assignment 03

September 24, 2021

1 Logistic regression for binary classification

1.1 import libraries

```
[]: import numpy as np
import matplotlib.pyplot as plt
import os
from tqdm import tqdm
```

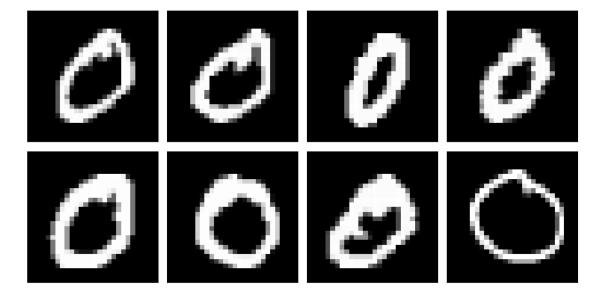
1.2 load data

```
[]: directory data = '/Users/lyuwan-u/Desktop/2021-2/
    →assignment-machine-learning-project/assignment03'
              = 'assignment_03_data.npz'
   filename data
   data
               = np.load(os.path.join(directory_data, filename_data))
   x_train = data['x_train']
   y_train = data['y_train']
   x test = data['x test']
   y_test = data['y_test']
   print('size of x_train :', x_train.shape)
   print('size of y_train :', y_train.shape)
   print('size of x_test :', x_test.shape)
   print('size of y_test :', y_test.shape)
   print('number of training image :', x_train.shape[0])
   print('height of training image :', x_train.shape[1])
   print('width of training image :', x_train.shape[2])
   print('number of testing image :', x_test.shape[0])
   print('height of testing image :', x_test.shape[1])
   print('width of testing image :', x_test.shape[2])
```

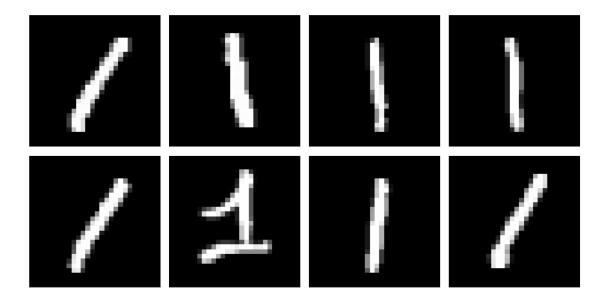
```
**************
   size of x_train : (10000, 28, 28)
   size of y_train : (10000,)
   **************
   size of x test: (1800, 28, 28)
   size of y_{test}: (1800,)
   *********
   number of training image: 10000
   height of training image: 28
   width of training image: 28
   *************
   number of testing image: 1800
   height of testing image: 28
   width of testing image: 28
    ***************
   $ git commit -m "YOUR MESSAGE" assignment_03.ipynb
   1.3 vectorize image data
[]: vector_x_train = x_train.reshape(x_train.shape[0], x_train.shape[1] * x_train.
     \rightarrowshape [2])
    vector x test
                   = x test.reshape(x test.shape[0], x test.shape[1] * x test.
     \rightarrowshape [2])
    print(vector_x_train.shape)
    print(vector_x_test.shape)
    (10000, 784)
    (1800, 784)
   $ git commit -m "YOUR MESSAGE" assignment_03.ipynb
    1.4 index for each class
[]: |index_train_0 = [i for i in range(len(y_train)) if y_train[i]==0]
    index_train_1 = [i for i in range(len(y_train)) if y_train[i]==1]
    index_test_0 = [i for i in range(len(y_test)) if y_test[i]==0]
    index_test_1 = [i for i in range(len(y_test)) if y_test[i]==1]
   $ git commit -m "YOUR MESSAGE" assignment_03.ipynb
   1.5 plot data
[]: def plot_data_grid(data, index_data, nRow, nCol):
        fig, axes = plt.subplots(nRow, nCol, constrained_layout=True, figsize=(nColu
     \rightarrow* 3, nRow * 3))
```

```
[]: nRow = 2
nCol = 4
nPlot = nRow * nCol
```

```
[]: index_data_0 = np.array(range(nPlot))
plot_data_grid(x_train, index_data_0, nRow, nCol)
```



```
[]: index_data_1 = index_data_0 + 5000
plot_data_grid(x_train, index_data_1, nRow, nCol)
```



\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.6 linear layer

```
[]: def layer_linear(input, weight):
    output = np.dot(input,weight.T)
    return output
```

\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.7 activation function: Sigmoid

```
[]: def activation_sigmoid(input):
    output = 1 / (1+np.exp(-input))
    return output
```

\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.8 compute prediction by the forward propagation of the neural network

```
[]: def compute_prediction(input, weight):
    output = layer_linear(input,weight)
    prediction = activation_sigmoid(output)
    return prediction
```

```
$ git commit -m "YOUR MESSAGE" assignment_03.ipynb
```

1.9 compute loss function

\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.10 compute gradient

```
[]: def compute_gradient(input, prediction, label):
    residual = (prediction-label).dot(input)
    gradient = residual / len(label)
    return gradient
```

\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.11 compute accuracy

\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.12 initialize weight

```
[]: length_weight = vector_x_train.shape[1]
  weight = np.ones(length_weight)
  weight = weight * 0.001

print('number of weights: ', length_weight)
```

number of weights: 784

```
$ git commit -m "YOUR MESSAGE" assignment_03.ipynb
```

