaml – **parse_S** and **parse_A** and **parse_B** can each call the other

```
let rec parse_S toks =
  if lookahead toks = Some "x" ||
    lookahead toks = Some "y" then
    parse_A toks (* S → A *)
  else if lookahead toks = Some "z" then
    parse_B toks (* S → B *)
  else raise (ParseError "parse_S")
and parse_A toks =
  if lookahead toks = Some "x" then
    match_tok toks "x" (* A → x *)
  else if lookahead toks = Some "y" then
    match_tok toks "y" (* A → y *)
  else raise (ParseError "parse_A")
and parse_B toks =
…
```

Execution Trace = Parse Tree

- If you draw the execution trace of the parser
  - You get the parse tree
- Examples
  - Grammar

    S → xyz

    S → abc
  - String “xyz”

    parse_S toks

      match_tok toks “x”

      match_tok toks “y”

      match_tok toks “z”

```
  S
 /|\
x y z
```

  - Grammar

    S → A | B

    A → x | y

    B → z
  - String “x”

    parse_S toks

      parse_A toks

        match_tok toks “x”

```
S
|
A
|
x
```

Predictive Parsing

- This is a predictive parser
  - Because the lookahead determines exactly which production to use
- This parsing strategy may fail on some grammars
  - Production First sets overlap
  - Possible infinite recursion
- Does not mean grammar is not usable
  - Just means this parsing method not powerful enough
  - May be able to change grammar

Conflicting First Sets

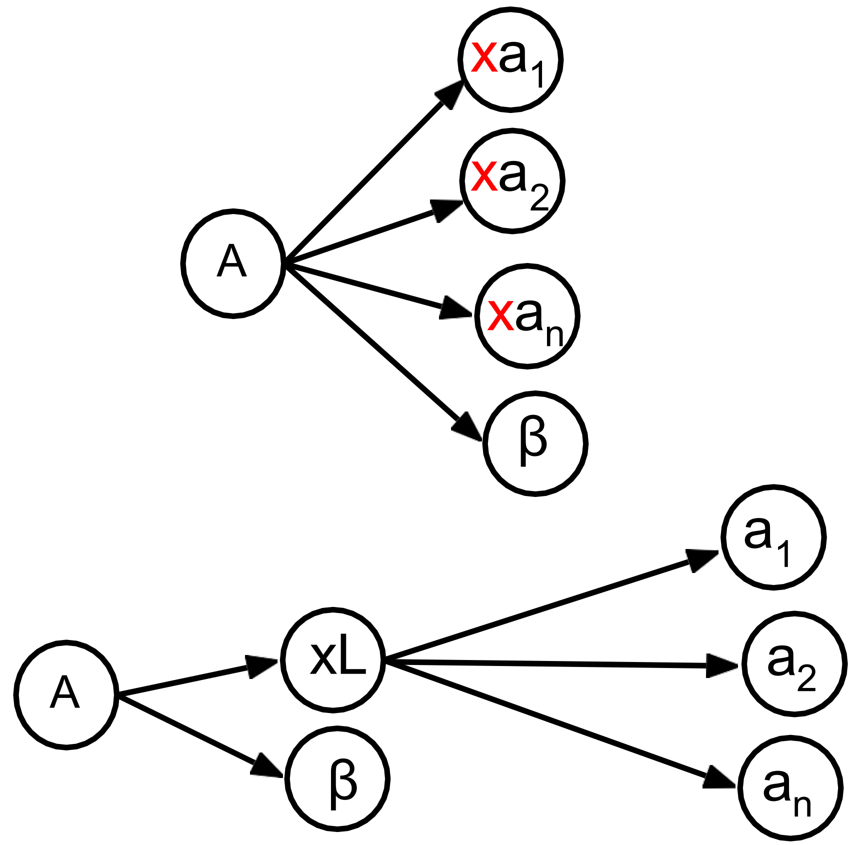
- Consider parsing the grammar $E \rightarrow ab \mid ac$
  - First(ab) = a
  - First(ac) = a

Parser cannot choose between RHS based on lookahead!

