

7 DYNAMICS

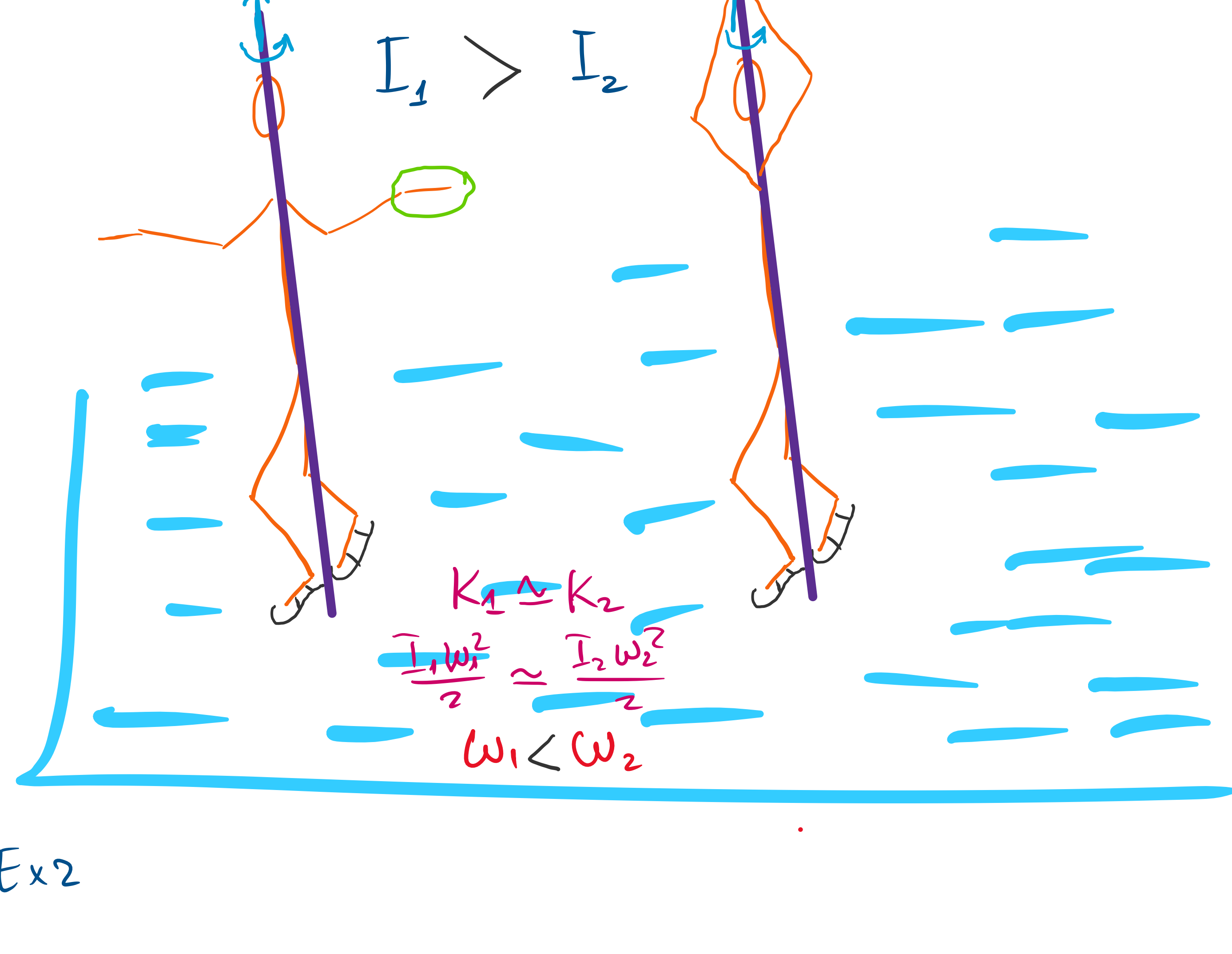
7.7. The momentum of inertia

A)

