RRSPH v3.0.19

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1 Experiment

1.1 Experiment directory

Experiment directory is a directory with parameters files and particles data. You should provide specifically prepared directory to solver.

Minimal experiment directory to start an experiment is presented below:

Any RRSPH simulation program started from parent directory will produce the following output:

```
Found experiments:

[-1] Change search directory

[0] experiment_00: (0/1) data/dump layers

Type experiment id you want to load:
```

You should type '0' and press 'Enter' in order to start simulation with specified parameters and initial state.

Experiment directories with 'ParticleParams.json' and initial state ('dump/0.csv') are usually generated with scripts. Mathematical model's 'ModelParams.json' is user-provided: manually or by SPH2DParamsGenerator app.

1.2 RRSPH package

1.2.1 SPH2D simulation

There are two simulation programs:

- SPH2D_OMP. SPH 2D solver running on CPU with OpenMP or single-threaded.
- SPH2D_CL. SPH 2D solver running on GPU with OpenCL runtime. It's executable file is distributed with CL source code in separate directory:

```
1
   SPH2D_CL.exe
+---cl
ArtificialViscosity.cl
        AverageVelocity.cl
        clErrorCodes.txt
        clparams.h
        common.h
        Density.cl
        EOS.cl
        ExternalForce.cl
        GridFind.cl
        GridUtils.h
        InternalForce.cl
```

```
| ParamsEnumeration.h
| SmoothingKernel.cl
| SmoothingKernel.h
| TimeIntegration.cl
|
\---experiment_00
| ModelParams.json
| ParticleParams.json
| SPH2DParams.json
| \---dump
| 0.csv
```

1.2.2 SPH2D Post-processing

There's several post-processing programs:

- WaterProfile. This app can be used to compute water profiles in space and time.
- FuncAtPoint. This app can be used to extract field variable at specified point in space by SPH smoothing.
- PartToGridConverter. This app can be used to convert SPH particles output into grid to process as mesh algorithm's output.

2 Parameters Scheme

2.1 Model Params

2.1.1 Target version

- params_target_version_major
- params_target_version_minor
- params_target_version_patch

2.1.2 Smoothing kernel function

Possible values:

• 1: SKF_CUBIC.

$$W(q) = \kappa_{\text{cubic}} \begin{cases} \frac{2}{3} - q^2 + \frac{1}{2}q^3 & q \le 1, \\ \frac{1}{6} (2 - q)^3 & 1 < q \le 2, \\ 0 & q > 2. \end{cases}$$
 (1)

• 2: SKF_GAUSS.

$$W(q) = \kappa_{\text{gauss}} \begin{cases} \frac{1}{h^2 \pi} e^{q^{-2}} & q \le 3, \\ 0 & q > 3. \end{cases}$$
 (2)

• 3: SKF_WENDLAND.

$$W(q) = \kappa_{\text{wendland}} \begin{cases} \left(1 - \frac{q}{2}\right)^4 (2q + 1) & q \le 2, \\ 0 & q > 2. \end{cases}$$
 (3)

• 3: SKF_DESBRUN.

$$W(q) = \kappa_{\text{desbrun}} \begin{cases} (2-q)^3 & q \le 2, \\ 0 & q > 2. \end{cases}$$

$$\tag{4}$$

2.1.3 Density

- density_treatment. Density integration function. Possible values of enumeration:
 - 0: DENSITY_SUMMATION. Use SPH summation over kernel:

$$\rho_j = \sum_i m_i W_{ji}. \tag{5}$$

- 1: DENSITY_CONTINUITY. Use integration of continuity equation:

$$\frac{D\rho_j}{Dt} = \sum_i m_i \vec{v_{ji}} \cdot \vec{\nabla}_j W_{ji}. \tag{6}$$

- 2: DENSITY_CONTINUITY_DELTA. Use integration of continuity equation with density diffussion:

$$\frac{D\rho_j}{Dt} = \sum_i m_i \vec{v}_{ji} \cdot \vec{\nabla}_j W_{ji} + 2\delta_{\text{density}} hc \sum_i m_i \frac{(\rho_i - \rho_j)}{\rho_i} \frac{\vec{r}_{ji}}{|\vec{r}_{ji}|^2} \cdot \vec{\nabla}_j W_{ji}. \tag{7}$$

• density_normalization. Enable boundary deficiency correction:

$$\rho_j = \frac{\sum_i m_i W_{ji}}{\sum_i \left(\frac{m_i}{\rho_i}\right) W_{ji}} \tag{8}$$

Optional. Available if density_treatment == 0.

