# assignment\_04

September 30, 2021

# 1 Classification for multiple classes based on softmax and cross entropy

## 1.1 import libraries

```
[]: import numpy as np
import matplotlib.pyplot as plt
import os
from tqdm import tqdm
```

#### 1.2 load data

```
[]: directory_data = '/Users/lyuwan-u/Desktop/2021-2/
    →assignment-machine-learning-project/assignment04'
   filename data
                = 'assignment 04 data.npz'
   data
                = np.load(os.path.join(directory_data, filename_data))
   x_train = data['x_train']
   y_train = data['y_train']
   x_test = data['x_test']
   y_test = data['y_test']
   print('size of x_train :', x_train.shape)
   print('size of y_train :', y_train.shape)
   print('size of x_test :', x_test.shape)
   print('size of y_test :', y_test.shape)
   print('number of training image :', x_train.shape[0])
   print('height of training image :', x_train.shape[1])
   print('width of training image :', x_train.shape[2])
   print('number of testing image :', x_test.shape[0])
   print('height of testing image :', x_test.shape[1])
   print('width of testing image :', x_test.shape[2])
```

```
****************
   size of x_train : (10000, 28, 28)
   size of y_train : (10000, 5)
   *************
   size of x_{test}: (4500, 28, 28)
   size of y_test : (4500, 5)
    **************
   number of training image: 10000
   height of training image: 28
   width of training image: 28
   *************
   number of testing image: 4500
   height of testing image: 28
   width of testing image: 28
   *************
   1.3 number of classes
[]: nClass = y train.shape[1]
    print('number of classes: ', nClass)
   number of classes: 5
   1.4 label data
[]: print('label data for training image 0: ', y_train[0])
    print('label data for training image 1: ', y_train[2000])
    print('label data for training image 2: ', y_train[4000])
    print('label data for training image 3: ', y_train[6000])
    print('label data for training image 4: ', y_train[8000])
   label data for training image 0: [1. 0. 0. 0. 0.]
   label data for training image 1: [0. 1. 0. 0. 0.]
   label data for training image 2: [0. 0. 1. 0. 0.]
   label data for training image 3: [0. 0. 0. 1. 0.]
   label data for training image 4: [0. 0. 0. 0. 1.]
   1.5 vectorize image data
[]: vector_x_train = x_train.reshape(x_train.shape[0], x_train.shape[1] * x_train.
    \rightarrowshape [2])
    vector_x_test
                  = x_test.reshape(x_test.shape[0], x_test.shape[1] * x_test.
     \rightarrowshape[2])
    print('dimension of the training data matrix: ', vector_x_train.shape)
    print('dimension of the testing data matrix: ', vector_x_test.shape)
```

```
print('dimension of the trainin label data: ', y_train.shape)
print('dimension of the testing label data: ', y_test.shape)
```

```
dimension of the training data matrix: (10000, 784) dimension of the testing data matrix: (4500, 784) dimension of the trainin label data: (10000, 5) dimension of the testing label data: (4500, 5)
```

#### 1.6 index for each class

```
[]: index_train = [[0] for i in range(nClass)]
index_test = [[0] for i in range(nClass)]

number_index_train = np.zeros(nClass)
number_index_test = np.zeros(nClass)

for i in range(nClass):

   index_train[i] = [[j for j in range(len(y_train)) if y_train[j][i] == 1]]
   index_test[i] = [[j for j in range(len(y_test)) if y_test[j][i] == 1]]

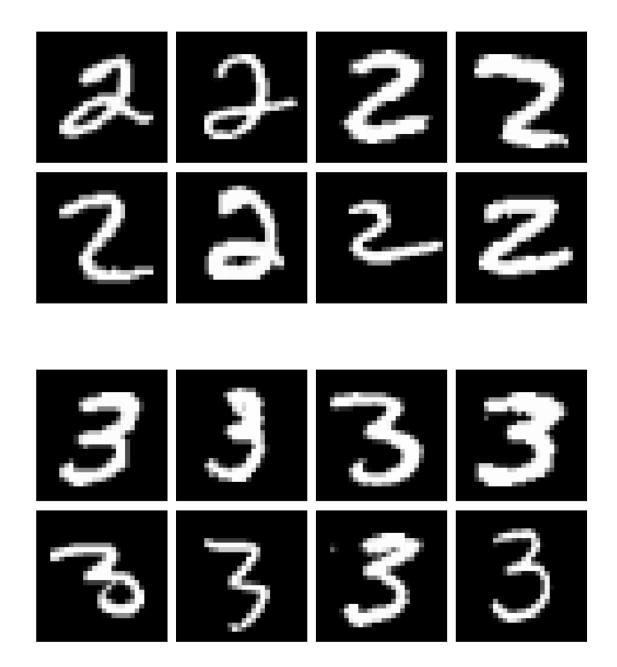
   number_index_train[i] = len(index_train[i][0])
   number_index_test[i] = len(index_test[i][0])

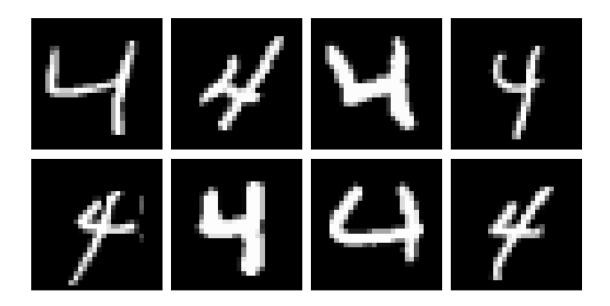
print('number of training images for each class: ', number_index_test)
```

```
number of training images for each class: [2000. 2000. 2000. 2000. 2000.] number of testing images for each class: [900. 900. 900. 900. 900.]
```

#### 1.7 plot data

```
plt.show()
[]: nRow
     nCol
             = 4
     nPlot
             = nRow * nCol
[]: for i in range(nClass):
         index_class_plot = index_train[i][0][0:nPlot]
        plot_data_grid(x_train, index_class_plot, nRow, nCol)
```





## 1.8 linear layer

```
[]: dim_input = vector_x_train.shape[1]
    dim_output = nClass
    weight = np.ones((dim_output, dim_input))
    weight = weight * 0.001

    print('size of weights: ', weight.shape)

size of weights: (5, 784)

[]: def layer_linear(input, weight):
    output = np.dot(input,weight.T)
    return output
```

