Project 2: Passive Radar and Motion Detection

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| 1. Introduction 2. **Principles of Passive Radar** 3. Procedures IMG_256 4. Relationship between TDOA and range   Range = TDOA × speed of light  TDOA is short for time difference of arrival. It reveals the difference of propagation delay between surveillance and reference signal.   1. Relationship between Doppler frequency shift and velocity   β is the angle from surveillance channel to reference channel, fD represents Doppler frequency shift, is the wavelength of the signal.   1. **Continuous-time Fourier Transform Realization in Matlab**     IMG_256  To emphasize, X is the samples of Fourier transform, ∆f=∆ω/2π=1/T   1. Task 1   **For the reference signal and the surveillance signal, draw their time domain waveform and their frequency domain waveform in their following processing process respectively: Original, After frequency conversion, After low-pass filtering**  Before signal processing, we need to filter out the signal of 2130-2135MHz (5M bandwidth), and reserve the signal of 2110-2130MHz(20Mbandwidth). So we need to convert the signal 2110-2130MHz to the frequency centered on 0 Hz.Then filter out the high-frequency signal through the low-pass filter.  We take data\_1.mat file as an example. This figure shows the original reference signal and the surveillance signals in the 0-0.5s required by the question. Only the first 0.01s is plotted below.      Then, to extract frequency components between 2110-2130MHz, we utilize DDC method to let 2120MHz to become the center. And since the carrier of the two original signal is 2123MHz, we need to left-shift 3MHz. The graph as followed shows the reference signal and the surveillance signals after DDC in the 0-0.5s required by the question.      Finally, to filter out the signal of 2130-2135MHz and reserve the signal of 2110-2130MHz, we used the LPF (Low pass filtering) to extract the signal spectrum between 2110MHz and 2130MHz. This figure shows the reference signal and the surveillance signals after LPF in the 0-0.5s required by the question.      As we can see, these signals are what we want.  Other 19 figures about the surveillance and reference signal between 0.5-10ss are on the appendix.   1. Task 2   **Draw the Range Doppler spectrum of the signal located at 0 ~ 0.5s, 2 ~ 2.5s, 5 ~ 5.5s and 7 ~ 7.5s(data is provided), range=0:5, doppler\_frequency\_shift=-40:2:40**  In Task2, we were asked to draw the range doppler spectrum. In task1, we obtain the signal of 2110-2130MHz (20Mbandwidth) after DDC and low-pass filter.   1. **Cross-Correlation**   Now we have the reference signal and surveillance signal of 2110-2130Mhz. To compute the displacement and velocity of the object, we can find the time difference of arrival (TDOA) τ and Doppler frequency shift fD from two processed signals with formulas provided in Introduction part. To find τ and fD, we can compute the cross-correlation of the two signals on frequency domain. The maximum value appears frequency domain on fD.   1. **Comparison between Ambiguity function and FFT() method** 2. Ambiguity Function   Firstly, we calculate the ambiguity function of reference data and surveillance data by traveling all possible (τ, fD), and select (τ’, f’) corresponding to the maximum value as the estimate value which τ' is the estimate of (τs - τr) and f’ is the estimate of fD. Use finite estimal method to calculate the Ambiguity Function   |  | | --- | | function [y] = AmbiguityFuntion(x1,x2,t,f,f\_s)  x2 = [zeros(1,ceil(t\*f\_s)) x2];  y = 0;  for i= 1:length(x1)  y = y + x1(i).\*conj(x2(i)).\*exp(-1i\*2\*pi\*f\*i\*(1/f\_s));  end  end |   For continues time:    For discrete time:     1. FFT Method   The ambiguity function is actually calculating the Fourier Transform of the cross-correlation. So we can directly compute the Correlation by fft() method. Since the duration of each data file is 0.5s, so the fundamental frequency is 1/0.5=2Hz. So we can fetch doppler frequency shift from -40Hz to 40Hz every 2 Hz as required. The realization code is as followed,   |  | | --- | | for t=1:length(tdoa)  s\_tau = [seq\_sur\_lpf(tdoa(t)+1:N),zeros(1,tdoa(t))];  temp(t,:) = fftshift(fft(s\_tau.\*conj(seq\_ref\_lpf)));  end  A\_TRD(idx\_start\_time,:,:) = temp(:, (-19+N/2:21+N/2)); |     To get the frequency components from -40Hz to 40Hz, the 41-medium components can be fetched after fftshift().  Using data\_1.mat file as an example, we can get exactly the same Range-Doppler spectrum from two method. To further investigate two methods, we compare them in the next step.   1. Complexity and Time   The calculate time of Ambiguity Function by fft() for each data. (t/s)   |  |  |  |  |  | | --- | --- | --- | --- | --- | | 4.73036920000000 | 3.91924190000000 | 3.87951340000000 | 3.97828320000000 | 3.91132390000000 | | 3.85358440000000 | 3.98467590000000 | 4.10776270000000 | 3.77962730000000 | 3.78376320000000 | | 3.88077600000000 | 4.11397910000000 | 4.13412020000000 | 3.74849250000000 | 4.13251750000000 | | 3.97507750000000 | 3.82223990000000 | 4.42361800000000 | 4.14010490000000 | 4.29882360000000 |     The calculate time of Ambiguity Function by integral for each data. (t/s)   |  |  |  |  |  | | --- | --- | --- | --- | --- | | 970.996146600000 | 964.537977000000 | 969.790953400000 | 979.566921200000 | 974.824273200000 | | 967.250441500000 | 962.859640900000 | 950.646226600000 | 950.099349900000 | 949.165743100000 | | 948.173874400000 | 950.717988700000 | 950.060159000000 | 948.684135400000 | 950.866340400000 | | 950.984549000000 | 953.039819700000 | 952.023245300000 | 949.247048200000 | 948.405483000000 |     From the result, we can say that the fft() method is much more efficient than integration method.   1. **Range-Doppler Spectrum**   Considering the velocity of this moving object is limited, it is not necessary to traverse all the τ and fD. Here we set the possible range of traversing—the travelling distance in 10 second is [0,72] (m), while the frequency is from -40 to 40 Hz.   1. 0-0.5 s   Doppler1  At time 0.0-0.5 s, the moving distance is around 12 m, the doppler frequency is around 4 Hz.   1. 2-2.5 s   Doppler5  At time 2.0-2.5 s, the moving distance is around 12 m, the doppler frequency is around 24 Hz.   1. 5-5.5 s   Doppler11  At time 5.0-5.5 s, the moving distance is around 0m, the doppler frequency is around -12 Hz.   1. 7-7.5 s   Doppler15  At time 7.0-7.5s, the moving distance is around 0 m, the doppler frequency is around -18 Hz.   1. Task 3   **Draw the Time-Doppler spectrum of the signal. We choose the maximum range of each data file, and put them together. CIT=0.5s.**  **The Time-Doppler Spectrum(TD spectrum)**  PZRLL{6BH)3UP`SY04`570O   1. Bonus and further research   **In Task 3, we draw the Time-Doppler spectrum of the signal with CIT=0.5s. To sketch a more accurate plot, we want CIT to be 0.1s. Then, with the relationship between Doppler frequency shift and velocity of the object, v-t and x-t graph can be created.**  To be cautious, 0.5s corresponds to fundamental frequency of 2Hz in frequency domain, 0.1s corresponds to 10 Hz. So we can’t directly use 0.1s signal to apply fft() method introduced in **Task2**. For CIT=0.1s, we extract 0.1s signal from data file first. After that, fill the rest of 0.4s with 0. Except this point, other procedures are exactly the same. The Time-Doppler spectrum is given below.  K{9OW48O`5N6)4QZ~`8IADK  Compare TD spectrum of CIT=0.5s with that of 0.1s, 0.1s-figure is more accurate. However, the plot is still confusing after t=9s.  Then, as we have already stored the maximum-value ranges for each duration, we can plot the Time-Range plot below.  IMG_256  With the formula connecting velocity and Doppler frequency shift, we plot v-t as follows.  IMG_256  However, v-t graph doesn’t match Time-range graph as expected. When t=2s-3s, the velocity is 2 meter per second, however, the range **doesn’t change** much in total. The reason is that one unit of TDOA(time difference of arrival) is 4e-8, so 12 meter for one unit of range. The speed is less than 2.5 meter per second, so the displacement is more likely to lower than 12 meter. As a result, the Time-range plot is not reliable enough to show the movement.  The velocity is more reliable. So we can calculate the exact displacement every moment by integrating velocity over time domain. The Displacement graph can be plotted below.  IMG_256 | |
| Experience |  |
| Distribution | 吴海涵、曾诗农、关馨语：30%；赵子昂：10% |
| Score |  |

