

Documentation for Merge Sorted Array

Problem Description

You are given two integer arrays `nums1` and `nums2`, both sorted in non-decreasing order. You are also given two integers `m` and `n`, representing the number of elements in `nums1` and `nums2`, respectively. The goal is to merge `nums1` and `nums2` into a single array sorted in non-decreasing order. The final sorted array should be stored inside the array `nums1`.

- `nums1` has a length of `m + n`, where the first `m` elements denote the elements that should be merged, and the last `n` elements are set to 0 and should be ignored.
- `nums2` has a length of `n`.

Example 1

Input:

`nums1 = [1, 2, 3, 0, 0, 0]`

`m = 3`

`nums2 = [2, 5, 6]`

`n = 3`

Output: `[1, 2, 2, 3, 5, 6]`

Explanation: The arrays we are merging are `[1, 2, 3]` and `[2, 5, 6]`. The result of the merge is `[1, 2, 2, 3, 5, 6]`.

Example 2

Input:

nums1 = [1]

m = 1

nums2 = []

n = 0

Output: [1]

Explanation: The arrays we are merging are [1] and []. The result of the merge is [1].

Example 3

Input:

nums1 = [0]

m = 0

nums2 = [1]

n = 1

Output: [1]

Explanation: The arrays we are merging are [] and [1]. The result of the merge is [1].

Constraints:

- `nums1.length == m + n`
- `nums2.length == n`
- $0 \leq m, n \leq 200$
- $1 \leq m + n \leq 200$
- $-10^9 \leq \text{nums1}[i], \text{nums2}[j] \leq 10^9$

Follow-up:

Can you come up with an algorithm that runs in $O(m + n)$ time?

Explanation

1. Pointers Initialization:

- `p1` is initialized to the last index of the non-zero elements in `nums1` (i.e., `m - 1`).
- `p2` is initialized to the last index of `nums2` (i.e., `n - 1`).
- `p` is initialized to the last index of `nums1` (i.e., `m + n - 1`).

2. Merging in Reverse Order:

- We compare elements from the end of `nums1` and `nums2`.
- We place the larger element at the current end position (`p`) of `nums1`.
- We move the respective pointers (`p1`, `p2`, `p`) accordingly.

3. Copy Remaining Elements:

- If any elements remain in `nums2` after the initial merge, we copy them into `nums1`.
- This is necessary because `nums1` might have leftover zeros if `nums2` had larger elements.

Time Complexity

- The algorithm runs in $O(m + n)$ time because each element from both arrays is processed exactly once.

Space Complexity

- The algorithm uses $O(1)$ extra space as it modifies `nums1` in place without using additional arrays.

This approach efficiently merges the two sorted arrays within the given constraints and ensures that the final result is stored in `nums1`.