

■ Documentation: Longest Uncommon Subsequence I

1. Problem Statement

Given two strings a and b , return the length of the longest uncommon subsequence between them. If no such uncommon subsequence exists, return -1 .

A subsequence is a string that can be derived from another string by deleting some characters without changing the order of the remaining characters. An uncommon subsequence is a subsequence that appears in one string but not the other.

2. Intuition

If two strings are not equal, the longer string itself is a valid uncommon subsequence, as it cannot be a subsequence of the shorter (or different) one. However, if both strings are exactly the same, then any subsequence of one is also a subsequence of the other—hence, no uncommon subsequence.

3. Key Observations

- If $a == b$, then every subsequence is shared \rightarrow return -1 .
- If $a \neq b$, then the longer string itself is a unique subsequence \rightarrow return $\max(\text{len}(a), \text{len}(b))$.

4. Approach

- Compare the strings:
 - If they are equal \rightarrow return -1 .
 - If they are not equal \rightarrow return the length of the longer string.
- No need to explore all subsequences (which would be exponential time) due to the above insight.

5. Edge Cases

- $a = \text{"abc"}, b = \text{"abc"} \rightarrow$ both are same \rightarrow return -1.
- $a = \text{"a"}, b = \text{"b"} \rightarrow$ both are different \rightarrow return 1.
- $a = \text{"abcd"}, b = \text{"ab"} \rightarrow$ different \rightarrow return 4.

6. Complexity Analysis

⌚ Time Complexity

- $O(1)$: Only comparison and length calculation.

📦 Space Complexity

- $O(1)$: No extra space used.

7. Alternative Approaches

- Brute-force: Generate all subsequences of both strings and check which ones are uncommon.
 - Not practical: Generating all subsequences has time complexity of $O(2^n)$.
 - Our current solution is optimal for this problem's constraints.

8. Test Cases

a	b	Output	Explanation
"aba"	"cdc"	3	Both are different; each of length 3
"aaa"	"aaa"	-1	Both are identical
"abc"	"def"	3	Different strings; any one is a valid uncommon subsequence
"a"	"b"	1	Single-character strings, different
"abcd"	"abc"	4	"abcd" is not a subsequence of "abc"

9. Final Thoughts

This problem appears simple, but it's a great example of how recognizing patterns can avoid unnecessary computation.

Instead of diving into complex subsequence generation, the key is understanding how identity and length determine uniqueness.