## 1.9 Softmax function

```
[]: def activation_softmax(input):
    input_exp = np.exp(input)
    partition = input_exp.sum(axis=1,keepdims=True)
    output = input_exp / partition
    return output
```

## 1.10 compute prediction by the forward propagation of the neural network

```
[]: def compute_prediction(input, weight):
    output = layer_linear(input,weight)
    prediction = activation_softmax(output)
    return prediction
```

#### 1.11 compute loss function

```
[]: def compute_loss(prediction, label):
    pred = np.log(prediction)
    loss = -(np.sum(np.sum(label*pred,axis=1)))/label.shape[0]
    return loss
```

```
[]: compute_loss(compute_prediction(vector_x_train,weight),y_train)
```

[]: 1.6094379124340998

```
[]: t = np.dot((compute_prediction(vector_x_train, weight)-y_train).T,vector_x_train)
print(t.shape)
```

(5, 784)

## 1.12 compute gradient

```
[]: def compute_gradient(input, prediction, label):
    gradient = np.dot((prediction-label).T,input)
    gradient = gradient / len(label)
    return gradient
```

```
[]: compute_gradient(vector_x_train,compute_prediction(vector_x_train,weight),y_train)
```

```
[]: array([[0., 0., 0., ..., 0., 0., 0.], [0., 0., 0., ..., 0., 0., 0.], [0., 0., 0., ..., 0., 0., 0.], [0., 0., 0., ..., 0., 0., 0.], [0., 0., 0., ..., 0., 0., 0.]])
```

### 1.13 compute accuracy

learning\_rate

= 0.5

```
[]: temp = compute_prediction(vector_x_train, weight)
     print(temp)
     print(max(temp[0]))
     print(np.where(temp[0] == max(temp[0])))
    [[0.2 0.2 0.2 0.2 0.2]
     [0.2 0.2 0.2 0.2 0.2]
     [0.2 0.2 0.2 0.2 0.2]
     [0.2 0.2 0.2 0.2 0.2]
     [0.2 0.2 0.2 0.2 0.2]
     [0.2 0.2 0.2 0.2 0.2]]
    (array([0, 1, 2, 3, 4]),)
[]: def compute accuracy(prediction, label):
                   = [True if list(prediction[i]).
     →index(max(prediction[i]))==list(label[i]).index(1) else False for i in_
      →range(len(label))]
        accuracy
                    = np.sum(bCorrect) / len(label)
        return accuracy
[]: compute_accuracy(compute_prediction(vector_x_train, weight), y_train)
[]: 0.2
    1.14 initialize weight
[]: dim_input = vector_x_train.shape[1]
     dim_output = nClass
     weight
                = np.ones((dim_output, dim_input))
                = weight * 0.001
     weight
    print('size of weights: ', weight.shape)
    size of weights: (5, 784)
    1.15 hyper-parameters
[]: number_iteration
                        = 2000
```

#### 1.16 variables for optimization information

```
[]: loss train iteration
                                 = np.zeros(number iteration)
     loss_test_iteration
                                 = np.zeros(number_iteration)
                                 = np.zeros(number_iteration)
     accuracy_train_iteration
                                 = np.zeros(number_iteration)
     accuracy_test_iteration
     pred_train_mean_iteration
                                 = np.zeros((nClass, number_iteration))
                                 = np.zeros((nClass, number_iteration))
     pred_train_std_iteration
                                 = np.zeros((nClass, number_iteration))
     pred_test_mean_iteration
     pred_test_std_iteration
                                 = np.zeros((nClass, number_iteration))
```

#### 1.17 gradient descent iterations

```
[]: for i in tqdm(range(number_iteration)):
        prediction_train
                            = compute_prediction(vector_x_train, weight)
        prediction_test
                            = compute_prediction(vector_x_test, weight)
        gradient_train
     →compute_gradient(vector_x_train,prediction_train,y_train)
                             = weight - learning_rate * gradient_train
        weight
        prediction_train
                            = compute_prediction(vector_x_train, weight)
        prediction_test
                            = compute_prediction(vector_x_test, weight)
                             = compute_loss(prediction_train,y_train)
        loss_train
        loss_test
                            = compute_loss(prediction_test,y_test)
        accuracy_train
                            = compute_accuracy(prediction_train,y_train)
                             = compute accuracy(prediction test, y test)
        accuracy_test
        for j in range(nClass):
                          = prediction_train[index_train[j][0]][:, j]
            pred_train
                          = prediction_test[index_test[j][0]][:, j]
            pred_test
            pred_train_mean_iteration[j, i] = np.mean(pred_train)
            pred_train_std_iteration[j, i] = np.std(pred_train)
            pred_test_mean_iteration[j, i] = np.mean(pred_test)
            pred_test_std_iteration[j, i] = np.std(pred_test)
        loss train iteration[i]
                                        = loss train
        loss_test_iteration[i]
                                         = loss_test
```

```
accuracy_train_iteration[i] = accuracy_train
accuracy_test_iteration[i] = accuracy_test
```

100%| | 2000/2000 [05:34<00:00, 5.97it/s]

