

# **Documentation for Edit Distance Problem and Solution**

## **Problem Statement**

The Edit Distance problem, also known as Levenshtein Distance, is a classic algorithmic problem that involves finding the minimum number of operations required to convert one string into another. The operations allowed are:

1. Insert a character
2. Delete a character
3. Replace a character

Given two strings, word1 and word2, the objective is to determine the minimum number of these operations needed to transform word1 into word2.

## **Example 1**

- **Input:** word1 = "horse", word2 = "ros"
- **Output:** 3
- **Explanation:**
  - horse -> rorse (replace 'h' with 'r')
  - rorse -> rose (remove 'r')
  - rose -> ros (remove 'e')

## **Example 2**

- **Input:** word1 = "intention", word2 = "execution"
- **Output:** 5

- **Explanation:**

- intention -> inention (remove 't')
- inention -> enention (replace 'i' with 'e')
- enention -> exention (replace 'n' with 'x')
- exention -> exection (replace 'n' with 'c')
- exection -> execution (insert 'u')

## **Constraints**

- $0 \leq \text{word1.length}, \text{word2.length} \leq 500$
- word1 and word2 consist of lowercase English letters.

## **Solution Explanation**

The solution to this problem uses dynamic programming (DP) to build a table that helps in calculating the minimum edit distance efficiently.

## **Steps to Solve**

### **1. Initialize Variables:**

- Determine the lengths of the two words, m and n.
- Create a DP table dp of size (m+1) x (n+1) initialized to zeros.

### **2. Base Case Initialization:**

- Fill the first row and the first column of the DP table:
- $\text{dp}[i][0] = i$  for all i from 0 to m (representing converting a string to an empty string by deleting characters).
- $\text{dp}[0][j] = j$  for all j from 0 to n (representing converting an empty string to a string by inserting characters).

### 3. Fill the DP Table:

- For each cell  $dp[i][j]$ , determine the minimum number of operations required:
- If  $word1[i-1] == word2[j-1]$ , no operation is needed ( $dp[i][j] = dp[i-1][j-1]$ ).
- Otherwise, consider the three possible operations (insert, delete, replace) and take the minimum value:
- $dp[i][j] = \min(dp[i-1][j] + 1, dp[i][j-1] + 1, dp[i-1][j-1] + 1)$

### 4. Return the Result:

- The value at  $dp[m][n]$  will be the minimum edit distance between word1 and word2.

## Explanation of the Code

- **Initialization:** The lengths of word1 and word2 are stored in m and n. A 2D list dp of size  $(m+1) \times (n+1)$  is created to store the minimum edit distances for substrings of word1 and word2.
- **Base Case Setup:** The first row and column of the DP table are initialized to represent converting to and from empty strings.
- **DP Table Filling:** The nested loops iterate through each character of word1 and word2, filling the DP table based on the minimum operations calculated.
- **Result Return:** The value at  $dp[m][n]$  represents the minimum number of operations required to convert word1 to word2.

This solution has a time complexity of  $O(m * n)$  and a space complexity of  $O(m * n)$ , making it efficient for the given problem constraints.