

In [1]:

```
import tensorflow as tf
#import tensorflow_datasets as tfds
```

## Baseline model

In [2]:

```
# Load Data
# tfds.list_builders()
# (train, test), info = tfds.load("mnist", split=['train', 'test'], with_info=True, as_supervised=True)
(x_train, y_train), (x_test, y_test) = tf.keras.datasets.mnist.load_data()
#(x_train, y_train), (x_test, y_test) = tf.keras.datasets.fashion_mnist.load_data()
```

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/mnist.npz>  
11493376/11490434 [=====] - 0s 0us/step  
11501568/11490434 [=====] - 0s 0us/step

In [3]:

```
# Baseline model definition
model = tf.keras.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    tf.keras.layers.Dense(16, activation='relu'),
    tf.keras.layers.Dense(16, activation='relu'),
    tf.keras.layers.Dense(10, activation='softmax')
])
```

In [4]:

```
# Baseline model compilation
model.compile(optimizer='adam',
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy'])
```

In [5]:

```
# Baseline model fitting
history = model.fit(x_train, y_train,
                    batch_size=128,
                    epochs=100,
                    validation_data=(x_test, y_test),
                    verbose=2)
```

```
Epoch 1/100
469/469 - 4s - loss: 3.4456 - sparse_categorical_accuracy: 0.1932 - val_loss: 2.0675 - val_sparse_categorical_accuracy: 0.2054 - 4s/epoch - 8ms/step
Epoch 2/100
469/469 - 2s - loss: 2.0427 - sparse_categorical_accuracy: 0.2061 - val_loss: 2.0334 - val_sparse_categorical_accuracy: 0.2078 - 2s/epoch - 4ms/step
Epoch 3/100
469/469 - 2s - loss: 2.0152 - sparse_categorical_accuracy: 0.2096 - val_loss: 2.0110 - val_sparse_categorical_accuracy: 0.2105 - 2s/epoch - 4ms/step
Epoch 4/100
469/469 - 2s - loss: 2.0011 - sparse_categorical_accuracy: 0.2094 - val_loss: 1.9966 - val_sparse_categorical_accuracy: 0.2126 - 2s/epoch - 4ms/step
Epoch 5/100
469/469 - 2s - loss: 1.9753 - sparse_categorical_accuracy: 0.2210 - val_loss: 1.9698 - val_sparse_categorical_accuracy: 0.2269 - 2s/epoch - 4ms/step
Epoch 6/100
469/469 - 1s - loss: 1.9513 - sparse_categorical_accuracy: 0.2305 - val_loss: 1.9511 - val_sparse_categorical_accuracy: 0.2342 - 1s/epoch - 3ms/step
Epoch 7/100
469/469 - 1s - loss: 1.9056 - sparse_categorical_accuracy: 0.2498 - val_loss: 1.8883 - val_sparse_categorical_accuracy: 0.2637 - 961ms/epoch - 2ms/step
Epoch 8/100
469/469 - 1s - loss: 1.7445 - sparse_categorical_accuracy: 0.3287 - val_loss: 1.5570 - val_sparse_categorical_accuracy: 0.4081 - 945ms/epoch - 2ms/step
Epoch 9/100
469/469 - 1s - loss: 1.4151 - sparse_categorical_accuracy: 0.4676 - val_loss: 1.2790 - val_sparse_categorical_accuracy: 0.5304 - 929ms/epoch - 2ms/step
Epoch 10/100
469/469 - 1s - loss: 1.1866 - sparse_categorical_accuracy: 0.5476 - val_loss: 1.1090 - val_sparse_categorical_accuracy: 0.5745 - 907ms/epoch - 2ms/step
Epoch 11/100
469/469 - 1s - loss: 1.0255 - sparse_categorical_accuracy: 0.6120 - val_loss: 0.9805 - val_sparse_categorical_accuracy: 0.6349 - 942ms/epoch - 2ms/step
```

Epoch 12/100  
469/469 - 1s - loss: 0.9026 - sparse\_categorical\_accuracy: 0.6537 - val\_loss: 0.8674 - val\_sparse\_categorical\_accuracy: 0.6579 - 893ms/epoch - 2ms/step

Epoch 13/100  
469/469 - 1s - loss: 0.8202 - sparse\_categorical\_accuracy: 0.7118 - val\_loss: 0.7815 - val\_sparse\_categorical\_accuracy: 0.7533 - 952ms/epoch - 2ms/step

Epoch 14/100  
469/469 - 1s - loss: 0.7487 - sparse\_categorical\_accuracy: 0.7584 - val\_loss: 0.7496 - val\_sparse\_categorical\_accuracy: 0.7687 - 967ms/epoch - 2ms/step

Epoch 15/100  
469/469 - 1s - loss: 0.6008 - sparse\_categorical\_accuracy: 0.8244 - val\_loss: 0.5650 - val\_sparse\_categorical\_accuracy: 0.8399 - 945ms/epoch - 2ms/step

Epoch 16/100  
469/469 - 1s - loss: 0.5404 - sparse\_categorical\_accuracy: 0.8450 - val\_loss: 0.5424 - val\_sparse\_categorical\_accuracy: 0.8508 - 912ms/epoch - 2ms/step

Epoch 17/100  
469/469 - 1s - loss: 0.5157 - sparse\_categorical\_accuracy: 0.8499 - val\_loss: 0.5190 - val\_sparse\_categorical\_accuracy: 0.8502 - 1s/epoch - 2ms/step

Epoch 18/100  
469/469 - 1s - loss: 0.4993 - sparse\_categorical\_accuracy: 0.8528 - val\_loss: 0.5070 - val\_sparse\_categorical\_accuracy: 0.8569 - 924ms/epoch - 2ms/step

Epoch 19/100  
469/469 - 1s - loss: 0.4791 - sparse\_categorical\_accuracy: 0.8581 - val\_loss: 0.4912 - val\_sparse\_categorical\_accuracy: 0.8545 - 915ms/epoch - 2ms/step

Epoch 20/100  
469/469 - 1s - loss: 0.4668 - sparse\_categorical\_accuracy: 0.8621 - val\_loss: 0.4812 - val\_sparse\_categorical\_accuracy: 0.8595 - 982ms/epoch - 2ms/step

Epoch 21/100  
469/469 - 1s - loss: 0.4516 - sparse\_categorical\_accuracy: 0.8670 - val\_loss: 0.5094 - val\_sparse\_categorical\_accuracy: 0.8524 - 923ms/epoch - 2ms/step

Epoch 22/100  
469/469 - 1s - loss: 0.4410 - sparse\_categorical\_accuracy: 0.8710 - val\_loss: 0.4602 - val\_sparse\_categorical\_accuracy: 0.8704 - 911ms/epoch - 2ms/step

Epoch 23/100  
469/469 - 1s - loss: 0.4346 - sparse\_categorical\_accuracy: 0.8749 - val\_loss: 0.4755 - val\_sparse\_categorical\_accuracy: 0.8687 - 912ms/epoch - 2ms/step

Epoch 24/100  
469/469 - 1s - loss: 0.4209 - sparse\_categorical\_accuracy: 0.8774 - val\_loss: 0.4358 - val\_sparse\_categorical\_accuracy: 0.8790 - 980ms/epoch - 2ms/step

Epoch 25/100  
469/469 - 1s - loss: 0.4155 - sparse\_categorical\_accuracy: 0.8796 - val\_loss: 0.4383 - val\_sparse\_categorical\_accuracy: 0.8751 - 897ms/epoch - 2ms/step

Epoch 26/100  
469/469 - 1s - loss: 0.4079 - sparse\_categorical\_accuracy: 0.8808 - val\_loss: 0.4496 - val\_sparse\_categorical\_accuracy: 0.8756 - 948ms/epoch - 2ms/step

Epoch 27/100  
469/469 - 1s - loss: 0.4049 - sparse\_categorical\_accuracy: 0.8815 - val\_loss: 0.4453 - val\_sparse\_categorical\_accuracy: 0.8780 - 976ms/epoch - 2ms/step

Epoch 28/100  
469/469 - 1s - loss: 0.4012 - sparse\_categorical\_accuracy: 0.8820 - val\_loss: 0.4422 - val\_sparse\_categorical\_accuracy: 0.8772 - 931ms/epoch - 2ms/step

Epoch 29/100  
469/469 - 1s - loss: 0.4027 - sparse\_categorical\_accuracy: 0.8819 - val\_loss: 0.4430 - val\_sparse\_categorical\_accuracy: 0.8766 - 933ms/epoch - 2ms/step

Epoch 30/100  
469/469 - 1s - loss: 0.3983 - sparse\_categorical\_accuracy: 0.8821 - val\_loss: 0.4251 - val\_sparse\_categorical\_accuracy: 0.8802 - 1s/epoch - 2ms/step

Epoch 31/100  
469/469 - 1s - loss: 0.3925 - sparse\_categorical\_accuracy: 0.8860 - val\_loss: 0.4491 - val\_sparse\_categorical\_accuracy: 0.8725 - 906ms/epoch - 2ms/step

Epoch 32/100  
469/469 - 1s - loss: 0.3920 - sparse\_categorical\_accuracy: 0.8857 - val\_loss: 0.4222 - val\_sparse\_categorical\_accuracy: 0.8826 - 954ms/epoch - 2ms/step

Epoch 33/100  
469/469 - 1s - loss: 0.3893 - sparse\_categorical\_accuracy: 0.8865 - val\_loss: 0.4262 - val\_sparse\_categorical\_accuracy: 0.8821 - 1s/epoch - 2ms/step

Epoch 34/100  
469/469 - 1s - loss: 0.3885 - sparse\_categorical\_accuracy: 0.8867 - val\_loss: 0.4428 - val\_sparse\_categorical\_accuracy: 0.8755 - 967ms/epoch - 2ms/step

Epoch 35/100  
469/469 - 1s - loss: 0.3839 - sparse\_categorical\_accuracy: 0.8868 - val\_loss: 0.4421 - val\_sparse\_categorical\_accuracy: 0.8770 - 966ms/epoch - 2ms/step

Epoch 36/100  
469/469 - 1s - loss: 0.3832 - sparse\_categorical\_accuracy: 0.8873 - val\_loss: 0.4250 - val\_sparse\_categorical\_accuracy: 0.8770 - 1s/epoch - 2ms/step

Epoch 37/100  
469/469 - 1s - loss: 0.3785 - sparse\_categorical\_accuracy: 0.8894 - val\_loss: 0.4270 - val\_sparse\_categorical\_accuracy: 0.8790 - 948ms/epoch - 2ms/step

Epoch 38/100  
469/469 - 1s - loss: 0.3787 - sparse\_categorical\_accuracy: 0.8888 - val\_loss: 0.4419 - val\_sparse\_categorical\_accuracy: 0.8768 - 916ms/epoch - 2ms/step

Epoch 39/100  
469/469 - 1s - loss: 0.3778 - sparse\_categorical\_accuracy: 0.8886 - val\_loss: 0.4331 - val\_sparse\_categorical\_accuracy: 0.8886 - 948ms/epoch - 2ms/step

tegorical\_accuracy: 0.8791 - 908ms/epoch - 2ms/step  
Epoch 40/100  
469/469 - 1s - loss: 0.3753 - sparse\_categorical\_accuracy: 0.8894 - val\_loss: 0.4236 - val\_sparse\_ca  
tegorical\_accuracy: 0.8792 - 959ms/epoch - 2ms/step  
Epoch 41/100  
469/469 - 1s - loss: 0.3711 - sparse\_categorical\_accuracy: 0.8902 - val\_loss: 0.4492 - val\_sparse\_ca  
tegorical\_accuracy: 0.8696 - 947ms/epoch - 2ms/step  
Epoch 42/100  
469/469 - 1s - loss: 0.3748 - sparse\_categorical\_accuracy: 0.8905 - val\_loss: 0.4278 - val\_sparse\_ca  
tegorical\_accuracy: 0.8807 - 966ms/epoch - 2ms/step  
Epoch 43/100  
469/469 - 1s - loss: 0.3717 - sparse\_categorical\_accuracy: 0.8914 - val\_loss: 0.4207 - val\_sparse\_ca  
tegorical\_accuracy: 0.8830 - 964ms/epoch - 2ms/step  
Epoch 44/100  
469/469 - 1s - loss: 0.3707 - sparse\_categorical\_accuracy: 0.8907 - val\_loss: 0.4355 - val\_sparse\_ca  
tegorical\_accuracy: 0.8793 - 982ms/epoch - 2ms/step  
Epoch 45/100  
469/469 - 1s - loss: 0.3662 - sparse\_categorical\_accuracy: 0.8928 - val\_loss: 0.4296 - val\_sparse\_ca  
tegorical\_accuracy: 0.8771 - 945ms/epoch - 2ms/step  
Epoch 46/100  
469/469 - 1s - loss: 0.3669 - sparse\_categorical\_accuracy: 0.8920 - val\_loss: 0.4294 - val\_sparse\_ca  
tegorical\_accuracy: 0.8789 - 994ms/epoch - 2ms/step  
Epoch 47/100  
469/469 - 1s - loss: 0.3666 - sparse\_categorical\_accuracy: 0.8911 - val\_loss: 0.4231 - val\_sparse\_ca  
tegorical\_accuracy: 0.8836 - 971ms/epoch - 2ms/step  
Epoch 48/100  
469/469 - 1s - loss: 0.3611 - sparse\_categorical\_accuracy: 0.8937 - val\_loss: 0.4325 - val\_sparse\_ca  
tegorical\_accuracy: 0.8741 - 981ms/epoch - 2ms/step  
Epoch 49/100  
469/469 - 1s - loss: 0.3565 - sparse\_categorical\_accuracy: 0.8954 - val\_loss: 0.4148 - val\_sparse\_ca  
tegorical\_accuracy: 0.8866 - 905ms/epoch - 2ms/step  
Epoch 50/100  
469/469 - 1s - loss: 0.3567 - sparse\_categorical\_accuracy: 0.8949 - val\_loss: 0.4275 - val\_sparse\_ca  
tegorical\_accuracy: 0.8801 - 964ms/epoch - 2ms/step  
Epoch 51/100  
469/469 - 1s - loss: 0.3575 - sparse\_categorical\_accuracy: 0.8953 - val\_loss: 0.4151 - val\_sparse\_ca  
tegorical\_accuracy: 0.8864 - 941ms/epoch - 2ms/step  
Epoch 52/100  
469/469 - 1s - loss: 0.3520 - sparse\_categorical\_accuracy: 0.8964 - val\_loss: 0.4027 - val\_sparse\_ca  
tegorical\_accuracy: 0.8854 - 1s/epoch - 2ms/step  
Epoch 53/100  
469/469 - 1s - loss: 0.3511 - sparse\_categorical\_accuracy: 0.8961 - val\_loss: 0.4273 - val\_sparse\_ca  
tegorical\_accuracy: 0.8841 - 963ms/epoch - 2ms/step  
Epoch 54/100  
469/469 - 1s - loss: 0.3512 - sparse\_categorical\_accuracy: 0.8964 - val\_loss: 0.4081 - val\_sparse\_ca  
tegorical\_accuracy: 0.8842 - 1s/epoch - 2ms/step  
Epoch 55/100  
469/469 - 1s - loss: 0.3498 - sparse\_categorical\_accuracy: 0.8962 - val\_loss: 0.4050 - val\_sparse\_ca  
tegorical\_accuracy: 0.8874 - 948ms/epoch - 2ms/step  
Epoch 56/100  
469/469 - 1s - loss: 0.3469 - sparse\_categorical\_accuracy: 0.8984 - val\_loss: 0.4187 - val\_sparse\_ca  
tegorical\_accuracy: 0.8874 - 968ms/epoch - 2ms/step  
Epoch 57/100  
469/469 - 1s - loss: 0.3465 - sparse\_categorical\_accuracy: 0.8981 - val\_loss: 0.4075 - val\_sparse\_ca  
tegorical\_accuracy: 0.8838 - 910ms/epoch - 2ms/step  
Epoch 58/100  
469/469 - 1s - loss: 0.3458 - sparse\_categorical\_accuracy: 0.8972 - val\_loss: 0.4048 - val\_sparse\_ca  
tegorical\_accuracy: 0.8881 - 958ms/epoch - 2ms/step  
Epoch 59/100  
469/469 - 1s - loss: 0.3386 - sparse\_categorical\_accuracy: 0.9001 - val\_loss: 0.3930 - val\_sparse\_ca  
tegorical\_accuracy: 0.8902 - 957ms/epoch - 2ms/step  
Epoch 60/100  
469/469 - 1s - loss: 0.3370 - sparse\_categorical\_accuracy: 0.9006 - val\_loss: 0.3987 - val\_sparse\_ca  
tegorical\_accuracy: 0.8885 - 958ms/epoch - 2ms/step  
Epoch 61/100  
469/469 - 1s - loss: 0.3374 - sparse\_categorical\_accuracy: 0.9016 - val\_loss: 0.3768 - val\_sparse\_ca  
tegorical\_accuracy: 0.8923 - 919ms/epoch - 2ms/step  
Epoch 62/100  
469/469 - 1s - loss: 0.3325 - sparse\_categorical\_accuracy: 0.9036 - val\_loss: 0.3728 - val\_sparse\_ca  
tegorical\_accuracy: 0.8974 - 956ms/epoch - 2ms/step  
Epoch 63/100  
469/469 - 1s - loss: 0.3297 - sparse\_categorical\_accuracy: 0.9050 - val\_loss: 0.3730 - val\_sparse\_ca  
tegorical\_accuracy: 0.8988 - 944ms/epoch - 2ms/step  
Epoch 64/100  
469/469 - 1s - loss: 0.3243 - sparse\_categorical\_accuracy: 0.9073 - val\_loss: 0.3828 - val\_sparse\_ca  
tegorical\_accuracy: 0.8968 - 997ms/epoch - 2ms/step  
Epoch 65/100  
469/469 - 1s - loss: 0.3262 - sparse\_categorical\_accuracy: 0.9068 - val\_loss: 0.3733 - val\_sparse\_ca  
tegorical\_accuracy: 0.8990 - 918ms/epoch - 2ms/step  
Epoch 66/100  
469/469 - 1s - loss: 0.3203 - sparse\_categorical\_accuracy: 0.9089 - val\_loss: 0.3668 - val\_sparse\_ca  
tegorical\_accuracy: 0.9012 - 908ms/epoch - 2ms/step  
Epoch 67/100

469/469 - 1s - loss: 0.3157 - sparse\_categorical\_accuracy: 0.9098 - val\_loss: 0.3612 - val\_sparse\_categorical\_accuracy: 0.8998 - 957ms/epoch - 2ms/step  
Epoch 68/100  
469/469 - 1s - loss: 0.3102 - sparse\_categorical\_accuracy: 0.9126 - val\_loss: 0.3753 - val\_sparse\_categorical\_accuracy: 0.8986 - 924ms/epoch - 2ms/step  
Epoch 69/100  
469/469 - 1s - loss: 0.3058 - sparse\_categorical\_accuracy: 0.9133 - val\_loss: 0.3451 - val\_sparse\_categorical\_accuracy: 0.9064 - 937ms/epoch - 2ms/step  
Epoch 70/100  
469/469 - 1s - loss: 0.3065 - sparse\_categorical\_accuracy: 0.9140 - val\_loss: 0.3536 - val\_sparse\_categorical\_accuracy: 0.9036 - 964ms/epoch - 2ms/step  
Epoch 71/100  
469/469 - 1s - loss: 0.3016 - sparse\_categorical\_accuracy: 0.9154 - val\_loss: 0.3562 - val\_sparse\_categorical\_accuracy: 0.9063 - 913ms/epoch - 2ms/step  
Epoch 72/100  
469/469 - 1s - loss: 0.3024 - sparse\_categorical\_accuracy: 0.9148 - val\_loss: 0.3446 - val\_sparse\_categorical\_accuracy: 0.9094 - 915ms/epoch - 2ms/step  
Epoch 73/100  
469/469 - 1s - loss: 0.2952 - sparse\_categorical\_accuracy: 0.9174 - val\_loss: 0.3640 - val\_sparse\_categorical\_accuracy: 0.9069 - 947ms/epoch - 2ms/step  
Epoch 74/100  
469/469 - 1s - loss: 0.2949 - sparse\_categorical\_accuracy: 0.9180 - val\_loss: 0.3362 - val\_sparse\_categorical\_accuracy: 0.9103 - 915ms/epoch - 2ms/step  
Epoch 75/100  
469/469 - 1s - loss: 0.2959 - sparse\_categorical\_accuracy: 0.9165 - val\_loss: 0.3396 - val\_sparse\_categorical\_accuracy: 0.9111 - 961ms/epoch - 2ms/step  
Epoch 76/100  
469/469 - 1s - loss: 0.2921 - sparse\_categorical\_accuracy: 0.9180 - val\_loss: 0.3464 - val\_sparse\_categorical\_accuracy: 0.9108 - 934ms/epoch - 2ms/step  
Epoch 77/100  
469/469 - 1s - loss: 0.2910 - sparse\_categorical\_accuracy: 0.9183 - val\_loss: 0.3488 - val\_sparse\_categorical\_accuracy: 0.9074 - 963ms/epoch - 2ms/step  
Epoch 78/100  
469/469 - 1s - loss: 0.2879 - sparse\_categorical\_accuracy: 0.9197 - val\_loss: 0.3381 - val\_sparse\_categorical\_accuracy: 0.9133 - 962ms/epoch - 2ms/step  
Epoch 79/100  
469/469 - 1s - loss: 0.2866 - sparse\_categorical\_accuracy: 0.9196 - val\_loss: 0.3448 - val\_sparse\_categorical\_accuracy: 0.9115 - 964ms/epoch - 2ms/step  
Epoch 80/100  
469/469 - 1s - loss: 0.2863 - sparse\_categorical\_accuracy: 0.9179 - val\_loss: 0.3301 - val\_sparse\_categorical\_accuracy: 0.9127 - 950ms/epoch - 2ms/step  
Epoch 81/100  
469/469 - 1s - loss: 0.2853 - sparse\_categorical\_accuracy: 0.9196 - val\_loss: 0.3368 - val\_sparse\_categorical\_accuracy: 0.9135 - 960ms/epoch - 2ms/step  
Epoch 82/100  
469/469 - 1s - loss: 0.2849 - sparse\_categorical\_accuracy: 0.9203 - val\_loss: 0.3482 - val\_sparse\_categorical\_accuracy: 0.9080 - 967ms/epoch - 2ms/step  
Epoch 83/100  
469/469 - 1s - loss: 0.2820 - sparse\_categorical\_accuracy: 0.9206 - val\_loss: 0.3386 - val\_sparse\_categorical\_accuracy: 0.9114 - 1s/epoch - 3ms/step  
Epoch 84/100  
469/469 - 1s - loss: 0.2830 - sparse\_categorical\_accuracy: 0.9205 - val\_loss: 0.3407 - val\_sparse\_categorical\_accuracy: 0.9101 - 1s/epoch - 3ms/step  
Epoch 85/100  
469/469 - 1s - loss: 0.2815 - sparse\_categorical\_accuracy: 0.9213 - val\_loss: 0.3372 - val\_sparse\_categorical\_accuracy: 0.9114 - 1s/epoch - 3ms/step  
Epoch 86/100  
469/469 - 1s - loss: 0.2799 - sparse\_categorical\_accuracy: 0.9213 - val\_loss: 0.3347 - val\_sparse\_categorical\_accuracy: 0.9108 - 909ms/epoch - 2ms/step  
Epoch 87/100  
469/469 - 1s - loss: 0.2772 - sparse\_categorical\_accuracy: 0.9227 - val\_loss: 0.3513 - val\_sparse\_categorical\_accuracy: 0.9081 - 993ms/epoch - 2ms/step  
Epoch 88/100  
469/469 - 1s - loss: 0.2796 - sparse\_categorical\_accuracy: 0.9206 - val\_loss: 0.3430 - val\_sparse\_categorical\_accuracy: 0.9126 - 959ms/epoch - 2ms/step  
Epoch 89/100  
469/469 - 1s - loss: 0.2771 - sparse\_categorical\_accuracy: 0.9214 - val\_loss: 0.3357 - val\_sparse\_categorical\_accuracy: 0.9148 - 918ms/epoch - 2ms/step  
Epoch 90/100  
469/469 - 1s - loss: 0.2778 - sparse\_categorical\_accuracy: 0.9216 - val\_loss: 0.3334 - val\_sparse\_categorical\_accuracy: 0.9153 - 975ms/epoch - 2ms/step  
Epoch 91/100  
469/469 - 1s - loss: 0.2750 - sparse\_categorical\_accuracy: 0.9217 - val\_loss: 0.3390 - val\_sparse\_categorical\_accuracy: 0.9092 - 912ms/epoch - 2ms/step  
Epoch 92/100  
469/469 - 1s - loss: 0.2755 - sparse\_categorical\_accuracy: 0.9220 - val\_loss: 0.3334 - val\_sparse\_categorical\_accuracy: 0.9149 - 911ms/epoch - 2ms/step  
Epoch 93/100  
469/469 - 1s - loss: 0.2728 - sparse\_categorical\_accuracy: 0.9234 - val\_loss: 0.3379 - val\_sparse\_categorical\_accuracy: 0.9114 - 907ms/epoch - 2ms/step  
Epoch 94/100  
469/469 - 1s - loss: 0.2720 - sparse\_categorical\_accuracy: 0.9224 - val\_loss: 0.3435 - val\_sparse\_categorical\_accuracy: 0.9128 - 972ms/epoch - 2ms/step