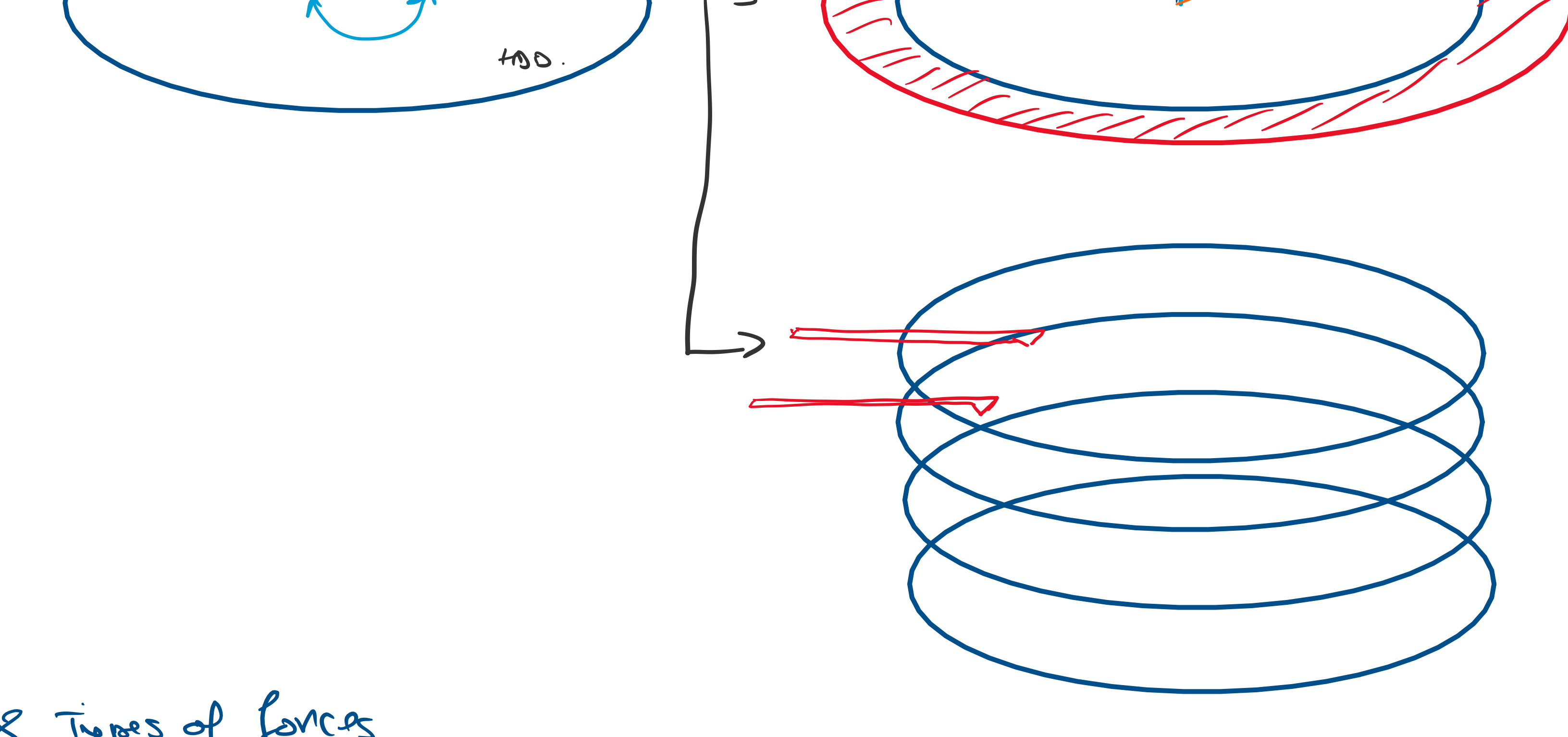
$$I = \int \rho(\vec{r}) s^2 dV$$

B) Examples

Ex1.