- density_skf. See section 2.1.2.
- density_delta_sph_coef. $\delta_{density}$ parameter in eq. 7. Mandatory if density_treatment == 2.

2.1.4 Equation of state

- eos_sound_vel_method. Method for sound velocity choosing. Possible values of enumeration:
 - 0: EOS_SOUND_VEL_DAM_BREAK. Use dam break assumption:

$$c = \sqrt{200gdc_k}. (9)$$

- 1: EOS_SOUND_VEL_SPECIFIC. Use custom sound velocity.

$$c = c_{\text{user}}. (10)$$

- eos_sound_vel_coef. c_k parameter in eq. 9.
 Mandatory if eos_sound_vel_method == 0.
- eos_sound_vel. User-provided sound velocity $c_{\rm user}$ in eq. 10. Mandatory if eos_sound_vel_method == 1.

2.1.5 Internal Forces

- intf_sph_approximation. SPH momentum equation form. Possible values of enumeration:
 - 1: INTF_SPH_APPROXIMATION_1. SPH momentum equation form:

$$\frac{D\vec{v}_j}{Dt} = -\sum_i m_i \left(\frac{p_i + p_j}{\rho_i \rho_j}\right) \vec{\nabla}_j W_{ji}. \tag{11}$$

- 2: INTF_SPH_APPROXIMATION_2. SPH momentum equation form:

$$\frac{D\vec{v}_j}{Dt} = -\sum_i m_i \left(\frac{p_j}{\rho_j^2} + \frac{p_i}{\rho_i^2}\right) \vec{\nabla}_j W_{ji}. \tag{12}$$

• intf_hsml_coef. h_k in smoothing kernel length equation:

$$h = \delta_0 \cdot h_k,\tag{13}$$

where δ_0 is initial distance between particles.

• intf_skf. See section 2.1.2.

2.1.6 Artificial Pressure

• artificial_pressure. Enable additional factor in momentum equation for tensile instability correction:

$$\frac{D\vec{v}_j}{Dt} = -\sum_i m_i \left(\frac{p_j}{\rho_j^2} + \frac{p_i}{\rho_i^2} + R\tilde{W}_{ji}^n \right) \vec{\nabla}_j W_{ji}, \tag{14}$$

where $R\tilde{W}_{ji}^n$ is artificial pressure term. SPH approximation function could be of both types.

$$R = R_i + R_j, (15)$$

where any indexed R_x is:

$$R_x = \begin{cases} \frac{\epsilon |p_x|}{\rho_x^2} & p_x < 0, \\ 0 & p_x \ge 0, \end{cases}$$
 (16)

where ϵ is artificial pressure coefficient.

$$\tilde{W}_{ji} = \frac{W(\vec{r}_{ji}, h)}{W(\delta_0, h)},\tag{17}$$

where δ_0 is initial distance between particles.

- artificial_pressure_skf. See section 2.1.2.
- artificial_pressure_index. Term n in eq. 14.
- artificial_pressure_coef. Term ϵ in eq. 16.

2.1.7 Artificial Viscosity

• artificial_viscosity. Enable additional factor in momentum equation for stability correction:

$$\frac{D\vec{v}_j}{Dt} = -\sum_i m_i \left(\frac{p_j}{\rho_j^2} + \frac{p_i}{\rho_i^2} + \Pi_{ji} \right) \vec{\nabla}_j W_{ji}, \tag{18}$$

where Π_{ji} is artificial viscosity term. SPH approximation function could be of both types. Π_{ji} is:

$$\Pi_{ji} = \begin{cases}
\frac{-\alpha_{\Pi} c_{ji} \phi_{ji} + \beta_{\Pi} \phi_{ji}^{2}}{\rho_{ji}^{2}} & \vec{v}_{ji} \cdot \vec{r}_{ji} < 0, \\
0 & \vec{v}_{ji} \cdot \vec{r}_{ji} \ge 0,
\end{cases}$$
(19)

