Documentation

The problem of finding the shortest palindrome involves converting a given string **s** into a palindrome by adding the minimum number of characters to the front of the string. A palindrome is a string that reads the same forwards and backward, and the goal is to achieve this by transforming **s** in the shortest way possible. The key to solving this problem efficiently is identifying the longest palindromic prefix in the string. Once we find this, we can append the remaining non-palindromic characters from the reversed string to the front of **s**.

We approach the solution by reversing the string **s**. This reversed version of the string helps in identifying the palindromic properties of **s**. We then combine the original string and its reversed version using a separator, ensuring no false matches occur while detecting palindromic prefixes. The combined string allows us to apply the Knuth-Morris-Pratt (KMP) algorithm, which is typically used for string matching but, in this case, helps to compute the longest prefix of the string which is also a suffix. This information is stored in the Longest Prefix Suffix (LPS) array, which tells us the length of the longest palindromic prefix in **s**.

The LPS array is built for the combined string, and the value at the last index of the LPS array indicates how much of the original string s is already a palindrome. Using this value, we can determine the number of characters that need to be added to the front of the string to make it a palindrome. These characters come from the reversed version of s. Once we know which characters to add, we append them to the front of s, resulting in the shortest possible palindrome. This method is efficient, with a time complexity of O(n) due to the linear time KMP algorithm, and a space complexity of O(n) for storing the LPS array. By using this approach, we can quickly and optimally find the shortest palindrome for any given input string.