

Documentation K-diff Pairs in an Array

1. Problem Statement

Given an array of integers `nums` and an integer `k`, return the number of unique `k`-diff pairs in the array.

A `k`-diff pair is defined as a pair $(\text{nums}[i], \text{nums}[j])$ such that:

- $0 \leq i, j < \text{nums.length}$
- $i \neq j$
- $|\text{nums}[i] - \text{nums}[j]| == k$

2. Intuition

To efficiently count unique pairs with absolute difference `k`, we use a frequency map (hash table). Depending on whether `k` is zero or positive, we either:

- Count elements that appear more than once (for $k = 0$), or
- Check if `num + k` exists for every unique number in the array (for $k > 0$).

3. Key Observations

- If $k < 0$, return 0 immediately — absolute difference can't be negative.
- For $k = 0$, pairs must consist of the same number appearing at least twice.
- For $k > 0$, we only need to check if `num + k` exists to ensure unique pairs.

4. Approach

- Use `collections.Counter` to build a frequency map of all elements.
- If $k == 0$:
 - Iterate through the map and count how many numbers appear more than once.
- If $k > 0$:
 - For each number, check if `num + k` exists in the map.
- Return the total count of such unique pairs.

5. Edge Cases

- Empty array \rightarrow output: 0
- $k < 0 \rightarrow$ output: 0
- All unique numbers, $k = 0 \rightarrow$ output: 0
- Multiple duplicates \rightarrow ensure unique pairs only
- Large values of $k \rightarrow$ should still be handled in linear time

6. Complexity Analysis

Time Complexity

- $O(n)$: where n is the length of the array.
 - `Counter(nums)` is $O(n)$
 - Loop through unique keys is $O(n)$ in worst case

Space Complexity

- $O(n)$: For storing frequency map in `Counter`

7. Alternative Approaches

- Brute-force (nested loops):
 - Time: $O(n^2)$
 - Space: $O(1)$
 - Not suitable for large inputs.
- Sorting + Two pointers:
 - Time: $O(n \log n)$
 - Space: $O(1)$ or $O(n)$ depending on sort implementation
 - Needs extra care to avoid counting duplicates.

8. Test Cases

Input	k	Output	Explanation
[3,1,4,1,5]	2	2	Pairs: (1,3), (3,5)
[1,2,3,4,5]	1	4	Pairs: (1,2), (2,3), (3,4), (4,5)
[1,3,1,5,4]	0	1	Only one duplicate: (1,1)
[1,2,3,4,5]	0	0	No duplicates
[1,1,1,1,1]	0	1	Only one unique duplicate (1,1)
[]	1	0	Empty input
[1,2,3,4,5]	-1	0	Negative k not valid

9. Final Thoughts

This problem is a great example of using hash maps for fast lookups and uniqueness tracking. The key is handling the $k = 0$ case correctly and avoiding double-counting. The solution is efficient and scalable for large inputs.