$$\phi_{ji} = \frac{h_{ji}\vec{v}_{ji} \cdot \vec{r}_{ji}}{|\vec{r}_{ji}|^2 + (\epsilon_{\Pi}h_{ji})^2},\tag{20}$$

$$\rho_{ji} = \frac{\rho_j + \rho_i}{2}, \quad c_{ji} = \frac{c_j + c_i}{2}, \quad h_{ji} = \frac{h_j + h_i}{2},$$
(21)

$$\vec{v}_{ji} = \vec{v}_j - \vec{v}_i, \quad \vec{r}_{ji} = \vec{r}_j - \vec{r}_i.$$
 (22)

- artificial_viscosity_skf. See section 2.1.2.
- artificial_shear_visc. Term α_{Π} in eq. 19.
- artificial_bulk_visc. Term β_{Π} in eq. 19.

2.1.8 Average Velocity

• average_velocity. Enable XSPH velocity smoothing factor:

$$\frac{D\vec{r_j}}{Dt} = \vec{v_j} + \vec{v_j}_{\text{avg}},\tag{23}$$

where v_{avg} is:

$$\vec{v}_{j \text{ avg}} = -\varepsilon_{\text{avg}} \sum_{i} \frac{m_{i}}{\rho_{i}} \vec{v}_{ji} W_{ji}. \tag{24}$$

- average_velocity_skf. See section 2.1.2.
- average_velocity_coef. Term ε_{avg} in eq. 24.

2.1.9 Time Integration

- simulation_time. Total simulation time to stop experiment.
- dt_correction_method. Method of Δt choosing. Possible values of enumeration:
 - 0: DT_CORRECTION_CONST_VALUE. Use user-provided constant value.

$$\Delta t_{\tau} = \Delta t_{\text{user}}.\tag{25}$$

- 1: DT_CORRECTION_CONST_CFL. Δt is computed before experiment start with CFL condition:

$$\Delta t_{\tau} = \Delta t_0 = \text{CFL} \frac{h}{c(1 + 1.2\alpha_{\Pi})} \tag{26}$$

- 2: DT_CORRECTION_DYNAMIC. Δt is computed on every step with CFL condition:

$$\Delta t_{\tau} = \text{CFL} \min(\Delta t_f, \Delta t_{\phi}), \tag{27}$$

$$\Delta t_f = \min_i \left(\sqrt{\frac{h}{a_i}} \right), \tag{28}$$

$$\Delta t_{\phi} = \min_{i} \left(\frac{h}{c + \phi} \right). \tag{29}$$

- dt. Term $\Delta t_{\rm user}$ in eq. 25.
- CFL_coef. Term CFL in eq. 26 and eq. 27.

2.1.10 Boundary Treatment

- boundary_treatment. Selects method for boundaries. Possible values of enumeration:
 - 0: SBT_DYNAMIC. Boundary particles are the same as fluid but have constant positions.
 - 1: SBT_REPULSIVE. Boundary particles are dynamic with additional term in momentum equation:

$$\frac{D\vec{v}_j}{Dt} = -\sum_i \left[m_i \left(\frac{p_j}{\rho_j^2} + \frac{p_i}{\rho_i^2} \right) \vec{\nabla}_j W_{ji} + \vec{\Upsilon}_{ji} \right], \tag{30}$$

where $\vec{\Upsilon}_{ji}$ is computed if j is fluid particle and i is boundary particle:

$$\vec{\Upsilon}_{ji} = \frac{\vec{r}_{ji}}{|\vec{r}_{ji}|} \begin{cases} D\left[\left(\frac{r_0}{|\vec{r}_{ji}|}\right)^{\alpha_1} - \left(\frac{r_0}{|\vec{r}_{ji}|}\right)^{\alpha_2}\right] & |\vec{r}_{ji}| \le r_0, \\ 0 & |\vec{r}_{ji}| > r_0. \end{cases}$$
(31)

Equation parameters are considered built-in:

$$r_0 = 2h,$$

 $D = 5gd,$
 $\alpha_1 = 12,$
 $\alpha_2 = 4,$
(32)

where d is initial water depth.