1.13 hyper-parameters

```
[]: number_iteration = 1000
learning_rate = 0.1
```

1.14 variables for optimization information

```
[]: loss_train_iteration
                                 = np.zeros(number_iteration)
     loss_test_iteration
                                 = np.zeros(number_iteration)
     accuracy_train_iteration
                                = np.zeros(number_iteration)
     accuracy_test_iteration
                                 = np.zeros(number_iteration)
     pred_0_train_mean_iteration = np.zeros(number_iteration)
     pred_0_train_std_iteration = np.zeros(number_iteration)
     pred_1_train_mean_iteration = np.zeros(number_iteration)
     pred_1_train_std_iteration = np.zeros(number_iteration)
     pred_0_test_mean_iteration = np.zeros(number_iteration)
     pred_0_test_std_iteration = np.zeros(number_iteration)
     pred_1_test_mean_iteration = np.zeros(number_iteration)
     pred_1_test_std_iteration = np.zeros(number_iteration)
```

1.15 gradient descent iterations

```
[]: for i in tqdm(range(number_iteration)):
                             = compute_prediction(vector_x_train, weight)
        prediction_train
        prediction_test
                             = compute_prediction(vector_x_test, weight)
        gradient_train
      →compute_gradient(vector_x_train,prediction_train,y_train)
                             = weight - learning_rate * gradient_train
        weight
        prediction_train
                             = compute_prediction(vector_x_train, weight)
                             = compute_prediction(vector_x_test, weight)
        prediction_test
        loss_train
                             = compute_loss(prediction_train,y_train)
        loss_test
                             = compute_loss(prediction_test,y_test)
                             = compute_accuracy(prediction_train,y_train)
        accuracy_train
                             = compute_accuracy(prediction_test,y_test)
        accuracy test
                      = prediction train[index train 0]
        pred train 0
```

```
pred_train_1
                = prediction_train[index_train_1]
pred_test_0
                = prediction_test[index_test_0]
                = prediction_test[index_test_1]
pred_test_1
pred_0_train_mean_iteration[i] = np.mean(pred_train_0)
pred_0_train_std_iteration[i]
                                = np.std(pred_train_0)
pred_1_train_mean_iteration[i] = np.mean(pred_train_1)
pred_1_train_std_iteration[i]
                                = np.std(pred_train_1)
pred_0_test_mean_iteration[i]
                                = np.mean(pred_train_0)
pred_0_test_std_iteration[i]
                                = np.std(pred_train_0)
pred_1_test_mean_iteration[i]
                                = np.mean(pred_train_1)
pred_1_test_std_iteration[i]
                                = np.std(pred_train_1)
loss_train_iteration[i]
                                = loss_train
loss_test_iteration[i]
                                = loss_test
accuracy_train_iteration[i]
                                = accuracy_train
accuracy_test_iteration[i]
                                = accuracy_test
```

```
100% | 1000/1000 [00:59<00:00, 16.94it/s] 
$ git commit -m "YOUR MESSAGE" assignment_03.ipynb
```

1.16 plot curve

```
[]: def plot_curve(data, x_label, y_label, title):
    plt.figure(figsize=(8, 6))
    plt.title(title)

    plt.plot(range(len(data)), data, '-', color='red')

    plt.xlabel(x_label)
    plt.ylabel(y_label)

    plt.tight_layout()
    plt.show()
```

```
[]: def plot_curve2(data1, label_data1, data2, label_data2, x_label, y_label, u
→title):

plt.figure(figsize=(8, 6))
plt.title(title)

plt.plot(range(len(data1)), data1, '-', color = 'blue', label = label_data1)
```

```
plt.plot(range(len(data2)), data2, '-', color = 'red', label = label_data2)

plt.xlabel(x_label)

plt.ylabel(y_label)

plt.tight_layout()
plt.show()
```

```
[]: def plot_curve_error(data_mean, data_std, x_label, y_label, title):
    plt.figure(figsize=(8, 6))
    plt.title(title)
    alpha = 0.3

    plt.plot(range(len(data_mean)), data_mean, '-', color = 'red')
    plt.fill_between(range(len(data_mean)), data_mean - data_std, data_mean +_u
    data_std, facecolor = 'blue', alpha = alpha)

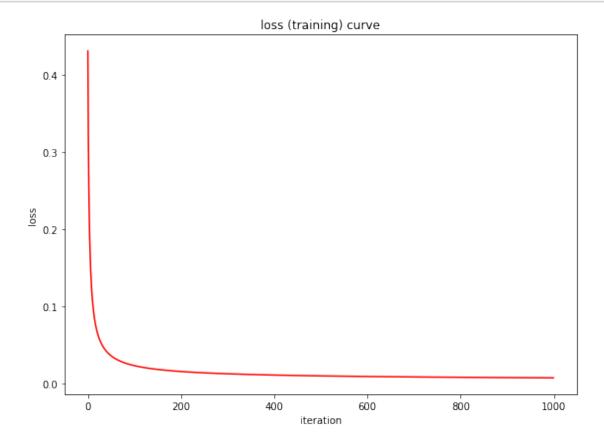
plt.xlabel(x_label)
    plt.ylabel(y_label)

plt.tight_layout()
    plt.show()
```

```
plt.tight_layout()
plt.show()
```

1.17 loss (training) curve

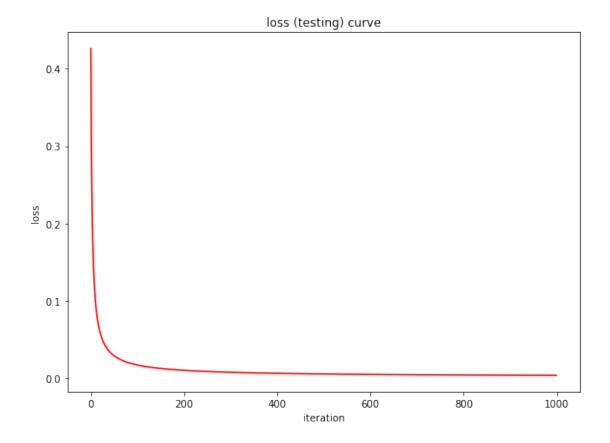
```
[]: plot_curve(loss_train_iteration, 'iteration', 'loss', 'loss (training) curve')
```