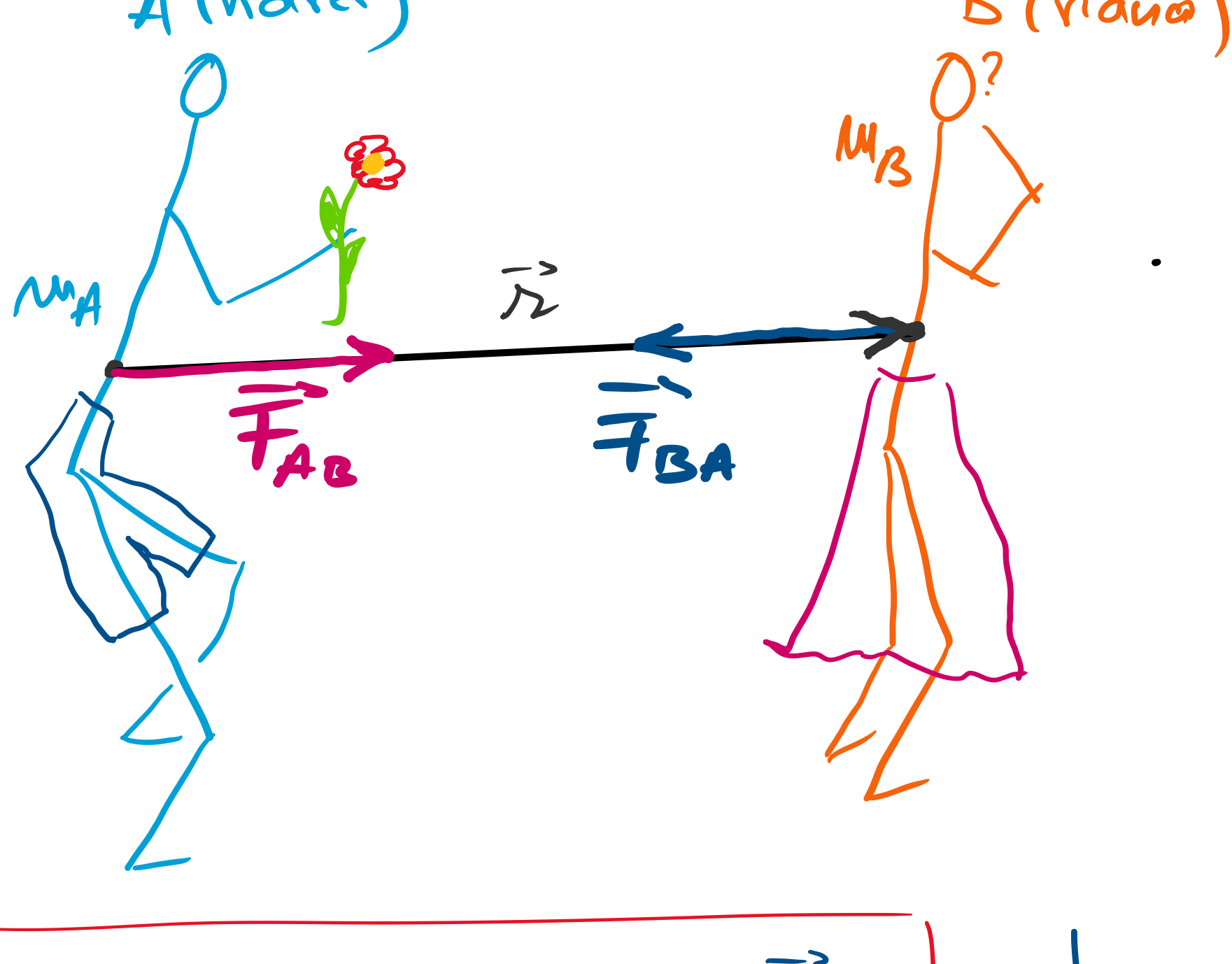


Ex2



8. Types of forces

8.1. The law of universal attraction



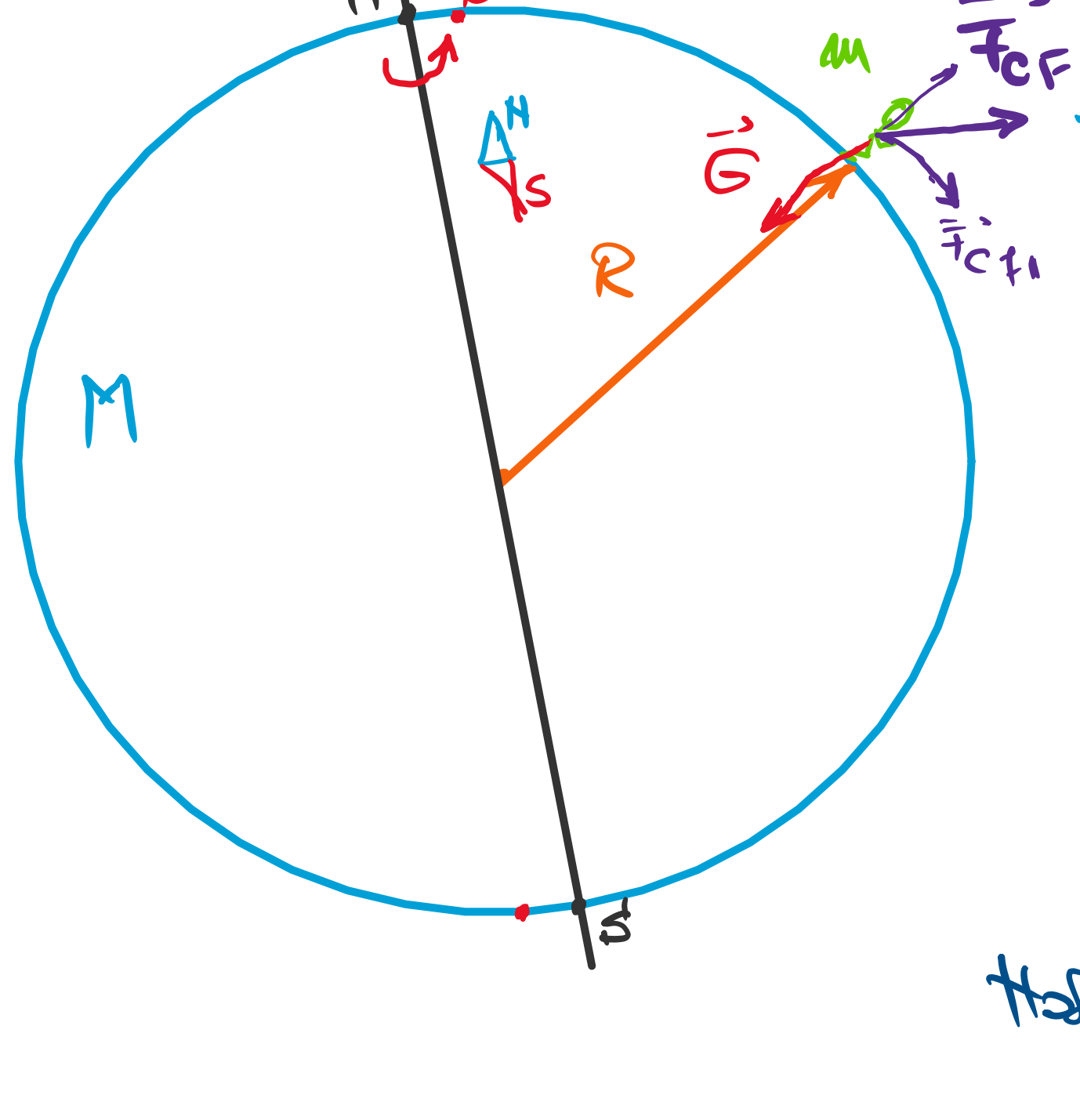
$$\vec{F}_{BA} = -\vec{F}_{AB} = G \frac{m_A \cdot m_B}{r^2} \frac{\vec{r}}{|\vec{r}|}$$

$G = 6.6732 \cdot 10^{-11} \frac{N \cdot m^2}{kg^2}$
the gravitational constant

Any two bodies are attracted to each other with a force directly proportional with the product of their masses and inversely proportional with the square of the distance between them.

8.2. The gravitational force

A)



$R \approx 6400 \text{ km}$

$h_{\text{ Everest}} \approx 8,848 \text{ km}$

$$G = G \frac{Mm}{R^2} \quad \left| \begin{array}{l} \vec{a} = \frac{\vec{F}}{m} \Rightarrow \\ \vec{F} = m \vec{a} = \vec{a} m \end{array} \right.$$

