

In [5]: ▶

```
1 from skimage.color import rgb2gray
2 from skimage import data
3 import matplotlib.pyplot as plt
4 import numpy as np
5 from scipy.linalg import svd
6 X = np.array([[1,1],[0,1],[-1,1]])
7 print(X)
8 print("")
9 print("")
10 print("")
11 print("")
12 U, singular, V_transpose = svd(X)
13 # print different components
14 print("U: ", U)
15 print("")
16 print("")
17 print("")
18 print("")
19 print("Singular array", singular)
20 print("")
21 print("")
22 print("")
23 print("")
24 print("V^{T}", V_transpose)
25
26
27 """
28 Calculate Pseudo inverse
29 """
30 # inverse of singular matrix is just the reciprocal of each element
31 singular_inv = 1.0 / singular
32 # create m x n matrix of zeroes and put singular values in it
33 s_inv = np.zeros(X.shape)
34 s_inv[0][0] = singular_inv[0]
35 s_inv[1][1] = singular_inv[1]
36 # calculate pseudoinverse
37 M = np.dot(np.dot(V_transpose.T, s_inv.T), U.T)
38 print(M)
```

```
[[ 1  1]
 [ 0  1]
 [-1  1]]
```

```
U: [[-0.57735027 -0.70710678  0.40824829]
     [-0.57735027  0.          -0.81649658]
     [-0.57735027  0.70710678  0.40824829]]
```

```
Singular array [1.73205081 1.41421356]
```

```
V^{T} [[-0. -1.]
        [-1. -0.]]
[[ 0.5          0.          -0.5          ]
 [ 0.33333333  0.33333333  0.33333333]]
```

In [6]: ▶

```
1 from skimage.color import rgb2gray
2 from skimage import data
3 import matplotlib.pyplot as plt
4 import numpy as np
5 from scipy.linalg import svd
6 X = np.array([[3,2,2],[2,3,-2]])
7 print(X)
8 print("")
9 print("")
10 print("")
11 print("")
12 U, singular, V_transpose = svd(X)
13 # print different components
14 print("U: ", U)
15 print("")
16 print("")
17 print("")
18 print("")
19 print("Singular array", singular)
20 print("")
21 print("")
22 print("")
23 print("")
24 print("V^{T}", V_transpose)
25
26
27 """
28 Calculate Pseudo inverse
29 """
30 # inverse of singular matrix is just the reciprocal of each element
31 singular_inv = 1.0 / singular
32 # create m x n matrix of zeroes and put singular values in it
33 s_inv = np.zeros(X.shape)
34 s_inv[0][0] = singular_inv[0]
35 s_inv[1][1] = singular_inv[1]
36 # calculate pseudoinverse
37 M = np.dot(np.dot(V_transpose.T, s_inv.T), U.T)
38 print(M)
```

```
[[ 3  2  2]
 [ 2  3 -2]]
```

```
U: [[ 0.70710678 -0.70710678]
     [ 0.70710678  0.70710678]]
```

```
Singular array [5. 3.]
```

```
V^{T} [[ 7.07106781e-01  7.07106781e-01  3.67439059e-16]
        [-2.35702260e-01  2.35702260e-01 -9.42809042e-01]
        [-6.66666667e-01  6.66666667e-01  3.33333333e-01]]
[[ 0.15555556  0.04444444]
 [ 0.04444444  0.15555556]
 [ 0.22222222 -0.22222222]]
```