\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.18 loss (testing) curve

```
[]: plot_curve(loss_test_iteration, 'iteration', 'loss', 'loss (testing) curve')
```

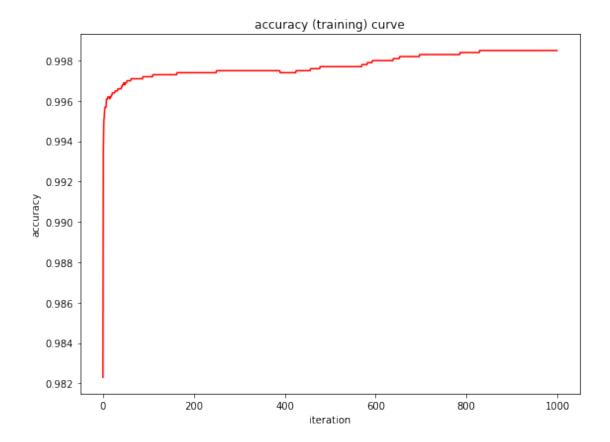


\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.19 accuracy (training) curve

```
[]: plot_curve(accuracy_train_iteration, 'iteration', 'accuracy', 'accuracy⊔

→(training) curve')
```

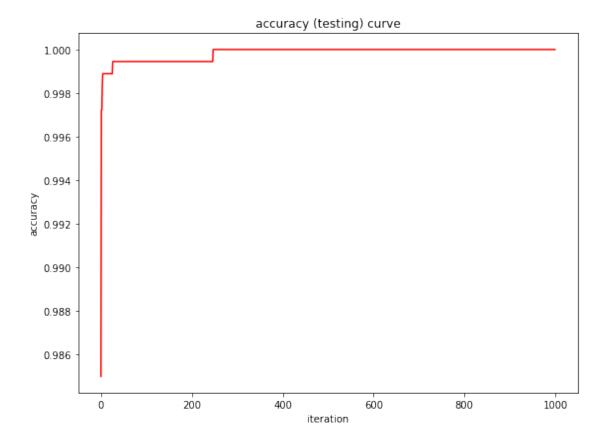


\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.20 accuracy (testing) curve

```
[]: plot_curve(accuracy_test_iteration, 'iteration', 'accuracy', 'accuracy

→(testing) curve')
```

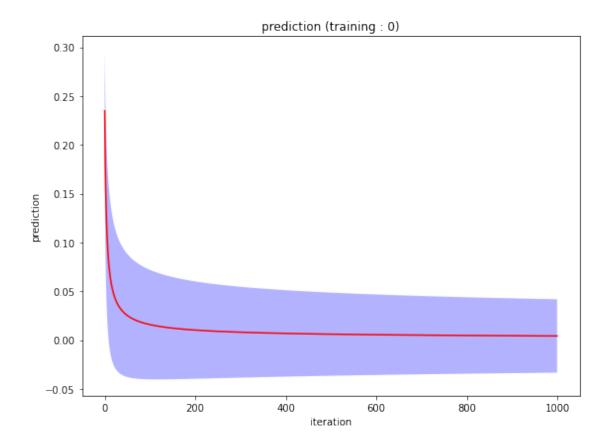


\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.21 plot prediction values

```
[]: plot_curve_error(pred_0_train_mean_iteration, pred_0_train_std_iteration, 

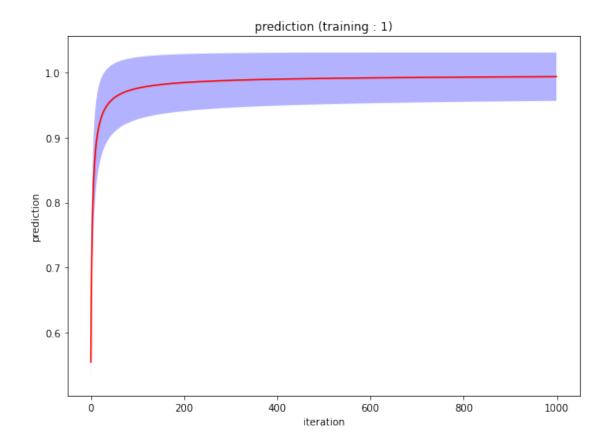
→'iteration', 'prediction', 'prediction (training : 0)')
```



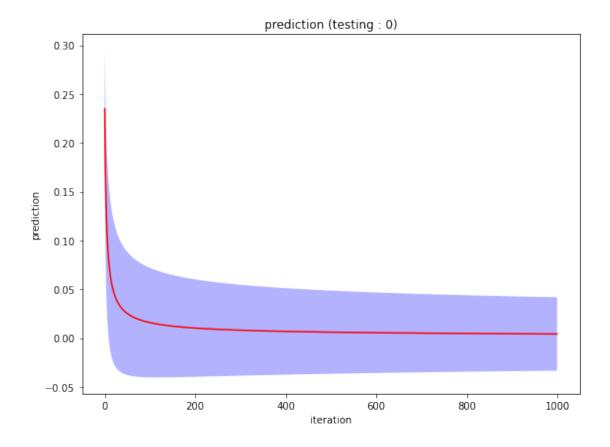
\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

```
[]: plot_curve_error(pred_1_train_mean_iteration, pred_1_train_std_iteration, 

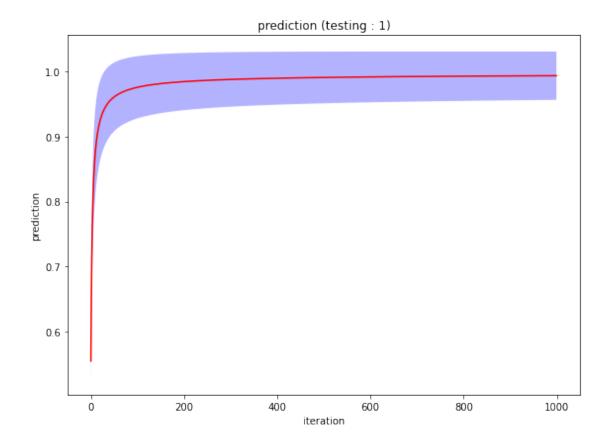
⇔'iteration', 'prediction', 'prediction (training : 1)')
```



```
$ git commit -m "YOUR MESSAGE" assignment_03.ipynb
```



