

In [1]:

```
import tensorflow as tf
```

In [2]:

```
# Load Data
```

```
(x_train, y_train), (x_test, y_test) = tf.keras.datasets.fashion_mnist.load_data()
```

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/train-labels-idx1-ubyte.gz>

32768/29515 [=====] - 0s 2us/step

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/train-images-idx3-ubyte.gz>

26427392/26421880 [=====] - 4s 0us/step

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/t10k-labels-idx1-ubyte.gz>

8192/5148 [=====] - 0s 0us/step

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/t10k-images-idx3-ubyte.gz>

4423680/4422102 [=====] - 1s 0us/step

## Baseline Model

In [3]:

```
# Baseline model definition
```

```
model = tf.keras.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    tf.keras.layers.Dense(16, activation='relu'),
    tf.keras.layers.Dense(16, activation='relu'),
    tf.keras.layers.Dense(10, activation='softmax')
])
```

In [4]:

```
# Baseline model compilation
```

```
# Learning rate 0.001
```

```
optimizer = tf.keras.optimizers.Adam(learning_rate=0.001)
```

```
model.compile(optimizer=optimizer,
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy']
              )
```

In [5]:

```
# Baseline model fitting
```

```
history = model.fit(x_train, y_train,
                    batch_size=128,
                    epochs=100,
                    validation_data=(x_test, y_test),
                    verbose=2
                    )
```

Epoch 1/100

469/469 - 1s - loss: 3.0479 - sparse\_categorical\_accuracy: 0.2256 - val\_loss: 1.7689 - val\_sparse\_categorical\_accuracy: 0.3199

Epoch 2/100

469/469 - 1s - loss: 1.6926 - sparse\_categorical\_accuracy: 0.3397 - val\_loss: 1.6341 - val\_sparse\_categorical\_accuracy: 0.3517

Epoch 3/100

469/469 - 1s - loss: 1.5966 - sparse\_categorical\_accuracy: 0.3520 - val\_loss: 1.5751 - val\_sparse\_categorical\_accuracy: 0.3547

Epoch 4/100

469/469 - 1s - loss: 1.5438 - sparse\_categorical\_accuracy: 0.3603 - val\_loss: 1.5355 - val\_sparse\_categorical\_accuracy: 0.3628

Epoch 5/100

469/469 - 1s - loss: 1.5112 - sparse\_categorical\_accuracy: 0.3658 - val\_loss: 1.4985 - val\_sparse\_categorical\_accuracy: 0.3681

Epoch 6/100

469/469 - 1s - loss: 1.4855 - sparse\_categorical\_accuracy: 0.3698 - val\_loss: 1.4886 - val\_sparse\_categorical\_accuracy: 0.3711

Epoch 7/100

469/469 - 1s - loss: 1.4772 - sparse\_categorical\_accuracy: 0.3702 - val\_loss: 1.4886 - val\_sparse\_categorical\_accuracy: 0.3741

Epoch 8/100

469/469 - 1s - loss: 1.3825 - sparse\_categorical\_accuracy: 0.4257 - val\_loss: 1.3746 - val\_sparse\_categorical\_accuracy: 0.3741

tegorical accuracy: 0.4438  
Epoch 9/100  
469/469 - 1s - loss: 1.2631 - sparse\_categorical\_accuracy: 0.4649 - val\_loss: 1.2530 - val\_sparse\_categorical\_accuracy: 0.4648  
Epoch 10/100  
469/469 - 1s - loss: 1.0655 - sparse\_categorical\_accuracy: 0.5362 - val\_loss: 0.9885 - val\_sparse\_categorical\_accuracy: 0.5598  
Epoch 11/100  
469/469 - 1s - loss: 0.9395 - sparse\_categorical\_accuracy: 0.5800 - val\_loss: 0.9447 - val\_sparse\_categorical\_accuracy: 0.5997  
Epoch 12/100  
469/469 - 1s - loss: 0.8987 - sparse\_categorical\_accuracy: 0.6113 - val\_loss: 0.8801 - val\_sparse\_categorical\_accuracy: 0.6272  
Epoch 13/100  
469/469 - 1s - loss: 0.8691 - sparse\_categorical\_accuracy: 0.6267 - val\_loss: 0.8794 - val\_sparse\_categorical\_accuracy: 0.6302  
Epoch 14/100  
469/469 - 1s - loss: 0.8504 - sparse\_categorical\_accuracy: 0.6366 - val\_loss: 0.8899 - val\_sparse\_categorical\_accuracy: 0.6214  
Epoch 15/100  
469/469 - 1s - loss: 0.8474 - sparse\_categorical\_accuracy: 0.6360 - val\_loss: 0.9469 - val\_sparse\_categorical\_accuracy: 0.6444  
Epoch 16/100  
469/469 - 1s - loss: 0.8313 - sparse\_categorical\_accuracy: 0.6437 - val\_loss: 0.8365 - val\_sparse\_categorical\_accuracy: 0.6411  
Epoch 17/100  
469/469 - 1s - loss: 0.8322 - sparse\_categorical\_accuracy: 0.6409 - val\_loss: 0.8536 - val\_sparse\_categorical\_accuracy: 0.6352  
Epoch 18/100  
469/469 - 1s - loss: 0.8387 - sparse\_categorical\_accuracy: 0.6388 - val\_loss: 0.8568 - val\_sparse\_categorical\_accuracy: 0.6413  
Epoch 19/100  
469/469 - 1s - loss: 0.8205 - sparse\_categorical\_accuracy: 0.6449 - val\_loss: 0.8600 - val\_sparse\_categorical\_accuracy: 0.6336  
Epoch 20/100  
469/469 - 1s - loss: 0.8180 - sparse\_categorical\_accuracy: 0.6456 - val\_loss: 0.8512 - val\_sparse\_categorical\_accuracy: 0.6437  
Epoch 21/100  
469/469 - 1s - loss: 0.8114 - sparse\_categorical\_accuracy: 0.6475 - val\_loss: 0.8448 - val\_sparse\_categorical\_accuracy: 0.6347  
Epoch 22/100  
469/469 - 1s - loss: 0.8200 - sparse\_categorical\_accuracy: 0.6447 - val\_loss: 0.8495 - val\_sparse\_categorical\_accuracy: 0.6426  
Epoch 23/100  
469/469 - 1s - loss: 0.8012 - sparse\_categorical\_accuracy: 0.6518 - val\_loss: 0.8691 - val\_sparse\_categorical\_accuracy: 0.6441  
Epoch 24/100  
469/469 - 1s - loss: 0.8079 - sparse\_categorical\_accuracy: 0.6490 - val\_loss: 0.8343 - val\_sparse\_categorical\_accuracy: 0.6404  
Epoch 25/100  
469/469 - 1s - loss: 0.8032 - sparse\_categorical\_accuracy: 0.6493 - val\_loss: 0.9195 - val\_sparse\_categorical\_accuracy: 0.6418  
Epoch 26/100  
469/469 - 1s - loss: 0.8014 - sparse\_categorical\_accuracy: 0.6494 - val\_loss: 0.8515 - val\_sparse\_categorical\_accuracy: 0.6372  
Epoch 27/100  
469/469 - 1s - loss: 0.8083 - sparse\_categorical\_accuracy: 0.6513 - val\_loss: 0.9022 - val\_sparse\_categorical\_accuracy: 0.6256  
Epoch 28/100  
469/469 - 1s - loss: 0.8074 - sparse\_categorical\_accuracy: 0.6510 - val\_loss: 0.8313 - val\_sparse\_categorical\_accuracy: 0.6440  
Epoch 29/100  
469/469 - 1s - loss: 0.8006 - sparse\_categorical\_accuracy: 0.6571 - val\_loss: 0.8351 - val\_sparse\_categorical\_accuracy: 0.6422  
Epoch 30/100  
469/469 - 1s - loss: 0.7819 - sparse\_categorical\_accuracy: 0.6578 - val\_loss: 0.8283 - val\_sparse\_categorical\_accuracy: 0.6451  
Epoch 31/100  
469/469 - 1s - loss: 0.7931 - sparse\_categorical\_accuracy: 0.6524 - val\_loss: 0.8537 - val\_sparse\_categorical\_accuracy: 0.6435  
Epoch 32/100  
469/469 - 1s - loss: 0.7851 - sparse\_categorical\_accuracy: 0.6527 - val\_loss: 0.8464 - val\_sparse\_categorical\_accuracy: 0.6370  
Epoch 33/100  
469/469 - 1s - loss: 0.7852 - sparse\_categorical\_accuracy: 0.6569 - val\_loss: 0.8797 - val\_sparse\_categorical\_accuracy: 0.6449  
Epoch 34/100  
469/469 - 1s - loss: 0.7794 - sparse\_categorical\_accuracy: 0.6662 - val\_loss: 0.8134 - val\_sparse\_categorical\_accuracy: 0.6693  
Epoch 35/100  
469/469 - 1s - loss: 0.7482 - sparse\_categorical\_accuracy: 0.7000 - val\_loss: 0.7743 - val\_sparse\_categorical\_accuracy: 0.7028  
Epoch 36/100