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Epoch 95/100
469/469 - 1s - loss: 0.2723 - sparse_categorical_accuracy: 0.9232 - val_loss: 0.3455 - val_sparse_categorical_accuracy: 0.9102 - 918ms/epoch - 2ms/step
Epoch 96/100
469/469 - 1s - loss: 0.2726 - sparse_categorical_accuracy: 0.9227 - val_loss: 0.3328 - val_sparse_categorical_accuracy: 0.9129 - 952ms/epoch - 2ms/step
Epoch 97/100
469/469 - 1s - loss: 0.2732 - sparse_categorical_accuracy: 0.9226 - val_loss: 0.3618 - val_sparse_categorical_accuracy: 0.9029 - 920ms/epoch - 2ms/step
Epoch 98/100
469/469 - 1s - loss: 0.2701 - sparse_categorical_accuracy: 0.9239 - val_loss: 0.3331 - val_sparse_categorical_accuracy: 0.9126 - 971ms/epoch - 2ms/step
Epoch 99/100
469/469 - 1s - loss: 0.2706 - sparse_categorical_accuracy: 0.9233 - val_loss: 0.3481 - val_sparse_categorical_accuracy: 0.9084 - 928ms/epoch - 2ms/step
Epoch 100/100
469/469 - 1s - loss: 0.2690 - sparse_categorical_accuracy: 0.9238 - val_loss: 0.3364 - val_sparse_categorical_accuracy: 0.9144 - 914ms/epoch - 2ms/step
```

In [6]:

```
# Baseline model evaluation
model.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 0s - loss: 0.3364 - sparse_categorical_accuracy: 0.9144 - 348ms/epoch - 1ms/step
```

Out[6]:

```
[0.33644601702690125, 0.9143999814987183]
```

In [7]:

```
import keras
from tensorflow.keras.layers import Layer
import keras.backend as K
import tensorflow as tf
from keras.datasets import cifar10
from keras.models import Model
from keras.layers import Conv2D, MaxPool2D, \
    Dropout, Dense, Input, concatenate, \
    GlobalAveragePooling2D, AveragePooling2D, \
    Flatten

import cv2
import numpy as np
from keras.datasets import cifar10
from keras import backend as K
#from keras.utils import np_utils
kernel_init = keras.initializers.glorot_uniform()
bias_init = keras.initializers.Constant(value=0.2)
```

In [8]:

```
# Inception V3 Module
def inception_module(x,
                    filters_1x1,
                    filters_3x3_reduce,
                    filters_3x3,
                    filters_5x5_reduce,
                    filters_5x5,
                    filters_pool_proj,
                    name=None):

    conv_1x1 = Conv2D(filters_1x1, (1, 1), padding='same', activation='relu', kernel_initializer=kernel_init, bias_initializer=bias_init)(x)

    conv_3x3_reduce = Conv2D(filters_3x3_reduce, (1, 1), padding='same', activation='relu', kernel_initializer=kernel_init, bias_initializer=bias_init)(x)
    conv_3x3 = Conv2D(filters_3x3, (3, 3), padding='same', activation='relu', kernel_initializer=kernel_init, bias_initializer=bias_init)(conv_3x3_reduce)

    conv_5x5_reduce = Conv2D(filters_5x5_reduce, (1, 1), padding='same', activation='relu', kernel_initializer=kernel_init, bias_initializer=bias_init)(x)
    conv_5x5 = Conv2D(filters_5x5, (5, 5), padding='same', activation='relu', kernel_initializer=kernel_init, bias_initializer=bias_init)(conv_5x5_reduce)

    pool_proj = MaxPool2D((3, 3), strides=(1, 1), padding='same')(x)
    pool_proj = Conv2D(filters_pool_proj, (1, 1), padding='same', activation='relu', kernel_initializer=kernel_init, bias_initializer=bias_init)(pool_proj)

    output = concatenate([conv_1x1, conv_3x3, conv_5x5, pool_proj], axis=1, name=name)

    return output
```

The baseline model with `kernel_initializer='glorot_uniform'`, `bias_initializer='zeros'`

## Try different models

**Model1:** adam optimizer with learning rate= $e^{-3}$ , random\_uniform initializer, dropout regularization with rate=0.1.

In [9]:

```
input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                      filters_1x1=1,
                      filters_3x3_reduce=1,
                      filters_3x3=1,
                      filters_5x5_reduce=1,
                      filters_5x5=1,
                      filters_pool_proj=1,
                      name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.1)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_uniform')(x)
model1 = Model(input_layer, x, name='inception_v1')
```

In [10]:

```
model1.compile(optimizer=tf.keras.optimizers.Adam(0.001),
               loss='sparse_categorical_crossentropy',
               metrics=['sparse_categorical_accuracy'])
```

In [11]:

```
history1 = model1.fit(x_train, y_train,
                      batch_size=128,
                      epochs=100,
                      validation_data=(x_test, y_test),
                      verbose=2)
```

```
Epoch 1/100
469/469 - 53s - loss: 0.9712 - sparse_categorical_accuracy: 0.7746 - val_loss: 0.3838 - val_sparse_c
ategorical_accuracy: 0.8945 - 53s/epoch - 113ms/step
Epoch 2/100
469/469 - 52s - loss: 0.4190 - sparse_categorical_accuracy: 0.8711 - val_loss: 0.3234 - val_sparse_c
ategorical_accuracy: 0.8981 - 52s/epoch - 111ms/step
Epoch 3/100
469/469 - 52s - loss: 0.3716 - sparse_categorical_accuracy: 0.8818 - val_loss: 0.2864 - val_sparse_c
ategorical_accuracy: 0.9110 - 52s/epoch - 111ms/step
Epoch 4/100
469/469 - 52s - loss: 0.3517 - sparse_categorical_accuracy: 0.8872 - val_loss: 0.2683 - val_sparse_c
ategorical_accuracy: 0.9155 - 52s/epoch - 111ms/step
Epoch 5/100
469/469 - 52s - loss: 0.3205 - sparse_categorical_accuracy: 0.8969 - val_loss: 0.2441 - val_sparse_c
ategorical_accuracy: 0.9243 - 52s/epoch - 111ms/step
Epoch 6/100
469/469 - 53s - loss: 0.2871 - sparse_categorical_accuracy: 0.9079 - val_loss: 0.2521 - val_sparse_c
ategorical_accuracy: 0.9205 - 53s/epoch - 112ms/step
Epoch 7/100
469/469 - 52s - loss: 0.2627 - sparse_categorical_accuracy: 0.9172 - val_loss: 0.2014 - val_sparse_c
ategorical_accuracy: 0.9372 - 52s/epoch - 111ms/step
Epoch 8/100
469/469 - 52s - loss: 0.2454 - sparse_categorical_accuracy: 0.9205 - val_loss: 0.1922 - val_sparse_c
ategorical_accuracy: 0.9413 - 52s/epoch - 111ms/step
Epoch 9/100
469/469 - 52s - loss: 0.2313 - sparse_categorical_accuracy: 0.9273 - val_loss: 0.1949 - val_sparse_c
ategorical_accuracy: 0.9399 - 52s/epoch - 112ms/step
Epoch 10/100
469/469 - 52s - loss: 0.2192 - sparse_categorical_accuracy: 0.9306 - val_loss: 0.1693 - val_sparse_c
ategorical_accuracy: 0.9475 - 52s/epoch - 111ms/step
Epoch 11/100
469/469 - 52s - loss: 0.2111 - sparse_categorical_accuracy: 0.9334 - val_loss: 0.1765 - val_sparse_c
ategorical_accuracy: 0.9451 - 52s/epoch - 111ms/step
Epoch 12/100
469/469 - 52s - loss: 0.2023 - sparse_categorical_accuracy: 0.9356 - val_loss: 0.1601 - val_sparse_c
ategorical_accuracy: 0.9513 - 52s/epoch - 111ms/step
```

Epoch 13/100  
469/469 - 52s - loss: 0.1945 - sparse\_categorical\_accuracy: 0.9388 - val\_loss: 0.1553 - val\_sparse\_categorical\_accuracy: 0.9521 - 52s/epoch - 111ms/step

Epoch 14/100  
469/469 - 52s - loss: 0.1915 - sparse\_categorical\_accuracy: 0.9390 - val\_loss: 0.1602 - val\_sparse\_categorical\_accuracy: 0.9507 - 52s/epoch - 112ms/step

Epoch 15/100  
469/469 - 52s - loss: 0.1866 - sparse\_categorical\_accuracy: 0.9406 - val\_loss: 0.1400 - val\_sparse\_categorical\_accuracy: 0.9563 - 52s/epoch - 111ms/step

Epoch 16/100  
469/469 - 52s - loss: 0.1826 - sparse\_categorical\_accuracy: 0.9426 - val\_loss: 0.1455 - val\_sparse\_categorical\_accuracy: 0.9539 - 52s/epoch - 112ms/step

Epoch 17/100  
469/469 - 52s - loss: 0.1779 - sparse\_categorical\_accuracy: 0.9431 - val\_loss: 0.1481 - val\_sparse\_categorical\_accuracy: 0.9543 - 52s/epoch - 111ms/step

Epoch 18/100  
469/469 - 52s - loss: 0.1746 - sparse\_categorical\_accuracy: 0.9443 - val\_loss: 0.1395 - val\_sparse\_categorical\_accuracy: 0.9570 - 52s/epoch - 112ms/step

Epoch 19/100  
469/469 - 52s - loss: 0.1723 - sparse\_categorical\_accuracy: 0.9451 - val\_loss: 0.1395 - val\_sparse\_categorical\_accuracy: 0.9564 - 52s/epoch - 112ms/step

Epoch 20/100  
469/469 - 52s - loss: 0.1719 - sparse\_categorical\_accuracy: 0.9464 - val\_loss: 0.1361 - val\_sparse\_categorical\_accuracy: 0.9564 - 52s/epoch - 112ms/step

Epoch 21/100  
469/469 - 53s - loss: 0.1694 - sparse\_categorical\_accuracy: 0.9470 - val\_loss: 0.1392 - val\_sparse\_categorical\_accuracy: 0.9550 - 53s/epoch - 112ms/step

Epoch 22/100  
469/469 - 53s - loss: 0.1662 - sparse\_categorical\_accuracy: 0.9473 - val\_loss: 0.1405 - val\_sparse\_categorical\_accuracy: 0.9564 - 53s/epoch - 113ms/step

Epoch 23/100  
469/469 - 52s - loss: 0.1666 - sparse\_categorical\_accuracy: 0.9463 - val\_loss: 0.1463 - val\_sparse\_categorical\_accuracy: 0.9531 - 52s/epoch - 112ms/step

Epoch 24/100  
469/469 - 53s - loss: 0.1628 - sparse\_categorical\_accuracy: 0.9487 - val\_loss: 0.1349 - val\_sparse\_categorical\_accuracy: 0.9572 - 53s/epoch - 112ms/step

Epoch 25/100  
469/469 - 53s - loss: 0.1632 - sparse\_categorical\_accuracy: 0.9488 - val\_loss: 0.1367 - val\_sparse\_categorical\_accuracy: 0.9563 - 53s/epoch - 112ms/step

Epoch 26/100  
469/469 - 53s - loss: 0.1615 - sparse\_categorical\_accuracy: 0.9499 - val\_loss: 0.1238 - val\_sparse\_categorical\_accuracy: 0.9621 - 53s/epoch - 112ms/step

Epoch 27/100  
469/469 - 53s - loss: 0.1600 - sparse\_categorical\_accuracy: 0.9498 - val\_loss: 0.1305 - val\_sparse\_categorical\_accuracy: 0.9590 - 53s/epoch - 112ms/step

Epoch 28/100  
469/469 - 53s - loss: 0.1564 - sparse\_categorical\_accuracy: 0.9498 - val\_loss: 0.1209 - val\_sparse\_categorical\_accuracy: 0.9599 - 53s/epoch - 113ms/step

Epoch 29/100  
469/469 - 53s - loss: 0.1541 - sparse\_categorical\_accuracy: 0.9515 - val\_loss: 0.1218 - val\_sparse\_categorical\_accuracy: 0.9605 - 53s/epoch - 113ms/step

Epoch 30/100  
469/469 - 53s - loss: 0.1547 - sparse\_categorical\_accuracy: 0.9509 - val\_loss: 0.1379 - val\_sparse\_categorical\_accuracy: 0.9553 - 53s/epoch - 113ms/step

Epoch 31/100  
469/469 - 53s - loss: 0.1524 - sparse\_categorical\_accuracy: 0.9526 - val\_loss: 0.1259 - val\_sparse\_categorical\_accuracy: 0.9600 - 53s/epoch - 113ms/step

Epoch 32/100  
469/469 - 53s - loss: 0.1500 - sparse\_categorical\_accuracy: 0.9525 - val\_loss: 0.1164 - val\_sparse\_categorical\_accuracy: 0.9629 - 53s/epoch - 113ms/step

Epoch 33/100  
469/469 - 53s - loss: 0.1491 - sparse\_categorical\_accuracy: 0.9530 - val\_loss: 0.1124 - val\_sparse\_categorical\_accuracy: 0.9629 - 53s/epoch - 112ms/step

Epoch 34/100  
469/469 - 53s - loss: 0.1481 - sparse\_categorical\_accuracy: 0.9534 - val\_loss: 0.1442 - val\_sparse\_categorical\_accuracy: 0.9537 - 53s/epoch - 112ms/step

Epoch 35/100  
469/469 - 53s - loss: 0.1468 - sparse\_categorical\_accuracy: 0.9538 - val\_loss: 0.1218 - val\_sparse\_categorical\_accuracy: 0.9622 - 53s/epoch - 112ms/step

Epoch 36/100  
469/469 - 53s - loss: 0.1439 - sparse\_categorical\_accuracy: 0.9546 - val\_loss: 0.1135 - val\_sparse\_categorical\_accuracy: 0.9630 - 53s/epoch - 112ms/step

Epoch 37/100  
469/469 - 52s - loss: 0.1438 - sparse\_categorical\_accuracy: 0.9552 - val\_loss: 0.1159 - val\_sparse\_categorical\_accuracy: 0.9622 - 52s/epoch - 112ms/step

Epoch 38/100  
469/469 - 52s - loss: 0.1398 - sparse\_categorical\_accuracy: 0.9557 - val\_loss: 0.1105 - val\_sparse\_categorical\_accuracy: 0.9642 - 52s/epoch - 111ms/step

Epoch 39/100  
469/469 - 52s - loss: 0.1407 - sparse\_categorical\_accuracy: 0.9559 - val\_loss: 0.1183 - val\_sparse\_categorical\_accuracy: 0.9604 - 52s/epoch - 111ms/step

Epoch 40/100  
469/469 - 52s - loss: 0.1395 - sparse\_categorical\_accuracy: 0.9561 - val\_loss: 0.1101 - val\_sparse\_categorical\_accuracy: 0.9604 - 52s/epoch - 111ms/step

ategorical\_accuracy: 0.9632 - 52s/epoch - 112ms/step  
Epoch 41/100  
469/469 - 52s - loss: 0.1387 - sparse\_categorical\_accuracy: 0.9557 - val\_loss: 0.1086 - val\_sparse\_c  
ategorical\_accuracy: 0.9652 - 52s/epoch - 111ms/step  
Epoch 42/100  
469/469 - 52s - loss: 0.1360 - sparse\_categorical\_accuracy: 0.9561 - val\_loss: 0.1127 - val\_sparse\_c  
ategorical\_accuracy: 0.9636 - 52s/epoch - 112ms/step  
Epoch 43/100  
469/469 - 52s - loss: 0.1353 - sparse\_categorical\_accuracy: 0.9573 - val\_loss: 0.1160 - val\_sparse\_c  
ategorical\_accuracy: 0.9642 - 52s/epoch - 112ms/step  
Epoch 44/100  
469/469 - 52s - loss: 0.1346 - sparse\_categorical\_accuracy: 0.9577 - val\_loss: 0.1196 - val\_sparse\_c  
ategorical\_accuracy: 0.9626 - 52s/epoch - 112ms/step  
Epoch 45/100  
469/469 - 52s - loss: 0.1336 - sparse\_categorical\_accuracy: 0.9575 - val\_loss: 0.1001 - val\_sparse\_c  
ategorical\_accuracy: 0.9681 - 52s/epoch - 111ms/step  
Epoch 46/100  
469/469 - 52s - loss: 0.1299 - sparse\_categorical\_accuracy: 0.9586 - val\_loss: 0.1021 - val\_sparse\_c  
ategorical\_accuracy: 0.9665 - 52s/epoch - 112ms/step  
Epoch 47/100  
469/469 - 52s - loss: 0.1307 - sparse\_categorical\_accuracy: 0.9593 - val\_loss: 0.1149 - val\_sparse\_c  
ategorical\_accuracy: 0.9640 - 52s/epoch - 112ms/step  
Epoch 48/100  
469/469 - 52s - loss: 0.1293 - sparse\_categorical\_accuracy: 0.9592 - val\_loss: 0.1043 - val\_sparse\_c  
ategorical\_accuracy: 0.9671 - 52s/epoch - 111ms/step  
Epoch 49/100  
469/469 - 52s - loss: 0.1308 - sparse\_categorical\_accuracy: 0.9583 - val\_loss: 0.1057 - val\_sparse\_c  
ategorical\_accuracy: 0.9648 - 52s/epoch - 111ms/step  
Epoch 50/100  
469/469 - 52s - loss: 0.1291 - sparse\_categorical\_accuracy: 0.9595 - val\_loss: 0.1050 - val\_sparse\_c  
ategorical\_accuracy: 0.9667 - 52s/epoch - 111ms/step  
Epoch 51/100  
469/469 - 52s - loss: 0.1272 - sparse\_categorical\_accuracy: 0.9607 - val\_loss: 0.1109 - val\_sparse\_c  
ategorical\_accuracy: 0.9649 - 52s/epoch - 111ms/step  
Epoch 52/100  
469/469 - 52s - loss: 0.1289 - sparse\_categorical\_accuracy: 0.9596 - val\_loss: 0.1020 - val\_sparse\_c  
ategorical\_accuracy: 0.9682 - 52s/epoch - 111ms/step  
Epoch 53/100  
469/469 - 52s - loss: 0.1289 - sparse\_categorical\_accuracy: 0.9598 - val\_loss: 0.1083 - val\_sparse\_c  
ategorical\_accuracy: 0.9649 - 52s/epoch - 111ms/step  
Epoch 54/100  
469/469 - 52s - loss: 0.1290 - sparse\_categorical\_accuracy: 0.9592 - val\_loss: 0.1026 - val\_sparse\_c  
ategorical\_accuracy: 0.9686 - 52s/epoch - 111ms/step  
Epoch 55/100  
469/469 - 52s - loss: 0.1274 - sparse\_categorical\_accuracy: 0.9597 - val\_loss: 0.1065 - val\_sparse\_c  
ategorical\_accuracy: 0.9662 - 52s/epoch - 111ms/step  
Epoch 56/100  
469/469 - 52s - loss: 0.1278 - sparse\_categorical\_accuracy: 0.9591 - val\_loss: 0.1008 - val\_sparse\_c  
ategorical\_accuracy: 0.9695 - 52s/epoch - 111ms/step  
Epoch 57/100  
469/469 - 52s - loss: 0.1259 - sparse\_categorical\_accuracy: 0.9604 - val\_loss: 0.1035 - val\_sparse\_c  
ategorical\_accuracy: 0.9663 - 52s/epoch - 111ms/step  
Epoch 58/100  
469/469 - 52s - loss: 0.1249 - sparse\_categorical\_accuracy: 0.9602 - val\_loss: 0.1070 - val\_sparse\_c  
ategorical\_accuracy: 0.9652 - 52s/epoch - 112ms/step  
Epoch 59/100  
469/469 - 52s - loss: 0.1244 - sparse\_categorical\_accuracy: 0.9596 - val\_loss: 0.1032 - val\_sparse\_c  
ategorical\_accuracy: 0.9670 - 52s/epoch - 111ms/step  
Epoch 60/100  
469/469 - 52s - loss: 0.1235 - sparse\_categorical\_accuracy: 0.9611 - val\_loss: 0.1003 - val\_sparse\_c  
ategorical\_accuracy: 0.9684 - 52s/epoch - 111ms/step  
Epoch 61/100  
469/469 - 52s - loss: 0.1207 - sparse\_categorical\_accuracy: 0.9617 - val\_loss: 0.1016 - val\_sparse\_c  
ategorical\_accuracy: 0.9674 - 52s/epoch - 111ms/step  
Epoch 62/100  
469/469 - 52s - loss: 0.1187 - sparse\_categorical\_accuracy: 0.9625 - val\_loss: 0.1004 - val\_sparse\_c  
ategorical\_accuracy: 0.9677 - 52s/epoch - 111ms/step  
Epoch 63/100  
469/469 - 52s - loss: 0.1216 - sparse\_categorical\_accuracy: 0.9613 - val\_loss: 0.1086 - val\_sparse\_c  
ategorical\_accuracy: 0.9655 - 52s/epoch - 111ms/step  
Epoch 64/100  
469/469 - 52s - loss: 0.1215 - sparse\_categorical\_accuracy: 0.9611 - val\_loss: 0.1069 - val\_sparse\_c  
ategorical\_accuracy: 0.9660 - 52s/epoch - 111ms/step  
Epoch 65/100  
469/469 - 52s - loss: 0.1202 - sparse\_categorical\_accuracy: 0.9619 - val\_loss: 0.1060 - val\_sparse\_c  
ategorical\_accuracy: 0.9652 - 52s/epoch - 111ms/step  
Epoch 66/100  
469/469 - 52s - loss: 0.1203 - sparse\_categorical\_accuracy: 0.9617 - val\_loss: 0.1071 - val\_sparse\_c  
ategorical\_accuracy: 0.9650 - 52s/epoch - 111ms/step  
Epoch 67/100  
469/469 - 52s - loss: 0.1194 - sparse\_categorical\_accuracy: 0.9623 - val\_loss: 0.1016 - val\_sparse\_c  
ategorical\_accuracy: 0.9685 - 52s/epoch - 111ms/step  
Epoch 68/100



[illegible]

```
Epoch 96/100
469/469 - 52s - loss: 0.1097 - sparse_categorical_accuracy: 0.9647 - val_loss: 0.0944 - val_sparse_c
ategorical_accuracy: 0.9708 - 52s/epoch - 111ms/step
Epoch 97/100
469/469 - 52s - loss: 0.1083 - sparse_categorical_accuracy: 0.9659 - val_loss: 0.1024 - val_sparse_c
ategorical_accuracy: 0.9673 - 52s/epoch - 112ms/step
Epoch 98/100
469/469 - 52s - loss: 0.1076 - sparse_categorical_accuracy: 0.9663 - val_loss: 0.0990 - val_sparse_c
ategorical_accuracy: 0.9682 - 52s/epoch - 112ms/step
Epoch 99/100
469/469 - 52s - loss: 0.1073 - sparse_categorical_accuracy: 0.9660 - val_loss: 0.1059 - val_sparse_c
ategorical_accuracy: 0.9675 - 52s/epoch - 111ms/step
Epoch 100/100
469/469 - 52s - loss: 0.1086 - sparse_categorical_accuracy: 0.9656 - val_loss: 0.0930 - val_sparse_c
ategorical_accuracy: 0.9699 - 52s/epoch - 111ms/step
```

In [12]:

```
model1.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 4s - loss: 0.0930 - sparse_categorical_accuracy: 0.9699 - 4s/epoch - 13ms/step
```

Out[12]:

```
[0.09297644346952438, 0.9699000120162964]
```

**Model2: adam optimizer with learning rate= $e^{-4}$ , random\_uniform initializer, dropout regularization with rate=0.1.**

In [13]:

```
input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                      filters_1x1=1,
                      filters_3x3_reduce=1,
                      filters_3x3=1,
                      filters_5x5_reduce=1,
                      filters_5x5=1,
                      filters_pool_proj=1,
                      name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.1)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_uniform')(x)
model2 = Model(input_layer, x, name='inception_v1')
```

In [14]:

```
model2.compile(optimizer=tf.keras.optimizers.Adam(0.0001),
               loss='sparse_categorical_crossentropy',
               metrics=['sparse_categorical_accuracy'])
```

In [15]:

```
history2 = model2.fit(x_train, y_train,
                      batch_size=128,
                      epochs=100,
                      validation_data=(x_test, y_test),
                      verbose=2)
```