\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb



\$ git commit -m "YOUR MESSAGE" assignment_03.ipynb

1.22 print values

```
[]: def print_curve(data, index):
    for i in range(len(index)):
        idx = index[i]
        val = data[idx]
        print('index = %4d, value = %12.10f' % (idx, val))
```

1.23 given iterations at which the values are presented

```
[]: index = np.array([0, 100, 200, 300, 400, 500, 600, 700, 800, 900])
```

1.24 training loss

```
[]: print_curve(loss_train_iteration, index)
    index =
               0, value = 0.4307224938
    index = 100, value = 0.0228587163
    index = 200, value = 0.0152848437
    index = 300, value = 0.0123252409
    index = 400, value = 0.0106733249
    index = 500, value = 0.0095914393
    index = 600, value = 0.0088148843
    index = 700, value = 0.0082233149
    index = 800, value = 0.0077534390
    index = 900, value = 0.0073684871
    $ git commit -m "YOUR MESSAGE" assignment_03.ipynb
          testing loss
    1.25
[]: print_curve(loss_test_iteration, index)
    index =
               0, value = 0.4263057540
    index = 100, value = 0.0167458571
    index = 200, value = 0.0099479648
    index = 300, value = 0.0074345387
    index = 400, value = 0.0060961283
    index = 500, value = 0.0052563282
    index = 600, value = 0.0046772451
    index = 700, value = 0.0042526445
    index = 800, value = 0.0039275776
    index = 900, value = 0.0036706180
    $ git commit -m "YOUR MESSAGE" assignment_03.ipynb
    1.26 training accuracy
[]: print_curve(accuracy_train_iteration, index)
               0, value = 0.9823000000
    index =
    index = 100, value = 0.9972000000
    index = 200, value = 0.9974000000
    index = 300, value = 0.9975000000
    index = 400, value = 0.9974000000
    index = 500, value = 0.9977000000
    index = 600, value = 0.9980000000
    index = 700, value = 0.9983000000
    index = 800, value = 0.9984000000
    index = 900, value = 0.9985000000
```

```
$ git commit -m "YOUR MESSAGE" assignment_03.ipynb
```

1.27 testing accuracy

```
index = 0, value = 0.9850000000
index = 100, value = 0.9994444444
index = 200, value = 0.9994444444
index = 300, value = 1.0000000000
index = 400, value = 1.0000000000
index = 500, value = 1.0000000000
index = 600, value = 1.0000000000
index = 600, value = 1.0000000000
index = 700, value = 1.0000000000
index = 800, value = 1.0000000000
index = 800, value = 1.00000000000
index = 900, value = 1.00000000000
$ git commit -m "YOUR MESSAGE" assignment_03.ipynb
```

1.28 functions for presenting the results

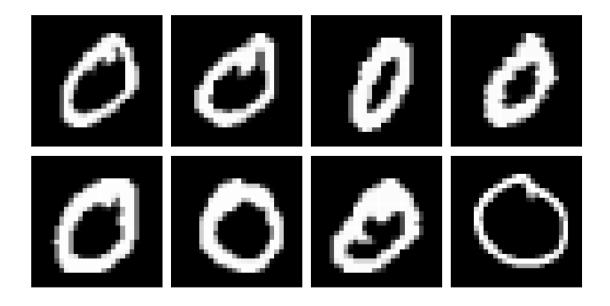
```
def function_results_01(data,nRow,nCol):
    nPlot = nRow * nCol
    index_data = np.array(range(nPlot))
    fig, axes = plt.
    subplots(nRow,nCol,constrained_layout=True,figsize=(nCol*3,nRow*3))

for i in range(nRow):
    for j in range(nCol):

        k = i * nCol + j
        index = index_data[k]

        axes[i,j].imshow(data[index],cmap='gray',vmin=0,vmax=1)
        axes[i,j].xaxis.set_visible(False)
        axes[i,j].yaxis.set_visible(False)
    plt.show()
```

```
[]: function_results_01(x_train,2,4)
```



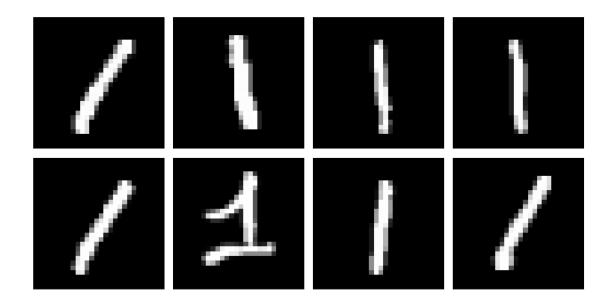
```
def function_results_02(data,nRow,nCol):
    nPlot = nRow * nCol
    index_data = np.array(range(nPlot))
    index_data = index_data + 5000
    fig, axes = plt.
    subplots(nRow,nCol,constrained_layout=True,figsize=(nCol*3,nRow*3))

for i in range(nRow):
    for j in range(nCol):

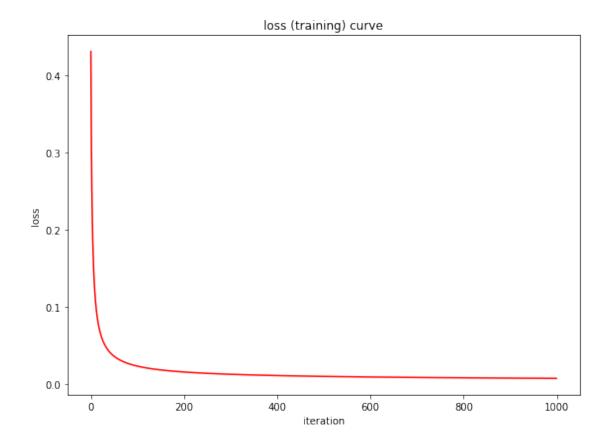
        k = i * nCol + j
        index = index_data[k]

        axes[i,j].imshow(data[index],cmap='gray',vmin=0,vmax=1)
        axes[i,j].xaxis.set_visible(False)
        axes[i,j].yaxis.set_visible(False)
        plt.show()
```