469/469 - 1s - loss: 0.7252 - sparse\_categorical\_accuracy: 0.7116 - val\_loss: 0.7558 - val\_sparse\_categorical\_accuracy: 0.7075  
Epoch 37/100  
469/469 - 1s - loss: 0.7022 - sparse\_categorical\_accuracy: 0.7196 - val\_loss: 0.7443 - val\_sparse\_categorical\_accuracy: 0.7161  
Epoch 38/100  
469/469 - 1s - loss: 0.6948 - sparse\_categorical\_accuracy: 0.7288 - val\_loss: 0.7105 - val\_sparse\_categorical\_accuracy: 0.7406  
Epoch 39/100  
469/469 - 1s - loss: 0.6682 - sparse\_categorical\_accuracy: 0.7437 - val\_loss: 0.7160 - val\_sparse\_categorical\_accuracy: 0.7451  
Epoch 40/100  
469/469 - 1s - loss: 0.6535 - sparse\_categorical\_accuracy: 0.7515 - val\_loss: 0.6914 - val\_sparse\_categorical\_accuracy: 0.7511  
Epoch 41/100  
469/469 - 1s - loss: 0.6460 - sparse\_categorical\_accuracy: 0.7576 - val\_loss: 0.6687 - val\_sparse\_categorical\_accuracy: 0.7598  
Epoch 42/100  
469/469 - 1s - loss: 0.6396 - sparse\_categorical\_accuracy: 0.7591 - val\_loss: 0.6826 - val\_sparse\_categorical\_accuracy: 0.7499  
Epoch 43/100  
469/469 - 1s - loss: 0.6255 - sparse\_categorical\_accuracy: 0.7655 - val\_loss: 0.6818 - val\_sparse\_categorical\_accuracy: 0.7394  
Epoch 44/100  
469/469 - 1s - loss: 0.6217 - sparse\_categorical\_accuracy: 0.7671 - val\_loss: 0.6897 - val\_sparse\_categorical\_accuracy: 0.7522  
Epoch 45/100  
469/469 - 1s - loss: 0.6184 - sparse\_categorical\_accuracy: 0.7687 - val\_loss: 0.6470 - val\_sparse\_categorical\_accuracy: 0.7626  
Epoch 46/100  
469/469 - 1s - loss: 0.6182 - sparse\_categorical\_accuracy: 0.7700 - val\_loss: 0.6450 - val\_sparse\_categorical\_accuracy: 0.7645  
Epoch 47/100  
469/469 - 1s - loss: 0.6124 - sparse\_categorical\_accuracy: 0.7717 - val\_loss: 0.6586 - val\_sparse\_categorical\_accuracy: 0.7626  
Epoch 48/100  
469/469 - 1s - loss: 0.5982 - sparse\_categorical\_accuracy: 0.7751 - val\_loss: 0.6512 - val\_sparse\_categorical\_accuracy: 0.7589  
Epoch 49/100  
469/469 - 1s - loss: 0.6012 - sparse\_categorical\_accuracy: 0.7727 - val\_loss: 0.6429 - val\_sparse\_categorical\_accuracy: 0.7688  
Epoch 50/100  
469/469 - 1s - loss: 0.5960 - sparse\_categorical\_accuracy: 0.7764 - val\_loss: 0.6621 - val\_sparse\_categorical\_accuracy: 0.7645  
Epoch 51/100  
469/469 - 1s - loss: 0.6081 - sparse\_categorical\_accuracy: 0.7740 - val\_loss: 0.6381 - val\_sparse\_categorical\_accuracy: 0.7695  
Epoch 52/100  
469/469 - 1s - loss: 0.5930 - sparse\_categorical\_accuracy: 0.7778 - val\_loss: 0.6474 - val\_sparse\_categorical\_accuracy: 0.7662  
Epoch 53/100  
469/469 - 1s - loss: 0.5908 - sparse\_categorical\_accuracy: 0.7796 - val\_loss: 0.6691 - val\_sparse\_categorical\_accuracy: 0.7647  
Epoch 54/100  
469/469 - 1s - loss: 0.5977 - sparse\_categorical\_accuracy: 0.7768 - val\_loss: 0.6440 - val\_sparse\_categorical\_accuracy: 0.7620  
Epoch 55/100  
469/469 - 1s - loss: 0.5826 - sparse\_categorical\_accuracy: 0.7812 - val\_loss: 0.6279 - val\_sparse\_categorical\_accuracy: 0.7738  
Epoch 56/100  
469/469 - 1s - loss: 0.5795 - sparse\_categorical\_accuracy: 0.7841 - val\_loss: 0.6341 - val\_sparse\_categorical\_accuracy: 0.7778  
Epoch 57/100  
469/469 - 1s - loss: 0.5819 - sparse\_categorical\_accuracy: 0.7835 - val\_loss: 0.6764 - val\_sparse\_categorical\_accuracy: 0.7613  
Epoch 58/100  
469/469 - 1s - loss: 0.5771 - sparse\_categorical\_accuracy: 0.7831 - val\_loss: 0.6409 - val\_sparse\_categorical\_accuracy: 0.7711  
Epoch 59/100  
469/469 - 1s - loss: 0.5719 - sparse\_categorical\_accuracy: 0.7865 - val\_loss: 0.6665 - val\_sparse\_categorical\_accuracy: 0.7587  
Epoch 60/100  
469/469 - 1s - loss: 0.5876 - sparse\_categorical\_accuracy: 0.7800 - val\_loss: 0.6440 - val\_sparse\_categorical\_accuracy: 0.7690  
Epoch 61/100  
469/469 - 1s - loss: 0.5770 - sparse\_categorical\_accuracy: 0.7851 - val\_loss: 0.6206 - val\_sparse\_categorical\_accuracy: 0.7821  
Epoch 62/100  
469/469 - 1s - loss: 0.5775 - sparse\_categorical\_accuracy: 0.7839 - val\_loss: 0.6650 - val\_sparse\_categorical\_accuracy: 0.7516  
Epoch 63/100  
469/469 - 1s - loss: 0.5756 - sparse\_categorical\_accuracy: 0.7875 - val\_loss: 0.6278 - val\_sparse\_categorical\_accuracy: 0.7754