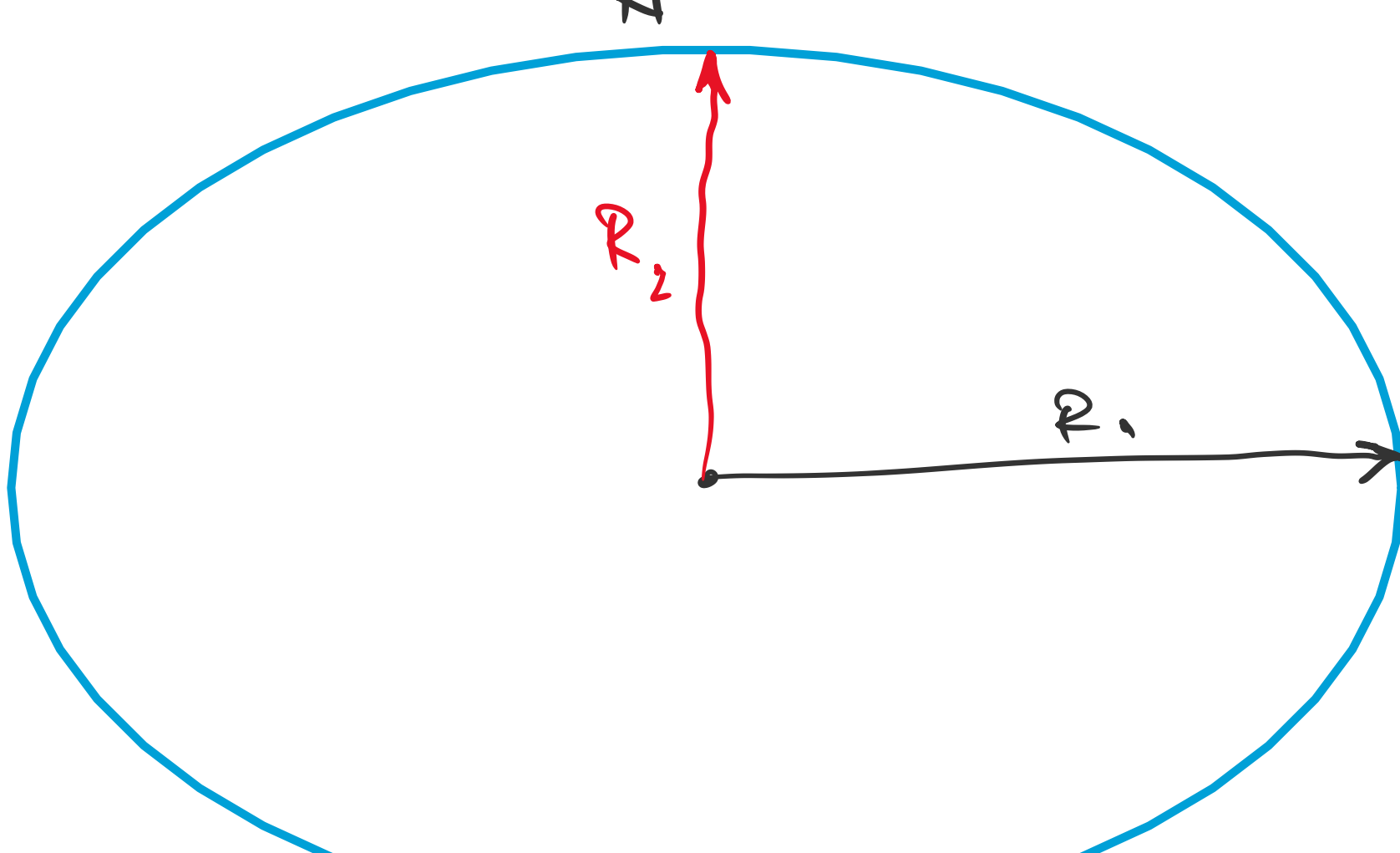
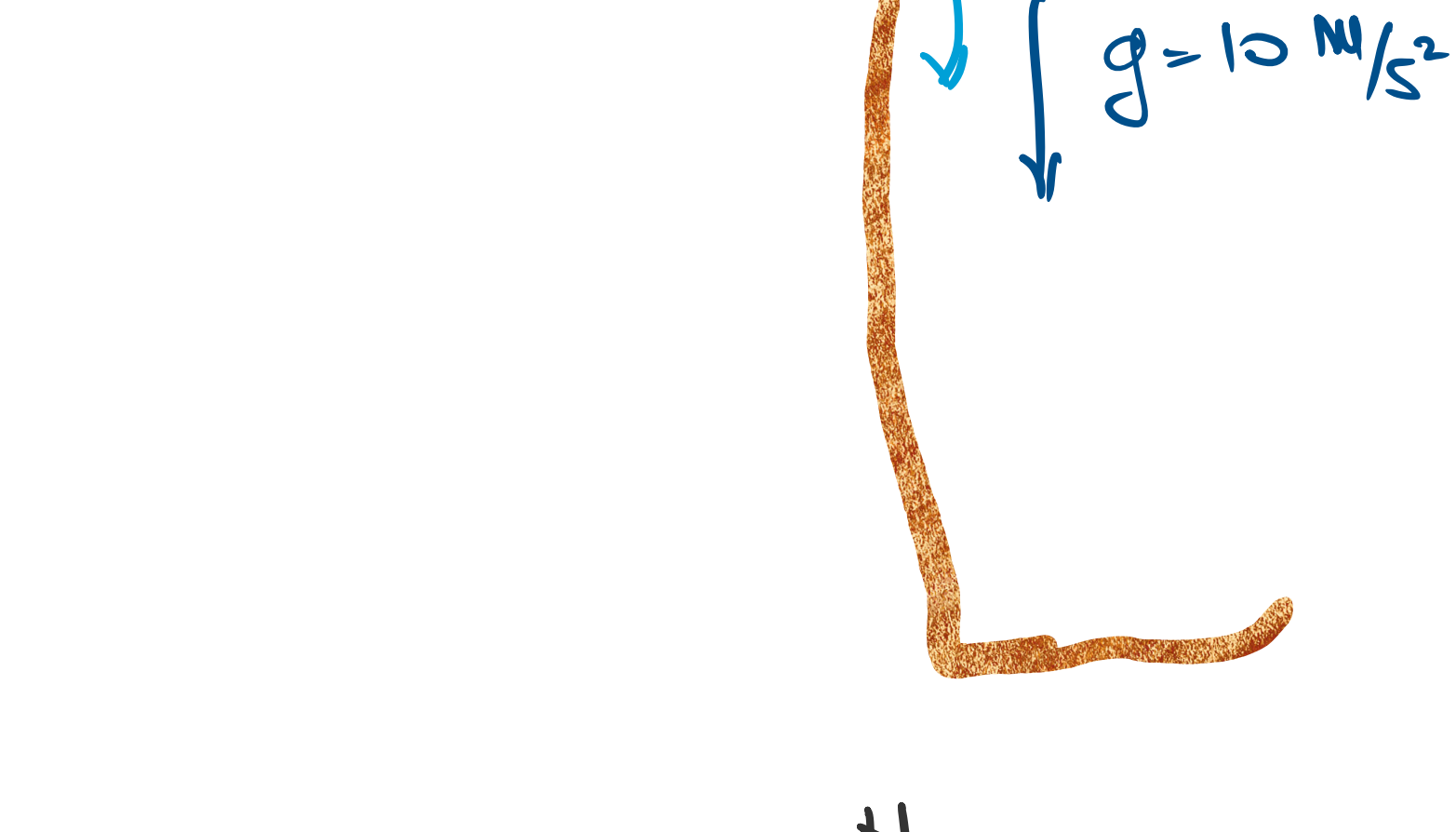
$$G = \frac{1}{g} \frac{M}{R} \cdot m$$