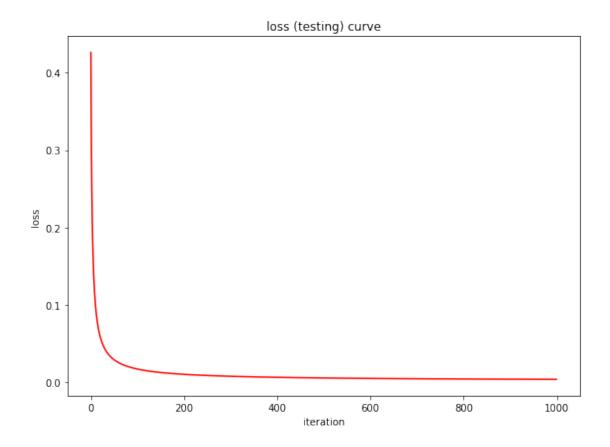
[]: function_results_02(x_train,nRow=2,nCol=4)

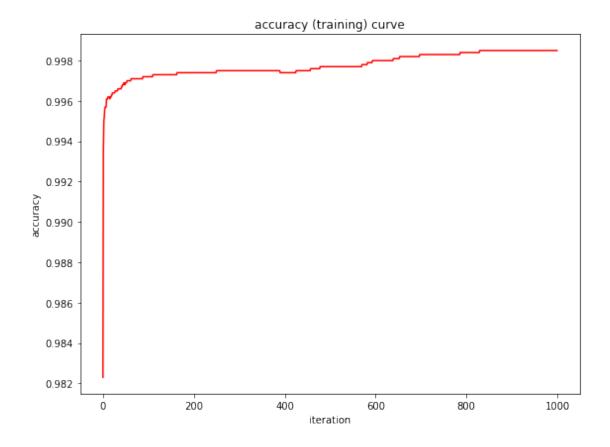


[]: function_results_03()



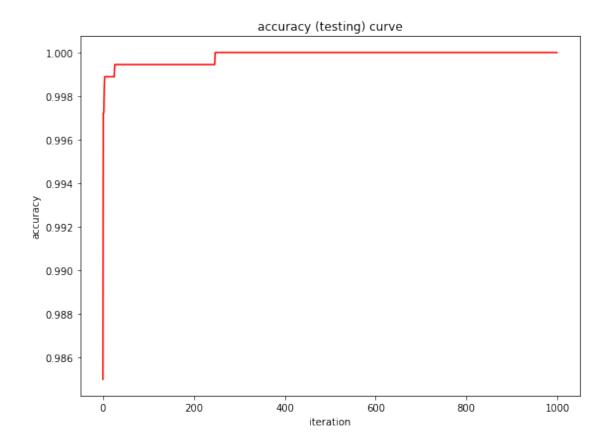
```
[]: def function_results_04():
    plot_curve(loss_test_iteration, 'iteration', 'loss', 'loss (testing) curve')
[]: function_results_04()
```





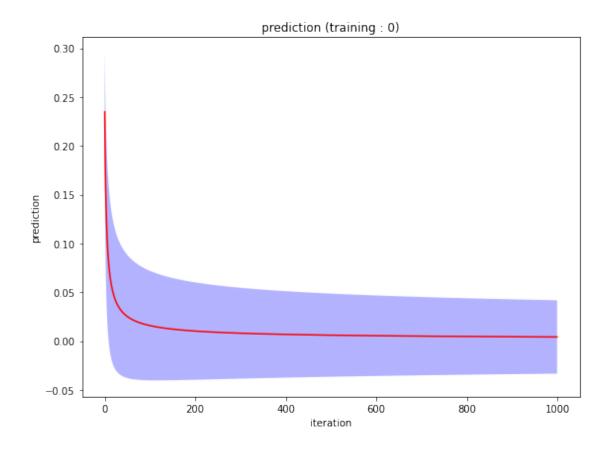
```
[]: def function_results_06():
    plot_curve(accuracy_test_iteration, 'iteration', 'accuracy', 'accuracy
    →(testing) curve')

[]: function_results_06()
```



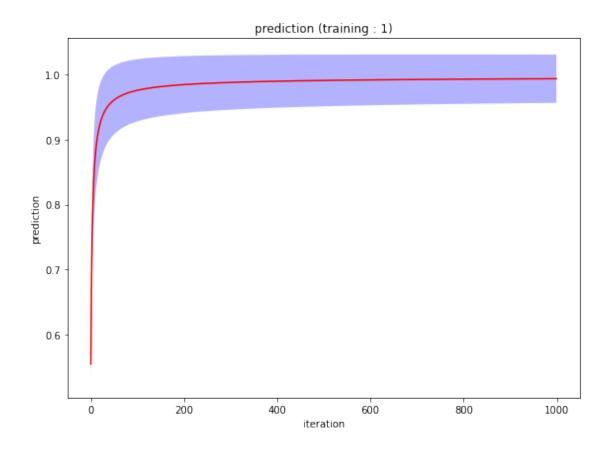
```
[]: def function_results_07():
    plot_curve_error(pred_0_train_mean_iteration, pred_0_train_std_iteration,
    →'iteration', 'prediction', 'prediction (training : 0)')

[]: function_results_07()
```



