



EECS 390 – Lecture 8

Higher-Order Functions

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Agenda

- Function Objects
- Functions as Parameters
- Nested Functions

Function Objects and State

- A **function object** (also called a **functor**) is an object that isn't a function but provides the same interface
- Allowing the function-call operator to be overloaded enables function objects to be defined
- Function objects can have state that is associated with an instance of the functor
 - State shared among all invocations of the same instance
 - Different than top-level functions, which only have state that is associated with a single invocation or with all invocations of the function

Function Objects in C++

- Functors can be written by defining a class that overloads the `operator()` member function

```
class Counter {  
public:  
    Counter : count(0) {}  
    int operator()() {  
        return count++;  
    }  
private:  
    int count;  
};
```

Can have
parameters, just
like functions

```
Counter counter1, counter2;  
cout << counter1() << endl; // prints 0  
cout << counter1() << endl; // prints 1  
cout << counter1() << endl; // prints 2  
cout << counter2() << endl; // prints 0  
cout << counter2() << endl; // prints 1  
cout << counter1() << endl; // prints 3
```

Function Objects in Python

- Functors overload the `__call__` special method

```
class Counter:
    def __init__(self):
        self.count = 0
    def __call__(self):
        self.count += 1
        return self.count - 1
```

More parameters
can go here

```
counter1 = Counter()
counter2 = Counter()
print(counter1()) # prints 0
print(counter1()) # prints 1
print(counter1()) # prints 2
print(counter2()) # prints 0
print(counter2()) # prints 1
print(counter1()) # prints 3
```

Function Pointers

- C and C++ allow top-level functions to be passed by pointer

```
void apply(int *A, size_t size, int (*f)(int)) {  
    for (; size > 0; --size, ++A)  
        *A = f(*A);  
}
```

```
int add_one(int x) {  
    return x + 1;  
}
```

```
int main() {  
    int A[5] = { 1, 2, 3, 4, 5 };  
    apply(A, 5, add_one);  
    cout << A[0] << ", " << A[1] << ", " << A[2]  
        << ", " << A[3] << ", " << A[4] << endl;  
}
```

Automatically
converted to
function pointer

Environment of Use

- ▶ A function passed as a parameter has three environments that can be associated with it
 - ▶ The environment where it was defined
 - ▶ The environment where it was referenced
 - ▶ The environment where it was called
- ▶ Scope policy determines which names are visible in the function
 - ▶ Static/lexical scope: names visible at the definition point
 - ▶ Dynamic scope: names visible at the point of use
- ▶ In dynamic scope, point of use can be where a function is referenced or where it is called

Binding Policy

- **Shallow binding:** non-local environment is environment from where a function is called
- **Deep binding:** non-local environment is environment from where a function is referenced

```
int foo(int (*bar)()) {  
    int x = 3;  
    return bar();  
}
```

Non-local
environment in
shallow binding

```
int baz() {  
    return x;  
}
```

Non-local
environment in
deep binding

```
int main() {  
    int x = 4;  
    print(foo(baz));  
}
```


Evaluating Function Calls

- Determine non-local environment
 - Static scope: active environment when the function is defined
 - Dynamic scope with deep binding: active environment when the function is named
 - Dynamic scope with shallow binding: active environment when the function is called
- Create new activation record and pass parameters
 - Call by value: obtain r-value of argument and copy it into the new activation record
 - Call by reference: obtain l-value of argument and bind the parameter to the corresponding object
 - Call by result: obtain l-value of argument, create uninitialized storage in new activation record
 - Call by name: create thunk from argument expression and current environment

Evaluating Function Calls

- ▶ Pause caller, execute body of callee in environment consisting of new activation record and the function's non-local environment
- ▶ When callee returns:
 - ▶ Store return value (usually in activation record of caller)
 - ▶ Copy r-values of call-by-result parameters into objects associated with argument l-values
 - ▶ Destroy activation record of callee (if using stack-based memory management)
 - ▶ Resume execution of caller
- ▶ The evaluation result of the function call is the return value of the callee

Nested Functions and Closures

- The ability to create a function from within another function is a key feature of functional programming
- Static scope requires that the newly created function have access to its definition environment
- A **closure** is the combination of a function and its enclosing environment
- Variables from the enclosing environment that are used in the function are **captured** by the closure

Nested Functions and State

- A closure encompasses state that can be accessed by the newly created function

```
def make_greater_than(threshold):  
    def greater_than(x):  
        return x > threshold  
    return greater_than
```

threshold
captured from
non-local
environment



```
>>> gt3 = make_greater_than(3)  
>>> gt30 = make_greater_than(30)  
>>> gt3(2)  
False  
>>> gt3(20)  
True  
>>> gt30(20), gt30(200)  
(False, True)
```