$$G = g m$$

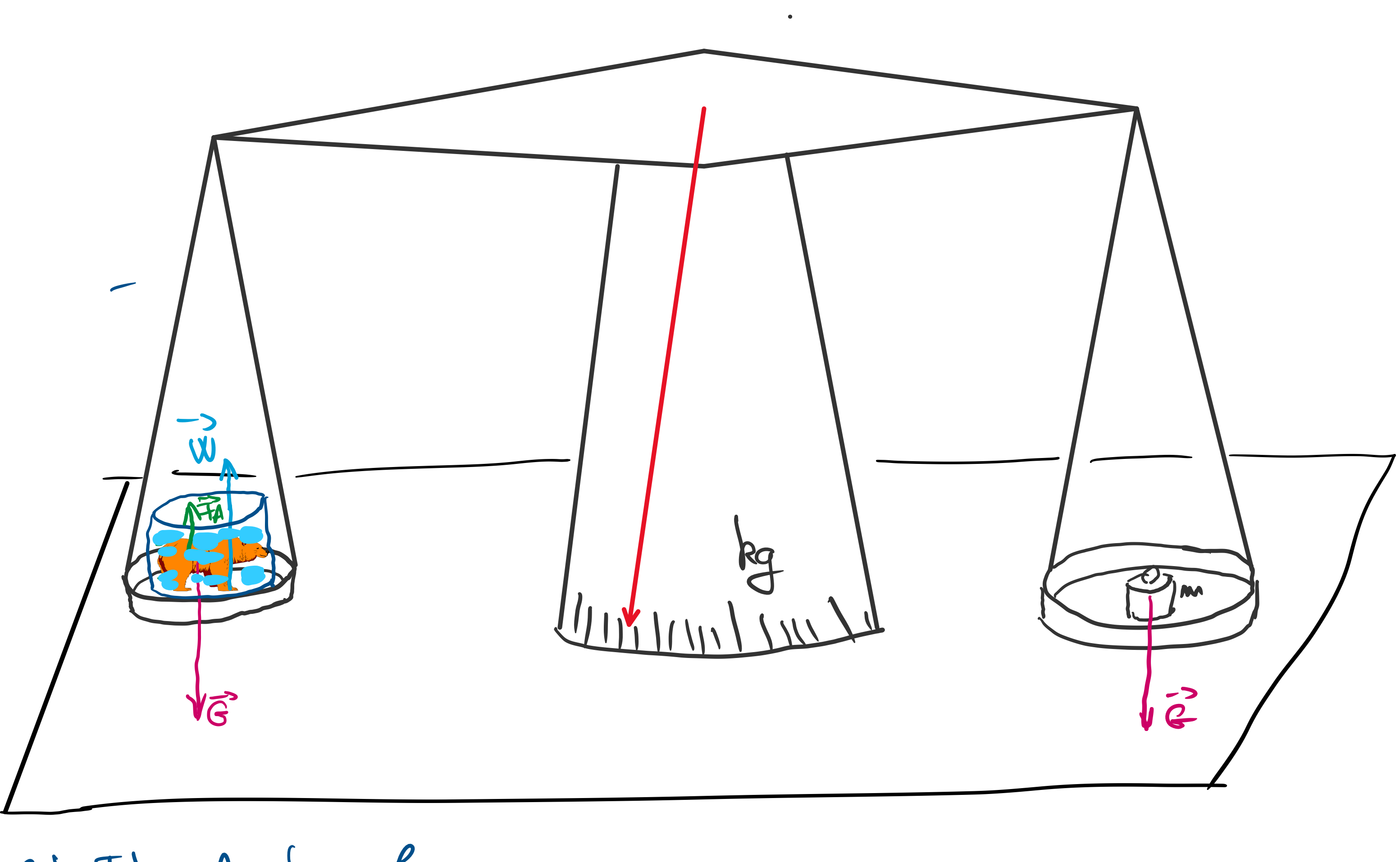
for $g = G \frac{M}{R^2}$ - the gravitational acceleration

$g \approx 9.81 \frac{m}{s^2}$ Obij-Koposa ✓

B)