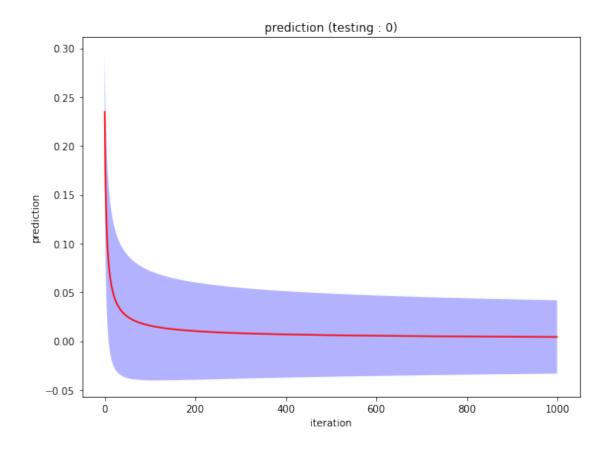
```
[]: def function_results_08():
    plot_curve_error(pred_1_train_mean_iteration, pred_1_train_std_iteration,
    →'iteration', 'prediction', 'prediction (training : 1)')

[]: function_results_08()
```

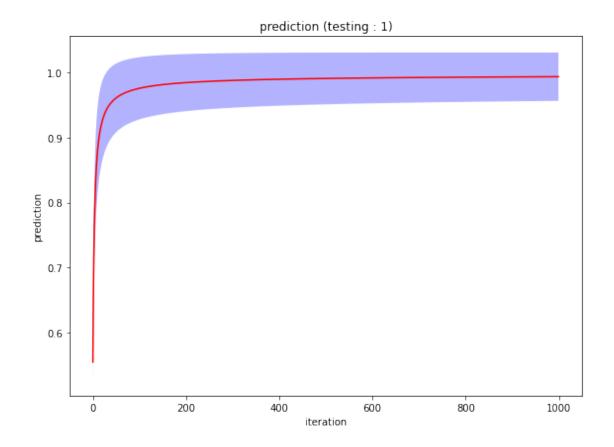


```
[]: def function_results_09():
    plot_curve_error(pred_0_test_mean_iteration, pred_0_test_std_iteration,
    →'iteration', 'prediction', 'prediction (testing : 0)')

[]: function_results_09()
```



```
[]: def function_results_10():
    plot_curve_error(pred_1_test_mean_iteration, pred_1_test_std_iteration, used_iteration, pred_iteration, pr
```



```
[]: def function_results_11(data):
    index = np.array([0,100,200,300,400,500,600,700,800,900])
    for idx in index:
        val = data[idx]
        print('index = %4d, value = %12.10f' % (idx, val))
[]: function_results_11(loss_train_iteration)
```

```
index = 0, value = 0.4307224938

index = 100, value = 0.0228587163

index = 200, value = 0.0152848437

index = 300, value = 0.0123252409

index = 400, value = 0.0106733249

index = 500, value = 0.0095914393

index = 600, value = 0.0088148843

index = 700, value = 0.0082233149

index = 800, value = 0.0077534390

index = 900, value = 0.0073684871
```

```
[]: def function_results_12(data):
         index = np.array([0,100,200,300,400,500,600,700,800,900])
        for idx in index:
            val = data[idx]
            print('index = %4d, value = %12.10f' % (idx, val))
[]: function_results_12(loss_test_iteration)
               0, value = 0.4263057540
    index =
    index = 100, value = 0.0167458571
    index = 200, value = 0.0099479648
    index = 300, value = 0.0074345387
    index = 400, value = 0.0060961283
    index = 500, value = 0.0052563282
    index = 600, value = 0.0046772451
    index = 700, value = 0.0042526445
    index = 800, value = 0.0039275776
    index = 900, value = 0.0036706180
[]: def function_results_13(data):
         index = np.array([0,100,200,300,400,500,600,700,800,900])
        for idx in index:
            val = data[idx]
            print('index = %4d, value = %12.10f' % (idx, val))
[]: function_results_13(accuracy_train_iteration)
               0, value = 0.9823000000
    index =
    index = 100, value = 0.9972000000
    index = 200, value = 0.9974000000
    index = 300, value = 0.9975000000
    index = 400, value = 0.9974000000
    index = 500, value = 0.9977000000
    index = 600, value = 0.9980000000
    index = 700, value = 0.9983000000
    index = 800, value = 0.9984000000
    index = 900, value = 0.9985000000
[]: def function_results_14(data):
         index = np.array([0,100,200,300,400,500,600,700,800,900])
        for idx in index:
```

```
val = data[idx]
print('index = %4d, value = %12.10f' % (idx, val))
```

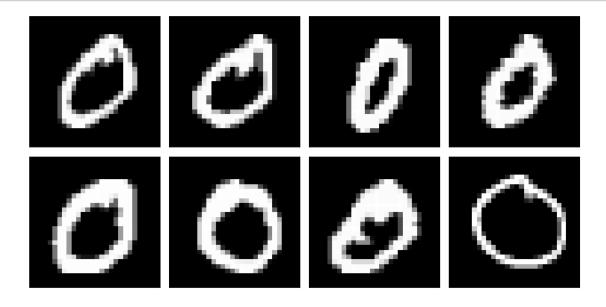
[]: function_results_14(accuracy_test_iteration)

```
index = 0, value = 0.9850000000
index = 100, value = 0.9994444444
index = 200, value = 0.9994444444
index = 300, value = 1.0000000000
index = 400, value = 1.0000000000
index = 500, value = 1.0000000000
index = 600, value = 1.0000000000
index = 700, value = 1.0000000000
index = 800, value = 1.0000000000
index = 900, value = 1.0000000000
```