- Parser fails whenever $A \rightarrow \alpha_1 \mid \alpha_2$ and
  - $First(\alpha_1) \cap First(\alpha_2)$!= ε or $\varnothing$
- Solution
  - Rewrite grammar using left factoring

Left Factoring Algorithm

- Given grammar
  - $A \rightarrow x\alpha_1 \mid x\alpha_2 \mid \ldots \mid x\alpha_n \mid \beta$
- Rewrite grammar as
  - $A \rightarrow xL \mid \beta$
  - $L \rightarrow \alpha_1 \mid \alpha_2 \mid \ldots \mid \alpha_n$
- Repeat as necessary



Left Factoring Algorithm

- Given grammar
  - $A \rightarrow x\alpha_1 \mid x\alpha_2 \mid \ldots \mid x\alpha_n \mid \beta$
- Rewrite grammar as
  - $A \rightarrow xL \mid \beta$
  - $L \rightarrow \alpha_1 \mid \alpha_2 \mid \ldots \mid \alpha_n$
- Examples
  - $S \rightarrow ab \mid ac$ ⇨ $S \rightarrow aL \quad L \rightarrow b \mid c$
  - $S \rightarrow abcA \mid abB \mid a$ ⇨ $S \rightarrow aL \quad L \rightarrow bcA \mid bB \mid \varepsilon$
  - $L \rightarrow bcA \mid bB \mid \varepsilon$ ⇨ $L \rightarrow bL' \mid \varepsilon \quad L' \rightarrow cA \mid B$

Alternative Approach

- Change structure of parser
  - First match common prefix of productions
  - Then use lookahead to chose between productions
- Example
  - Consider parsing the grammar E → a+b | a*b | a

```
let parse_E toks =
  let toks = match_tok "a" in (* common prefix *)
  if lookahead toks = Some "+" then (* E → a+b *)
    let toks = match_tok toks "+" in
    match_tok toks "b")
  else if lookahead toks = Some "*" then (* E → a*b *)
    let toks = match_tok toks "*" in
    match_tok toks "b")
  else toks (* E → a *)
```

Left Recursion

- Consider grammar $S \rightarrow Sa \mid \varepsilon$
  - Try writing parser

```
let rec parse_S toks =
    if lookahead toks = Some "a" then
        let toks = parse_S toks in
        match_tok "a" (* S → Sa *)
    else toks
```

  - Body of parse_S toks has an infinite loop!
    - Infinite loop occurs in grammar with left recursion

Right Recursion

- Consider grammar S → aS | ε   Again, First(aS) = a
  - Try writing parser

```
let rec parse_S toks =
    if lookahead toks = Some "a" then
      let toks = match_tok "a" in
      parse_S toks (* S → aS *)
    else toks
```

  - Will parse_S toks infinite loop?
    - Invoking match_tok will advance lookahead, eventually stop
  - Top-down parsers handles grammar w/ right recursion

Algorithm To Eliminate Left Recursion

- Given grammar
  - $A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \ldots \mid A\alpha_n \mid \beta$
    - β must exist or no derivation will yield a string
- Rewrite grammar as (repeat as needed)
  - $A \rightarrow \beta L$
  - $L \rightarrow \alpha_1 L \mid \alpha_2 L \mid \ldots \mid \alpha_n L \mid \varepsilon$
- Replaces left recursion with right recursion
- Examples
  - $S \rightarrow Sa \mid \varepsilon$ ⇨ $S \rightarrow L \quad L \rightarrow aL \mid \varepsilon$
  - $S \rightarrow Sa \mid Sb \mid c$ ⇨ $S \rightarrow cL \quad L \rightarrow aL \mid bL \mid \varepsilon$

Quiz #4

- What does the following code parse?

```
let parse_S toks =
  if lookahead toks = Some "a" then
    let toks = match_tok toks "a" in
    let toks = match_tok toks "x" in
    let toks = match_tok toks "y" in
    match_tok toks "q"
  else
    raise (ParseError "parse_S")
```

A. $S \rightarrow axyq$
B. $S \rightarrow a \mid q$
C. $S \rightarrow aaxy \mid qq$
D. $S \rightarrow axy \mid q$

Quiz #4

- What does the following code parse?

```
let parse_S toks =
  if lookahead toks = Some "a" then
    let toks = match_tok toks "a" in
    let toks = match_tok toks "x" in
    let toks = match_tok toks "y" in
    match_tok toks "q"
  else
    raise (ParseError "parse_S")
```