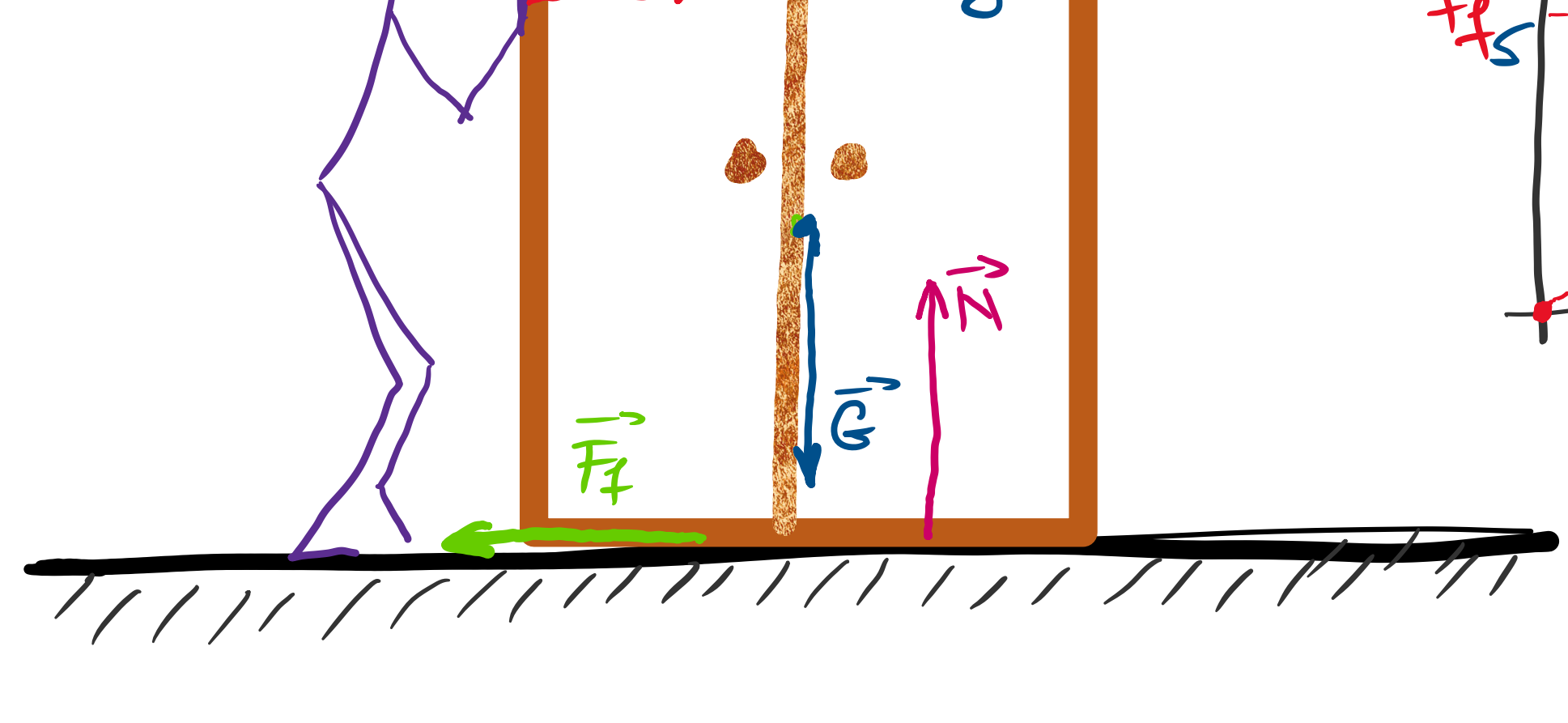


8.3. The weight



8.4. The friction force

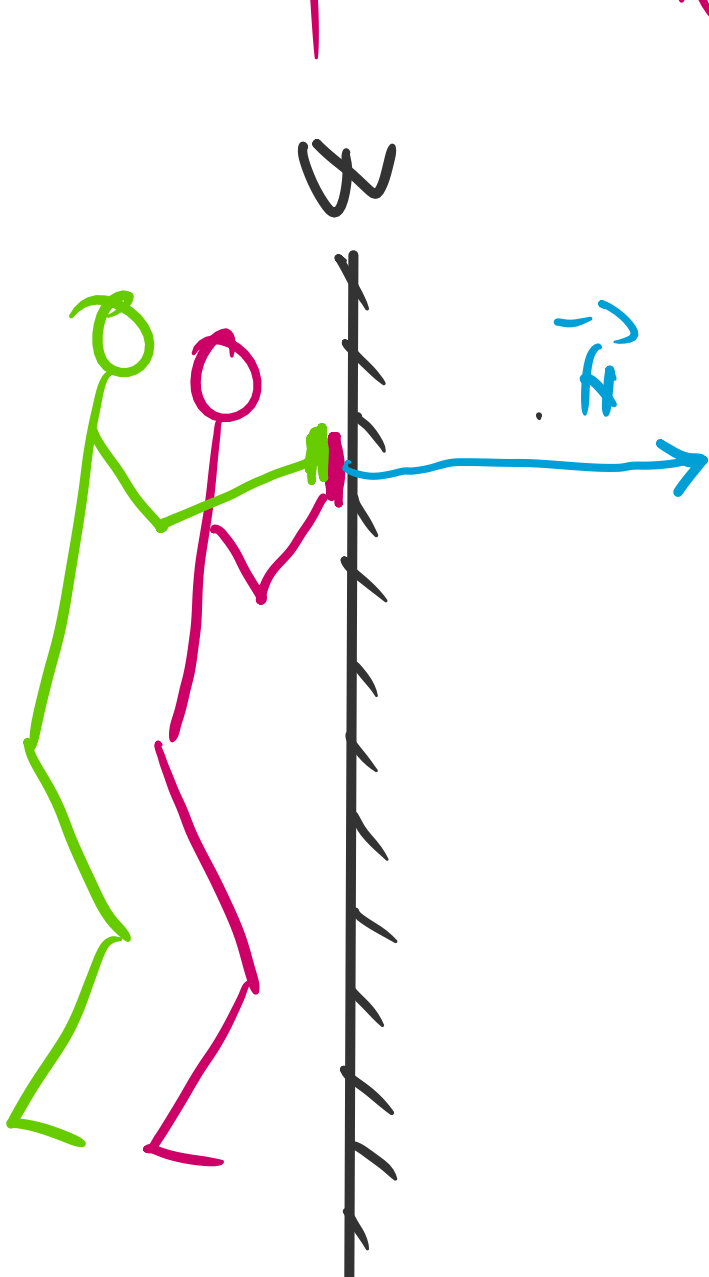
A) at sliding



Friction is a force that slowed down or obstruct the motion of an object against another object or it can be observed between two adjacent layers of a liquid (a fluid).