### 1.18 plot curve

```
[]: def plot_curve(data, x_label, y_label, title):
    plt.figure(figsize=(8, 6))
    plt.title(title)

    plt.plot(range(len(data)), data, '-', color='red')

    plt.xlabel(x_label)
    plt.ylabel(y_label)

    plt.tight_layout()
    plt.show()
```

```
[]: def plot_curve_error(data_mean, data_std, x_label, y_label, title):
    plt.figure(figsize=(8, 6))
    plt.title(title)
    alpha = 0.3

    plt.plot(range(len(data_mean)), data_mean, '-', color = 'red')
    plt.fill_between(range(len(data_mean)), data_mean - data_std, data_mean +_u
    data_std, facecolor = 'blue', alpha = alpha)

plt.xlabel(x_label)
```

```
plt.ylabel(y_label)

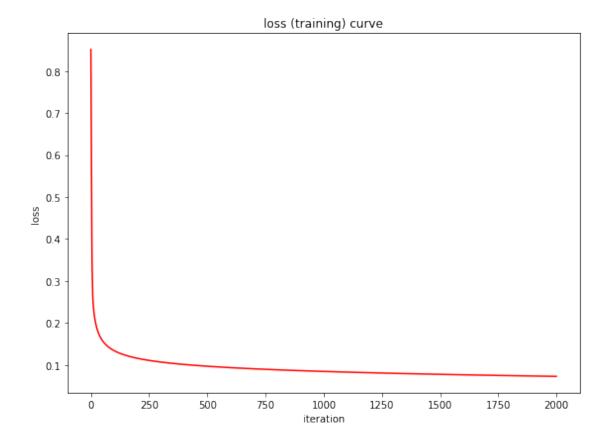
plt.tight_layout()

plt.show()
```

```
[]: def plot_curve_error2(data1_mean, data1_std, data1_label, data2_mean,__
     →data2_std, data2_label, x_label, y_label, title):
         plt.figure(figsize=(8, 6))
         plt.title(title)
         alpha = 0.3
         plt.plot(range(len(data1_mean)), data1_mean, '-', color = 'blue', label =_
     →data1_label)
         plt.fill_between(range(len(data1_mean)), data1_mean - data1_std, data1_mean_
     →+ data1_std, facecolor = 'blue', alpha = alpha)
         plt.plot(range(len(data2_mean)), data2_mean, '-', color = 'red', label = __
     →data2_label)
         plt.fill_between(range(len(data2_mean)), data2_mean - data2_std, data2_mean⊔
     →+ data2_std, facecolor = 'red', alpha = alpha)
         plt.xlabel(x_label)
         plt.ylabel(y_label)
         plt.tight_layout()
         plt.show()
```

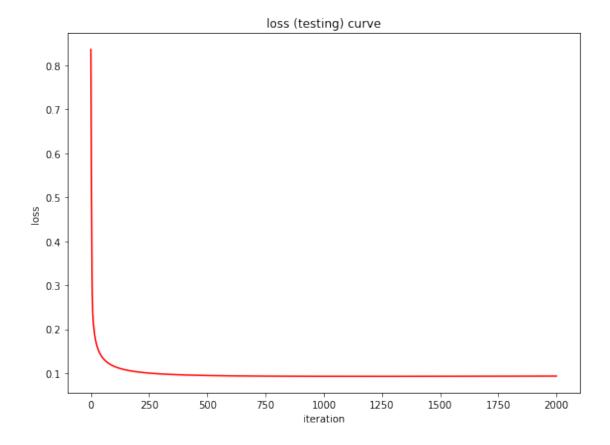
## 1.19 loss (training) curve

```
[]: plot_curve(loss_train_iteration, 'iteration', 'loss', 'loss (training) curve')
```



# 1.20 loss (testing) curve

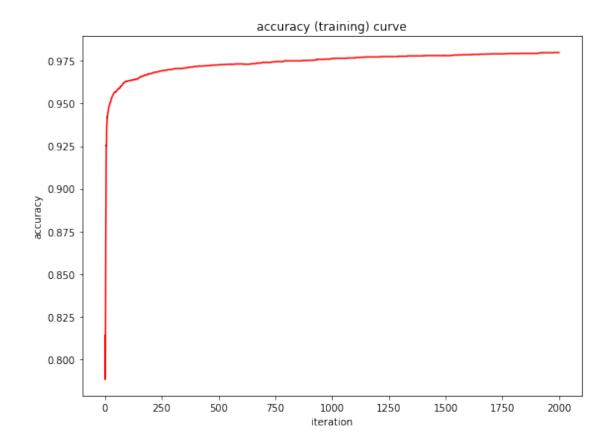
```
[]: plot_curve(loss_test_iteration, 'iteration', 'loss', 'loss (testing) curve')
```



# 1.21 accuracy (training) curve

```
[]: plot_curve(accuracy_train_iteration, 'iteration', 'accuracy', 'accuracy⊔

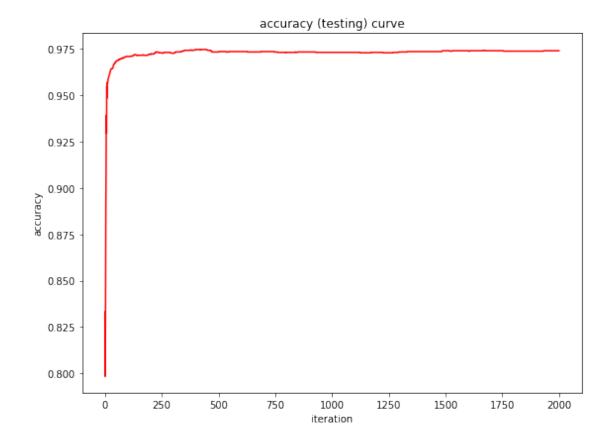
⇔(training) curve')
```



# 1.22 accuracy (testing) curve

```
[]: plot_curve(accuracy_test_iteration, 'iteration', 'accuracy', 'accuracy⊔

⇔(testing) curve')
```

