

Documentation for Find All Numbers Disappeared in an Array

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1. Problem Statement

We are given an array `nums` of length n , where each element in `nums` is within the range $[1, n]$. Some numbers in this range may be missing from `nums`.

Our task is to return an array of all missing numbers in the range $[1, n]$ that do not appear in `nums`.

Example 1

Input: `nums = [4,3,2,7,8,2,3,1]`

Output: `[5,6]`

Example 2

Input: `nums = [1,1]`

Output: `[2]`

2. Intuition

Since all numbers are within the range $[1, n]$, we can efficiently determine missing numbers by leveraging index-based marking techniques instead of using extra space.

A number is missing from `nums` if its corresponding index has never been visited.

3. Key Observations

- Every number x in `nums` is in the range $[1, n]$, so it can be mapped to index $x - 1$.
- If a number exists in the array, we mark its corresponding index as negative.
- After processing all numbers, indices that remain positive indicate missing numbers.

4. Approach

Step 1: Mark Visited Indices

- Iterate through `nums`.
- For each `num`, calculate its corresponding index: `index = abs(num) - 1`.
- Mark `nums[index]` as negative to indicate presence.

Step 2: Identify Missing Numbers

- After the first pass, any index i where `nums[i]` remains positive corresponds to a missing number $i + 1$.

Example Walkthrough

Input: `nums = [4,3,2,7,8,2,3,1]`

Processing Steps:

Step	nums State
Initial	[4,3,2,7,8,2,3,1]
Mark 4	[4,3,2,-7,8,2,3,1]
Mark 3	[4,3,-2,-7,8,2,3,1]
Mark 2	[4,-3,-2,-7,8,2,3,1]
Mark 7	[4,-3,-2,-7,8,2,-3,1]
Mark 8	[4,-3,-2,-7,8,2,-3,-1]
Mark 2 (again)	[4,-3,-2,-7,8,2,-3,-1]
Mark 3 (again)	[4,-3,-2,-7,8,2,-3,-1]
Mark 1	[-4,-3,-2,-7,8,2,-3,-1]

Step 2: Identify Missing Numbers

- The remaining positive values at indices 4 and 5 indicate that numbers 5 and 6 are missing.

5. Edge Cases

Case	Example	Expected Output
All numbers present	[1,2,3,4,5]	[]
All numbers missing except one	[1,1,1,1,1]	[2,3,4,5]
Single-element array	[1]	[]
Minimum input size	[1]	[]
All elements are duplicates	[2,2,2,2]	[1,3,4]

6. Complexity Analysis

Time Complexity

- $O(n)$: We iterate through nums twice (once for marking, once for finding positives).

Space Complexity

- $O(1)$: No extra space is used apart from the output list (modifies nums in-place).

7. Alternative Approaches

Approach	Time Complexity	Space Complexity	Notes
Using HashSet	$O(n)$	$O(n)$	Uses extra space
Sorting + Binary Search	$O(n \log n)$	$O(1)$	Not optimal

8. Test Cases

```
def test_solution():
    sol = Solution()
    assert sol.findDisappearedNumbers([4,3,2,7,8,2,3,1]) == [5,6]
    assert sol.findDisappearedNumbers([1,1]) == [2]
    assert sol.findDisappearedNumbers([1,2,3,4,5]) == []
    assert sol.findDisappearedNumbers([2,2,2,2]) == [1,3,4]
    assert sol.findDisappearedNumbers([1]) == []
    print("All test cases passed!")

test_solution()
```

9. Final Thoughts

- This approach efficiently finds missing numbers with $O(n)$ time and $O(1)$ space.
- It works well with large inputs since it avoids extra memory usage.
- The downside is that it modifies the input array, so if the original order must be preserved, an alternative approach like using a HashSet should be used.