Documentation for maximalRectangle Solution

Problem Description

The problem requires finding the largest rectangle containing only '1's in a given binary matrix (composed of '0's and '1's) and returning its area.

Solution Overview

The solution leverages a histogrambased approach to efficiently compute the largest rectangle of '1's for each row in the matrix.

maximalRectangle Method

This method computes the maximal rectangle in a binary matrix.

- 1. <u>Input Validation</u>: If the matrix is empty or the first row is empty, return 0.
- 2. <u>Initialize Variables:</u>
 - rows and cols to store the dimensions of the matrix.
 - heights, a list of zeros with length equal to the number of columns, to store the height of the histogram bars.
 - max_area to store the maximum area of the rectangle found so far.

3. <u>Iterate Through Each Row:</u>

- For each element in the row, update the corresponding height in the heights array.
- If the element is '1', increment the height by 1; otherwise, reset the height to 0.
- 4. <u>Calculate Max Area:</u> For each updated histogram, calculate the maximum area using the largestRectangleArea helper method.
- 5. **Return Result:** Return the maximum area found.

largestRectangleArea Method

This method calculates the largest rectangle area in a histogram using a stackbased approach.

1. Append Zero: Append a zero to the heights list to ensure the last bar is processed.

2. Initialize Variables:

- stack to keep track of indices of the histogram bars.
- max area to store the maximum area of the rectangle found so far.

3. <u>Iterate Through Heights:</u>

- For each bar, maintain a nondecreasing order in the stack.
- If the current bar is lower than the bar at the index stored at the top of the stack, pop the stack and calculate the area.
- The width of the rectangle is determined by the difference between the current index and the index of the new top of the stack.
- 4. Pop Last Element: Remove the appended zero to restore the original list.
- 5. Return Result: Return the maximum area found.

Example 1

```
matrix = [["1","0","1","0","0"],["1","0","1","1","1"],["1","1","1","1","1","1"],["1","0","0","1","0"]]
solution = Solution()
output = solution.maximalRectangle(matrix)
print(output) # Output: 6
```

Example 2

```
matrix = [["0"]]
solution = Solution()
output = solution.maximalRectangle(matrix)
print(output) # Output: 0
```

Example 3

```
matrix = [["1"]]
solution = Solution()
output = solution.maximalRectangle(matrix)
print(output) # Output: 1
```

Constraints

- The number of rows (rows) is between 1 and 200.
- The number of columns (cols) is between 1 and 200.
- Each element in the matrix is either '0' or '1'.

This solution effectively transforms each row into a histogram and uses a stackbased method to find the largest rectangle in each histogram, achieving efficient computation.