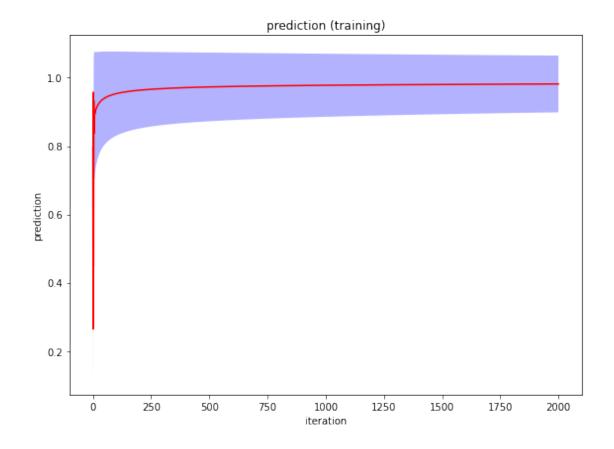


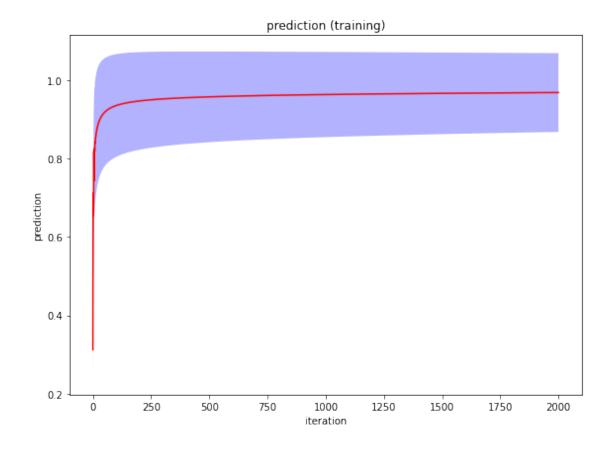
# 1.23 plot prediction values

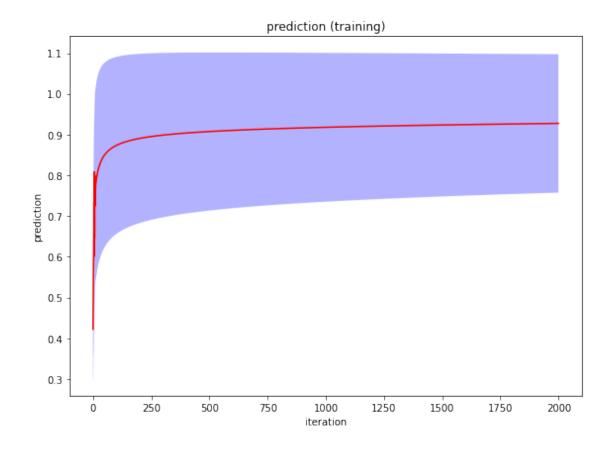
```
[]: for i in range(nClass):

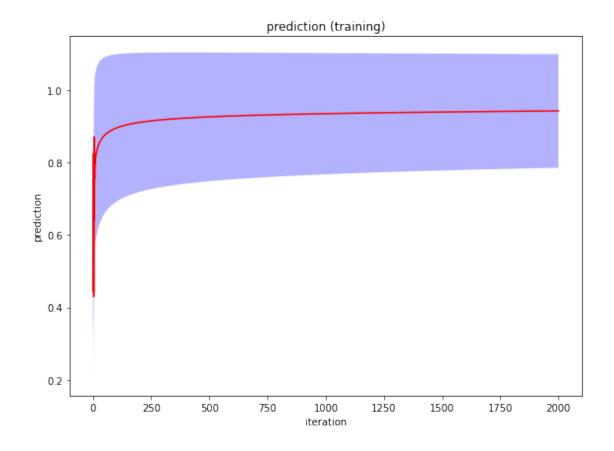
plot_curve_error(pred_train_mean_iteration[i], pred_train_std_iteration[i],

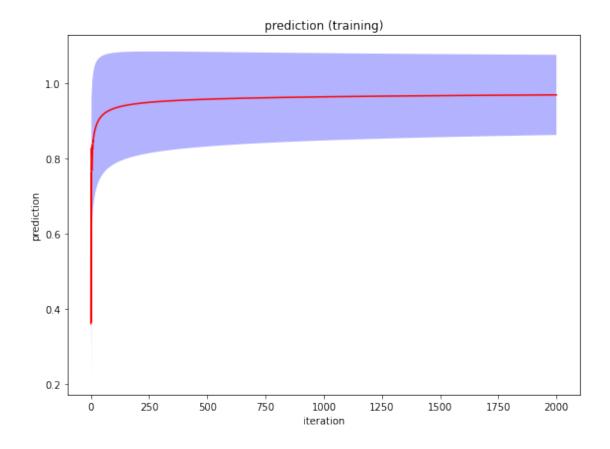
→'iteration', 'prediction', 'prediction (training)')
```