```
Epoch 1/100
469/469 - 53s - loss: 1.9642 - sparse_categorical_accuracy: 0.5036 - val_loss: 1.6752 - val_sparse_c
ategorical_accuracy: 0.7477 - 53s/epoch - 113ms/step
Epoch 2/100
469/469 - 52s - loss: 1.3738 - sparse_categorical_accuracy: 0.7804 - val_loss: 1.0907 - val_sparse_c
ategorical_accuracy: 0.8542 - 52s/epoch - 110ms/step
Epoch 3/100
469/469 - 52s - loss: 0.9748 - sparse_categorical_accuracy: 0.8523 - val_loss: 0.7782 - val_sparse_c
ategorical_accuracy: 0.8883 - 52s/epoch - 110ms/step
Epoch 4/100
469/469 - 52s - loss: 0.7113 - sparse_categorical_accuracy: 0.8871 - val_loss: 0.5566 - val_sparse_c
ategorical_accuracy: 0.9170 - 52s/epoch - 110ms/step
Epoch 5/100
469/469 - 52s - loss: 0.5367 - sparse_categorical_accuracy: 0.9057 - val_loss: 0.4216 - val_sparse_c
ategorical_accuracy: 0.9269 - 52s/epoch - 110ms/step
Epoch 6/100
469/469 - 52s - loss: 0.4213 - sparse_categorical_accuracy: 0.9164 - val_loss: 0.3323 - val_sparse_c
```

ategorical accuracy: 0.9365 - 52s/epoch - 111ms/step  
Epoch 7/100  
469/469 - 52s - loss: 0.3488 - sparse\_categorical\_accuracy: 0.9237 - val\_loss: 0.2746 - val\_sparse\_c  
ategorical accuracy: 0.9414 - 52s/epoch - 110ms/step  
Epoch 8/100  
469/469 - 52s - loss: 0.2983 - sparse\_categorical\_accuracy: 0.9302 - val\_loss: 0.2342 - val\_sparse\_c  
ategorical accuracy: 0.9449 - 52s/epoch - 110ms/step  
Epoch 9/100  
469/469 - 52s - loss: 0.2652 - sparse\_categorical\_accuracy: 0.9328 - val\_loss: 0.2077 - val\_sparse\_c  
ategorical accuracy: 0.9485 - 52s/epoch - 110ms/step  
Epoch 10/100  
469/469 - 52s - loss: 0.2407 - sparse\_categorical\_accuracy: 0.9375 - val\_loss: 0.1864 - val\_sparse\_c  
ategorical accuracy: 0.9508 - 52s/epoch - 110ms/step  
Epoch 11/100  
469/469 - 52s - loss: 0.2215 - sparse\_categorical\_accuracy: 0.9405 - val\_loss: 0.1741 - val\_sparse\_c  
ategorical accuracy: 0.9532 - 52s/epoch - 110ms/step  
Epoch 12/100  
469/469 - 52s - loss: 0.2051 - sparse\_categorical\_accuracy: 0.9432 - val\_loss: 0.1630 - val\_sparse\_c  
ategorical accuracy: 0.9551 - 52s/epoch - 111ms/step  
Epoch 13/100  
469/469 - 52s - loss: 0.1965 - sparse\_categorical\_accuracy: 0.9437 - val\_loss: 0.1536 - val\_sparse\_c  
ategorical accuracy: 0.9568 - 52s/epoch - 111ms/step  
Epoch 14/100  
469/469 - 52s - loss: 0.1867 - sparse\_categorical\_accuracy: 0.9459 - val\_loss: 0.1455 - val\_sparse\_c  
ategorical accuracy: 0.9587 - 52s/epoch - 111ms/step  
Epoch 15/100  
469/469 - 52s - loss: 0.1798 - sparse\_categorical\_accuracy: 0.9480 - val\_loss: 0.1395 - val\_sparse\_c  
ategorical accuracy: 0.9589 - 52s/epoch - 111ms/step  
Epoch 16/100  
469/469 - 52s - loss: 0.1734 - sparse\_categorical\_accuracy: 0.9495 - val\_loss: 0.1336 - val\_sparse\_c  
ategorical accuracy: 0.9614 - 52s/epoch - 111ms/step  
Epoch 17/100  
469/469 - 52s - loss: 0.1661 - sparse\_categorical\_accuracy: 0.9512 - val\_loss: 0.1302 - val\_sparse\_c  
ategorical accuracy: 0.9628 - 52s/epoch - 111ms/step  
Epoch 18/100  
469/469 - 52s - loss: 0.1605 - sparse\_categorical\_accuracy: 0.9526 - val\_loss: 0.1274 - val\_sparse\_c  
ategorical accuracy: 0.9632 - 52s/epoch - 111ms/step  
Epoch 19/100  
469/469 - 52s - loss: 0.1576 - sparse\_categorical\_accuracy: 0.9531 - val\_loss: 0.1220 - val\_sparse\_c  
ategorical accuracy: 0.9637 - 52s/epoch - 111ms/step  
Epoch 20/100  
469/469 - 52s - loss: 0.1543 - sparse\_categorical\_accuracy: 0.9546 - val\_loss: 0.1202 - val\_sparse\_c  
ategorical accuracy: 0.9640 - 52s/epoch - 111ms/step  
Epoch 21/100  
469/469 - 52s - loss: 0.1491 - sparse\_categorical\_accuracy: 0.9556 - val\_loss: 0.1189 - val\_sparse\_c  
ategorical accuracy: 0.9646 - 52s/epoch - 112ms/step  
Epoch 22/100  
469/469 - 52s - loss: 0.1479 - sparse\_categorical\_accuracy: 0.9556 - val\_loss: 0.1152 - val\_sparse\_c  
ategorical accuracy: 0.9649 - 52s/epoch - 111ms/step  
Epoch 23/100  
469/469 - 52s - loss: 0.1475 - sparse\_categorical\_accuracy: 0.9560 - val\_loss: 0.1135 - val\_sparse\_c  
ategorical accuracy: 0.9654 - 52s/epoch - 112ms/step  
Epoch 24/100  
469/469 - 52s - loss: 0.1426 - sparse\_categorical\_accuracy: 0.9572 - val\_loss: 0.1128 - val\_sparse\_c  
ategorical accuracy: 0.9656 - 52s/epoch - 112ms/step  
Epoch 25/100  
469/469 - 52s - loss: 0.1407 - sparse\_categorical\_accuracy: 0.9581 - val\_loss: 0.1122 - val\_sparse\_c  
ategorical accuracy: 0.9652 - 52s/epoch - 112ms/step  
Epoch 26/100  
469/469 - 52s - loss: 0.1397 - sparse\_categorical\_accuracy: 0.9576 - val\_loss: 0.1095 - val\_sparse\_c  
ategorical accuracy: 0.9666 - 52s/epoch - 112ms/step  
Epoch 27/100  
469/469 - 52s - loss: 0.1390 - sparse\_categorical\_accuracy: 0.9581 - val\_loss: 0.1089 - val\_sparse\_c  
ategorical accuracy: 0.9668 - 52s/epoch - 112ms/step  
Epoch 28/100  
469/469 - 52s - loss: 0.1373 - sparse\_categorical\_accuracy: 0.9587 - val\_loss: 0.1054 - val\_sparse\_c  
ategorical accuracy: 0.9667 - 52s/epoch - 111ms/step  
Epoch 29/100  
469/469 - 52s - loss: 0.1333 - sparse\_categorical\_accuracy: 0.9599 - val\_loss: 0.1061 - val\_sparse\_c  
ategorical accuracy: 0.9672 - 52s/epoch - 112ms/step  
Epoch 30/100  
469/469 - 52s - loss: 0.1318 - sparse\_categorical\_accuracy: 0.9607 - val\_loss: 0.1037 - val\_sparse\_c  
ategorical accuracy: 0.9678 - 52s/epoch - 111ms/step  
Epoch 31/100  
469/469 - 52s - loss: 0.1322 - sparse\_categorical\_accuracy: 0.9597 - val\_loss: 0.1025 - val\_sparse\_c  
ategorical accuracy: 0.9686 - 52s/epoch - 112ms/step  
Epoch 32/100  
469/469 - 52s - loss: 0.1306 - sparse\_categorical\_accuracy: 0.9601 - val\_loss: 0.1015 - val\_sparse\_c  
ategorical accuracy: 0.9691 - 52s/epoch - 112ms/step  
Epoch 33/100  
469/469 - 52s - loss: 0.1285 - sparse\_categorical\_accuracy: 0.9607 - val\_loss: 0.1008 - val\_sparse\_c  
ategorical accuracy: 0.9678 - 52s/epoch - 112ms/step  
Epoch 34/100

[illegible]

```
Epoch 62/100  
469/469 - 52s - loss: 0.1077 - sparse_categorical_accuracy: 0.9657 - val_loss: 0.0860 - val_sparse_c  
ategorical_accuracy: 0.9709 - 52s/epoch - 112ms/step  
Epoch 63/100  
469/469 - 52s - loss: 0.1091 - sparse_categorical_accuracy: 0.9656 - val_loss: 0.0864 - val_sparse_c  
ategorical_accuracy: 0.9725 - 52s/epoch - 112ms/step  
Epoch 64/100  
469/469 - 52s - loss: 0.1053 - sparse_categorical_accuracy: 0.9670 - val_loss: 0.0853 - val_sparse_c  
ategorical_accuracy: 0.9723 - 52s/epoch - 111ms/step  
Epoch 65/100  
469/469 - 52s - loss: 0.1044 - sparse_categorical_accuracy: 0.9673 - val_loss: 0.0864 - val_sparse_c  
ategorical_accuracy: 0.9719 - 52s/epoch - 111ms/step  
Epoch 66/100  
469/469 - 52s - loss: 0.1059 - sparse_categorical_accuracy: 0.9668 - val_loss: 0.0838 - val_sparse_c  
ategorical_accuracy: 0.9725 - 52s/epoch - 111ms/step  
Epoch 67/100  
469/469 - 52s - loss: 0.1063 - sparse_categorical_accuracy: 0.9666 - val_loss: 0.0845 - val_sparse_c  
ategorical_accuracy: 0.9724 - 52s/epoch - 112ms/step  
Epoch 68/100  
469/469 - 52s - loss: 0.1057 - sparse_categorical_accuracy: 0.9669 - val_loss: 0.0837 - val_sparse_c  
ategorical_accuracy: 0.9732 - 52s/epoch - 111ms/step  
Epoch 69/100  
469/469 - 52s - loss: 0.1050 - sparse_categorical_accuracy: 0.9668 - val_loss: 0.0837 - val_sparse_c  
ategorical_accuracy: 0.9722 - 52s/epoch - 112ms/step  
Epoch 70/100  
469/469 - 52s - loss: 0.1038 - sparse_categorical_accuracy: 0.9674 - val_loss: 0.0829 - val_sparse_c  
ategorical_accuracy: 0.9730 - 52s/epoch - 112ms/step  
Epoch 71/100  
469/469 - 52s - loss: 0.1035 - sparse_categorical_accuracy: 0.9671 - val_loss: 0.0837 - val_sparse_c  
ategorical_accuracy: 0.9723 - 52s/epoch - 111ms/step  
Epoch 72/100  
469/469 - 52s - loss: 0.1012 - sparse_categorical_accuracy: 0.9678 - val_loss: 0.0826 - val_sparse_c  
ategorical_accuracy: 0.9739 - 52s/epoch - 111ms/step  
Epoch 73/100  
469/469 - 52s - loss: 0.1032 - sparse_categorical_accuracy: 0.9675 - val_loss: 0.0823 - val_sparse_c  
ategorical_accuracy: 0.9727 - 52s/epoch - 112ms/step  
Epoch 74/100  
469/469 - 52s - loss: 0.1015 - sparse_categorical_accuracy: 0.9679 - val_loss: 0.0825 - val_sparse_c  
ategorical_accuracy: 0.9728 - 52s/epoch - 112ms/step  
Epoch 75/100  
469/469 - 52s - loss: 0.1016 - sparse_categorical_accuracy: 0.9683 - val_loss: 0.0851 - val_sparse_c  
ategorical_accuracy: 0.9711 - 52s/epoch - 111ms/step  
Epoch 76/100  
469/469 - 52s - loss: 0.1034 - sparse_categorical_accuracy: 0.9668 - val_loss: 0.0819 - val_sparse_c  
ategorical_accuracy: 0.9729 - 52s/epoch - 111ms/step  
Epoch 77/100  
469/469 - 52s - loss: 0.1016 - sparse_categorical_accuracy: 0.9682 - val_loss: 0.0800 - val_sparse_c  
ategorical_accuracy: 0.9735 - 52s/epoch - 111ms/step  
Epoch 78/100  
469/469 - 52s - loss: 0.1010 - sparse_categorical_accuracy: 0.9684 - val_loss: 0.0807 - val_sparse_c  
ategorical_accuracy: 0.9735 - 52s/epoch - 112ms/step  
Epoch 79/100  
469/469 - 52s - loss: 0.1023 - sparse_categorical_accuracy: 0.9675 - val_loss: 0.0832 - val_sparse_c  
ategorical_accuracy: 0.9740 - 52s/epoch - 112ms/step  
Epoch 80/100  
469/469 - 52s - loss: 0.0999 - sparse_categorical_accuracy: 0.9690 - val_loss: 0.0820 - val_sparse_c  
ategorical_accuracy: 0.9723 - 52s/epoch - 112ms/step  
Epoch 81/100  
469/469 - 52s - loss: 0.1010 - sparse_categorical_accuracy: 0.9685 - val_loss: 0.0821 - val_sparse_c  
ategorical_accuracy: 0.9729 - 52s/epoch - 112ms/step  
Epoch 82/100  
469/469 - 52s - loss: 0.1004 - sparse_categorical_accuracy: 0.9687 - val_loss: 0.0805 - val_sparse_c  
ategorical_accuracy: 0.9736 - 52s/epoch - 112ms/step  
Epoch 83/100  
469/469 - 54s - loss: 0.1013 - sparse_categorical_accuracy: 0.9679 - val_loss: 0.0799 - val_sparse_c  
ategorical_accuracy: 0.9741 - 54s/epoch - 114ms/step  
Epoch 84/100  
469/469 - 53s - loss: 0.0986 - sparse_categorical_accuracy: 0.9691 - val_loss: 0.0806 - val_sparse_c  
ategorical_accuracy: 0.9729 - 53s/epoch - 112ms/step  
Epoch 85/100  
469/469 - 52s - loss: 0.0971 - sparse_categorical_accuracy: 0.9697 - val_loss: 0.0807 - val_sparse_c  
ategorical_accuracy: 0.9733 - 52s/epoch - 112ms/step  
Epoch 86/100  
469/469 - 53s - loss: 0.0981 - sparse_categorical_accuracy: 0.9690 - val_loss: 0.0809 - val_sparse_c  
ategorical_accuracy: 0.9723 - 53s/epoch - 112ms/step  
Epoch 87/100  
469/469 - 52s - loss: 0.0975 - sparse_categorical_accuracy: 0.9691 - val_loss: 0.0808 - val_sparse_c  
ategorical_accuracy: 0.9732 - 52s/epoch - 112ms/step  
Epoch 88/100  
469/469 - 52s - loss: 0.0968 - sparse_categorical_accuracy: 0.9697 - val_loss: 0.0813 - val_sparse_c  
ategorical_accuracy: 0.9722 - 52s/epoch - 112ms/step  
Epoch 89/100  
469/469 - 53s - loss: 0.0969 - sparse categorical accuracy: 0.9689 - val loss: 0.0806 - val sparse c
```

```
ategorical_accuracy: 0.9733 - 53s/epoch - 112ms/step
Epoch 90/100
469/469 - 52s - loss: 0.0974 - sparse_categorical_accuracy: 0.9695 - val_loss: 0.0796 - val_sparse_c
ategorical_accuracy: 0.9726 - 52s/epoch - 112ms/step
Epoch 91/100
469/469 - 52s - loss: 0.0975 - sparse_categorical_accuracy: 0.9693 - val_loss: 0.0794 - val_sparse_c
ategorical_accuracy: 0.9743 - 52s/epoch - 111ms/step
Epoch 92/100
469/469 - 52s - loss: 0.0961 - sparse_categorical_accuracy: 0.9695 - val_loss: 0.0789 - val_sparse_c
ategorical_accuracy: 0.9740 - 52s/epoch - 112ms/step
Epoch 93/100
469/469 - 52s - loss: 0.0991 - sparse_categorical_accuracy: 0.9689 - val_loss: 0.0792 - val_sparse_c
ategorical_accuracy: 0.9740 - 52s/epoch - 111ms/step
Epoch 94/100
469/469 - 52s - loss: 0.0976 - sparse_categorical_accuracy: 0.9689 - val_loss: 0.0794 - val_sparse_c
ategorical_accuracy: 0.9736 - 52s/epoch - 111ms/step
Epoch 95/100
469/469 - 52s - loss: 0.0966 - sparse_categorical_accuracy: 0.9700 - val_loss: 0.0783 - val_sparse_c
ategorical_accuracy: 0.9737 - 52s/epoch - 112ms/step
Epoch 96/100
469/469 - 52s - loss: 0.0964 - sparse_categorical_accuracy: 0.9694 - val_loss: 0.0779 - val_sparse_c
ategorical_accuracy: 0.9740 - 52s/epoch - 112ms/step
Epoch 97/100
469/469 - 52s - loss: 0.0947 - sparse_categorical_accuracy: 0.9697 - val_loss: 0.0800 - val_sparse_c
ategorical_accuracy: 0.9744 - 52s/epoch - 112ms/step
Epoch 98/100
469/469 - 52s - loss: 0.0962 - sparse_categorical_accuracy: 0.9690 - val_loss: 0.0799 - val_sparse_c
ategorical_accuracy: 0.9736 - 52s/epoch - 111ms/step
Epoch 99/100
469/469 - 52s - loss: 0.0964 - sparse_categorical_accuracy: 0.9701 - val_loss: 0.0786 - val_sparse_c
ategorical_accuracy: 0.9739 - 52s/epoch - 111ms/step
Epoch 100/100
469/469 - 52s - loss: 0.0965 - sparse_categorical_accuracy: 0.9695 - val_loss: 0.0780 - val_sparse_c
ategorical_accuracy: 0.9742 - 52s/epoch - 111ms/step
```

In [16]:

```
model2.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 4s - loss: 0.0780 - sparse_categorical_accuracy: 0.9742 - 4s/epoch - 14ms/step
```

Out[16]:

```
[0.07802172750234604, 0.9742000102996826]
```

**Model3: adam optimizer with learning rate= $e^{-3}$ , random\_normal initializer, dropout regularization with rate=0.1.**

In [17]:

```
input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                     filters_1x1=1,
                     filters_3x3_reduce=1,
                     filters_3x3=1,
                     filters_5x5_reduce=1,
                     filters_5x5=1,
                     filters_pool_proj=1,
                     name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.1)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_uniform')(x)
model3 = Model(input_layer, x, name='inception_v1')
```

In [18]:

```
model3.compile(optimizer=tf.keras.optimizers.Adam(0.001),
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy']
              )
```

In [19]:

```
history3 = model3.fit(x_train, y_train,  
                      batch_size=128,  
                      epochs=100,  
                      validation_data=(x_test, y_test),  
                      verbose=2  
                      )
```

Epoch 1/100

469/469 - 54s - loss: 0.9932 - sparse\_categorical\_accuracy: 0.7682 - val\_loss: 0.3869 - val\_sparse\_categorical\_accuracy: 0.8969 - 54s/epoch - 114ms/step

Epoch 2/100

469/469 - 52s - loss: 0.4003 - sparse\_categorical\_accuracy: 0.8785 - val\_loss: 0.2898 - val\_sparse\_categorical\_accuracy: 0.9084 - 52s/epoch - 111ms/step

Epoch 3/100

469/469 - 52s - loss: 0.3441 - sparse\_categorical\_accuracy: 0.8905 - val\_loss: 0.2455 - val\_sparse\_categorical\_accuracy: 0.9250 - 52s/epoch - 111ms/step

Epoch 4/100

469/469 - 52s - loss: 0.3152 - sparse\_categorical\_accuracy: 0.8994 - val\_loss: 0.2297 - val\_sparse\_categorical\_accuracy: 0.9277 - 52s/epoch - 111ms/step

Epoch 5/100

469/469 - 52s - loss: 0.2865 - sparse\_categorical\_accuracy: 0.9082 - val\_loss: 0.2129 - val\_sparse\_categorical\_accuracy: 0.9337 - 52s/epoch - 111ms/step

Epoch 6/100

469/469 - 52s - loss: 0.2523 - sparse\_categorical\_accuracy: 0.9194 - val\_loss: 0.1935 - val\_sparse\_categorical\_accuracy: 0.9378 - 52s/epoch - 111ms/step

Epoch 7/100

469/469 - 52s - loss: 0.2287 - sparse\_categorical\_accuracy: 0.9278 - val\_loss: 0.1886 - val\_sparse\_categorical\_accuracy: 0.9423 - 52s/epoch - 111ms/step

Epoch 8/100

469/469 - 52s - loss: 0.2146 - sparse\_categorical\_accuracy: 0.9320 - val\_loss: 0.1999 - val\_sparse\_categorical\_accuracy: 0.9385 - 52s/epoch - 111ms/step

Epoch 9/100

469/469 - 52s - loss: 0.2040 - sparse\_categorical\_accuracy: 0.9365 - val\_loss: 0.1516 - val\_sparse\_categorical\_accuracy: 0.9544 - 52s/epoch - 111ms/step

Epoch 10/100

469/469 - 52s - loss: 0.1950 - sparse\_categorical\_accuracy: 0.9380 - val\_loss: 0.1567 - val\_sparse\_categorical\_accuracy: 0.9533 - 52s/epoch - 111ms/step

Epoch 11/100

469/469 - 52s - loss: 0.1867 - sparse\_categorical\_accuracy: 0.9409 - val\_loss: 0.1409 - val\_sparse\_categorical\_accuracy: 0.9563 - 52s/epoch - 111ms/step

Epoch 12/100

469/469 - 52s - loss: 0.1820 - sparse\_categorical\_accuracy: 0.9431 - val\_loss: 0.1387 - val\_sparse\_categorical\_accuracy: 0.9576 - 52s/epoch - 112ms/step

Epoch 13/100

469/469 - 53s - loss: 0.1767 - sparse\_categorical\_accuracy: 0.9443 - val\_loss: 0.1388 - val\_sparse\_categorical\_accuracy: 0.9583 - 53s/epoch - 112ms/step

Epoch 14/100

469/469 - 53s - loss: 0.1712 - sparse\_categorical\_accuracy: 0.9459 - val\_loss: 0.1431 - val\_sparse\_categorical\_accuracy: 0.9559 - 53s/epoch - 112ms/step

Epoch 15/100

469/469 - 52s - loss: 0.1681 - sparse\_categorical\_accuracy: 0.9463 - val\_loss: 0.1291 - val\_sparse\_categorical\_accuracy: 0.9611 - 52s/epoch - 112ms/step

Epoch 16/100

469/469 - 52s - loss: 0.1655 - sparse\_categorical\_accuracy: 0.9474 - val\_loss: 0.1298 - val\_sparse\_categorical\_accuracy: 0.9610 - 52s/epoch - 112ms/step

Epoch 17/100

469/469 - 52s - loss: 0.1605 - sparse\_categorical\_accuracy: 0.9501 - val\_loss: 0.1327 - val\_sparse\_categorical\_accuracy: 0.9585 - 52s/epoch - 112ms/step

Epoch 18/100

469/469 - 53s - loss: 0.1576 - sparse\_categorical\_accuracy: 0.9499 - val\_loss: 0.1264 - val\_sparse\_categorical\_accuracy: 0.9615 - 53s/epoch - 112ms/step

Epoch 19/100

469/469 - 53s - loss: 0.1592 - sparse\_categorical\_accuracy: 0.9495 - val\_loss: 0.1289 - val\_sparse\_categorical\_accuracy: 0.9595 - 53s/epoch - 112ms/step

Epoch 20/100

469/469 - 53s - loss: 0.1539 - sparse\_categorical\_accuracy: 0.9517 - val\_loss: 0.1262 - val\_sparse\_categorical\_accuracy: 0.9620 - 53s/epoch - 112ms/step

Epoch 21/100

469/469 - 52s - loss: 0.1511 - sparse\_categorical\_accuracy: 0.9521 - val\_loss: 0.1323 - val\_sparse\_categorical\_accuracy: 0.9593 - 52s/epoch - 112ms/step

Epoch 22/100

469/469 - 52s - loss: 0.1501 - sparse\_categorical\_accuracy: 0.9521 - val\_loss: 0.1335 - val\_sparse\_categorical\_accuracy: 0.9589 - 52s/epoch - 112ms/step

Epoch 23/100

469/469 - 52s - loss: 0.1502 - sparse\_categorical\_accuracy: 0.9519 - val\_loss: 0.1189 - val\_sparse\_categorical\_accuracy: 0.9644 - 52s/epoch - 112ms/step

Epoch 24/100

469/469 - 52s - loss: 0.1470 - sparse\_categorical\_accuracy: 0.9532 - val\_loss: 0.1155 - val\_sparse\_categorical\_accuracy: 0.9657 - 52s/epoch - 112ms/step

Epoch 25/100

469/469 - 52s - loss: 0.1468 - sparse\_categorical\_accuracy: 0.9528 - val\_loss: 0.1266 - val\_sparse\_categorical\_accuracy: 0.9657 - 52s/epoch - 112ms/step

ategorical\_accuracy: 0.9626 - 52s/epoch - 112ms/step  
Epoch 26/100  
469/469 - 52s - loss: 0.1414 - sparse\_categorical\_accuracy: 0.9546 - val\_loss: 0.1147 - val\_sparse\_c  
ategorical\_accuracy: 0.9654 - 52s/epoch - 111ms/step  
Epoch 27/100  
469/469 - 52s - loss: 0.1437 - sparse\_categorical\_accuracy: 0.9538 - val\_loss: 0.1147 - val\_sparse\_c  
ategorical\_accuracy: 0.9654 - 52s/epoch - 111ms/step  
Epoch 28/100  
469/469 - 52s - loss: 0.1415 - sparse\_categorical\_accuracy: 0.9545 - val\_loss: 0.1339 - val\_sparse\_c  
ategorical\_accuracy: 0.9590 - 52s/epoch - 111ms/step  
Epoch 29/100  
469/469 - 52s - loss: 0.1369 - sparse\_categorical\_accuracy: 0.9565 - val\_loss: 0.1206 - val\_sparse\_c  
ategorical\_accuracy: 0.9632 - 52s/epoch - 112ms/step  
Epoch 30/100  
469/469 - 52s - loss: 0.1398 - sparse\_categorical\_accuracy: 0.9555 - val\_loss: 0.1100 - val\_sparse\_c  
ategorical\_accuracy: 0.9658 - 52s/epoch - 112ms/step  
Epoch 31/100  
469/469 - 52s - loss: 0.1383 - sparse\_categorical\_accuracy: 0.9558 - val\_loss: 0.1165 - val\_sparse\_c  
ategorical\_accuracy: 0.9649 - 52s/epoch - 112ms/step  
Epoch 32/100  
469/469 - 52s - loss: 0.1386 - sparse\_categorical\_accuracy: 0.9557 - val\_loss: 0.1019 - val\_sparse\_c  
ategorical\_accuracy: 0.9704 - 52s/epoch - 112ms/step  
Epoch 33/100  
469/469 - 52s - loss: 0.1351 - sparse\_categorical\_accuracy: 0.9570 - val\_loss: 0.1215 - val\_sparse\_c  
ategorical\_accuracy: 0.9612 - 52s/epoch - 112ms/step  
Epoch 34/100  
469/469 - 52s - loss: 0.1367 - sparse\_categorical\_accuracy: 0.9565 - val\_loss: 0.1020 - val\_sparse\_c  
ategorical\_accuracy: 0.9688 - 52s/epoch - 112ms/step  
Epoch 35/100  
469/469 - 53s - loss: 0.1352 - sparse\_categorical\_accuracy: 0.9562 - val\_loss: 0.1136 - val\_sparse\_c  
ategorical\_accuracy: 0.9656 - 53s/epoch - 112ms/step  
Epoch 36/100  
469/469 - 52s - loss: 0.1328 - sparse\_categorical\_accuracy: 0.9579 - val\_loss: 0.1111 - val\_sparse\_c  
ategorical\_accuracy: 0.9668 - 52s/epoch - 111ms/step  
Epoch 37/100  
469/469 - 53s - loss: 0.1334 - sparse\_categorical\_accuracy: 0.9577 - val\_loss: 0.1075 - val\_sparse\_c  
ategorical\_accuracy: 0.9670 - 53s/epoch - 112ms/step  
Epoch 38/100  
469/469 - 52s - loss: 0.1325 - sparse\_categorical\_accuracy: 0.9577 - val\_loss: 0.1188 - val\_sparse\_c  
ategorical\_accuracy: 0.9612 - 52s/epoch - 112ms/step  
Epoch 39/100  
469/469 - 52s - loss: 0.1328 - sparse\_categorical\_accuracy: 0.9580 - val\_loss: 0.1054 - val\_sparse\_c  
ategorical\_accuracy: 0.9676 - 52s/epoch - 112ms/step  
Epoch 40/100  
469/469 - 52s - loss: 0.1286 - sparse\_categorical\_accuracy: 0.9592 - val\_loss: 0.0996 - val\_sparse\_c  
ategorical\_accuracy: 0.9698 - 52s/epoch - 112ms/step  
Epoch 41/100  
469/469 - 53s - loss: 0.1279 - sparse\_categorical\_accuracy: 0.9592 - val\_loss: 0.1005 - val\_sparse\_c  
ategorical\_accuracy: 0.9688 - 53s/epoch - 112ms/step  
Epoch 42/100  
469/469 - 52s - loss: 0.1281 - sparse\_categorical\_accuracy: 0.9589 - val\_loss: 0.1032 - val\_sparse\_c  
ategorical\_accuracy: 0.9669 - 52s/epoch - 112ms/step  
Epoch 43/100  
469/469 - 52s - loss: 0.1260 - sparse\_categorical\_accuracy: 0.9597 - val\_loss: 0.1080 - val\_sparse\_c  
ategorical\_accuracy: 0.9662 - 52s/epoch - 112ms/step  
Epoch 44/100  
469/469 - 52s - loss: 0.1309 - sparse\_categorical\_accuracy: 0.9579 - val\_loss: 0.0987 - val\_sparse\_c  
ategorical\_accuracy: 0.9703 - 52s/epoch - 111ms/step  
Epoch 45/100  
469/469 - 52s - loss: 0.1259 - sparse\_categorical\_accuracy: 0.9601 - val\_loss: 0.1079 - val\_sparse\_c  
ategorical\_accuracy: 0.9662 - 52s/epoch - 111ms/step  
Epoch 46/100  
469/469 - 52s - loss: 0.1276 - sparse\_categorical\_accuracy: 0.9593 - val\_loss: 0.1204 - val\_sparse\_c  
ategorical\_accuracy: 0.9624 - 52s/epoch - 112ms/step  
Epoch 47/100  
469/469 - 52s - loss: 0.1254 - sparse\_categorical\_accuracy: 0.9600 - val\_loss: 0.1013 - val\_sparse\_c  
ategorical\_accuracy: 0.9688 - 52s/epoch - 112ms/step  
Epoch 48/100  
469/469 - 52s - loss: 0.1240 - sparse\_categorical\_accuracy: 0.9609 - val\_loss: 0.0982 - val\_sparse\_c  
ategorical\_accuracy: 0.9695 - 52s/epoch - 112ms/step  
Epoch 49/100  
469/469 - 52s - loss: 0.1256 - sparse\_categorical\_accuracy: 0.9597 - val\_loss: 0.1005 - val\_sparse\_c  
ategorical\_accuracy: 0.9694 - 52s/epoch - 112ms/step  
Epoch 50/100  
469/469 - 52s - loss: 0.1250 - sparse\_categorical\_accuracy: 0.9600 - val\_loss: 0.0960 - val\_sparse\_c  
ategorical\_accuracy: 0.9704 - 52s/epoch - 112ms/step  
Epoch 51/100  
469/469 - 52s - loss: 0.1225 - sparse\_categorical\_accuracy: 0.9607 - val\_loss: 0.1048 - val\_sparse\_c  
ategorical\_accuracy: 0.9679 - 52s/epoch - 112ms/step  
Epoch 52/100  
469/469 - 52s - loss: 0.1216 - sparse\_categorical\_accuracy: 0.9613 - val\_loss: 0.1195 - val\_sparse\_c  
ategorical\_accuracy: 0.9623 - 52s/epoch - 112ms/step  
Epoch 53/100



469/469 - 53s - loss: 0.1210 - sparse\_categorical\_accuracy: 0.9612 - val\_loss: 0.1014 - val\_sparse\_categorical\_accuracy: 0.9676 - 53s/epoch - 112ms/step  
Epoch 54/100  
469/469 - 52s - loss: 0.1232 - sparse\_categorical\_accuracy: 0.9598 - val\_loss: 0.0963 - val\_sparse\_categorical\_accuracy: 0.9697 - 52s/epoch - 112ms/step  
Epoch 55/100  
469/469 - 52s - loss: 0.1201 - sparse\_categorical\_accuracy: 0.9620 - val\_loss: 0.0959 - val\_sparse\_categorical\_accuracy: 0.9710 - 52s/epoch - 112ms/step  
Epoch 56/100  
469/469 - 52s - loss: 0.1219 - sparse\_categorical\_accuracy: 0.9613 - val\_loss: 0.0977 - val\_sparse\_categorical\_accuracy: 0.9716 - 52s/epoch - 111ms/step  
Epoch 57/100  
469/469 - 52s - loss: 0.1190 - sparse\_categorical\_accuracy: 0.9611 - val\_loss: 0.0917 - val\_sparse\_categorical\_accuracy: 0.9730 - 52s/epoch - 112ms/step  
Epoch 58/100  
469/469 - 53s - loss: 0.1185 - sparse\_categorical\_accuracy: 0.9616 - val\_loss: 0.1123 - val\_sparse\_categorical\_accuracy: 0.9661 - 53s/epoch - 112ms/step  
Epoch 59/100  
469/469 - 52s - loss: 0.1194 - sparse\_categorical\_accuracy: 0.9618 - val\_loss: 0.1012 - val\_sparse\_categorical\_accuracy: 0.9684 - 52s/epoch - 112ms/step  
Epoch 60/100  
469/469 - 52s - loss: 0.1179 - sparse\_categorical\_accuracy: 0.9620 - val\_loss: 0.0911 - val\_sparse\_categorical\_accuracy: 0.9717 - 52s/epoch - 112ms/step  
Epoch 61/100  
469/469 - 52s - loss: 0.1170 - sparse\_categorical\_accuracy: 0.9625 - val\_loss: 0.0981 - val\_sparse\_categorical\_accuracy: 0.9689 - 52s/epoch - 112ms/step  
Epoch 62/100  
469/469 - 52s - loss: 0.1152 - sparse\_categorical\_accuracy: 0.9629 - val\_loss: 0.0913 - val\_sparse\_categorical\_accuracy: 0.9720 - 52s/epoch - 111ms/step  
Epoch 63/100  
469/469 - 52s - loss: 0.1149 - sparse\_categorical\_accuracy: 0.9635 - val\_loss: 0.1042 - val\_sparse\_categorical\_accuracy: 0.9692 - 52s/epoch - 112ms/step  
Epoch 64/100  
469/469 - 53s - loss: 0.1155 - sparse\_categorical\_accuracy: 0.9635 - val\_loss: 0.1025 - val\_sparse\_categorical\_accuracy: 0.9696 - 53s/epoch - 112ms/step  
Epoch 65/100  
469/469 - 52s - loss: 0.1164 - sparse\_categorical\_accuracy: 0.9628 - val\_loss: 0.1004 - val\_sparse\_categorical\_accuracy: 0.9700 - 52s/epoch - 111ms/step  
Epoch 66/100  
469/469 - 52s - loss: 0.1119 - sparse\_categorical\_accuracy: 0.9637 - val\_loss: 0.0980 - val\_sparse\_categorical\_accuracy: 0.9703 - 52s/epoch - 111ms/step  
Epoch 67/100  
469/469 - 52s - loss: 0.1126 - sparse\_categorical\_accuracy: 0.9632 - val\_loss: 0.0923 - val\_sparse\_categorical\_accuracy: 0.9711 - 52s/epoch - 112ms/step  
Epoch 68/100  
469/469 - 52s - loss: 0.1119 - sparse\_categorical\_accuracy: 0.9642 - val\_loss: 0.0884 - val\_sparse\_categorical\_accuracy: 0.9730 - 52s/epoch - 111ms/step  
Epoch 69/100  
469/469 - 52s - loss: 0.1079 - sparse\_categorical\_accuracy: 0.9653 - val\_loss: 0.0913 - val\_sparse\_categorical\_accuracy: 0.9727 - 52s/epoch - 112ms/step  
Epoch 70/100  
469/469 - 52s - loss: 0.1087 - sparse\_categorical\_accuracy: 0.9654 - val\_loss: 0.0891 - val\_sparse\_categorical\_accuracy: 0.9739 - 52s/epoch - 112ms/step  
Epoch 71/100  
469/469 - 53s - loss: 0.1083 - sparse\_categorical\_accuracy: 0.9654 - val\_loss: 0.0832 - val\_sparse\_categorical\_accuracy: 0.9756 - 53s/epoch - 112ms/step  
Epoch 72/100  
469/469 - 52s - loss: 0.1043 - sparse\_categorical\_accuracy: 0.9662 - val\_loss: 0.1004 - val\_sparse\_categorical\_accuracy: 0.9687 - 52s/epoch - 111ms/step  
Epoch 73/100  
469/469 - 52s - loss: 0.1045 - sparse\_categorical\_accuracy: 0.9662 - val\_loss: 0.0865 - val\_sparse\_categorical\_accuracy: 0.9738 - 52s/epoch - 111ms/step  
Epoch 74/100  
469/469 - 52s - loss: 0.1047 - sparse\_categorical\_accuracy: 0.9665 - val\_loss: 0.0930 - val\_sparse\_categorical\_accuracy: 0.9713 - 52s/epoch - 111ms/step  
Epoch 75/100  
469/469 - 52s - loss: 0.1052 - sparse\_categorical\_accuracy: 0.9660 - val\_loss: 0.0933 - val\_sparse\_categorical\_accuracy: 0.9711 - 52s/epoch - 112ms/step  
Epoch 76/100  
469/469 - 52s - loss: 0.1021 - sparse\_categorical\_accuracy: 0.9678 - val\_loss: 0.0816 - val\_sparse\_categorical\_accuracy: 0.9771 - 52s/epoch - 111ms/step  
Epoch 77/100  
469/469 - 52s - loss: 0.1025 - sparse\_categorical\_accuracy: 0.9668 - val\_loss: 0.0974 - val\_sparse\_categorical\_accuracy: 0.9695 - 52s/epoch - 112ms/step  
Epoch 78/100  
469/469 - 52s - loss: 0.1040 - sparse\_categorical\_accuracy: 0.9664 - val\_loss: 0.0810 - val\_sparse\_categorical\_accuracy: 0.9759 - 52s/epoch - 112ms/step  
Epoch 79/100  
469/469 - 52s - loss: 0.0991 - sparse\_categorical\_accuracy: 0.9679 - val\_loss: 0.0807 - val\_sparse\_categorical\_accuracy: 0.9744 - 52s/epoch - 112ms/step  
Epoch 80/100  
469/469 - 52s - loss: 0.1009 - sparse\_categorical\_accuracy: 0.9678 - val\_loss: 0.0836 - val\_sparse\_categorical\_accuracy: 0.9740 - 52s/epoch - 111ms/step

Epoch 81/100  
 469/469 - 53s - loss: 0.0993 - sparse\_categorical\_accuracy: 0.9683 - val\_loss: 0.0875 - val\_sparse\_categorical\_accuracy: 0.9728 - 53s/epoch - 112ms/step  
 Epoch 82/100  
 469/469 - 52s - loss: 0.0984 - sparse\_categorical\_accuracy: 0.9682 - val\_loss: 0.0822 - val\_sparse\_categorical\_accuracy: 0.9742 - 52s/epoch - 111ms/step  
 Epoch 83/100  
 469/469 - 52s - loss: 0.0973 - sparse\_categorical\_accuracy: 0.9690 - val\_loss: 0.0832 - val\_sparse\_categorical\_accuracy: 0.9749 - 52s/epoch - 112ms/step  
 Epoch 84/100  
 469/469 - 52s - loss: 0.0977 - sparse\_categorical\_accuracy: 0.9688 - val\_loss: 0.0889 - val\_sparse\_categorical\_accuracy: 0.9724 - 52s/epoch - 111ms/step  
 Epoch 85/100  
 469/469 - 52s - loss: 0.0981 - sparse\_categorical\_accuracy: 0.9690 - val\_loss: 0.0805 - val\_sparse\_categorical\_accuracy: 0.9743 - 52s/epoch - 112ms/step  
 Epoch 86/100  
 469/469 - 52s - loss: 0.0986 - sparse\_categorical\_accuracy: 0.9691 - val\_loss: 0.0850 - val\_sparse\_categorical\_accuracy: 0.9746 - 52s/epoch - 112ms/step  
 Epoch 87/100  
 469/469 - 52s - loss: 0.0981 - sparse\_categorical\_accuracy: 0.9682 - val\_loss: 0.0776 - val\_sparse\_categorical\_accuracy: 0.9763 - 52s/epoch - 112ms/step  
 Epoch 88/100  
 469/469 - 52s - loss: 0.0955 - sparse\_categorical\_accuracy: 0.9697 - val\_loss: 0.0806 - val\_sparse\_categorical\_accuracy: 0.9765 - 52s/epoch - 111ms/step  
 Epoch 89/100  
 469/469 - 52s - loss: 0.0955 - sparse\_categorical\_accuracy: 0.9697 - val\_loss: 0.0826 - val\_sparse\_categorical\_accuracy: 0.9738 - 52s/epoch - 112ms/step  
 Epoch 90/100  
 469/469 - 52s - loss: 0.0958 - sparse\_categorical\_accuracy: 0.9693 - val\_loss: 0.0792 - val\_sparse\_categorical\_accuracy: 0.9765 - 52s/epoch - 111ms/step  
 Epoch 91/100  
 469/469 - 52s - loss: 0.0957 - sparse\_categorical\_accuracy: 0.9691 - val\_loss: 0.0874 - val\_sparse\_categorical\_accuracy: 0.9732 - 52s/epoch - 111ms/step  
 Epoch 92/100  
 469/469 - 53s - loss: 0.0951 - sparse\_categorical\_accuracy: 0.9697 - val\_loss: 0.0842 - val\_sparse\_categorical\_accuracy: 0.9739 - 53s/epoch - 112ms/step  
 Epoch 93/100  
 469/469 - 52s - loss: 0.0929 - sparse\_categorical\_accuracy: 0.9696 - val\_loss: 0.0834 - val\_sparse\_categorical\_accuracy: 0.9750 - 52s/epoch - 112ms/step  
 Epoch 94/100  
 469/469 - 52s - loss: 0.0937 - sparse\_categorical\_accuracy: 0.9697 - val\_loss: 0.0840 - val\_sparse\_categorical\_accuracy: 0.9750 - 52s/epoch - 112ms/step  
 Epoch 95/100  
 469/469 - 52s - loss: 0.0930 - sparse\_categorical\_accuracy: 0.9704 - val\_loss: 0.0827 - val\_sparse\_categorical\_accuracy: 0.9747 - 52s/epoch - 112ms/step  
 Epoch 96/100  
 469/469 - 52s - loss: 0.0972 - sparse\_categorical\_accuracy: 0.9689 - val\_loss: 0.0783 - val\_sparse\_categorical\_accuracy: 0.9759 - 52s/epoch - 112ms/step  
 Epoch 97/100  
 469/469 - 52s - loss: 0.0928 - sparse\_categorical\_accuracy: 0.9703 - val\_loss: 0.0823 - val\_sparse\_categorical\_accuracy: 0.9746 - 52s/epoch - 112ms/step  
 Epoch 98/100  
 469/469 - 53s - loss: 0.0925 - sparse\_categorical\_accuracy: 0.9702 - val\_loss: 0.0815 - val\_sparse\_categorical\_accuracy: 0.9750 - 53s/epoch - 112ms/step  
 Epoch 99/100  
 469/469 - 52s - loss: 0.0929 - sparse\_categorical\_accuracy: 0.9706 - val\_loss: 0.0796 - val\_sparse\_categorical\_accuracy: 0.9753 - 52s/epoch - 112ms/step  
 Epoch 100/100  
 469/469 - 52s - loss: 0.0937 - sparse\_categorical\_accuracy: 0.9695 - val\_loss: 0.0802 - val\_sparse\_categorical\_accuracy: 0.9749 - 52s/epoch - 112ms/step

In [20]:

```
model3.evaluate(x_test, y_test, verbose=2)
```

313/313 - 4s - loss: 0.0802 - sparse\_categorical\_accuracy: 0.9749 - 4s/epoch - 13ms/step

Out[20]:

```
[0.0802013948559761, 0.9749000072479248]
```

**Model4:** adam optimizer with learning rate= $e^{-4}$ , random\_normal initializer, dropout regularization with rate=0.1.

In [21]:

```
input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                      filters_1x1=1,
                      filters_3x3_reduce=1,
                      filters_3x3=1,
                      filters_5x5_reduce=1,
                      filters_5x5=1,
                      filters_pool_proj=1,
                      name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.1)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_uniform')(x)
model4 = Model(input_layer, x, name='inception_v1')
```

In [22]:

```
model4.compile(optimizer=tf.keras.optimizers.Adam(0.0001),
               loss='sparse_categorical_crossentropy',
               metrics=['sparse_categorical_accuracy'])
```

In [23]:

```
history4 = model4.fit(x_train, y_train,
                      batch_size=128,
                      epochs=100,
                      validation_data=(x_test, y_test),
                      verbose=2)
```