A. S → axyq
B. S → a | q
C. S → aaxy | qq
D. S → axy | q

Quiz #5

- What does the following code parse?

```
let rec parse_S toks =
  if lookahead toks = Some "a" then
    let toks = match_tok toks "a" in
    parse_S toks
  else if lookahead toks = Some "q" then
    let toks = match_tok toks "q" in
    match_tok toks "p")
  else
    raise (ParseError "parse_S")
```

A. $S \rightarrow aS \mid qp$
B. $S \rightarrow a \mid S \mid qp$
C. $S \rightarrow aqSp$
D. $S \rightarrow a \mid q$

Quiz #5

- What does the following code parse?

```
let rec parse_S toks =
  if lookahead toks = Some "a" then
    let toks = match_tok toks "a" in
    parse_S toks
  else if lookahead toks = Some "q" then
    let toks = match_tok toks "q" in
    match_tok toks "p")
  else
    raise (ParseError "parse_S")
```

A. $S \rightarrow aS \mid qp$
B. $S \rightarrow a \mid S \mid qp$
C. $S \rightarrow aqSp$
D. $S \rightarrow a \mid q$

Quiz #6

Can recursive descent parse this grammar?

$$\boxed{\begin{array}{l} S \rightarrow aBa \\ B \rightarrow bC \\ C \rightarrow \varepsilon \mid Cc \end{array}}$$

A. Yes
B. No

Quiz #6

Can recursive descent parse this grammar?

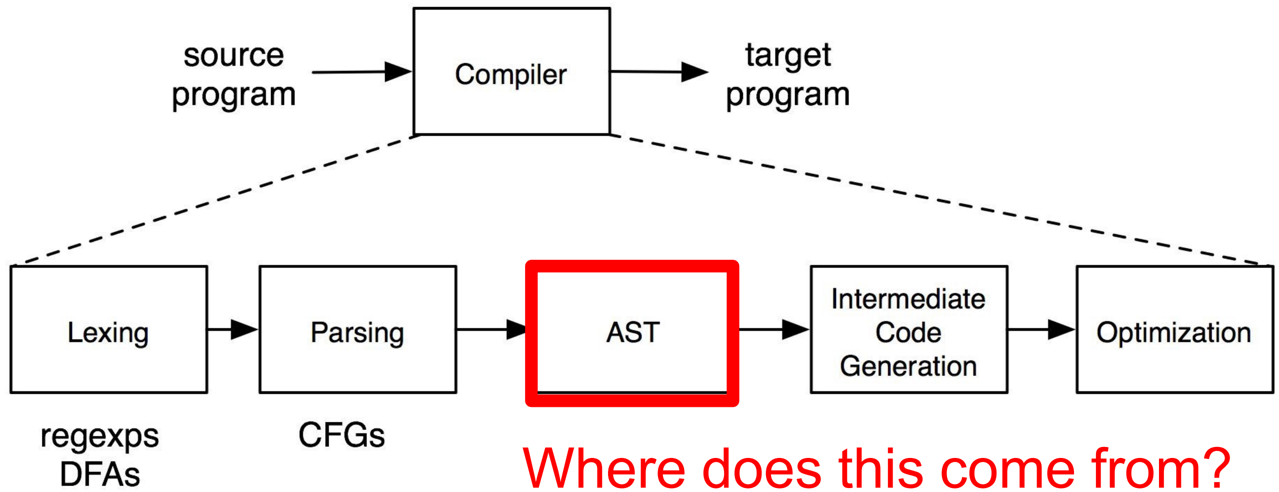
$$
\begin{aligned}
S &\rightarrow aBa \\
B &\rightarrow bC \\
C &\rightarrow \varepsilon \mid Cc
\end{aligned}
$$

A. Yes

B. No

(due to left recursion)

Recall: The Compilation Process



Where does this come from?