Modifying Non-Local State

- Languages may allow non-local variables to be modified

```
def make_account(balance):  
    def deposit(amount):  
        nonlocal balance  
        balance += amount  
        return balance  
    def withdraw(amount):  
        nonlocal balance  
        if 0 <= amount <= balance:  
            balance -= amount  
            return amount  
        else:  
            return 0  
    return deposit, withdraw
```

```
>>> deposit, withdraw = \  
    make_account(100)  
>>> withdraw(10)  
10  
>>> deposit(0)  
90  
>>> withdraw(20)  
20  
>>> deposit(0)  
70  
>>> deposit(10)  
80  
>>> withdraw(100)  
0  
>>> deposit(0)  
80
```

Decorators

- A common pattern in Python is to transform a function or class by applying a higher-order function to it, called a **decorator**
- Standard syntax for decorating functions:

```
@<decorator>  
def <name>(<parameters>):  
    <body>
```

- Mostly equivalent to:

```
def <name>(<parameters>):  
    <body>
```

```
<name> = <decorator>(<name>)
```

Trace Example

- Example: decorator that traces function calls

```
def trace(fn):  
    def tracer(*args):  
        arg_str = ', '.join(repr(arg)  
                             for arg in args)  
        print(f'{fn.__name__}({arg_str})')  
        return fn(*args)  
    return tracer
```

**“Representation”
string**

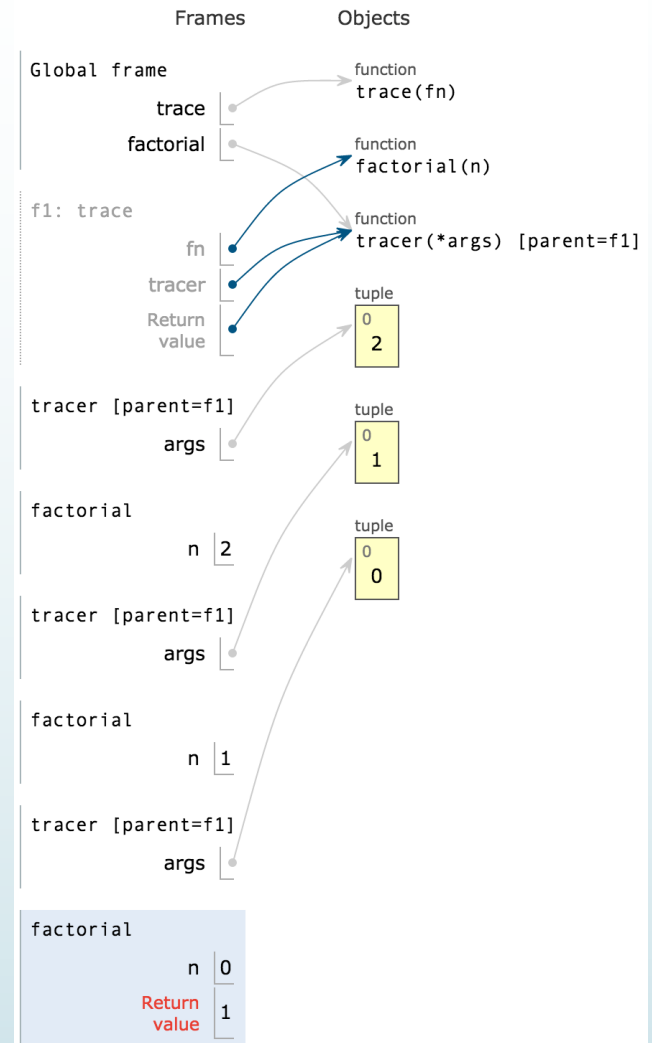
```
@trace  
def factorial(n):  
    if n == 0:  
        return 1  
    return n * factorial(n - 1)
```

```
>>> factorial(5)  
factorial(5)  
factorial(4)  
factorial(3)  
factorial(2)  
factorial(1)  
factorial(0)  
120
```

Mutual Recursion

- A decorated recursive function results in **mutual recursion** where multiple functions make recursive calls indirectly through each other

```
>>> factorial(2)
factorial(2)
factorial(1)
factorial(0)
2
```



Partial Application

- Specify some arguments to a function, then specify remaining arguments later
- If function takes n arguments and k are supplied, results in function that takes $n - k$ arguments

```
def partial(func, *args):  
    def newfunc(*nargs):  
        return func(*args, *nargs)  
    return newfunc
```

```
>>> power_of_two = partial(pow, 2)  
>>> power_of_two(3)  
8  
>>> power_of_two(7)  
128
```

Currying

- Transforms a function that takes n arguments into a series of n functions that each take in one argument
- In some languages, all functions are curried

```
def curry2(func):  
    def curriedA(a):  
        def curriedB(b):  
            return func(a, b)  
        return curriedB  
    return curriedA
```

```
>>> curried_pow = curry2(pow)  
>>> curried_pow(2)(3)  
8
```

Uncurrying

- We can also do the reverse transformation

```
def uncurry2(func):  
    def uncurried(a, b):  
        return func(a)(b)  
    return uncurried
```

```
>>> uncurried_pow = uncurry2(curried_pow)  
>>> uncurried_pow(2, 3)  
8
```