2 RESULTS

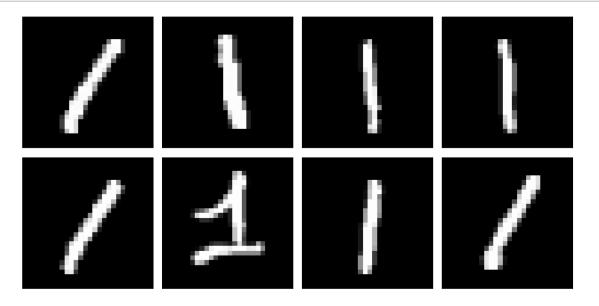
2.1 # 01. plot examples of the input training images for '0'

[]: function_results_01(x_train,2,4)



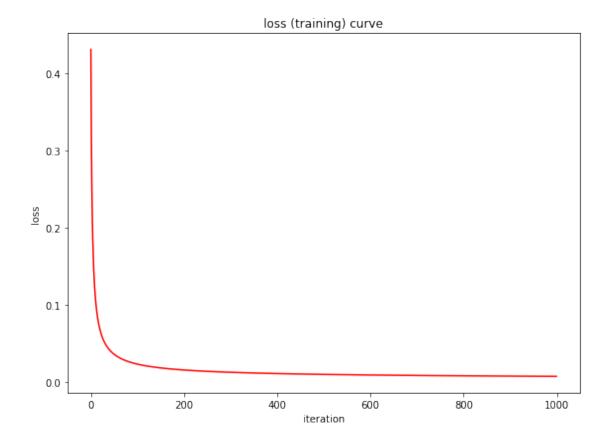
2.2 # 02. plot examples of the input training images for '1'

[]: function_results_02(x_train,2,4)



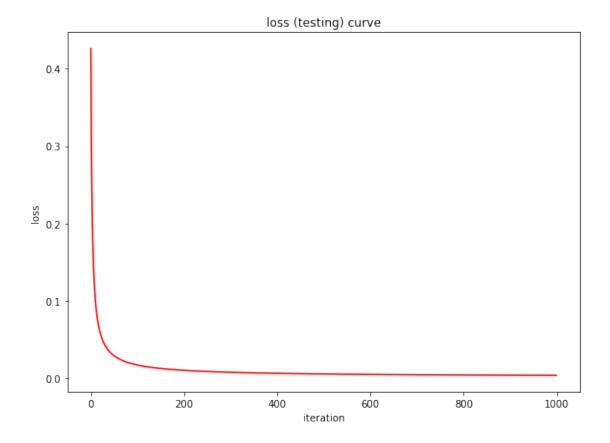
2.3 # 03. plot the training loss curve (x-axis: iteration, y-axis: loss)

[]: function_results_03()



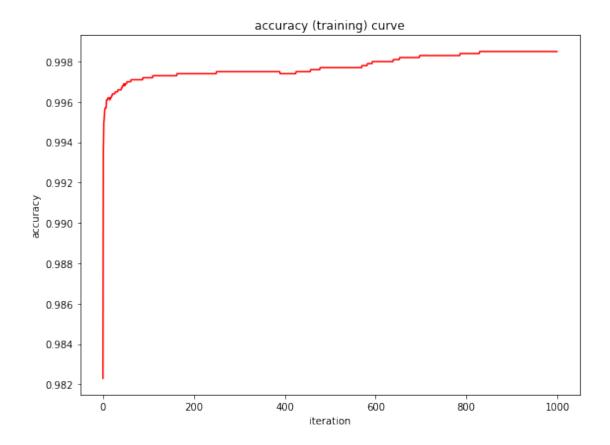
2.4~#~04. plot the testing loss curve (x-axis: iteration, y-axis: loss)

[]: function_results_04()



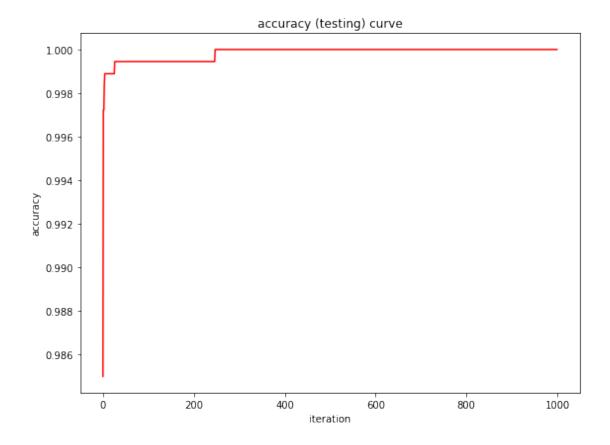
2.5~#~05. plot the training accuracy curve (x-axis: iteration, y-axis: accuracy)

[]: function_results_05()



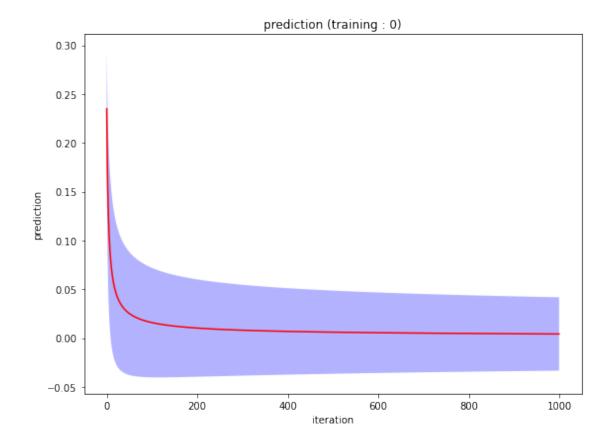
2.6 # 06. plot the testing accuracy curve (x-axis: iteration, y-axis: accuracy)