2.1.11 Numerical Waves Maker

- nwm. Waves maker method. Possible values of enumeration:
 - 0: NWM_NO_WAVES. No waves generator.
 - 2: NWM_METHOD_DYNAMIC. First order waves generator. Piston-type wavemaker.
 Makes waves with surface displacement of type:

$$\eta(x,t) = \frac{H}{2}\cos(\omega t - kx + \delta),\tag{33}$$

where H is wave height, x is distance and δ is the initial phase. $\omega = 2\pi/T$ is the angular frequency and $k = 2\pi/L$ is the wave number with T equal to the wave period and L the wave length.

Piston displacement equation is:

$$e_1(t) = \frac{S_0}{2}\sin(\omega t + \delta),\tag{34}$$

where S_0 is piston magnitude:

$$S_0 = H \frac{\sinh kd \cosh kd + kd}{2 \sinh kd^2},\tag{35}$$

where d is depth.

-4: NWM_METHOD_WALL_DISAPPEAR.

Methods NWM_METHOD_DYNAMIC and NWM_METHOD_WALL_DISAPPEAR require ParticleParams to provide nwm_particles_start and nwm_particles_end.

- nwm_time_start. Simulation time when NWM starts to generate waves.
 Optional parameter.
- nwm_wave_length. Wave length L to be generated.

 Mandatory when nwm == NWM_METHOD_DYNAMIC.
- nwm_wave_magnitude. Wave height H to be generated.

 Mandatory when nwm == NWM_METHOD_DYNAMIC.

2.1.12 Output Control

- save_time. Program will produce output for further processing every save_time seconds of simulation. See 'data' directory of experiment.
- save_velocity. Enable velocity saving in output.
- save_pressure. Enable pressure saving in output.
- save_density. Enable density saving in output.

2.1.13 Dump Control

- use_dump. Enable dump dump creation.
- dump_time. Program will produce dump every dump_time seconds of simulation. You can use that point in time to start from later. See 'dump' directory of experiment.

2.1.14 Time Estimation

- use_custom_time_estimate_step. Enables user-set time estimation step. Program will print amount of time left for simulation to finish every k steps. If not set, program will print time estimation with every output.
- \bullet step_time_estimate. Term k in previous statement.

2.1.15 Consistency Control

- consistency_check. Enable consistency control: check if variables are NaN or infinite; check particles are outside of simulation domain.
- consistency_treatment. Selects method for consistency control. Possible values of enumeration:
 - 0: CONSISTENCY_PRINT. Prints warning message on inconsistent value of variables and continues simulation. Simulation with such values of variables is undefined.
 - 1: CONSISTENCY_STOP. Prints error message and stop simulation process.
 - 2: CONSISTENCY_FIX. Fixes particles leaving simulation domain (mark them as non-existing). Prints error message and stop simulation process on NaN or infinite values of variables.

2.1.16 Optimization

- max_neighbours. Maximum number of neighbours for particle. Affects on allocated memory for grid of neighbours.
- local_threads. Local threads number for OpenCL kernels and OpenMP parallel sections.

2.2 Particle Params

2.2.1 Target version

- params_target_version_major
- params_target_version_minor
- params_target_version_patch

2.2.2 Particle count

- nfluid. Fluid particles count.
- nvirt. Boundary (virtual) particles count.
- ntotal. Total particles count (fluid + boundary).

2.2.3 Geometry

These parameters describe simulation domain area.

- x_mingeom. Left side of the domain.
- x_maxgeom. Right side of the domain.
- y_mingeom. Bottom of the domain.
- y_maxgeom. Top of the domain.

2.2.4 Particles parameters

- delta. Initial distance between particles δ_0 .
- rho0. Reference density of particles ρ_0 . Optional parameter. Default value is $\rho_0 = 1000$.

2.2.5 Extra parameters

• depth. Reference depth of the fluid d.

Optional parameter. By default $d = \max_{i} y_i$ on the start.

2.2.6 Numerical Waves Maker

If nwm is piston or disappearing wall, affected boundary particles are from the contiguous block characterized by two indices: [start; end).

- nwm_particles_start. Index of the first particle in moving or disappearing block.
- nwm_particles_end. Index of the next to the last particle in moving or disappearing block.