• The friction force

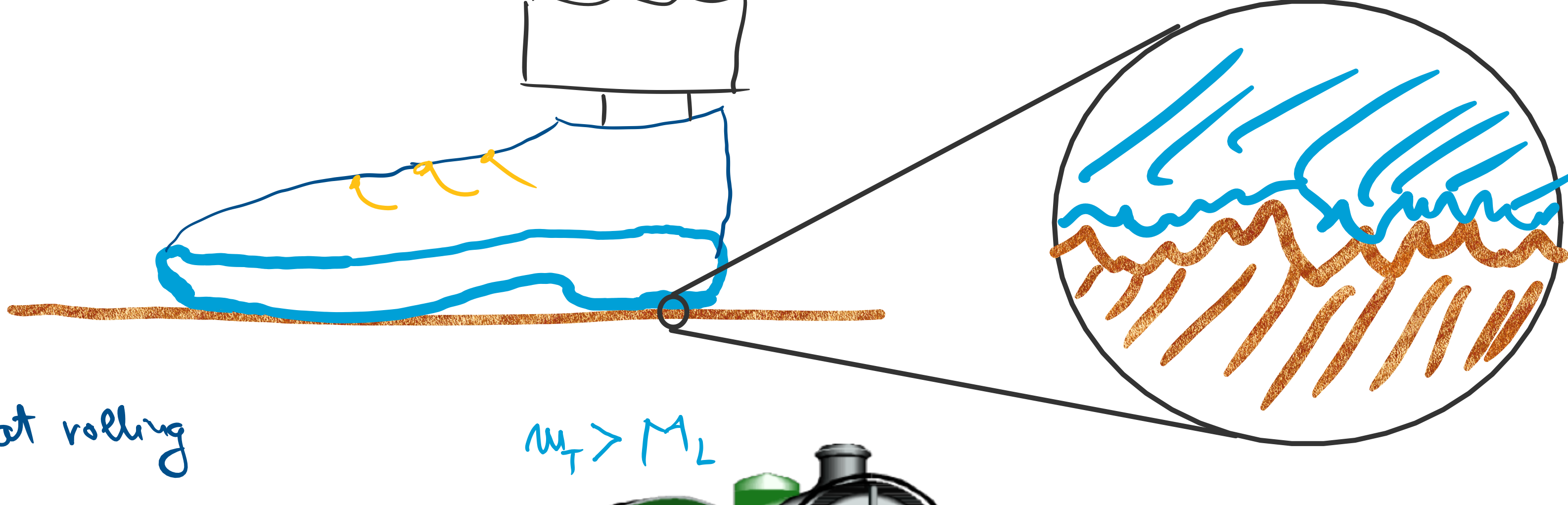
- depend on
 - the nature (materials) of bodies in contact
 - the degree of polishing
 - the normal force, N
- independent of the magnitude (area) of surfaces in contact