[]: function_results_06()



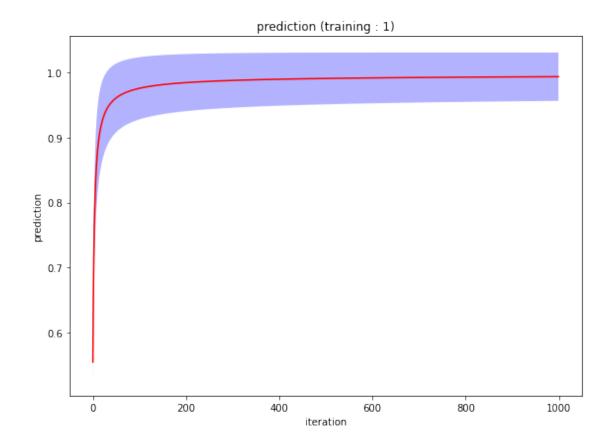
2.7 # 07. plot the training prediction curve (mean and std) for image 0 (x-axis: iteration, y-axis: prediction)

```
[]: function_results_07()
```



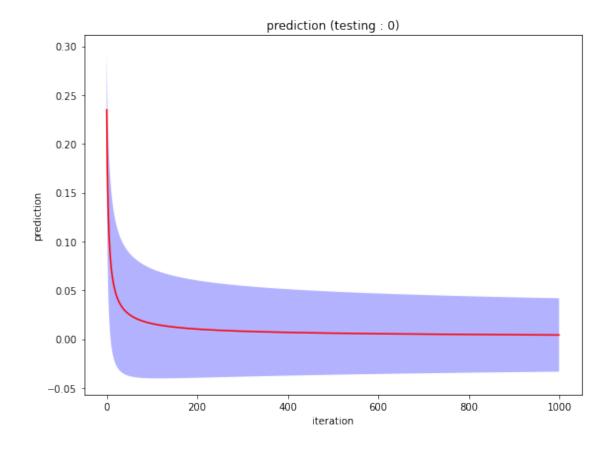
2.8 # 08. plot the training prediction curve (mean and std) for image 1 (x-axis: iteration, y-axis: prediction)

[]: function_results_08()



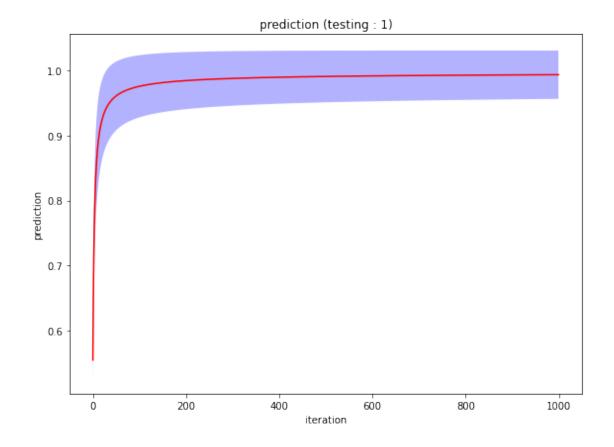
2.9 # 09. plot the testing prediction curve (mean and std) for image 0 (x-axis: iteration, y-axis: prediction)

[]: function_results_09()



2.10 # 10. plot the testing prediction curve (mean and std) for image 1 (x-axis: iteration, y-axis: prediction)

[]: function_results_10()



$2.11 \quad \# \ 11.$ print the training loss at iterations 0, 100, 200, 300, 400, 500, 600, 700, 800, 900

[]: function_results_11(loss_train_iteration)

```
index = 0, value = 0.4307224938

index = 100, value = 0.0228587163

index = 200, value = 0.0152848437

index = 300, value = 0.0123252409

index = 400, value = 0.0106733249

index = 500, value = 0.0095914393

index = 600, value = 0.0082233149

index = 700, value = 0.0077534390

index = 900, value = 0.0073684871
```

2.12 # 12. print the testing loss at iterations 0, 100, 200, 300, 400, 500, 600, 700, 800, 900

```
[]: function_results_12(loss_test_iteration)
    index =
               0, value = 0.4263057540
    index =
            100, value = 0.0167458571
    index = 200, value = 0.0099479648
    index = 300, value = 0.0074345387
    index = 400, value = 0.0060961283
    index = 500, value = 0.0052563282
    index = 600, value = 0.0046772451
    index = 700, value = 0.0042526445
    index = 800, value = 0.0039275776
    index = 900, value = 0.0036706180
          # 13. print the training accuracy at iterations 0, 100, 200, 300, 400, 500,
          600, 700, 800, 900
[]: function_results_13(accuracy_train_iteration)
    index =
               0, value = 0.9823000000
    index = 100, value = 0.9972000000
    index = 200, value = 0.9974000000
    index = 300, value = 0.9975000000
    index = 400, value = 0.9974000000
    index = 500, value = 0.9977000000
    index = 600, value = 0.9980000000
    index = 700, value = 0.9983000000
    index = 800, value = 0.9984000000
    index = 900, value = 0.9985000000
          # 14. print the testing accuracy at iterations 0, 100, 200, 300, 400, 500,
          600, 700, 800, 900
[]: function_results_14(accuracy_test_iteration)
               0, value = 0.9850000000
    index =
    index = 100, value = 0.9994444444
    index = 200, value = 0.9994444444
    index = 300, value = 1.0000000000
    index = 400, value = 1.0000000000
    index = 500, value = 1.0000000000
    index = 600, value = 1.0000000000
    index = 700, value = 1.0000000000
    index = 800, value = 1.0000000000
    index = 900, value = 1.0000000000
```