Epoch 64/100  
469/469 - 1s - loss: 0.5726 - sparse\_categorical\_accuracy: 0.7849 - val\_loss: 0.6569 - val\_sparse\_categorical\_accuracy: 0.7673  
Epoch 65/100  
469/469 - 1s - loss: 0.5702 - sparse\_categorical\_accuracy: 0.7879 - val\_loss: 0.6286 - val\_sparse\_categorical\_accuracy: 0.7710  
Epoch 66/100  
469/469 - 1s - loss: 0.5681 - sparse\_categorical\_accuracy: 0.7873 - val\_loss: 0.6338 - val\_sparse\_categorical\_accuracy: 0.7755  
Epoch 67/100  
469/469 - 1s - loss: 0.5617 - sparse\_categorical\_accuracy: 0.7887 - val\_loss: 0.6126 - val\_sparse\_categorical\_accuracy: 0.7843  
Epoch 68/100  
469/469 - 1s - loss: 0.5612 - sparse\_categorical\_accuracy: 0.7891 - val\_loss: 0.7142 - val\_sparse\_categorical\_accuracy: 0.7451  
Epoch 69/100  
469/469 - 1s - loss: 0.5611 - sparse\_categorical\_accuracy: 0.7892 - val\_loss: 0.6316 - val\_sparse\_categorical\_accuracy: 0.7744  
Epoch 70/100  
469/469 - 1s - loss: 0.5557 - sparse\_categorical\_accuracy: 0.7916 - val\_loss: 0.6313 - val\_sparse\_categorical\_accuracy: 0.7744  
Epoch 71/100  
469/469 - 1s - loss: 0.5595 - sparse\_categorical\_accuracy: 0.7904 - val\_loss: 0.6879 - val\_sparse\_categorical\_accuracy: 0.7452  
Epoch 72/100  
469/469 - 1s - loss: 0.5630 - sparse\_categorical\_accuracy: 0.7885 - val\_loss: 0.6591 - val\_sparse\_categorical\_accuracy: 0.7483  
Epoch 73/100  
469/469 - 1s - loss: 0.5574 - sparse\_categorical\_accuracy: 0.7903 - val\_loss: 0.6343 - val\_sparse\_categorical\_accuracy: 0.7758  
Epoch 74/100  
469/469 - 1s - loss: 0.5636 - sparse\_categorical\_accuracy: 0.7892 - val\_loss: 0.6414 - val\_sparse\_categorical\_accuracy: 0.7568  
Epoch 75/100  
469/469 - 1s - loss: 0.5650 - sparse\_categorical\_accuracy: 0.7866 - val\_loss: 0.6263 - val\_sparse\_categorical\_accuracy: 0.7728  
Epoch 76/100  
469/469 - 1s - loss: 0.5464 - sparse\_categorical\_accuracy: 0.7946 - val\_loss: 0.6052 - val\_sparse\_categorical\_accuracy: 0.7809  
Epoch 77/100  
469/469 - 1s - loss: 0.5445 - sparse\_categorical\_accuracy: 0.7950 - val\_loss: 0.6187 - val\_sparse\_categorical\_accuracy: 0.7830  
Epoch 78/100  
469/469 - 1s - loss: 0.5530 - sparse\_categorical\_accuracy: 0.7919 - val\_loss: 0.6313 - val\_sparse\_categorical\_accuracy: 0.7713  
Epoch 79/100  
469/469 - 1s - loss: 0.5487 - sparse\_categorical\_accuracy: 0.7944 - val\_loss: 0.6239 - val\_sparse\_categorical\_accuracy: 0.7759  
Epoch 80/100  
469/469 - 1s - loss: 0.5482 - sparse\_categorical\_accuracy: 0.7947 - val\_loss: 0.6061 - val\_sparse\_categorical\_accuracy: 0.7791  
Epoch 81/100  
469/469 - 1s - loss: 0.5452 - sparse\_categorical\_accuracy: 0.7977 - val\_loss: 0.6112 - val\_sparse\_categorical\_accuracy: 0.7835  
Epoch 82/100  
469/469 - 1s - loss: 0.5476 - sparse\_categorical\_accuracy: 0.7972 - val\_loss: 0.5969 - val\_sparse\_categorical\_accuracy: 0.7880  
Epoch 83/100  
469/469 - 1s - loss: 0.5374 - sparse\_categorical\_accuracy: 0.7991 - val\_loss: 0.6148 - val\_sparse\_categorical\_accuracy: 0.7832  
Epoch 84/100  
469/469 - 1s - loss: 0.5443 - sparse\_categorical\_accuracy: 0.7972 - val\_loss: 0.7188 - val\_sparse\_categorical\_accuracy: 0.7331  
Epoch 85/100  
469/469 - 1s - loss: 0.5511 - sparse\_categorical\_accuracy: 0.7936 - val\_loss: 0.6116 - val\_sparse\_categorical\_accuracy: 0.7722  
Epoch 86/100  
469/469 - 1s - loss: 0.5325 - sparse\_categorical\_accuracy: 0.8014 - val\_loss: 0.6109 - val\_sparse\_categorical\_accuracy: 0.7865  
Epoch 87/100  
469/469 - 1s - loss: 0.5416 - sparse\_categorical\_accuracy: 0.7994 - val\_loss: 0.6093 - val\_sparse\_categorical\_accuracy: 0.7857  
Epoch 88/100  
469/469 - 1s - loss: 0.5355 - sparse\_categorical\_accuracy: 0.7986 - val\_loss: 0.5964 - val\_sparse\_categorical\_accuracy: 0.7820  
Epoch 89/100  
469/469 - 1s - loss: 0.5385 - sparse\_categorical\_accuracy: 0.7975 - val\_loss: 0.6067 - val\_sparse\_categorical\_accuracy: 0.7872  
Epoch 90/100  
469/469 - 1s - loss: 0.5339 - sparse\_categorical\_accuracy: 0.8011 - val\_loss: 0.6044 - val\_sparse\_categorical\_accuracy: 0.7907  
Epoch 91/100  
469/469 - 1s - loss: 0.5316 - sparse\_categorical\_accuracy: 0.8030 - val\_loss: 0.6080 - val\_sparse\_categorical\_accuracy: 0.7907

```
tegorical_accuracy: 0.7866
Epoch 92/100
469/469 - 1s - loss: 0.5433 - sparse_categorical_accuracy: 0.7970 - val_loss: 0.5991 - val_sparse_ca
tegorical_accuracy: 0.7848
Epoch 93/100
469/469 - 1s - loss: 0.5256 - sparse_categorical_accuracy: 0.8054 - val_loss: 0.6332 - val_sparse_ca
tegorical_accuracy: 0.7752
Epoch 94/100
469/469 - 1s - loss: 0.5334 - sparse_categorical_accuracy: 0.8013 - val_loss: 0.6054 - val_sparse_ca
tegorical_accuracy: 0.7862
Epoch 95/100
469/469 - 1s - loss: 0.5315 - sparse_categorical_accuracy: 0.8022 - val_loss: 0.6144 - val_sparse_ca
tegorical_accuracy: 0.7799
Epoch 96/100
469/469 - 1s - loss: 0.5260 - sparse_categorical_accuracy: 0.8057 - val_loss: 0.6060 - val_sparse_ca
tegorical_accuracy: 0.7810
Epoch 97/100
469/469 - 1s - loss: 0.5305 - sparse_categorical_accuracy: 0.8016 - val_loss: 0.5992 - val_sparse_ca
tegorical_accuracy: 0.7905
Epoch 98/100
469/469 - 1s - loss: 0.5264 - sparse_categorical_accuracy: 0.8071 - val_loss: 0.6071 - val_sparse_ca
tegorical_accuracy: 0.7851
Epoch 99/100
469/469 - 1s - loss: 0.5264 - sparse_categorical_accuracy: 0.8042 - val_loss: 0.5991 - val_sparse_ca
tegorical_accuracy: 0.7879
Epoch 100/100
469/469 - 1s - loss: 0.5294 - sparse_categorical_accuracy: 0.8028 - val_loss: 0.5960 - val_sparse_ca
tegorical_accuracy: 0.7901
```

In [6]:

```
# Baseline model evaluation
model.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 0s - loss: 0.5960 - sparse_categorical_accuracy: 0.7901
```