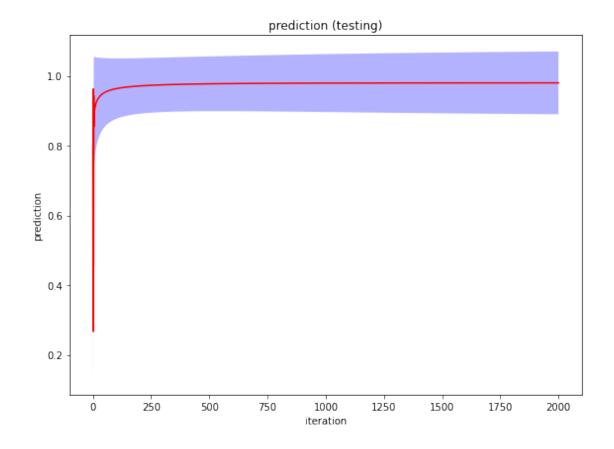


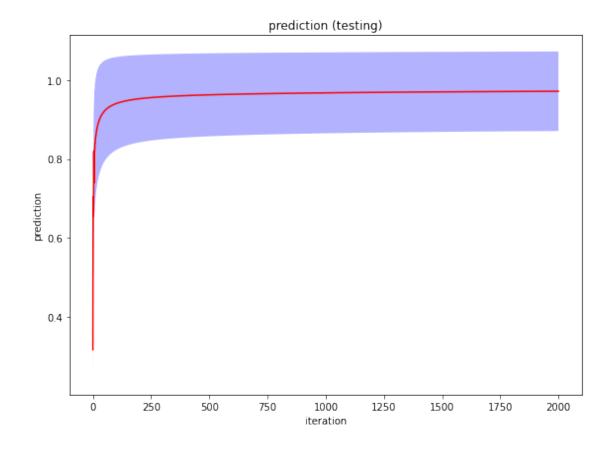


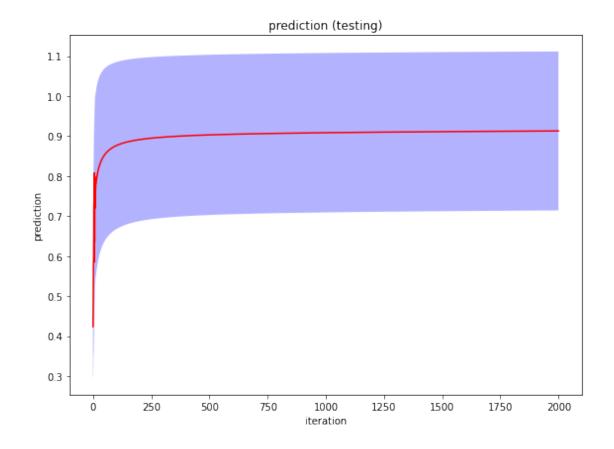


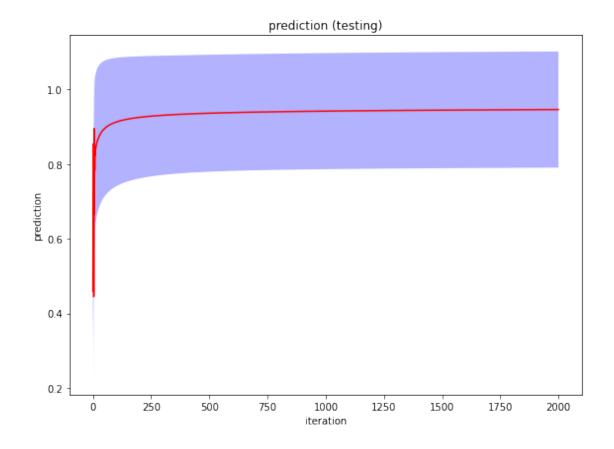


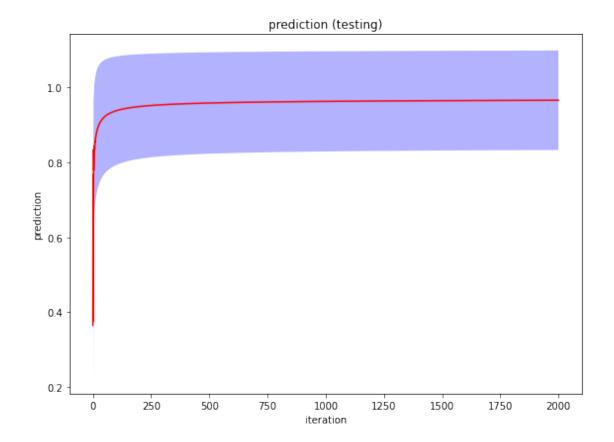












# 1.24 print values

```
[]: def print_curve(data, index):
    for i in range(len(index)):
        idx = index[i]
        val = data[idx]
        print('index = %4d, value = %12.10f' % (idx, val))
```

# 1.25 given iterations at which the values are presented

```
[]: index = np.array([0, 100, 200, 300, 400, 500, 600, 700, 800, 900])
```

# 1.26 training loss

```
[]: print_curve(loss_train_iteration, index)
index = 0, value = 0.8516388787
```

```
index = 100, value = 0.1339429389
    index = 200, value = 0.1157748007
    index = 300, value = 0.1069166127
    index = 400, value = 0.1011699953
    index = 500, value = 0.0969356204
    index = 600, value = 0.0935861772
    index = 700, value = 0.0908157813
    index = 800, value = 0.0884532877
    index = 900, value = 0.0863934761
    1.27 testing loss
[]: print_curve(loss_test_iteration, index)
    index =
               0, value = 0.8360542535
    index = 100, value = 0.1155831250
    index = 200, value = 0.1030645859
    index = 300, value = 0.0984429816
    index = 400, value = 0.0961438411
    index = 500, value = 0.0948397523
    index = 600, value = 0.0940481203
    index = 700, value = 0.0935513893
    index = 800, value = 0.0932376237
    index = 900, value = 0.0930438257
    1.28 training accuracy
[]: print_curve(accuracy_train_iteration, index)
               0, value = 0.8142000000
    index =
    index = 100, value = 0.9630000000
    index = 200, value = 0.9674000000
    index = 300, value = 0.9701000000
    index = 400, value = 0.9716000000
    index = 500, value = 0.9725000000
    index = 600, value = 0.9731000000
    index = 700, value = 0.9739000000
    index = 800, value = 0.9749000000
    index = 900, value = 0.9752000000
    1.29
         testing accuracy
```

[]: print\_curve(accuracy\_test\_iteration, index)

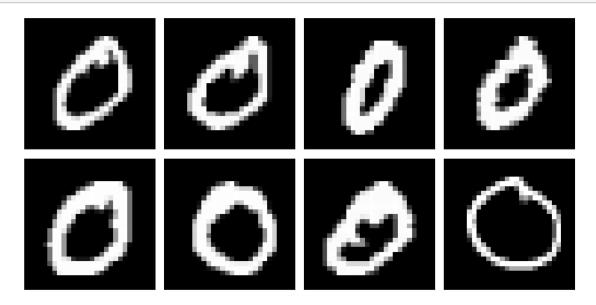
index = 100, value = 0.9708888889 index = 200, value = 0.9720000000 index = 300, value = 0.9726666667

index =

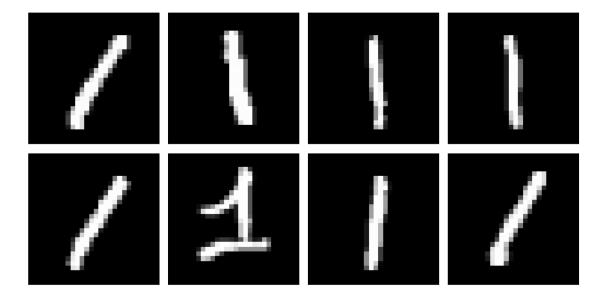
0, value = 0.8331111111

## 1.30 functions for presenting the results

## []: function\_results\_01(x\_train,2,4)



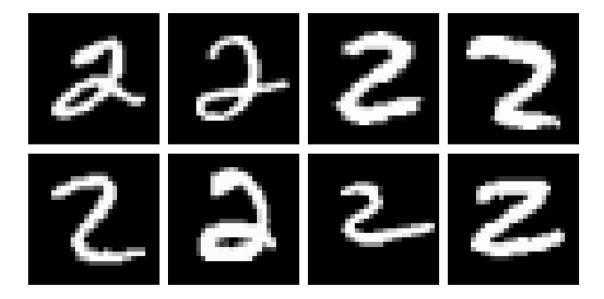
## []: function\_results\_02(x\_train,2,4)



```
[]: def function_results_03(data,nRow,nCol):
    fig, axes = plt.subplots(nRow, nCol, constrained_layout=True, figsize=(nCol_
    ** 3, nRow * 3))
    nPlot = nRow * nCol

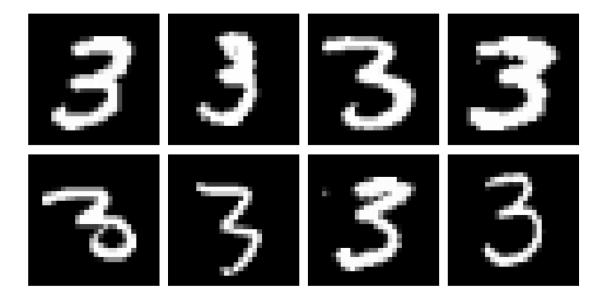
index_data = index_train[2][0][0:nPlot]
```