2.3 Computing Params

2.3.1 Software version

- SPH2D_version_major
- SPH2D_version_minor
- SPH2D_version_patch

2.3.2 Params module version

- params_version_major
- params_version_minor
- params_version_patch

2.3.3 Common module version

- SPH2D_common_version_major
- SPH2D_common_version_minor
- SPH2D_common_version_patch

2.3.4 Computing module version

- SPH2D_specific_version_major
- SPH2D_specific_version_minor
- SPH2D_specific_version_patch
- SPH2D_specific_version_name

2.3.5 Computed constants

• mass. Mass of the particle m:

$$m = \rho_0 \delta_0^{\dim}. \tag{36}$$

• hsml. Smoothing length h:

$$h = \delta_0 h_k. (37)$$

- cell_scale_k. Size of grid cell in terms of h. Equals to 3 if any kernel is gauss. Equals to 2 otherwise.
- \bullet maxn. Maximum count of particles in simulation:

$$\max_{n} = 2^{1 + \lfloor \log_2 \operatorname{ntotal} \rfloor} \tag{38}$$

- max_cells. Count of grid cells to be processed.
- start_simulation_time

2.3.6 Numerical Waves Maker

- nwm_wave_number . Generated wave number k.
- \bullet nwm_freq. Generated wave angular frequency $\omega.$
- nwm_piston_magnitude. If nwm is dynamic, piston magnitude S_0 computed by eq. 35.

2.3.7 Particle type

- TYPE_WATER. Fluid particles type identifier in output.
- TYPE_BOUNDARY. Water particles type identifier in output.
- TYPE_NON_EXISTENT. Identifier of particles that are not exist.

2.4 Loading Params

It could be useful to load just a part of output data. Any post processing program will load files with respect to 'LoadingParams.json'. Computing programs can't start experiment where 'LoadingParams.json' exists.

- every_layers. Load every n^{th} layer. Optional parameter. Default value is 1.
- from. Skip all layers before t_{from} second.
 Optional parameter. Default value is 0.
- to. Skip all layers after t_{to} second. Optional parameter. Default value is t_{max} .

2.5 Height Testing Params

2.5.1 Common part

- mode. Mode of height testing. Possible values are:
 - "space",
 - "time".
- y0. y₀ in eq. 41 and 44.

 Optional parameter. Default value is 0.
- y_k. y_k in eq. 41 and 44.
- search_n. Smoothing factor s_n : for a given point x_i program will search particles with max y in interval $[x_i hs_n; x_i + hs_n]$, where h is smoothing length.
- particles_type. Type of particles to consider. See section 2.3.7. Optional parameter. Default value is null (all particles are considered).

2.5.2 Space profile

Calculate space profile (y values) for a given points of time:

$$y_i = \max_i (y([x_i - hs_n; x_i + hs_n])),$$
 (39)

$$i = \lceil \frac{1}{\delta_0} (\texttt{x_maxgeom} - \texttt{x_mingeom}) \rceil. \tag{40}$$

Space profile points are transformed by coefficients and terms:

$$\begin{cases} \bar{x} = x_k(x - x_0), \\ \bar{y} = y_k(y - y_0). \end{cases}$$

$$\tag{41}$$

- t. Array of points in time to calculate time profile. Each point will be separate output file.
- x0. x₀ in eq. 41.
 Optional parameter. Default value is 0.
- x_k. x_k in eq. 41.
 Optional parameter. Default value is 1.

2.5.3 Time profile

Calculate time profile (y values) for a given points in space:

$$y_i = \max_i (y([x - hs_n; x + hs_n])),$$
 (42)

$$i = \lceil \frac{1}{\Delta t} (\texttt{simulation_time} - \texttt{save_time}) \rceil. \tag{43}$$

Time profile points are transformed by coefficients and terms:

$$\begin{cases}
\bar{t} = t_k(t - t_0), \\
\bar{y} = y_k(y - y_0).
\end{cases}$$
(44)

- x. Array of points in space to calculate time profile. Each point will be separate output file.
- t0. t_0 in eq. 44. Optional parameter. Default value is 0.
- t_k. t_k in eq. 44. Optional parameter. Default value is 1.