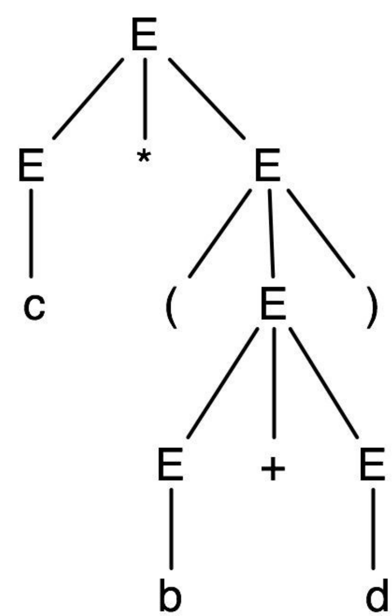
Parse Trees to ASTs

- Parse trees are a representation of a parse, with all of the syntactic elements present
  - Parentheses
  - Extra nonterminals for precedence
- This extra stuff is needed for parsing

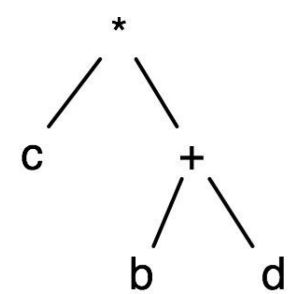
- Lots of that stuff is not needed to actually implement a compiler or interpreter
  - So in the abstract syntax tree we get rid of it

Abstract Syntax Trees (ASTs)

- An abstract syntax tree is a more compact, abstract representation of a parse tree, with only the essential parts



parse tree



AST

Example: Simple Assignment

E → *id* = *n* | { L }
L → E ; L | ε

```
type token = Tok_Num (* of string *)
           | Tok_Id (* of string *)
           | Tok_Eq | Tok_Semi
           | Tok_Lbrace
           | Tok_Rbrace
```

- Here, *id* stands for a general identifier (variable), like **`a`**, **`bob`**, **`chandra`**, **`toy`**, etc.
  - The scanner will match this via a regular expression, and can track of what the actual string was; we'll ignore here
- Similar situation for *n*, which represents an integer

Matching Strings; no AST

$E \rightarrow id = n \mid \{ L \}$
$L \rightarrow E ; L \mid \varepsilon$

```
type token = Tok_Num (* of string *)
           | Tok_Id (* of string *)
           | Tok_Eq | Tok_Semi
           | Tok_Lbrace
           | Tok_Rbrace
```

```
let rec parse_E (toks:token list) =
  match lookahead toks with
   | Some Tok_Id ->  (* E → id = n *)
    let toks = match_tok toks Tok_Id in
    let toks = match_tok toks Tok_Eq in
    match_tok  toks Tok_Num
   | Some Tok_Lbrace -> (* E → { L } *)
    let toks = match_tok toks Tok_Lbrace in
    let toks = parse_L toks in
    match_tok toks Tok_Rbrace
   | _ -> raise (ParseError "parse_E")
```

```
and parse_L (toks:token list) =
  match lookahead toks with
   | Some Tok_Id
   | Some Tok_Lbrace -> (* L → E ; L *)
     let toks = parse_E toks in
     let toks = match_tok toks Tok_Semi
     in parse_L  toks
   | _ ->
  (* L → ε *)  toks
```

Defining the AST

$E \rightarrow id = n \mid \{ L \}$
$L \rightarrow E \; ; L \mid \varepsilon$

```
type token = Tok_Num of string
           | Tok_Id of string
           | Tok_Eq | Tok_Semi
           | Tok_Lbrace
           | Tok_Rbrace

type stmt =
| Assign of string * int
| Block of stmt list
```

- The AST is just a sequence of assignment statements

Parsing, producing AST

E → *id* = *n* | { L }
L → E ; L | ε

```
let rec parse_E toks: (token list * stmt) =
match lookahead toks with
 Some (Tok_Id v) ->
   let toks = match_tok toks (Tok_Id v) in
   let toks = match_tok toks Tok_Eq in
   let Some (Tok_Num n) = lookahead toks in
   let toks = match_tok (Tok_Num n) in
   Assign (v, int_of_string n)
 | Some Tok_Lbrace ->
   let toks = match_tok toks Tok_Lbrace in
   let toks, stms = parse_L toks in
   let toks = match_tok toks Tok_Rbrace in
   toks, Block stms
 | _ -> raise (ParseError "parse_E")
```

```
type token = Tok_Num of string
           | Tok_Id of string
           | Tok_Eq | Tok_Semi
           | Tok_Lbrace
           | Tok_Rbrace

type stmt =
   Assign of string * int
 | Block of stmt list

and parse_L toks: (token list * stmt list) =
match lookahead toks with
  | Some (Tok_Id _)
  | Some Tok_Lbrace ->
      let toks, stm = parse_E toks in
      let toks = match_tok toks Tok_Semi in
      let toks, stms = parse_L toks in
      toks, stm :: stms
  | _ -> toks, []
```