```
Epoch 1/100
469/469 - 54s - loss: 2.0564 - sparse_categorical_accuracy: 0.4430 - val_loss: 1.7816 - val_sparse_c
ategorical_accuracy: 0.6562 - 54s/epoch - 114ms/step
Epoch 2/100
469/469 - 52s - loss: 1.5660 - sparse_categorical_accuracy: 0.7212 - val_loss: 1.2929 - val_sparse_c
ategorical_accuracy: 0.8171 - 52s/epoch - 112ms/step
Epoch 3/100
469/469 - 52s - loss: 1.1771 - sparse_categorical_accuracy: 0.8075 - val_loss: 0.9574 - val_sparse_c
ategorical_accuracy: 0.8673 - 52s/epoch - 112ms/step
Epoch 4/100
469/469 - 52s - loss: 0.8664 - sparse_categorical_accuracy: 0.8464 - val_loss: 0.6902 - val_sparse_c
ategorical_accuracy: 0.8890 - 52s/epoch - 112ms/step
Epoch 5/100
469/469 - 52s - loss: 0.6703 - sparse_categorical_accuracy: 0.8669 - val_loss: 0.5344 - val_sparse_c
ategorical_accuracy: 0.8998 - 52s/epoch - 111ms/step
Epoch 6/100
469/469 - 52s - loss: 0.5501 - sparse_categorical_accuracy: 0.8763 - val_loss: 0.4366 - val_sparse_c
ategorical_accuracy: 0.9092 - 52s/epoch - 112ms/step
Epoch 7/100
469/469 - 53s - loss: 0.4694 - sparse_categorical_accuracy: 0.8859 - val_loss: 0.3730 - val_sparse_c
ategorical_accuracy: 0.9162 - 53s/epoch - 112ms/step
Epoch 8/100
469/469 - 53s - loss: 0.4172 - sparse_categorical_accuracy: 0.8914 - val_loss: 0.3310 - val_sparse_c
ategorical_accuracy: 0.9208 - 53s/epoch - 112ms/step
Epoch 9/100
469/469 - 53s - loss: 0.3797 - sparse_categorical_accuracy: 0.8967 - val_loss: 0.2967 - val_sparse_c
ategorical_accuracy: 0.9236 - 53s/epoch - 112ms/step
Epoch 10/100
469/469 - 53s - loss: 0.3518 - sparse_categorical_accuracy: 0.9003 - val_loss: 0.2710 - val_sparse_c
ategorical_accuracy: 0.9289 - 53s/epoch - 112ms/step
Epoch 11/100
469/469 - 53s - loss: 0.3318 - sparse_categorical_accuracy: 0.9034 - val_loss: 0.2570 - val_sparse_c
ategorical_accuracy: 0.9279 - 53s/epoch - 113ms/step
Epoch 12/100
469/469 - 53s - loss: 0.3140 - sparse_categorical_accuracy: 0.9064 - val_loss: 0.2379 - val_sparse_c
ategorical_accuracy: 0.9337 - 53s/epoch - 112ms/step
Epoch 13/100
469/469 - 53s - loss: 0.3035 - sparse_categorical_accuracy: 0.9081 - val_loss: 0.2283 - val_sparse_c
ategorical_accuracy: 0.9350 - 53s/epoch - 112ms/step
Epoch 14/100
469/469 - 53s - loss: 0.2901 - sparse_categorical_accuracy: 0.9120 - val_loss: 0.2190 - val_sparse_c
ategorical_accuracy: 0.9363 - 53s/epoch - 112ms/step
Epoch 15/100
469/469 - 53s - loss: 0.2818 - sparse_categorical_accuracy: 0.9152 - val_loss: 0.2114 - val_sparse_c
ategorical_accuracy: 0.9384 - 53s/epoch - 113ms/step
Epoch 16/100
```

469/469 - 53s - loss: 0.2746 - sparse\_categorical\_accuracy: 0.9158 - val\_loss: 0.2031 - val\_sparse\_categorical\_accuracy: 0.9400 - 53s/epoch - 113ms/step  
Epoch 17/100  
469/469 - 53s - loss: 0.2683 - sparse\_categorical\_accuracy: 0.9164 - val\_loss: 0.1997 - val\_sparse\_categorical\_accuracy: 0.9398 - 53s/epoch - 112ms/step  
Epoch 18/100  
469/469 - 53s - loss: 0.2610 - sparse\_categorical\_accuracy: 0.9181 - val\_loss: 0.1923 - val\_sparse\_categorical\_accuracy: 0.9421 - 53s/epoch - 113ms/step  
Epoch 19/100  
469/469 - 53s - loss: 0.2549 - sparse\_categorical\_accuracy: 0.9204 - val\_loss: 0.1878 - val\_sparse\_categorical\_accuracy: 0.9423 - 53s/epoch - 112ms/step  
Epoch 20/100  
469/469 - 52s - loss: 0.2504 - sparse\_categorical\_accuracy: 0.9215 - val\_loss: 0.1822 - val\_sparse\_categorical\_accuracy: 0.9440 - 52s/epoch - 112ms/step  
Epoch 21/100  
469/469 - 53s - loss: 0.2444 - sparse\_categorical\_accuracy: 0.9238 - val\_loss: 0.1817 - val\_sparse\_categorical\_accuracy: 0.9441 - 53s/epoch - 113ms/step  
Epoch 22/100  
469/469 - 53s - loss: 0.2409 - sparse\_categorical\_accuracy: 0.9233 - val\_loss: 0.1769 - val\_sparse\_categorical\_accuracy: 0.9454 - 53s/epoch - 112ms/step  
Epoch 23/100  
469/469 - 52s - loss: 0.2377 - sparse\_categorical\_accuracy: 0.9254 - val\_loss: 0.1773 - val\_sparse\_categorical\_accuracy: 0.9455 - 52s/epoch - 112ms/step  
Epoch 24/100  
469/469 - 53s - loss: 0.2356 - sparse\_categorical\_accuracy: 0.9249 - val\_loss: 0.1710 - val\_sparse\_categorical\_accuracy: 0.9470 - 53s/epoch - 112ms/step  
Epoch 25/100  
469/469 - 53s - loss: 0.2306 - sparse\_categorical\_accuracy: 0.9264 - val\_loss: 0.1687 - val\_sparse\_categorical\_accuracy: 0.9482 - 53s/epoch - 112ms/step  
Epoch 26/100  
469/469 - 53s - loss: 0.2300 - sparse\_categorical\_accuracy: 0.9263 - val\_loss: 0.1636 - val\_sparse\_categorical\_accuracy: 0.9499 - 53s/epoch - 112ms/step  
Epoch 27/100  
469/469 - 53s - loss: 0.2252 - sparse\_categorical\_accuracy: 0.9281 - val\_loss: 0.1622 - val\_sparse\_categorical\_accuracy: 0.9499 - 53s/epoch - 113ms/step  
Epoch 28/100  
469/469 - 53s - loss: 0.2200 - sparse\_categorical\_accuracy: 0.9301 - val\_loss: 0.1631 - val\_sparse\_categorical\_accuracy: 0.9493 - 53s/epoch - 112ms/step  
Epoch 29/100  
469/469 - 53s - loss: 0.2179 - sparse\_categorical\_accuracy: 0.9305 - val\_loss: 0.1626 - val\_sparse\_categorical\_accuracy: 0.9486 - 53s/epoch - 112ms/step  
Epoch 30/100  
469/469 - 53s - loss: 0.2174 - sparse\_categorical\_accuracy: 0.9308 - val\_loss: 0.1589 - val\_sparse\_categorical\_accuracy: 0.9505 - 53s/epoch - 112ms/step  
Epoch 31/100  
469/469 - 53s - loss: 0.2154 - sparse\_categorical\_accuracy: 0.9323 - val\_loss: 0.1548 - val\_sparse\_categorical\_accuracy: 0.9519 - 53s/epoch - 112ms/step  
Epoch 32/100  
469/469 - 53s - loss: 0.2097 - sparse\_categorical\_accuracy: 0.9336 - val\_loss: 0.1531 - val\_sparse\_categorical\_accuracy: 0.9534 - 53s/epoch - 113ms/step  
Epoch 33/100  
469/469 - 53s - loss: 0.2108 - sparse\_categorical\_accuracy: 0.9327 - val\_loss: 0.1516 - val\_sparse\_categorical\_accuracy: 0.9531 - 53s/epoch - 113ms/step  
Epoch 34/100  
469/469 - 53s - loss: 0.2083 - sparse\_categorical\_accuracy: 0.9336 - val\_loss: 0.1518 - val\_sparse\_categorical\_accuracy: 0.9545 - 53s/epoch - 112ms/step  
Epoch 35/100  
469/469 - 53s - loss: 0.2055 - sparse\_categorical\_accuracy: 0.9346 - val\_loss: 0.1502 - val\_sparse\_categorical\_accuracy: 0.9538 - 53s/epoch - 112ms/step  
Epoch 36/100  
469/469 - 53s - loss: 0.2024 - sparse\_categorical\_accuracy: 0.9343 - val\_loss: 0.1466 - val\_sparse\_categorical\_accuracy: 0.9561 - 53s/epoch - 113ms/step  
Epoch 37/100  
469/469 - 53s - loss: 0.2037 - sparse\_categorical\_accuracy: 0.9346 - val\_loss: 0.1496 - val\_sparse\_categorical\_accuracy: 0.9536 - 53s/epoch - 112ms/step  
Epoch 38/100  
469/469 - 53s - loss: 0.2008 - sparse\_categorical\_accuracy: 0.9356 - val\_loss: 0.1483 - val\_sparse\_categorical\_accuracy: 0.9540 - 53s/epoch - 113ms/step  
Epoch 39/100  
469/469 - 53s - loss: 0.1960 - sparse\_categorical\_accuracy: 0.9367 - val\_loss: 0.1429 - val\_sparse\_categorical\_accuracy: 0.9573 - 53s/epoch - 112ms/step  
Epoch 40/100  
469/469 - 53s - loss: 0.1962 - sparse\_categorical\_accuracy: 0.9373 - val\_loss: 0.1417 - val\_sparse\_categorical\_accuracy: 0.9571 - 53s/epoch - 112ms/step  
Epoch 41/100  
469/469 - 53s - loss: 0.1930 - sparse\_categorical\_accuracy: 0.9378 - val\_loss: 0.1400 - val\_sparse\_categorical\_accuracy: 0.9593 - 53s/epoch - 112ms/step  
Epoch 42/100  
469/469 - 53s - loss: 0.1929 - sparse\_categorical\_accuracy: 0.9380 - val\_loss: 0.1372 - val\_sparse\_categorical\_accuracy: 0.9582 - 53s/epoch - 112ms/step  
Epoch 43/100  
469/469 - 53s - loss: 0.1920 - sparse\_categorical\_accuracy: 0.9388 - val\_loss: 0.1398 - val\_sparse\_categorical\_accuracy: 0.9571 - 53s/epoch - 113ms/step

```
Epoch 44/100
469/469 - 53s - loss: 0.1900 - sparse_categorical_accuracy: 0.9393 - val_loss: 0.1375 - val_sparse_c
ategorical_accuracy: 0.9567 - 53s/epoch - 113ms/step
Epoch 45/100
469/469 - 53s - loss: 0.1878 - sparse_categorical_accuracy: 0.9398 - val_loss: 0.1401 - val_sparse_c
ategorical_accuracy: 0.9574 - 53s/epoch - 112ms/step
Epoch 46/100
469/469 - 53s - loss: 0.1864 - sparse_categorical_accuracy: 0.9401 - val_loss: 0.1352 - val_sparse_c
ategorical_accuracy: 0.9594 - 53s/epoch - 112ms/step
Epoch 47/100
469/469 - 53s - loss: 0.1877 - sparse_categorical_accuracy: 0.9397 - val_loss: 0.1351 - val_sparse_c
ategorical_accuracy: 0.9596 - 53s/epoch - 112ms/step
Epoch 48/100
469/469 - 53s - loss: 0.1843 - sparse_categorical_accuracy: 0.9413 - val_loss: 0.1351 - val_sparse_c
ategorical_accuracy: 0.9590 - 53s/epoch - 112ms/step
Epoch 49/100
469/469 - 53s - loss: 0.1841 - sparse_categorical_accuracy: 0.9406 - val_loss: 0.1326 - val_sparse_c
ategorical_accuracy: 0.9591 - 53s/epoch - 113ms/step
Epoch 50/100
469/469 - 53s - loss: 0.1820 - sparse_categorical_accuracy: 0.9425 - val_loss: 0.1303 - val_sparse_c
ategorical_accuracy: 0.9610 - 53s/epoch - 113ms/step
Epoch 51/100
469/469 - 53s - loss: 0.1813 - sparse_categorical_accuracy: 0.9416 - val_loss: 0.1308 - val_sparse_c
ategorical_accuracy: 0.9595 - 53s/epoch - 113ms/step
Epoch 52/100
469/469 - 53s - loss: 0.1807 - sparse_categorical_accuracy: 0.9416 - val_loss: 0.1287 - val_sparse_c
ategorical_accuracy: 0.9607 - 53s/epoch - 112ms/step
Epoch 53/100
469/469 - 53s - loss: 0.1792 - sparse_categorical_accuracy: 0.9430 - val_loss: 0.1286 - val_sparse_c
ategorical_accuracy: 0.9605 - 53s/epoch - 112ms/step
Epoch 54/100
469/469 - 53s - loss: 0.1781 - sparse_categorical_accuracy: 0.9427 - val_loss: 0.1311 - val_sparse_c
ategorical_accuracy: 0.9595 - 53s/epoch - 112ms/step
Epoch 55/100
469/469 - 53s - loss: 0.1769 - sparse_categorical_accuracy: 0.9429 - val_loss: 0.1275 - val_sparse_c
ategorical_accuracy: 0.9619 - 53s/epoch - 113ms/step
Epoch 56/100
469/469 - 53s - loss: 0.1792 - sparse_categorical_accuracy: 0.9414 - val_loss: 0.1266 - val_sparse_c
ategorical_accuracy: 0.9626 - 53s/epoch - 113ms/step
Epoch 57/100
469/469 - 53s - loss: 0.1757 - sparse_categorical_accuracy: 0.9440 - val_loss: 0.1281 - val_sparse_c
ategorical_accuracy: 0.9616 - 53s/epoch - 112ms/step
Epoch 58/100
469/469 - 53s - loss: 0.1734 - sparse_categorical_accuracy: 0.9444 - val_loss: 0.1265 - val_sparse_c
ategorical_accuracy: 0.9615 - 53s/epoch - 113ms/step
Epoch 59/100
469/469 - 53s - loss: 0.1738 - sparse_categorical_accuracy: 0.9446 - val_loss: 0.1258 - val_sparse_c
ategorical_accuracy: 0.9628 - 53s/epoch - 113ms/step
Epoch 60/100
469/469 - 53s - loss: 0.1729 - sparse_categorical_accuracy: 0.9442 - val_loss: 0.1245 - val_sparse_c
ategorical_accuracy: 0.9618 - 53s/epoch - 113ms/step
Epoch 61/100
469/469 - 53s - loss: 0.1744 - sparse_categorical_accuracy: 0.9441 - val_loss: 0.1267 - val_sparse_c
ategorical_accuracy: 0.9623 - 53s/epoch - 114ms/step
Epoch 62/100
469/469 - 53s - loss: 0.1712 - sparse_categorical_accuracy: 0.9445 - val_loss: 0.1234 - val_sparse_c
ategorical_accuracy: 0.9623 - 53s/epoch - 113ms/step
Epoch 63/100
469/469 - 53s - loss: 0.1712 - sparse_categorical_accuracy: 0.9450 - val_loss: 0.1209 - val_sparse_c
ategorical_accuracy: 0.9628 - 53s/epoch - 113ms/step
Epoch 64/100
469/469 - 53s - loss: 0.1698 - sparse_categorical_accuracy: 0.9450 - val_loss: 0.1247 - val_sparse_c
ategorical_accuracy: 0.9636 - 53s/epoch - 112ms/step
Epoch 65/100
469/469 - 53s - loss: 0.1698 - sparse_categorical_accuracy: 0.9460 - val_loss: 0.1229 - val_sparse_c
ategorical_accuracy: 0.9615 - 53s/epoch - 113ms/step
Epoch 66/100
469/469 - 53s - loss: 0.1696 - sparse_categorical_accuracy: 0.9451 - val_loss: 0.1225 - val_sparse_c
ategorical_accuracy: 0.9620 - 53s/epoch - 113ms/step
Epoch 67/100
469/469 - 53s - loss: 0.1692 - sparse_categorical_accuracy: 0.9456 - val_loss: 0.1207 - val_sparse_c
ategorical_accuracy: 0.9638 - 53s/epoch - 113ms/step
Epoch 68/100
469/469 - 53s - loss: 0.1676 - sparse_categorical_accuracy: 0.9464 - val_loss: 0.1220 - val_sparse_c
ategorical_accuracy: 0.9637 - 53s/epoch - 112ms/step
Epoch 69/100
469/469 - 53s - loss: 0.1686 - sparse_categorical_accuracy: 0.9458 - val_loss: 0.1210 - val_sparse_c
ategorical_accuracy: 0.9640 - 53s/epoch - 113ms/step
Epoch 70/100
469/469 - 53s - loss: 0.1677 - sparse_categorical_accuracy: 0.9469 - val_loss: 0.1199 - val_sparse_c
ategorical_accuracy: 0.9638 - 53s/epoch - 112ms/step
Epoch 71/100
469/469 - 53s - loss: 0.1668 - sparse_categorical_accuracy: 0.9458 - val_loss: 0.1205 - val_sparse_c
```

ategorical\_accuracy: 0.9636 - 53s/epoch - 112ms/step  
Epoch 72/100  
469/469 - 53s - loss: 0.1644 - sparse\_categorical\_accuracy: 0.9456 - val\_loss: 0.1183 - val\_sparse\_c  
ategorical\_accuracy: 0.9647 - 53s/epoch - 113ms/step  
Epoch 73/100  
469/469 - 53s - loss: 0.1631 - sparse\_categorical\_accuracy: 0.9479 - val\_loss: 0.1203 - val\_sparse\_c  
ategorical\_accuracy: 0.9631 - 53s/epoch - 113ms/step  
Epoch 74/100  
469/469 - 53s - loss: 0.1663 - sparse\_categorical\_accuracy: 0.9468 - val\_loss: 0.1167 - val\_sparse\_c  
ategorical\_accuracy: 0.9641 - 53s/epoch - 113ms/step  
Epoch 75/100  
469/469 - 53s - loss: 0.1664 - sparse\_categorical\_accuracy: 0.9461 - val\_loss: 0.1182 - val\_sparse\_c  
ategorical\_accuracy: 0.9637 - 53s/epoch - 113ms/step  
Epoch 76/100  
469/469 - 53s - loss: 0.1656 - sparse\_categorical\_accuracy: 0.9464 - val\_loss: 0.1181 - val\_sparse\_c  
ategorical\_accuracy: 0.9650 - 53s/epoch - 113ms/step  
Epoch 77/100  
469/469 - 53s - loss: 0.1648 - sparse\_categorical\_accuracy: 0.9467 - val\_loss: 0.1183 - val\_sparse\_c  
ategorical\_accuracy: 0.9644 - 53s/epoch - 113ms/step  
Epoch 78/100  
469/469 - 53s - loss: 0.1640 - sparse\_categorical\_accuracy: 0.9478 - val\_loss: 0.1169 - val\_sparse\_c  
ategorical\_accuracy: 0.9637 - 53s/epoch - 113ms/step  
Epoch 79/100  
469/469 - 53s - loss: 0.1624 - sparse\_categorical\_accuracy: 0.9474 - val\_loss: 0.1158 - val\_sparse\_c  
ategorical\_accuracy: 0.9658 - 53s/epoch - 113ms/step  
Epoch 80/100  
469/469 - 53s - loss: 0.1609 - sparse\_categorical\_accuracy: 0.9488 - val\_loss: 0.1158 - val\_sparse\_c  
ategorical\_accuracy: 0.9662 - 53s/epoch - 113ms/step  
Epoch 81/100  
469/469 - 53s - loss: 0.1626 - sparse\_categorical\_accuracy: 0.9478 - val\_loss: 0.1159 - val\_sparse\_c  
ategorical\_accuracy: 0.9652 - 53s/epoch - 113ms/step  
Epoch 82/100  
469/469 - 53s - loss: 0.1620 - sparse\_categorical\_accuracy: 0.9480 - val\_loss: 0.1166 - val\_sparse\_c  
ategorical\_accuracy: 0.9645 - 53s/epoch - 113ms/step  
Epoch 83/100  
469/469 - 53s - loss: 0.1632 - sparse\_categorical\_accuracy: 0.9482 - val\_loss: 0.1150 - val\_sparse\_c  
ategorical\_accuracy: 0.9650 - 53s/epoch - 113ms/step  
Epoch 84/100  
469/469 - 57s - loss: 0.1595 - sparse\_categorical\_accuracy: 0.9488 - val\_loss: 0.1138 - val\_sparse\_c  
ategorical\_accuracy: 0.9655 - 57s/epoch - 122ms/step  
Epoch 85/100  
469/469 - 53s - loss: 0.1609 - sparse\_categorical\_accuracy: 0.9493 - val\_loss: 0.1140 - val\_sparse\_c  
ategorical\_accuracy: 0.9648 - 53s/epoch - 114ms/step  
Epoch 86/100  
469/469 - 53s - loss: 0.1610 - sparse\_categorical\_accuracy: 0.9486 - val\_loss: 0.1174 - val\_sparse\_c  
ategorical\_accuracy: 0.9644 - 53s/epoch - 113ms/step  
Epoch 87/100  
469/469 - 53s - loss: 0.1592 - sparse\_categorical\_accuracy: 0.9490 - val\_loss: 0.1160 - val\_sparse\_c  
ategorical\_accuracy: 0.9656 - 53s/epoch - 113ms/step  
Epoch 88/100  
469/469 - 53s - loss: 0.1617 - sparse\_categorical\_accuracy: 0.9484 - val\_loss: 0.1133 - val\_sparse\_c  
ategorical\_accuracy: 0.9663 - 53s/epoch - 112ms/step  
Epoch 89/100  
469/469 - 53s - loss: 0.1590 - sparse\_categorical\_accuracy: 0.9498 - val\_loss: 0.1162 - val\_sparse\_c  
ategorical\_accuracy: 0.9653 - 53s/epoch - 113ms/step  
Epoch 90/100  
469/469 - 53s - loss: 0.1567 - sparse\_categorical\_accuracy: 0.9496 - val\_loss: 0.1146 - val\_sparse\_c  
ategorical\_accuracy: 0.9658 - 53s/epoch - 113ms/step  
Epoch 91/100  
469/469 - 53s - loss: 0.1565 - sparse\_categorical\_accuracy: 0.9498 - val\_loss: 0.1148 - val\_sparse\_c  
ategorical\_accuracy: 0.9664 - 53s/epoch - 112ms/step  
Epoch 92/100  
469/469 - 53s - loss: 0.1559 - sparse\_categorical\_accuracy: 0.9492 - val\_loss: 0.1140 - val\_sparse\_c  
ategorical\_accuracy: 0.9654 - 53s/epoch - 112ms/step  
Epoch 93/100  
469/469 - 53s - loss: 0.1577 - sparse\_categorical\_accuracy: 0.9496 - val\_loss: 0.1135 - val\_sparse\_c  
ategorical\_accuracy: 0.9664 - 53s/epoch - 112ms/step  
Epoch 94/100  
469/469 - 53s - loss: 0.1562 - sparse\_categorical\_accuracy: 0.9496 - val\_loss: 0.1122 - val\_sparse\_c  
ategorical\_accuracy: 0.9663 - 53s/epoch - 113ms/step  
Epoch 95/100  
469/469 - 53s - loss: 0.1556 - sparse\_categorical\_accuracy: 0.9496 - val\_loss: 0.1135 - val\_sparse\_c  
ategorical\_accuracy: 0.9654 - 53s/epoch - 113ms/step  
Epoch 96/100  
469/469 - 53s - loss: 0.1554 - sparse\_categorical\_accuracy: 0.9505 - val\_loss: 0.1136 - val\_sparse\_c  
ategorical\_accuracy: 0.9659 - 53s/epoch - 112ms/step  
Epoch 97/100  
469/469 - 53s - loss: 0.1521 - sparse\_categorical\_accuracy: 0.9517 - val\_loss: 0.1123 - val\_sparse\_c  
ategorical\_accuracy: 0.9676 - 53s/epoch - 112ms/step  
Epoch 98/100  
469/469 - 53s - loss: 0.1557 - sparse\_categorical\_accuracy: 0.9499 - val\_loss: 0.1130 - val\_sparse\_c  
ategorical\_accuracy: 0.9665 - 53s/epoch - 112ms/step  
Epoch 99/100

469/469 - 53s - loss: 0.1556 - sparse\_categorical\_accuracy: 0.9494 - val\_loss: 0.1099 - val\_sparse\_categorical\_accuracy: 0.9667 - 53s/epoch - 112ms/step  
Epoch 100/100  
469/469 - 53s - loss: 0.1571 - sparse\_categorical\_accuracy: 0.9498 - val\_loss: 0.1114 - val\_sparse\_categorical\_accuracy: 0.9663 - 53s/epoch - 112ms/step

In [24]:

```
model4.evaluate(x_test, y_test, verbose=2)
```

313/313 - 4s - loss: 0.1114 - sparse\_categorical\_accuracy: 0.9663 - 4s/epoch - 13ms/step

Out[24]:

```
[0.11144724488258362, 0.9663000106811523]
```

**Model5: adam optimizer with learning rate= $e^{-3}$ , random\_uniform initializer, dropout regularization with rate=0.2.**

In [25]:

```
input_layer = Input(shape=(28, 28,1))  
x = inception_module(input_layer,  
                      filters_1x1=1,  
                      filters_3x3_reduce=1,  
                      filters_3x3=1,  
                      filters_5x5_reduce=1,  
                      filters_5x5=1,  
                      filters_pool_proj=1,  
                      name='inception_3a')  
x = tf.keras.layers.BatchNormalization()(x)  
x = MaxPool2D((3, 3))(x)  
x = tf.keras.layers.Flatten()(x)  
x = Dropout(0.2)(x)  
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)  
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)  
x = tf.keras.layers.BatchNormalization()(x)  
x = Dense(10, activation='softmax', kernel_initializer='random_uniform')(x)  
model5 = Model(input_layer, x, name='inception_v1')
```

In [26]:

```
model5.compile(optimizer=tf.keras.optimizers.Adam(0.001),  
               loss='sparse_categorical_crossentropy',  
               metrics=['sparse_categorical_accuracy'])
```

In [27]:

```
history5 = model5.fit(x_train, y_train,  
                      batch_size=128,  
                      epochs=100,  
                      validation_data=(x_test, y_test),  
                      verbose=2)
```

Epoch 1/100

469/469 - 54s - loss: 0.8432 - sparse\_categorical\_accuracy: 0.8047 - val\_loss: 0.2481 - val\_sparse\_categorical\_accuracy: 0.9427 - 54s/epoch - 115ms/step

Epoch 2/100

469/469 - 52s - loss: 0.2471 - sparse\_categorical\_accuracy: 0.9296 - val\_loss: 0.1435 - val\_sparse\_categorical\_accuracy: 0.9582 - 52s/epoch - 112ms/step

Epoch 3/100

469/469 - 53s - loss: 0.1998 - sparse\_categorical\_accuracy: 0.9379 - val\_loss: 0.1294 - val\_sparse\_categorical\_accuracy: 0.9611 - 53s/epoch - 112ms/step

Epoch 4/100

469/469 - 53s - loss: 0.1800 - sparse\_categorical\_accuracy: 0.9438 - val\_loss: 0.1117 - val\_sparse\_categorical\_accuracy: 0.9658 - 53s/epoch - 112ms/step

Epoch 5/100

469/469 - 53s - loss: 0.1727 - sparse\_categorical\_accuracy: 0.9458 - val\_loss: 0.1038 - val\_sparse\_categorical\_accuracy: 0.9680 - 53s/epoch - 112ms/step

Epoch 6/100

469/469 - 53s - loss: 0.1626 - sparse\_categorical\_accuracy: 0.9492 - val\_loss: 0.1076 - val\_sparse\_categorical\_accuracy: 0.9649 - 53s/epoch - 112ms/step

Epoch 7/100

469/469 - 56s - loss: 0.1601 - sparse\_categorical\_accuracy: 0.9491 - val\_loss: 0.1027 - val\_sparse\_categorical\_accuracy: 0.9667 - 56s/epoch - 120ms/step

Epoch 8/100

469/469 - 53s - loss: 0.1503 - sparse\_categorical\_accuracy: 0.9522 - val\_loss: 0.1003 - val\_sparse\_categorical\_accuracy: 0.9672 - 53s/epoch - 112ms/step

Epoch 9/100

469/469 - 54s - loss: 0.1465 - sparse\_categorical\_accuracy: 0.9539 - val\_loss: 0.0923 - val\_sparse\_categorical\_accuracy: 0.9706 - 54s/epoch - 114ms/step