## []: function\_results\_03(x\_train,2,4)



```
axes[i, j].imshow(data[index], cmap='gray', vmin=0, vmax=1)
axes[i, j].xaxis.set_visible(False)
axes[i, j].yaxis.set_visible(False)
plt.show()
```

```
[]: function_results_04(x_train,2,4)
```



```
def function_results_05(data,nRow,nCol):
    fig, axes = plt.subplots(nRow, nCol, constrained_layout=True, figsize=(nCol_u
    ** 3, nRow * 3))
    nPlot = nRow * nCol

    index_data = index_train[4][0][0:nPlot]

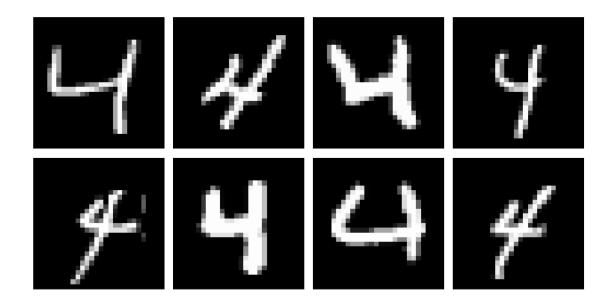
    for i in range(nRow):
        for j in range(nCol):

        k = i * nCol + j
        index = index_data[k]

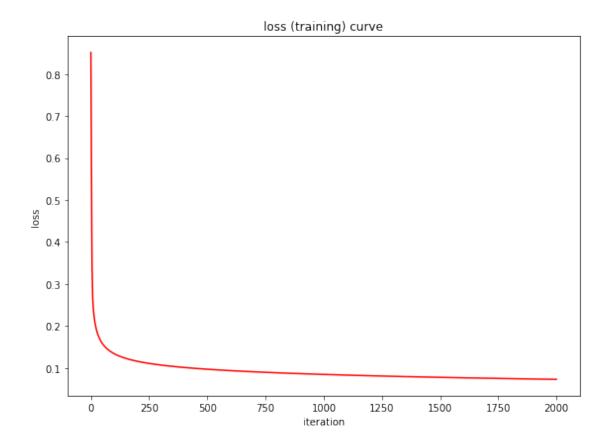
        axes[i, j].imshow(data[index], cmap='gray', vmin=0, vmax=1)
        axes[i, j].xaxis.set_visible(False)
        axes[i, j].yaxis.set_visible(False)

        plt.show()
```

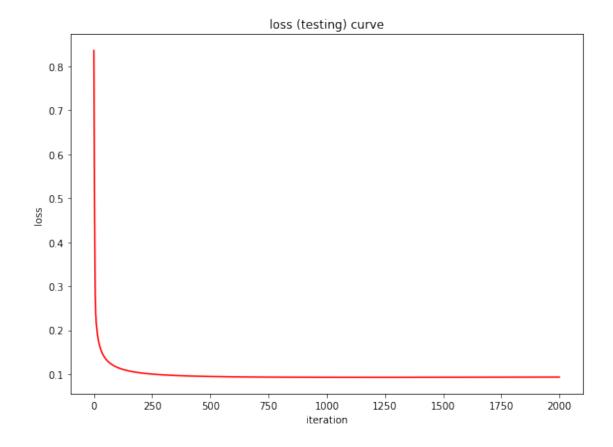
[]: function\_results\_05(x\_train,2,4)

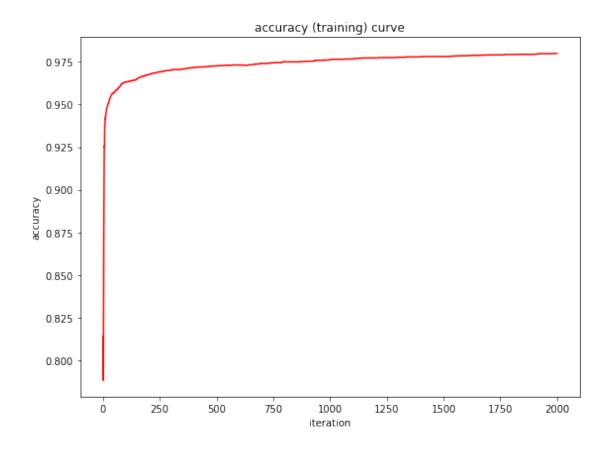


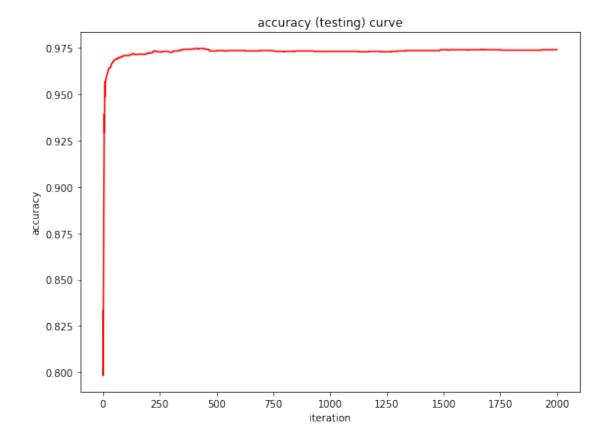
[]: function\_results\_06()



```
[]: def function_results_07():
    plot_curve(loss_test_iteration, 'iteration', 'loss', 'loss (testing) curve')
[]: function_results_07()
```







```
[]: def function_results_10(data):
    index = np.array([0, 100, 200, 300, 400, 500, 600, 700, 800, 900])
    for i in range(len(index)):

        idx = index[i]
        val = data[idx]

        print('index = %4d, value = %12.10f' % (idx, val))
```

