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CSCI 271

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Analysis of Spreadsheet:

Analysis of random array:

- $C(n)/n$: increase steadily i.e (240,964 to 5,033,418) showing $C(n)$ grows faster than n
- $C(n)/n^2$: Stabilizes around 0.25 (0.241 to 0.252), indicating $C(n) \approx (n^{2/4})$ confirming the same growth rate
- $C(n)/n^3$: Decreases (0.000241 to 0.000013), showing $C(n)$ grows slower than n^3
- $C(2n)/C(n)$: Approximately 4 (3.957 to 3.995), consistent with $O(n^2)$ as $((2n)^2 / n^2) = 4$

Analysis of ascending array:

- $C(n)/\sqrt{n}$: Increases (31.606 to 141.071), showing $C(n) \sim n$ grows faster than \sqrt{n}
- $C(n)/n$: Stabilizes at ~ 1 (0.999 to 0.9999), confirming $C(n) = n - 1$, same growth rate.
- $C(n)/n^2$: Decreases (0.001 to 0.000050), showing $C(n)$ grows slower than n^2
- $C(2n)/C(n)$: Exactly 2.000 or 2.001, consistent with $C(n) = n - 1$, as $(2n-1)/(n-1) \approx 2$

Analysis of descending array:

- $C(n)/n$: Increases (499.5 to 9,999.065), showing $C(n)$ grows faster than n
- $C(n)/n^2$: Stabilizes at ~ 0.5 (0.4995 to 0.4999), confirming $C(n) \approx (n^{2/2})$, same growth rate
- $C(n)/n^3$: Decreases (0.0005 to 0.000001), showing $C(n)$ grows slower than n^3
- $C(2n)/C(n)$: Exactly 4.000 or 4.001, consistent with $O(n^2)$

Hypothesis:

- Random order (average case): $C(n) \approx (n^2/4)$, so $O(n^2)$
- Ascending order (best case): $C(n) = n - 1$, so $O(n)$
- Descending order (worst case): $C(n) = ((n-1)n/2)$, so $O(n^2)$

Justification:

- **Random Order:**
 - $C(n)/n^2$ stabilizes around 0.25, matching the expected $(n^2/4)$.
 - $C(n)/n$ increases, confirming faster growth than n
 - $C(n)/n^3$ decreases, confirming slower growth than n^3
 - $C(2n)/C(n) \approx 4$ consistent with $O(n^2)$
 - The data aligns with the average-case for Insertion Sort
- **Ascending Order:**
 - $C(n)/n$ stabilizes at ~ 1 , matching $C(n) = n - 1$
 - $C(n)/\sqrt{n}$ increases, confirming faster growth than \sqrt{n}
 - $C(n)/n^2$ decreases, confirming slower growth than n^2
 - $C(2n)/C(n) \approx 2$ consistent with $O(n)$
 - The exact values i.e. (999 for $n=1000$) confirm the best-case formula
- **Descending Order:**
 - $C(n)/n^2$ stabilizes at ~ 0.5 , matching $(n^2/2)$
 - $C(n)/n$ increases, confirming faster growth than n
 - $C(n)/n^3$ decreases, confirming slower growth than n^3
 - $C(2n)/C(n) \approx 4$ consistent with $O(n^2)$
 - The values closely follow the worst-case formula $((n-1)n/2)$ i.e. (for $n=1000$, $((999 \cdot 1000)/2) = 499500$ exactly matching the output).

The $g(n)$ functions show faster, same, and slower growth, and the $C(2n)/C(n)$ ratios confirm the complexities.