```
Epoch 10/100
469/469 - 53s - loss: 0.1434 - sparse_categorical_accuracy: 0.9538 - val_loss: 0.0875 - val_sparse_c
ategorical_accuracy: 0.9718 - 53s/epoch - 112ms/step
Epoch 11/100
469/469 - 53s - loss: 0.1397 - sparse_categorical_accuracy: 0.9548 - val_loss: 0.0902 - val_sparse_c
ategorical_accuracy: 0.9705 - 53s/epoch - 113ms/step
Epoch 12/100
469/469 - 53s - loss: 0.1361 - sparse_categorical_accuracy: 0.9571 - val_loss: 0.0890 - val_sparse_c
ategorical_accuracy: 0.9708 - 53s/epoch - 112ms/step
Epoch 13/100
469/469 - 53s - loss: 0.1337 - sparse_categorical_accuracy: 0.9575 - val_loss: 0.0819 - val_sparse_c
ategorical_accuracy: 0.9733 - 53s/epoch - 112ms/step
Epoch 14/100
469/469 - 53s - loss: 0.1310 - sparse_categorical_accuracy: 0.9580 - val_loss: 0.0893 - val_sparse_c
ategorical_accuracy: 0.9712 - 53s/epoch - 112ms/step
Epoch 15/100
469/469 - 53s - loss: 0.1276 - sparse_categorical_accuracy: 0.9586 - val_loss: 0.0864 - val_sparse_c
ategorical_accuracy: 0.9711 - 53s/epoch - 112ms/step
Epoch 16/100
469/469 - 53s - loss: 0.1291 - sparse_categorical_accuracy: 0.9584 - val_loss: 0.0954 - val_sparse_c
ategorical_accuracy: 0.9691 - 53s/epoch - 112ms/step
Epoch 17/100
469/469 - 53s - loss: 0.1269 - sparse_categorical_accuracy: 0.9587 - val_loss: 0.0829 - val_sparse_c
ategorical_accuracy: 0.9730 - 53s/epoch - 113ms/step
Epoch 18/100
469/469 - 53s - loss: 0.1221 - sparse_categorical_accuracy: 0.9603 - val_loss: 0.0758 - val_sparse_c
ategorical_accuracy: 0.9752 - 53s/epoch - 112ms/step
Epoch 19/100
469/469 - 53s - loss: 0.1239 - sparse_categorical_accuracy: 0.9596 - val_loss: 0.0798 - val_sparse_c
ategorical_accuracy: 0.9750 - 53s/epoch - 113ms/step
Epoch 20/100
469/469 - 53s - loss: 0.1234 - sparse_categorical_accuracy: 0.9601 - val_loss: 0.0835 - val_sparse_c
ategorical_accuracy: 0.9743 - 53s/epoch - 112ms/step
Epoch 21/100
469/469 - 53s - loss: 0.1208 - sparse_categorical_accuracy: 0.9610 - val_loss: 0.0765 - val_sparse_c
ategorical_accuracy: 0.9760 - 53s/epoch - 113ms/step
Epoch 22/100
469/469 - 53s - loss: 0.1206 - sparse_categorical_accuracy: 0.9613 - val_loss: 0.0772 - val_sparse_c
ategorical_accuracy: 0.9753 - 53s/epoch - 112ms/step
Epoch 23/100
469/469 - 53s - loss: 0.1171 - sparse_categorical_accuracy: 0.9621 - val_loss: 0.0789 - val_sparse_c
ategorical_accuracy: 0.9740 - 53s/epoch - 113ms/step
Epoch 24/100
469/469 - 53s - loss: 0.1164 - sparse_categorical_accuracy: 0.9614 - val_loss: 0.0737 - val_sparse_c
ategorical_accuracy: 0.9764 - 53s/epoch - 113ms/step
Epoch 25/100
469/469 - 53s - loss: 0.1160 - sparse_categorical_accuracy: 0.9628 - val_loss: 0.0708 - val_sparse_c
ategorical_accuracy: 0.9785 - 53s/epoch - 113ms/step
Epoch 26/100
469/469 - 53s - loss: 0.1164 - sparse_categorical_accuracy: 0.9622 - val_loss: 0.0730 - val_sparse_c
ategorical_accuracy: 0.9764 - 53s/epoch - 113ms/step
Epoch 27/100
469/469 - 53s - loss: 0.1176 - sparse_categorical_accuracy: 0.9617 - val_loss: 0.0715 - val_sparse_c
ategorical_accuracy: 0.9775 - 53s/epoch - 112ms/step
Epoch 28/100
469/469 - 53s - loss: 0.1140 - sparse_categorical_accuracy: 0.9635 - val_loss: 0.0771 - val_sparse_c
ategorical_accuracy: 0.9749 - 53s/epoch - 113ms/step
Epoch 29/100
469/469 - 53s - loss: 0.1110 - sparse_categorical_accuracy: 0.9638 - val_loss: 0.0765 - val_sparse_c
ategorical_accuracy: 0.9753 - 53s/epoch - 113ms/step
Epoch 30/100
469/469 - 53s - loss: 0.1129 - sparse_categorical_accuracy: 0.9632 - val_loss: 0.0710 - val_sparse_c
ategorical_accuracy: 0.9770 - 53s/epoch - 112ms/step
Epoch 31/100
469/469 - 53s - loss: 0.1128 - sparse_categorical_accuracy: 0.9633 - val_loss: 0.0700 - val_sparse_c
ategorical_accuracy: 0.9777 - 53s/epoch - 112ms/step
Epoch 32/100
469/469 - 53s - loss: 0.1108 - sparse_categorical_accuracy: 0.9644 - val_loss: 0.0692 - val_sparse_c
ategorical_accuracy: 0.9779 - 53s/epoch - 113ms/step
Epoch 33/100
469/469 - 53s - loss: 0.1120 - sparse_categorical_accuracy: 0.9634 - val_loss: 0.0767 - val_sparse_c
ategorical_accuracy: 0.9750 - 53s/epoch - 112ms/step
Epoch 34/100
469/469 - 53s - loss: 0.1095 - sparse_categorical_accuracy: 0.9642 - val_loss: 0.0765 - val_sparse_c
ategorical_accuracy: 0.9764 - 53s/epoch - 113ms/step
Epoch 35/100
469/469 - 53s - loss: 0.1119 - sparse_categorical_accuracy: 0.9646 - val_loss: 0.0778 - val_sparse_c
ategorical_accuracy: 0.9749 - 53s/epoch - 112ms/step
Epoch 36/100
469/469 - 53s - loss: 0.1110 - sparse_categorical_accuracy: 0.9637 - val_loss: 0.0715 - val_sparse_c
ategorical_accuracy: 0.9757 - 53s/epoch - 112ms/step
Epoch 37/100
469/469 - 53s - loss: 0.1082 - sparse_categorical_accuracy: 0.9644 - val_loss: 0.0749 - val_sparse_c
```



[illegible]

[illegible]

Epoch 93/100  
 469/469 - 53s - loss: 0.0969 - sparse\_categorical\_accuracy: 0.9679 - val\_loss: 0.0637 - val\_sparse\_categorical\_accuracy: 0.9788 - 53s/epoch - 112ms/step  
 Epoch 94/100  
 469/469 - 53s - loss: 0.0968 - sparse\_categorical\_accuracy: 0.9688 - val\_loss: 0.0647 - val\_sparse\_categorical\_accuracy: 0.9787 - 53s/epoch - 112ms/step  
 Epoch 95/100  
 469/469 - 52s - loss: 0.0937 - sparse\_categorical\_accuracy: 0.9690 - val\_loss: 0.0629 - val\_sparse\_categorical\_accuracy: 0.9794 - 52s/epoch - 112ms/step  
 Epoch 96/100  
 469/469 - 53s - loss: 0.0950 - sparse\_categorical\_accuracy: 0.9692 - val\_loss: 0.0627 - val\_sparse\_categorical\_accuracy: 0.9793 - 53s/epoch - 112ms/step  
 Epoch 97/100  
 469/469 - 53s - loss: 0.0945 - sparse\_categorical\_accuracy: 0.9690 - val\_loss: 0.0619 - val\_sparse\_categorical\_accuracy: 0.9808 - 53s/epoch - 112ms/step  
 Epoch 98/100  
 469/469 - 53s - loss: 0.0921 - sparse\_categorical\_accuracy: 0.9699 - val\_loss: 0.0635 - val\_sparse\_categorical\_accuracy: 0.9788 - 53s/epoch - 112ms/step  
 Epoch 99/100  
 469/469 - 53s - loss: 0.0972 - sparse\_categorical\_accuracy: 0.9688 - val\_loss: 0.0603 - val\_sparse\_categorical\_accuracy: 0.9804 - 53s/epoch - 113ms/step  
 Epoch 100/100  
 469/469 - 53s - loss: 0.0958 - sparse\_categorical\_accuracy: 0.9687 - val\_loss: 0.0614 - val\_sparse\_categorical\_accuracy: 0.9794 - 53s/epoch - 113ms/step

In [28]:

```
model5.evaluate(x_test, y_test, verbose=2)
```

313/313 - 4s - loss: 0.0614 - sparse\_categorical\_accuracy: 0.9794 - 4s/epoch - 13ms/step

Out[28]:

```
[0.0613691546022892, 0.9793999791145325]
```

**Model6: adam optimizer with learning rate= $e^{-4}$ , random\_uniform initializer, dropout regularization with rate=0.2.**

In [29]:

```
input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                     filters_1x1=1,
                     filters_3x3_reduce=1,
                     filters_3x3=1,
                     filters_5x5_reduce=1,
                     filters_5x5=1,
                     filters_pool_proj=1,
                     name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.2)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_uniform')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_uniform')(x)
model6 = Model(input_layer, x, name='inception_v1')
```

In [30]:

```
model6.compile(optimizer=tf.keras.optimizers.Adam(0.0001),
              loss='sparse_categorical_crossentropy',
              metrics=['sparse_categorical_accuracy'])
```

In [31]:

```
history6 = model6.fit(x_train, y_train,
                    batch_size=128,
                    epochs=100,
                    validation_data=(x_test, y_test),
                    verbose=2)
```

Epoch 1/100  
 469/469 - 54s - loss: 2.0855 - sparse\_categorical\_accuracy: 0.4488 - val\_loss: 1.8832 - val\_sparse\_categorical\_accuracy: 0.6610 - 54s/epoch - 115ms/step  
 Epoch 2/100  
 469/469 - 53s - loss: 1.6718 - sparse\_categorical\_accuracy: 0.6506 - val\_loss: 1.4267 - val\_sparse\_categorical\_accuracy: 0.7515 - 53s/epoch - 113ms/step  
 Epoch 3/100  
 469/469 - 53s - loss: 1.3215 - sparse\_categorical\_accuracy: 0.7239 - val\_loss: 1.0785 - val\_sparse\_c

ategorical accuracy: 0.8166 - 53s/epoch - 112ms/step  
Epoch 4/100  
469/469 - 53s - loss: 1.0307 - sparse\_categorical\_accuracy: 0.7755 - val\_loss: 0.8302 - val\_sparse\_c  
ategorical accuracy: 0.8522 - 53s/epoch - 113ms/step  
Epoch 5/100  
469/469 - 53s - loss: 0.8388 - sparse\_categorical\_accuracy: 0.8053 - val\_loss: 0.6562 - val\_sparse\_c  
ategorical accuracy: 0.8659 - 53s/epoch - 112ms/step  
Epoch 6/100  
469/469 - 53s - loss: 0.6993 - sparse\_categorical\_accuracy: 0.8195 - val\_loss: 0.5278 - val\_sparse\_c  
ategorical accuracy: 0.8772 - 53s/epoch - 112ms/step  
Epoch 7/100  
469/469 - 53s - loss: 0.6142 - sparse\_categorical\_accuracy: 0.8294 - val\_loss: 0.4651 - val\_sparse\_c  
ategorical accuracy: 0.8841 - 53s/epoch - 113ms/step  
Epoch 8/100  
469/469 - 53s - loss: 0.5653 - sparse\_categorical\_accuracy: 0.8353 - val\_loss: 0.4191 - val\_sparse\_c  
ategorical accuracy: 0.8912 - 53s/epoch - 114ms/step  
Epoch 9/100  
469/469 - 53s - loss: 0.5342 - sparse\_categorical\_accuracy: 0.8395 - val\_loss: 0.3901 - val\_sparse\_c  
ategorical accuracy: 0.8932 - 53s/epoch - 113ms/step  
Epoch 10/100  
469/469 - 53s - loss: 0.5130 - sparse\_categorical\_accuracy: 0.8440 - val\_loss: 0.3730 - val\_sparse\_c  
ategorical accuracy: 0.8950 - 53s/epoch - 113ms/step  
Epoch 11/100  
469/469 - 53s - loss: 0.4925 - sparse\_categorical\_accuracy: 0.8468 - val\_loss: 0.3521 - val\_sparse\_c  
ategorical accuracy: 0.9011 - 53s/epoch - 113ms/step  
Epoch 12/100  
469/469 - 53s - loss: 0.4842 - sparse\_categorical\_accuracy: 0.8464 - val\_loss: 0.3451 - val\_sparse\_c  
ategorical accuracy: 0.9017 - 53s/epoch - 113ms/step  
Epoch 13/100  
469/469 - 53s - loss: 0.4734 - sparse\_categorical\_accuracy: 0.8513 - val\_loss: 0.3348 - val\_sparse\_c  
ategorical accuracy: 0.9015 - 53s/epoch - 114ms/step  
Epoch 14/100  
469/469 - 53s - loss: 0.4612 - sparse\_categorical\_accuracy: 0.8531 - val\_loss: 0.3244 - val\_sparse\_c  
ategorical accuracy: 0.9048 - 53s/epoch - 114ms/step  
Epoch 15/100  
469/469 - 53s - loss: 0.4553 - sparse\_categorical\_accuracy: 0.8544 - val\_loss: 0.3211 - val\_sparse\_c  
ategorical accuracy: 0.9051 - 53s/epoch - 113ms/step  
Epoch 16/100  
469/469 - 53s - loss: 0.4479 - sparse\_categorical\_accuracy: 0.8541 - val\_loss: 0.3109 - val\_sparse\_c  
ategorical accuracy: 0.9080 - 53s/epoch - 113ms/step  
Epoch 17/100  
469/469 - 53s - loss: 0.4383 - sparse\_categorical\_accuracy: 0.8589 - val\_loss: 0.3030 - val\_sparse\_c  
ategorical accuracy: 0.9077 - 53s/epoch - 113ms/step  
Epoch 18/100  
469/469 - 53s - loss: 0.4352 - sparse\_categorical\_accuracy: 0.8596 - val\_loss: 0.2985 - val\_sparse\_c  
ategorical accuracy: 0.9096 - 53s/epoch - 113ms/step  
Epoch 19/100  
469/469 - 53s - loss: 0.4286 - sparse\_categorical\_accuracy: 0.8599 - val\_loss: 0.2936 - val\_sparse\_c  
ategorical accuracy: 0.9102 - 53s/epoch - 114ms/step  
Epoch 20/100  
469/469 - 53s - loss: 0.4285 - sparse\_categorical\_accuracy: 0.8608 - val\_loss: 0.2929 - val\_sparse\_c  
ategorical accuracy: 0.9095 - 53s/epoch - 113ms/step  
Epoch 21/100  
469/469 - 53s - loss: 0.4194 - sparse\_categorical\_accuracy: 0.8641 - val\_loss: 0.2874 - val\_sparse\_c  
ategorical accuracy: 0.9116 - 53s/epoch - 113ms/step  
Epoch 22/100  
469/469 - 53s - loss: 0.4229 - sparse\_categorical\_accuracy: 0.8625 - val\_loss: 0.2858 - val\_sparse\_c  
ategorical accuracy: 0.9120 - 53s/epoch - 113ms/step  
Epoch 23/100  
469/469 - 53s - loss: 0.4164 - sparse\_categorical\_accuracy: 0.8638 - val\_loss: 0.2829 - val\_sparse\_c  
ategorical accuracy: 0.9127 - 53s/epoch - 113ms/step  
Epoch 24/100  
469/469 - 53s - loss: 0.4129 - sparse\_categorical\_accuracy: 0.8663 - val\_loss: 0.2919 - val\_sparse\_c  
ategorical accuracy: 0.9073 - 53s/epoch - 113ms/step  
Epoch 25/100  
469/469 - 53s - loss: 0.4074 - sparse\_categorical\_accuracy: 0.8669 - val\_loss: 0.2788 - val\_sparse\_c  
ategorical accuracy: 0.9121 - 53s/epoch - 114ms/step  
Epoch 26/100  
469/469 - 53s - loss: 0.4066 - sparse\_categorical\_accuracy: 0.8666 - val\_loss: 0.2714 - val\_sparse\_c  
ategorical accuracy: 0.9151 - 53s/epoch - 113ms/step  
Epoch 27/100  
469/469 - 53s - loss: 0.4023 - sparse\_categorical\_accuracy: 0.8695 - val\_loss: 0.2664 - val\_sparse\_c  
ategorical accuracy: 0.9166 - 53s/epoch - 113ms/step  
Epoch 28/100  
469/469 - 53s - loss: 0.3986 - sparse\_categorical\_accuracy: 0.8692 - val\_loss: 0.2745 - val\_sparse\_c  
ategorical accuracy: 0.9130 - 53s/epoch - 113ms/step  
Epoch 29/100  
469/469 - 53s - loss: 0.3935 - sparse\_categorical\_accuracy: 0.8724 - val\_loss: 0.2711 - val\_sparse\_c  
ategorical accuracy: 0.9144 - 53s/epoch - 113ms/step  
Epoch 30/100  
469/469 - 53s - loss: 0.3908 - sparse\_categorical\_accuracy: 0.8716 - val\_loss: 0.2632 - val\_sparse\_c  
ategorical accuracy: 0.9170 - 53s/epoch - 114ms/step  
Epoch 31/100

469/469 - 53s - loss: 0.3878 - sparse\_categorical\_accuracy: 0.8735 - val\_loss: 0.2658 - val\_sparse\_categorical\_accuracy: 0.9153 - 53s/epoch - 114ms/step  
Epoch 32/100  
469/469 - 53s - loss: 0.3882 - sparse\_categorical\_accuracy: 0.8737 - val\_loss: 0.2604 - val\_sparse\_categorical\_accuracy: 0.9167 - 53s/epoch - 114ms/step  
Epoch 33/100  
469/469 - 53s - loss: 0.3811 - sparse\_categorical\_accuracy: 0.8761 - val\_loss: 0.2533 - val\_sparse\_categorical\_accuracy: 0.9211 - 53s/epoch - 114ms/step  
Epoch 34/100  
469/469 - 53s - loss: 0.3848 - sparse\_categorical\_accuracy: 0.8737 - val\_loss: 0.2555 - val\_sparse\_categorical\_accuracy: 0.9189 - 53s/epoch - 113ms/step  
Epoch 35/100  
469/469 - 53s - loss: 0.3778 - sparse\_categorical\_accuracy: 0.8762 - val\_loss: 0.2534 - val\_sparse\_categorical\_accuracy: 0.9193 - 53s/epoch - 112ms/step  
Epoch 36/100  
469/469 - 53s - loss: 0.3716 - sparse\_categorical\_accuracy: 0.8789 - val\_loss: 0.2492 - val\_sparse\_categorical\_accuracy: 0.9218 - 53s/epoch - 114ms/step  
Epoch 37/100  
469/469 - 53s - loss: 0.3721 - sparse\_categorical\_accuracy: 0.8789 - val\_loss: 0.2484 - val\_sparse\_categorical\_accuracy: 0.9212 - 53s/epoch - 114ms/step  
Epoch 38/100  
469/469 - 53s - loss: 0.3710 - sparse\_categorical\_accuracy: 0.8796 - val\_loss: 0.2442 - val\_sparse\_categorical\_accuracy: 0.9229 - 53s/epoch - 113ms/step  
Epoch 39/100  
469/469 - 53s - loss: 0.3662 - sparse\_categorical\_accuracy: 0.8809 - val\_loss: 0.2373 - val\_sparse\_categorical\_accuracy: 0.9259 - 53s/epoch - 113ms/step  
Epoch 40/100  
469/469 - 53s - loss: 0.3593 - sparse\_categorical\_accuracy: 0.8839 - val\_loss: 0.2393 - val\_sparse\_categorical\_accuracy: 0.9230 - 53s/epoch - 114ms/step  
Epoch 41/100  
469/469 - 53s - loss: 0.3586 - sparse\_categorical\_accuracy: 0.8838 - val\_loss: 0.2359 - val\_sparse\_categorical\_accuracy: 0.9242 - 53s/epoch - 113ms/step  
Epoch 42/100  
469/469 - 54s - loss: 0.3509 - sparse\_categorical\_accuracy: 0.8872 - val\_loss: 0.2356 - val\_sparse\_categorical\_accuracy: 0.9254 - 54s/epoch - 114ms/step  
Epoch 43/100  
469/469 - 54s - loss: 0.3441 - sparse\_categorical\_accuracy: 0.8891 - val\_loss: 0.2309 - val\_sparse\_categorical\_accuracy: 0.9287 - 54s/epoch - 114ms/step  
Epoch 44/100  
469/469 - 53s - loss: 0.3358 - sparse\_categorical\_accuracy: 0.8913 - val\_loss: 0.2327 - val\_sparse\_categorical\_accuracy: 0.9247 - 53s/epoch - 113ms/step  
Epoch 45/100  
469/469 - 53s - loss: 0.3334 - sparse\_categorical\_accuracy: 0.8919 - val\_loss: 0.2203 - val\_sparse\_categorical\_accuracy: 0.9323 - 53s/epoch - 113ms/step  
Epoch 46/100  
469/469 - 53s - loss: 0.3231 - sparse\_categorical\_accuracy: 0.8963 - val\_loss: 0.2160 - val\_sparse\_categorical\_accuracy: 0.9334 - 53s/epoch - 113ms/step  
Epoch 47/100  
469/469 - 53s - loss: 0.3105 - sparse\_categorical\_accuracy: 0.9007 - val\_loss: 0.2097 - val\_sparse\_categorical\_accuracy: 0.9355 - 53s/epoch - 114ms/step  
Epoch 48/100  
469/469 - 53s - loss: 0.3008 - sparse\_categorical\_accuracy: 0.9026 - val\_loss: 0.2008 - val\_sparse\_categorical\_accuracy: 0.9377 - 53s/epoch - 113ms/step  
Epoch 49/100  
469/469 - 53s - loss: 0.2933 - sparse\_categorical\_accuracy: 0.9046 - val\_loss: 0.2002 - val\_sparse\_categorical\_accuracy: 0.9368 - 53s/epoch - 114ms/step  
Epoch 50/100  
469/469 - 53s - loss: 0.2813 - sparse\_categorical\_accuracy: 0.9102 - val\_loss: 0.1913 - val\_sparse\_categorical\_accuracy: 0.9424 - 53s/epoch - 113ms/step  
Epoch 51/100  
469/469 - 53s - loss: 0.2705 - sparse\_categorical\_accuracy: 0.9140 - val\_loss: 0.1869 - val\_sparse\_categorical\_accuracy: 0.9419 - 53s/epoch - 113ms/step  
Epoch 52/100  
469/469 - 53s - loss: 0.2678 - sparse\_categorical\_accuracy: 0.9151 - val\_loss: 0.1839 - val\_sparse\_categorical\_accuracy: 0.9434 - 53s/epoch - 113ms/step  
Epoch 53/100  
469/469 - 53s - loss: 0.2629 - sparse\_categorical\_accuracy: 0.9157 - val\_loss: 0.1849 - val\_sparse\_categorical\_accuracy: 0.9410 - 53s/epoch - 114ms/step  
Epoch 54/100  
469/469 - 53s - loss: 0.2551 - sparse\_categorical\_accuracy: 0.9191 - val\_loss: 0.1746 - val\_sparse\_categorical\_accuracy: 0.9461 - 53s/epoch - 113ms/step  
Epoch 55/100  
469/469 - 53s - loss: 0.2547 - sparse\_categorical\_accuracy: 0.9189 - val\_loss: 0.1732 - val\_sparse\_categorical\_accuracy: 0.9448 - 53s/epoch - 113ms/step  
Epoch 56/100  
469/469 - 53s - loss: 0.2527 - sparse\_categorical\_accuracy: 0.9204 - val\_loss: 0.1726 - val\_sparse\_categorical\_accuracy: 0.9464 - 53s/epoch - 113ms/step  
Epoch 57/100  
469/469 - 53s - loss: 0.2455 - sparse\_categorical\_accuracy: 0.9212 - val\_loss: 0.1645 - val\_sparse\_categorical\_accuracy: 0.9479 - 53s/epoch - 113ms/step  
Epoch 58/100  
469/469 - 53s - loss: 0.2431 - sparse\_categorical\_accuracy: 0.9231 - val\_loss: 0.1632 - val\_sparse\_categorical\_accuracy: 0.9491 - 53s/epoch - 113ms/step

Epoch 59/100  
469/469 - 53s - loss: 0.2376 - sparse\_categorical\_accuracy: 0.9252 - val\_loss: 0.1637 - val\_sparse\_categorical\_accuracy: 0.9470 - 53s/epoch - 114ms/step

Epoch 60/100  
469/469 - 53s - loss: 0.2367 - sparse\_categorical\_accuracy: 0.9247 - val\_loss: 0.1689 - val\_sparse\_categorical\_accuracy: 0.9465 - 53s/epoch - 114ms/step

Epoch 61/100  
469/469 - 53s - loss: 0.2320 - sparse\_categorical\_accuracy: 0.9269 - val\_loss: 0.1601 - val\_sparse\_categorical\_accuracy: 0.9493 - 53s/epoch - 114ms/step

Epoch 62/100  
469/469 - 53s - loss: 0.2325 - sparse\_categorical\_accuracy: 0.9262 - val\_loss: 0.1660 - val\_sparse\_categorical\_accuracy: 0.9489 - 53s/epoch - 113ms/step

Epoch 63/100  
469/469 - 53s - loss: 0.2261 - sparse\_categorical\_accuracy: 0.9283 - val\_loss: 0.1548 - val\_sparse\_categorical\_accuracy: 0.9526 - 53s/epoch - 113ms/step

Epoch 64/100  
469/469 - 53s - loss: 0.2244 - sparse\_categorical\_accuracy: 0.9289 - val\_loss: 0.1536 - val\_sparse\_categorical\_accuracy: 0.9518 - 53s/epoch - 114ms/step

Epoch 65/100  
469/469 - 53s - loss: 0.2206 - sparse\_categorical\_accuracy: 0.9293 - val\_loss: 0.1485 - val\_sparse\_categorical\_accuracy: 0.9548 - 53s/epoch - 114ms/step

Epoch 66/100  
469/469 - 54s - loss: 0.2189 - sparse\_categorical\_accuracy: 0.9309 - val\_loss: 0.1476 - val\_sparse\_categorical\_accuracy: 0.9551 - 54s/epoch - 114ms/step

Epoch 67/100  
469/469 - 53s - loss: 0.2149 - sparse\_categorical\_accuracy: 0.9315 - val\_loss: 0.1466 - val\_sparse\_categorical\_accuracy: 0.9555 - 53s/epoch - 114ms/step

Epoch 68/100  
469/469 - 53s - loss: 0.2131 - sparse\_categorical\_accuracy: 0.9322 - val\_loss: 0.1465 - val\_sparse\_categorical\_accuracy: 0.9561 - 53s/epoch - 113ms/step

Epoch 69/100  
469/469 - 53s - loss: 0.2122 - sparse\_categorical\_accuracy: 0.9328 - val\_loss: 0.1441 - val\_sparse\_categorical\_accuracy: 0.9571 - 53s/epoch - 113ms/step

Epoch 70/100  
469/469 - 53s - loss: 0.2110 - sparse\_categorical\_accuracy: 0.9335 - val\_loss: 0.1453 - val\_sparse\_categorical\_accuracy: 0.9547 - 53s/epoch - 113ms/step

Epoch 71/100  
469/469 - 53s - loss: 0.2064 - sparse\_categorical\_accuracy: 0.9348 - val\_loss: 0.1447 - val\_sparse\_categorical\_accuracy: 0.9554 - 53s/epoch - 113ms/step

Epoch 72/100  
469/469 - 53s - loss: 0.2046 - sparse\_categorical\_accuracy: 0.9348 - val\_loss: 0.1365 - val\_sparse\_categorical\_accuracy: 0.9589 - 53s/epoch - 113ms/step

Epoch 73/100  
469/469 - 53s - loss: 0.2034 - sparse\_categorical\_accuracy: 0.9351 - val\_loss: 0.1347 - val\_sparse\_categorical\_accuracy: 0.9573 - 53s/epoch - 113ms/step

Epoch 74/100  
469/469 - 53s - loss: 0.2018 - sparse\_categorical\_accuracy: 0.9351 - val\_loss: 0.1358 - val\_sparse\_categorical\_accuracy: 0.9582 - 53s/epoch - 113ms/step

Epoch 75/100  
469/469 - 53s - loss: 0.1982 - sparse\_categorical\_accuracy: 0.9377 - val\_loss: 0.1338 - val\_sparse\_categorical\_accuracy: 0.9571 - 53s/epoch - 114ms/step

Epoch 76/100  
469/469 - 53s - loss: 0.1963 - sparse\_categorical\_accuracy: 0.9381 - val\_loss: 0.1309 - val\_sparse\_categorical\_accuracy: 0.9604 - 53s/epoch - 113ms/step

Epoch 77/100  
469/469 - 53s - loss: 0.1959 - sparse\_categorical\_accuracy: 0.9384 - val\_loss: 0.1331 - val\_sparse\_categorical\_accuracy: 0.9595 - 53s/epoch - 113ms/step

Epoch 78/100  
469/469 - 53s - loss: 0.1929 - sparse\_categorical\_accuracy: 0.9395 - val\_loss: 0.1293 - val\_sparse\_categorical\_accuracy: 0.9609 - 53s/epoch - 113ms/step

Epoch 79/100  
469/469 - 53s - loss: 0.1926 - sparse\_categorical\_accuracy: 0.9400 - val\_loss: 0.1261 - val\_sparse\_categorical\_accuracy: 0.9628 - 53s/epoch - 113ms/step

Epoch 80/100  
469/469 - 53s - loss: 0.1907 - sparse\_categorical\_accuracy: 0.9396 - val\_loss: 0.1258 - val\_sparse\_categorical\_accuracy: 0.9608 - 53s/epoch - 114ms/step

Epoch 81/100  
469/469 - 54s - loss: 0.1902 - sparse\_categorical\_accuracy: 0.9387 - val\_loss: 0.1310 - val\_sparse\_categorical\_accuracy: 0.9598 - 54s/epoch - 114ms/step

Epoch 82/100  
469/469 - 53s - loss: 0.1888 - sparse\_categorical\_accuracy: 0.9395 - val\_loss: 0.1252 - val\_sparse\_categorical\_accuracy: 0.9611 - 53s/epoch - 113ms/step

Epoch 83/100  
469/469 - 53s - loss: 0.1900 - sparse\_categorical\_accuracy: 0.9391 - val\_loss: 0.1241 - val\_sparse\_categorical\_accuracy: 0.9619 - 53s/epoch - 114ms/step

Epoch 84/100  
469/469 - 53s - loss: 0.1863 - sparse\_categorical\_accuracy: 0.9404 - val\_loss: 0.1236 - val\_sparse\_categorical\_accuracy: 0.9615 - 53s/epoch - 113ms/step

Epoch 85/100  
469/469 - 53s - loss: 0.1833 - sparse\_categorical\_accuracy: 0.9415 - val\_loss: 0.1209 - val\_sparse\_categorical\_accuracy: 0.9633 - 53s/epoch - 113ms/step

Epoch 86/100  
469/469 - 53s - loss: 0.1855 - sparse\_categorical\_accuracy: 0.9407 - val\_loss: 0.1203 - val\_sparse\_categorical\_accuracy: 0.9633 - 53s/epoch - 113ms/step