## []: function\_results\_10(loss\_train\_iteration)

```
index = 0, value = 0.8516388787
index = 100, value = 0.1339429389
index = 200, value = 0.1157748007
index = 300, value = 0.1069166127
index = 400, value = 0.1011699953
index = 500, value = 0.0969356204
index = 600, value = 0.0935861772
index = 700, value = 0.0908157813
index = 800, value = 0.0884532877
```

```
index = 900, value = 0.0863934761
[]: def function_results_11(data):
         index = np.array([0, 100, 200, 300, 400, 500, 600, 700, 800, 900])
        for i in range(len(index)):
            idx = index[i]
            val = data[idx]
            print('index = %4d, value = %12.10f' % (idx, val))
[]: function_results_11(loss_test_iteration)
    index =
               0, value = 0.8360542535
    index = 100, value = 0.1155831250
    index = 200, value = 0.1030645859
    index = 300, value = 0.0984429816
    index = 400, value = 0.0961438411
    index = 500, value = 0.0948397523
    index = 600, value = 0.0940481203
    index = 700, value = 0.0935513893
    index = 800, value = 0.0932376237
    index = 900, value = 0.0930438257
[]: def function_results_12(data):
         index = np.array([0, 100, 200, 300, 400, 500, 600, 700, 800, 900])
        for i in range(len(index)):
            idx = index[i]
            val = data[idx]
            print('index = %4d, value = %12.10f' % (idx, val))
[]: function_results_12(accuracy_train_iteration)
               0, value = 0.8142000000
    index =
    index = 100, value = 0.9630000000
    index = 200, value = 0.9674000000
    index = 300, value = 0.9701000000
    index = 400, value = 0.9716000000
    index = 500, value = 0.9725000000
    index = 600, value = 0.9731000000
    index = 700, value = 0.9739000000
    index = 800, value = 0.9749000000
    index = 900, value = 0.9752000000
```

```
[]: def function_results_13(data):
    index = np.array([0, 100, 200, 300, 400, 500, 600, 700, 800, 900])
    for i in range(len(index)):

        idx = index[i]
        val = data[idx]

        print('index = %4d, value = %12.10f' % (idx, val))
```

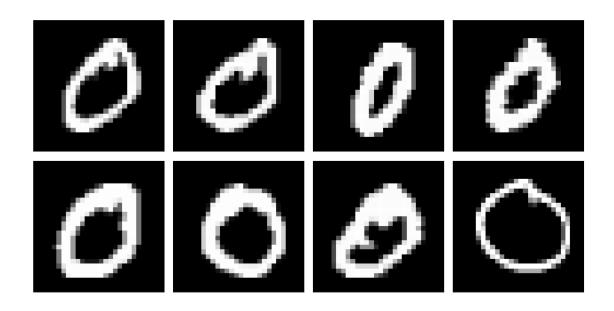
## []: function\_results\_13(accuracy\_test\_iteration)

```
index = 0, value = 0.8331111111
index = 100, value = 0.9708888889
index = 200, value = 0.9720000000
index = 300, value = 0.9726666667
index = 400, value = 0.9744444444
index = 500, value = 0.9733333333
index = 600, value = 0.973555556
index = 700, value = 0.973555556
index = 800, value = 0.9731111111
index = 900, value = 0.97333333333
```

## 2 RESULTS

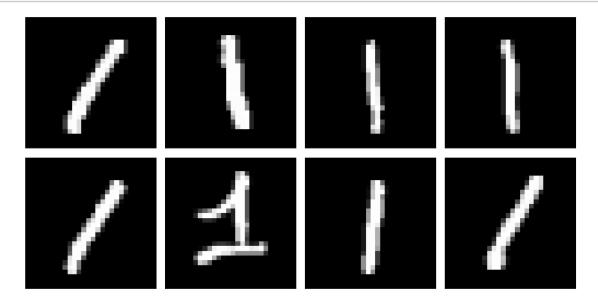
# 2.1 # 01. plot the input images for '0'

```
[]: function_results_01(x_train,2,4)
```



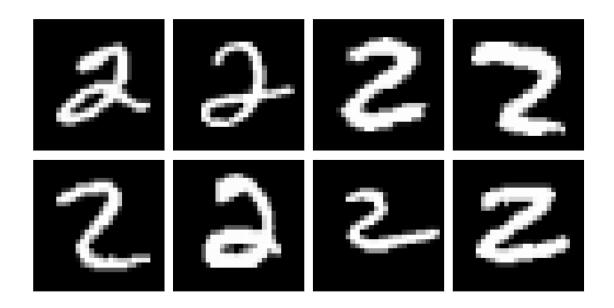
2.2 # 02. plot the input images for '1'

[]: function\_results\_02(x\_train,2,4)



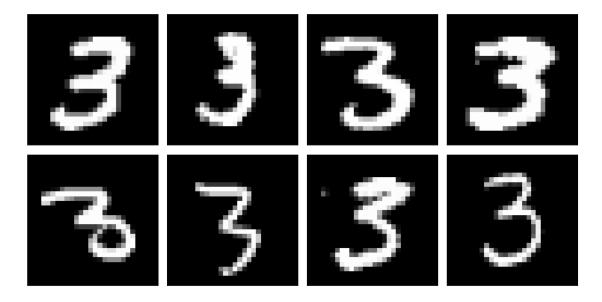
2.3 # 03. plot the input images for '2'

[]: function\_results\_03(x\_train,2,4)



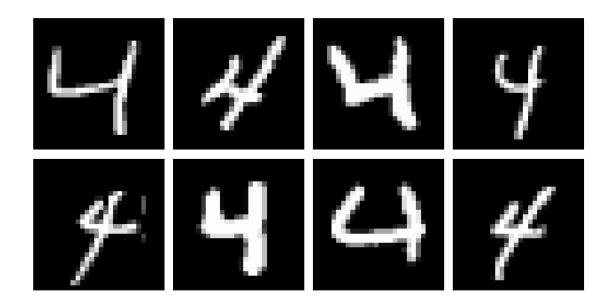
# 2.4 # 04. plot the input images for '3'

[]: function\_results\_04(x\_train,2,4)