Out[6]:

```
[0.5960487723350525, 0.7900999784469604]
```

In [7]:

```
# Learning rate 0.0001
optimizer = tf.keras.optimizers.Adam(learning_rate=0.0001)

model.compile(optimizer=optimizer,
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy']
            )
history = model.fit(x_train, y_train,
                  batch_size=128,
                  epochs=100,
                  validation_data=(x_test, y_test),
                  verbose=2
                )
```

```
Epoch 1/100
469/469 - 1s - loss: 0.5069 - sparse_categorical_accuracy: 0.8130 - val_loss: 0.5828 - val_sparse_ca
tegorical_accuracy: 0.7944
Epoch 2/100
469/469 - 1s - loss: 0.5022 - sparse_categorical_accuracy: 0.8135 - val_loss: 0.5814 - val_sparse_ca
tegorical_accuracy: 0.7980
Epoch 3/100
469/469 - 1s - loss: 0.4978 - sparse_categorical_accuracy: 0.8159 - val_loss: 0.5829 - val_sparse_ca
tegorical_accuracy: 0.7924
Epoch 4/100
469/469 - 1s - loss: 0.4972 - sparse_categorical_accuracy: 0.8149 - val_loss: 0.5795 - val_sparse_ca
tegorical_accuracy: 0.7968
Epoch 5/100
469/469 - 1s - loss: 0.4959 - sparse_categorical_accuracy: 0.8147 - val_loss: 0.5825 - val_sparse_ca
tegorical_accuracy: 0.7932
Epoch 6/100
469/469 - 1s - loss: 0.4940 - sparse_categorical_accuracy: 0.8162 - val_loss: 0.5800 - val_sparse_ca
tegorical_accuracy: 0.7986
Epoch 7/100
469/469 - 1s - loss: 0.4933 - sparse_categorical_accuracy: 0.8178 - val_loss: 0.5818 - val_sparse_ca
tegorical_accuracy: 0.7934
Epoch 8/100
469/469 - 1s - loss: 0.4928 - sparse_categorical_accuracy: 0.8180 - val_loss: 0.5818 - val_sparse_ca
tegorical_accuracy: 0.7964
Epoch 9/100
469/469 - 1s - loss: 0.4924 - sparse_categorical_accuracy: 0.8189 - val_loss: 0.5802 - val_sparse_ca
tegorical_accuracy: 0.7992
Epoch 10/100
```

469/469 - 1s - loss: 0.4925 - sparse\_categorical\_accuracy: 0.8188 - val\_loss: 0.5786 - val\_sparse\_categorical\_accuracy: 0.7980  
Epoch 11/100  
469/469 - 1s - loss: 0.4929 - sparse\_categorical\_accuracy: 0.8183 - val\_loss: 0.5815 - val\_sparse\_categorical\_accuracy: 0.7975  
Epoch 12/100  
469/469 - 1s - loss: 0.4918 - sparse\_categorical\_accuracy: 0.8184 - val\_loss: 0.5828 - val\_sparse\_categorical\_accuracy: 0.7961  
Epoch 13/100  
469/469 - 1s - loss: 0.4911 - sparse\_categorical\_accuracy: 0.8192 - val\_loss: 0.5837 - val\_sparse\_categorical\_accuracy: 0.7953  
Epoch 14/100  
469/469 - 1s - loss: 0.4905 - sparse\_categorical\_accuracy: 0.8194 - val\_loss: 0.5794 - val\_sparse\_categorical\_accuracy: 0.7982  
Epoch 15/100  
469/469 - 1s - loss: 0.4906 - sparse\_categorical\_accuracy: 0.8195 - val\_loss: 0.5823 - val\_sparse\_categorical\_accuracy: 0.7979  
Epoch 16/100  
469/469 - 1s - loss: 0.4903 - sparse\_categorical\_accuracy: 0.8195 - val\_loss: 0.5793 - val\_sparse\_categorical\_accuracy: 0.7971  
Epoch 17/100  
469/469 - 1s - loss: 0.4897 - sparse\_categorical\_accuracy: 0.8193 - val\_loss: 0.5797 - val\_sparse\_categorical\_accuracy: 0.7976  
Epoch 18/100  
469/469 - 1s - loss: 0.4898 - sparse\_categorical\_accuracy: 0.8192 - val\_loss: 0.5811 - val\_sparse\_categorical\_accuracy: 0.7955  
Epoch 19/100  
469/469 - 1s - loss: 0.4890 - sparse\_categorical\_accuracy: 0.8205 - val\_loss: 0.5833 - val\_sparse\_categorical\_accuracy: 0.7936  
Epoch 20/100  
469/469 - 1s - loss: 0.4891 - sparse\_categorical\_accuracy: 0.8187 - val\_loss: 0.5816 - val\_sparse\_categorical\_accuracy: 0.7957  
Epoch 21/100  
469/469 - 1s - loss: 0.4886 - sparse\_categorical\_accuracy: 0.8201 - val\_loss: 0.5812 - val\_sparse\_categorical\_accuracy: 0.7944  
Epoch 22/100  
469/469 - 1s - loss: 0.4881 - sparse\_categorical\_accuracy: 0.8195 - val\_loss: 0.5801 - val\_sparse\_categorical\_accuracy: 0.7980  
Epoch 23/100  
469/469 - 1s - loss: 0.4869 - sparse\_categorical\_accuracy: 0.8207 - val\_loss: 0.5848 - val\_sparse\_categorical\_accuracy: 0.7966  
Epoch 24/100  
469/469 - 1s - loss: 0.4884 - sparse\_categorical\_accuracy: 0.8199 - val\_loss: 0.5840 - val\_sparse\_categorical\_accuracy: 0.7965  
Epoch 25/100  
469/469 - 1s - loss: 0.4881 - sparse\_categorical\_accuracy: 0.8204 - val\_loss: 0.5835 - val\_sparse\_categorical\_accuracy: 0.7978  
Epoch 26/100  
469/469 - 1s - loss: 0.4868 - sparse\_categorical\_accuracy: 0.8210 - val\_loss: 0.5815 - val\_sparse\_categorical\_accuracy: 0.7979  
Epoch 27/100  
469/469 - 1s - loss: 0.4864 - sparse\_categorical\_accuracy: 0.8207 - val\_loss: 0.5838 - val\_sparse\_categorical\_accuracy: 0.7957  
Epoch 28/100  
469/469 - 1s - loss: 0.4862 - sparse\_categorical\_accuracy: 0.8209 - val\_loss: 0.5835 - val\_sparse\_categorical\_accuracy: 0.7948  
Epoch 29/100  
469/469 - 1s - loss: 0.4864 - sparse\_categorical\_accuracy: 0.8210 - val\_loss: 0.5865 - val\_sparse\_categorical\_accuracy: 0.7963  
Epoch 30/100  
469/469 - 1s - loss: 0.4867 - sparse\_categorical\_accuracy: 0.8209 - val\_loss: 0.5858 - val\_sparse\_categorical\_accuracy: 0.7948  
Epoch 31/100  
469/469 - 1s - loss: 0.4861 - sparse\_categorical\_accuracy: 0.8212 - val\_loss: 0.5846 - val\_sparse\_categorical\_accuracy: 0.7982  
Epoch 32/100  
469/469 - 1s - loss: 0.4856 - sparse\_categorical\_accuracy: 0.8208 - val\_loss: 0.5843 - val\_sparse\_categorical\_accuracy: 0.7968  
Epoch 33/100  
469/469 - 1s - loss: 0.4851 - sparse\_categorical\_accuracy: 0.8208 - val\_loss: 0.5829 - val\_sparse\_categorical\_accuracy: 0.7972  
Epoch 34/100  
469/469 - 1s - loss: 0.4849 - sparse\_categorical\_accuracy: 0.8207 - val\_loss: 0.5855 - val\_sparse\_categorical\_accuracy: 0.7980  
Epoch 35/100  
469/469 - 1s - loss: 0.4853 - sparse\_categorical\_accuracy: 0.8210 - val\_loss: 0.5863 - val\_sparse\_categorical\_accuracy: 0.7956  
Epoch 36/100  
469/469 - 1s - loss: 0.4848 - sparse\_categorical\_accuracy: 0.8215 - val\_loss: 0.5873 - val\_sparse\_categorical\_accuracy: 0.7984  
Epoch 37/100  
469/469 - 1s - loss: 0.4846 - sparse\_categorical\_accuracy: 0.8211 - val\_loss: 0.5846 - val\_sparse\_categorical\_accuracy: 0.7973