1. Appendix
2. Task1 for 20 files

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| spectrum_duration1 | spectrum_duration2 |
| spectrum_duration3 | spectrum_duration4 |
| spectrum_duration5 | spectrum_duration6 |
| spectrum_duration7 | spectrum_duration8 |
| spectrum_duration9 | spectrum_duration10 |
| spectrum_duration11 | spectrum_duration12 |
| spectrum_duration13 | spectrum_duration14 |
| spectrum_duration15 | spectrum_duration16 |
| spectrum_duration17 | spectrum_duration18 |
| spectrum_duration19 | spectrum_duration20 |

1. Task2 for 30 files

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| **Doppler1** | Doppler2 |
| Doppler3 | Doppler4 |
| Doppler5 | Doppler6 |
| Doppler7 | Doppler8 |
| Doppler9 | Doppler10 |
| Doppler11 | Doppler12 |
| Doppler13 | Doppler14 |
| Doppler15 | Doppler16 |
| Doppler17 | Doppler18 |
| Doppler19 | Doppler20 |

### Experience

In this project, we learn how to calculate the velocity of moving object by signal from radar. The working principle is doppler principle and we apply it in practice by analysing the raw signal recorded by radar. After calculating the ambiguity function of the reference signal and surveillance signal, we can draw the doppler spectrum which clearly reflected the state of motion of the object. Furthermore, we were able to plot the v-t and x-t diagram.

From principle to practice, there were many details we should pay attention to. For example, how to remove the frequency we do not need? Here we need the Butterworth filter and DCC to pre process the signal. As for ambiguity function, we considered how to realize time shift for discrete signal and the range of traversing and interval of frequency and time are also critical. For bonus, we found that it is convenience to calculate ambiguity function by fft() in MATLAB, we have proved that in previous lab. After modified, the computation complexity significantly decrease.