```

ategorical_accuracy: 0.9628 - 53s/epoch - 113ms/step
Epoch 87/100
469/469 - 53s - loss: 0.1846 - sparse_categorical_accuracy: 0.9419 - val_loss: 0.1198 - val_sparse_c
ategorical_accuracy: 0.9627 - 53s/epoch - 113ms/step
Epoch 88/100
469/469 - 53s - loss: 0.1830 - sparse_categorical_accuracy: 0.9416 - val_loss: 0.1200 - val_sparse_c
ategorical_accuracy: 0.9617 - 53s/epoch - 113ms/step
Epoch 89/100
469/469 - 54s - loss: 0.1795 - sparse_categorical_accuracy: 0.9419 - val_loss: 0.1192 - val_sparse_c
ategorical_accuracy: 0.9614 - 54s/epoch - 114ms/step
Epoch 90/100
469/469 - 54s - loss: 0.1776 - sparse_categorical_accuracy: 0.9436 - val_loss: 0.1207 - val_sparse_c
ategorical_accuracy: 0.9614 - 54s/epoch - 114ms/step
Epoch 91/100
469/469 - 53s - loss: 0.1791 - sparse_categorical_accuracy: 0.9427 - val_loss: 0.1197 - val_sparse_c
ategorical_accuracy: 0.9628 - 53s/epoch - 114ms/step
Epoch 92/100
469/469 - 53s - loss: 0.1769 - sparse_categorical_accuracy: 0.9433 - val_loss: 0.1149 - val_sparse_c
ategorical_accuracy: 0.9637 - 53s/epoch - 114ms/step
Epoch 93/100
469/469 - 53s - loss: 0.1778 - sparse_categorical_accuracy: 0.9428 - val_loss: 0.1161 - val_sparse_c
ategorical_accuracy: 0.9636 - 53s/epoch - 114ms/step
Epoch 94/100
469/469 - 53s - loss: 0.1794 - sparse_categorical_accuracy: 0.9430 - val_loss: 0.1169 - val_sparse_c
ategorical_accuracy: 0.9631 - 53s/epoch - 114ms/step
Epoch 95/100
469/469 - 53s - loss: 0.1750 - sparse_categorical_accuracy: 0.9431 - val_loss: 0.1160 - val_sparse_c
ategorical_accuracy: 0.9642 - 53s/epoch - 114ms/step
Epoch 96/100
469/469 - 53s - loss: 0.1738 - sparse_categorical_accuracy: 0.9451 - val_loss: 0.1135 - val_sparse_c
ategorical_accuracy: 0.9662 - 53s/epoch - 113ms/step
Epoch 97/100
469/469 - 53s - loss: 0.1726 - sparse_categorical_accuracy: 0.9447 - val_loss: 0.1170 - val_sparse_c
ategorical_accuracy: 0.9635 - 53s/epoch - 113ms/step
Epoch 98/100
469/469 - 53s - loss: 0.1747 - sparse_categorical_accuracy: 0.9437 - val_loss: 0.1136 - val_sparse_c
ategorical_accuracy: 0.9655 - 53s/epoch - 114ms/step
Epoch 99/100
469/469 - 53s - loss: 0.1716 - sparse_categorical_accuracy: 0.9450 - val_loss: 0.1117 - val_sparse_c
ategorical_accuracy: 0.9658 - 53s/epoch - 114ms/step
Epoch 100/100
469/469 - 54s - loss: 0.1733 - sparse_categorical_accuracy: 0.9442 - val_loss: 0.1127 - val_sparse_c
ategorical_accuracy: 0.9660 - 54s/epoch - 114ms/step

```

In [32]:

```
model6.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 4s - loss: 0.1127 - sparse_categorical_accuracy: 0.9660 - 4s/epoch - 14ms/step
```

Out[32]:

```
[0.11269041895866394, 0.9660000205039978]
```

**Model7: adam optimizer with learning rate= $e^{-3}$ , random\_normal initializer, dropout regularization with rate=0.2.**

In [33]:

```

input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                    filters_1x1=1,
                    filters_3x3_reduce=1,
                    filters_3x3=1,
                    filters_5x5_reduce=1,
                    filters_5x5=1,
                    filters_pool_proj=1,
                    name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.2)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_normal')(x)
model7 = Model(input_layer, x, name='inception_v1')

```

In [34]:

```
model7.compile(optimizer=tf.keras.optimizers.Adam(0.001),
               loss='sparse_categorical_crossentropy',
               metrics=['sparse_categorical_accuracy'])
```

In [35]:

```
history7 = model7.fit(x_train, y_train,
                     batch_size=128,
                     epochs=100,
                     validation_data=(x_test, y_test),
                     verbose=2)
```

```
Epoch 1/100
469/469 - 54s - loss: 0.8778 - sparse_categorical_accuracy: 0.7723 - val_loss: 0.2721 - val_sparse_c
ategorical_accuracy: 0.9356 - 54s/epoch - 115ms/step
Epoch 2/100
469/469 - 53s - loss: 0.2546 - sparse_categorical_accuracy: 0.9257 - val_loss: 0.1494 - val_sparse_c
ategorical_accuracy: 0.9580 - 53s/epoch - 112ms/step
Epoch 3/100
469/469 - 53s - loss: 0.1932 - sparse_categorical_accuracy: 0.9399 - val_loss: 0.1190 - val_sparse_c
ategorical_accuracy: 0.9653 - 53s/epoch - 113ms/step
Epoch 4/100
469/469 - 53s - loss: 0.1736 - sparse_categorical_accuracy: 0.9461 - val_loss: 0.1052 - val_sparse_c
ategorical_accuracy: 0.9692 - 53s/epoch - 113ms/step
Epoch 5/100
469/469 - 53s - loss: 0.1611 - sparse_categorical_accuracy: 0.9487 - val_loss: 0.1031 - val_sparse_c
ategorical_accuracy: 0.9684 - 53s/epoch - 113ms/step
Epoch 6/100
469/469 - 53s - loss: 0.1535 - sparse_categorical_accuracy: 0.9512 - val_loss: 0.0903 - val_sparse_c
ategorical_accuracy: 0.9736 - 53s/epoch - 113ms/step
Epoch 7/100
469/469 - 53s - loss: 0.1492 - sparse_categorical_accuracy: 0.9531 - val_loss: 0.0957 - val_sparse_c
ategorical_accuracy: 0.9702 - 53s/epoch - 113ms/step
Epoch 8/100
469/469 - 53s - loss: 0.1432 - sparse_categorical_accuracy: 0.9539 - val_loss: 0.0967 - val_sparse_c
ategorical_accuracy: 0.9698 - 53s/epoch - 113ms/step
Epoch 9/100
469/469 - 53s - loss: 0.1375 - sparse_categorical_accuracy: 0.9564 - val_loss: 0.0890 - val_sparse_c
ategorical_accuracy: 0.9724 - 53s/epoch - 113ms/step
Epoch 10/100
469/469 - 53s - loss: 0.1339 - sparse_categorical_accuracy: 0.9578 - val_loss: 0.0828 - val_sparse_c
ategorical_accuracy: 0.9736 - 53s/epoch - 114ms/step
Epoch 11/100
469/469 - 53s - loss: 0.1316 - sparse_categorical_accuracy: 0.9577 - val_loss: 0.0855 - val_sparse_c
ategorical_accuracy: 0.9735 - 53s/epoch - 114ms/step
Epoch 12/100
469/469 - 53s - loss: 0.1292 - sparse_categorical_accuracy: 0.9589 - val_loss: 0.0912 - val_sparse_c
ategorical_accuracy: 0.9713 - 53s/epoch - 113ms/step
Epoch 13/100
469/469 - 53s - loss: 0.1269 - sparse_categorical_accuracy: 0.9592 - val_loss: 0.0822 - val_sparse_c
ategorical_accuracy: 0.9751 - 53s/epoch - 113ms/step
Epoch 14/100
469/469 - 53s - loss: 0.1218 - sparse_categorical_accuracy: 0.9606 - val_loss: 0.0800 - val_sparse_c
ategorical_accuracy: 0.9764 - 53s/epoch - 114ms/step
Epoch 15/100
469/469 - 53s - loss: 0.1214 - sparse_categorical_accuracy: 0.9618 - val_loss: 0.0835 - val_sparse_c
ategorical_accuracy: 0.9737 - 53s/epoch - 113ms/step
Epoch 16/100
469/469 - 53s - loss: 0.1215 - sparse_categorical_accuracy: 0.9610 - val_loss: 0.0763 - val_sparse_c
ategorical_accuracy: 0.9757 - 53s/epoch - 113ms/step
Epoch 17/100
469/469 - 53s - loss: 0.1208 - sparse_categorical_accuracy: 0.9613 - val_loss: 0.0790 - val_sparse_c
ategorical_accuracy: 0.9755 - 53s/epoch - 113ms/step
Epoch 18/100
469/469 - 53s - loss: 0.1179 - sparse_categorical_accuracy: 0.9626 - val_loss: 0.0841 - val_sparse_c
ategorical_accuracy: 0.9731 - 53s/epoch - 113ms/step
Epoch 19/100
469/469 - 53s - loss: 0.1150 - sparse_categorical_accuracy: 0.9633 - val_loss: 0.0804 - val_sparse_c
ategorical_accuracy: 0.9774 - 53s/epoch - 113ms/step
Epoch 20/100
469/469 - 53s - loss: 0.1167 - sparse_categorical_accuracy: 0.9619 - val_loss: 0.0785 - val_sparse_c
ategorical_accuracy: 0.9763 - 53s/epoch - 113ms/step
Epoch 21/100
469/469 - 53s - loss: 0.1163 - sparse_categorical_accuracy: 0.9622 - val_loss: 0.0772 - val_sparse_c
ategorical_accuracy: 0.9761 - 53s/epoch - 113ms/step
Epoch 22/100
469/469 - 53s - loss: 0.1156 - sparse_categorical_accuracy: 0.9627 - val_loss: 0.0801 - val_sparse_c
ategorical_accuracy: 0.9747 - 53s/epoch - 113ms/step
Epoch 23/100
```



[illegible]

```
Epoch 51/100
469/469 - 53s - loss: 0.1029 - sparse_categorical_accuracy: 0.9662 - val_loss: 0.0712 - val_sparse_c
ategorical_accuracy: 0.9783 - 53s/epoch - 113ms/step
Epoch 52/100
469/469 - 53s - loss: 0.1016 - sparse_categorical_accuracy: 0.9676 - val_loss: 0.0663 - val_sparse_c
ategorical_accuracy: 0.9792 - 53s/epoch - 114ms/step
Epoch 53/100
469/469 - 53s - loss: 0.1015 - sparse_categorical_accuracy: 0.9674 - val_loss: 0.0700 - val_sparse_c
ategorical_accuracy: 0.9781 - 53s/epoch - 113ms/step
Epoch 54/100
469/469 - 53s - loss: 0.1006 - sparse_categorical_accuracy: 0.9668 - val_loss: 0.0722 - val_sparse_c
ategorical_accuracy: 0.9769 - 53s/epoch - 113ms/step
Epoch 55/100
469/469 - 53s - loss: 0.0993 - sparse_categorical_accuracy: 0.9675 - val_loss: 0.0668 - val_sparse_c
ategorical_accuracy: 0.9797 - 53s/epoch - 113ms/step
Epoch 56/100
469/469 - 53s - loss: 0.0996 - sparse_categorical_accuracy: 0.9683 - val_loss: 0.0643 - val_sparse_c
ategorical_accuracy: 0.9811 - 53s/epoch - 113ms/step
Epoch 57/100
469/469 - 53s - loss: 0.1022 - sparse_categorical_accuracy: 0.9675 - val_loss: 0.0696 - val_sparse_c
ategorical_accuracy: 0.9792 - 53s/epoch - 113ms/step
Epoch 58/100
469/469 - 53s - loss: 0.0974 - sparse_categorical_accuracy: 0.9681 - val_loss: 0.0689 - val_sparse_c
ategorical_accuracy: 0.9796 - 53s/epoch - 113ms/step
Epoch 59/100
469/469 - 53s - loss: 0.0999 - sparse_categorical_accuracy: 0.9681 - val_loss: 0.0696 - val_sparse_c
ategorical_accuracy: 0.9795 - 53s/epoch - 114ms/step
Epoch 60/100
469/469 - 53s - loss: 0.1017 - sparse_categorical_accuracy: 0.9673 - val_loss: 0.0671 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 113ms/step
Epoch 61/100
469/469 - 53s - loss: 0.0994 - sparse_categorical_accuracy: 0.9674 - val_loss: 0.0662 - val_sparse_c
ategorical_accuracy: 0.9810 - 53s/epoch - 113ms/step
Epoch 62/100
469/469 - 53s - loss: 0.0983 - sparse_categorical_accuracy: 0.9681 - val_loss: 0.0685 - val_sparse_c
ategorical_accuracy: 0.9785 - 53s/epoch - 113ms/step
Epoch 63/100
469/469 - 53s - loss: 0.0972 - sparse_categorical_accuracy: 0.9685 - val_loss: 0.0732 - val_sparse_c
ategorical_accuracy: 0.9782 - 53s/epoch - 113ms/step
Epoch 64/100
469/469 - 53s - loss: 0.1002 - sparse_categorical_accuracy: 0.9671 - val_loss: 0.0652 - val_sparse_c
ategorical_accuracy: 0.9808 - 53s/epoch - 112ms/step
Epoch 65/100
469/469 - 53s - loss: 0.0990 - sparse_categorical_accuracy: 0.9673 - val_loss: 0.0707 - val_sparse_c
ategorical_accuracy: 0.9789 - 53s/epoch - 114ms/step
Epoch 66/100
469/469 - 53s - loss: 0.0983 - sparse_categorical_accuracy: 0.9678 - val_loss: 0.0655 - val_sparse_c
ategorical_accuracy: 0.9806 - 53s/epoch - 113ms/step
Epoch 67/100
469/469 - 53s - loss: 0.1000 - sparse_categorical_accuracy: 0.9673 - val_loss: 0.0653 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 113ms/step
Epoch 68/100
469/469 - 53s - loss: 0.0968 - sparse_categorical_accuracy: 0.9692 - val_loss: 0.0663 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 113ms/step
Epoch 69/100
469/469 - 53s - loss: 0.0979 - sparse_categorical_accuracy: 0.9675 - val_loss: 0.0682 - val_sparse_c
ategorical_accuracy: 0.9795 - 53s/epoch - 114ms/step
Epoch 70/100
469/469 - 53s - loss: 0.0972 - sparse_categorical_accuracy: 0.9687 - val_loss: 0.0650 - val_sparse_c
ategorical_accuracy: 0.9807 - 53s/epoch - 113ms/step
Epoch 71/100
469/469 - 53s - loss: 0.0966 - sparse_categorical_accuracy: 0.9687 - val_loss: 0.0649 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 114ms/step
Epoch 72/100
469/469 - 53s - loss: 0.0972 - sparse_categorical_accuracy: 0.9679 - val_loss: 0.0680 - val_sparse_c
ategorical_accuracy: 0.9785 - 53s/epoch - 114ms/step
Epoch 73/100
469/469 - 53s - loss: 0.0964 - sparse_categorical_accuracy: 0.9688 - val_loss: 0.0685 - val_sparse_c
ategorical_accuracy: 0.9784 - 53s/epoch - 113ms/step
Epoch 74/100
469/469 - 53s - loss: 0.0986 - sparse_categorical_accuracy: 0.9683 - val_loss: 0.0664 - val_sparse_c
ategorical_accuracy: 0.9788 - 53s/epoch - 114ms/step
Epoch 75/100
469/469 - 53s - loss: 0.0974 - sparse_categorical_accuracy: 0.9684 - val_loss: 0.0645 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 113ms/step
Epoch 76/100
469/469 - 53s - loss: 0.0948 - sparse_categorical_accuracy: 0.9688 - val_loss: 0.0656 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 114ms/step
Epoch 77/100
469/469 - 53s - loss: 0.0949 - sparse_categorical_accuracy: 0.9691 - val_loss: 0.0671 - val_sparse_c
ategorical_accuracy: 0.9794 - 53s/epoch - 113ms/step
Epoch 78/100
469/469 - 53s - loss: 0.0960 - sparse_categorical_accuracy: 0.9688 - val_loss: 0.0649 - val_sparse_c
```

```

ategorical_accuracy: 0.9804 - 53s/epoch - 113ms/step
Epoch 79/100
469/469 - 53s - loss: 0.0946 - sparse_categorical_accuracy: 0.9693 - val_loss: 0.0648 - val_sparse_c
ategorical_accuracy: 0.9804 - 53s/epoch - 114ms/step
Epoch 80/100
469/469 - 53s - loss: 0.0978 - sparse_categorical_accuracy: 0.9680 - val_loss: 0.0671 - val_sparse_c
ategorical_accuracy: 0.9800 - 53s/epoch - 113ms/step
Epoch 81/100
469/469 - 53s - loss: 0.0967 - sparse_categorical_accuracy: 0.9682 - val_loss: 0.0675 - val_sparse_c
ategorical_accuracy: 0.9785 - 53s/epoch - 113ms/step
Epoch 82/100
469/469 - 53s - loss: 0.0964 - sparse_categorical_accuracy: 0.9697 - val_loss: 0.0643 - val_sparse_c
ategorical_accuracy: 0.9806 - 53s/epoch - 114ms/step
Epoch 83/100
469/469 - 53s - loss: 0.0948 - sparse_categorical_accuracy: 0.9685 - val_loss: 0.0649 - val_sparse_c
ategorical_accuracy: 0.9796 - 53s/epoch - 114ms/step
Epoch 84/100
469/469 - 53s - loss: 0.0944 - sparse_categorical_accuracy: 0.9697 - val_loss: 0.0645 - val_sparse_c
ategorical_accuracy: 0.9801 - 53s/epoch - 113ms/step
Epoch 85/100
469/469 - 53s - loss: 0.0954 - sparse_categorical_accuracy: 0.9689 - val_loss: 0.0669 - val_sparse_c
ategorical_accuracy: 0.9797 - 53s/epoch - 113ms/step
Epoch 86/100
469/469 - 53s - loss: 0.0945 - sparse_categorical_accuracy: 0.9692 - val_loss: 0.0651 - val_sparse_c
ategorical_accuracy: 0.9805 - 53s/epoch - 113ms/step
Epoch 87/100
469/469 - 53s - loss: 0.0959 - sparse_categorical_accuracy: 0.9689 - val_loss: 0.0668 - val_sparse_c
ategorical_accuracy: 0.9789 - 53s/epoch - 114ms/step
Epoch 88/100
469/469 - 53s - loss: 0.0949 - sparse_categorical_accuracy: 0.9692 - val_loss: 0.0666 - val_sparse_c
ategorical_accuracy: 0.9800 - 53s/epoch - 113ms/step
Epoch 89/100
469/469 - 53s - loss: 0.0934 - sparse_categorical_accuracy: 0.9697 - val_loss: 0.0646 - val_sparse_c
ategorical_accuracy: 0.9794 - 53s/epoch - 113ms/step
Epoch 90/100
469/469 - 53s - loss: 0.0934 - sparse_categorical_accuracy: 0.9700 - val_loss: 0.0640 - val_sparse_c
ategorical_accuracy: 0.9794 - 53s/epoch - 112ms/step
Epoch 91/100
469/469 - 53s - loss: 0.0945 - sparse_categorical_accuracy: 0.9694 - val_loss: 0.0641 - val_sparse_c
ategorical_accuracy: 0.9808 - 53s/epoch - 112ms/step
Epoch 92/100
469/469 - 53s - loss: 0.0936 - sparse_categorical_accuracy: 0.9691 - val_loss: 0.0663 - val_sparse_c
ategorical_accuracy: 0.9796 - 53s/epoch - 113ms/step
Epoch 93/100
469/469 - 53s - loss: 0.0925 - sparse_categorical_accuracy: 0.9701 - val_loss: 0.0657 - val_sparse_c
ategorical_accuracy: 0.9785 - 53s/epoch - 114ms/step
Epoch 94/100
469/469 - 53s - loss: 0.0929 - sparse_categorical_accuracy: 0.9698 - val_loss: 0.0657 - val_sparse_c
ategorical_accuracy: 0.9803 - 53s/epoch - 113ms/step
Epoch 95/100
469/469 - 53s - loss: 0.0932 - sparse_categorical_accuracy: 0.9696 - val_loss: 0.0679 - val_sparse_c
ategorical_accuracy: 0.9793 - 53s/epoch - 113ms/step
Epoch 96/100
469/469 - 53s - loss: 0.0913 - sparse_categorical_accuracy: 0.9696 - val_loss: 0.0679 - val_sparse_c
ategorical_accuracy: 0.9792 - 53s/epoch - 113ms/step
Epoch 97/100
469/469 - 53s - loss: 0.0940 - sparse_categorical_accuracy: 0.9690 - val_loss: 0.0672 - val_sparse_c
ategorical_accuracy: 0.9790 - 53s/epoch - 113ms/step
Epoch 98/100
469/469 - 53s - loss: 0.0925 - sparse_categorical_accuracy: 0.9701 - val_loss: 0.0650 - val_sparse_c
ategorical_accuracy: 0.9795 - 53s/epoch - 114ms/step
Epoch 99/100
469/469 - 53s - loss: 0.0940 - sparse_categorical_accuracy: 0.9695 - val_loss: 0.0654 - val_sparse_c
ategorical_accuracy: 0.9806 - 53s/epoch - 113ms/step
Epoch 100/100
469/469 - 53s - loss: 0.0931 - sparse_categorical_accuracy: 0.9700 - val_loss: 0.0707 - val_sparse_c
ategorical_accuracy: 0.9778 - 53s/epoch - 113ms/step

```

In [36]:

```
model7.evaluate(x_test, y_test, verbose=2)
```

```
313/313 - 4s - loss: 0.0707 - sparse_categorical_accuracy: 0.9778 - 4s/epoch - 13ms/step
```

Out[36]:

```
[0.07072369754314423, 0.9778000116348267]
```

**Model8:** adam optimizer with learning rate= $e^{-4}$ , random\_normal initializer, dropout regularization with rate=0.2.

In [37]:

```
input_layer = Input(shape=(28, 28,1))
x = inception_module(input_layer,
                      filters_1x1=1,
                      filters_3x3_reduce=1,
                      filters_3x3=1,
                      filters_5x5_reduce=1,
                      filters_5x5=1,
                      filters_pool_proj=1,
                      name='inception_3a')
x = tf.keras.layers.BatchNormalization()(x)
x = MaxPool2D((3, 3))(x)
x = tf.keras.layers.Flatten()(x)
x = Dropout(0.2)(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.Dense(16, activation='relu', kernel_initializer='random_normal')(x)
x = tf.keras.layers.BatchNormalization()(x)
x = Dense(10, activation='softmax', kernel_initializer='random_normal')(x)
model8 = Model(input_layer, x, name='inception_v1')
```

In [38]:

```
model8.compile(optimizer=tf.keras.optimizers.Adam(0.0001),
               loss='sparse_categorical_crossentropy',
               metrics=['sparse_categorical_accuracy']
               )
```

In [39]:

```
history8 = model8.fit(x_train, y_train,
                      batch_size=128,
                      epochs=100,
                      validation_data=(x_test, y_test),
                      verbose=2
                      )
```

```
Epoch 1/100
469/469 - 54s - loss: 2.0019 - sparse_categorical_accuracy: 0.3940 - val_loss: 1.6929 - val_sparse_c
ategorical_accuracy: 0.6367 - 54s/epoch - 116ms/step
Epoch 2/100
469/469 - 53s - loss: 1.5047 - sparse_categorical_accuracy: 0.6314 - val_loss: 1.2433 - val_sparse_c
ategorical_accuracy: 0.7304 - 53s/epoch - 113ms/step
Epoch 3/100
469/469 - 53s - loss: 1.1574 - sparse_categorical_accuracy: 0.7271 - val_loss: 0.9346 - val_sparse_c
ategorical_accuracy: 0.8106 - 53s/epoch - 114ms/step
Epoch 4/100
469/469 - 53s - loss: 0.9142 - sparse_categorical_accuracy: 0.7806 - val_loss: 0.7155 - val_sparse_c
ategorical_accuracy: 0.8499 - 53s/epoch - 114ms/step
Epoch 5/100
469/469 - 53s - loss: 0.7577 - sparse_categorical_accuracy: 0.8063 - val_loss: 0.5890 - val_sparse_c
ategorical_accuracy: 0.8720 - 53s/epoch - 113ms/step
Epoch 6/100
469/469 - 53s - loss: 0.6601 - sparse_categorical_accuracy: 0.8213 - val_loss: 0.5017 - val_sparse_c
ategorical_accuracy: 0.8784 - 53s/epoch - 113ms/step
Epoch 7/100
469/469 - 53s - loss: 0.5968 - sparse_categorical_accuracy: 0.8299 - val_loss: 0.4491 - val_sparse_c
ategorical_accuracy: 0.8827 - 53s/epoch - 113ms/step
Epoch 8/100
469/469 - 53s - loss: 0.5527 - sparse_categorical_accuracy: 0.8362 - val_loss: 0.4164 - val_sparse_c
ategorical_accuracy: 0.8863 - 53s/epoch - 113ms/step
Epoch 9/100
469/469 - 53s - loss: 0.5238 - sparse_categorical_accuracy: 0.8412 - val_loss: 0.3873 - val_sparse_c
ategorical_accuracy: 0.8911 - 53s/epoch - 114ms/step
Epoch 10/100
469/469 - 53s - loss: 0.5042 - sparse_categorical_accuracy: 0.8446 - val_loss: 0.3692 - val_sparse_c
ategorical_accuracy: 0.8924 - 53s/epoch - 113ms/step
Epoch 11/100
469/469 - 53s - loss: 0.4899 - sparse_categorical_accuracy: 0.8471 - val_loss: 0.3590 - val_sparse_c
ategorical_accuracy: 0.8952 - 53s/epoch - 114ms/step
Epoch 12/100
469/469 - 53s - loss: 0.4757 - sparse_categorical_accuracy: 0.8503 - val_loss: 0.3461 - val_sparse_c
ategorical_accuracy: 0.8972 - 53s/epoch - 113ms/step
Epoch 13/100
469/469 - 53s - loss: 0.4653 - sparse_categorical_accuracy: 0.8526 - val_loss: 0.3398 - val_sparse_c
ategorical_accuracy: 0.8956 - 53s/epoch - 113ms/step
Epoch 14/100
469/469 - 53s - loss: 0.4582 - sparse_categorical_accuracy: 0.8534 - val_loss: 0.3286 - val_sparse_c
ategorical_accuracy: 0.8993 - 53s/epoch - 114ms/step
Epoch 15/100
469/469 - 53s - loss: 0.4462 - sparse_categorical_accuracy: 0.8582 - val_loss: 0.3223 - val_sparse_c
ategorical_accuracy: 0.9027 - 53s/epoch - 113ms/step
Epoch 16/100
```

469/469 - 53s - loss: 0.4403 - sparse\_categorical\_accuracy: 0.8585 - val\_loss: 0.3140 - val\_sparse\_categorical\_accuracy: 0.9044 - 53s/epoch - 113ms/step  
Epoch 17/100  
469/469 - 53s - loss: 0.4351 - sparse\_categorical\_accuracy: 0.8611 - val\_loss: 0.3163 - val\_sparse\_categorical\_accuracy: 0.9031 - 53s/epoch - 113ms/step  
Epoch 18/100  
469/469 - 53s - loss: 0.4292 - sparse\_categorical\_accuracy: 0.8606 - val\_loss: 0.3074 - val\_sparse\_categorical\_accuracy: 0.9054 - 53s/epoch - 113ms/step  
Epoch 19/100  
469/469 - 53s - loss: 0.4244 - sparse\_categorical\_accuracy: 0.8620 - val\_loss: 0.3124 - val\_sparse\_categorical\_accuracy: 0.9026 - 53s/epoch - 113ms/step  
Epoch 20/100  
469/469 - 53s - loss: 0.4197 - sparse\_categorical\_accuracy: 0.8638 - val\_loss: 0.3026 - val\_sparse\_categorical\_accuracy: 0.9077 - 53s/epoch - 113ms/step  
Epoch 21/100  
469/469 - 53s - loss: 0.4108 - sparse\_categorical\_accuracy: 0.8677 - val\_loss: 0.2987 - val\_sparse\_categorical\_accuracy: 0.9065 - 53s/epoch - 113ms/step  
Epoch 22/100  
469/469 - 53s - loss: 0.4063 - sparse\_categorical\_accuracy: 0.8676 - val\_loss: 0.2945 - val\_sparse\_categorical\_accuracy: 0.9088 - 53s/epoch - 114ms/step  
Epoch 23/100  
469/469 - 53s - loss: 0.4037 - sparse\_categorical\_accuracy: 0.8678 - val\_loss: 0.2865 - val\_sparse\_categorical\_accuracy: 0.9108 - 53s/epoch - 114ms/step  
Epoch 24/100  
469/469 - 53s - loss: 0.4024 - sparse\_categorical\_accuracy: 0.8700 - val\_loss: 0.2835 - val\_sparse\_categorical\_accuracy: 0.9128 - 53s/epoch - 113ms/step  
Epoch 25/100  
469/469 - 53s - loss: 0.3940 - sparse\_categorical\_accuracy: 0.8708 - val\_loss: 0.2794 - val\_sparse\_categorical\_accuracy: 0.9138 - 53s/epoch - 113ms/step  
Epoch 26/100  
469/469 - 53s - loss: 0.3888 - sparse\_categorical\_accuracy: 0.8741 - val\_loss: 0.2770 - val\_sparse\_categorical\_accuracy: 0.9169 - 53s/epoch - 113ms/step  
Epoch 27/100  
469/469 - 53s - loss: 0.3830 - sparse\_categorical\_accuracy: 0.8743 - val\_loss: 0.2718 - val\_sparse\_categorical\_accuracy: 0.9157 - 53s/epoch - 114ms/step  
Epoch 28/100  
469/469 - 53s - loss: 0.3741 - sparse\_categorical\_accuracy: 0.8792 - val\_loss: 0.2672 - val\_sparse\_categorical\_accuracy: 0.9190 - 53s/epoch - 113ms/step  
Epoch 29/100  
469/469 - 53s - loss: 0.3681 - sparse\_categorical\_accuracy: 0.8800 - val\_loss: 0.2636 - val\_sparse\_categorical\_accuracy: 0.9198 - 53s/epoch - 114ms/step  
Epoch 30/100  
469/469 - 53s - loss: 0.3621 - sparse\_categorical\_accuracy: 0.8824 - val\_loss: 0.2565 - val\_sparse\_categorical\_accuracy: 0.9205 - 53s/epoch - 113ms/step  
Epoch 31/100  
469/469 - 53s - loss: 0.3537 - sparse\_categorical\_accuracy: 0.8849 - val\_loss: 0.2528 - val\_sparse\_categorical\_accuracy: 0.9223 - 53s/epoch - 113ms/step  
Epoch 32/100  
469/469 - 53s - loss: 0.3489 - sparse\_categorical\_accuracy: 0.8870 - val\_loss: 0.2499 - val\_sparse\_categorical\_accuracy: 0.9239 - 53s/epoch - 113ms/step  
Epoch 33/100  
469/469 - 53s - loss: 0.3386 - sparse\_categorical\_accuracy: 0.8911 - val\_loss: 0.2460 - val\_sparse\_categorical\_accuracy: 0.9252 - 53s/epoch - 114ms/step  
Epoch 34/100  
469/469 - 53s - loss: 0.3356 - sparse\_categorical\_accuracy: 0.8909 - val\_loss: 0.2432 - val\_sparse\_categorical\_accuracy: 0.9252 - 53s/epoch - 113ms/step  
Epoch 35/100  
469/469 - 53s - loss: 0.3275 - sparse\_categorical\_accuracy: 0.8936 - val\_loss: 0.2377 - val\_sparse\_categorical\_accuracy: 0.9264 - 53s/epoch - 113ms/step  
Epoch 36/100  
469/469 - 53s - loss: 0.3235 - sparse\_categorical\_accuracy: 0.8949 - val\_loss: 0.2344 - val\_sparse\_categorical\_accuracy: 0.9272 - 53s/epoch - 113ms/step  
Epoch 37/100  
469/469 - 53s - loss: 0.3204 - sparse\_categorical\_accuracy: 0.8957 - val\_loss: 0.2310 - val\_sparse\_categorical\_accuracy: 0.9296 - 53s/epoch - 114ms/step  
Epoch 38/100  
469/469 - 53s - loss: 0.3098 - sparse\_categorical\_accuracy: 0.8995 - val\_loss: 0.2257 - val\_sparse\_categorical\_accuracy: 0.9321 - 53s/epoch - 114ms/step  
Epoch 39/100  
469/469 - 53s - loss: 0.3116 - sparse\_categorical\_accuracy: 0.8997 - val\_loss: 0.2261 - val\_sparse\_categorical\_accuracy: 0.9319 - 53s/epoch - 114ms/step  
Epoch 40/100  
469/469 - 53s - loss: 0.3069 - sparse\_categorical\_accuracy: 0.9010 - val\_loss: 0.2219 - val\_sparse\_categorical\_accuracy: 0.9327 - 53s/epoch - 113ms/step  
Epoch 41/100  
469/469 - 53s - loss: 0.3031 - sparse\_categorical\_accuracy: 0.9024 - val\_loss: 0.2197 - val\_sparse\_categorical\_accuracy: 0.9330 - 53s/epoch - 113ms/step  
Epoch 42/100  
469/469 - 53s - loss: 0.3013 - sparse\_categorical\_accuracy: 0.9024 - val\_loss: 0.2191 - val\_sparse\_categorical\_accuracy: 0.9337 - 53s/epoch - 114ms/step  
Epoch 43/100  
469/469 - 53s - loss: 0.2980 - sparse\_categorical\_accuracy: 0.9038 - val\_loss: 0.2184 - val\_sparse\_categorical\_accuracy: 0.9329 - 53s/epoch - 113ms/step

```
Epoch 44/100
469/469 - 53s - loss: 0.2953 - sparse_categorical_accuracy: 0.9047 - val_loss: 0.2124 - val_sparse_c
ategorical_accuracy: 0.9352 - 53s/epoch - 114ms/step
Epoch 45/100
469/469 - 53s - loss: 0.2940 - sparse_categorical_accuracy: 0.9045 - val_loss: 0.2171 - val_sparse_c
ategorical_accuracy: 0.9334 - 53s/epoch - 114ms/step
Epoch 46/100
469/469 - 53s - loss: 0.2939 - sparse_categorical_accuracy: 0.9051 - val_loss: 0.2138 - val_sparse_c
ategorical_accuracy: 0.9352 - 53s/epoch - 113ms/step
Epoch 47/100
469/469 - 53s - loss: 0.2906 - sparse_categorical_accuracy: 0.9049 - val_loss: 0.2093 - val_sparse_c
ategorical_accuracy: 0.9363 - 53s/epoch - 113ms/step
Epoch 48/100
469/469 - 53s - loss: 0.2878 - sparse_categorical_accuracy: 0.9077 - val_loss: 0.2077 - val_sparse_c
ategorical_accuracy: 0.9369 - 53s/epoch - 113ms/step
Epoch 49/100
469/469 - 53s - loss: 0.2858 - sparse_categorical_accuracy: 0.9081 - val_loss: 0.2086 - val_sparse_c
ategorical_accuracy: 0.9368 - 53s/epoch - 113ms/step
Epoch 50/100
469/469 - 53s - loss: 0.2842 - sparse_categorical_accuracy: 0.9076 - val_loss: 0.2053 - val_sparse_c
ategorical_accuracy: 0.9368 - 53s/epoch - 113ms/step
Epoch 51/100
469/469 - 53s - loss: 0.2842 - sparse_categorical_accuracy: 0.9089 - val_loss: 0.2052 - val_sparse_c
ategorical_accuracy: 0.9390 - 53s/epoch - 113ms/step
Epoch 52/100
469/469 - 53s - loss: 0.2819 - sparse_categorical_accuracy: 0.9086 - val_loss: 0.2024 - val_sparse_c
ategorical_accuracy: 0.9394 - 53s/epoch - 113ms/step
Epoch 53/100
469/469 - 53s - loss: 0.2808 - sparse_categorical_accuracy: 0.9090 - val_loss: 0.2050 - val_sparse_c
ategorical_accuracy: 0.9388 - 53s/epoch - 113ms/step
Epoch 54/100
469/469 - 53s - loss: 0.2772 - sparse_categorical_accuracy: 0.9109 - val_loss: 0.2021 - val_sparse_c
ategorical_accuracy: 0.9397 - 53s/epoch - 114ms/step
Epoch 55/100
469/469 - 53s - loss: 0.2781 - sparse_categorical_accuracy: 0.9103 - val_loss: 0.1999 - val_sparse_c
ategorical_accuracy: 0.9413 - 53s/epoch - 114ms/step
Epoch 56/100
469/469 - 53s - loss: 0.2746 - sparse_categorical_accuracy: 0.9118 - val_loss: 0.1987 - val_sparse_c
ategorical_accuracy: 0.9399 - 53s/epoch - 113ms/step
Epoch 57/100
469/469 - 53s - loss: 0.2737 - sparse_categorical_accuracy: 0.9110 - val_loss: 0.2010 - val_sparse_c
ategorical_accuracy: 0.9389 - 53s/epoch - 114ms/step
Epoch 58/100
469/469 - 53s - loss: 0.2757 - sparse_categorical_accuracy: 0.9115 - val_loss: 0.1956 - val_sparse_c
ategorical_accuracy: 0.9412 - 53s/epoch - 113ms/step
Epoch 59/100
469/469 - 53s - loss: 0.2732 - sparse_categorical_accuracy: 0.9115 - val_loss: 0.1949 - val_sparse_c
ategorical_accuracy: 0.9415 - 53s/epoch - 113ms/step
Epoch 60/100
469/469 - 53s - loss: 0.2735 - sparse_categorical_accuracy: 0.9115 - val_loss: 0.1960 - val_sparse_c
ategorical_accuracy: 0.9401 - 53s/epoch - 113ms/step
Epoch 61/100
469/469 - 53s - loss: 0.2667 - sparse_categorical_accuracy: 0.9128 - val_loss: 0.1933 - val_sparse_c
ategorical_accuracy: 0.9429 - 53s/epoch - 113ms/step
Epoch 62/100
469/469 - 53s - loss: 0.2702 - sparse_categorical_accuracy: 0.9134 - val_loss: 0.1925 - val_sparse_c
ategorical_accuracy: 0.9422 - 53s/epoch - 114ms/step
Epoch 63/100
469/469 - 53s - loss: 0.2688 - sparse_categorical_accuracy: 0.9130 - val_loss: 0.1924 - val_sparse_c
ategorical_accuracy: 0.9430 - 53s/epoch - 114ms/step
Epoch 64/100
469/469 - 53s - loss: 0.2687 - sparse_categorical_accuracy: 0.9124 - val_loss: 0.1909 - val_sparse_c
ategorical_accuracy: 0.9431 - 53s/epoch - 114ms/step
Epoch 65/100
469/469 - 53s - loss: 0.2679 - sparse_categorical_accuracy: 0.9128 - val_loss: 0.1916 - val_sparse_c
ategorical_accuracy: 0.9430 - 53s/epoch - 114ms/step
Epoch 66/100
469/469 - 53s - loss: 0.2645 - sparse_categorical_accuracy: 0.9160 - val_loss: 0.1901 - val_sparse_c
ategorical_accuracy: 0.9436 - 53s/epoch - 114ms/step
Epoch 67/100
469/469 - 53s - loss: 0.2627 - sparse_categorical_accuracy: 0.9160 - val_loss: 0.1876 - val_sparse_c
ategorical_accuracy: 0.9441 - 53s/epoch - 114ms/step
Epoch 68/100
469/469 - 53s - loss: 0.2641 - sparse_categorical_accuracy: 0.9140 - val_loss: 0.1906 - val_sparse_c
ategorical_accuracy: 0.9429 - 53s/epoch - 114ms/step
Epoch 69/100
469/469 - 53s - loss: 0.2618 - sparse_categorical_accuracy: 0.9163 - val_loss: 0.1878 - val_sparse_c
ategorical_accuracy: 0.9434 - 53s/epoch - 113ms/step
Epoch 70/100
469/469 - 53s - loss: 0.2609 - sparse_categorical_accuracy: 0.9159 - val_loss: 0.1879 - val_sparse_c
ategorical_accuracy: 0.9435 - 53s/epoch - 114ms/step
Epoch 71/100
469/469 - 54s - loss: 0.2590 - sparse_categorical_accuracy: 0.9171 - val_loss: 0.1870 - val_sparse_c
```

[illegible]

469/469 - 53s - loss: 0.2346 - sparse\_categorical\_accuracy: 0.9250 - val\_loss: 0.1645 - val\_sparse\_categorical\_accuracy: 0.9505 - 53s/epoch - 114ms/step  
Epoch 100/100  
469/469 - 53s - loss: 0.2301 - sparse\_categorical\_accuracy: 0.9252 - val\_loss: 0.1641 - val\_sparse\_categorical\_accuracy: 0.9500 - 53s/epoch - 114ms/step

In [40]:

```
model8.evaluate(x_test, y_test, verbose=2)
```

313/313 - 4s - loss: 0.1641 - sparse\_categorical\_accuracy: 0.9500 - 4s/epoch - 13ms/step

Out[40]:

```
[0.1640833020210266, 0.949999988079071]
```

## Plots

In [41]:

```
import matplotlib.pyplot as plt
```

Plots for different kernel initializers



In [42]:

```
training_accuracy0 = history.history['sparse_categorical_accuracy']
validation_accuracy0 = history.history['val_sparse_categorical_accuracy']

training_accuracy1 = history1.history['sparse_categorical_accuracy']
validation_accuracy1 = history1.history['val_sparse_categorical_accuracy']

training_accuracy2 = history2.history['sparse_categorical_accuracy']
validation_accuracy2 = history2.history['val_sparse_categorical_accuracy']

training_accuracy3 = history3.history['sparse_categorical_accuracy']
validation_accuracy3 = history3.history['val_sparse_categorical_accuracy']

training_accuracy4 = history4.history['sparse_categorical_accuracy']
validation_accuracy4 = history4.history['val_sparse_categorical_accuracy']

training_accuracy5 = history5.history['sparse_categorical_accuracy']
validation_accuracy5 = history5.history['val_sparse_categorical_accuracy']

training_accuracy6 = history6.history['sparse_categorical_accuracy']
validation_accuracy6 = history6.history['val_sparse_categorical_accuracy']

training_accuracy7 = history7.history['sparse_categorical_accuracy']
validation_accuracy7 = history7.history['val_sparse_categorical_accuracy']

training_accuracy8 = history8.history['sparse_categorical_accuracy']
validation_accuracy8 = history8.history['val_sparse_categorical_accuracy']

epochs_range=range(100)

plt.figure(figsize=(8, 8))
plt.subplot(1, 2, 1)
plt.plot(epochs_range, training_accuracy0, label='Train Acc for Baseline')
plt.plot(epochs_range, training_accuracy1, label='Train Acc for Model1')
plt.plot(epochs_range, training_accuracy2, label='Train Acc for Model2')
plt.plot(epochs_range, training_accuracy3, label='Train Acc for Model3')
plt.plot(epochs_range, training_accuracy4, label='Train Acc for Model4')
plt.plot(epochs_range, training_accuracy5, label='Train Acc for Model5')
plt.plot(epochs_range, training_accuracy6, label='Train Acc for Model6')
plt.plot(epochs_range, training_accuracy7, label='Train Acc for Model7')
plt.plot(epochs_range, training_accuracy8, label='Train Acc for Model8')
plt.legend(loc='lower right')
plt.title('Training Accuracy For All Models')

plt.subplot(1, 2, 2)
plt.plot(epochs_range, validation_accuracy0, label='Val Acc for Baseline')
plt.plot(epochs_range, validation_accuracy1, label='Val Acc for Model1')
plt.plot(epochs_range, validation_accuracy2, label='Val Acc for Model2')
plt.plot(epochs_range, validation_accuracy3, label='Val Acc for Model3')
plt.plot(epochs_range, validation_accuracy4, label='Val Acc for Model4')
plt.plot(epochs_range, validation_accuracy5, label='Val Acc for Model5')
plt.plot(epochs_range, validation_accuracy6, label='Val Acc for Model6')
plt.plot(epochs_range, validation_accuracy7, label='Val Acc for Model7')
plt.plot(epochs_range, validation_accuracy8, label='Val Acc for Model8')
plt.legend(loc='lower right')
plt.title('Validation Accuracy For All Models')
plt.show()
```

