

## 519. Random Flip Matrix

There is an  $m \times n$  binary grid matrix with all the values set 0 initially. Design an algorithm to randomly pick an index  $(i, j)$  where  $\text{matrix}[i][j] == 0$  and flips it to 1. All the indices  $(i, j)$  where  $\text{matrix}[i][j] == 0$  should be equally likely to be returned.

Optimize your algorithm to minimize the number of calls made to the built-in random function of your language and optimize the time and space complexity.

### *Implement the Solution class:*

- `Solution(int m, int n)` Initializes the object with the size of the binary matrix  $m$  and  $n$ .
- `int[] flip()` Returns a random index  $[i, j]$  of the matrix where  $\text{matrix}[i][j] == 0$  and flips it to 1.
- `void reset()` Resets all the values of the matrix to be 0.

### Example 1:

- **Input**
  - `["Solution", "flip", "flip", "flip", "reset", "flip"]`
  - `[[3, 1], [], [], [], [], []]`
- **Output**
  - `[null, [1, 0], [2, 0], [0, 0], null, [2, 0]]`
- **Explanation**
  - `Solution solution = new Solution(3, 1);`
  - `solution.flip();` // return `[1, 0]`, `[0,0]`, `[1,0]`, and `[2,0]` should be equally likely to be returned.
  - `solution.flip();` // return `[2, 0]`, Since `[1,0]` was returned, `[2,0]` and `[0,0]`
  - `solution.flip();` // return `[0, 0]`, Based on the previously returned indices, only `[0,0]` can be returned.
  - `solution.reset();` // All the values are reset to 0 and can be returned.
  - `solution.flip();` // return `[2, 0]`, `[0,0]`, `[1,0]`, and `[2,0]` should be equally likely to be returned.

### Constraints:

- $1 \leq m, n \leq 10^4$
- There will be at least one free cell for each call to flip.
- At most 1000 calls will be made to flip and reset.