Epoch 38/100  
469/469 - 1s - loss: 0.4843 - sparse\_categorical\_accuracy: 0.8223 - val\_loss: 0.5862 - val\_sparse\_categorical\_accuracy: 0.7980  
Epoch 39/100  
469/469 - 1s - loss: 0.4847 - sparse\_categorical\_accuracy: 0.8214 - val\_loss: 0.5887 - val\_sparse\_categorical\_accuracy: 0.7959  
Epoch 40/100  
469/469 - 1s - loss: 0.4844 - sparse\_categorical\_accuracy: 0.8215 - val\_loss: 0.5867 - val\_sparse\_categorical\_accuracy: 0.7963  
Epoch 41/100  
469/469 - 1s - loss: 0.4838 - sparse\_categorical\_accuracy: 0.8219 - val\_loss: 0.5839 - val\_sparse\_categorical\_accuracy: 0.7971  
Epoch 42/100  
469/469 - 1s - loss: 0.4843 - sparse\_categorical\_accuracy: 0.8214 - val\_loss: 0.5867 - val\_sparse\_categorical\_accuracy: 0.7977  
Epoch 43/100  
469/469 - 1s - loss: 0.4842 - sparse\_categorical\_accuracy: 0.8218 - val\_loss: 0.5889 - val\_sparse\_categorical\_accuracy: 0.7983  
Epoch 44/100  
469/469 - 1s - loss: 0.4844 - sparse\_categorical\_accuracy: 0.8213 - val\_loss: 0.5926 - val\_sparse\_categorical\_accuracy: 0.7951  
Epoch 45/100  
469/469 - 1s - loss: 0.4843 - sparse\_categorical\_accuracy: 0.8218 - val\_loss: 0.5886 - val\_sparse\_categorical\_accuracy: 0.7934  
Epoch 46/100  
469/469 - 1s - loss: 0.4833 - sparse\_categorical\_accuracy: 0.8219 - val\_loss: 0.5886 - val\_sparse\_categorical\_accuracy: 0.7981  
Epoch 47/100  
469/469 - 1s - loss: 0.4834 - sparse\_categorical\_accuracy: 0.8224 - val\_loss: 0.5901 - val\_sparse\_categorical\_accuracy: 0.7977  
Epoch 48/100  
469/469 - 1s - loss: 0.4831 - sparse\_categorical\_accuracy: 0.8215 - val\_loss: 0.5914 - val\_sparse\_categorical\_accuracy: 0.7941  
Epoch 49/100  
469/469 - 1s - loss: 0.4828 - sparse\_categorical\_accuracy: 0.8221 - val\_loss: 0.5927 - val\_sparse\_categorical\_accuracy: 0.7961  
Epoch 50/100  
469/469 - 1s - loss: 0.4832 - sparse\_categorical\_accuracy: 0.8220 - val\_loss: 0.5884 - val\_sparse\_categorical\_accuracy: 0.7966  
Epoch 51/100  
469/469 - 1s - loss: 0.4821 - sparse\_categorical\_accuracy: 0.8229 - val\_loss: 0.5928 - val\_sparse\_categorical\_accuracy: 0.7957  
Epoch 52/100  
469/469 - 1s - loss: 0.4822 - sparse\_categorical\_accuracy: 0.8219 - val\_loss: 0.5871 - val\_sparse\_categorical\_accuracy: 0.7962  
Epoch 53/100  
469/469 - 1s - loss: 0.4820 - sparse\_categorical\_accuracy: 0.8228 - val\_loss: 0.5919 - val\_sparse\_categorical\_accuracy: 0.7961  
Epoch 54/100  
469/469 - 1s - loss: 0.4817 - sparse\_categorical\_accuracy: 0.8233 - val\_loss: 0.5949 - val\_sparse\_categorical\_accuracy: 0.7980  
Epoch 55/100  
469/469 - 1s - loss: 0.4838 - sparse\_categorical\_accuracy: 0.8212 - val\_loss: 0.5937 - val\_sparse\_categorical\_accuracy: 0.7969  
Epoch 56/100  
469/469 - 1s - loss: 0.4821 - sparse\_categorical\_accuracy: 0.8228 - val\_loss: 0.5983 - val\_sparse\_categorical\_accuracy: 0.7957  
Epoch 57/100  
469/469 - 1s - loss: 0.4817 - sparse\_categorical\_accuracy: 0.8231 - val\_loss: 0.5999 - val\_sparse\_categorical\_accuracy: 0.7909  
Epoch 58/100  
469/469 - 1s - loss: 0.4810 - sparse\_categorical\_accuracy: 0.8231 - val\_loss: 0.5945 - val\_sparse\_categorical\_accuracy: 0.7971  
Epoch 59/100  
469/469 - 1s - loss: 0.4809 - sparse\_categorical\_accuracy: 0.8233 - val\_loss: 0.5927 - val\_sparse\_categorical\_accuracy: 0.7978  
Epoch 60/100  
469/469 - 1s - loss: 0.4809 - sparse\_categorical\_accuracy: 0.8228 - val\_loss: 0.5954 - val\_sparse\_categorical\_accuracy: 0.7958  
Epoch 61/100  
469/469 - 1s - loss: 0.4810 - sparse\_categorical\_accuracy: 0.8223 - val\_loss: 0.5974 - val\_sparse\_categorical\_accuracy: 0.7966  
Epoch 62/100  
469/469 - 1s - loss: 0.4805 - sparse\_categorical\_accuracy: 0.8227 - val\_loss: 0.5982 - val\_sparse\_categorical\_accuracy: 0.7982  
Epoch 63/100  
469/469 - 1s - loss: 0.4801 - sparse\_categorical\_accuracy: 0.8232 - val\_loss: 0.5967 - val\_sparse\_categorical\_accuracy: 0.7960  
Epoch 64/100  
469/469 - 1s - loss: 0.4809 - sparse\_categorical\_accuracy: 0.8231 - val\_loss: 0.5941 - val\_sparse\_categorical\_accuracy: 0.7948  
Epoch 65/100  
469/469 - 1s - loss: 0.4805 - sparse\_categorical\_accuracy: 0.8230 - val\_loss: 0.5959 - val\_sparse\_categorical\_accuracy: 0.7948

tegorical\_accuracy: 0.7945  
Epoch 66/100  
469/469 - 1s - loss: 0.4804 - sparse\_categorical\_accuracy: 0.8236 - val\_loss: 0.5969 - val\_sparse\_ca  
tegorical\_accuracy: 0.7974  
Epoch 67/100  
469/469 - 1s - loss: 0.4796 - sparse\_categorical\_accuracy: 0.8241 - val\_loss: 0.5953 - val\_sparse\_ca  
tegorical\_accuracy: 0.7986  
Epoch 68/100  
469/469 - 1s - loss: 0.4804 - sparse\_categorical\_accuracy: 0.8232 - val\_loss: 0.5948 - val\_sparse\_ca  
tegorical\_accuracy: 0.7986  
Epoch 69/100  
469/469 - 1s - loss: 0.4810 - sparse\_categorical\_accuracy: 0.8227 - val\_loss: 0.5950 - val\_sparse\_ca  
tegorical\_accuracy: 0.7984  
Epoch 70/100  
469/469 - 1s - loss: 0.4800 - sparse\_categorical\_accuracy: 0.8237 - val\_loss: 0.5979 - val\_sparse\_ca  
tegorical\_accuracy: 0.7994  
Epoch 71/100  
469/469 - 1s - loss: 0.4802 - sparse\_categorical\_accuracy: 0.8231 - val\_loss: 0.5983 - val\_sparse\_ca  
tegorical\_accuracy: 0.7981  
Epoch 72/100  
469/469 - 1s - loss: 0.4791 - sparse\_categorical\_accuracy: 0.8239 - val\_loss: 0.5946 - val\_sparse\_ca  
tegorical\_accuracy: 0.7989  
Epoch 73/100  
469/469 - 1s - loss: 0.4799 - sparse\_categorical\_accuracy: 0.8232 - val\_loss: 0.5978 - val\_sparse\_ca  
tegorical\_accuracy: 0.7959  
Epoch 74/100  
469/469 - 1s - loss: 0.4794 - sparse\_categorical\_accuracy: 0.8236 - val\_loss: 0.5939 - val\_sparse\_ca  
tegorical\_accuracy: 0.7970  
Epoch 75/100  
469/469 - 1s - loss: 0.4800 - sparse\_categorical\_accuracy: 0.8235 - val\_loss: 0.5996 - val\_sparse\_ca  
tegorical\_accuracy: 0.7963  
Epoch 76/100  
469/469 - 1s - loss: 0.4792 - sparse\_categorical\_accuracy: 0.8239 - val\_loss: 0.5990 - val\_sparse\_ca  
tegorical\_accuracy: 0.7965  
Epoch 77/100  
469/469 - 1s - loss: 0.4799 - sparse\_categorical\_accuracy: 0.8234 - val\_loss: 0.6012 - val\_sparse\_ca  
tegorical\_accuracy: 0.7952  
Epoch 78/100  
469/469 - 1s - loss: 0.4781 - sparse\_categorical\_accuracy: 0.8242 - val\_loss: 0.6036 - val\_sparse\_ca  
tegorical\_accuracy: 0.7980  
Epoch 79/100  
469/469 - 1s - loss: 0.4784 - sparse\_categorical\_accuracy: 0.8234 - val\_loss: 0.5983 - val\_sparse\_ca  
tegorical\_accuracy: 0.7982  
Epoch 80/100  
469/469 - 1s - loss: 0.4782 - sparse\_categorical\_accuracy: 0.8238 - val\_loss: 0.5981 - val\_sparse\_ca  
tegorical\_accuracy: 0.7975  
Epoch 81/100  
469/469 - 1s - loss: 0.4791 - sparse\_categorical\_accuracy: 0.8236 - val\_loss: 0.6002 - val\_sparse\_ca  
tegorical\_accuracy: 0.7958  
Epoch 82/100  
469/469 - 1s - loss: 0.4789 - sparse\_categorical\_accuracy: 0.8244 - val\_loss: 0.6011 - val\_sparse\_ca  
tegorical\_accuracy: 0.7971  
Epoch 83/100  
469/469 - 1s - loss: 0.4782 - sparse\_categorical\_accuracy: 0.8245 - val\_loss: 0.6019 - val\_sparse\_ca  
tegorical\_accuracy: 0.7981  
Epoch 84/100  
469/469 - 1s - loss: 0.4781 - sparse\_categorical\_accuracy: 0.8243 - val\_loss: 0.6015 - val\_sparse\_ca  
tegorical\_accuracy: 0.7991  
Epoch 85/100  
469/469 - 1s - loss: 0.4779 - sparse\_categorical\_accuracy: 0.8246 - val\_loss: 0.5995 - val\_sparse\_ca  
tegorical\_accuracy: 0.7981  
Epoch 86/100  
469/469 - 1s - loss: 0.4795 - sparse\_categorical\_accuracy: 0.8234 - val\_loss: 0.6024 - val\_sparse\_ca  
tegorical\_accuracy: 0.7971  
Epoch 87/100  
469/469 - 1s - loss: 0.4798 - sparse\_categorical\_accuracy: 0.8226 - val\_loss: 0.6014 - val\_sparse\_ca  
tegorical\_accuracy: 0.7984  
Epoch 88/100  
469/469 - 1s - loss: 0.4781 - sparse\_categorical\_accuracy: 0.8242 - val\_loss: 0.6023 - val\_sparse\_ca  
tegorical\_accuracy: 0.7980  
Epoch 89/100  
469/469 - 1s - loss: 0.4773 - sparse\_categorical\_accuracy: 0.8247 - val\_loss: 0.6021 - val\_sparse\_ca  
tegorical\_accuracy: 0.7967  
Epoch 90/100  
469/469 - 1s - loss: 0.4781 - sparse\_categorical\_accuracy: 0.8242 - val\_loss: 0.5997 - val\_sparse\_ca  
tegorical\_accuracy: 0.7986  
Epoch 91/100  
469/469 - 1s - loss: 0.4777 - sparse\_categorical\_accuracy: 0.8241 - val\_loss: 0.6023 - val\_sparse\_ca  
tegorical\_accuracy: 0.7992  
Epoch 92/100  
469/469 - 1s - loss: 0.4773 - sparse\_categorical\_accuracy: 0.8250 - val\_loss: 0.6045 - val\_sparse\_ca  
tegorical\_accuracy: 0.7971  
Epoch 93/100



```
469/469 - 1s - loss: 0.4773 - sparse_categorical_accuracy: 0.8245 - val_loss: 0.6087 - val_sparse_categorical_accuracy: 0.7968
Epoch 94/100
469/469 - 1s - loss: 0.4792 - sparse_categorical_accuracy: 0.8236 - val_loss: 0.6005 - val_sparse_categorical_accuracy: 0.7977
Epoch 95/100
469/469 - 1s - loss: 0.4772 - sparse_categorical_accuracy: 0.8250 - val_loss: 0.6016 - val_sparse_categorical_accuracy: 0.7980
Epoch 96/100
469/469 - 1s - loss: 0.4776 - sparse_categorical_accuracy: 0.8243 - val_loss: 0.6010 - val_sparse_categorical_accuracy: 0.7985
Epoch 97/100
469/469 - 1s - loss: 0.4765 - sparse_categorical_accuracy: 0.8252 - val_loss: 0.6077 - val_sparse_categorical_accuracy: 0.7948
Epoch 98/100
469/469 - 1s - loss: 0.4764 - sparse_categorical_accuracy: 0.8253 - val_loss: 0.6048 - val_sparse_categorical_accuracy: 0.7969
Epoch 99/100
469/469 - 1s - loss: 0.4762 - sparse_categorical_accuracy: 0.8259 - val_loss: 0.6027 - val_sparse_categorical_accuracy: 0.7984
Epoch 100/100
469/469 - 1s - loss: 0.4772 - sparse_categorical_accuracy: 0.8247 - val_loss: 0.6074 - val_sparse_categorical_accuracy: 0.7957
```

In [8]:

```
# Learning rate 0.0001
model.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 0s - loss: 0.6074 - sparse_categorical_accuracy: 0.7957
```

Out[8]:

```
[0.6074172854423523, 0.7957000136375427]
```

In [9]:

```
# Learning rate 0.00001
optimizer = tf.keras.optimizers.Adam(learning_rate=0.00001)

model.compile(optimizer=optimizer,
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy']
            )
history = model.fit(x_train, y_train,
                   batch_size=128,
                   epochs=100,
                   validation_data=(x_test, y_test),
                   verbose=2
                  )
```

```
Epoch 1/100
469/469 - 1s - loss: 0.4751 - sparse_categorical_accuracy: 0.8258 - val_loss: 0.6023 - val_sparse_categorical_accuracy: 0.7977
Epoch 2/100
469/469 - 1s - loss: 0.4738 - sparse_categorical_accuracy: 0.8259 - val_loss: 0.6027 - val_sparse_categorical_accuracy: 0.7990
Epoch 3/100
469/469 - 1s - loss: 0.4735 - sparse_categorical_accuracy: 0.8264 - val_loss: 0.6023 - val_sparse_categorical_accuracy: 0.7985
Epoch 4/100
469/469 - 1s - loss: 0.4733 - sparse_categorical_accuracy: 0.8265 - val_loss: 0.6031 - val_sparse_categorical_accuracy: 0.7976
Epoch 5/100
469/469 - 1s - loss: 0.4732 - sparse_categorical_accuracy: 0.8264 - val_loss: 0.6038 - val_sparse_categorical_accuracy: 0.7979
Epoch 6/100
469/469 - 1s - loss: 0.4731 - sparse_categorical_accuracy: 0.8263 - val_loss: 0.6040 - val_sparse_categorical_accuracy: 0.7986
Epoch 7/100
469/469 - 1s - loss: 0.4730 - sparse_categorical_accuracy: 0.8265 - val_loss: 0.6042 - val_sparse_categorical_accuracy: 0.7985
Epoch 8/100
469/469 - 1s - loss: 0.4729 - sparse_categorical_accuracy: 0.8264 - val_loss: 0.6043 - val_sparse_categorical_accuracy: 0.7983
Epoch 9/100
469/469 - 1s - loss: 0.4728 - sparse_categorical_accuracy: 0.8263 - val_loss: 0.6042 - val_sparse_categorical_accuracy: 0.7991
Epoch 10/100
469/469 - 1s - loss: 0.4729 - sparse_categorical_accuracy: 0.8264 - val_loss: 0.6038 - val_sparse_categorical_accuracy: 0.7976
Epoch 11/100
469/469 - 1s - loss: 0.4728 - sparse_categorical_accuracy: 0.8264 - val_loss: 0.6054 - val_sparse_categorical_accuracy: 0.7988
```

[illegible]

[illegible]

[illegible]

```
Epoch 95/100
469/469 - 1s - loss: 0.4713 - sparse_categorical_accuracy: 0.8274 - val_loss: 0.6094 - val_sparse_categorical_accuracy: 0.7978
Epoch 96/100
469/469 - 1s - loss: 0.4713 - sparse_categorical_accuracy: 0.8273 - val_loss: 0.6095 - val_sparse_categorical_accuracy: 0.7980
Epoch 97/100
469/469 - 1s - loss: 0.4714 - sparse_categorical_accuracy: 0.8275 - val_loss: 0.6098 - val_sparse_categorical_accuracy: 0.7977
Epoch 98/100
469/469 - 1s - loss: 0.4713 - sparse_categorical_accuracy: 0.8271 - val_loss: 0.6109 - val_sparse_categorical_accuracy: 0.7974
Epoch 99/100
469/469 - 1s - loss: 0.4713 - sparse_categorical_accuracy: 0.8276 - val_loss: 0.6091 - val_sparse_categorical_accuracy: 0.7980
Epoch 100/100
469/469 - 1s - loss: 0.4713 - sparse_categorical_accuracy: 0.8276 - val_loss: 0.6095 - val_sparse_categorical_accuracy: 0.7990
```

In [10]:

```
# Learning rate 0.00001
model.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 0s - loss: 0.6095 - sparse_categorical_accuracy: 0.7990
```

Out[10]:

```
[0.6095350384712219, 0.7990000247955322]
```

In [11]:

```
# SGD
model = tf.keras.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    tf.keras.layers.Dense(16, activation='relu'),
    tf.keras.layers.Dense(16, activation='relu'),
    tf.keras.layers.Dense(10, activation='softmax')
])

model.compile(optimizer='sgd',
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy'])

history = model.fit(x_train, y_train,
                    batch_size=128,
                    epochs=100,
                    validation_data=(x_test, y_test),
                    verbose=2)
```

```
Epoch 1/100
469/469 - 1s - loss: 4.1699 - sparse_categorical_accuracy: 0.0984 - val_loss: 2.3032 - val_sparse_categorical_accuracy: 0.1000
Epoch 2/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0982 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
Epoch 3/100
469/469 - 1s - loss: 2.3028 - sparse_categorical_accuracy: 0.0967 - val_loss: 2.3032 - val_sparse_categorical_accuracy: 0.1000
Epoch 4/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0972 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
Epoch 5/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0982 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
Epoch 6/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0974 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
Epoch 7/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0981 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
Epoch 8/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0979 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.0999
Epoch 9/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0971 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.0999
Epoch 10/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0973 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
Epoch 11/100
469/469 - 1s - loss: 2.3025 - sparse_categorical_accuracy: 0.0975 - val_loss: 2.3031 - val_sparse_categorical_accuracy: 0.1000
```

[illegible]

469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0974 - val\_loss: 2.3028 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 40/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0993 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.0999  
Epoch 41/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0962 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 42/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0975 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 43/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0983 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.0999  
Epoch 44/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0974 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.0999  
Epoch 45/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0970 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.0999  
Epoch 46/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0956 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 47/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0980 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.0999  
Epoch 48/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0984 - val\_loss: 2.3027 - val\_sparse\_categorical\_accuracy: 0.0999  
Epoch 49/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0972 - val\_loss: 2.3026 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 50/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0974 - val\_loss: 2.3026 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 51/100  
469/469 - 1s - loss: 2.3025 - sparse\_categorical\_accuracy: 0.0980 - val\_loss: 2.3026 - val\_sparse\_categorical\_accuracy: 0.1000  
Epoch 52/100  
469/469 - 1s - loss: 2.3024 - sparse\_categorical\_accuracy: 0.0955 - val\_loss: 2.3023 - val\_sparse\_categorical\_accuracy: 0.1001  
Epoch 53/100  
469/469 - 1s - loss: 2.3023 - sparse\_categorical\_accuracy: 0.0982 - val\_loss: 2.3020 - val\_sparse\_categorical\_accuracy: 0.1003  
Epoch 54/100  
469/469 - 1s - loss: 2.3021 - sparse\_categorical\_accuracy: 0.0978 - val\_loss: 2.3016 - val\_sparse\_categorical\_accuracy: 0.1004  
Epoch 55/100  
469/469 - 1s - loss: 2.3020 - sparse\_categorical\_accuracy: 0.0975 - val\_loss: 2.3014 - val\_sparse\_categorical\_accuracy: 0.1006  
Epoch 56/100  
469/469 - 1s - loss: 2.3016 - sparse\_categorical\_accuracy: 0.0977 - val\_loss: 2.3016 - val\_sparse\_categorical\_accuracy: 0.1004  
Epoch 57/100  
469/469 - 1s - loss: 2.3018 - sparse\_categorical\_accuracy: 0.0985 - val\_loss: 2.3012 - val\_sparse\_categorical\_accuracy: 0.1005  
Epoch 58/100  
469/469 - 1s - loss: 2.3018 - sparse\_categorical\_accuracy: 0.0978 - val\_loss: 2.3010 - val\_sparse\_categorical\_accuracy: 0.1004  
Epoch 59/100  
469/469 - 1s - loss: 2.3007 - sparse\_categorical\_accuracy: 0.0984 - val\_loss: 2.2964 - val\_sparse\_categorical\_accuracy: 0.1061  
Epoch 60/100  
469/469 - 1s - loss: 2.2637 - sparse\_categorical\_accuracy: 0.1191 - val\_loss: 2.2126 - val\_sparse\_categorical\_accuracy: 0.1472  
Epoch 61/100  
469/469 - 1s - loss: 2.1646 - sparse\_categorical\_accuracy: 0.1663 - val\_loss: 2.0838 - val\_sparse\_categorical\_accuracy: 0.2027  
Epoch 62/100  
469/469 - 1s - loss: 2.0371 - sparse\_categorical\_accuracy: 0.2175 - val\_loss: 2.0069 - val\_sparse\_categorical\_accuracy: 0.2330  
Epoch 63/100  
469/469 - 1s - loss: 1.9881 - sparse\_categorical\_accuracy: 0.2352 - val\_loss: 1.8927 - val\_sparse\_categorical\_accuracy: 0.2530  
Epoch 64/100  
469/469 - 1s - loss: 1.8158 - sparse\_categorical\_accuracy: 0.2908 - val\_loss: 1.7579 - val\_sparse\_categorical\_accuracy: 0.3021  
Epoch 65/100  
469/469 - 1s - loss: 1.7669 - sparse\_categorical\_accuracy: 0.2788 - val\_loss: 1.6618 - val\_sparse\_categorical\_accuracy: 0.3573  
Epoch 66/100  
469/469 - 1s - loss: 1.5590 - sparse\_categorical\_accuracy: 0.3406 - val\_loss: 1.5188 - val\_sparse\_categorical\_accuracy: 0.3438