In [10]:

```

1  # Python3 Program to decompose
2  # a matrix into lower and
3  # upper triangular matrix
4  MAX = 100
5
6
7  def luDecomposition(mat, n):
8
9      lower = [[0 for x in range(n)]
10               for y in range(n)]
11      upper = [[0 for x in range(n)]
12               for y in range(n)]
13
14      # Decomposing matrix into Upper
15      # and Lower triangular matrix
16      for i in range(n):
17
18          # Upper Triangular
19          for k in range(i, n):
20
21              # Summation of L(i, j) * U(j, k)
22              sum = 0
23              for j in range(i):
24                  sum += (lower[i][j] * upper[j][k])
25
26              # Evaluating U(i, k)
27              upper[i][k] = mat[i][k] - sum
28
29          # Lower Triangular
30          for k in range(i, n):
31              if (i == k):
32                  lower[i][i] = 1 # Diagonal as 1
33              else:
34
35                  # Summation of L(k, j) * U(j, i)
36                  sum = 0
37                  for j in range(i):
38                      sum += (lower[k][j] * upper[j][i])
39
40                  # Evaluating L(k, i)
41                  lower[k][i] = int((mat[k][i] - sum) /
42                                     upper[i][i])
43
44      # setw is for displaying nicely
45      print("Lower Triangular\t\tUpper Triangular")
46
47      # Displaying the result :
48      for i in range(n):
49
50          # Lower
51          for j in range(n):
52              print(lower[i][j], end="\t")
53          print("", end="\t")
54
55          # Upper
56          for j in range(n):
57              print(upper[i][j], end="\t")

```

```
58         print("")
59
60
61     # Driver code
62     mat = [[2, -1, -2],
63           [-4, 6, 3],
64           [-4, -2, 8]]
65
66     luDecomposition(mat, 3)
67
68     # This code is contributed by mits
69
```

Lower Triangular

| | | |
|----|----|---|
| 1 | 0 | 0 |
| -2 | 1 | 0 |
| -2 | -1 | 1 |

Upper Triangular

| | | |
|---|----|----|
| 2 | -1 | -2 |
| 0 | 4 | -1 |
| 0 | 0 | 3 |

In [11]:

```

1  # Python3 Program to decompose
2  # a matrix into lower and
3  # upper triangular matrix
4  MAX = 100
5
6
7  def luDecomposition(mat, n):
8
9      lower = [[0 for x in range(n)]
10               for y in range(n)]
11      upper = [[0 for x in range(n)]
12               for y in range(n)]
13
14      # Decomposing matrix into Upper
15      # and Lower triangular matrix
16      for i in range(n):
17
18          # Upper Triangular
19          for k in range(i, n):
20
21              # Summation of L(i, j) * U(j, k)
22              sum = 0
23              for j in range(i):
24                  sum += (lower[i][j] * upper[j][k])
25
26              # Evaluating U(i, k)
27              upper[i][k] = mat[i][k] - sum
28
29          # Lower Triangular
30          for k in range(i, n):
31              if (i == k):
32                  lower[i][i] = 1 # Diagonal as 1
33              else:
34
35                  # Summation of L(k, j) * U(j, i)
36                  sum = 0
37                  for j in range(i):
38                      sum += (lower[k][j] * upper[j][i])
39
40                  # Evaluating L(k, i)
41                  lower[k][i] = int((mat[k][i] - sum) /
42                                     upper[i][i])
43
44      # setw is for displaying nicely
45      print("Lower Triangular\t\tUpper Triangular")
46
47      # Displaying the result :
48      for i in range(n):
49
50          # Lower
51          for j in range(n):
52              print(lower[i][j], end="\t")
53          print("", end="\t")
54
55          # Upper
56          for j in range(n):
57              print(upper[i][j], end="\t")

```

```
58         print("")
59
60
61     # Driver code
62     mat = [[2, -9, 8],
63           [-1, 5, 3],
64           [1, 2, 3]]
65
66     luDecomposition(mat, 3)
67
68     # This code is contributed by mits
69
```

Lower Triangular

| | | |
|---|---|---|
| 1 | 0 | 0 |
| 0 | 1 | 0 |
| 0 | 0 | 1 |

Upper Triangular

| | | |
|---|----|---|
| 2 | -9 | 8 |
| 0 | 5 | 3 |
| 0 | 0 | 3 |