

Question 4.5 from CTCI: Find the Next Successor

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Question

Write an algorithm to find the next node (e.g., in-order successor) of a given node in a binary search tree where each node has a link to its parent. You will write a function which takes a `TreeNode e` and returns a `TreeNode p` which is the successor of `e`.

Explanation and Algorithm

We approach this problem by thinking very, very carefully about what happens on an in-order traversal. On an in-order traversal, we visit `X.left`, then `X`, then `X.right`. So, if we want to find `X.successor()`, we do the following:

1. If `X` has a right child, then the successor must be on the right side of `X` (because of the order in which we visit nodes). Specifically, the left-most child must be the first node visited in that subtree.
2. Else, we go to `Xs` parent (call it `P`).
 - If `X` was a left child (`P.left = X`), then `P` is the successor of `X`
 - If `X` was a right child (`P.right = X`), then we have fully visited `P`, so we call `successor(P)`.

Hints

1. Think about how in-order traversal works. What are the possible cases of the given node; is it a left child or right child of its parent node?
2. What should we do if the given node is a right child? If it's a left child?

Code

```
public static TreeNode inorderSucc(TreeNode e) {
    if (e != null) {
        TreeNode p;
        // Found right children -> return 1st inorder node on right
        if (e.parent == null || e.right != null) {
            p = leftMostChild(e.right);
        } else {
            // Go up until were on left instead of right (case 2b)
            while ((p = e.parent) != null) {
                if (p.left == e) {
                    break;
                }
                e = p;
            }
        }
        return p;
    }
    return null;
}

public static TreeNode leftMostChild(TreeNode e) {
    if (e == null) return null;
    while (e.left != null) e = e.left;
    return e;
}
```

Big O analysis

The time complexity of this algorithm is $O(h)$, where h is the height of the binary search tree. This is because we will, at worst, have to iterate through each "level" of the tree until we reach the bottom/left-most child node.

Sources

Question, answer and other material taken from Cracking the Coding Interview 6th edition by Gayle Laakmann McDowell.