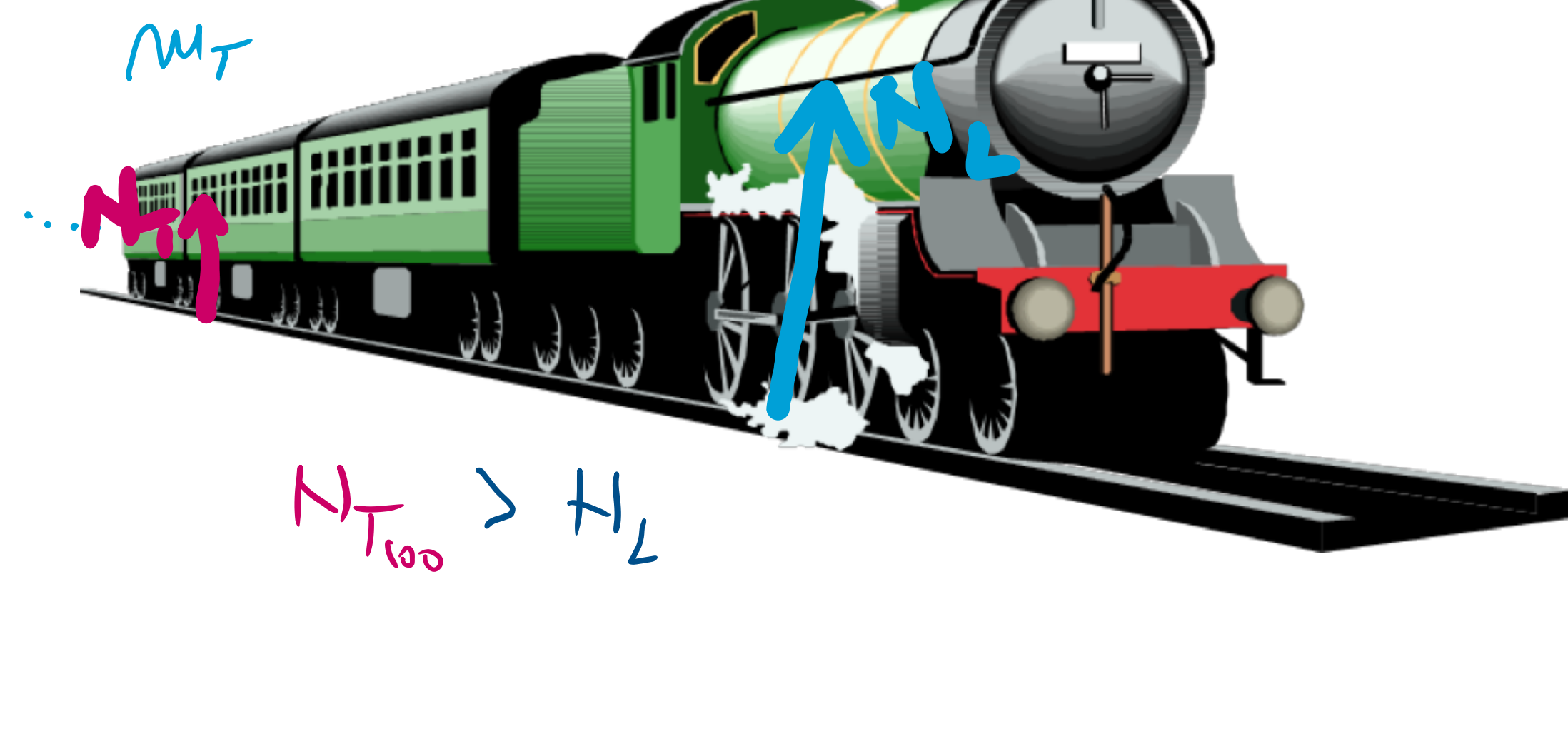
$$F_{f_s} = \mu_s \cdot N$$

the friction coefficient at sliding

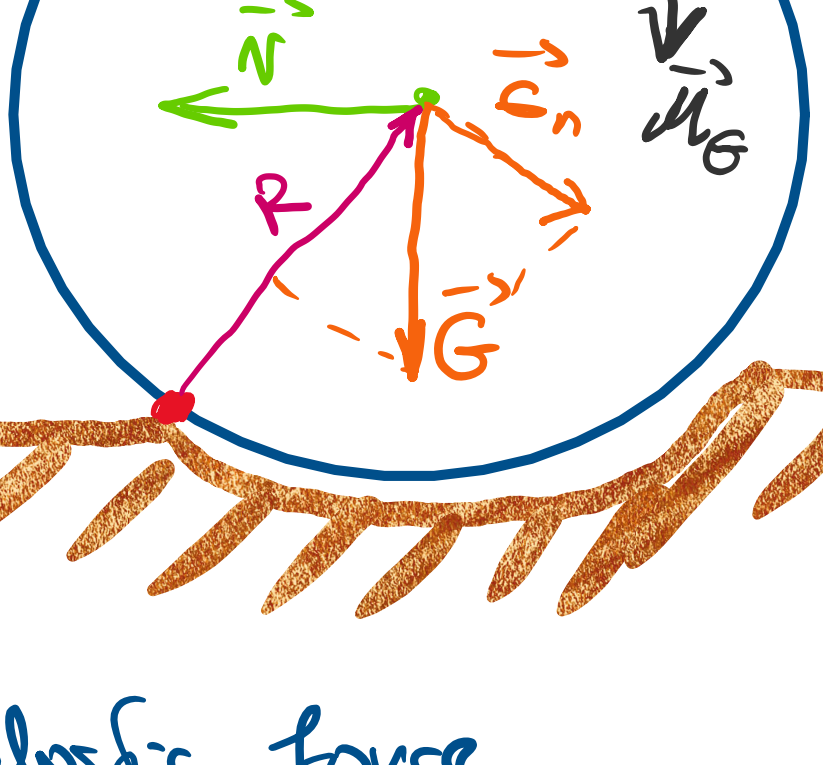
<https://phys.utcluj.ro/resurse/Facultati/Constructii/2020-2021/Aplicatii/CutietaGol/>



B) at rolling



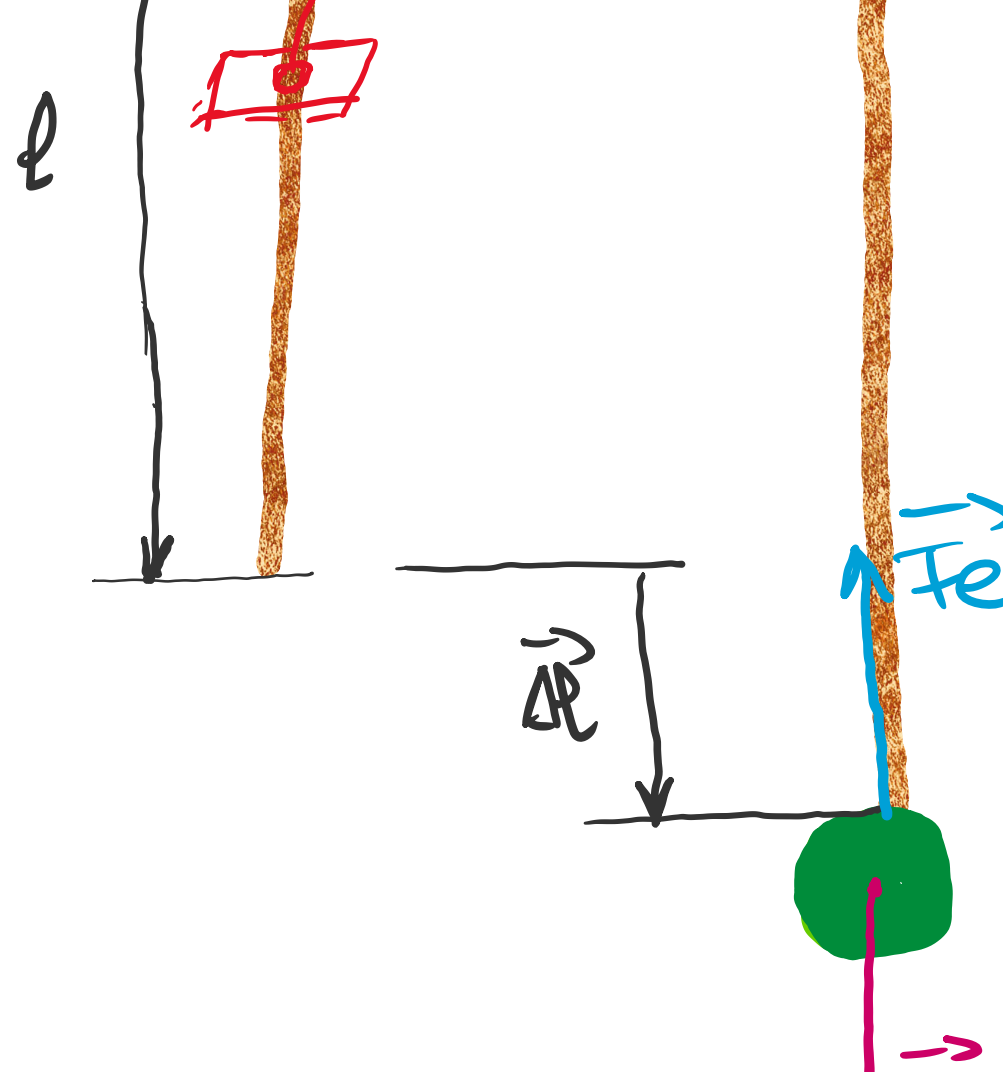
$$N_{T00} > H_L$$



$$F_{f_2} = \mu_2 \frac{N}{R}$$

↑ friction coefficient at rolling

8.5 The elastic force



$$\frac{F}{S} = E \frac{\Delta l}{l}$$

- the Hooke's law

E - the modulus of elasticity $[E]_{SI} = \frac{N}{m^2}$ (the Young's modulus)

for $\sigma = \frac{F}{S}$ - the stress

2° $\epsilon = \frac{\Delta l}{l}$ - the strain

$$\sigma = E \epsilon$$

- the Hooke's law

$$\vec{F}_e + \vec{F} = 0$$

$$\vec{F}_e = -\vec{F} = -\frac{S \cdot E \cdot \Delta l}{l} \Rightarrow \vec{F}_e = -\frac{S \cdot E}{l} \cdot \Delta l$$

Note

$k_e = \frac{S}{l} E$ - the elastic constant

$$\vec{F}_e = -k_e \Delta \vec{l}$$

- the elastic force