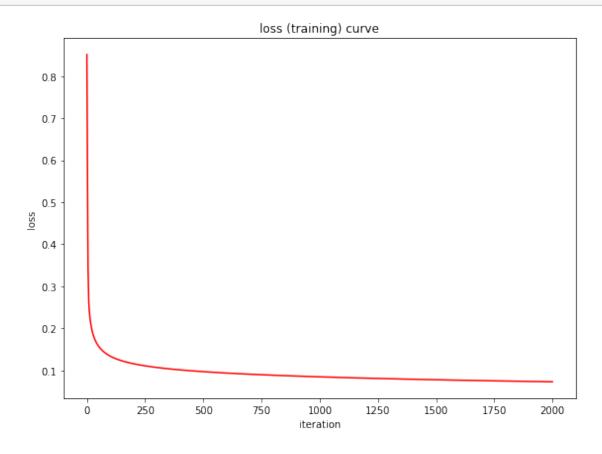
2.5 # 05. plot the input images for '4'

[]: function\_results\_05(x\_train,2,4)



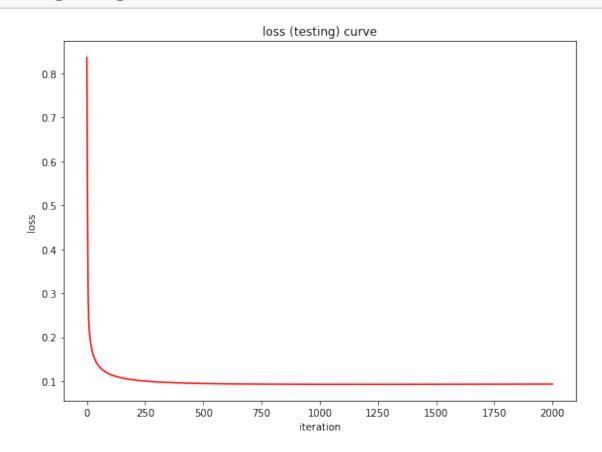
2.6 # 06. plot the training loss curve (x-axis: iteration, y-axis: loss)

# []: function\_results\_06()



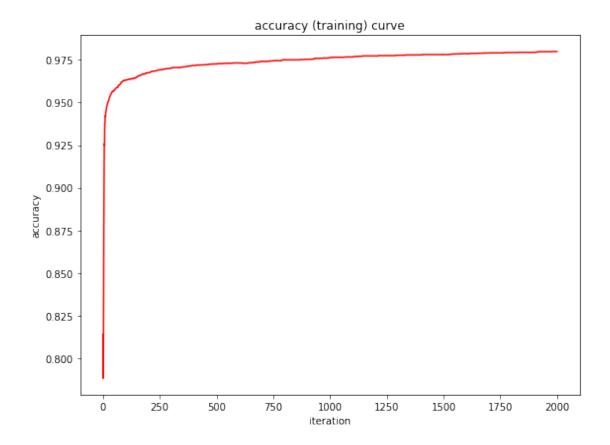
# 2.7 # 07. plot the testing loss curve (x-axis: iteration, y-axis: loss)

# []: function\_results\_07()



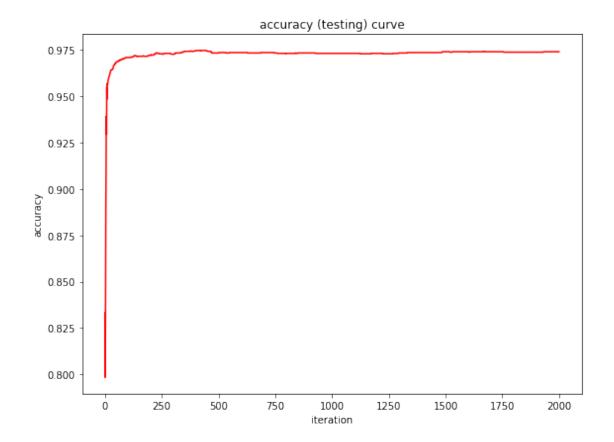
# 2.8 # 08. plot the training accuracy curve (x-axis: iteration, y-axis: accuracy)

[]: function\_results\_08()



2.9 # 09. plot the testing accuracy curve (x-axis: iteration, y-axis: accuracy)

[]: function\_results\_09()



# 2.10 # 10. print the training loss at iterations 0, 100, 200, 300, 400, 500, 600, 700, 800, 900

## []: function\_results\_10(loss\_train\_iteration)

```
index = 0, value = 0.8516388787

index = 100, value = 0.1339429389

index = 200, value = 0.1157748007

index = 300, value = 0.1069166127

index = 400, value = 0.1011699953

index = 500, value = 0.0969356204

index = 600, value = 0.0935861772

index = 700, value = 0.0908157813

index = 800, value = 0.0884532877

index = 900, value = 0.0863934761
```

2.11 # 11. print the testing loss at iterations 0, 100, 200, 300, 400, 500, 600, 700, 800, 900

```
[]: function_results_11(loss_test_iteration)
    index =
               0, value = 0.8360542535
    index =
            100, value = 0.1155831250
    index = 200, value = 0.1030645859
    index = 300, value = 0.0984429816
    index = 400, value = 0.0961438411
    index = 500, value = 0.0948397523
    index = 600, value = 0.0940481203
    index = 700, value = 0.0935513893
    index = 800, value = 0.0932376237
    index = 900, value = 0.0930438257
          # 12. print the training accuracy at iterations 0, 100, 200, 300, 400, 500,
          600, 700, 800, 900
[]: function_results_12(accuracy_train_iteration)
    index =
               0, value = 0.8142000000
    index = 100, value = 0.9630000000
    index = 200, value = 0.9674000000
    index = 300, value = 0.9701000000
    index = 400, value = 0.9716000000
    index = 500, value = 0.9725000000
    index = 600, value = 0.9731000000
    index = 700, value = 0.9739000000
    index = 800, value = 0.9749000000
    index = 900, value = 0.9752000000
          # 13. print the testing accuracy at iterations 0, 100, 200, 300, 400, 500,
          600, 700, 800, 900
[]: function_results_13(accuracy_test_iteration)
               0, value = 0.8331111111
    index =
    index = 100, value = 0.9708888889
    index = 200, value = 0.9720000000
    index = 300, value = 0.9726666667
    index = 400, value = 0.9744444444
    index = 500, value = 0.9733333333
    index = 600, value = 0.9735555556
    index = 700, value = 0.973555556
    index = 800, value = 0.9731111111
    index = 900, value = 0.97333333333
```

[]: