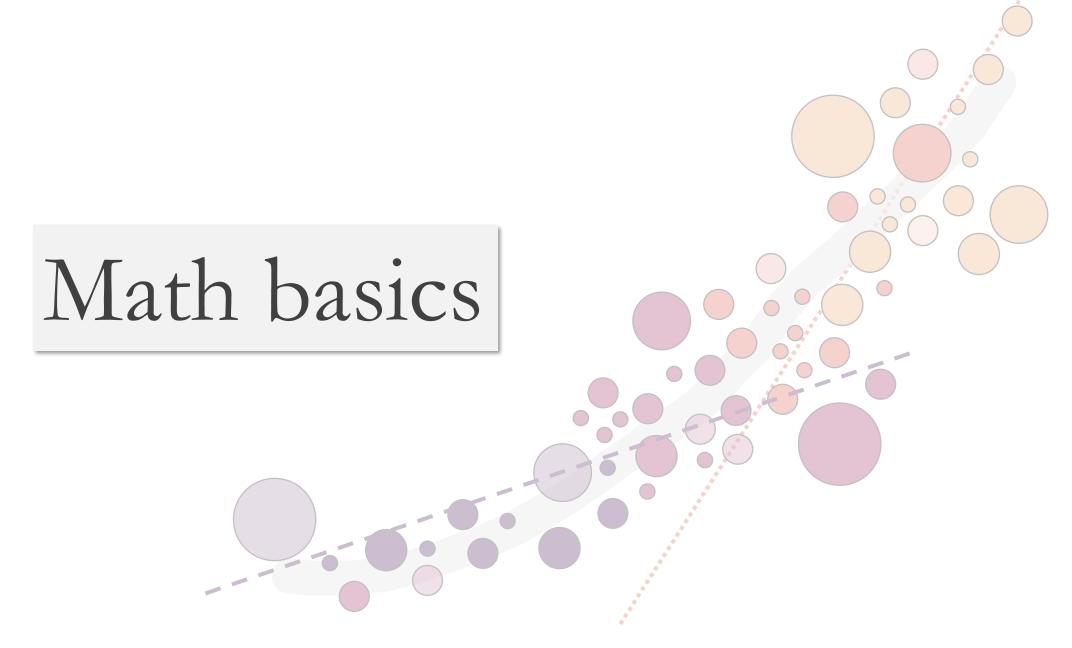
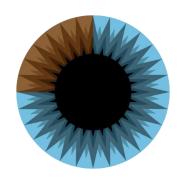


Spring 2024



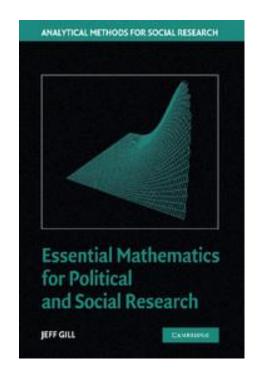
Resources

3blue1brown



The Bright Side of Mathematics





Textbook:

Gill, J. (2006). Essential Mathematics for Political and Social Research (Analytical Methods for Social Research). Cambridge: Cambridge University

Press. doi:10.1017/CBO9780511606656

No need to buy it! You have access to PDFs of the chapters via the Royal Library.

• This course is on YouTube!

https://www.youtube.com/playlist?list=PLvJwKACYy5 MTdnrzxx 1sN389dS9OB3S



Powers

Zero property

$$x^0 = 1$$

One property

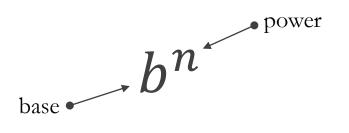
$$x^1 = x$$

Power notation

$$power(x, a) = x^a$$

Fraction Property

$$\left(\frac{x}{y}\right)^{a} = \left(\frac{x^{a}}{y^{a}}\right) = x^{a}y^{-a}$$



When *n* is a positive integer, exponentiation corresponds to repeated multiplication of the base.

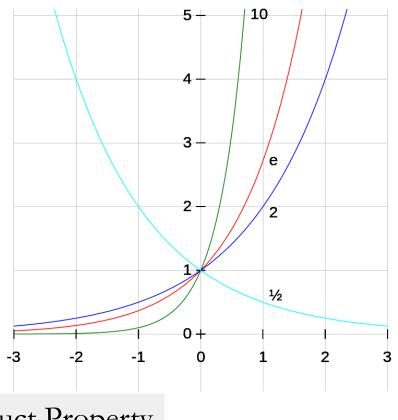
$$b^n = \underbrace{b \times b \times \cdots \times b \times b}_{\text{n times}}$$

Nested Exponents

$$(x^a)^b = x^{ab}$$

Distributive Property

$$(xy)^a = x^a y^a$$



Product Property

$$x^{a} * x^{b} = x^{a+b}$$

Ratio Property

$$x^{\frac{a}{b}} = (x^{\frac{a}{b}})^{\frac{1}{b}} = (x^{\frac{1}{b}})^{\frac{a}{b}} = \sqrt[b]{x^{\frac{a}{b}}}$$



Logarithms

The logarithm of a number x to the base b is the exponent to which b must be raised to produce x.

$$y = \log_b x \leftrightarrow x = b^y$$

Exponentiation

$$\log_{b}(b^{x}) = b^{\log_{b}(x)} = x$$

Zero/one

$$\log_b(1) = 0$$

Division

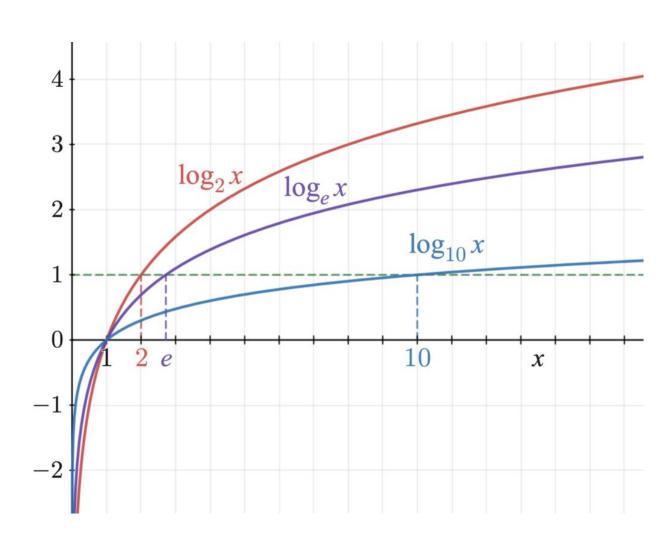
$$\log\left(\frac{x}{y}\right) = \log(x) - \log(y)$$

Multiplication

$$\log(x * y) = \log(x) + \log(y)$$

Changing base

$$\log_a x = \frac{\log_b x}{\log_b a}$$





Find the value of y

a.
$$\log_8 \frac{1}{64} = y$$
 b. $\log_6 36 = y$ c. $\log_7 1 = y$ d. $\log_4 \frac{1}{4} = y$

b.
$$\log_6 36 = y$$

$$\mathbf{c.} \log_7 1 = y$$

d.
$$\log_4 \frac{1}{4} = y$$

Write the following expressions in terms of logs of x, y and z.

e.
$$\log(xy)^{\frac{1}{3}}$$

f.
$$\log x \sqrt{z}$$

g.
$$\log \frac{x^3y^2}{z}$$

g.
$$\log \frac{x^3y^2}{z}$$
 h. $\log \frac{\sqrt{x} \cdot \sqrt[3]{y^2}}{z^4}$

True or False?

i.
$$\frac{\log a}{\log b} = \log(a - b)$$

i.
$$\frac{\log a}{\log b} = \log(a - b)$$
 j. $\log(a - b) = \log a - \log b$ k. $-\ln\left(\frac{1}{x}\right) = \ln x$

$$\mathbf{k.} - \ln\left(\frac{1}{x}\right) = \ln x$$