Epoch 67/100  
469/469 - 1s - loss: 1.4704 - sparse\_categorical\_accuracy: 0.3495 - val\_loss: 1.4799 - val\_sparse\_categorical\_accuracy: 0.3320  
Epoch 68/100  
469/469 - 1s - loss: 1.4223 - sparse\_categorical\_accuracy: 0.3596 - val\_loss: 1.4811 - val\_sparse\_categorical\_accuracy: 0.3142  
Epoch 69/100  
469/469 - 1s - loss: 1.3937 - sparse\_categorical\_accuracy: 0.3657 - val\_loss: 1.3939 - val\_sparse\_categorical\_accuracy: 0.3798  
Epoch 70/100  
469/469 - 1s - loss: 1.4371 - sparse\_categorical\_accuracy: 0.3597 - val\_loss: 1.7483 - val\_sparse\_categorical\_accuracy: 0.2903  
Epoch 71/100  
469/469 - 1s - loss: 1.6981 - sparse\_categorical\_accuracy: 0.2813 - val\_loss: 1.6548 - val\_sparse\_categorical\_accuracy: 0.2960  
Epoch 72/100  
469/469 - 1s - loss: 2.0228 - sparse\_categorical\_accuracy: 0.1892 - val\_loss: 2.3262 - val\_sparse\_categorical\_accuracy: 0.1056  
Epoch 73/100  
469/469 - 1s - loss: 2.2517 - sparse\_categorical\_accuracy: 0.1008 - val\_loss: 2.1872 - val\_sparse\_categorical\_accuracy: 0.1087  
Epoch 74/100  
469/469 - 1s - loss: 2.1293 - sparse\_categorical\_accuracy: 0.1784 - val\_loss: 2.0777 - val\_sparse\_categorical\_accuracy: 0.1998  
Epoch 75/100  
469/469 - 1s - loss: 2.0333 - sparse\_categorical\_accuracy: 0.1991 - val\_loss: 1.9935 - val\_sparse\_categorical\_accuracy: 0.1999  
Epoch 76/100  
469/469 - 1s - loss: 1.9582 - sparse\_categorical\_accuracy: 0.1996 - val\_loss: 1.9265 - val\_sparse\_categorical\_accuracy: 0.2000  
Epoch 77/100  
469/469 - 1s - loss: 1.9035 - sparse\_categorical\_accuracy: 0.2007 - val\_loss: 1.8773 - val\_sparse\_categorical\_accuracy: 0.1995  
Epoch 78/100  
469/469 - 1s - loss: 1.8585 - sparse\_categorical\_accuracy: 0.1995 - val\_loss: 1.8434 - val\_sparse\_categorical\_accuracy: 0.1999  
Epoch 79/100  
469/469 - 1s - loss: 1.8250 - sparse\_categorical\_accuracy: 0.1994 - val\_loss: 1.8354 - val\_sparse\_categorical\_accuracy: 0.1953  
Epoch 80/100  
469/469 - 1s - loss: 1.8008 - sparse\_categorical\_accuracy: 0.1980 - val\_loss: 1.8011 - val\_sparse\_categorical\_accuracy: 0.1977  
Epoch 81/100  
469/469 - 1s - loss: 1.7802 - sparse\_categorical\_accuracy: 0.1978 - val\_loss: 1.7721 - val\_sparse\_categorical\_accuracy: 0.1999  
Epoch 82/100  
469/469 - 1s - loss: 1.7657 - sparse\_categorical\_accuracy: 0.2001 - val\_loss: 1.7639 - val\_sparse\_categorical\_accuracy: 0.2001  
Epoch 83/100  
469/469 - 1s - loss: 1.7530 - sparse\_categorical\_accuracy: 0.1992 - val\_loss: 1.7473 - val\_sparse\_categorical\_accuracy: 0.1983  
Epoch 84/100  
469/469 - 1s - loss: 1.7430 - sparse\_categorical\_accuracy: 0.2002 - val\_loss: 1.7535 - val\_sparse\_categorical\_accuracy: 0.1996  
Epoch 85/100  
469/469 - 1s - loss: 1.7358 - sparse\_categorical\_accuracy: 0.1980 - val\_loss: 1.7310 - val\_sparse\_categorical\_accuracy: 0.1993  
Epoch 86/100  
469/469 - 1s - loss: 1.7283 - sparse\_categorical\_accuracy: 0.1990 - val\_loss: 1.7257 - val\_sparse\_categorical\_accuracy: 0.1989  
Epoch 87/100  
469/469 - 1s - loss: 1.7238 - sparse\_categorical\_accuracy: 0.1991 - val\_loss: 1.7229 - val\_sparse\_categorical\_accuracy: 0.1983  
Epoch 88/100  
469/469 - 1s - loss: 1.7234 - sparse\_categorical\_accuracy: 0.1979 - val\_loss: 1.7307 - val\_sparse\_categorical\_accuracy: 0.2002  
Epoch 89/100  
469/469 - 1s - loss: 1.7158 - sparse\_categorical\_accuracy: 0.1989 - val\_loss: 1.7153 - val\_sparse\_categorical\_accuracy: 0.1996  
Epoch 90/100  
469/469 - 1s - loss: 1.7150 - sparse\_categorical\_accuracy: 0.1968 - val\_loss: 1.7180 - val\_sparse\_categorical\_accuracy: 0.1977  
Epoch 91/100  
469/469 - 1s - loss: 1.7084 - sparse\_categorical\_accuracy: 0.1951 - val\_loss: 1.7092 - val\_sparse\_categorical\_accuracy: 0.2001  
Epoch 92/100  
469/469 - 1s - loss: 1.7035 - sparse\_categorical\_accuracy: 0.1966 - val\_loss: 1.7063 - val\_sparse\_categorical\_accuracy: 0.1984  
Epoch 93/100  
469/469 - 1s - loss: 1.7034 - sparse\_categorical\_accuracy: 0.1986 - val\_loss: 1.7040 - val\_sparse\_categorical\_accuracy: 0.2005  
Epoch 94/100  
469/469 - 1s - loss: 1.6985 - sparse\_categorical\_accuracy: 0.1990 - val\_loss: 1.7016 - val\_sparse\_categorical\_accuracy: 0.2005



```
tegorical_accuracy: 0.1999
Epoch 95/100
469/469 - 1s - loss: 1.6979 - sparse_categorical_accuracy: 0.1992 - val_loss: 1.7018 - val_sparse_ca
tegorical_accuracy: 0.1998
Epoch 96/100
469/469 - 1s - loss: 1.7495 - sparse_categorical_accuracy: 0.1951 - val_loss: 3.1656 - val_sparse_ca
tegorical_accuracy: 0.1015
Epoch 97/100
469/469 - 1s - loss: 2.9357 - sparse_categorical_accuracy: 0.1002 - val_loss: 2.7323 - val_sparse_ca
tegorical_accuracy: 0.1013
Epoch 98/100
469/469 - 1s - loss: 2.5954 - sparse_categorical_accuracy: 0.0995 - val_loss: 2.4841 - val_sparse_ca
tegorical_accuracy: 0.1013
Epoch 99/100
469/469 - 1s - loss: 2.4214 - sparse_categorical_accuracy: 0.1002 - val_loss: 2.3723 - val_sparse_ca
tegorical_accuracy: 0.1013
Epoch 100/100
469/469 - 1s - loss: 2.3477 - sparse_categorical_accuracy: 0.0989 - val_loss: 2.3278 - val_sparse_ca
tegorical_accuracy: 0.1013
```

In [12]:

```
model.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 0s - loss: 2.3278 - sparse_categorical_accuracy: 0.1013
```

Out[12]:

```
[2.327831506729126, 0.10130000114440918]
```